

Title: Discussion 4

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Abstract:

$$\bar{J} = (g^{-1} \bar{\partial} g)$$

$$J = (g^{-1} \partial g)$$

$$\begin{matrix} \nearrow J^a \\ \rightarrow J^{\hat{\alpha}}, J^{\hat{\beta}} \\ \searrow J^{mn} \end{matrix}$$

$$a = 0 \dots 9$$

$$\hat{\alpha}, \hat{\beta} = 1 \dots 16$$

$$mn \in SO(4,1) \sim SO(5)$$

$$g \in PSU(2,2|4) / SO(4,1) \times SO(5)$$

$$(\gamma^{0(234)})_{\alpha\beta} = \delta_{\alpha\beta}$$

$$\int d^2z \left(J^a \bar{J}^a + (J^{\hat{\alpha}} \bar{J}^{\hat{\beta}} - J^{\hat{\beta}} \bar{J}^{\hat{\alpha}}) \delta_{\hat{\alpha}\hat{\beta}} + \frac{1}{2} (J^{\hat{\alpha}} \bar{J}^{\hat{\alpha}} + J^{\hat{\beta}} \bar{J}^{\hat{\beta}}) \delta_{\hat{\alpha}\hat{\beta}} \right) \left(\frac{1}{2} (\partial \theta^{\hat{\alpha}} \bar{\partial} \theta^{\hat{\beta}} - \partial \theta^{\hat{\beta}} \bar{\partial} \theta^{\hat{\alpha}}) \right)$$

$$+ \omega \bar{\nabla} \lambda + \hat{\omega} \nabla \hat{\lambda} + R(\omega \not{X} \hat{\omega} \hat{\lambda})$$

$$\omega \bar{\nabla} \lambda = \omega \bar{\partial} \lambda + (\omega \gamma^{mn} \not{J}) J_{mn}$$

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$$J = (g^{-1} \partial g)$$

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$$\hat{\alpha}, \hat{\beta} = 1 \dots 16$$

$$mn \in SO(4,1) \sim SO(5)$$

$$g \in PSU(2,2|4) / SO(4,1) \times SO(5)$$

$$(\gamma^{01234})_{\alpha\beta} = \delta_{\alpha\beta}$$

$$\begin{aligned} & r^2 \int d^2z \left(J^a \bar{J}^a + (J^{\hat{\alpha}} \bar{J}^{\hat{\beta}} - J^{\hat{\beta}} \bar{J}^{\hat{\alpha}}) \delta_{\hat{\alpha}\hat{\beta}} \right. \\ & \quad \left. + \frac{1}{2} (J^{\hat{\alpha}} \bar{J}^{\hat{\alpha}} + J^{\hat{\beta}} \bar{J}^{\hat{\beta}}) \delta_{\hat{\alpha}\hat{\beta}} \right. \\ & \quad \left. + \omega \bar{\nabla} \lambda + \hat{\omega} \nabla \hat{\lambda} + R(\omega \not{\lambda} \hat{\omega} \hat{\lambda}) \right) \\ & \quad \left(\frac{1}{2} (\partial \theta^{\hat{\alpha}} \bar{\partial} \theta^{\hat{\beta}} - \partial \theta^{\hat{\beta}} \bar{\partial} \theta^{\hat{\alpha}}) \right) \end{aligned}$$

$$\omega \bar{\nabla} \lambda = \omega \bar{\partial} \lambda + (\omega \gamma^{mn}) \bar{J}_{mn}$$

$$\bar{J} = (g^{-1} \partial g)$$

$$J = (g^{-1} \partial g)$$

$$\begin{matrix} J^a & a=0 \dots 9 \\ J^\alpha, J^{\hat{\alpha}} & \alpha, \hat{\alpha}=1 \dots 16 \\ J^{mn} & m, n \in SO(4,1) \sim SO(5) \end{matrix}$$

$$g \in PSU(2,2|4) / SO(4,1) \sim SO(5)$$

$$(\gamma^{0(2,3,4)})_{\alpha\beta} = \delta_{\alpha\beta}$$

$$S = r^2 \int d^4x \left(J^a \bar{J}^a + (J^\alpha \bar{J}^{\hat{\alpha}} - J^{\hat{\alpha}} \bar{J}^\alpha) \delta_{\alpha\hat{\alpha}} + \frac{1}{2} (J^\alpha \bar{J}^{\hat{\alpha}} + J^{\hat{\alpha}} \bar{J}^\alpha) \delta_{\alpha\hat{\alpha}} + \omega \bar{\nabla} \lambda + \hat{\omega} \nabla \hat{\lambda} + R(\omega \star \hat{\omega} \hat{\lambda}) \right) \left(\frac{1}{2} \partial \theta^\alpha \bar{\partial} \theta^{\hat{\alpha}} - \partial \theta^{\hat{\alpha}} \bar{\partial} \theta^\alpha \right)$$

$$\omega \bar{\nabla} \lambda = \omega \bar{\partial} \lambda + (\omega \gamma^{mn} \lambda) J_{mn}$$

$$\frac{1}{J^\alpha \bar{J}^{\hat{\alpha}} \delta_{\alpha\hat{\alpha}}}$$

$$B = \left(\frac{1}{4!} \right) \left(\hat{\lambda} J^\alpha (\gamma_{\alpha} J)^{\hat{\alpha}} \right)$$

$$\bar{\partial} B = Q \lambda$$

$$\begin{aligned}
S_{\text{Trivial}} &= S_{\text{top}} = S_{r^2=0} = S_{G/G} \\
S_{\text{Trivial}} &= r^2 \int d^2 z \left(J^a \bar{J}^b \left(\frac{1}{4} \frac{\gamma_{ab}^I}{\lambda^I} \right) + \cancel{\frac{1}{4} \frac{\gamma_{ab}^I}{\lambda^I}} + J^v \bar{J}^2 \delta_{2,2} \right) \\
&= \int d^2 z (Q, \lambda) + \dots \\
S &= S_{\text{Trivial}} + S' \\
S' &= \frac{1}{4} \int d^2 z \left(\frac{\gamma_{ab}^I}{\lambda^I} \right) (J^a \bar{J}^b - J^b \bar{J}^a) + (J^v \bar{J}^2 - J^2 \bar{J}^v) \delta_{2,2}
\end{aligned}$$

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$$\begin{matrix} J^a \\ J^{\hat{a}}, J^{\hat{b}} \\ J^{mn} \end{matrix}$$

$$a=0 \dots 9$$

$$\alpha, \beta=1 \dots 16$$

$$m \in SO(4,1) \sim SO(5)$$

$$PSU(2,2|4)$$

$$PSU(2,2|4)$$

gauge-fix

$$T^a, T^{\hat{a}}, T^{\hat{b}}$$

$$PSU(2,2|4)$$

$$SO(4,1) \times SO(5)$$

$$S = r^2 \int d^2z \left(J^a \bar{J}^a + (J^{\hat{a}} \bar{J}^{\hat{a}} - J^{\hat{b}} \bar{J}^{\hat{b}}) \delta_{\hat{a}\hat{b}} + \frac{1}{2} (J^{\hat{c}} \bar{J}^{\hat{c}} + J^{\hat{d}} \bar{J}^{\hat{d}}) \delta_{\hat{c}\hat{d}} + \omega \bar{\nabla} \lambda + \hat{\omega} \nabla \hat{\lambda} + R(\omega \times \hat{\omega} \hat{\lambda}) \right) \left(\frac{1}{2} (\partial \theta^{\hat{a}} \bar{\partial} \theta^{\hat{a}} - \partial \theta^{\hat{b}} \bar{\partial} \theta^{\hat{b}}) \right)$$

$$+ \omega \bar{\nabla} \lambda + \hat{\omega} \nabla \hat{\lambda} + R(\omega \times \hat{\omega} \hat{\lambda})$$

$$\omega \bar{\nabla} \lambda = \omega \bar{\partial} \lambda + \omega \gamma^{mn} \lambda J_{mn}$$

$$\frac{1}{\lambda^2} \bar{\partial} \lambda \delta_{\hat{a}}^{\hat{a}}$$

$$B = \left(\frac{1}{4\pi} \right) \left(\hat{\lambda} J^{\hat{a}} (\partial_{\hat{a}} J)^{\hat{b}} \right)$$

$$\bar{\partial} B = Q \lambda$$

$$\bar{J} = (g^{-1} \partial g)$$

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$$T^a, T^{\hat{a}}, T^{\hat{b}}$$

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$$SO(4,1) \times SO(5)$$

$$S = r^2 \int d^2 \bar{z} \left(J^a \bar{J}^a + (J^{\hat{a}} \bar{J}^{\hat{a}} - J^{\hat{b}} \bar{J}^{\hat{b}}) \delta_{\hat{a}\hat{b}} + \frac{1}{2} (J^{\hat{c}} \bar{J}^{\hat{c}} + J^{\hat{d}} \bar{J}^{\hat{d}}) \delta_{\hat{c}\hat{d}} \right) \left(\frac{1}{2} \partial \theta^{\hat{a}} \bar{\partial} \theta^{\hat{a}} - \partial \theta^{\hat{b}} \bar{\partial} \theta^{\hat{b}} \right)$$

$$Q \left(\frac{\theta^{\hat{a}} \hat{a}^2 \delta_{\hat{a}\hat{b}}}{\lambda} \right)$$

$$+ \omega \bar{\nabla} \lambda + \hat{\omega} \nabla \hat{\lambda} + R(\omega \times \hat{\omega} \hat{\lambda})$$

$$Q(\cdot) = \frac{1}{\lambda^2 \bar{\lambda}^2 \delta_{\hat{a}\hat{b}}}$$

$$\omega \bar{\nabla} \lambda = \omega \bar{\partial} \lambda + \omega \gamma^{mn} \lambda J_{mn}$$

$$B = \left(\frac{1}{4\lambda} \right) \left(\hat{\lambda} J^{\hat{a}} (\partial_{\hat{a}} J)^{\hat{b}} \right)$$

$$\bar{\partial} B = Q \lambda$$

$$\begin{aligned}
 \bar{J} &= (g^{-1} \partial g) \\
 J &= (g^{-1} \partial g) \\
 \Lambda_a &= (g^{-1} (\lambda_L - \lambda_R) g)_a \\
 f^a_{bc} \Lambda_a & \quad \text{PSU}(2,2|4) \quad \text{PSU}(2,2|4) \quad \xrightarrow{\text{gauge-fix}} \quad T^+, T^-, T^z \quad \text{PSU}(2,2|4) / \text{SO}(4,1) \times \text{SO}(5) \\
 S &= r^2 \int d^4x \left(J^a \bar{J}^a + (J^+ \bar{J}^- - J^- \bar{J}^+) \delta_{12} + \frac{1}{2} (J^+ \bar{J}^z + J^z \bar{J}^+) \delta_{12} \right) \left(\partial_\mu \theta^\mu \bar{\partial} \theta^\mu - \partial \theta^\mu \bar{\partial} \theta^\mu \right) \\
 &\quad + \frac{1}{2} (J^- \bar{J}^z + J^z \bar{J}^-) \delta_{12} \\
 Q &\left(\frac{\theta^\mu \bar{\partial}^2 \delta_{12}}{\lambda_1} \right) + \omega \bar{\nabla} \lambda + \hat{\omega} \nabla \hat{\lambda} + R(\omega \hat{\omega} \hat{\lambda}) \\
 Q &= \frac{1}{\int \bar{J}^a J_a} \\
 \bar{\nabla} \lambda &= \omega \bar{\partial} \lambda + \omega \gamma^m_{-1} J_m \\
 B &= \left(\frac{1}{4!} \right) \left(\hat{\lambda} J^+ (\hat{\lambda} J)^z \right) \quad \bar{\partial} B = Q \lambda
 \end{aligned}$$





