

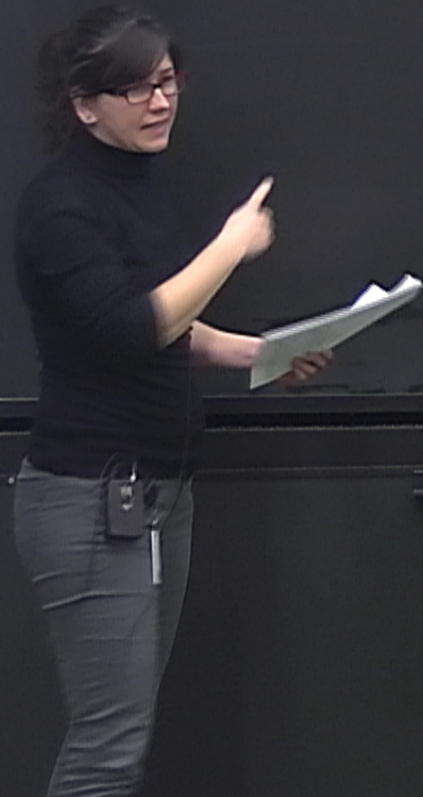
Title: Quantum Information Review-4

Date: Feb 20, 2015 11:30 AM

URL: <http://pirsa.org/15020064>

Abstract:

Linear Optics

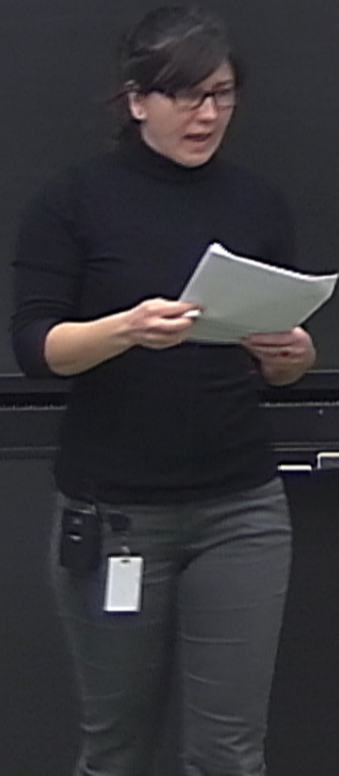


Linear Optics

- States of light to enc

Linear Optics

- States of light to encode q. information



Linear Optics

- States of light to encode q. information

\hat{a} - annihilation

\hat{a}^\dagger - creation operator

$$\hat{a}|n\rangle = \sqrt{n}|n-1\rangle$$

$$\hat{a}^\dagger|n\rangle = \sqrt{n+1}|n+1\rangle$$

Linear Optics

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"numb"

Linear Optics

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 \hat{a}^\dagger - creation operator

$$\hat{a}|n\rangle = \sqrt{n}|n-1\rangle$$

$$\hat{a}^\dagger|n\rangle = \sqrt{n+1}|n+1\rangle$$

$$\hat{n} = \hat{a}^\dagger \hat{a} \quad \text{"number operator"}$$

$$\hat{n}|n\rangle = n|n\rangle$$

Linear Optics

- States of light to encode q. information
- \hat{a} - annihilation
 \hat{a}^+ - creation operator

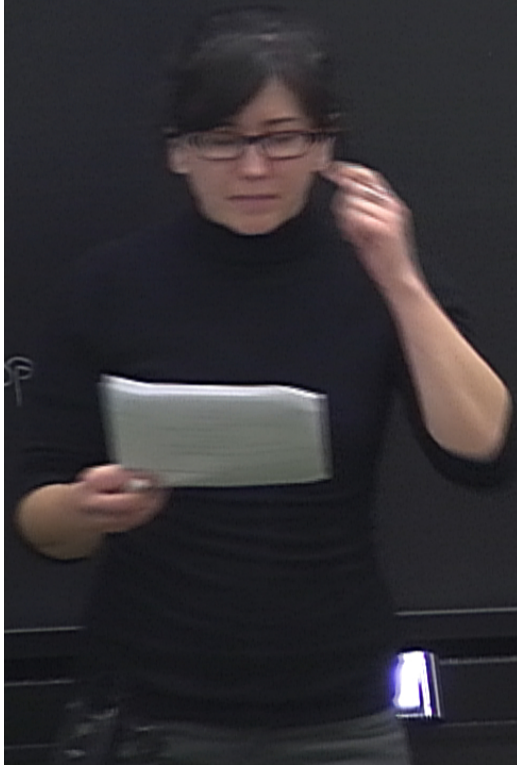
$$\hat{a}|n\rangle = \sqrt{n}|n-1\rangle$$

$$\hat{a}^+|n\rangle = \sqrt{n+1}|n+1\rangle$$

$$\hat{n} = \hat{a}^+ \hat{a} \quad \text{"number operator"}$$

$$\hat{n}|n\rangle = n|n\rangle$$

Satisfies (3), (6), (7)



Satisfies (5), (6), (7)

Single photons

rator"

Single photons

Dual-rail e

Single photons

Dual-rail encoding

a, b

a

b

Polarization encoding

Single photons

Dual-rail encoding

a, b

a _____



$$|0\rangle_L = |1\rangle_a |0\rangle_b \rightarrow |0\rangle_L$$

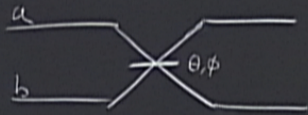
$$|1\rangle_L = |0\rangle_a |1\rangle_b \rightarrow e^{i\phi} |1\rangle_L$$

Polarization encoding

Dual

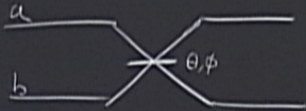
encoding

Dual-rail



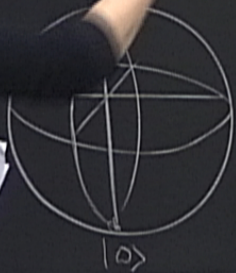
Polarization

Dual-rail



$$|0\rangle_L \rightarrow \cos\theta |0\rangle_L + e^{i\phi} \sin\theta |1\rangle_L$$

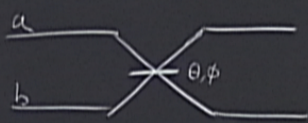
$$|1\rangle_L \rightarrow e^{i\phi} \cos\theta |0\rangle_L + \sin\theta |1\rangle_L$$



Polarization

Polarization

Dual-rail



$$|0\rangle_L \rightarrow \cos\theta |0\rangle_L + e^{i\phi} \sin\theta |1\rangle_L$$

$$|1\rangle_L \rightarrow e^{i\phi} \sin\theta |0\rangle_L + \cos\theta |1\rangle_L$$



coding

$$a|n\rangle = \sqrt{n+1}|n+1\rangle$$

$$\hat{n}|n\rangle = n|n\rangle$$

Single photons

Dual-rail encoding

b

b

$$|0\rangle_L = |0\rangle_a |0\rangle_b \rightarrow |0\rangle_L$$

$$\rightarrow e^{i\theta} |1\rangle_L$$

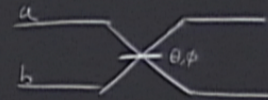
Polarization encoding

Two polarization modes x, y

$$|0\rangle_L = |1\rangle_x |0\rangle_y = |x\rangle$$

$$|1\rangle_L = |0\rangle_x |1\rangle_y = |y\rangle$$

Dual-rail



$$|0\rangle_L \rightarrow \cos\theta |0\rangle_L + e^{i\phi} \sin\theta |1\rangle_L$$

$$|1\rangle_L \rightarrow e^{i\phi} \sin\theta |0\rangle_L + \cos\theta |1\rangle_L$$



$$a|n\rangle = \sqrt{n+1}|n+1\rangle$$

$$\hat{n}|n\rangle = n|n\rangle$$

Single photons

Dual-rail encoding

a, b



$$|0\rangle_L = |1\rangle_a |0\rangle_b \rightarrow |0\rangle_L$$

$$|1\rangle_L = |0\rangle_a |1\rangle_b \rightarrow e^{i\phi} |1\rangle_L$$

Polarization encoding

Two polarization modes x, y

$$|0\rangle_L = |1\rangle_x |0\rangle_y = |x\rangle$$

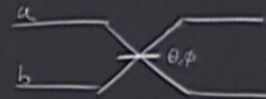
$$|1\rangle_L = |0\rangle_x |1\rangle_y = |y\rangle$$

$$|H\rangle, |V\rangle$$

$$|D\rangle, |A\rangle$$

$$|R\rangle, |L\rangle$$

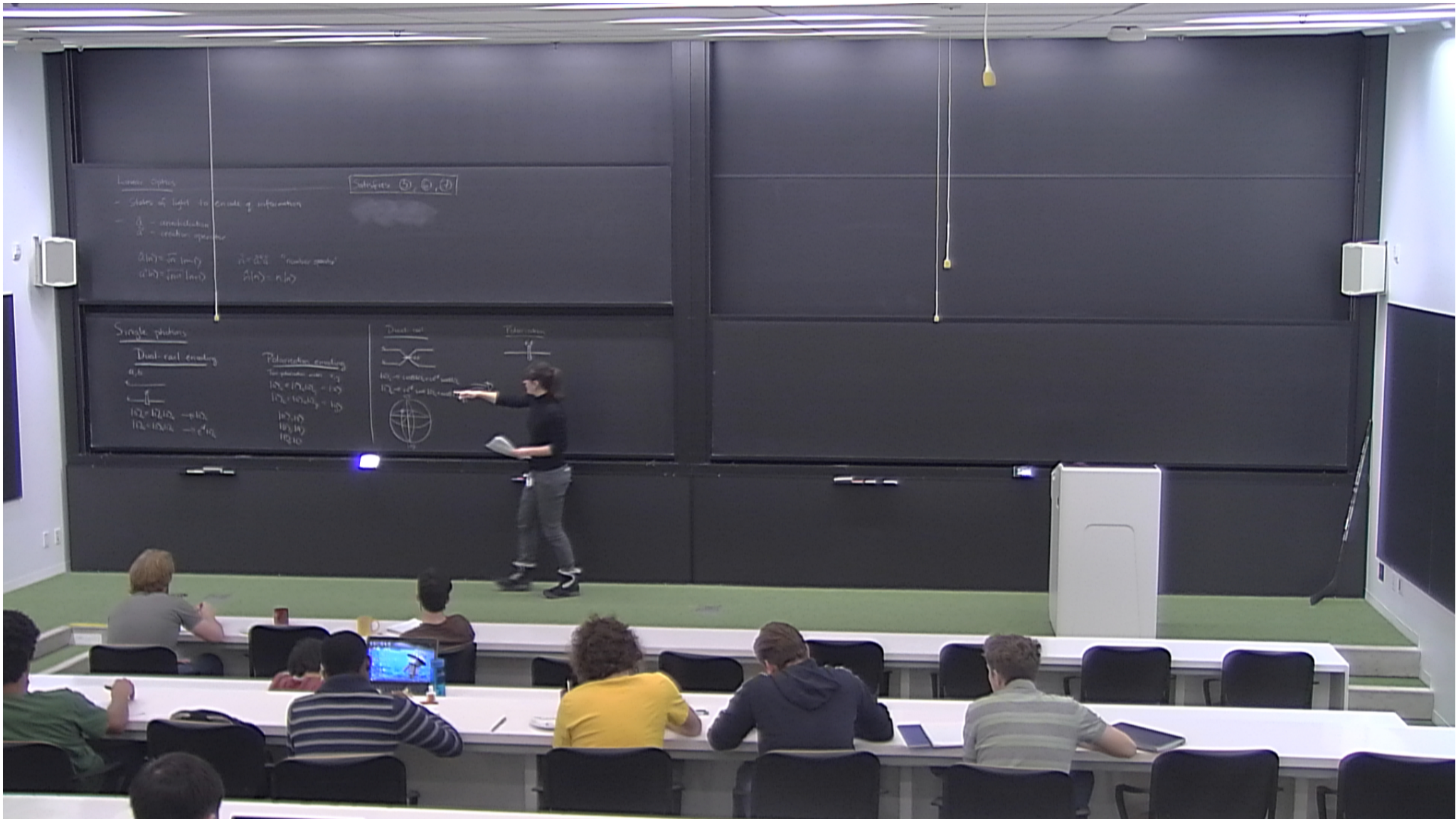
Dual-rail

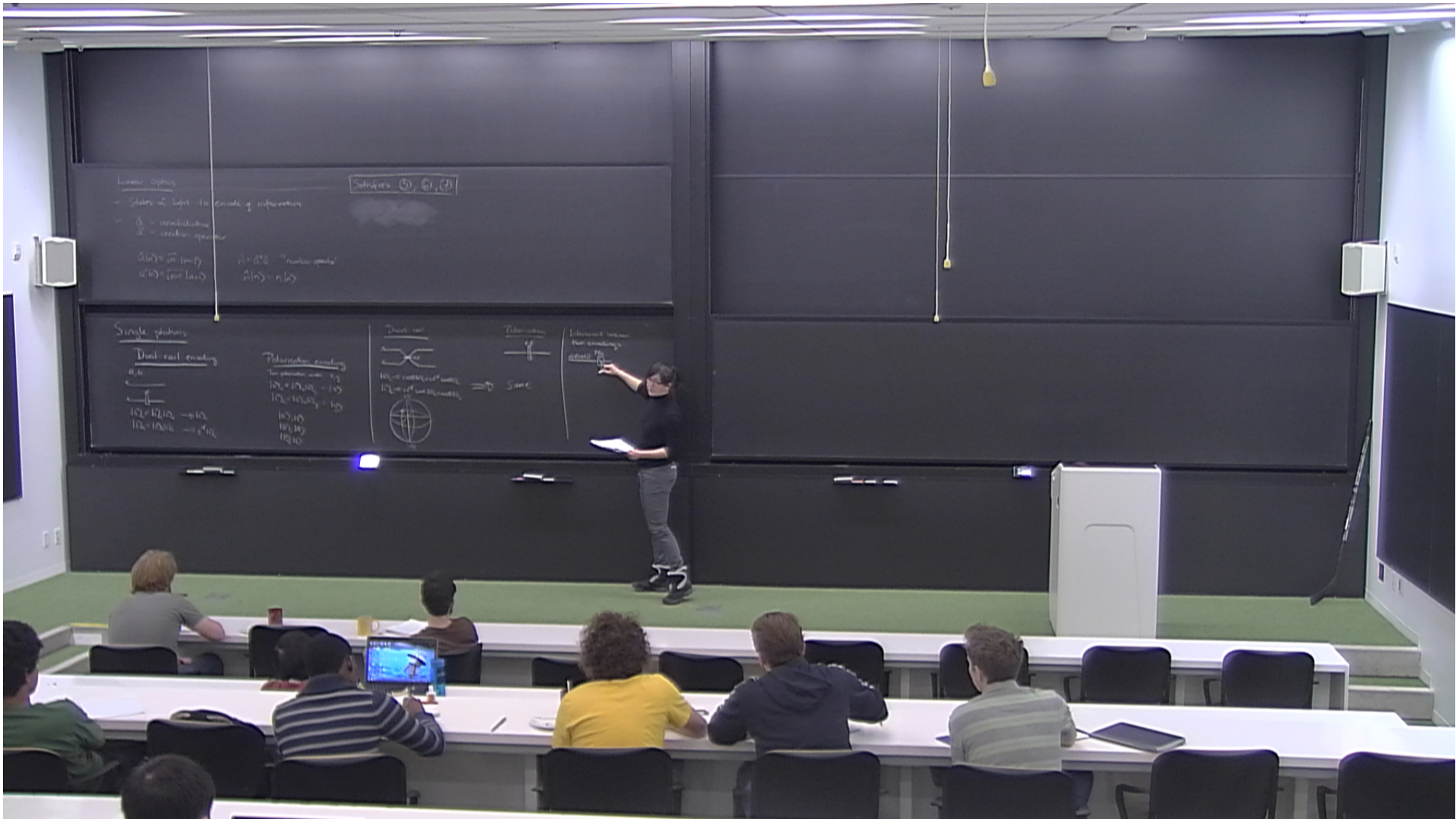


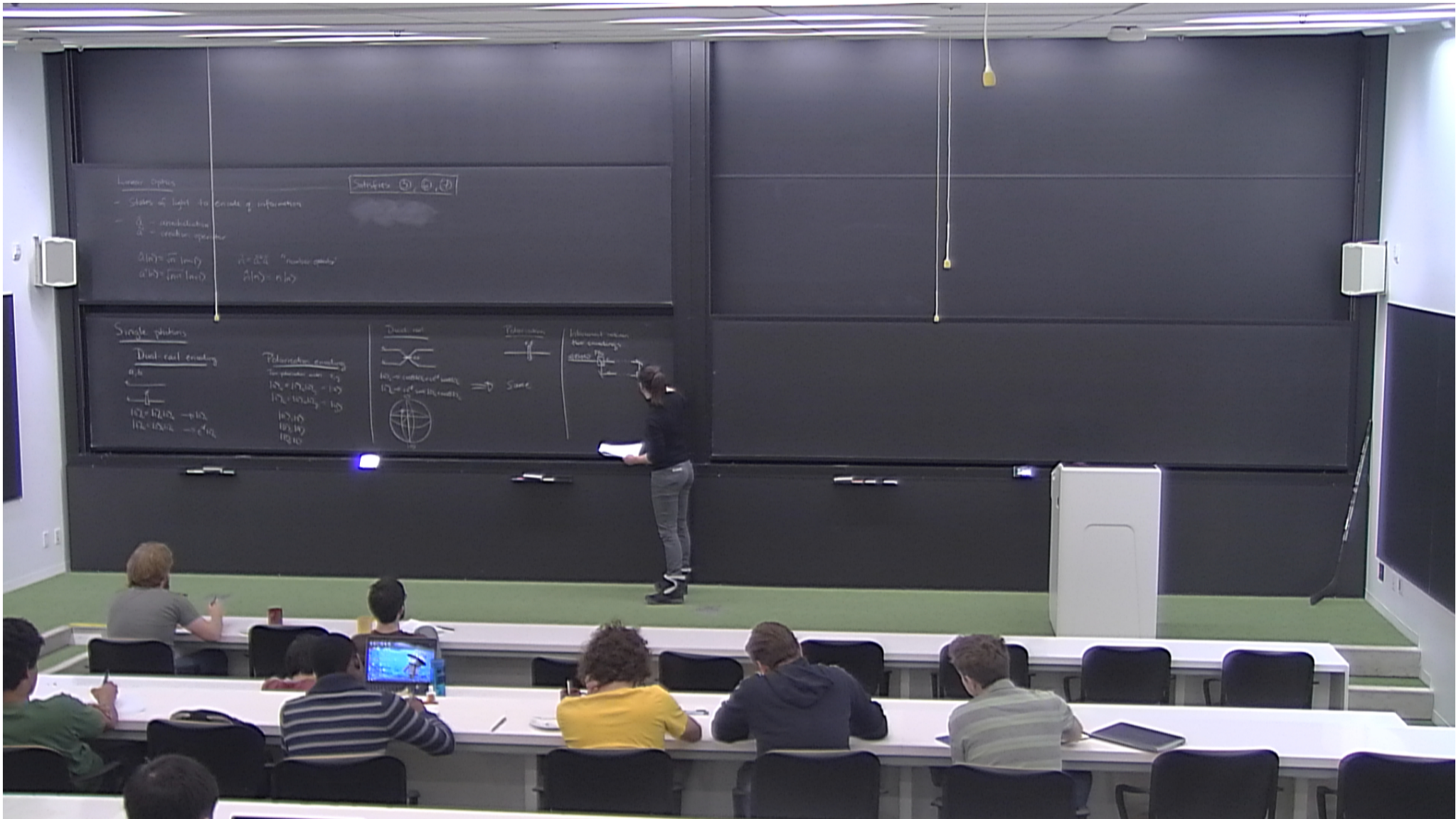
$$|0\rangle_L \rightarrow \cos\theta |0\rangle_L + e^{i\phi} \sin\theta |1\rangle_L$$

$$|1\rangle_L \rightarrow e^{i\phi} \sin\theta |0\rangle_L + \cos\theta |1\rangle_L$$









ation encoding

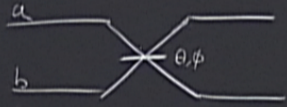
ation modes x, y

$$|x\rangle|0\rangle_y = |x\rangle$$

$$|0\rangle_x|1\rangle_y = |y\rangle$$

- $|1\rangle$
- $|2\rangle$
- $|3\rangle$

Dual-rail

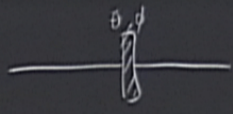


$$\cos\theta|0\rangle_L + e^{i\phi}\sin\theta|1\rangle_L$$

$$\Rightarrow e^{i\phi}\sin\theta|0\rangle_L + \cos\theta|1\rangle_L$$

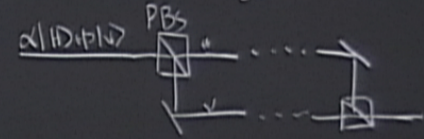


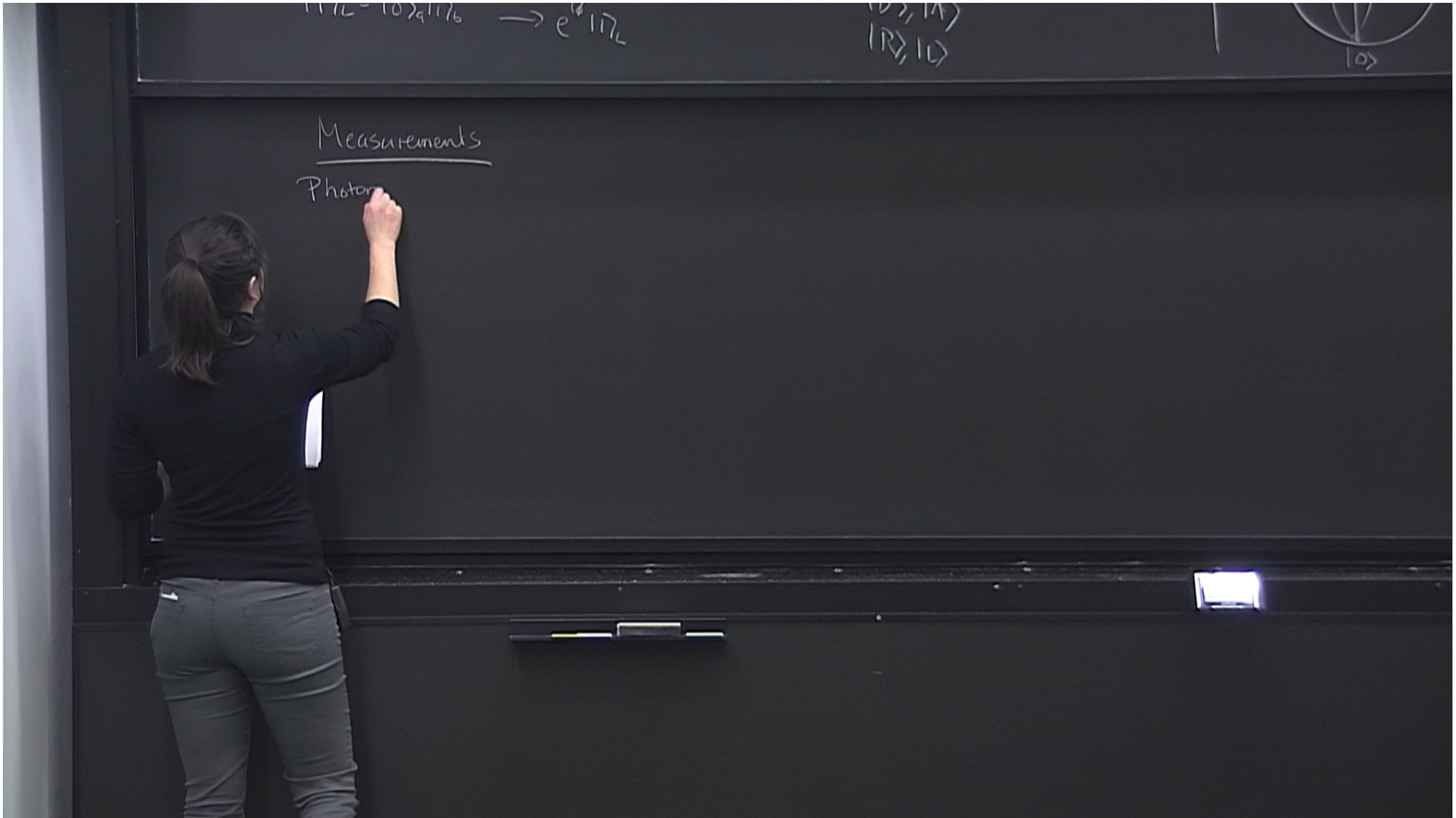
Polarization



Same

Interconvert between two encodings.





$$|11\rangle_L = |0\rangle_a |1\rangle_b \rightarrow e^{i\theta} |11\rangle_L$$

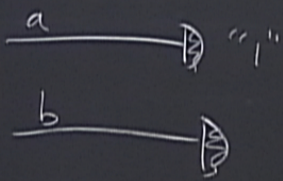
$$|0\rangle_a |1\rangle_b \\ |1\rangle_a |0\rangle_b$$



Measurements

Photon counting.

Dual Rail



$$|1\rangle_L \rightarrow e^{i\phi} |1\rangle_L$$

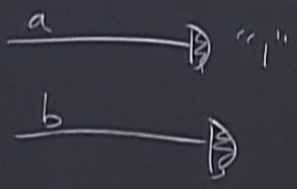
$$|0\rangle, |1\rangle$$
$$|R\rangle, |L\rangle$$



Measurements

Photon counting.

Dual Rail



Polarized



Single photon sources

11, 10
10

Single photon sources

Most common source

Ideally:

- on-demand
- efficient
- robust
- easy to implement

} don't exist

$|1\rangle$
 $|0\rangle$



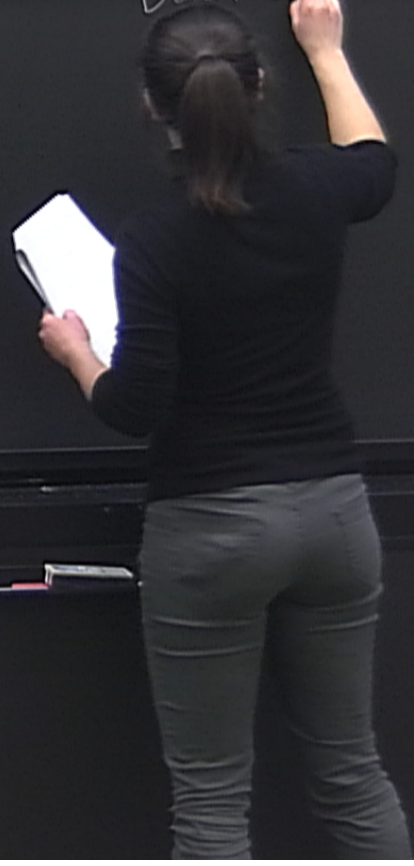
Single photon sources

Ideally:

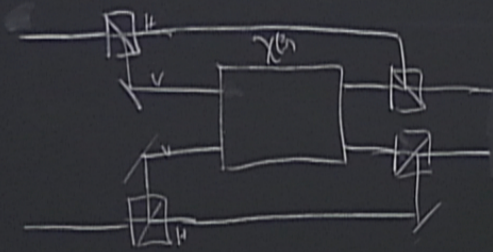
- on-demand
- efficient
- robust
- easy to implement

} don't exist

Most common source - Spontaneous Parametric
Down ω



Entangling gate

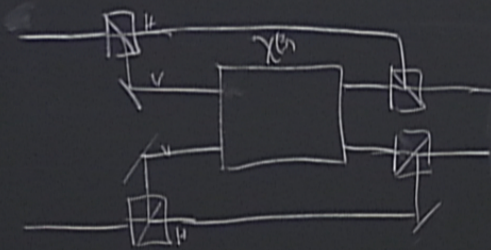


want $Kt = \pi/2$
now have $Kt \approx 10^{-18}$

$$\begin{aligned} |HH\rangle &= |HH\rangle \\ |HV\rangle &= |HV\rangle \\ |VH\rangle &= |VH\rangle \\ |VV\rangle &= e^{i2Kt} |VV\rangle \end{aligned}$$



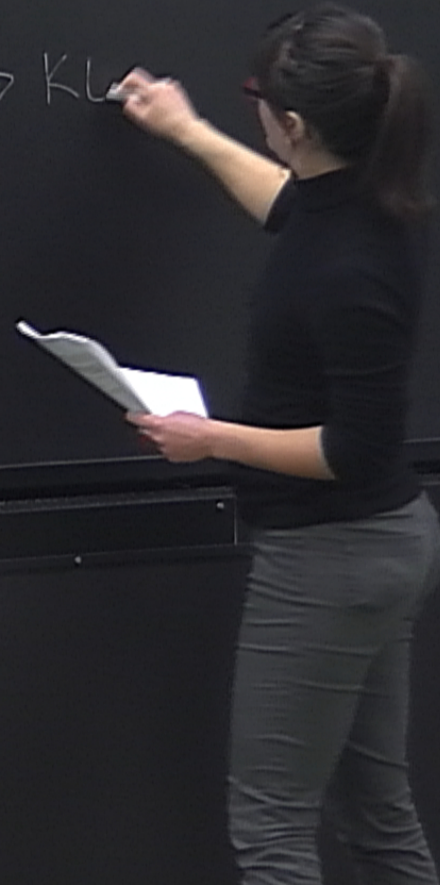
Entangling gate



$$\begin{aligned}
 |HH\rangle &= |HH\rangle \\
 |HV\rangle &= |HV\rangle \\
 |VH\rangle &= |VH\rangle \\
 |VV\rangle &= e^{i2\chi t} |VV\rangle
 \end{aligned}$$

want $\chi t = \pi/2$
 now have $\chi t \approx 10^{-18}$

Fortunately \rightarrow KL

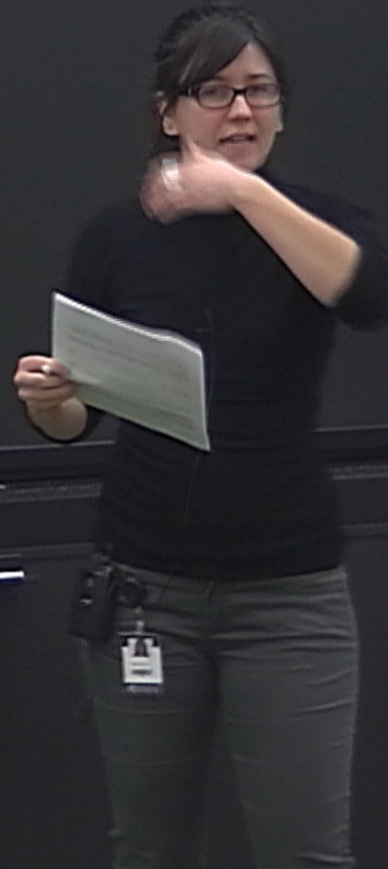


KLM

- ① Non-deterministic entangling gates possible
- ② Prob. of

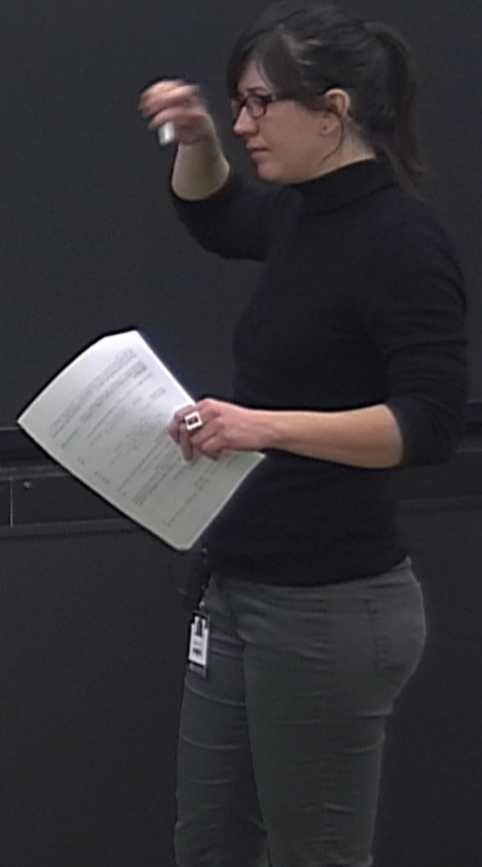
KLM

- ① Non-deterministic entangling gates possible
- ② Prob. of success can be increased arb. close to one.

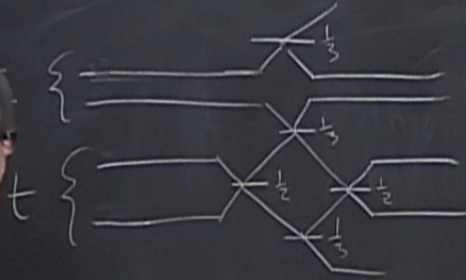


KLM

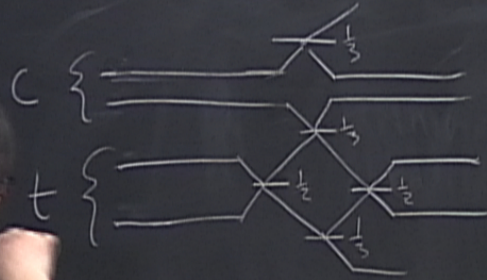
- ① Non-deterministic entangling gates possible
- ② Prob. of success can be increased arb. close to one.
- ③ Using quantum coding, can make resource-efficient



O'Brien, G. Prude.

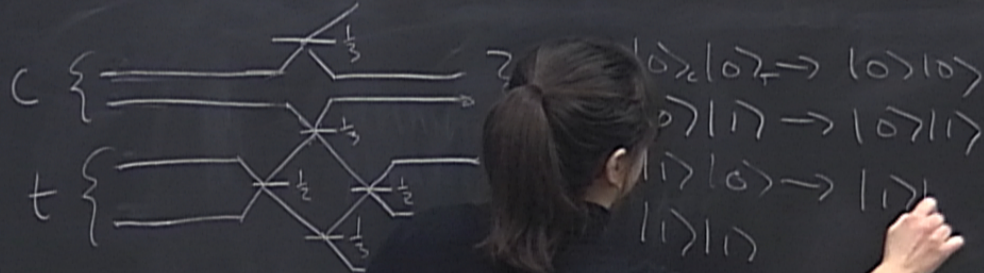


O'Brien, G. Prude . . .

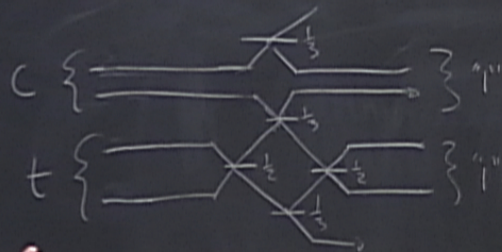


$$\begin{aligned} |0\rangle_c |0\rangle_t &\rightarrow |0\rangle_c |0\rangle_t \\ |0\rangle_c |1\rangle_t &\rightarrow |0\rangle_c |1\rangle_t \end{aligned}$$

O'Brien, G. Prude . . .



O'Brien, G. Prude . . .



$$\begin{aligned} |0\rangle_C |0\rangle_T &\rightarrow |0\rangle_C |0\rangle_T \\ |0\rangle_C |1\rangle_T &\rightarrow |0\rangle_C |1\rangle_T \\ |1\rangle_C |0\rangle_T &\rightarrow |1\rangle_C |1\rangle_T \\ |1\rangle_C |1\rangle_T &\rightarrow |1\rangle_C |0\rangle_T \end{aligned}$$

Succeeds $\frac{1}{9}$ time

