

Title: Quantum control in foundational experiments

Date: May 05, 2015 03:30 PM

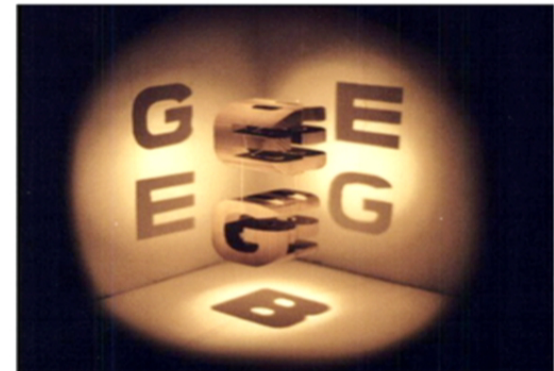
URL: <http://pirsa.org/15050016>

Abstract: <p>Using quantum control in foundational experiments allows new theoretical and experimental possibilities. We show how, e.g., quantum controlling devices reverse a temporal ordering in detection. We consider probing of waveâ€“particle duality in quantum-controlled and the entanglement-assisted delayed-choice experiments. Then we discuss other situations where quantum control may be useful, and finally demonstrate how the techniques we developed are applied to the study of consistency of the classically reasonable requirements. In a version of the delayed-choice experiment which ostensibly combines determinism, independence of hidden variables on the conducted experiments, and wave-particle objectivity we show that these ideas are incompatible with any theory, not only with quantum mechanics.</p>

## OUTLINE

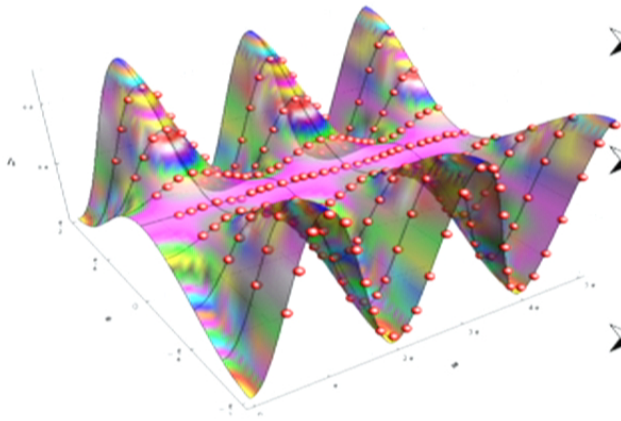
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- ❑ Complementarity & delayed choice
- ❑ Hidden variables 101
- ❑ Quantum control
- ❑ Entangled control
- ❑ Contradictions without quantum theory



## REFERENCES

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- Ionicioiu and Terno, Phys. Rev. Lett. **107**, 230406 (2011).
  - Céleri, Gomes, Ionicioiu, Jennewein, Mann, and Terno, Found. Phys. **44**, 576 (2014).
  - Ionicioiu, Jennewein, Mann, and Terno, Nature Comm. **5**, 3997 (2014)
  - Ionicioiu, Mann, and Terno, Phys. Rev. Lett. **114**, 060405 (2015)
- ❑ Ma, Kofler, and Zeilinger, *Delayed-choice gedanken experiments and their realizations*, arXiv:1407.2930v1

# **PART 1**

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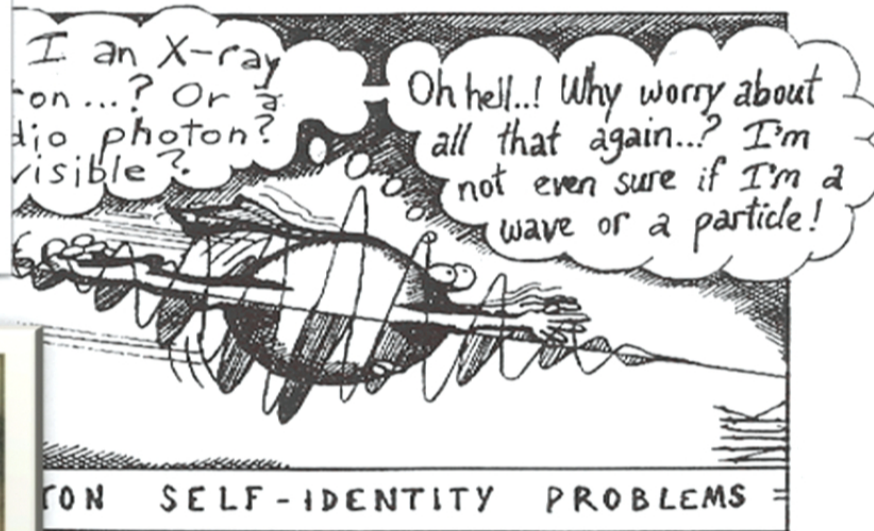
## ***COMPLEMENTARITY & DELAYED CHOICE***

A bit of history

Complementarity

WDC

# LIGHT: WAVES vs PARTICLES



Photons are particles

Photons are waves

# LIGHT: WAVES vs PARTICLES



I an  
on...?  
dio ph  
visible



! Why worry about  
at again...? I'm  
even sure if I'm a  
ave or a partide!



TON

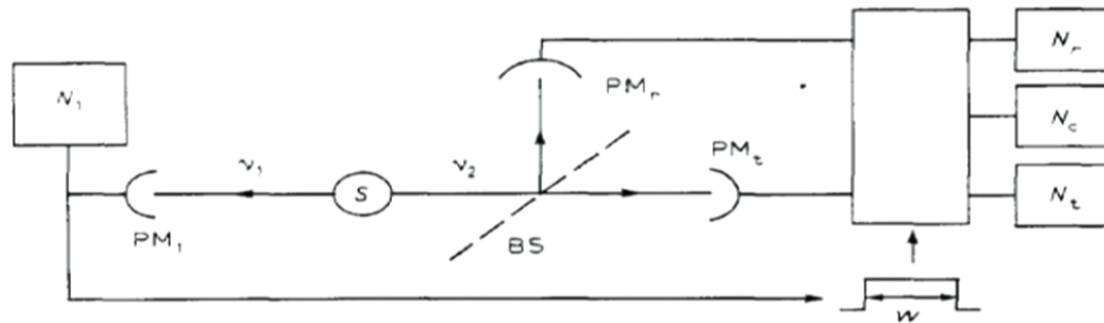


Photons are particles

Photons are waves

# PHOTONS

## *at last*

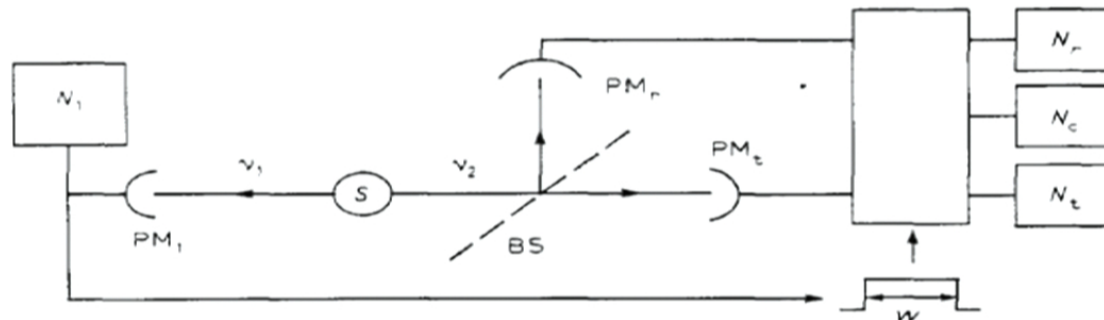


Single photons **behave as** particles

Grangier, Roger and Aspect  
Europhys. Lett. **1**, 173 (1986)

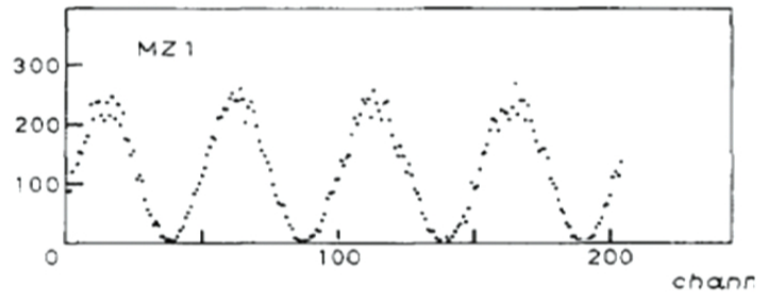
# PHOTONS

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Grangier, Roger and Aspect  
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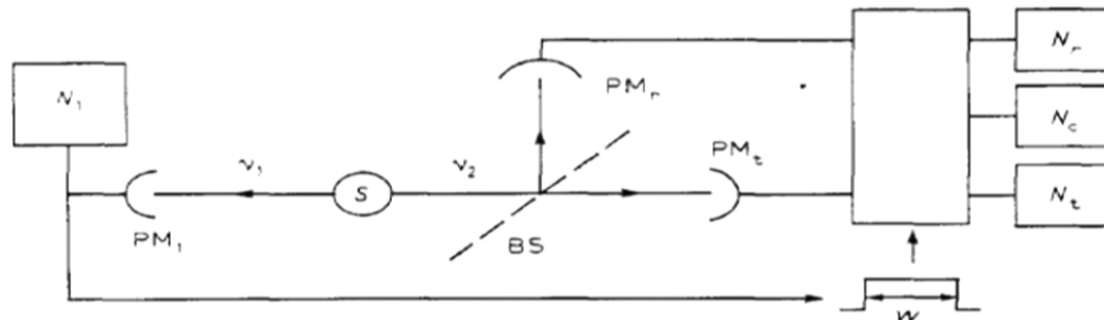
Single photons **behave as particles**  
Single photons **behave as waves**





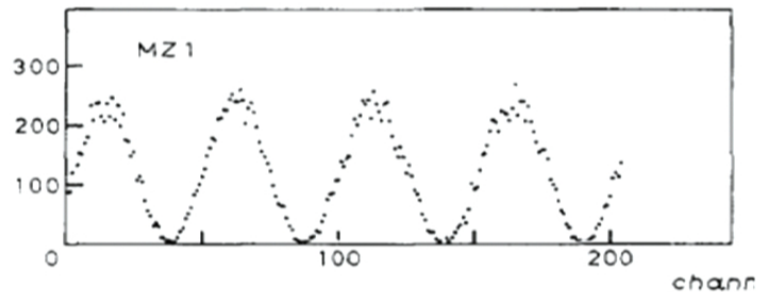
# PHOTONS

## at last



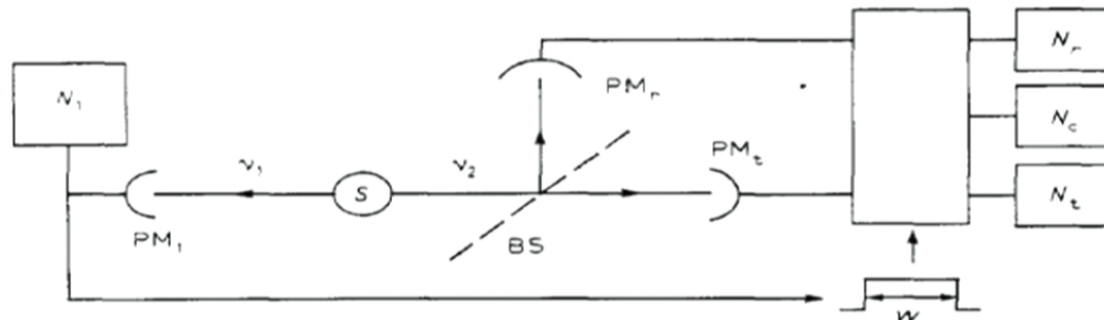
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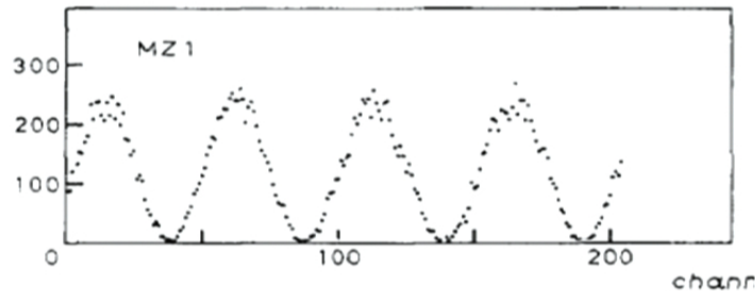
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Grangier, Roger and Aspect  
Europhys. Lett. **1**, 173 (1986)

Single photons **behave as particles**  
Single photons **behave as waves**



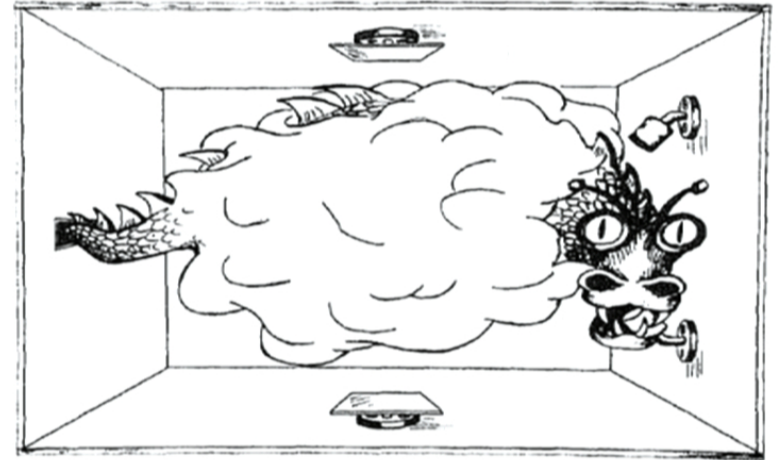
### DEFINITIONS

*Particles*: no interference,  
▶ single path  
*Waves*: interference,  
▶ both paths

## COMPLEMENTARITY: *a modern version*

... the information provided by different experimental procedures that in principle cannot, because of the physical character of the needed apparatus, be performed simultaneously, cannot be represented by any mathematically allowed quantum state of the system. The elements of information obtainable from incompatible measurements are said to be *complementary*.

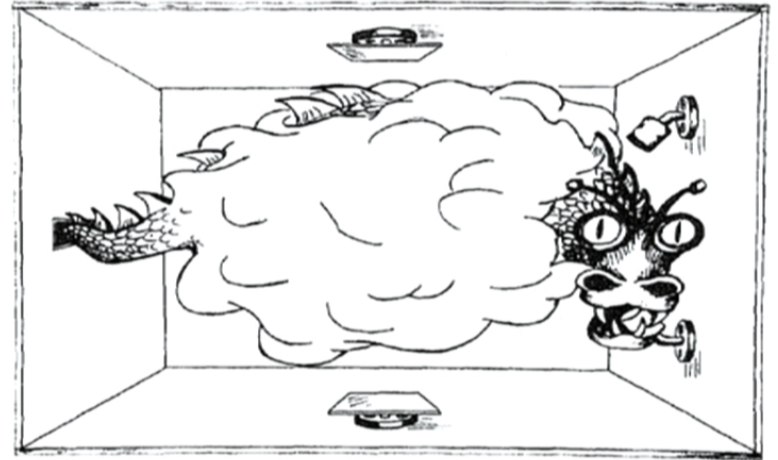
Stapp, in *Compendium of Quantum Physics*



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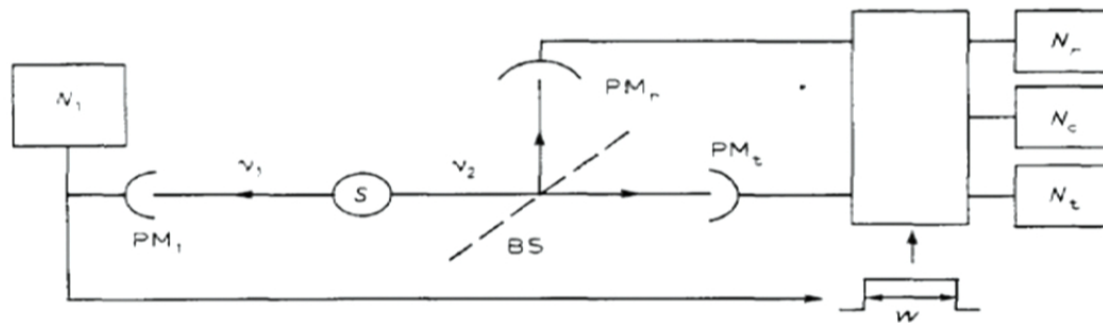
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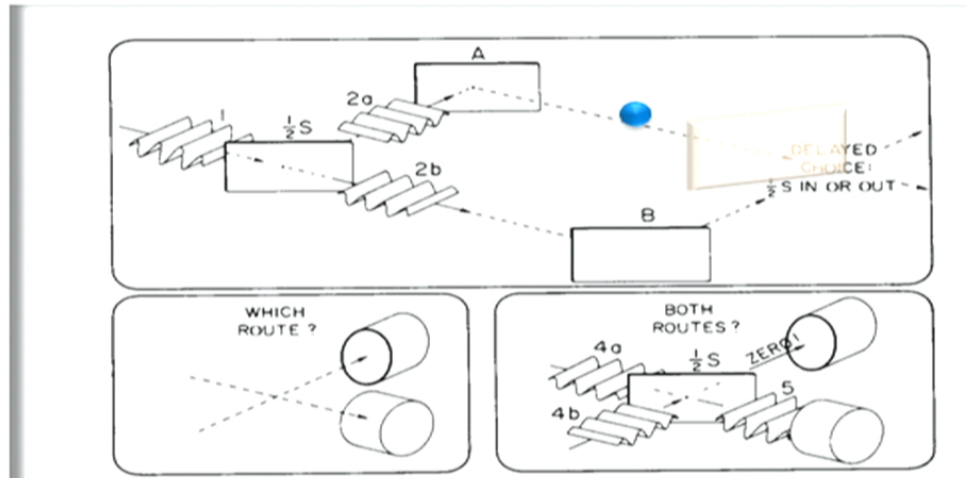
# COMPLEMENTARITY: *a conspiracy*



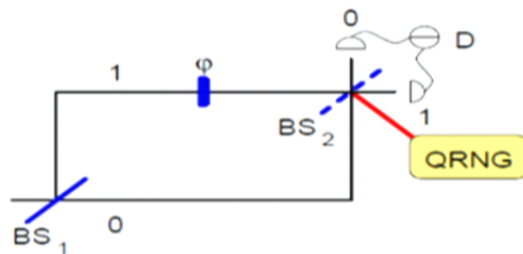
The photon could know in advance of entering the apparatus whether the latter has been set up in the “wave” configuration with  $BS_2$  in place or the “particle” one ( $BS_2$  removed) and adjust accordingly.



# DELAYED CHOICE



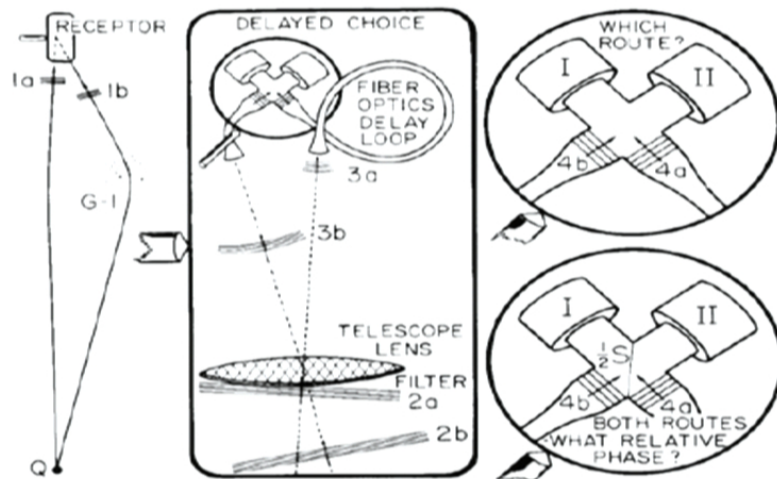
Wheeler, 1978, 1984



By making the choice to close or open the MZI when the photon is already in, it is forced not to change its mind

# DELAYED CHOICE

*[a tagline v. 1.0]*



Hitch guide: to deal with  
The ensuing english

...we discover "by which route" it came with one arrangement; or by the other, what the relative phase is of the waves associated with the passage of the photon from source to receptor by both routes" {perhaps 50,000 light years apart as they pass the lensing galaxy G-1. But the photon has already passed that galaxy billions of years before we made our decision

In this sense, we have a strange inversion of the normal order of time. We, now, by moving the mirror in or out have an unavoidable effect on what we have a right to say about the already past history of that photon

## HV THEORIES

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**Purpose:** reproduce observed statistics and maintain classical concepts  
Viewed as [likely] inadequate, but consistent world view



# HV THEORIES

---

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Viewed as [likely] inadequate, but consistent world view

## Counter-HV action

- ◇ consider a set-up
- ◇ make a QM prediction
- ◇ make a HV prediction
- ◇ compare
  - ◇ get a contradiction
- ◇ make an experiment



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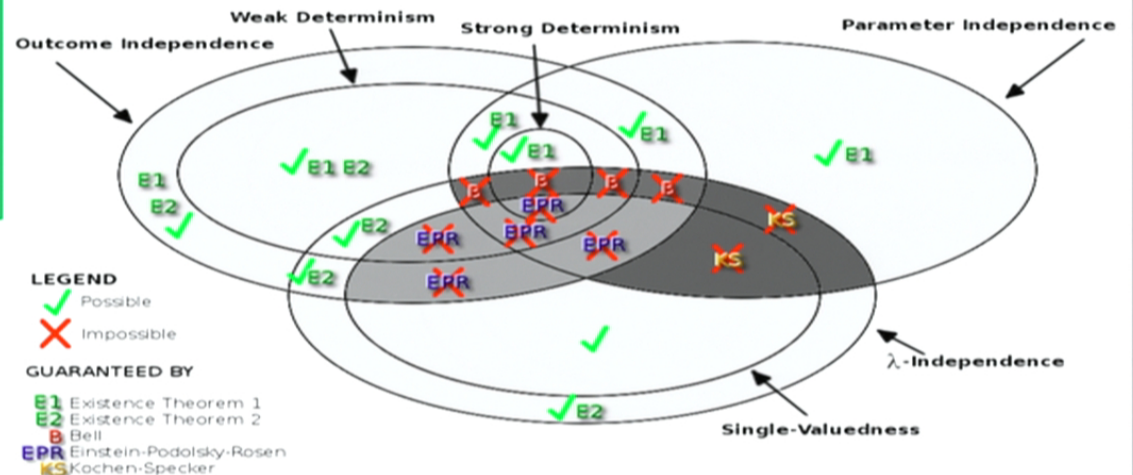
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  - get a contradiction
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## Counter-counter-HV action

- find a loophole
- introduce conspiratorial correlations

Brandenburger & Yanofsky  
JPA **41** 425302 (2008) ▶



# HV THEORIES

---

Measurements  
and settings:

$A, A'; B, B'$

Outcomes

$a, a'; b, b'$

Brandenburger  
& Yanofsky,  
J. Phys. A **315**,  
966 (2007)

# HV THEORIES

❑ **Determinism:** once hidden variables are defined, there are no residual randomness [several flavors]

$$\forall A \exists a: p(a | A, \lambda) = 1 \quad \blacktriangleleft \text{strong}$$

❑ **Parameter independence:** the outcome of any measurement depends only on the HV and the set-up of this measurement

$$p(a | A, B, C, \dots, \lambda) = p(a | A, \lambda)$$

❑ **HV ( $\lambda$ -)independence:** determination of the hidden variable is independent of the choice of measurement

$$p(\lambda | A, B \dots) = p(\lambda | A', B' \dots)$$

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Brandenburger  
& Yanofsky,  
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$A, A'; B, B'$

Outcomes

$a, a'; b, b'$

Brandenburger  
& Yanofsky,  
J. Phys. A **315**,  
966 (2007)

*Locality, contextuality,  
Bell inequalities, ... are  
all derived from these  
three axioms*

# HV THEORIES

---

## *Extensions & questions*

- What is the basis for assertion of wave-particle duality?
- Can we detect “it” first and decide what was it later?
- Is space-like separation necessary?
- What if the controlling devices are quantum?

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## Conspiracy & counter-conspiracy



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- A hidden variable  $\lambda = p, w$  set at production/before splitting
- Reproduction of the observed data for some  $p(a, b, \lambda)$



# HV THEORIES

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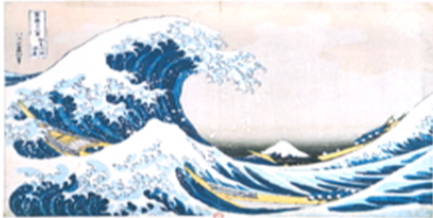
$$\text{data } q(a, b) = \sum_{\lambda=p, w} p(a, b, \lambda) = \sum_{\lambda=p, w} \text{HV theory } p(a, b | \lambda) \times \text{IC } p(\lambda)$$



# OBJECTIVITY

## *a.k.a. DEFINITNESS*

Photons are either particles  $\lambda = p$  or waves  $\lambda = w$



$$p(a | b = 1, \lambda = w) = (\cos^2 \frac{\phi}{2}, \sin^2 \frac{\phi}{2})$$



$$p(a | b = 0, \lambda = p) = (\frac{1}{2}, \frac{1}{2})$$

$$p(a | b = 0, \lambda = w) = (x, 1 - x)$$

$$p(a | b = 1, \lambda = p) = (y, 1 - y)$$



# WDC

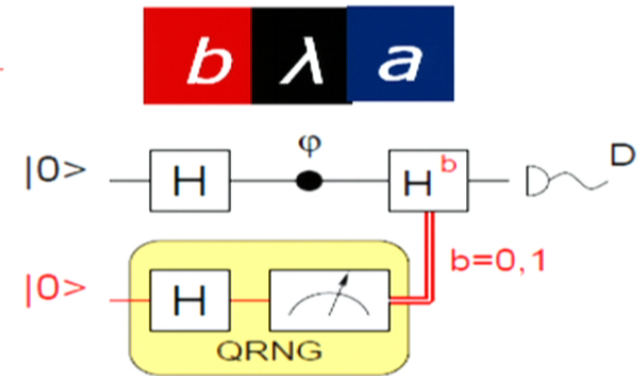
Logic

$$n(a, b) = \sum_{\lambda} p(a | b, \lambda) p(\lambda | b) n(b)$$

Causal:

$$p(\lambda | b) = \delta_{\lambda p} \delta_{b0} + \delta_{\lambda w} \delta_{b1}$$

This is the target of WDC experiments. Dismissed<sup>†</sup>



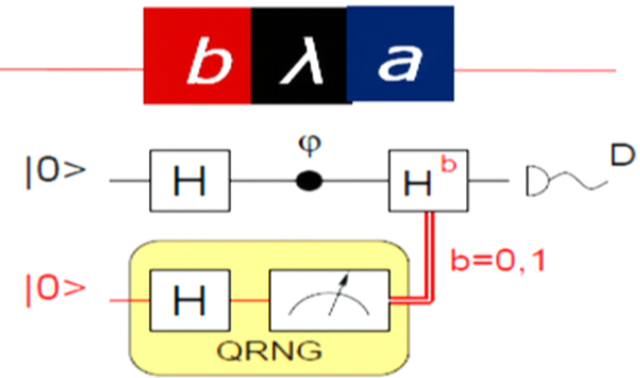
# WDC Logic

$$q(a,b) = \sum_{\lambda} p(a|b,\lambda) \times p(\lambda|b) \times n(b)$$

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<sup>†</sup> unless “even more mind boggling” conspiracies are allowed [e.g.: a correlation between HV of a photon & QRNG]

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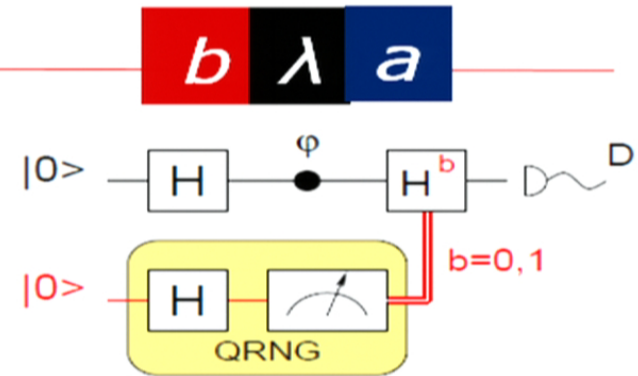
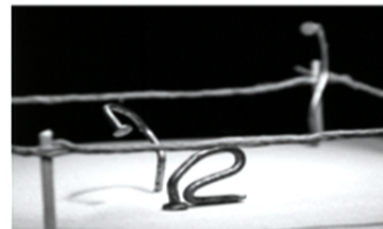
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Stochastic...

$$p(\lambda|b) = p(\lambda) = (p, 1-p)$$

Consistency requirements resurrect wave-particle duality<sup>†</sup>:

$$p(a|b, \lambda) = p(a|b)$$

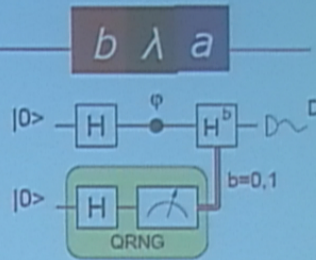


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# WDC Logic

$$q(a,b) = \sum_{\lambda} \boxed{\text{data}} \quad \boxed{\text{HV theory}} \quad \boxed{\text{IC}} \quad \boxed{n(b)}$$

$$q(a,b) = \sum_{\lambda} p(a|b,\lambda) \times p(\lambda|b) \times n(b)$$



Causal:

$$p(\lambda|b) = \delta_{\lambda p} \delta_{b0} + \delta_{\lambda w} \delta_{b1}$$

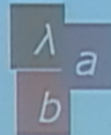
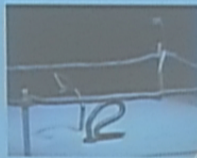
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# DELAYED CHOICE

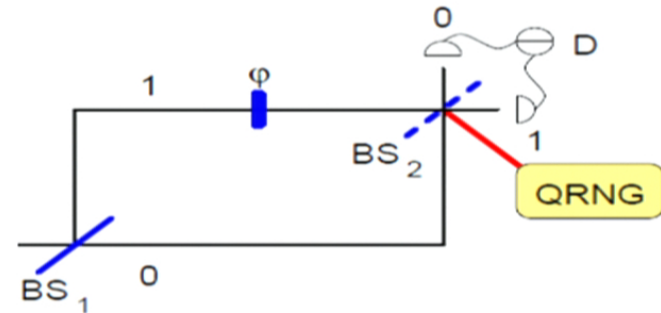
## + QRNG

Open interferometer [particle]

$$q(a) = \left(\frac{1}{2}, \frac{1}{2}\right)$$

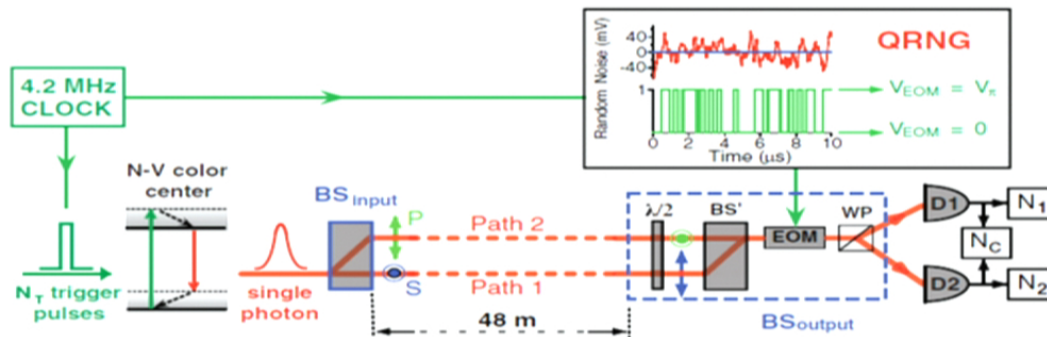
Closed interferometer [wave]

$$q(a) = \left(\cos^2 \frac{\phi}{2}, \sin^2 \frac{\phi}{2}\right)$$



**b**

Jacques *et al.*,  
Science **315**, 966 (2007)



**a**

Spacelike separation between  
the source and the RNG

## **PART 3**

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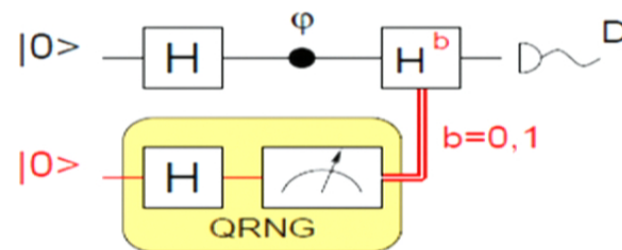
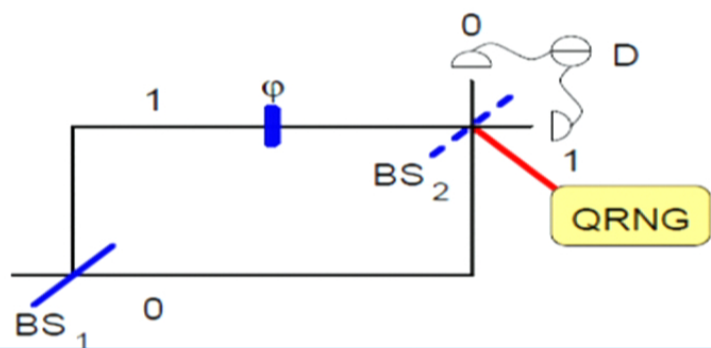
### ***QUANTUM CONTROL***

Evolution of control

Different set-ups and complementarity

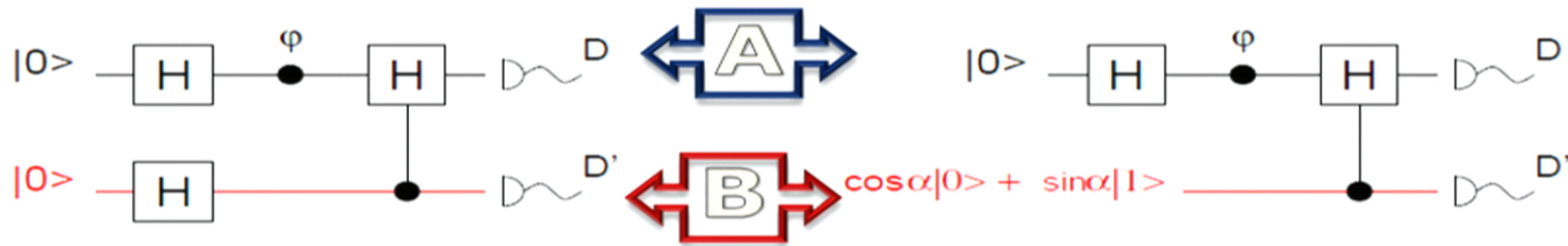
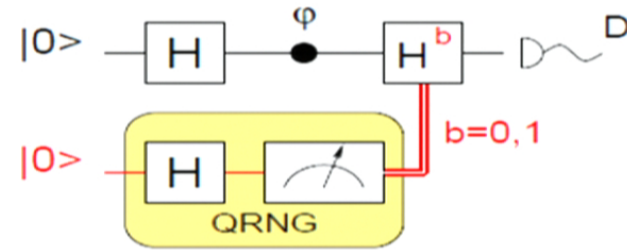
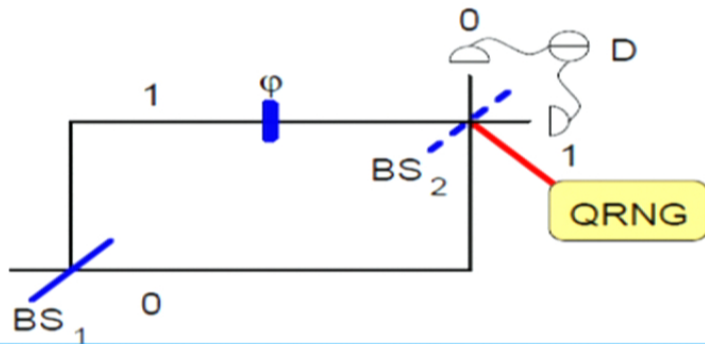
Some experiments

# QUANTUM CONTROL



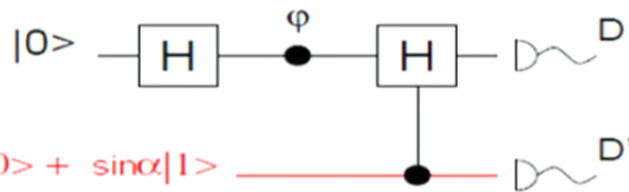


# QUANTUM CONTROL



DC

+ Q



- We can detect "it" first and decide what was it later
- No space-like separation
- Duality restored OR HV pushed away (half-step)

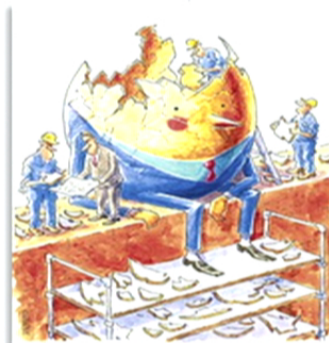
Consistency requirements resurrect wave-particle duality:

$$p(a | b, \lambda) = p(a | b)$$

$$p = 0, x = \frac{1}{2}$$

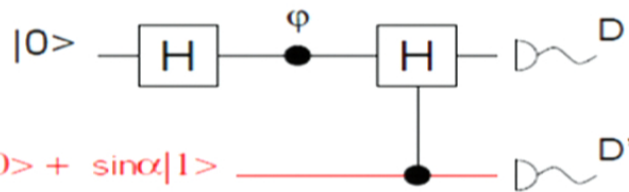
$$p = 1, y = \cos^2 \frac{\phi}{2}$$

$$x = \frac{1}{2}, y = \cos^2 \frac{\phi}{2}$$



DC

+ Q



- Can we detect "it" first and decide what was it later
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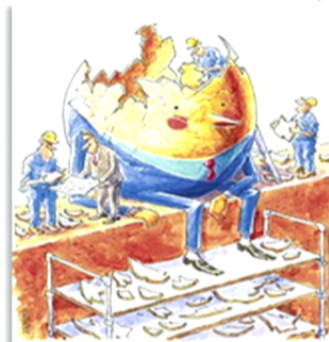
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$$x = \frac{1}{2}, y = \cos^2 \frac{\phi}{2}$$



Or  
imply a higher level conspiracy

$$p(\lambda) = (\cos^2 \alpha, \sin^2 \alpha)$$

Small print:

- If you don't mind this weird causal interaction... but can get rid of it by more delays ... but
- HV only on a photon

## DELAYED CHOICE | COMPLEMENTARITY

---

### *[a tagline v 2.0]*

- ❑ Complementary phenomena can be observed with a single experimental setup, provided that a component of the apparatus is a quantum device in a superposition state. Instead of complementarity of experimental setups (Bohr's view) we have complementarity of the experimental data.
- ❑ There is no inversion of the normal order of time—in our case we measure the photon before the ancilla deciding the experimental setup (open or closed interferometer). It is only after we interpret the photon data, by correlating them with the results of the ancilla, that either a particlelike or wavelike behaviour emerges: behaviour is in the eye of the observer.

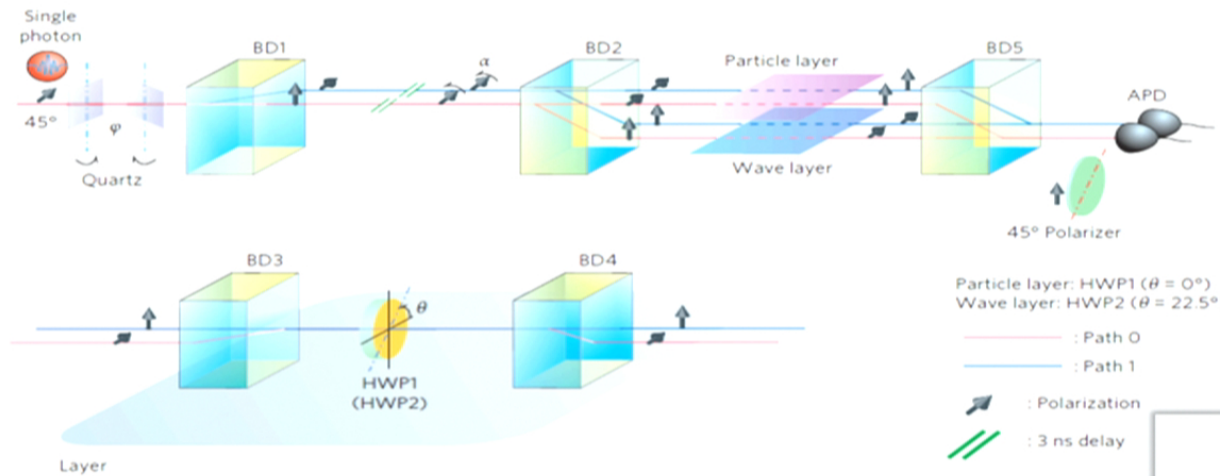
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# EXPERIMENTS



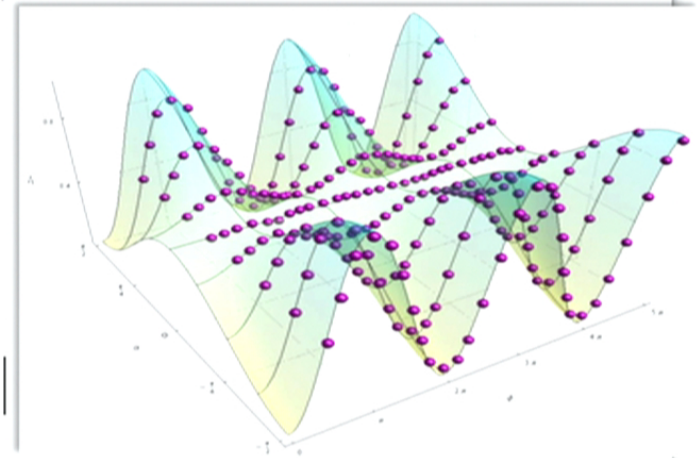
QOpt  
implementation

Tang *et al.*,  
Nature Phot. **6**,  
602 (2012)

- ❑ demonstration of standard predictions
- ❑ different counting statistics for

and 
$$|\psi_f\rangle = \cos \alpha |\psi_p\rangle |0\rangle + \sin \alpha |\psi_w\rangle |1\rangle$$

$$\rho = \cos^2 \alpha |\psi_p\rangle \langle \psi_p| + \sin^2 \alpha |\psi_w\rangle \langle \psi_w|$$

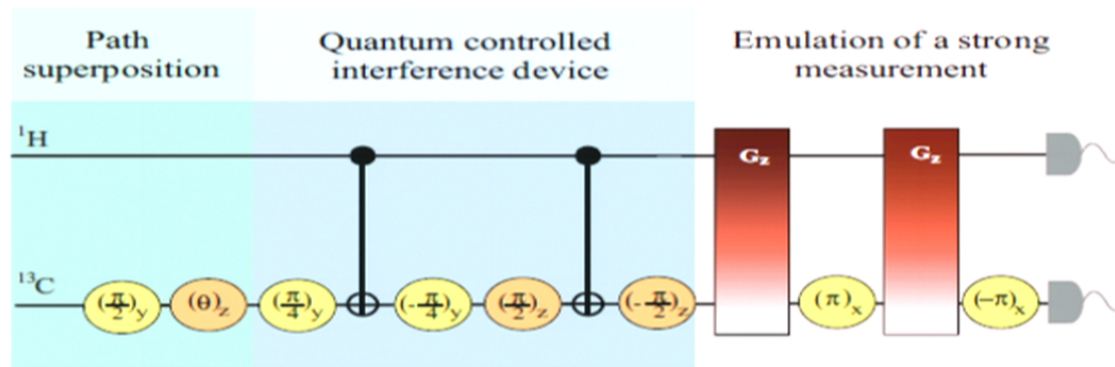


# EXPERIMENTS

## “exotic” systems

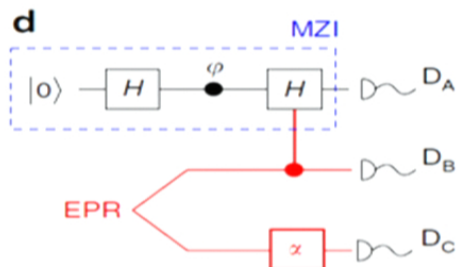
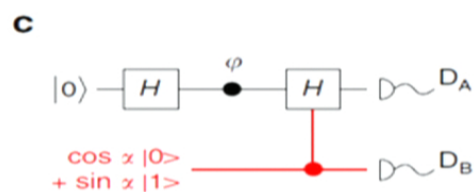
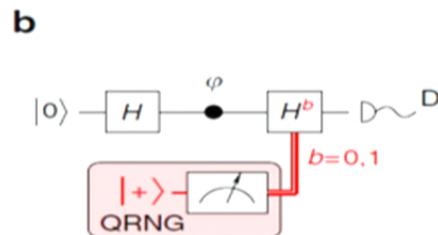
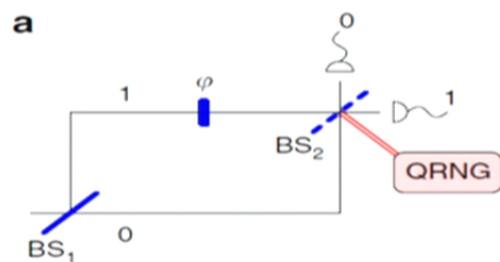
Since there is no space-like separation, it can be done with NMR

Auccaise *et al*, Phys. Rev. A **85**, 032121 (2012)



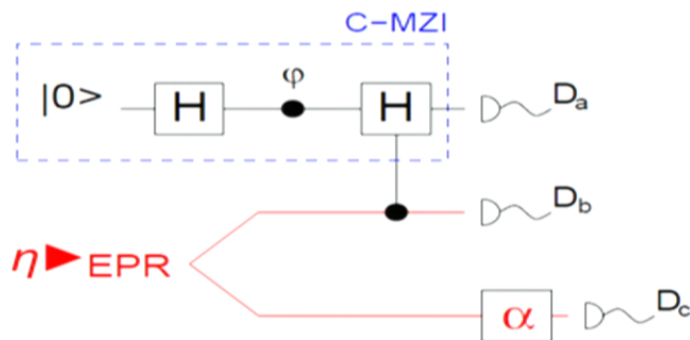
The first block represents the initial state preparation and employs the two interferometric paths. The second block performs a controlled interference between the two superposition paths encoded in the carbon spin. A controlled-Hadamard gate is decomposed in four single-qubit rotations and two CNOT gates. The third block emulates a strong measurement of the hydrogen spin in the  $\sigma_z$  eigenbasis by means of partial dephasing circuit

# DC + entanglement





# DC + entanglement



## Box 1 | Three classical assumptions.

**Wave-particle objectivity.** We define particles and waves according to the experimental behaviour in an open, respectively closed, MZI<sup>11</sup>. A particle in an open interferometer ( $b = 0$ ) is insensitive to the phase shift in one of the arms and therefore has the statistics

$$p(a | b = 0, \Lambda) = (\frac{1}{2}, \frac{1}{2}), \quad \forall \Lambda \in \mathcal{L}_p. \quad (3)$$

In contrast, a wave in a closed MZI ( $b = 1$ ) shows interference

$$p(a | b = 1, \Lambda) = (\cos^2 \frac{\varphi}{2}, \sin^2 \frac{\varphi}{2}), \quad \forall \Lambda \in \mathcal{L}_w. \quad (4)$$

The sets  $\mathcal{L}_p$  and  $\mathcal{L}_w$  must be disjoint; otherwise, there are values of  $\Lambda$  that introduce wave-particle duality. Writing  $\mathcal{L}_p \cup \mathcal{L}_w = \mathcal{L}$ , the wave/particle property is expressed by a mapping  $\lambda: \mathcal{L} \mapsto \{p, w\}$  and the sets  $\mathcal{L}_p = \lambda^{-1}(p)$ ,  $\mathcal{L}_w = \lambda^{-1}(w)$  are the pre-images of  $p$ ,  $w$  under the function  $\lambda$ .

**Determinism.** The HV  $\Lambda$  determines the individual outcomes of the detection<sup>3</sup>. Specifically, for the setup of (Fig. 1d)

$$p(a, b, c | \Lambda) = \chi_{abc}(\Lambda), \quad (5)$$

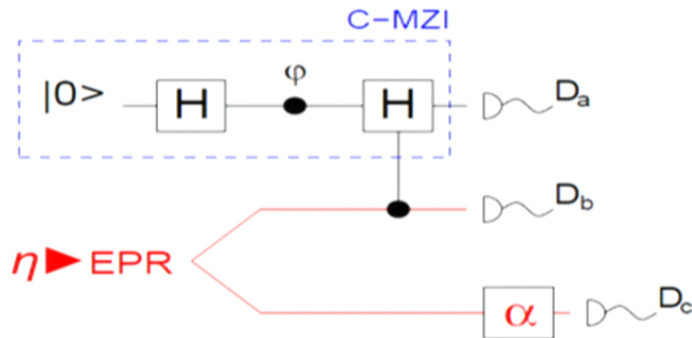
where the indicator function  $\chi = 1$ , if  $\Lambda$  belongs to some predetermined set, and  $\chi = 0$  otherwise.

**Local independence.** The HV  $\Lambda$  are split into  $\Lambda_1$  and  $\Lambda_2$ , and the prior probability distribution has a product structure

$$p(\Lambda) = f(\Lambda_1)F(\Lambda_2), \quad (6)$$

for some probability distributions  $f$  and  $F$ , where the subscripts 1 and 2, respectively, refer to the photon A and the pair BC. Such bilocal variables have been previously considered in ref. 29.

# DC + entanglement



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## DC + entanglement

## logic

1. QM analysis:  $q(a,b,c)$

2. Solution to the constraints: finding the HV theory

$$p(a,b,c,\lambda) : \sum_{\lambda=p,w} p(a,b,c,\lambda) = p(a,b,c) \equiv q(a,b,c)$$

A non-trivial HV theory requires that  $\lambda$  is determined by the degree of entanglement:

$$p(\lambda) = (\eta, 1 - \eta)$$



## DC + entanglement

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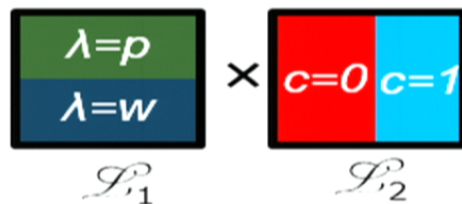
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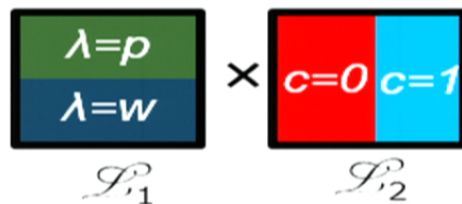
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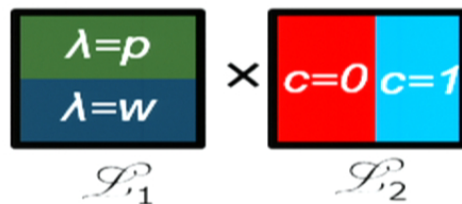
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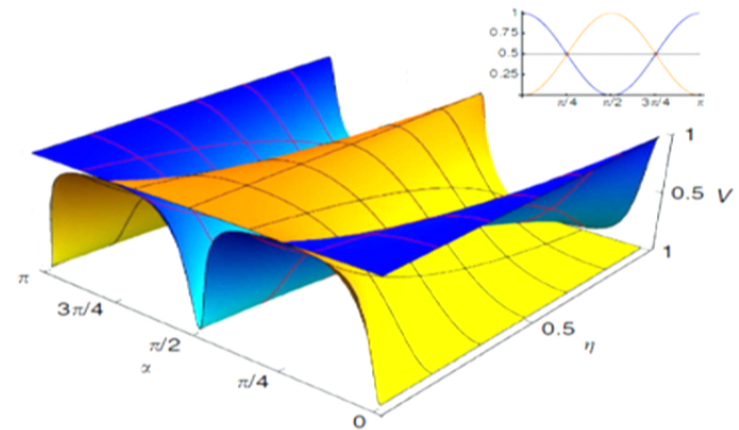
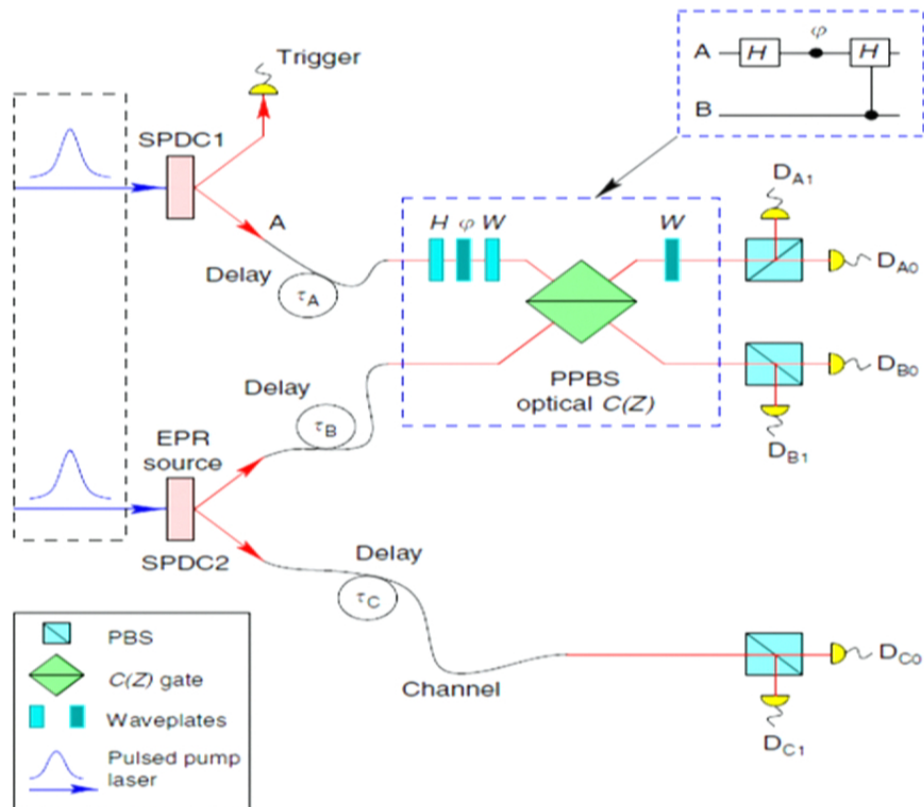


### CONTRADICTION

Solution for  $p(a,b,c,\lambda)$  exists only if

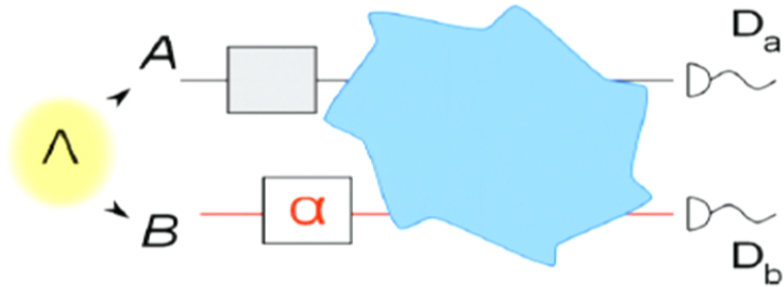
$$\cos^2 \alpha = 0$$

# DC + entanglement experimental signature



IJMT,  
Nature Comm. **5**, 3997 (2014)

## THREE INCOMPATIBLE ASSUMPTIONS



Empirical statistics

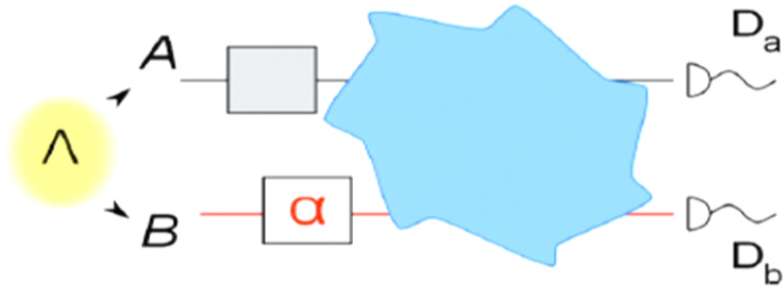
$$e(a, b) = (xe_p, (1-x)e_w, x(1-e_p), (1-x)(1-e_w))$$

$$e(b) = (x, 1-x) \quad \blacktriangleleft \text{controller}$$

two types of stats  $\blacktriangleright$   $\bar{e}_p(a) = (e_p, 1 - e_p), \quad \bar{e}_w(a) = (e_w, 1 - e_w)$



## THREE INCOMPATIBLE ASSUMPTIONS



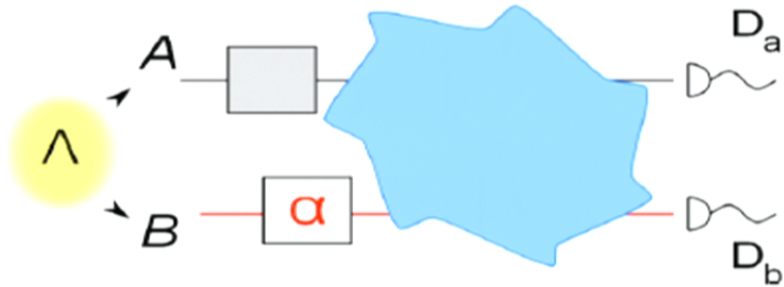
Empirical statistics

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# THREE INCOMPATIBLE ASSUMPTIONS



**(\*) Adequacy**

Empirical statistics

$$e(a, b) = (xe_p, (1-x)e_w, x(1-e_p), (1-x)(1-e_w))$$

$$e(b) = (x, 1-x) \quad \blacktriangleleft \text{controller}$$

two types of stats  $\blacktriangleright \bar{e}_p(a) = (e_p, 1 - e_p), \quad \bar{e}_w(a) = (e_w, 1 - e_w)$

$$e(a, b) = p(a, b) = \sum_{\Lambda} p(a, b, \Lambda) = \sum_{\Lambda} p(a, b|\Lambda) p(\Lambda)$$

## THREE INCOMPATIBLE ASSUMPTIONS

---

The system is definitely s one or another

$$p(a|b = 1, \lambda = w) = \bar{e}_w(a)$$

$$p(a|b = 0, \lambda = p) = \bar{e}_p(a)$$

**(i) Objectivity**

$$\lambda = \lambda(\Lambda)$$

## THREE INCOMPATIBLE ASSUMPTIONS

The system is definitely s one or another

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**(i) Objectivity**

$$\lambda = \lambda(\Lambda)$$

HV theory is (weakly) deterministic

$$p(a, b|\Lambda) = \chi_{ab}(\Lambda)$$

**(ii) Determinism**

00

01

10

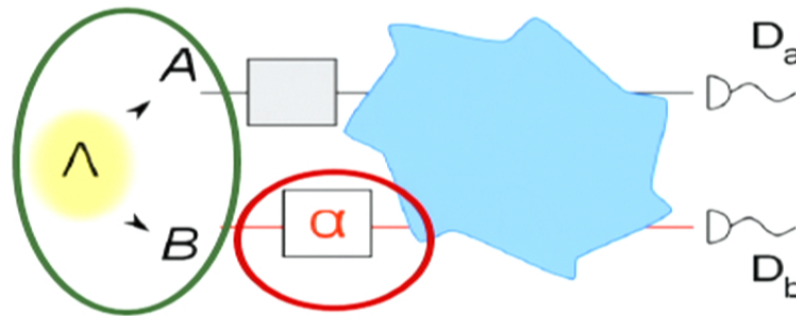
11

Boundaries of the regions  
depend on the settings

# THREE INCOMPATIBLE ASSUMPTIONS

Is  $\lambda$ -independent

**(iii) Independence**



$p(\Lambda)$  is independent of the settings

IMT, Phys. Rev. Lett. **114**,  
060405 (2015)

# THREE INCOMPATIBLE ASSUMPTIONS

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## LOGIC

**Stage 1:** find a unique non-trivial solution to (i)-(iii)  
Ignoring how it arises from  $\Lambda$

# THREE INCOMPATIBLE ASSUMPTIONS

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**Stage 1:** find a unique non-trivial solution to (i)-(iii)

Ignoring how it arises from  $\Lambda$

Exists, but

$$p_s(\lambda | b) = \delta_{\lambda p} \delta_{b0} + \delta_{\lambda w} \delta_{b1} = p_s(b | \lambda)$$

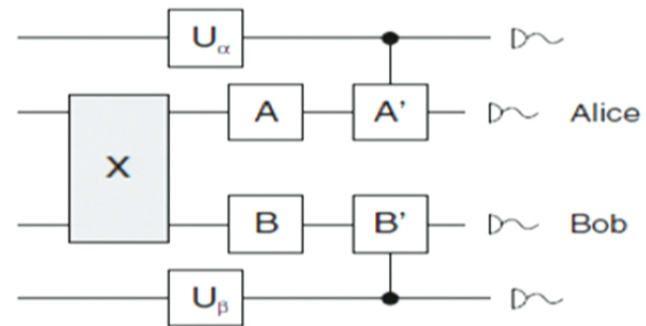
$$p_s(a, b, \lambda) = e(a, b) p_s(b | \lambda)$$

00	01
10	11
p	w

# FUTURE

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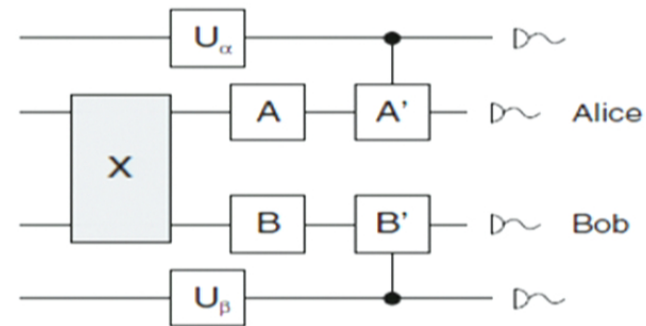
Quantum-controlled CHSH?



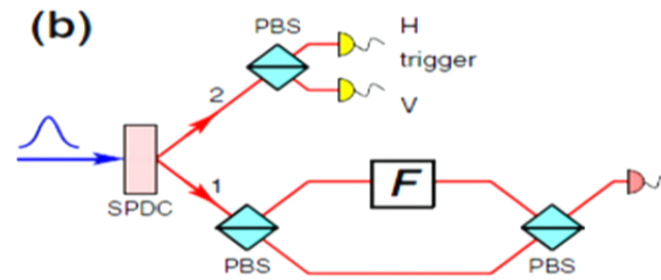
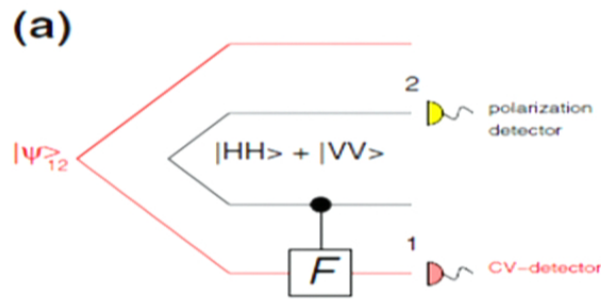


# FUTURE

Quantum-controlled CHSH?



Quantum-controlled von Weizsäcker?



Céleri, Gomes, IJMT, Found. Phys. **44**, 576 (2014)

## SUMMARY

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- Hidden variables are useful
- Quantum control: practical & conceptual features
- Entangled control
- Don't (always) blame quantum mechanics
- More?

Thanks to  
Roger Colbeck  
Bert Englert  
Mile Gu  
Gerard Milburn  
Alberto Peruzzo  
Valerio Scarani

