

Title: Optical frequency standards for gravitational wave detection

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Abstract: <p>Gravitational waves (GW) imprint apparent Doppler shifts on the frequency of photons propagating between an emitter and detector of light. This forms the basis of a method to detect mHz GW using Doppler velocimetry between pairs of satellites [1]. The crucial component in such GW detectors is the frequency standard on board the emitting and receiving satellites. I will discuss how recent developments in atomic clock technology have led to devices that could be sufficiently sensitive to probe astrophysically interesting sources. I will present a design for a robust, space-capable optical frequency standard [2], that is being developed at York.</p>

<p>References</p>

<p>[1] JW Armstrong, Living Rev. Relativity 9, (2006), 1 [2] AC Vutha, arXiv:1501.01733 (2015)</p>

# Optical frequency standards for gravitational wave detection

Amar Vutha  
York University  
Funding: Society in Science, ETH Zurich

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## Other work

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### New candidate molecules for electron EDM search experiments: HgBr, RaBr

*(collaboration: BP Das group, Indian Inst. of Astrophysics)*

*Mercury monohalides: suitability for electron EDM searches*  
*arXiv: 1410.1438*

### Measurement of 2S-2P Lamb shift in hydrogen to shed light on proton radius puzzle

Developed a new method (variant of Ramsey scheme) to measure Lamb shift with high precision

Data-taking in progress, systematic effects being studied

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# Clocks

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Clock = Oscillator + Frequency reference + Counter

Quartz watch = Electric circuit + Quartz crystal + Electric counter

Audio "clock" = Cello + Tuning fork + Electric counter

Optical clock = Laser + Atoms + Optical counter  
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# What can you do with a good clock ?

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Precise measurements

Accuracy of directly measuring

length  $10^{-9}$

temperature  $10^{-6}$

mass  $10^{-8}$

frequency  $10^{-17}$

Ranging + Navigation

*distance = time x speed of light*

Communication

*accurate frequency synthesis*

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# Performance of a frequency standard

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Precision:  $\frac{\delta f}{f} \sim \frac{1}{f_0 \sqrt{NT\tau}}$  FUNDAMENTAL LIMIT

oscillation frequency

SNR factor  
=  $\sqrt{N}$ (atoms)

coherence time

averaging time

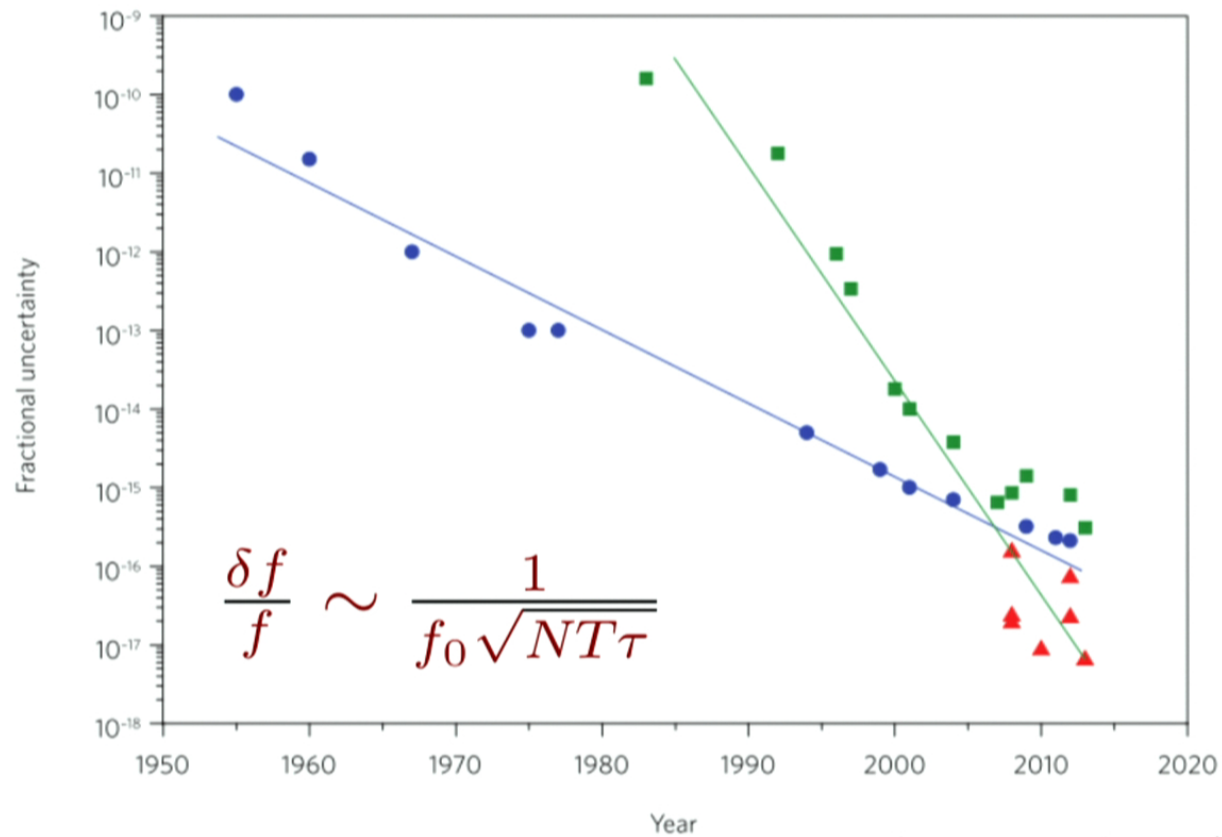
Accuracy: *determined by design*

Example: similar performance achieved with

*optical lattice clocks* ....  $N \sim 10^4$

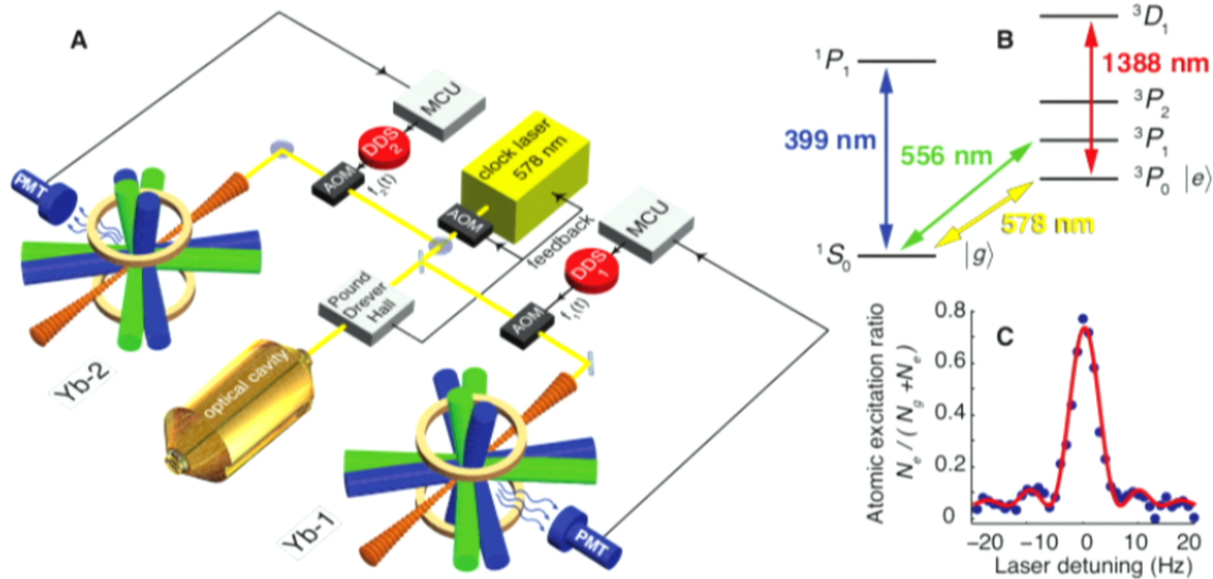
*ion clocks* ....  $N=1$

# State of the art



Margolis, *Nature Physics* (2014)

# State of the art



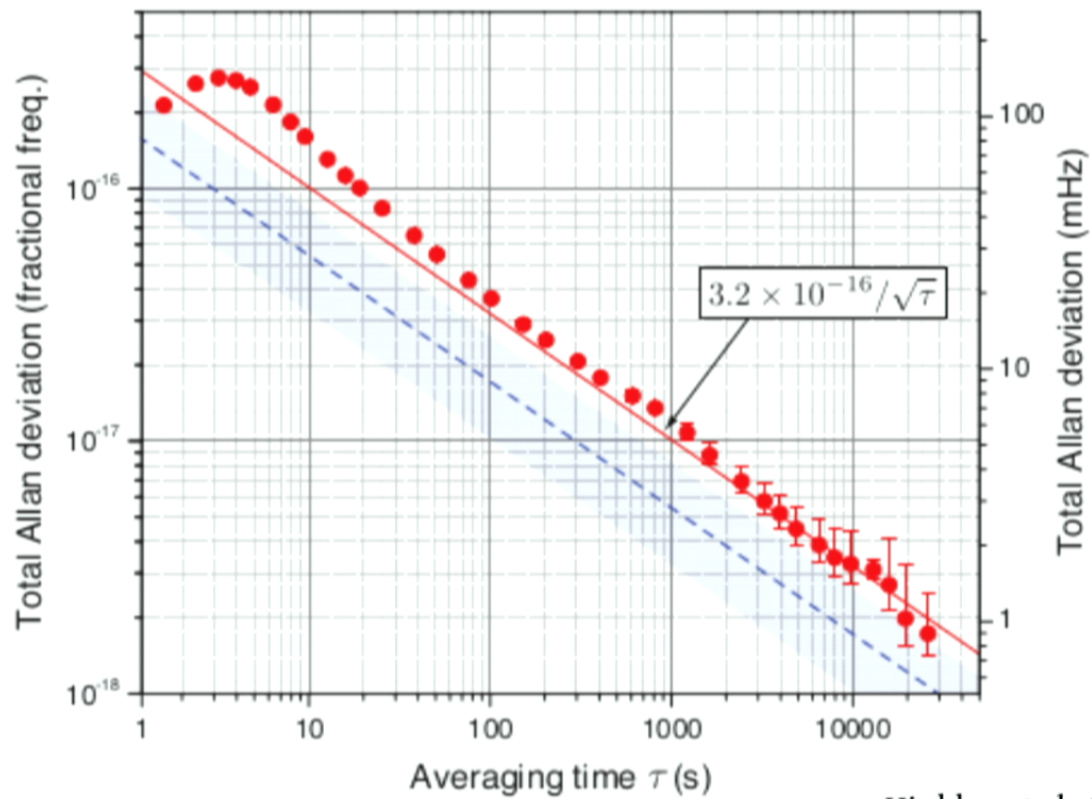
Hinkley *et al.*, Science (2013)

$$\frac{\delta f}{f} \sim \frac{1}{f_0 \sqrt{NT\tau}}$$

$N \sim 10^4$  atoms

$T = 500$  ms

# State of the art: optical lattice clocks



Hinkley *et al.*, Science (2013)



# Gravity & clocks

---

Waterloo: 330 m + m.s.l.



$$\frac{\Delta\nu}{\nu} \simeq 10^{-14} \quad (1000x \text{ sensitivity of optical clocks})$$

Toronto: 210 m + m.s.l.

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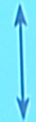
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Calibration of GR shift is the main limitation to optical clock comparisons across long baselines

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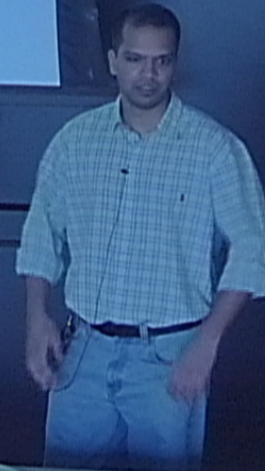
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## GW effect on an emitter-receiver pair

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$$ds^2 = dt^2 - (dz^2 + dx^2 + dy^2) - h_+[k(z-t)](dx^2 - dy^2) - 2h_\times[k(z-t)]dxdy$$

Conserved momenta are  $p_z + p_t, p_x, p_y$

Photon momentum is a null vector  $p \cdot p = 0$

$$p = \left[ \frac{\gamma}{2}(1 + \delta); \alpha, \beta, \frac{\gamma}{2}(1 - \delta) \right]$$

$$\alpha = p_0 \sin \theta \cos \phi$$

$$\beta = p_0 \sin \theta \sin \phi$$

$$\gamma = p_0 \cos \theta$$

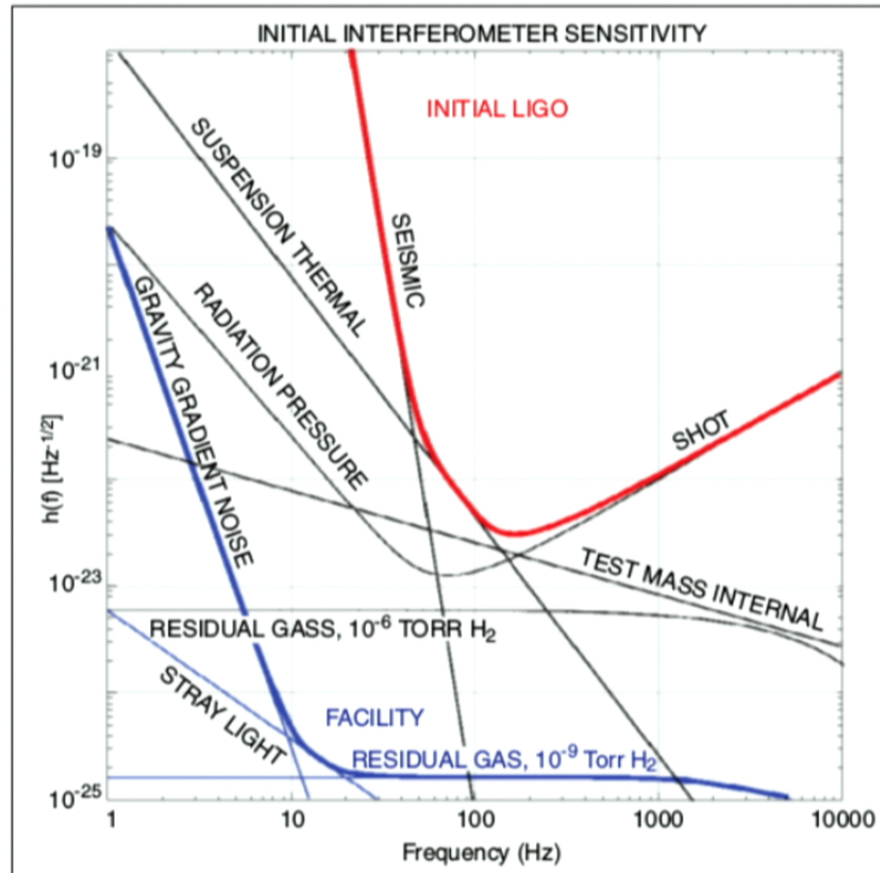
$$\delta(z, t) = \frac{\alpha^2 + \beta^2 + (\alpha^2 - \beta^2)h_+ + 2\alpha\beta h_\times}{\gamma^2}$$

$$= \tan^2 \theta (1 + \cos 2\phi h_+ + \sin 2\phi h_\times)$$

$$\frac{\nu_e}{\nu_r} = \frac{1 + \delta_e}{1 + \delta_d} \approx 1 + \sin^2 \theta (\cos 2\phi h_+ + \sin 2\phi h_\times)$$

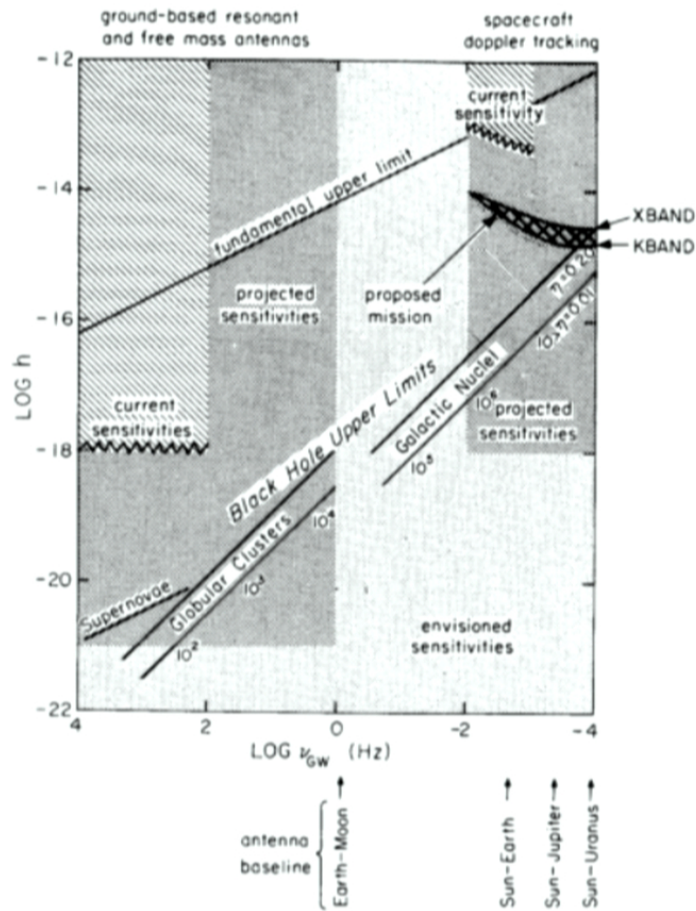
GW amplitude shows up in frequency differences

# Terrestrial interferometers



*Flanagan & Hughes,  
New J. Phys. (2005)*

# GW detection in the $\mu\text{Hz}$ - $\text{mHz}$ band

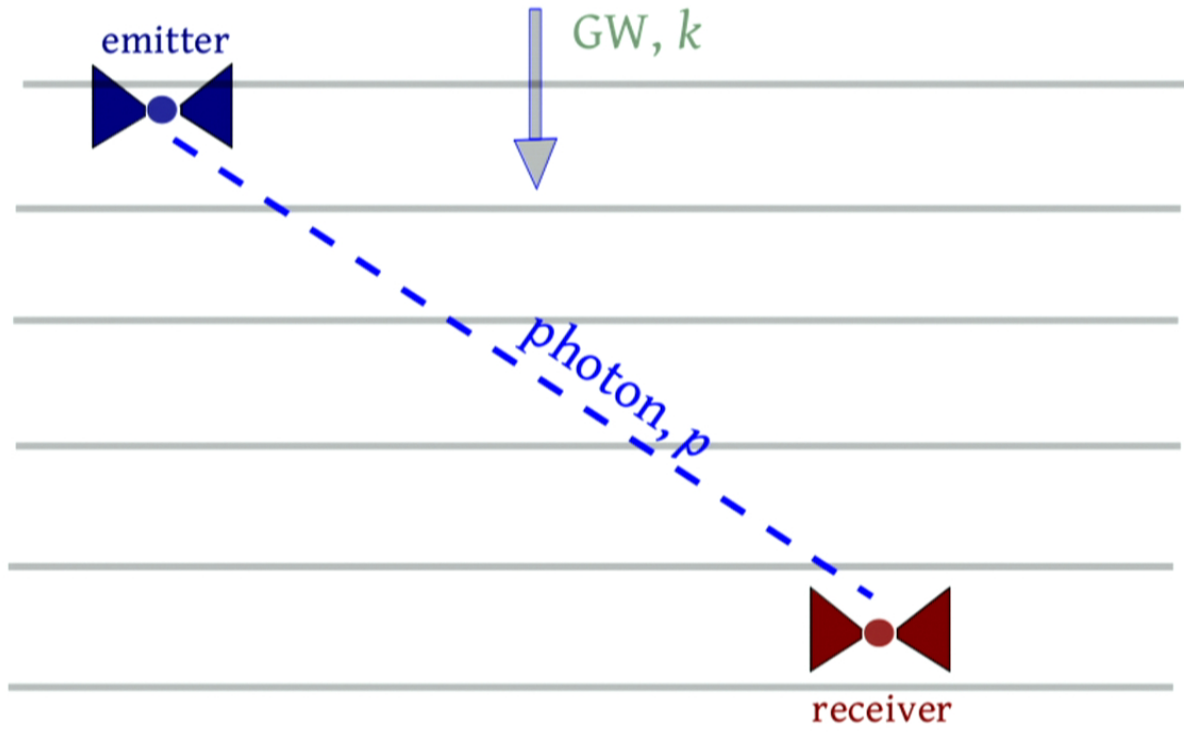


*Gravitational waves can be detected by precise Doppler measurements*

Kaufman (1970),  
 Estabrook & Wahlquist (1975),  
 Smarr *et al.* (1983)

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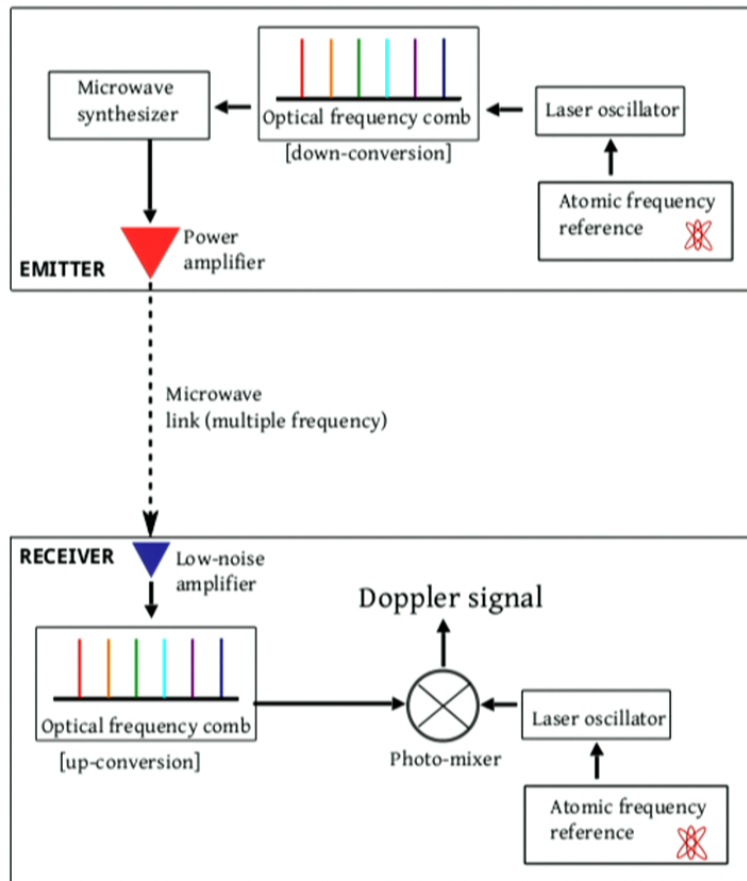
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# Frequency comparison scheme



Absolute distance locking is not necessary

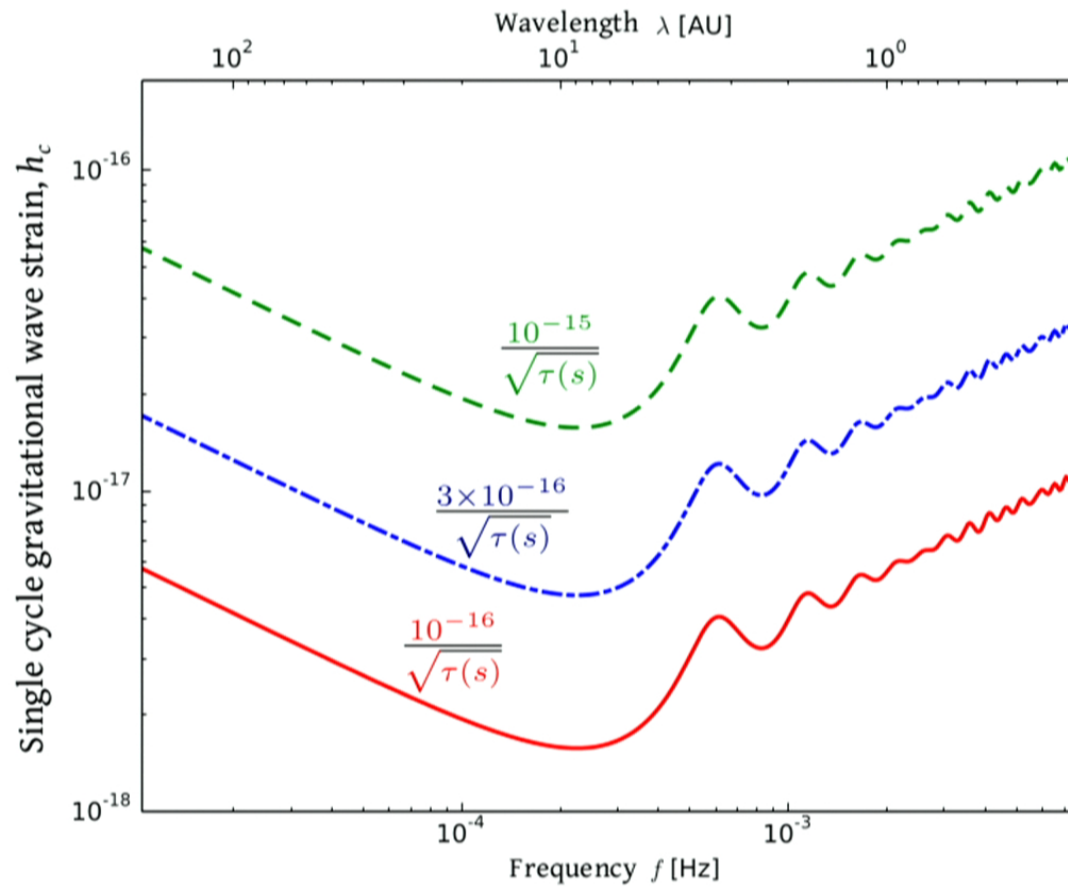
Multiple-frequency microwave link to suppress refractive index fluctuations

Possibly direct optical links in future

Compact frequency combs have been demonstrated

*Papp et al., arXiv:1309.3525*

# GW sensitivity of optical frequency standards

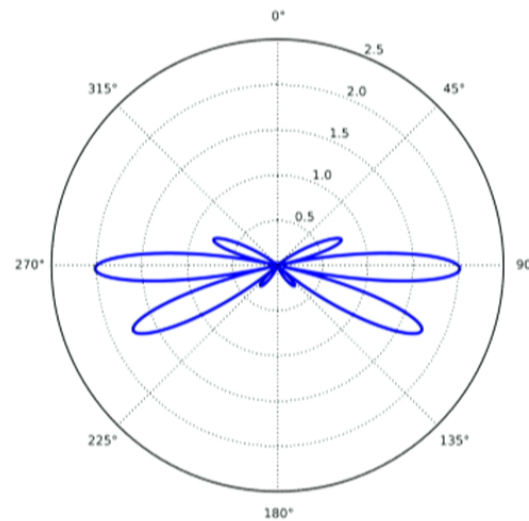
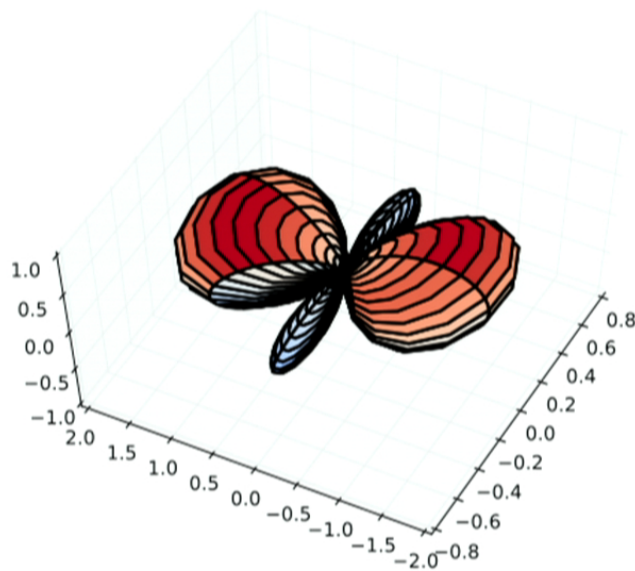


# Clock arrays

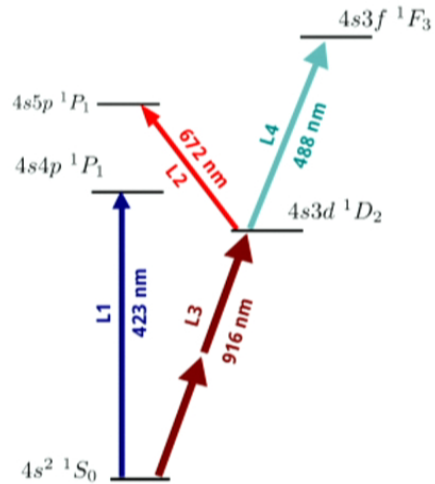
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GW amplitude is linear in fractional frequency shift

Combined signals from different emitter-detector pairs can be used to improve directional sensitivity



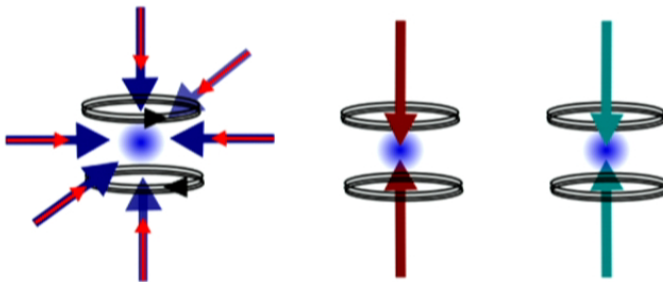
# Calcium 2-photon optical clock



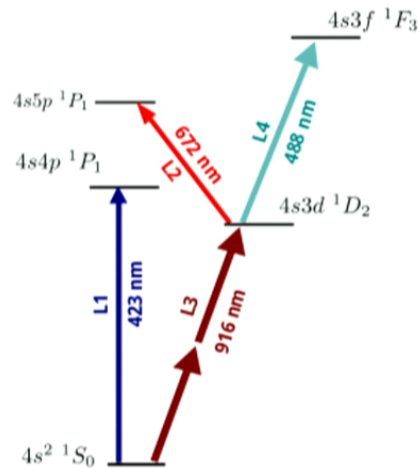
2-photon clock transition is  
Doppler- and recoil-free

Doesn't need optical lattice  
=> simpler architecture

Good prospects for portability  
and maintenance-free operation

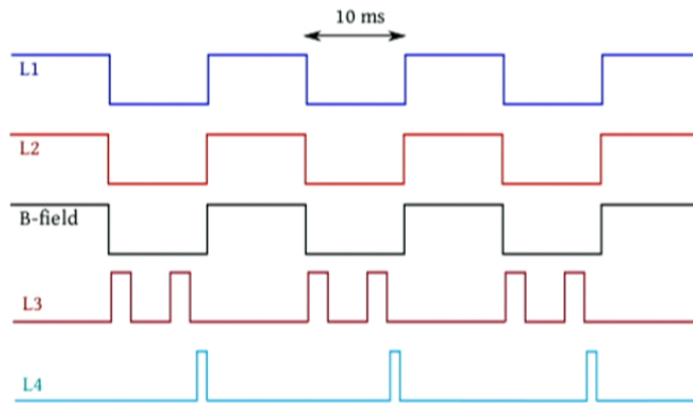


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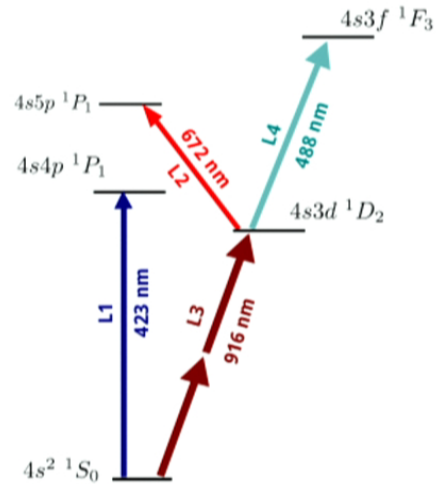
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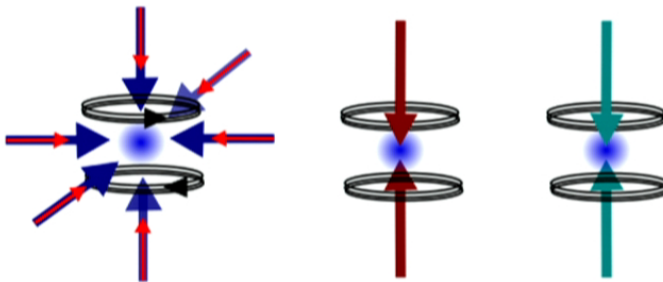
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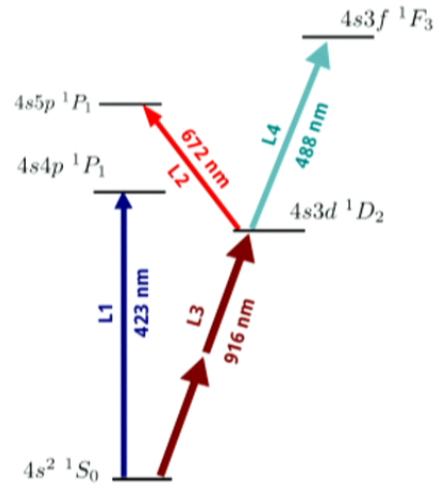
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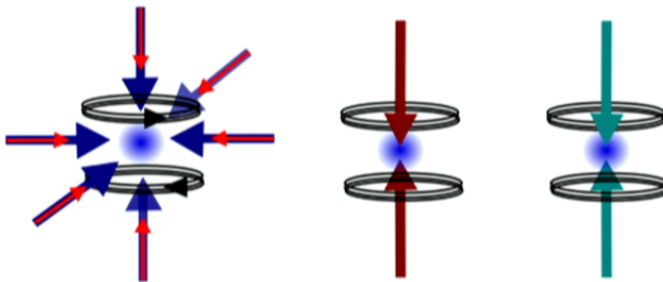
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## Where next

Continuous clocks ?

$$\frac{\delta f}{f} \sim \frac{1}{f_0 \sqrt{N \tau^2}}$$

*Faster averaging, better performance*

