

Title: Black hole information loss and discreteness of quantum geometry

Date: Apr 23, 2015 04:00 PM

URL: <http://pirsa.org/15040068>

Abstract: <p>In an approach to quantum gravity where space-time arises from coarse graining of fundamentally discrete structures, black hole formation and subsequent evaporation could be described by a unitary evolution without the problems encountered by standard remnant scenarios or the schemes where information is assumed to come out with the radiation while semiclassical evaporation (firewalls and complementarity). I point out the possibility that the final state is purified by correlations with the fundamental pre-geometric structures (in the sense of Wheeler) which are available in such approaches, and, like defects in the underlying space-time weave, can carry zero energy.</p>

Black Hole Information Loss in Quantum Gravity

**Revisiting the question
with an emphasis on discreteness**

PI

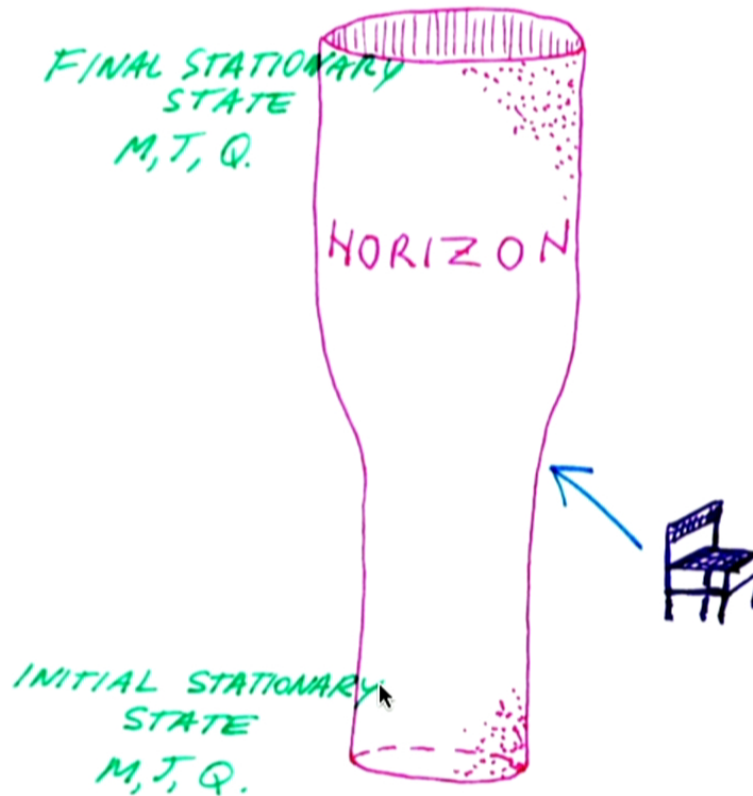
April 2015

**Alejandro Perez
Centre de Physique Théorique,
Marseille, France.**

Thursday 23 April 15

Black hole mechanics: analogy with thermodynamics

(2)



Some definitions

$$\left\{ \begin{array}{l} \Omega \equiv \text{horizon angular velocity} \\ \kappa \equiv \text{surface gravity ('grav. force' at horizon)} \\ \text{If } \ell^a = \text{killing generator, then } \ell^a \nabla_a \ell^b = \kappa \ell^b. \\ \Phi \equiv \text{electromagnetic potential.} \end{array} \right.$$

0th law: the surface gravity κ is constant on the horizon.

1st law:

$$\delta M = \frac{\kappa}{8\pi} \delta A + \underbrace{\Omega \delta J + \Phi \delta Q}_{\text{work terms}}$$

2nd law:

$$\delta A \geq 0$$

3rd law: the surface gravity value $\kappa = 0$ (extremal BH) cannot be reached by any physical process.

Black Hole Entropy

Temperature at infinity

$$T_{\infty} = \frac{\kappa}{2\pi}$$



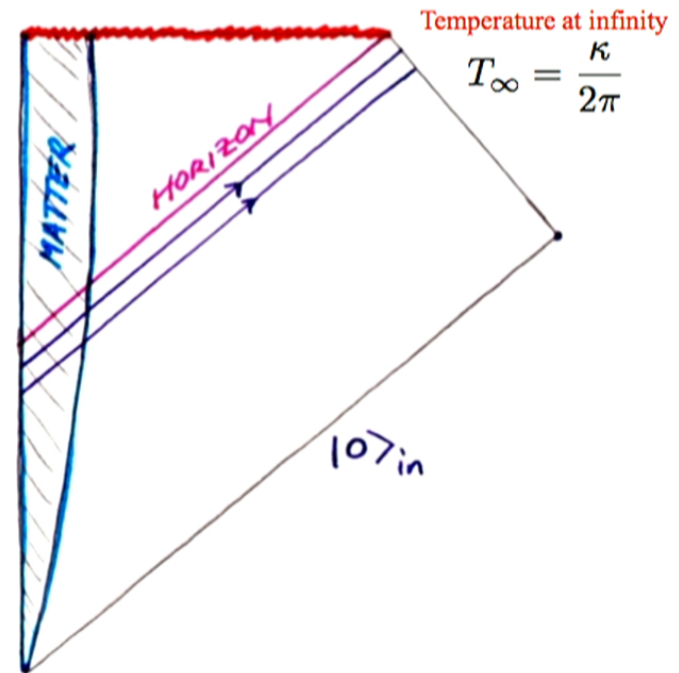
From the first law

$$\delta M = \frac{\kappa}{8\pi} \delta A + \Omega \delta J + \Phi \delta Q$$



One infers the ENTROPY

$$S = \frac{A}{4\ell_p^2}$$



Black Hole Entropy

Temperature at infinity

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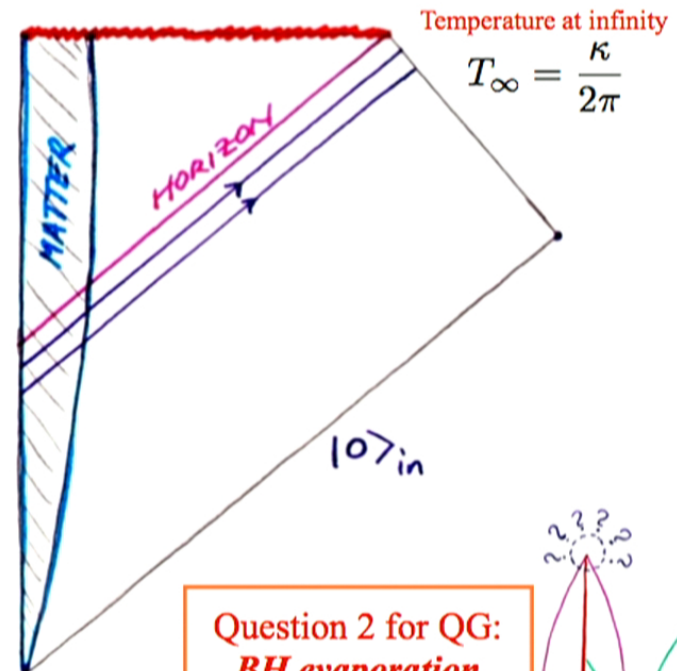
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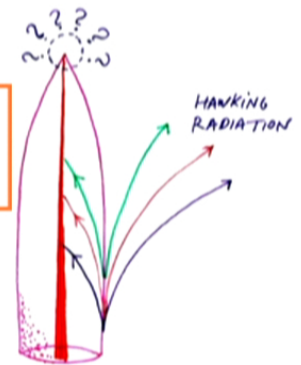
$$S = \frac{A}{4\ell_p^2}$$

Question 1 for QG:
*how to get S from
statistical mechanics.*



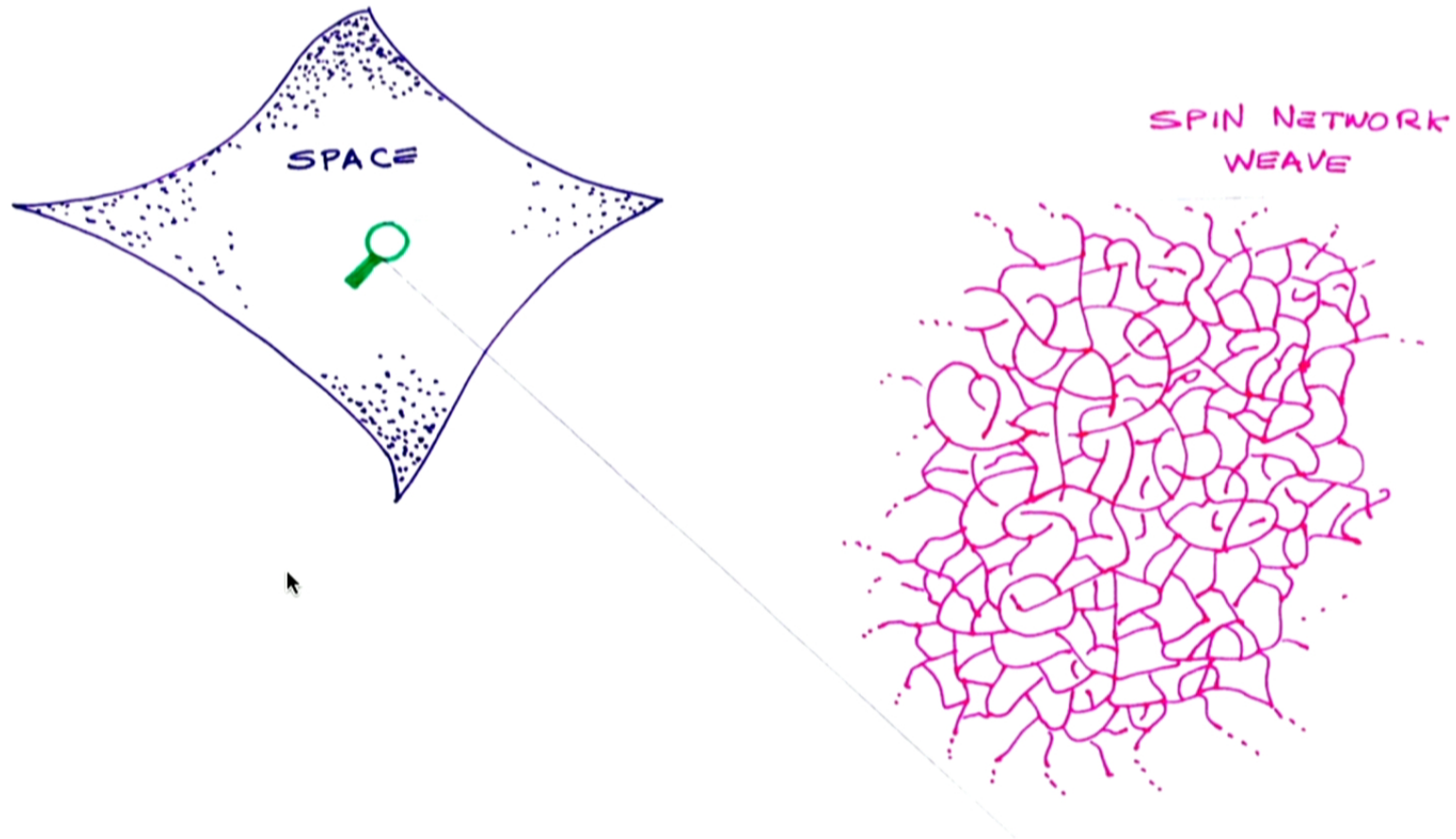
Question 2 for QG:
BH evaporation.

Question 3 for QG:
*information and
unitarity.*



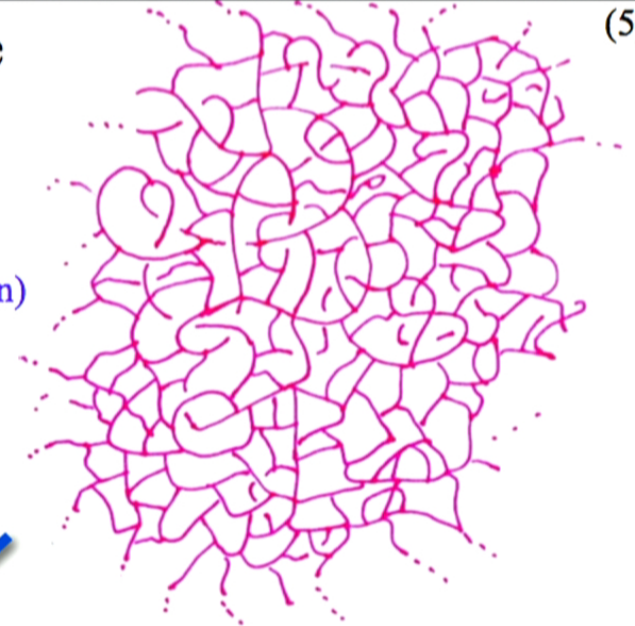
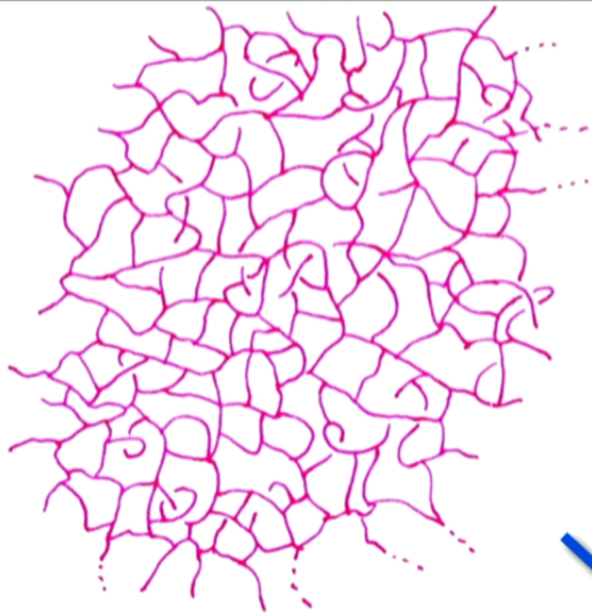
Quantum spacetime is made of discrete weave like excitations

(Ashtekar-Smolín-Rovelli)



Different weave states define the same spacetime

Smooth geometry is obtained by
coarse graining (Ashtekar et al. Rovelli-Smolín)

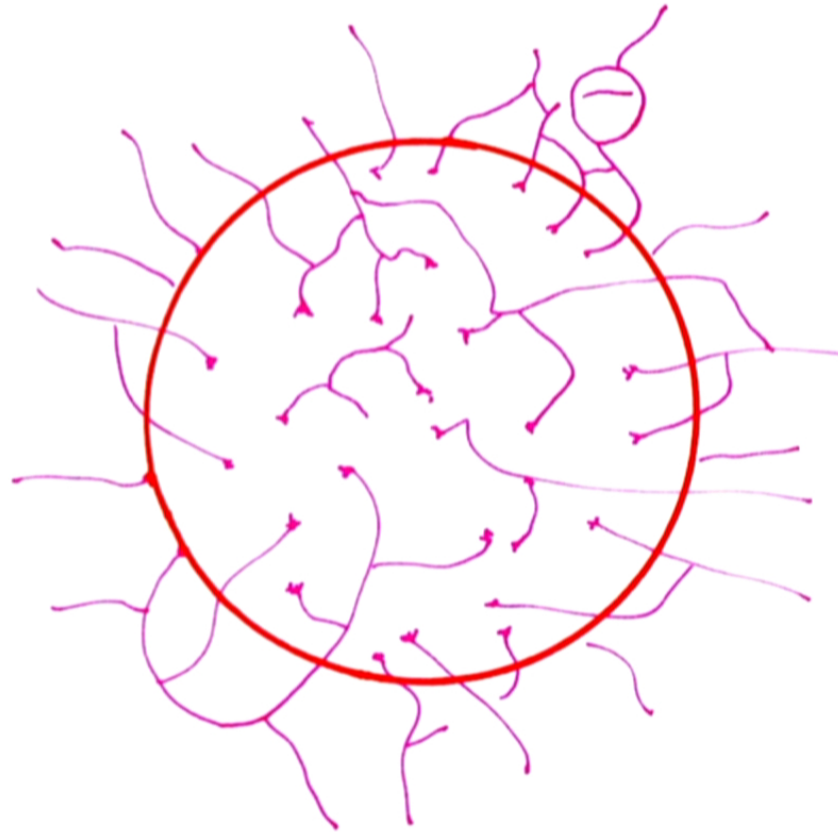


Q1: Black Hole Entropy is Horizon Entropy

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$$S_{stat} = \frac{A}{4G_N\hbar} + \eta \frac{\sqrt{A}}{\sqrt{\gamma G\hbar}}$$

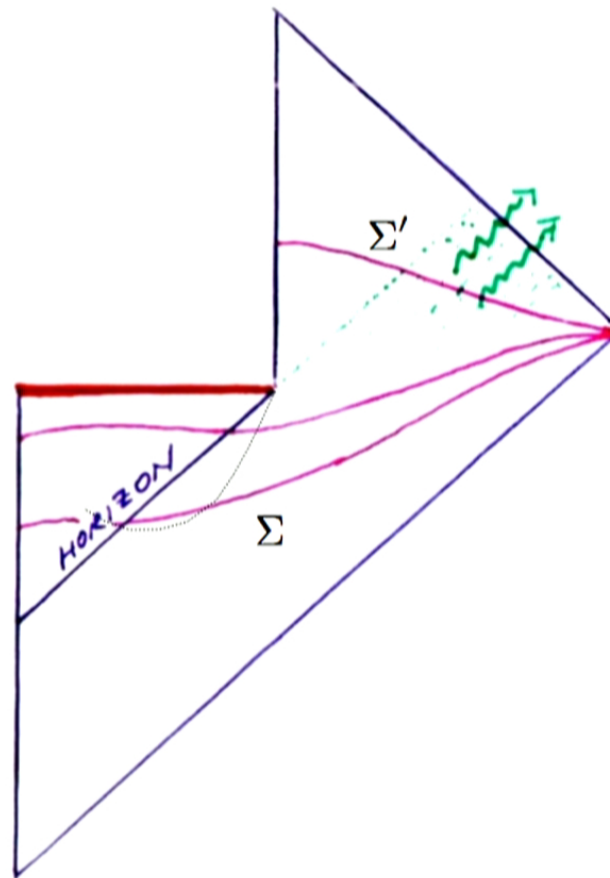
(Ghosh-Noui-AP 2014)



(Alesci, Ashtekar, Baez, Barbero, Bianchi, Borja, Corichi, Diaz-Polo, Engle, Frodden, Ghosh, Krasnov, Livine, Lewandowski, Majumdar, Mitra, Noui, AP, Pranzetti, Rovelli, Sahlmann, Terno, Thiemann, Villasenor, etc.)

Q3: Information loss paradox

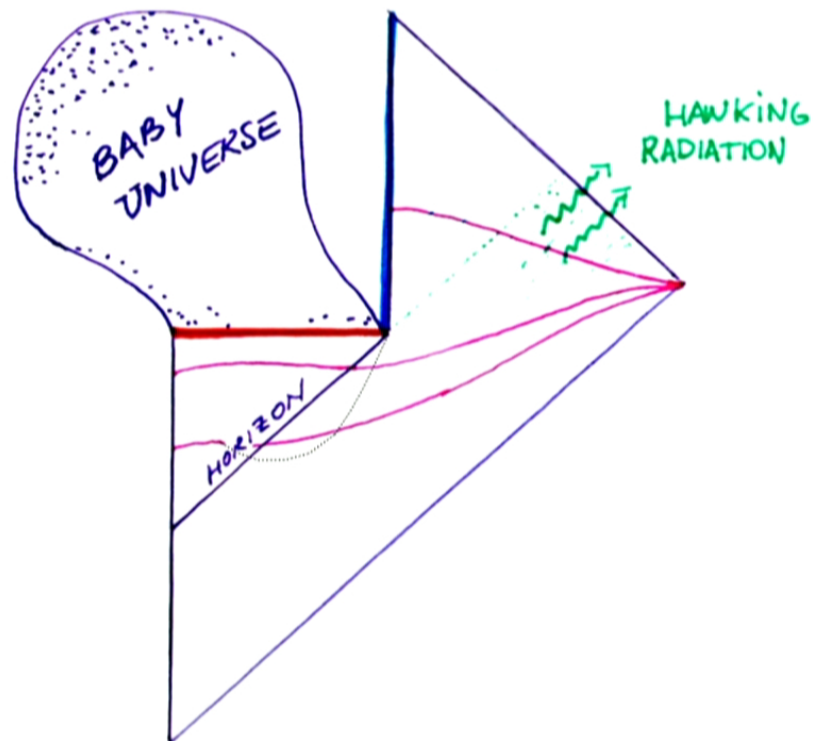
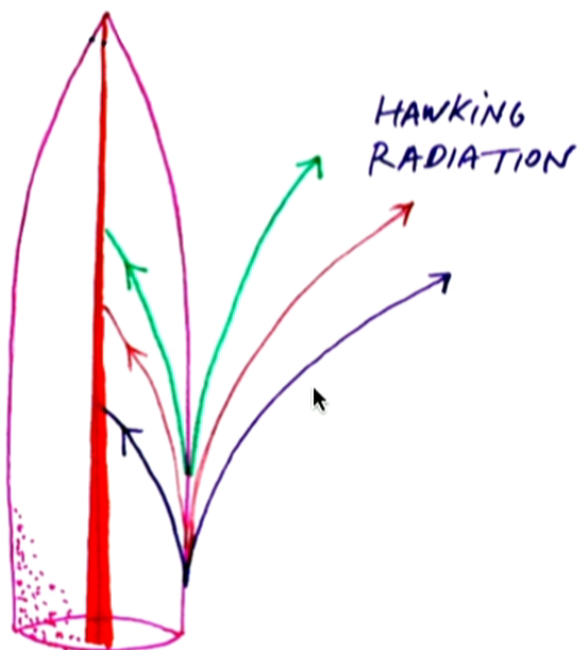
(Hawking 1976)



For a review on possibilities see
Hossenfelder-Smolin, Phys.Rev. D81
(2010) 064009

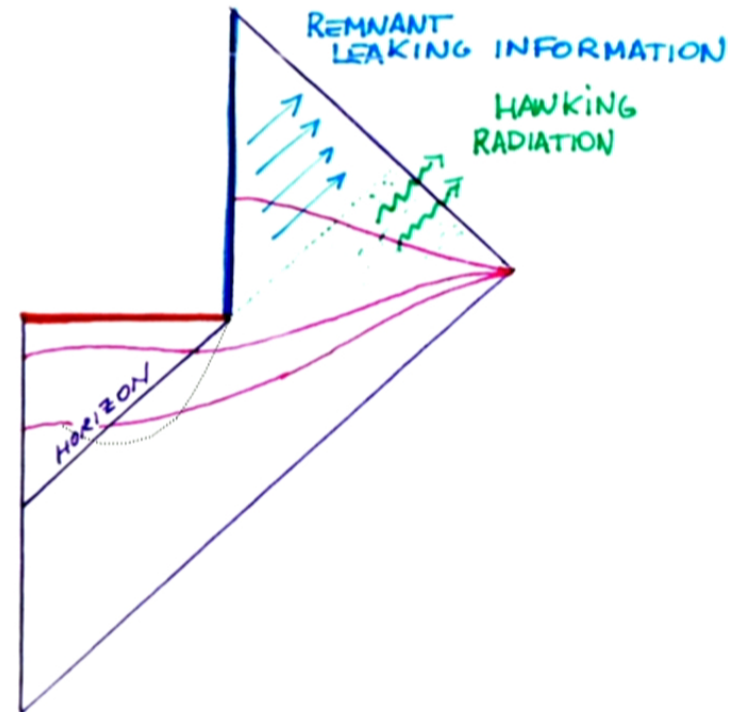
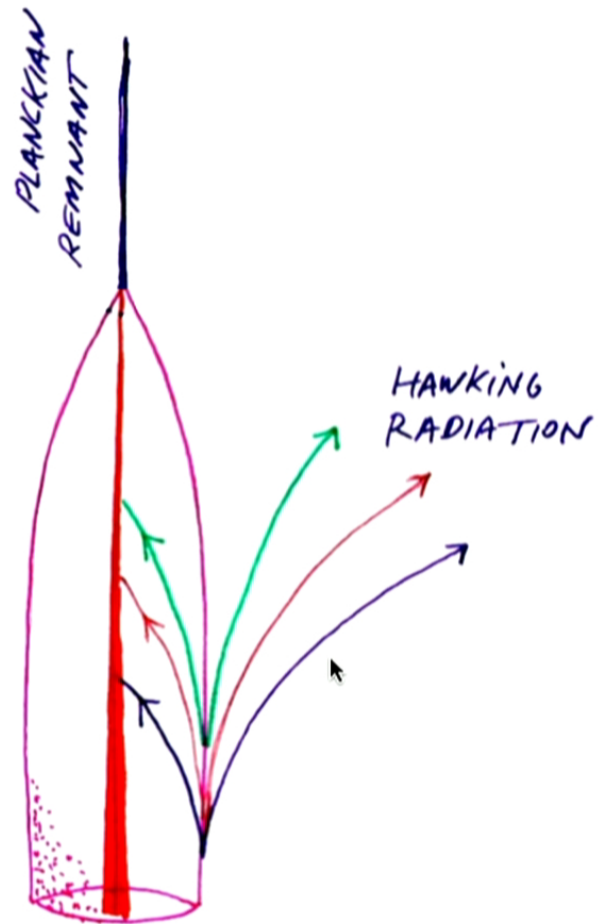
Proposal 1: baby universe

NOTHING
HAPPENS



Proposal 2: Remnants

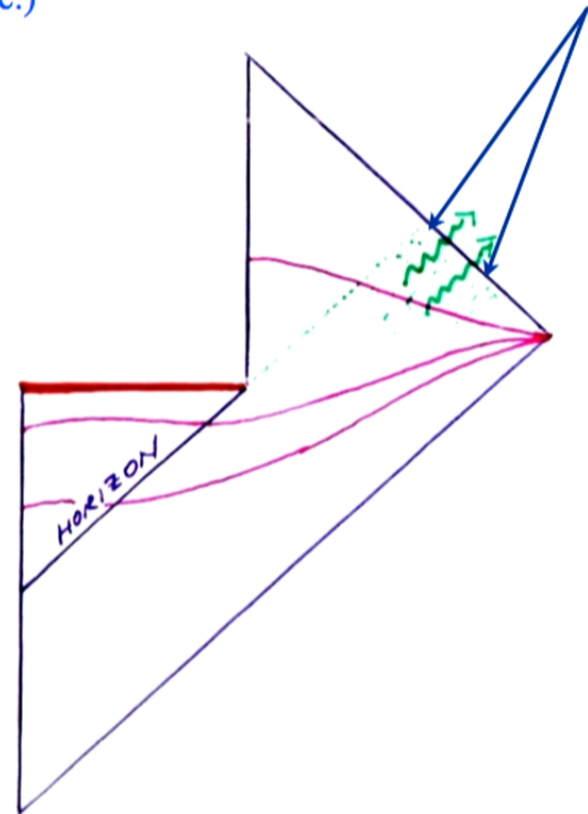
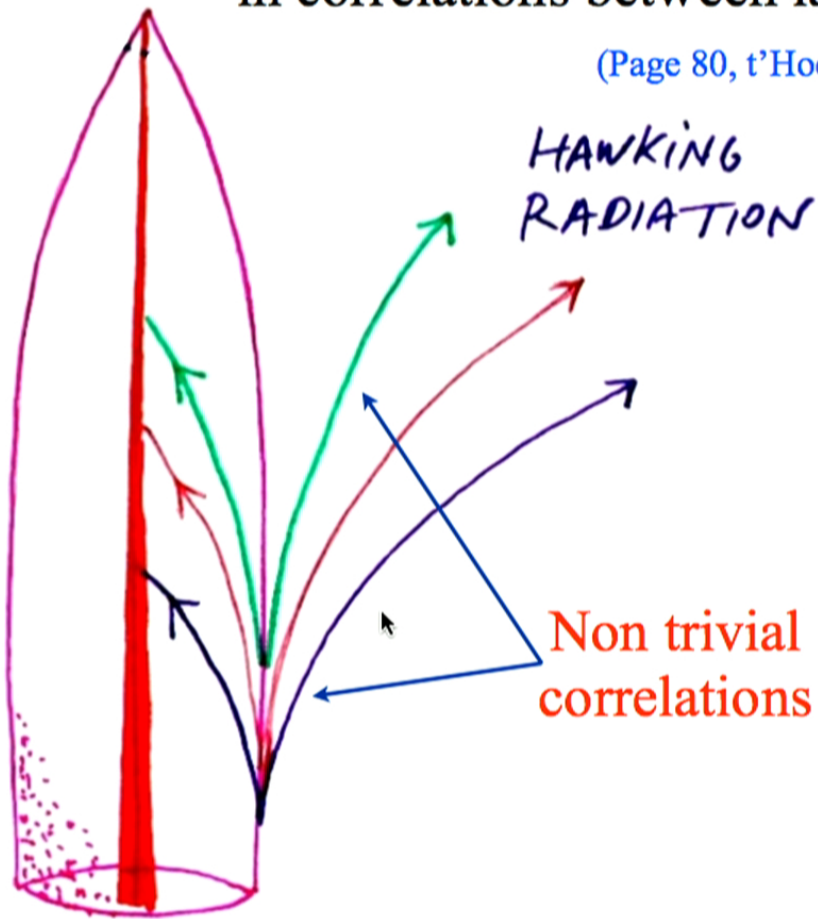
(Giddings 94, Banks 95)



Proposal 3:
 information is to be recovered
 in correlations between late and early hawking radiation

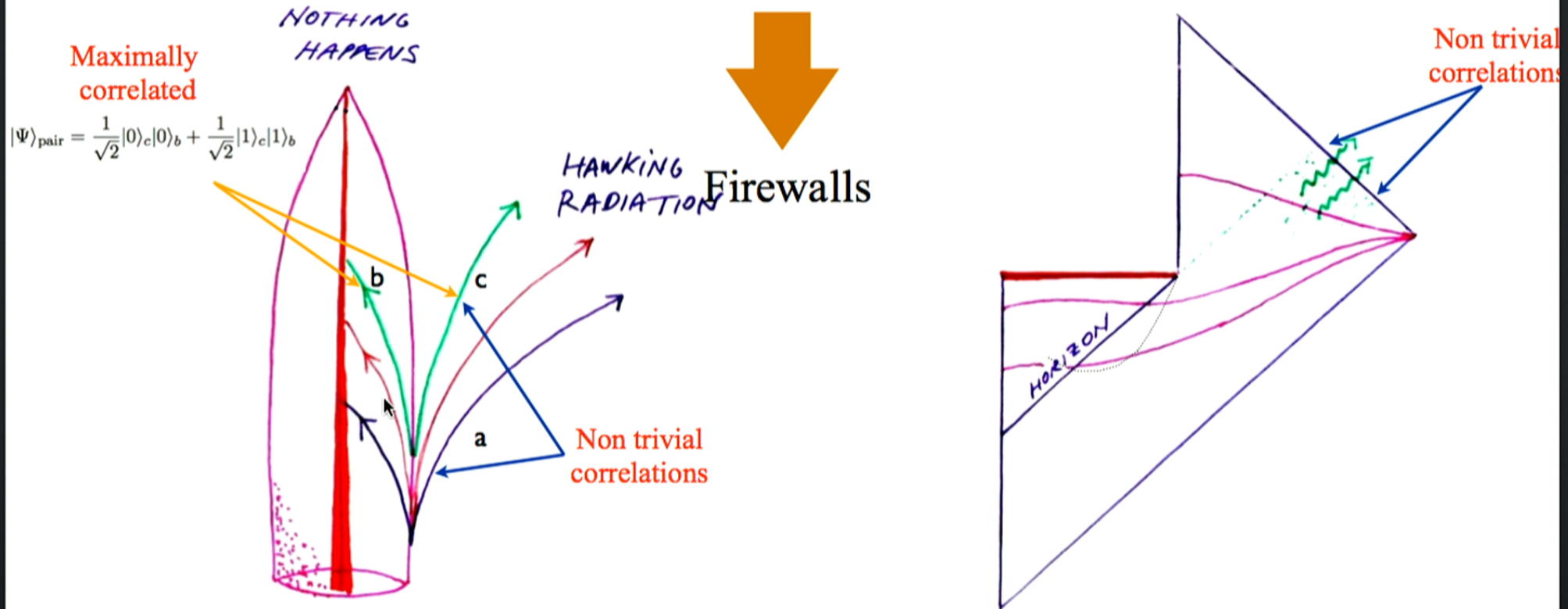
(Page 80, t'Hooft 90, Susskind 93, etc.)

**Non trivial
 correlations**



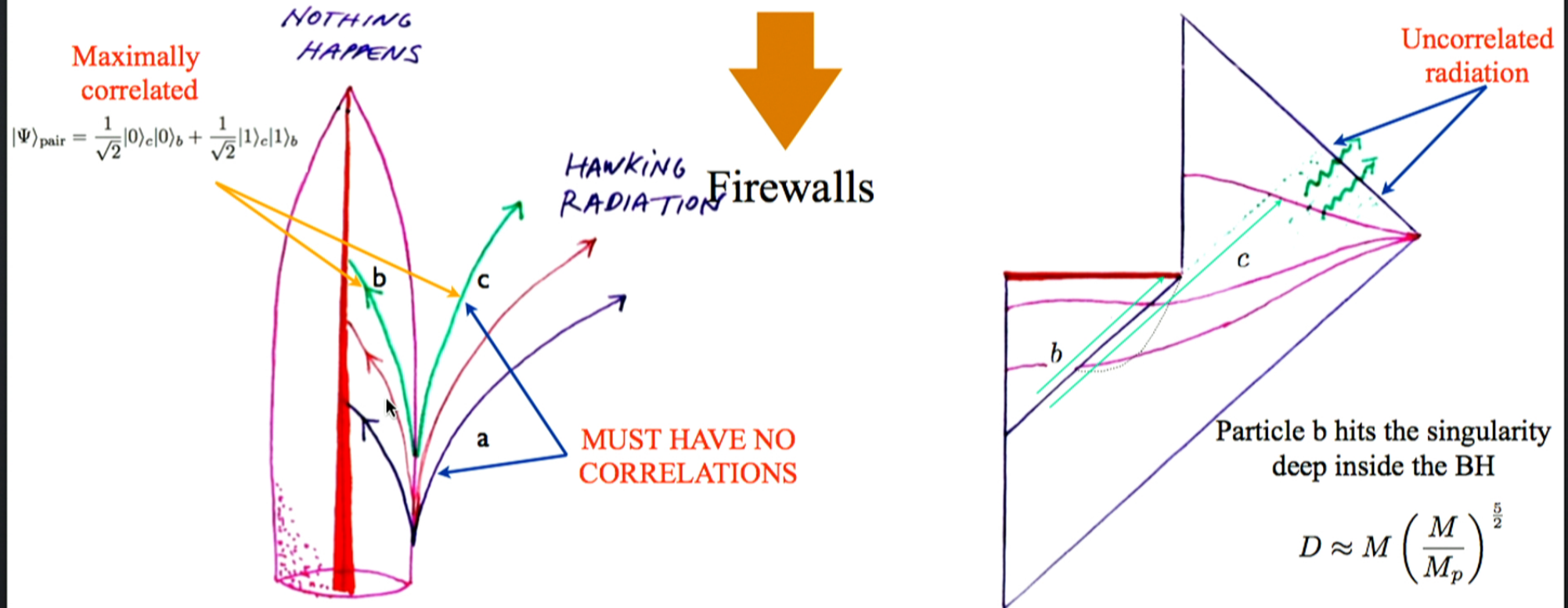
Proposal 3: information is to be recovered in correlations between late and early hawking radiation

(Almeheiri-Marolf-Polchinski-Sully
2013; S. L. Braunstein, S. Pirandola, and Kyczkowski, 2013)



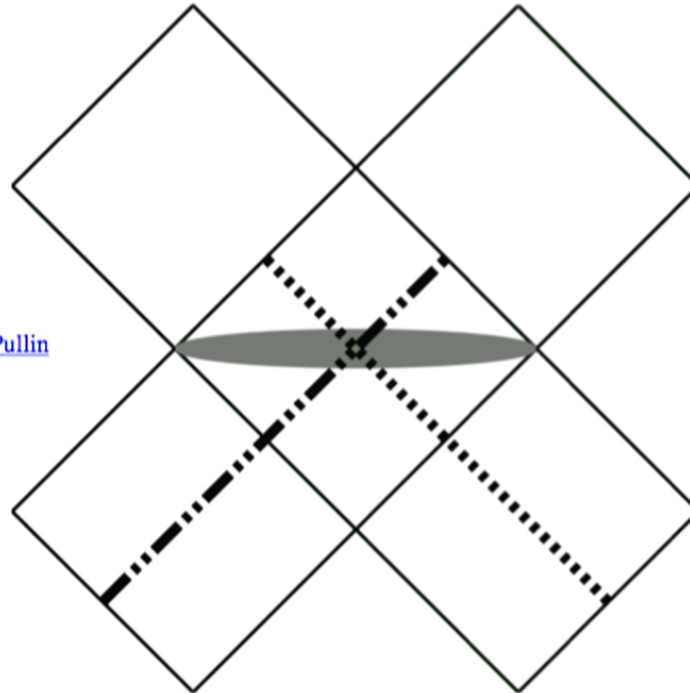
Proposal 3: information is to be recovered in correlations between late and early hawking radiation

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Bouncing at the singularity

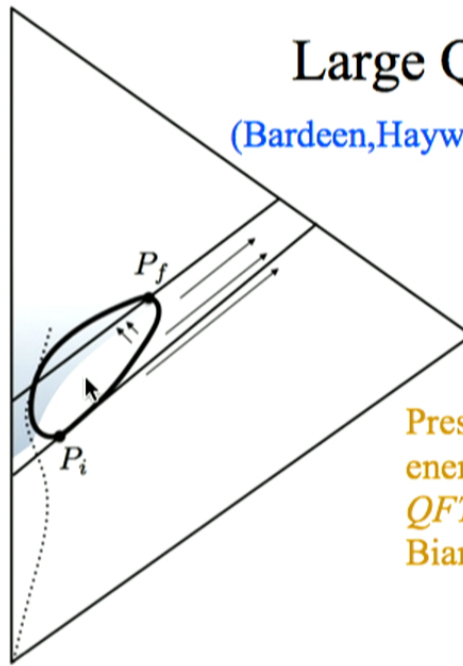
Quantum shells in a quantum space-time
[Rodolfo Gambini](#) (Republica U., Montevideo), [Jorge Pullin](#)
(Louisiana State U.). Aug 20, 2014. 5 pp.
Published in *Class.Quant.Grav.* 32 (2015) 3, 035003



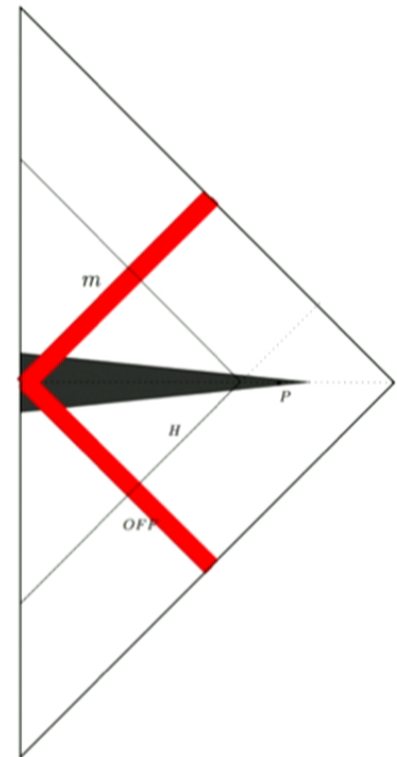
Proposal 4: Planck Stars

Large QG effects at low curvature

(Bardeen, Hayward, Rovelli-Vidotto, Rovelli-Haggard, etc)

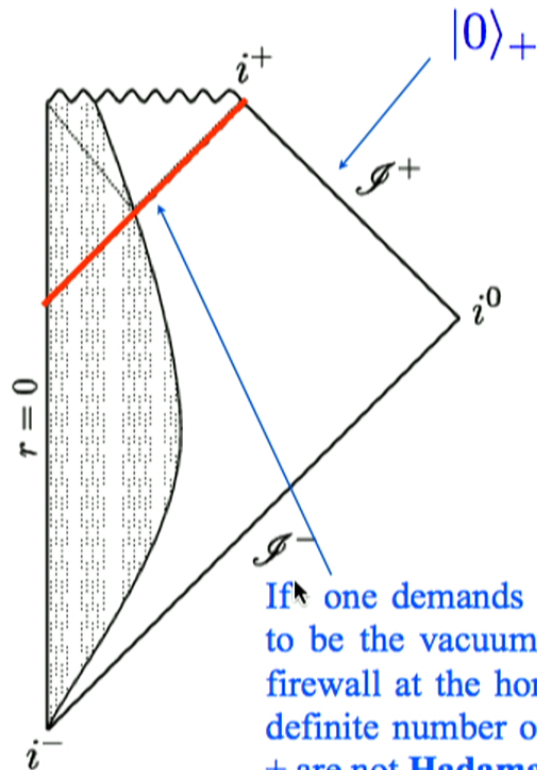


Present proposals are ruled out by energy conservation *if unitarity in the QFT sector holds* ([arXiv:1409.0144](#) Bianchi-De Lorenzo-Smerlak).



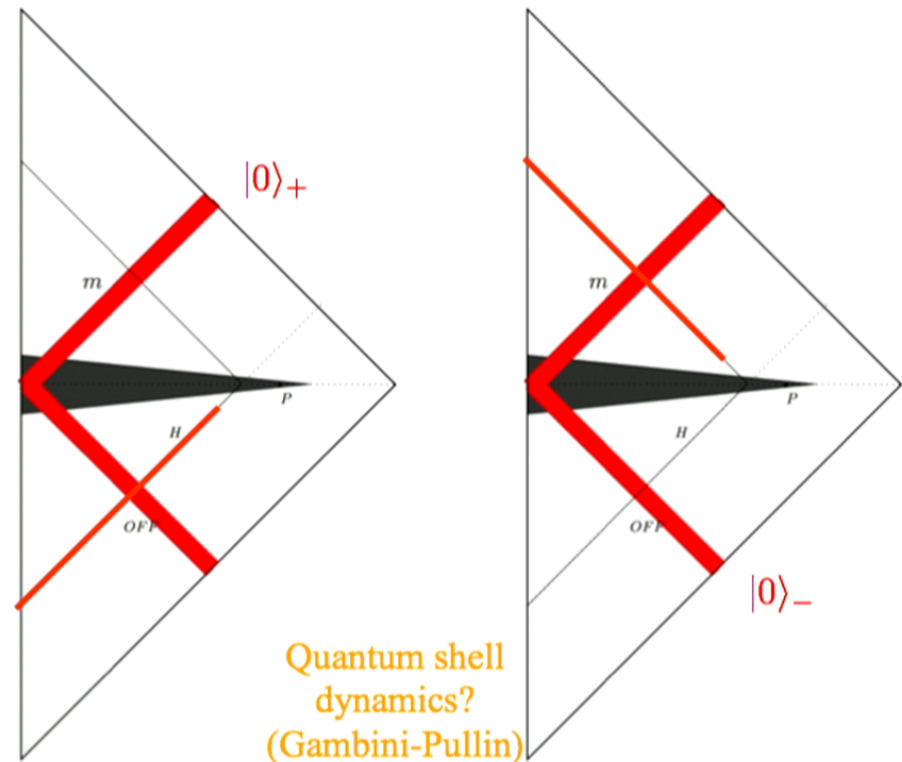
Expect modifications of the bounce scenario from back reaction

(18)



If one demands the state at \mathcal{S}^+ to be the vacuum then there is a firewall at the horizon (states with definite number of particles at \mathcal{S}^+ are not Hadamard states).

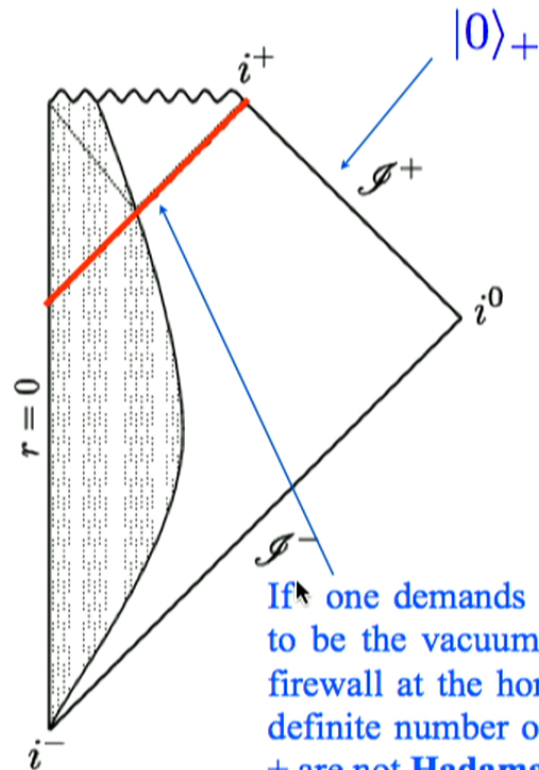
Quantum effects break time symmetry of the Haggard-Rovelli's **Fireworks** framework.



Quantum shell dynamics?
(Gambini-Pullin)

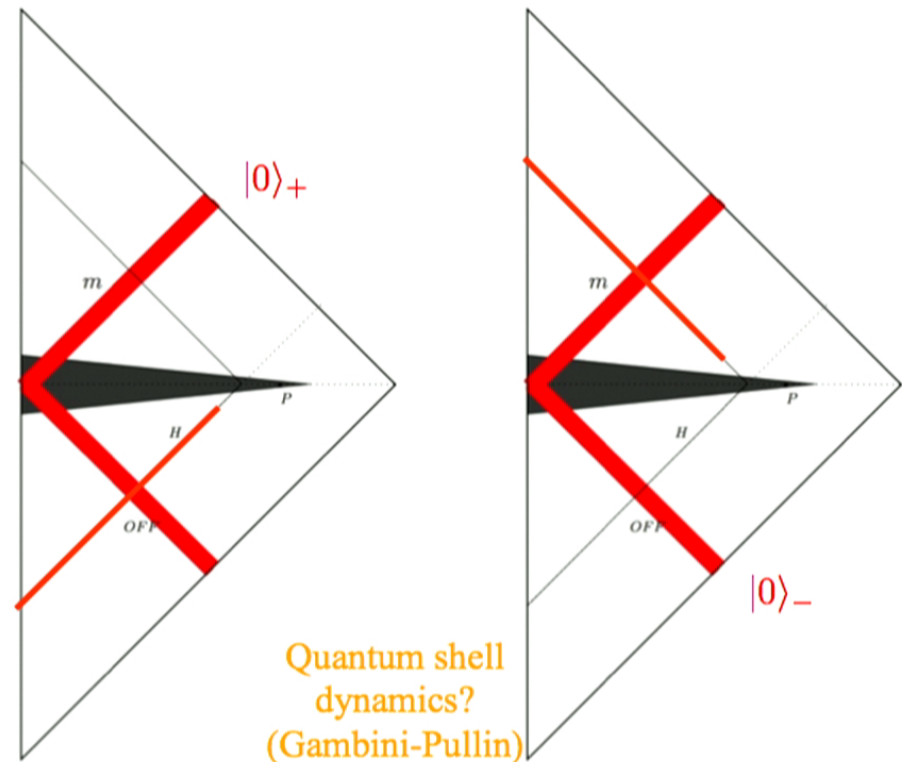
Expect modifications of the bounce scenario from back reaction

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If one demands the state at \mathcal{I}^+ to be the vacuum then there is a firewall at the horizon (states with definite number of particles at \mathcal{I}^+ are not Hadamard states).

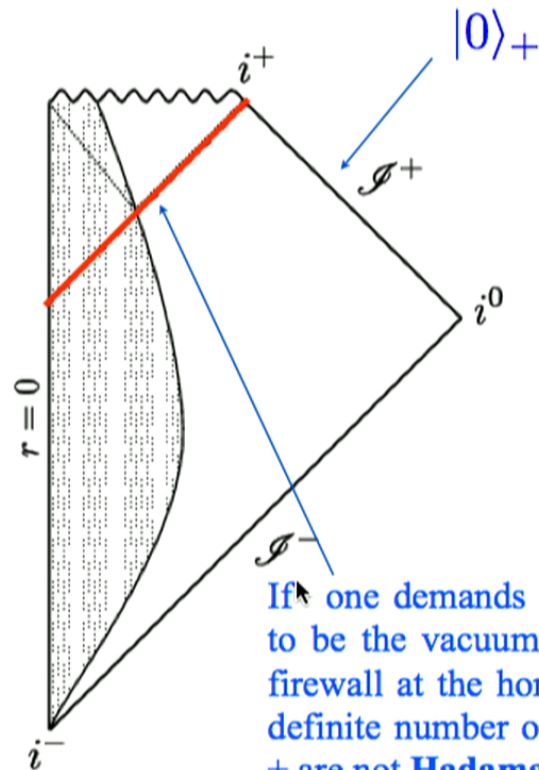
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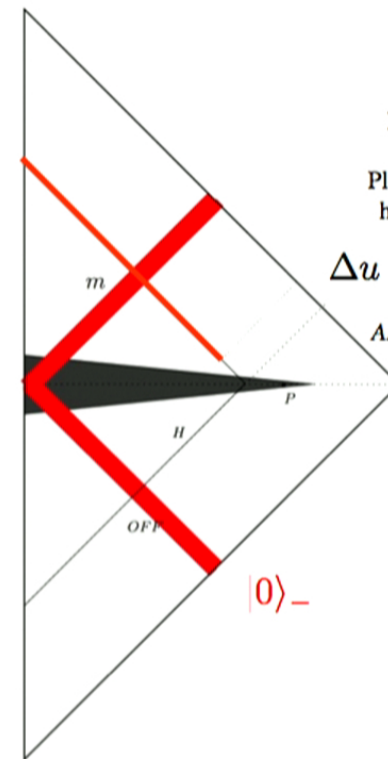
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Quantum effects break time symmetry of the Haggard-Rovelli's **Fireworks** framework.



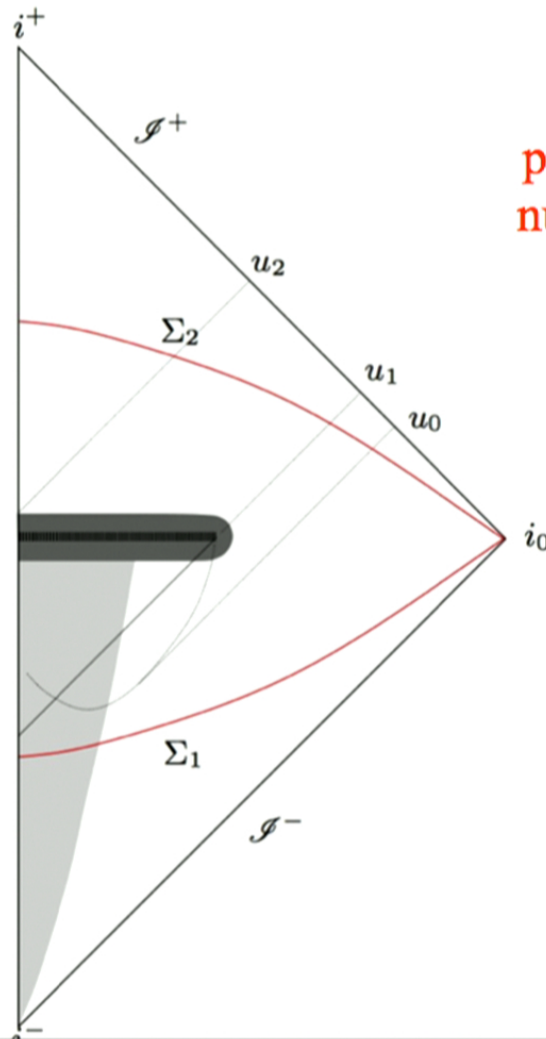
Energy momentum tensor becomes Planckian at the future horizon very quickly

$$\Delta u \approx M \log M/M_p$$

AP. and T. De Lorenzo

Revisiting the Ashtekar-Bojowald paradigm

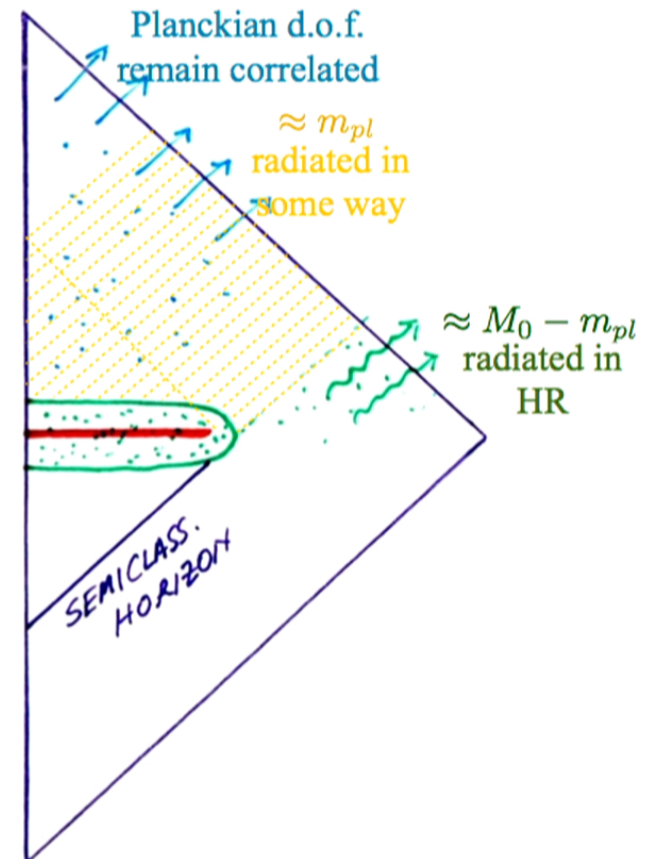
The story told from the perspective of observers at future null infinity is a **semiclassical one**



The Ashtekar-Bojowald paradigm: Uncorrelated Hawking radiation

The constraint that a small (Planckian) amount of mass is radiated while the naked *would-be-singularity* is visible suggests **the lack of unitarity** of the EQFT degrees of freedom ([arXiv:1409.0144](#) Bianchi-De Lorenzo-Smerlak).

Solution: EQFT unitarity is broken while fundamental quantum gravity unitarity holds. Information is retrieved in correlations of **Planckian quantum geometry degrees of freedom** (after *would-be-singularity* becomes visible) that are **entangled with radiation in Hawking era**.



Gravitational collapse is highly time asymmetric

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two ways of presenting the spacetime

The story told from the perspective of observers at future null infinity is a **semiclassical one**

The local version of the story must be told by **quantum gravity**

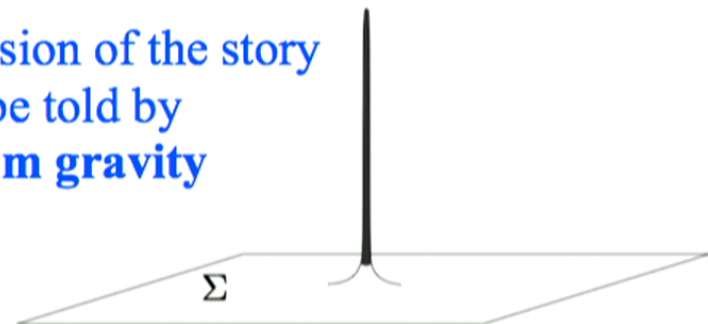
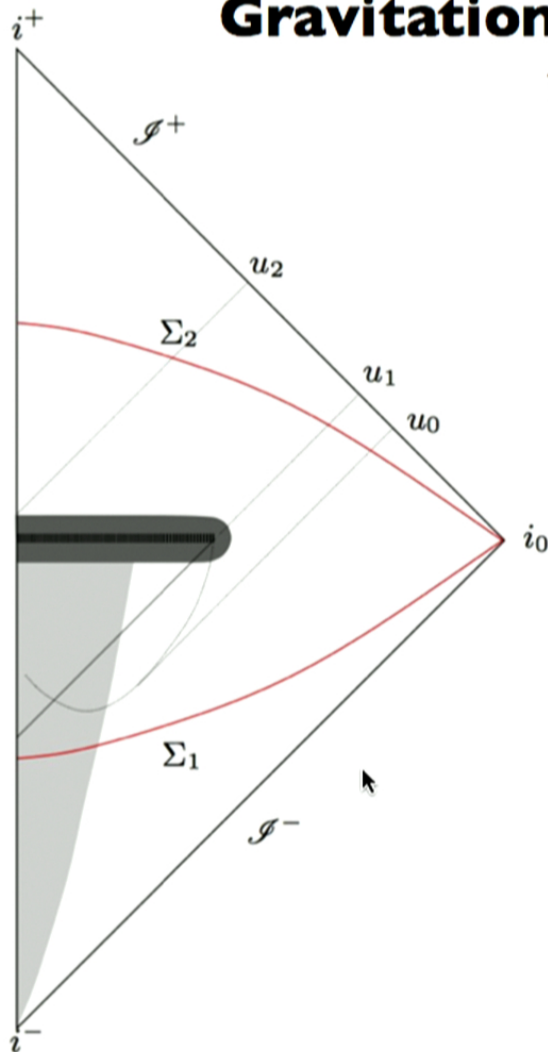
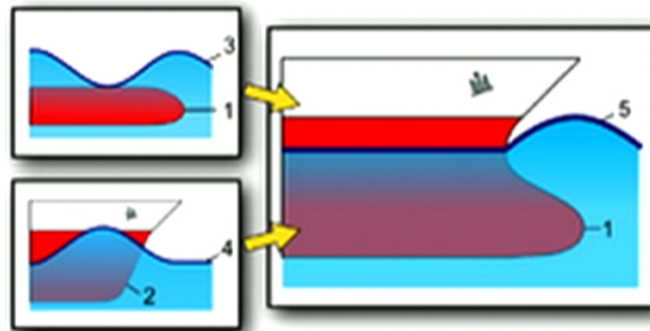
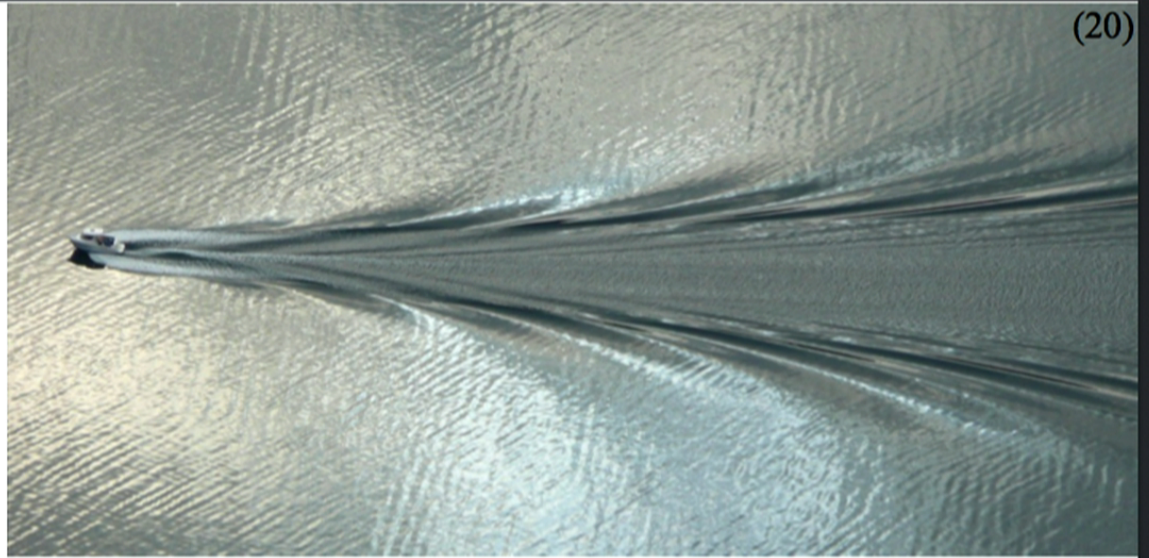


FIG. 8: A qualitative representation of the Riemannian geometry of Σ and Σ' of Fig 5. The shaded regions are those 'touching' the quantum region.



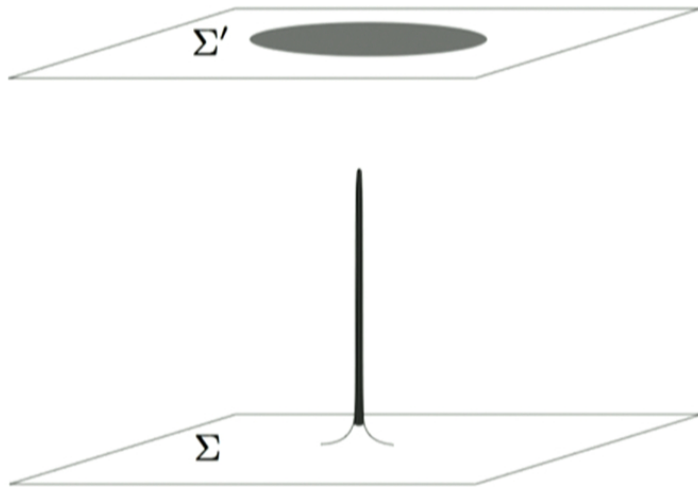
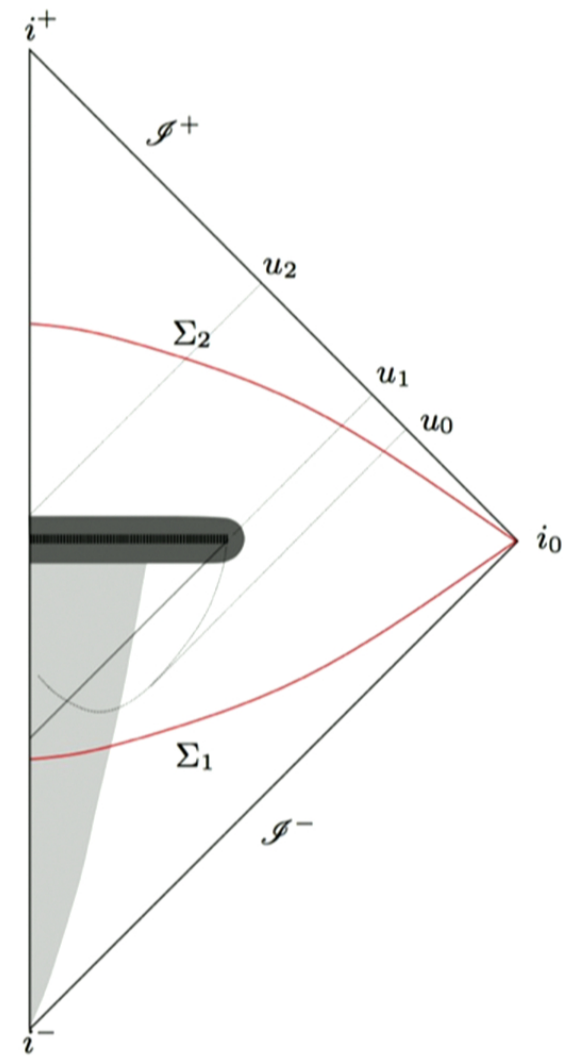


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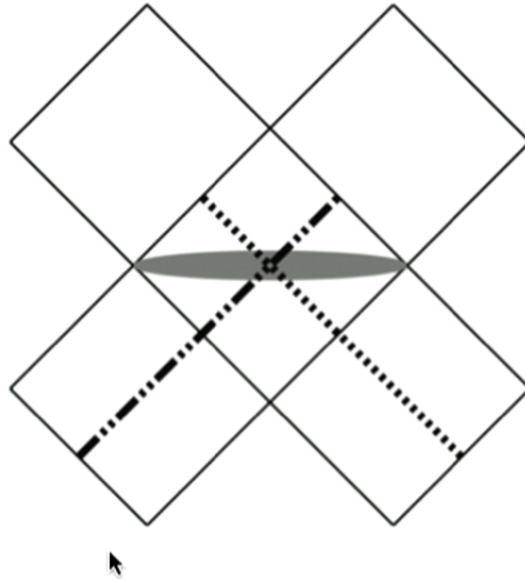
$$V(\Sigma) \propto M^3(M/\ell_p)^\alpha. \quad (3)$$

where the missing proportionality constant and α depend on the interior dynamics. For instance one gets $\alpha = 1/2$ if one (toy-)models the evaporation process with an advanced Vaidya metric. We can estimate the scaling of



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Quantum shells in a quantum space-time
 Rodolfo Gambini (Republica U., Montevideo), Jorge Pullin
 (Louisiana State U.). Aug 20, 2014. 5 pp.
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$$\langle T_{ab} u^a u^b \rangle \approx -\frac{\ell_p^2 M}{48r^5} \left[1 + \left(\frac{r}{u} \right)^4 \right]$$

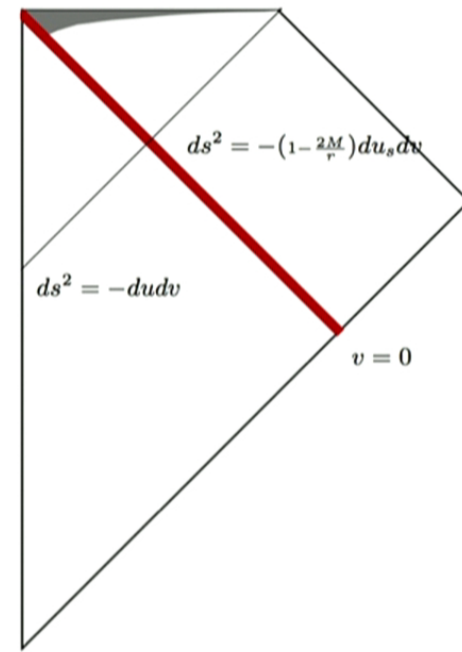


FIG. 6: 2d spherical black hole made from the gravitational collapse of a spherical pulse of energy M . The metric is flat inside the shell and Schwarzschild outside. Continuity of the metric across the shell implies the following relationship between retarded time $u = t - r$ and $u_s = t - r_*$ (for r_* the standard tortoise coordinate): $u_s = u - 4M \log(1 + \frac{u}{4M})$ and $v_s = v$. Coordinates are chosen so that the shell collapse takes place at $v = 0$. The expectation value of the energy momentum tensor in the Unruh vacuum is known in close form [65] everywhere in the spacetime. The shaded area denotes qualitatively the region where observers falling along ∂_r detect energy densities smaller than some negative fixed value.

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Where does information go?

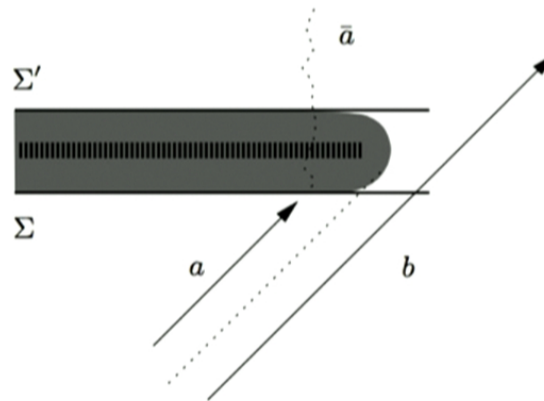
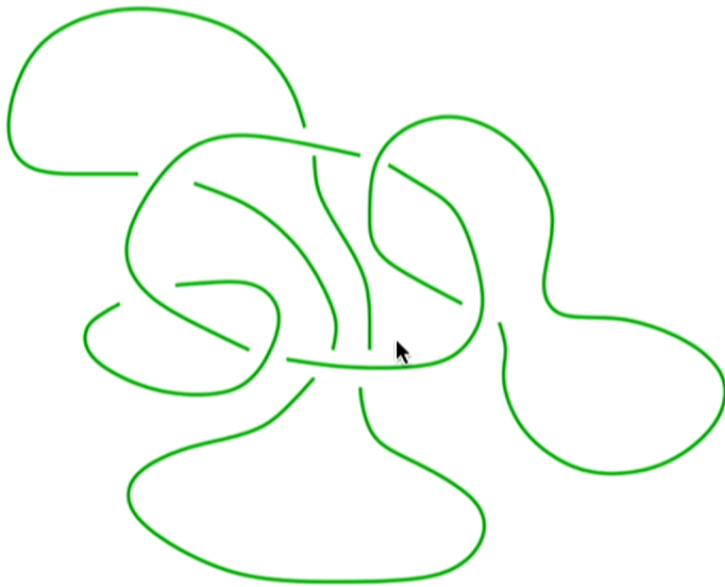


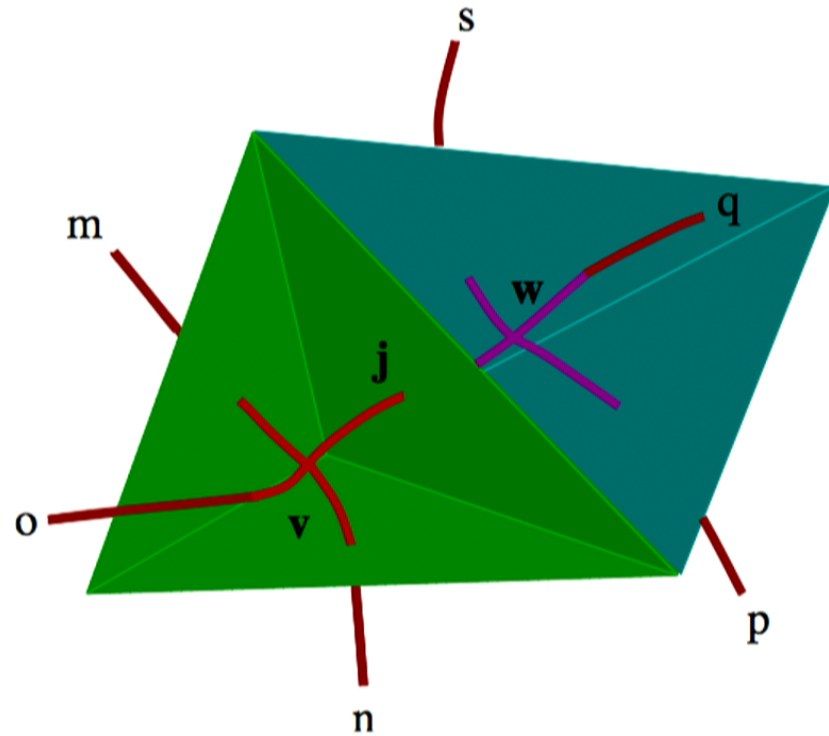
FIG. 5: Two instants of ‘time’ before and after the *would-be-singularity*. The spacial surface Σ is a latest surface where the space-time notion is still applicable. The surface Σ' is the earliest space-like surface in the flat emerging flat space-time across the *would-be-singularity*. The particles a and b are created close to the BH horizon. Particle b escapes to infinity as Hawking radiation. Particle a falls into the singularity, deposits its negative energy load, striped off its energy it emerges unitarily transformed into a defect \bar{a} in the quantum weave state describing flat space-time to the future of the *would-be-singularity*.

Candidates for information carriers

Degenerate geometries

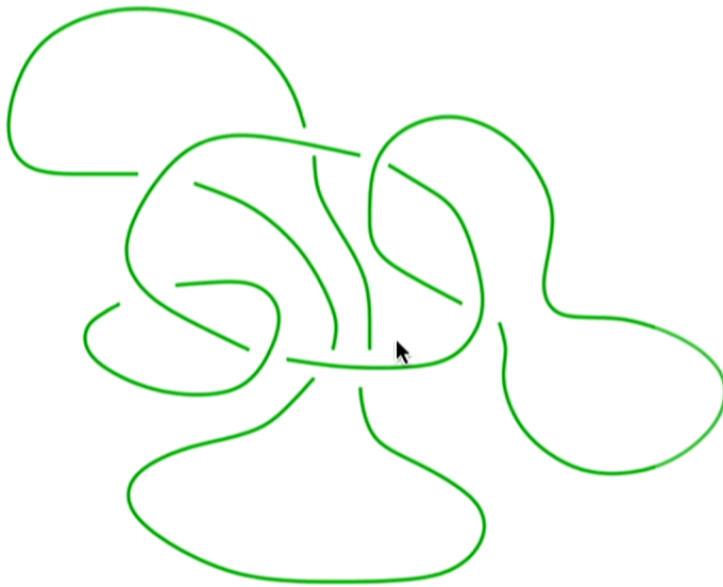


The volume q-bit

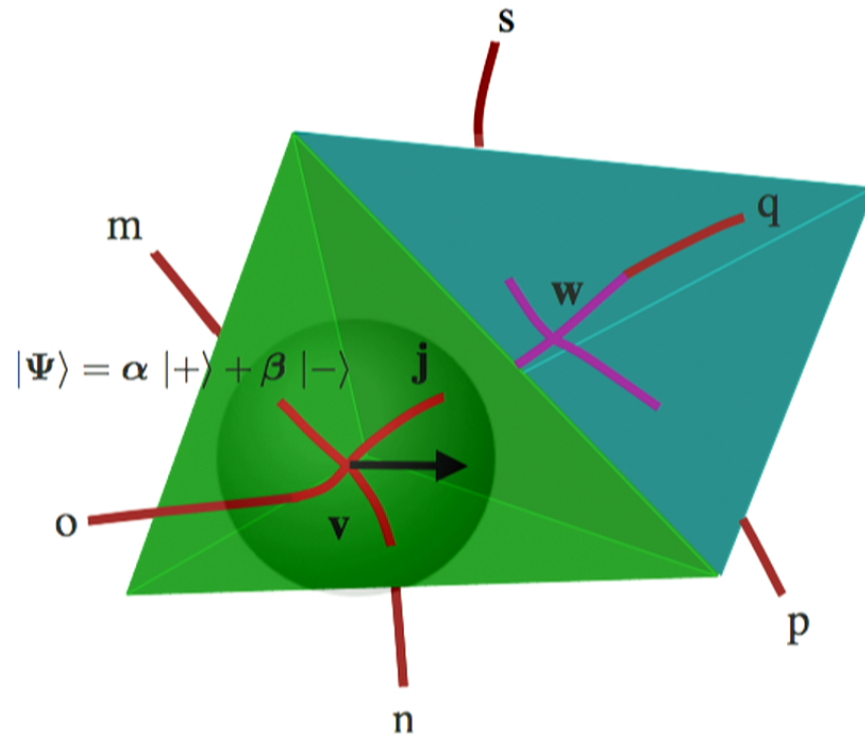


Candidates for information carriers

Degenerate geometries



The volume q-bit



Candidates for information carriers

Independent of quantization prescriptions

T. Thiemann J.Math.Phys. 39 (1998) 3347-3371

C. Rovelli, L. Smolin, Nucl.Phys. B442 (1995) 593-622, Nucl.Phys. B456 (1995) 753

[E. Bianchi](#), [P. Dona](#), [S. Speziale](#). Phys.Rev. D83 (2011) 044035

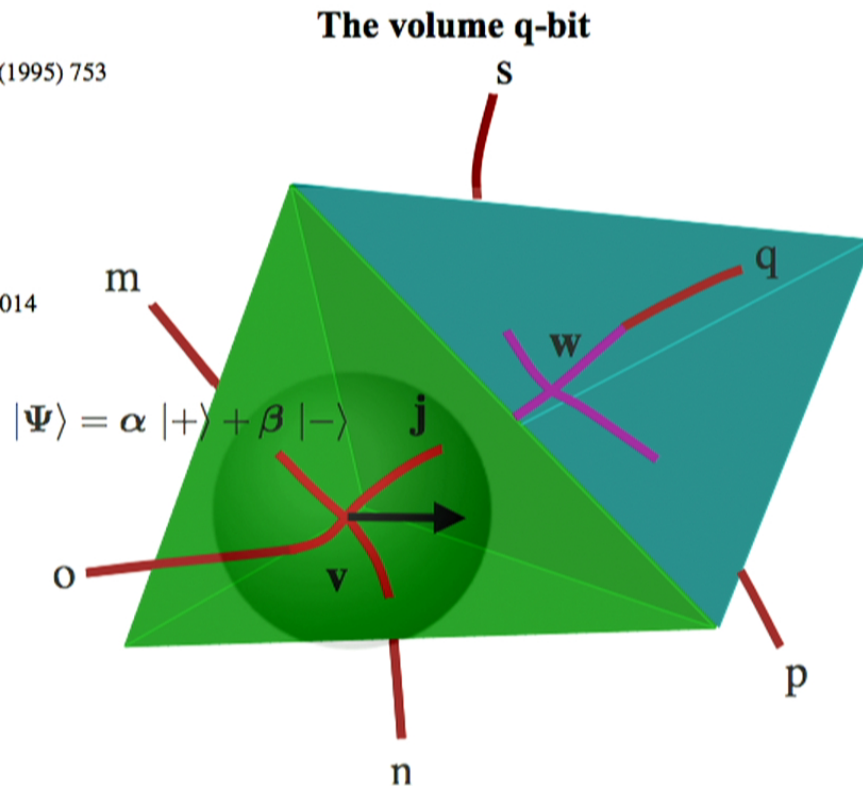
Fermions should interact with these q-bits

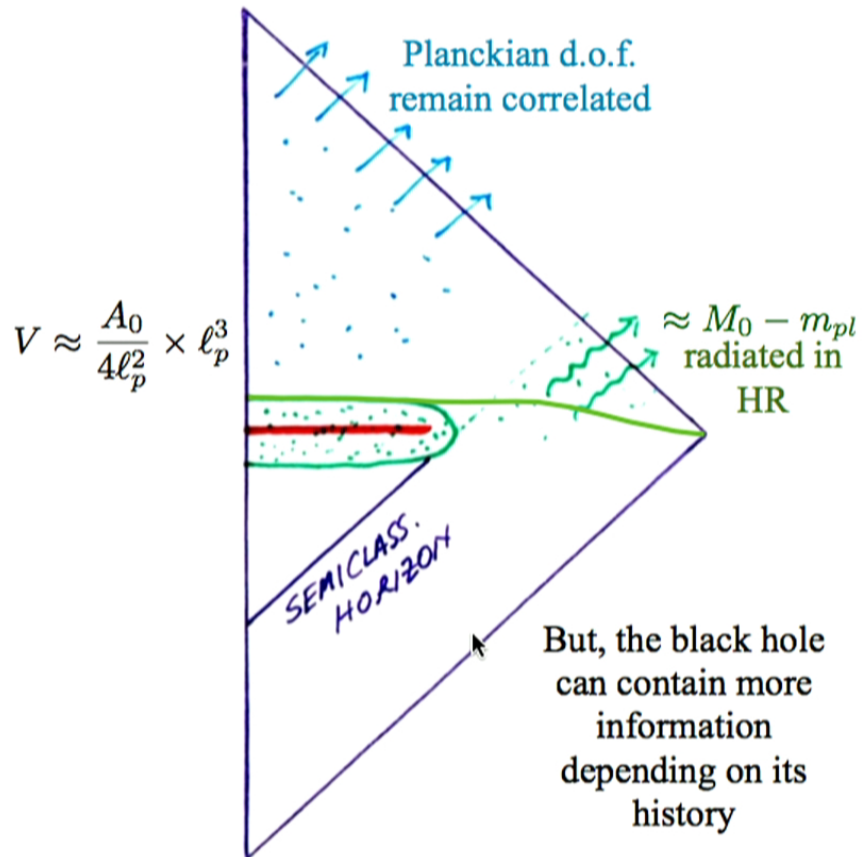
M. Christodoulou, A. Riello, C. Rovelli. Int.J.Mod.Phys. D21 (2012) 1242014

Work in progress in collaboration with [Speziale and De Lorenzo](#)

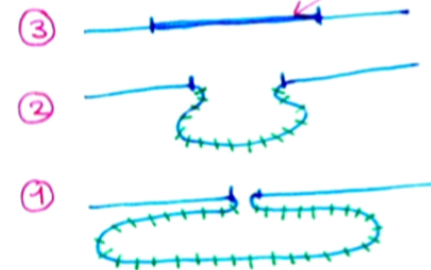
What of all this remains in physical states?

Lorentz invariance?





FLAT
MINKOWSKI
SLICE



VOLUME

$V = \left(\frac{M_0}{M_p}\right)^2 \ell_p^3$

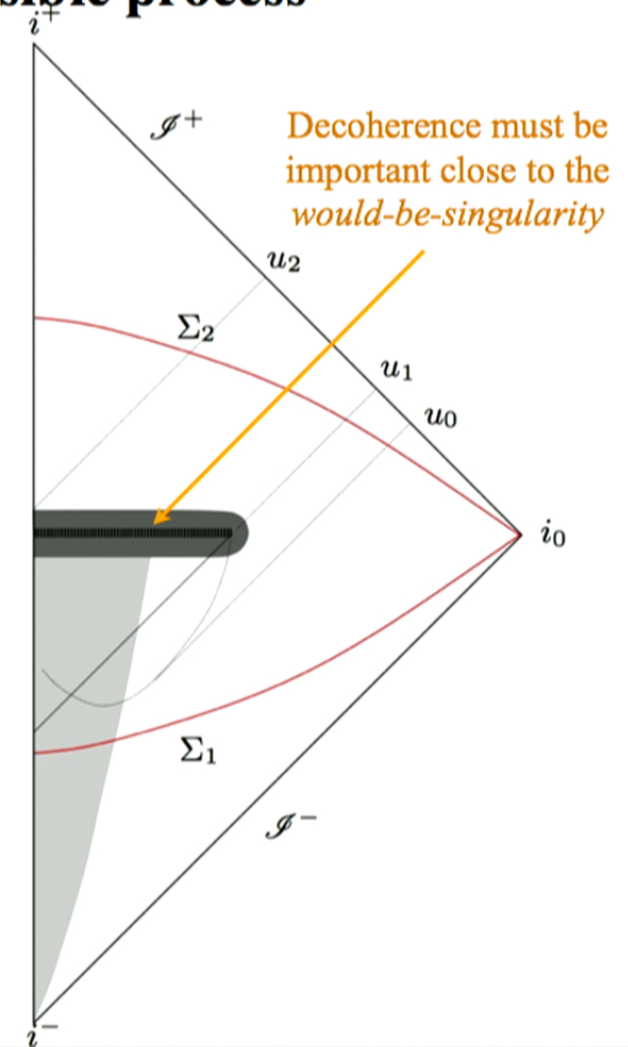
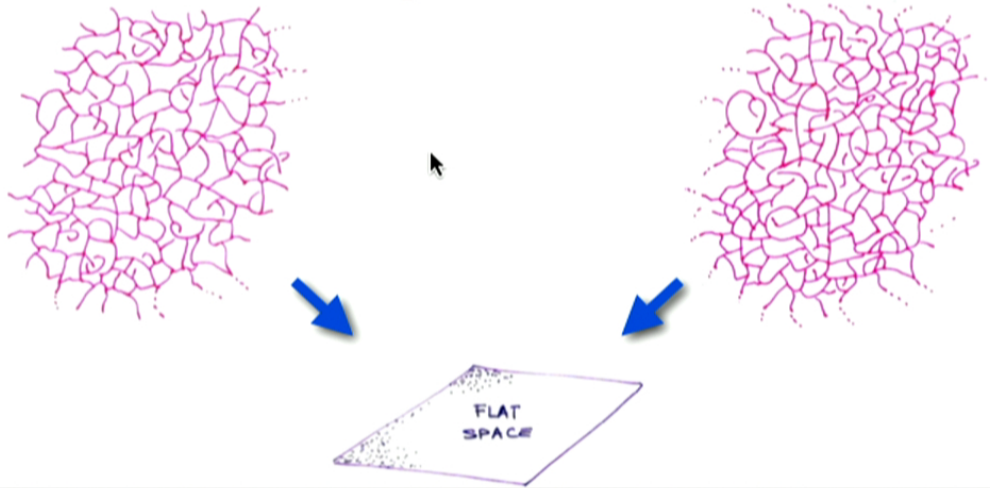
$$L = V^{1/3} \approx \left(\frac{M_0}{M_\odot}\right)^{2/3} \times 10^{-11} m$$

$$L_\odot \approx 10^{-11} m$$

$$L(10^{15} g) \approx 10^{-22} m \approx 10^{-2} \ell_{LHC}$$

Gravitational collapse is an irreversible process

- Gravitational collapse **spacetime is highly asymmetric**.
- **Firewalls:** Purification cannot take place during Hawking era.
- Purification via EQFT degrees of freedom after Hawking era on an effective non-singular background is not possible (Hayward scenario) (from results by Bianchi-De Lorenzo-Smerlak).
- **Natural possibility:** Purification via decoherence with Planckian quantum geometry structure.
- **Initial and final “flat” space-times are not the same.**



LQG IS NOT HOLOGRAPHIC

But what about all the holographic phenomenology? (e.g. the **Bousso bound**; a theorem by Bousso-Casini-Maldacena, Phys.Rev. D90 (2014) 4, 044002)

$$S_{\rho_0}(\rho) = -\text{Tr}[\rho \log \rho] + \text{Tr}[\rho_0 \log \rho_0].$$

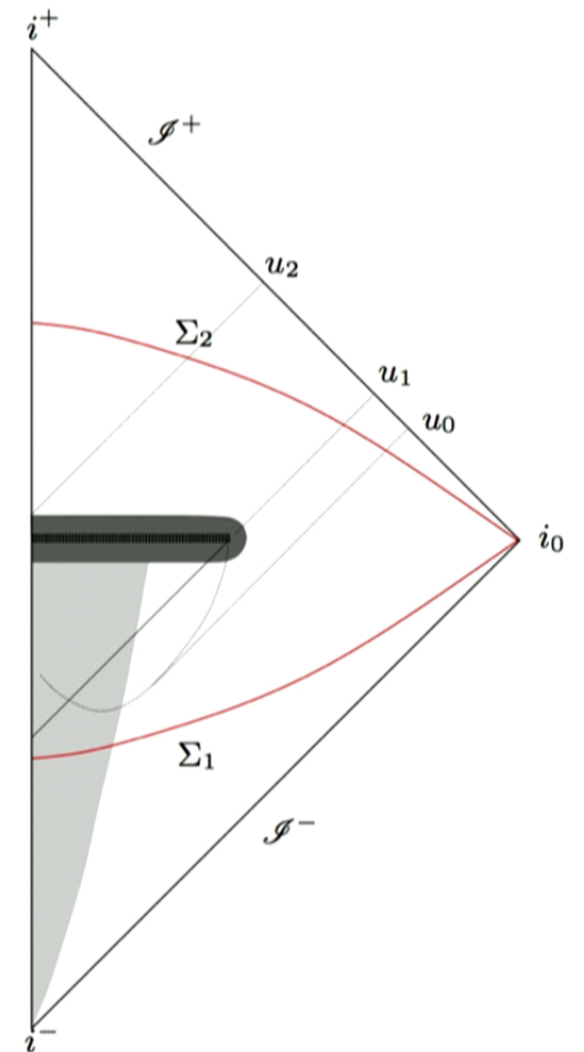
a fact about EQFT degrees of freedom that does not contradict a non-holographic fundamental framework.

Bianchi's computation of BH entropy changes (Semiclassics: Einsteins equations+QFT) [arXiv:1211.0522](https://arxiv.org/abs/1211.0522)

$$\delta S_{thermo} = \frac{\delta A}{4G_N \hbar}$$

versus the computation of BH entropy in LQG (microstructure of quantum geometry)

$$S_{stat} = \frac{A}{4G_N \hbar} + \eta \frac{\sqrt{A}}{\sqrt{\gamma G \hbar}}$$



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INFORMATION need not have WEIGHT

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From Unruh 2012 “Decoherence without dissipation”

Consider two particles, which for sake of simplicity I will assume have the same mass, and live in a 1+1 dimensional spacetime. They interact only when in contact with each other, and their interaction is mediated by some hidden degrees of freedom which are represented by a number N of spin 1/2 objects, with spins operators \vec{S}_i . The interaction Hamiltonian is assumed to be of the form $\delta(x_1 - x_2) \sum_i S_i^3$ where $S^3 = \frac{1}{2}\sigma^3$ the third Pauli spin matrix, while the Kinetic energy is the usual $\frac{1}{2m}(p_1^2 + p_2^2)$.

$$Y = (x_1 + x_2)/2 \quad (1)$$

$$y = (x_1 - x_2) \quad (2)$$

the Schroedinger equation becomes

$$i\partial_t \Psi(t, Y, y, \{s_i\}) = -\frac{1}{m}\partial_Y^2 \Psi - \frac{1}{2m}\partial_y^2 \Psi + \mu\delta(y)\left(\sum_i S_i^3\right)\Psi \quad (3)$$



From Unruh and Wald 95

$$H = \frac{1}{2} \int \{[\pi(t, x) - h(x)q]^2 + [\partial_x \phi(t, x)]^2\} dx + \frac{\omega}{2}(p^2 + q^2 - \frac{1}{2})[1 + \alpha(S_z + s)] + F(S_z),$$

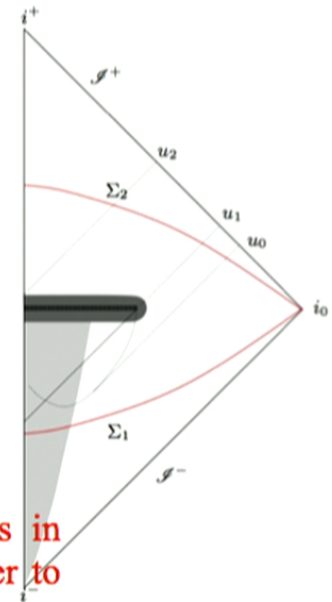
Conclusions

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- Quantum geometry is expected to be ‘atomistic’ in non perturbative QG
- Smooth spacetime arises from coarse graining.
- Discrete Planckian structure explains Hawking entropy.
- Purification via EQFT degrees of freedom does not work:
 1. During Hawking era due to the **firewall problem**.
 2. After Hawking era on an effective non-singular background due to **energy conservation**.
- **Natural possibility:** Purification via decoherence with Planckian quantum geometry structure (important close to the *would-be-singularity*).
- **Initial and final “flat” space-times are not the same:** EQFT scattering approach cannot describe the fundamental physics.
- The firewall argument is a problem for ADS-CFT type of scenarios not for ‘atomistic’ QG theories.
- In this scenario the Hawking evaporation process is analogous to standard irreversible processes (breaking a glass, burning a newspaper)

Outlook

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- Can one take into account non perturbative back reaction effects in spherical quantum gravity? (Gambini-Pullin theory with scalar matter to show 'time asymmetry' of *would-be-singularity*)
- Can one effectively describe the decoherence effect of EQFT? (quantum cosmology, structure formation effects, unitarity loss in QFT)



Thank you very much!

For further reading:
**“No firewalls in quantum gravity:
the role of discreteness of quantum
geometry in resolving the
information loss paradox”**
[arXiv:1410.7062](#)
to appear in CQG

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R. Penrose, J. Pullin, A. Riello, C.
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D. Sudarsky for discussions.