Title: Cosmology in Massive GravityLand

Date: Feb 10, 2015 11:00 AM

URL: http://pirsa.org/15020088

Abstract: The last years have seen a renewed interest in theories of massive gravity. They represent an infra-red modification of gravity where the gravitational force weakens at very large scales. Heuristically, they provide the playground to understand a possible modification of GR which could potentially provide a dynamical solution to the cosmological constant problem. In this talk I will discuss a number of theoretical aspects of massive gravity theories, focusing on the relevance of the so-called Vainstein mechanism, both at the classical and the quantum level. I will also discuss how we can use cosmology from the early and late universe to constrain these theories. For example, what does the Cosmic Microwave Background Radiation know about the graviton mass?

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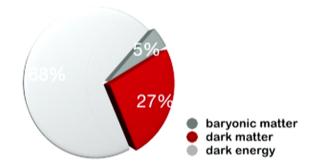
"The data is king. If what you're working on has nothing to do with data, it's not worth working on."

David Lyth

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∧CDM —a phenomenological model

- ACDM seems a good fit to theoretical data
- but we don't really understand Λ!
- there's been much effort in developing infra-red modifications of gravity as a means to explain Λ



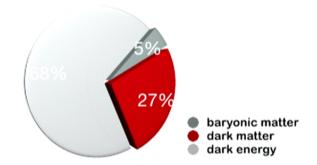
if the precision era has taught us anything, is that the theory needs to press on more boldly to catch up with observational precision.

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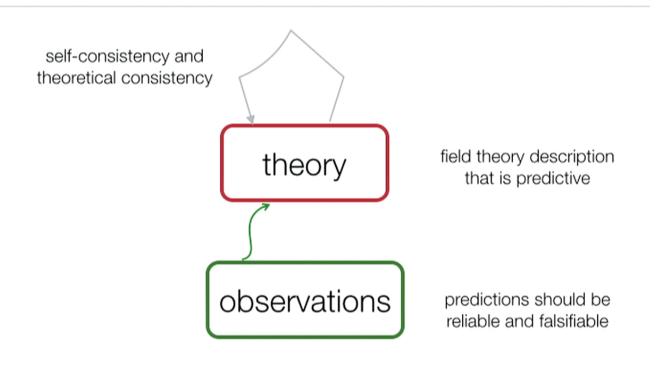


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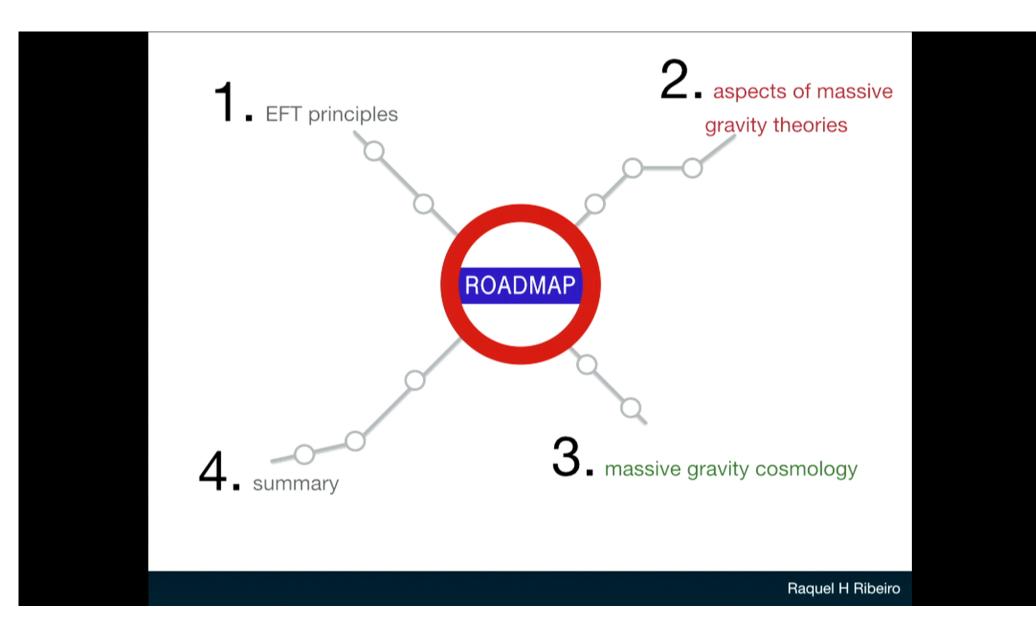
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gravity and cosmology-many unknowns



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traditional principles of EFTs

write a tower of interactions which are categorised by power counting

$$\mathcal{L}_{tEFT}(\phi) = \int d^4x \, \left\{ \mathcal{L}_{low-energy} + \sum_i c_i \frac{\mathscr{O}_{\beta}(\phi)}{\Lambda^{\beta}} \Lambda^4 \right\}$$
strong coupling scale

- interactions in O cannot be made large without the EFT running out of control
- we say these operators are irrelevant and unimportant
- they can be protected against large quantum effects if there exists a symmetry

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new way of looking at EFTs: redressing effect

- ▶ EFTs like massive gravity rely large derivative/kinetic interactions
- Examples of scalar theories:
 - ▶ P(X) theories, where $X=-(\partial \phi)^2/\Lambda^4 \rightarrow P(X) \supseteq DBI$, power-law models ~ $\Lambda^4 X^n$
 - the cubic galileon $S = \int d^4x \left\{ -\frac{1}{2} (\partial \phi)^2 \frac{1}{\Lambda^3} \Box \phi (\partial \phi)^2 \right\}$
- Our interest is in theories which can exhibit a Vainshtein/kinetic mechanism.
 This means large interactions.

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why are these theories special? Defayet et al. hep-th/0106001 Nicolis & Rattazzi hep-th/0404159

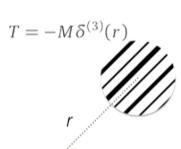
case study: cubic galileon coupled to spherically distributed matter:

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For large background sources and small enough distances:

$$F_{\phi}(r) \sim \phi'(r) \sim \sqrt{\frac{M\Lambda^3}{M_{\rm Pl}r}} \longrightarrow \Box \phi \gg \Lambda^3$$

$$r_{\star} \equiv rac{1}{\Lambda} \left(rac{M}{4\pi M_{
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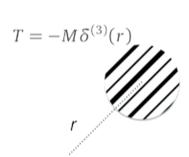
Vainshtein radius

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Vainshtein radius

Split the field into background+perturbations, & canonically normalise

$$\mathcal{L} \supseteq -\frac{1}{2} (\partial \delta \hat{\phi})^2 - \frac{1}{Z^{3/2} \Lambda^3} \Box (\delta \hat{\phi}) (\partial \delta \hat{\phi})^2 + \cdots$$
with $Z \sim 1 + \frac{\Box \phi}{\Lambda^3} \gg 1$

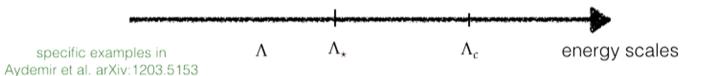
redressed strong coupling scale

$$S = \int d^4x \left\{ -\frac{1}{2} (\partial \phi)^2 - \frac{1}{\Lambda^3} \Box \phi (\partial \phi)^2 + \frac{\phi}{M_{\rm Pl}} T \right\}$$

 \triangleright if interactions are large, $\Box \phi \gg \Lambda^3$ then the strong coupling scale is redressed

$$\Lambda_\star = \sqrt{Z} \Lambda \gg \Lambda$$
 environmentally dependent

perturbative unitarity does not break at Λ, and we can trust the EFT description beyond that scale

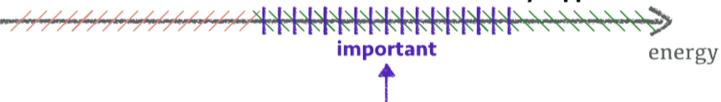


EFTs for large derivative interactions

These EFTs are perfectly well-defined around $E \sim \Lambda$.

$$\begin{array}{c|c} \textbf{relevant} & \textbf{irrelevant} \\ \\ \mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{low-energy}} + \sum \frac{f_{\alpha}(\partial\,\phi\,,\partial^{\,2}\phi\,)}{\Lambda^{\alpha}}\; \Lambda^{4} + \sum \frac{\mathscr{O}_{\beta}}{\Lambda^{\beta}}\; \Lambda^{4} \end{array}$$

truly suppressed at Λ



reorganised derivative hierarchy

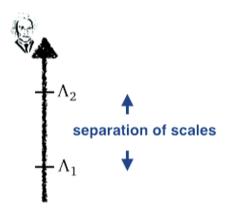
Within the EFT unifying framework, there is no distinction between classical or quantum mechanical origin of the operators.

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organised EFTs: traditional and novel

traditional EFTs

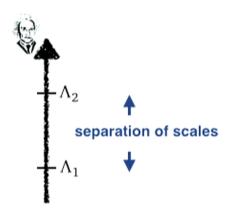


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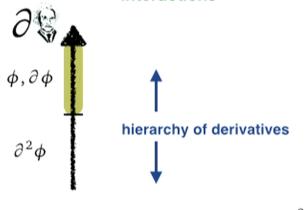
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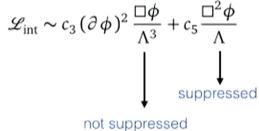
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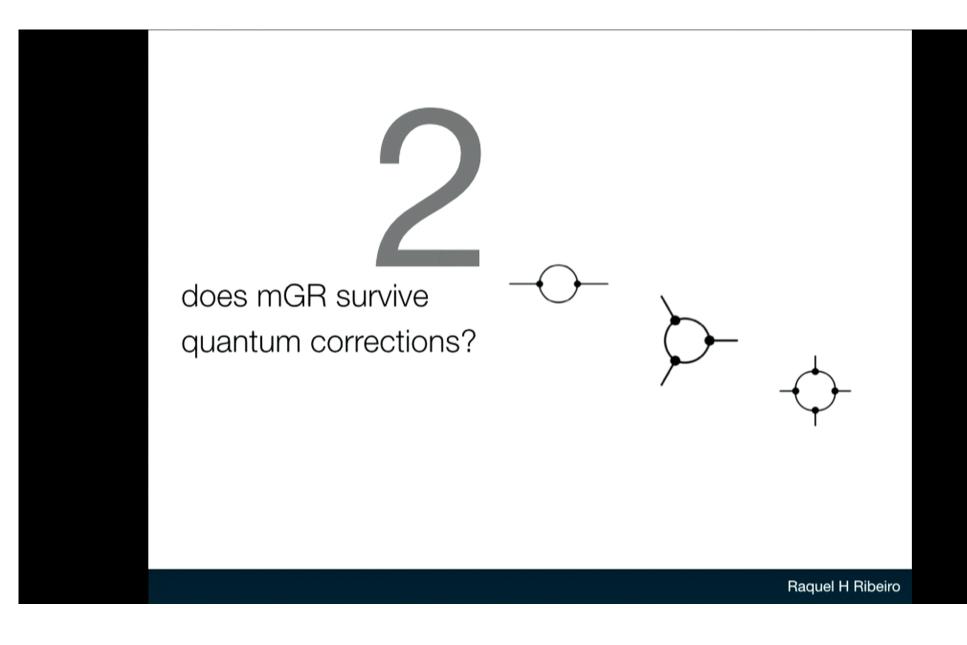
example: galileon-type interactions



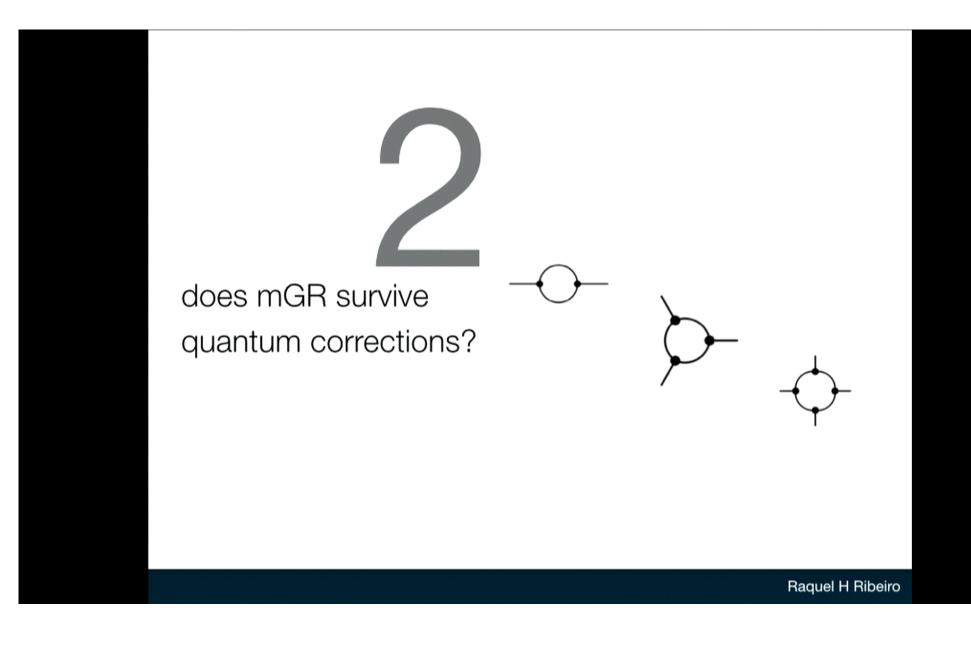


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why are quantum corrections relevant?

This is a spectacular problem!



credit: open university, hacked by RHR

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quantum corrections can ruin the EFT

- technically unnatural: if they change the coefficients of the existing operators
- ▶ if they generate relevant & important operators, destabilising the potential

Pick up a theory. We can determine its regime of validity at one-loop by requiring

$$|\mathcal{L}_{\text{classical}}| \gg |\mathcal{L}_{\text{one-loop}}|$$

The EFT is built out of classical and quantum operators.

how to compute quantum corrections?

For simplicity, consider a scalar theory and compute the one-loop effective action.

- 1. Split the field into a background piece and perturbations $\phi = \phi_0 + \delta \phi$
- 2. Compute the quadratic action for fluctuations

$$\delta S = -\frac{1}{2} \int d^4 x \left\{ Z^{\mu\nu} [\phi_0] \, \partial_\mu \delta \phi \, \, \partial_\nu \delta \phi \right\}$$

3. Covariantise this.

$$\Gamma_{\text{1-loop}} = \frac{1}{2} \log \det \left\{ Z^{\mu \nu} [\phi_0] \nabla_{\mu} \nabla_{\nu} \right\} \qquad \qquad Z^{\mu \nu} = \sqrt{g_{\text{eff}}} \ g_{\text{eff}}^{\mu \nu}$$

the one-loop effective action

UV-divergences are organised as a Seeley - DeWitt expansion

Barvinsky & Vilkovisky Phys.Rept. 119 (1985) & Nucl.Phys. B333 (1990)

Avramidi arXiv:math-ph/0107018

now select the universal, physical log divergences (throw away the power-laws) cf. Burgess & London

hep-ph/9203216

and use dimensional regularisation

$$\left(\Gamma_{1-\text{loop}}^{\text{log}} \sim \int d^4 x \sqrt{g_{\text{eff}}} \left\{ R^2 + 2R_{\mu\nu}R^{\mu\nu} \right\} \right)$$

these are all curvature quantities built out of the effective metric

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geometrical intuition

when are these quantum corrections small?

$$|\sqrt{g_{\rm eff}}\,R^2[\,g_{eff}\,]\,|\ll |\mathcal{L}_{\rm classical}|$$
 while $|Z^\mu_{\ \nu}|\gg 1$

the stability of the EFT under quantum effects is determined by this condition for all theories regardless of invoking a special symmetry

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- let us get back to the cubic galileon $Z \sim 1 + \frac{\Box \phi}{\Delta 3}$
- so the effective metric will depend on second order derivatives of the fields (and will potentially have some constant terms as well). recall that:

$$g_{\mu\nu}^{\rm eff} = Z_{\mu\nu} \sqrt{g}$$

- so the logarithmic quantum effects we've calculated can only generate higher order derivative operators
- for quantum corrections do be under control, background configurations are such that

$$\phi \sim \Lambda$$

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cf. Luty et al. hep-th/0303116 Nicolis & Rattazzi hep-th/0404159

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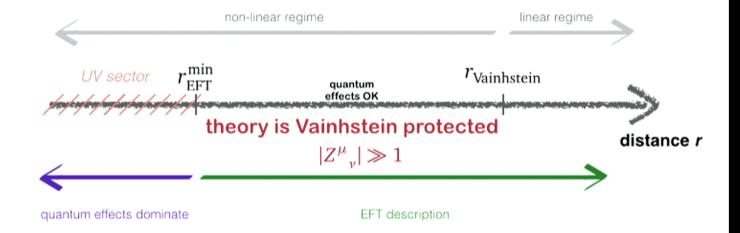
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dynamical regimes

We see a Vainhstein screening effect at the quantum level

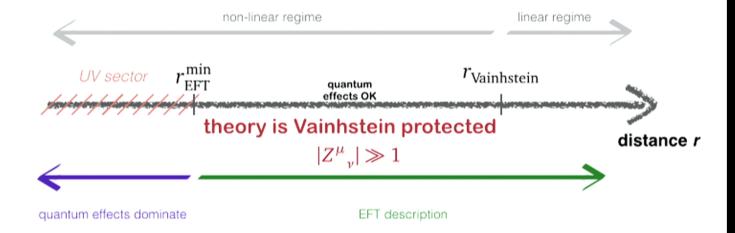


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benefits of the one-loop effective action

- method is quite generic and accounts for all one-loop effects
- results are robust for all theories exhibiting the Vainhstein mechanism
- it's still possible to do better using the DRGE and Wetterich equation

let's apply what we've learned to mGR

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mGR action

dRGT [de Rham, Gabadadze & Tolley] 1007.0443 & 1011.1232

Interactions are algebraically special (very constrained) and ghost-free

$$\mathcal{L}_{\text{mGR}} = \frac{M_{\text{Pl}}^2}{2} \sqrt{-g} \left(R[g] + \frac{m^2}{4} \sum_{n=0}^{4} \tilde{\alpha}_n \mathcal{U}_n[X] \right)$$

$$X^{\mu}_{\ \nu} \equiv \left(\sqrt{g^{-1}f}\right)^{\mu}_{\ \nu}$$

involves two metrics

To be precise, they are

$$\mathcal{U}_2 = \left[X\right]^2 - \left[X^2\right]$$

$$\mathcal{U}_3 = [X]^3 - 3[X][X^2] + 2[X^3]$$

$$\mathcal{U}_4 = [X]^4 - 6[X]^2[X^2] + 8[X^3][X] + 3[X^2]^2 - 6[X^4]$$

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mGR encompasses a class of theories

Interactions are finite, algebraically special and ghost-free (classically)

$$\mathcal{L}_{\text{mGR}} = \frac{M_g^2}{2} \left(\sqrt{-g} R[g] + \frac{M_f^2}{2 M_g^2} \sqrt{-f} R[f] + \sqrt{-g} \frac{m^2}{4} \sum_{n=0}^4 \tilde{\alpha}_n \mathcal{U}_n[X] \right)$$

$$X^{\mu}_{\ \nu} \equiv \left(\sqrt{g^{-1}f}\right)^{\mu}_{\ \nu}$$

In this class of theories there are two metrics, by construction:

- ightharpoonup if $f_{\mu\nu}$ is fixed (Minkowski) , the theory is known as **massive gravity**.
- \triangleright if $f_{\mu\nu}$ is dynamical, we call it **massive biGravity** and add the EH term

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mGR corrected by quantum loops

eg. in dimensional regularisation

making a theorist very nervous!

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mGR corrected by quantum loops

eg. in dimensional regularisation

making a theorist very nervous!

Why? The detuning of the potential, on its own, is not worrisome.

For large background configurations however, where the Vainshtein mechanism is active, the mass of the induced ghost can be made arbitrarily small. This is bad!

riding with ghosts can be OK

The 1-loop effective action resums all these corrections

$$\mathcal{L}_{\rm quantum}^{\rm 1-loop} \sim m^4 \; \frac{1}{Z(h_0)} \; \frac{h^2}{M_{\rm Pl}^2} \;$$

'Alice in QuantumLand

tensor object

Focusing on the helicity-0 mode again

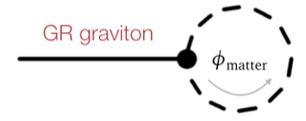
$$\mathcal{L}_{\rm quantum}^{\rm 1-loop} \sim \frac{1}{Z(h_0)} \, \frac{(\partial^2 \pi)^2}{M_{\rm pl}^2} \ll \mathcal{L}_{\rm classical}$$

The graviton mass m and the interaction coefficients $\tilde{\alpha}_n$ are technically natural.

coupling mGR to matter
$$S_{\text{matter}} = \int d^4x \sqrt{-g} \mathcal{L}_{\text{matter}}(g, \phi_{\text{matter}})$$

what types of coupling can we have? let's assume the minimal coupling and focus on the 1-point function, to start with.

Assume we couple GR with a matter sector.



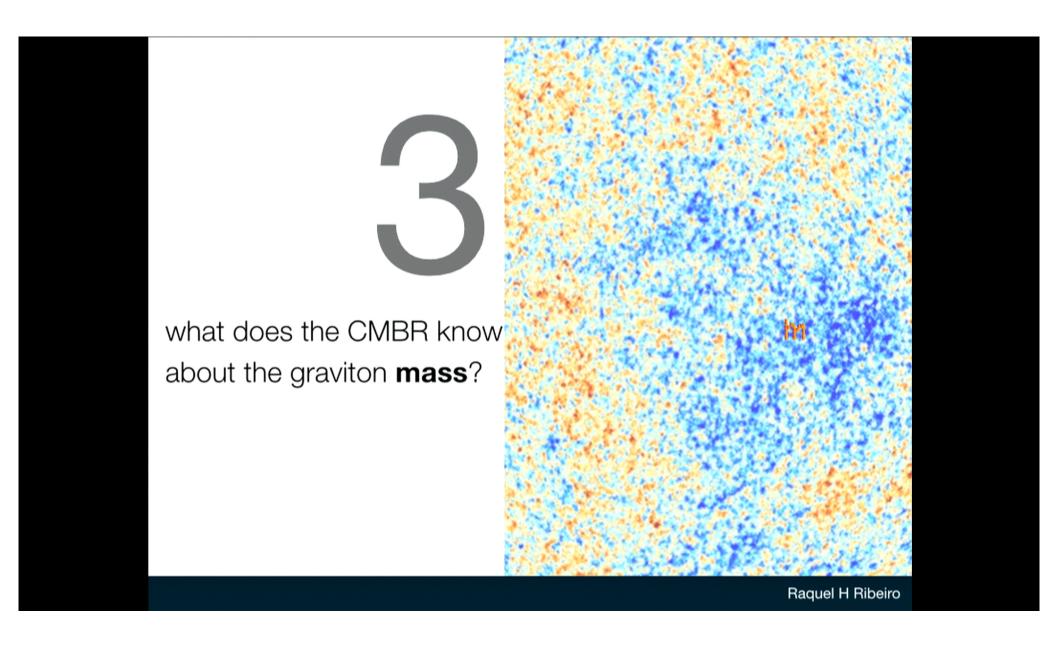
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coupling biGravity to matter

what types of coupling are sensible?

- only the metric **g** couples to the matter sector
- --- \wedge \wedge $[g] = \sqrt{g}$



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cosmology in mGR

- cosmology is one of the motivations behind these theories
- absence of diffeomorphism invariance implies no spatially flat or closed FLRW solutions
 D'Amico et al.
- some solutions are known to exhibit instabilities (eg: infinitely strong coupling and gradient instabilities) or issues with the Higuchi bound

Massive Gravity Cosmology is still in its infancy

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coupling biGravity to matter non-trivially

Does this coupling pass all the tests?

No, the ghost is excited on highly anisotropic backgrounds.

But on relatively smooth backgrounds, theory is perfectly well defined at $E\sim\Lambda_3$.

And, one-loop corrections do not introduce any ghost degree of freedom (though they do correct the graviton mass m).

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This theory has interesting phenomenological applications:

with this non-minimal coupling, mGR does admit FLRW solutions.
no-go

 \triangleright self-accelerated background probes no ghosts at $E \sim \Lambda_3$.

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riangle Start with the action $\mathscr{L}=L_{
m mGR}+\mathscr{L}_
ho(g,
ho)+\mathscr{L}_\chi(g_{
m eff},\chi)$

and choose $\mathrm{d} s_g^2 = -N(t)^2 \mathrm{d} t^2 + a(t)^2 \mathrm{d} \vec{x}^2$ and unitary gauge for the Stuckelberg fields.

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 \triangleright Within the decoupling limit and for a spatially homogeneous field χ_0 :

$$m^2 M_{\rm Pl}^2 (aN)^{-1} \partial_t (a^2 - a^3) = 2AB \ \tilde{a}^2 H \left(\frac{\dot{\chi}_0^2}{2\tilde{N}^2} - V(\chi_0) \right)$$

We obtain a modified Friedmann equation:

$$3M_{\rm Pl}^2 H^2 = \rho + \frac{m^2 M_{\rm Pl}^2}{2B a^2} \left[5B + 2(A - 6B)a - 3(A - 2B)a^2 \right] + 2A \left(\frac{\tilde{a}}{a} \right)^3 V(\chi_0)$$

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We obtain a modified Friedmann equation:

$$3M_{\rm Pl}^2 H^2 = \rho + \frac{m^2 M_{\rm Pl}^2}{2B a^2} \left[5B + 2(A - 6B)a - 3(A - 2B)a^2 \right] + 2A \left(\frac{\tilde{a}}{a} \right)^3 V(\chi_0)$$

riangleright Start with the action $\mathscr{L}=L_{ ext{mGR}}+\mathscr{L}_{
ho}(g,
ho)+\mathscr{L}_{\chi}(g_{ ext{eff}},\chi)$

and choose $ds_g^2 = -N(t)^2 dt^2 + a(t)^2 d\vec{x}^2$ and unitary gauge for the Stuckelberg fields.

 \triangleright Within the decoupling limit and for a spatially homogeneous field χ_0 :

$$m^{2}M_{\rm Pl}^{2}(aN)^{-1}\partial_{t}(a^{2}-a^{3}) = 2AB \ \tilde{a}^{2}H\left(\frac{\dot{\chi}_{0}^{2}}{2\tilde{N}^{2}}-V(\chi_{0})\right)$$

We obtain a modified Friedmann equation:

$$3M_{\rm Pl}^2 H^2 = \rho + \frac{m^2 M_{\rm Pl}^2}{2B a^2} \left[5B + 2(A - 6B)a - 3(A - 2B)a^2 \right] + 2A \left(\frac{\tilde{a}}{a} \right)^3 V(\chi_0)$$

FLRW cosmology works

What does the CMBR know about the graviton mass?

Raquel H Ribeiro

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Massive Gravity in the CMBR

- the helicity-2 mode is massive, so the dispersion relation for GWs changes
- b the primordial spectrum of GWs is directly affected by the graviton mass

Raquel H Ribeiro

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Massive Gravity in the CMBR

- > the helicity-2 mode is massive, so the dispersion relation for GWs changes
- the primordial spectrum of GWs is directly affected by the graviton mass

Make the splitting $g_{\mu\nu}=\eta_{\mu\nu}+h_{\mu\nu}$ and compute the quadratic action:

$$S_{\text{tensors}}^{(2)} \sim M_{\text{Pl}}^2 \int d^4x \left[\dot{h}^{ij} \dot{h}_{ij} + \frac{h^{ij}}{a^2} \nabla^2 h_{ij} - m^2 f(\tilde{\alpha}_n) h^{ij} h_{ij} \right]$$

Comoving momenta larger than the graviton mass are unaffected. Any changes in the tensor spectrum are only visible for low multipole number.

See also Dubovsky et al. 0907.1658

Raquel H Ribeiro

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BiGravity in the CMBR

ightharpoons In bigravity, we perturb both metrics $g_{\mu
u}=\eta_{\mu
u}+h_{\mu
u}$ and $f_{\mu
u}=\eta_{\mu
u}+\ell_{\mu
u}$

Focus on a regime where the diagonalisation can be done, and the action reads

$$S_{\rm tensors,biGrav}^{(2)} \sim \int {\rm d}^4x \left[M_+^2 \left(\dot{v}_+^{ij} \dot{v}_{ij}^+ + \frac{v_+^{ij}}{a^2} \, \nabla^2 v_{ij}^+ \right) + M_-^2 \left(\dot{v}_-^{ij} \dot{v}_{ij}^- + \frac{v_-^{ij}}{a^2} \, \nabla^2 v_{ij}^- - m_{\rm eff}^2 v_-^{ij} v_{ij}^- \right) \right]$$

$$massless \ mode \ (2 \ dof) \qquad massive \ mode \ (5 \ dof)$$

Raquel H Ribeiro

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BiGravity in the CMBR

ightharpoons In bigravity, we perturb both metrics $g_{\mu
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$$massless \ mode \ (2 \ dof) \qquad massive \ mode \ (5 \ dof)$$

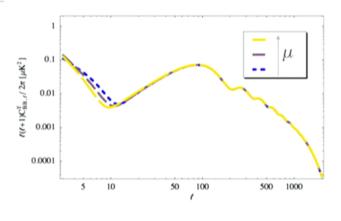
The tensor-to-scalar ratio in these theories is $r_{
m BiGrav} = r_{
m GR} + arepsilon \; r_{
m mGR}$

work in preparation



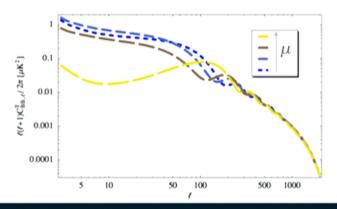
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hints of a massive graviton in the CMBR



μ here is a placeholder for the mass of the massive tensor mode

if the graviton mass is very small, power spectrum is insensitive to that mass

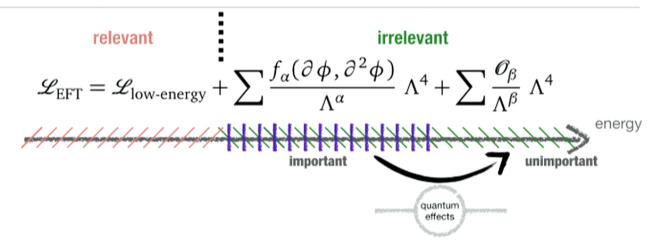


plots from Dubovsky et al. 0907.1658

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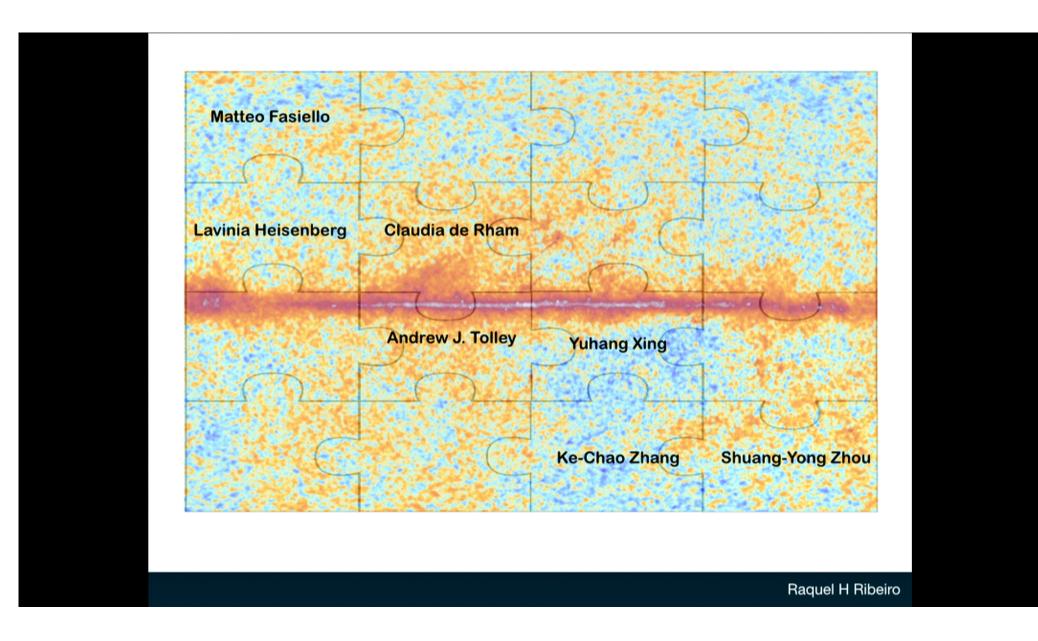
EFTs as a preferred toolkit



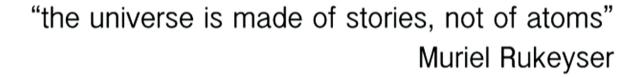
- notion of theory error becomes clearer
- the range of scales of the EFT is defined
- role of symmetry becomes more subtle
- applications to all theories exhibiting the Vainshtein mechanism (including galileons)

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EFT principles in 1405.5213, massive gravity considerations in 1307.7169, 1408.1678, 1409.3834

+ more to come soon

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