

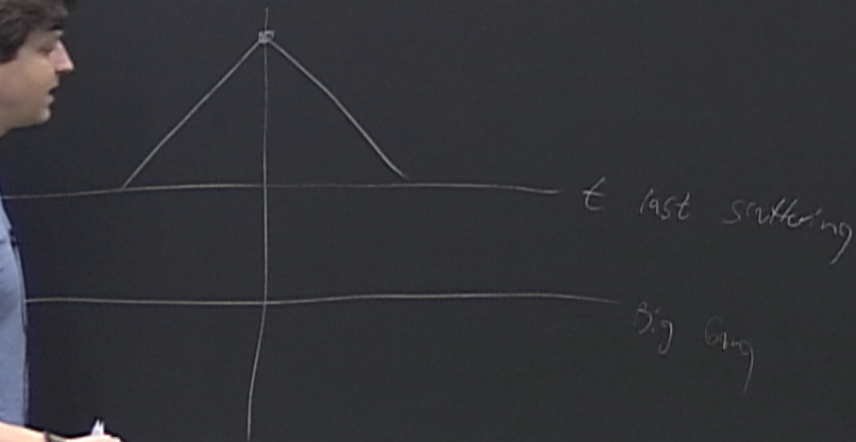
Title: Cosmology Review-15

Date: Feb 13, 2015 11:30 AM

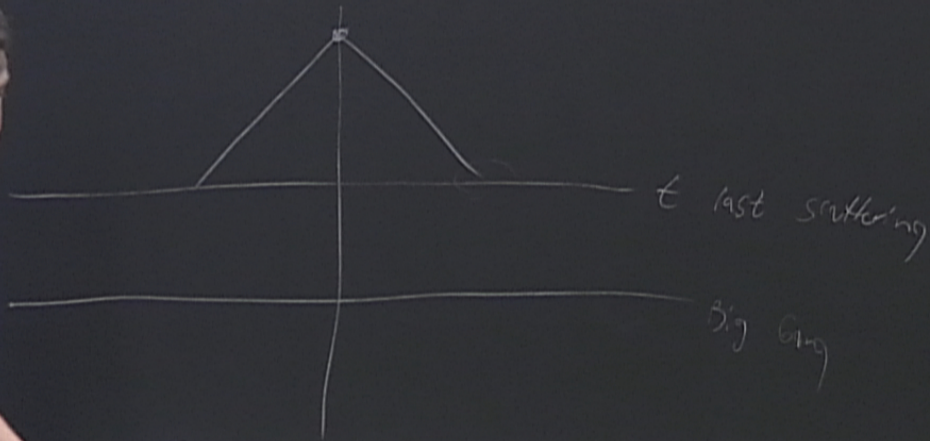
URL: <http://pirsa.org/15020038>

Abstract:

## Late-time effects

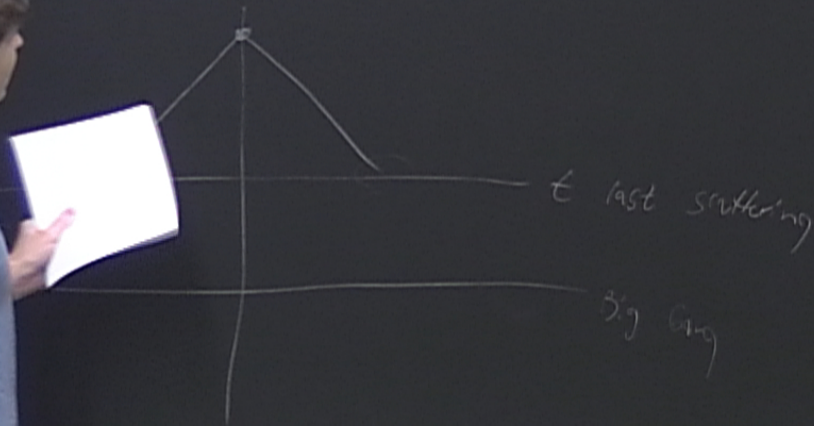


## Late-time effects



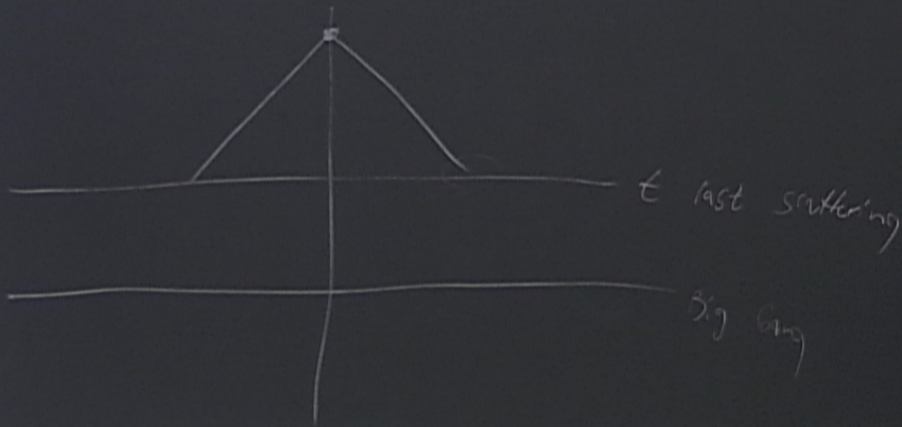
- doppler effect
- Sachs-Wolfe effect

## Late-time effects



- doppler effect
- sachs-wolfe effect
- integrated Sachs-wolfe effect
- Sunyaev-Zel'dovich effect

## Late-time effects



• doppler effect

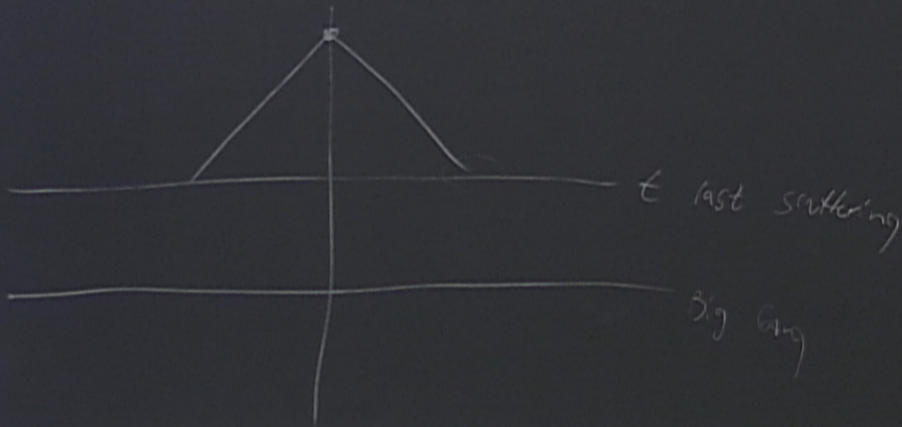
• Sachs-Wolfe effect

• Integrated Sachs-Wolfe effect

• Reissner-Nordström-Zel'dovich effect

(gravitational lensing)

## Late-time effects



- doppler effect
- sachs-wolfe effect
- integrated Sachs-wolfe effect
- Sunyaev-Zeldovich effect
- gravitational lensing

matter density contrast  $\delta(x) = \frac{\delta \rho_m(x)}{\rho_m}$

$$\ddot{\delta} + 2H\dot{\delta} - 4\pi G\rho\delta = 0$$

matter density contrast

$$\delta(x) = \frac{\delta \rho_m(x)}{\rho_m}$$

$$\ddot{\delta} + 2H\dot{\delta} - 4\pi G\rho\delta = 0$$

$$H^2 = \frac{8\pi G}{3} (\underbrace{\rho_m + \rho_r}_\rho) =$$



matter density contrast  $\delta(x) = \frac{\delta \rho_m(x)}{\rho_m}$

$$\ddot{\delta} + 2H\dot{\delta} - 4\pi G\rho\delta = 0$$

$$H^2 = \frac{8\pi G}{3} (\underbrace{\rho_m + \rho_r}_\rho) = \frac{8\pi G}{3} \frac{\rho_{eq}}{2}$$

matter density contrast  $\delta(x) = \frac{\delta \rho_m(x)}{\rho_m}$

$$x = \frac{a}{a_{eq}}$$

$$\ddot{\delta} + 2H\dot{\delta} - 4\pi G \rho \delta = 0$$

$$H^2 = \frac{8\pi G}{3} (\underbrace{\rho_m + \rho_r}_\rho) = \frac{8\pi G}{3} \frac{\rho_{eq}}{2} \left[ \left(\frac{a_{eq}}{a}\right)^3 + \left(\frac{a_{eq}}{a}\right)^4 \right]$$

matter density contrast

$$\delta(x) = \frac{\delta \rho_m(x)}{\rho_m}$$

$$x = \frac{a}{a_{eq}}$$

$x \gg 1$

$$\ddot{\delta} + 2H\dot{\delta} - 4\pi G \rho \delta = 0$$

$$H^2 = \frac{8\pi G}{3} (\underbrace{\rho_m + \rho_r}_\rho) = \frac{8\pi G}{3} \frac{\rho_{eq}}{2} \left[ \left(\frac{a_{eq}}{a}\right)^3 + \left(\frac{a_{eq}}{a}\right)^4 \right]$$

$$\delta(x) = \frac{\delta \rho_m(x)}{\rho_m}$$

$$x = \frac{a}{a_{eq}}$$

$x \gg 1$  matter domination  
 $x \ll 1$  rad

$$\frac{8\pi 6}{3} \frac{\rho_{eq}}{2} \left[ \left( \frac{a_{eq}}{a} \right)^3 + \left( \frac{a_{eq}}{a} \right)^4 \right]$$

$$\delta(x) = \frac{\delta \rho_m(x)}{\rho_m}$$

$$x = \frac{a}{a_{eq}}$$

$x \gg 1$  matter domination

$x \ll 1$  radiation domination

$$x^2 \left(1 + \frac{1}{x}\right) \frac{d^2 \delta}{dx^2} + \frac{3}{2} x \left[1 + \frac{2}{3x}\right] \frac{d\delta}{dx} - \frac{3}{2} \delta = 0$$

$$\frac{8\pi G}{3} \frac{\rho_{eq}}{2} \left[ \dots \right]$$

$$\delta(x) = \frac{\delta \rho_m(x)}{\rho_m}$$

$$x = \frac{a}{a_{eq}}$$

$x \gg 1$  matter domination

$x \ll 1$  radiation domination

$$\frac{8\pi G}{3} \frac{\rho_{eq}}{2} \left[ \left( \frac{a_{eq}}{a} \right)^3 + \left( \frac{a_{eq}}{a} \right)^4 \right]$$

$$x^2 \left( 1 + \frac{1}{x} \right) \frac{d^2 \delta}{dx^2} + \frac{3}{2} x \left[ 1 + \frac{2}{3x} \right] \frac{d\delta}{dx} - \frac{3}{2} \delta = 0$$

Solution  $x \ll 1 \Rightarrow \delta(x) \sim \ln$

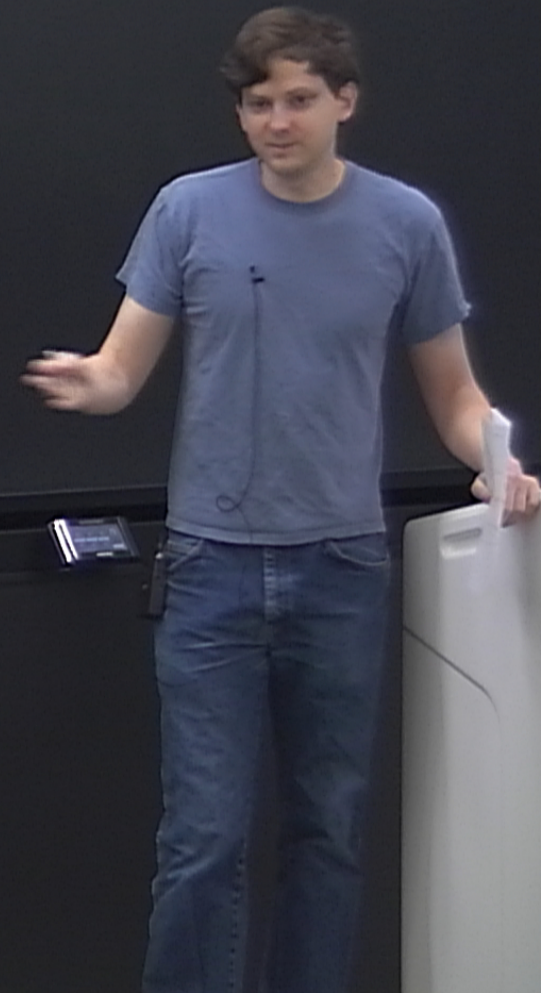
Solution  $x \ll 1 \Rightarrow \delta(x) \sim \ln x$

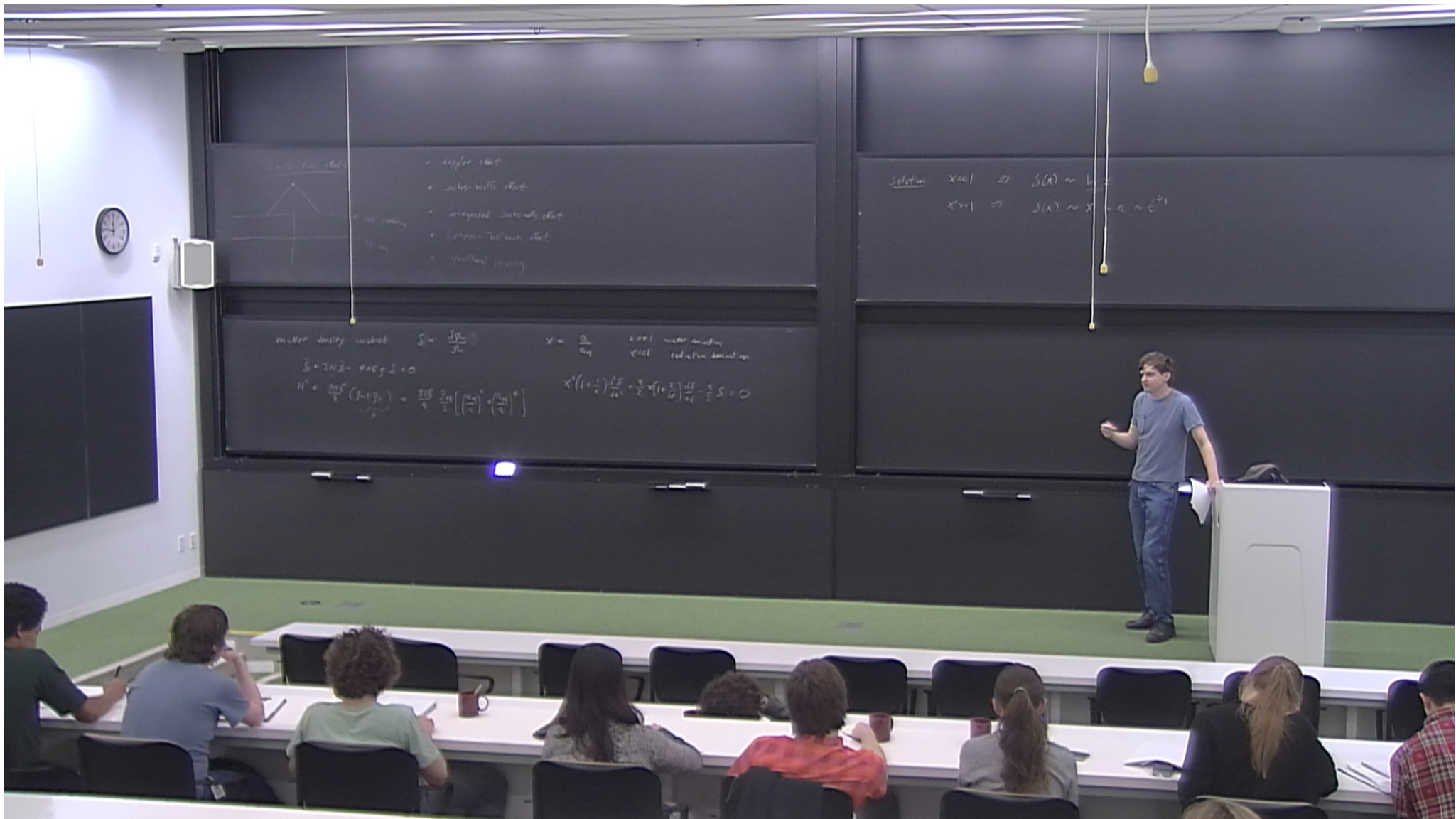
$x \gg 1 \Rightarrow \delta(x) \sim x \sim a \sim t^{4/3}$

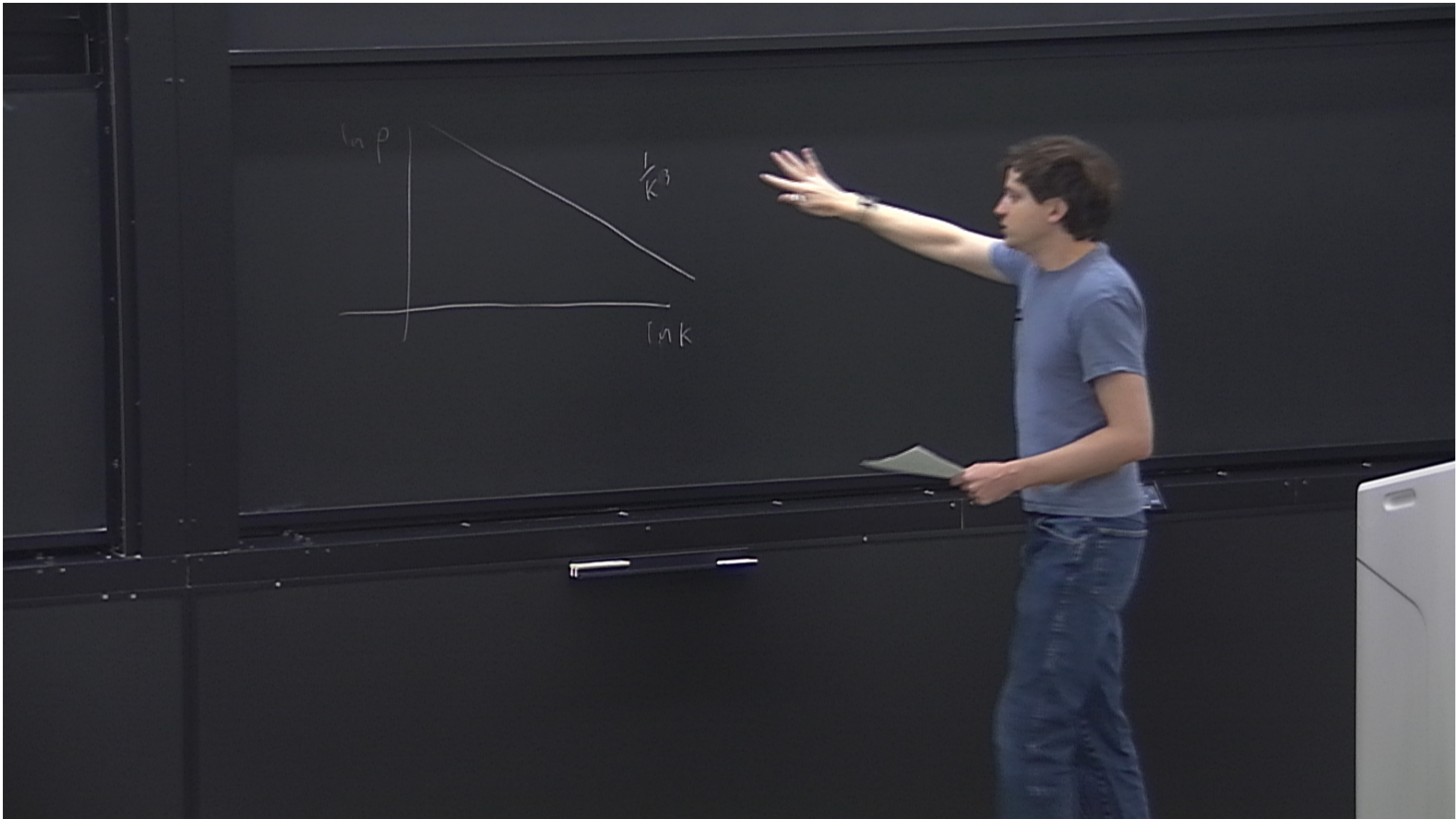


Solution

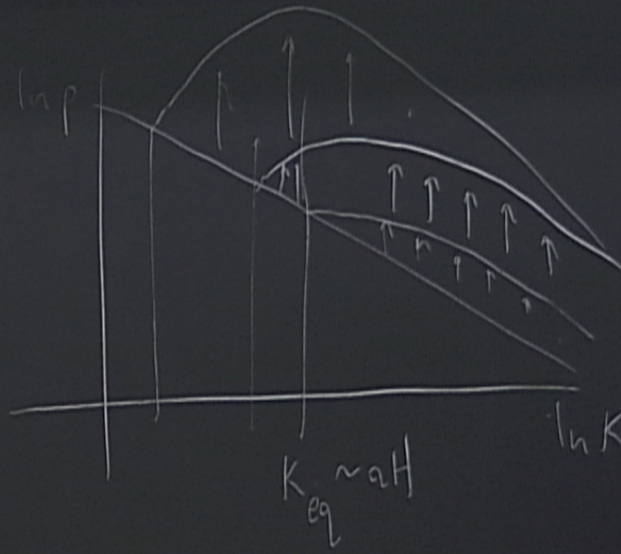
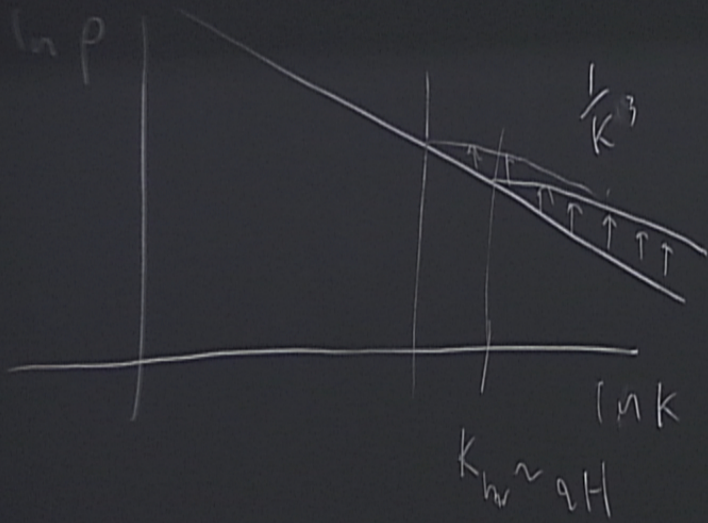
$$x \ll 1 \Rightarrow \delta(x) \sim \ln x$$
$$x \gg 1 \Rightarrow \delta(x) \sim x \sim a \sim t^{4/3}$$











matter density contrast

$$\delta(\vec{x}, t) = \delta \rho_m(\vec{x}, t)$$

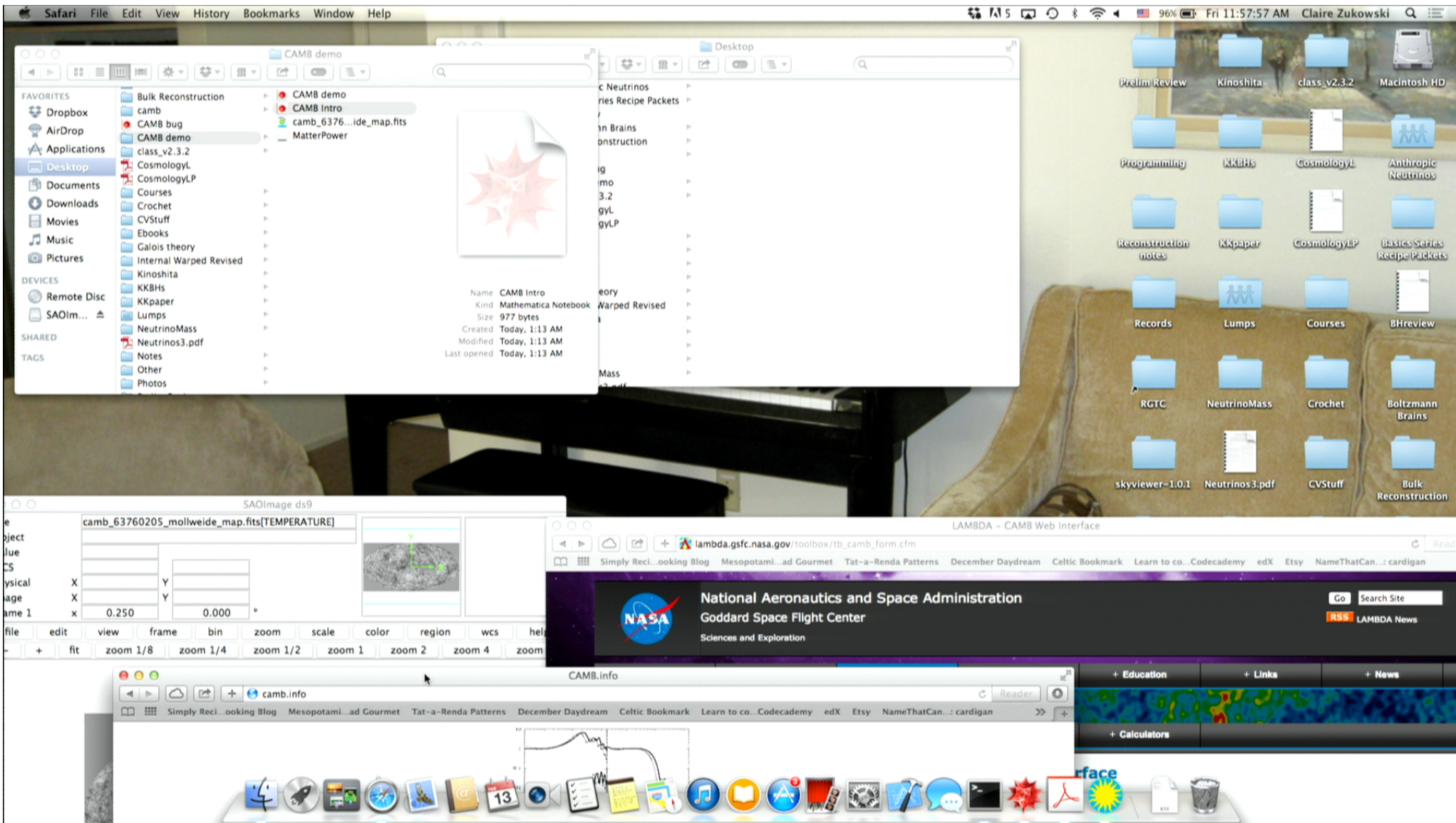
$$x = \frac{a}{a_{eq}}$$

$x \gg 1$   
 $x \ll 1$

$$\ddot{\delta} + 2H\dot{\delta} - 4\pi G \rho \delta = 0$$

$$H^2 = \frac{8\pi G}{3} \underbrace{(\rho_m + \rho_r)}_{\rho} = \left[ \left( \frac{a_{eq}}{a} \right)^4 \right]$$

$$x^2 \left( 1 + \frac{1}{x} \right) \frac{d^2 \delta}{dx^2} + \frac{3}{2} \delta = 0$$







SAOImage DS9 File Edit View Frame Bin Zoom Scale Color Region WCS Analysis Window Help

LAMBDA - CAMB Web Interface

lambda.gsfc.nasa.gov/toolbox/tb\_camb\_form.cfm

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11 Redshift 0.96 Scalar Spectral Index 0.005 Scalar Pivot 2 kmax  
 0.5 Width of Transition 0 Scalar Run Count 0.005 Tensor Pivot 5 k per logit  
 1 Ionization Fraction

File: camb\_63760205\_mollweide\_map.fits[TEMPERATURE]  
 Object:   
 Value:   
 WCS:   
 Physical X Y   
 Image X Y   
 Frame 1 x 0.250 0.000 \*

file edit view frame bin zoom scale color region wcs help  
 - + fit zoom 1/8 zoom 1/4 zoom 1/2 zoom 1 zoom 2 zoom 4 zoom 8

Initial Scalar Perturbatio  
 Adiabatic

For Vector Modes:  
 Regular (Neutrino Vorticity M...

• The ratio is that of the  
 • Supply 'Number' values  
 • To get  $\mu K^2$ , set a realistic  
 •  $k_{max}=0.5$  is enough fo

Performance and Rep...

Feedback Level Print  
 Lensing Method Curved Cor  
 Accurate BB No  
 Accurate EE No

• Massive Neutrino Appr  
 • Accurate EE: Set to yes  
 • Tensor Neutrinos: Indic  
 • Truncate late radiation  
 • Accuracy Boosts: High

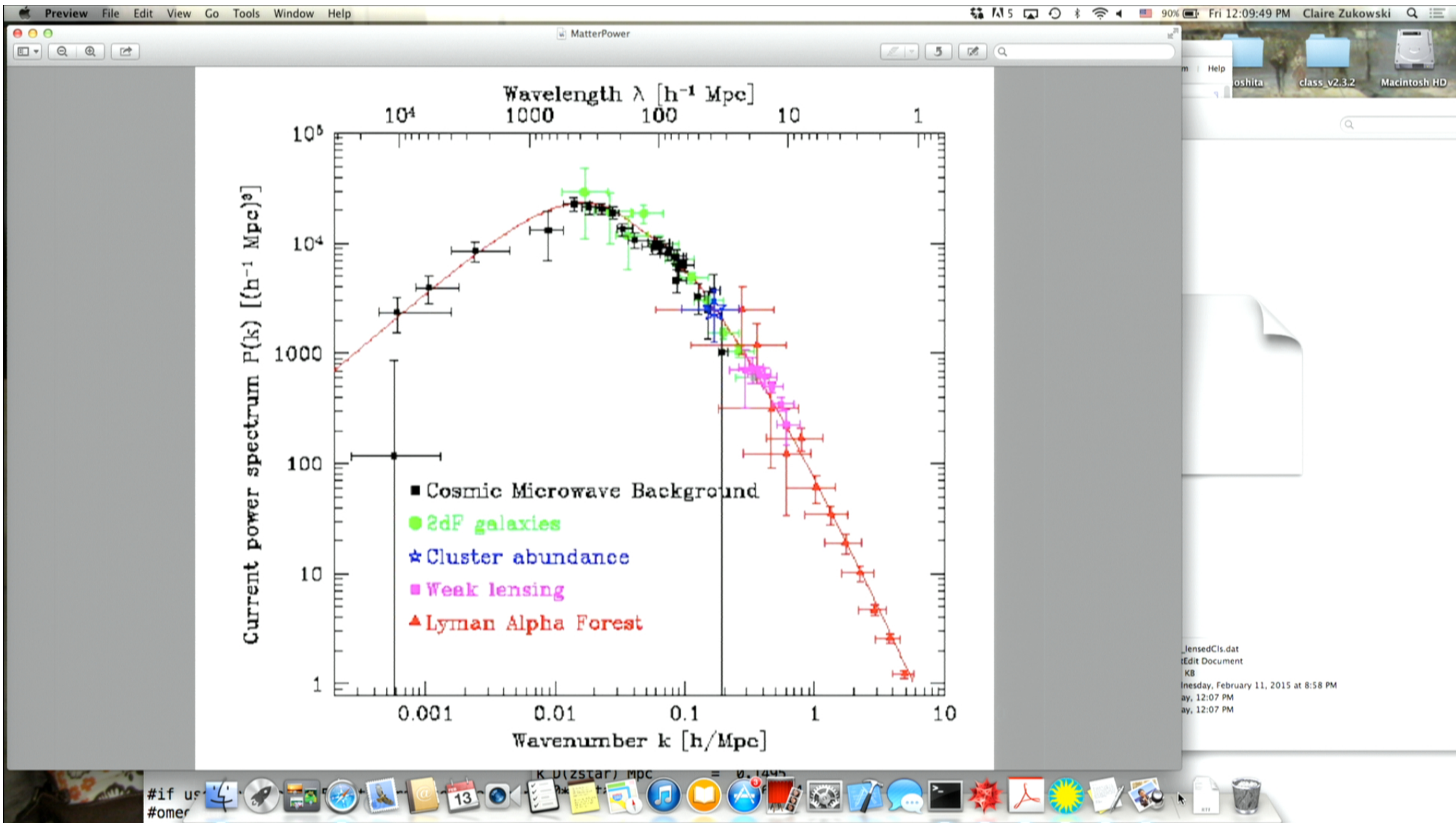
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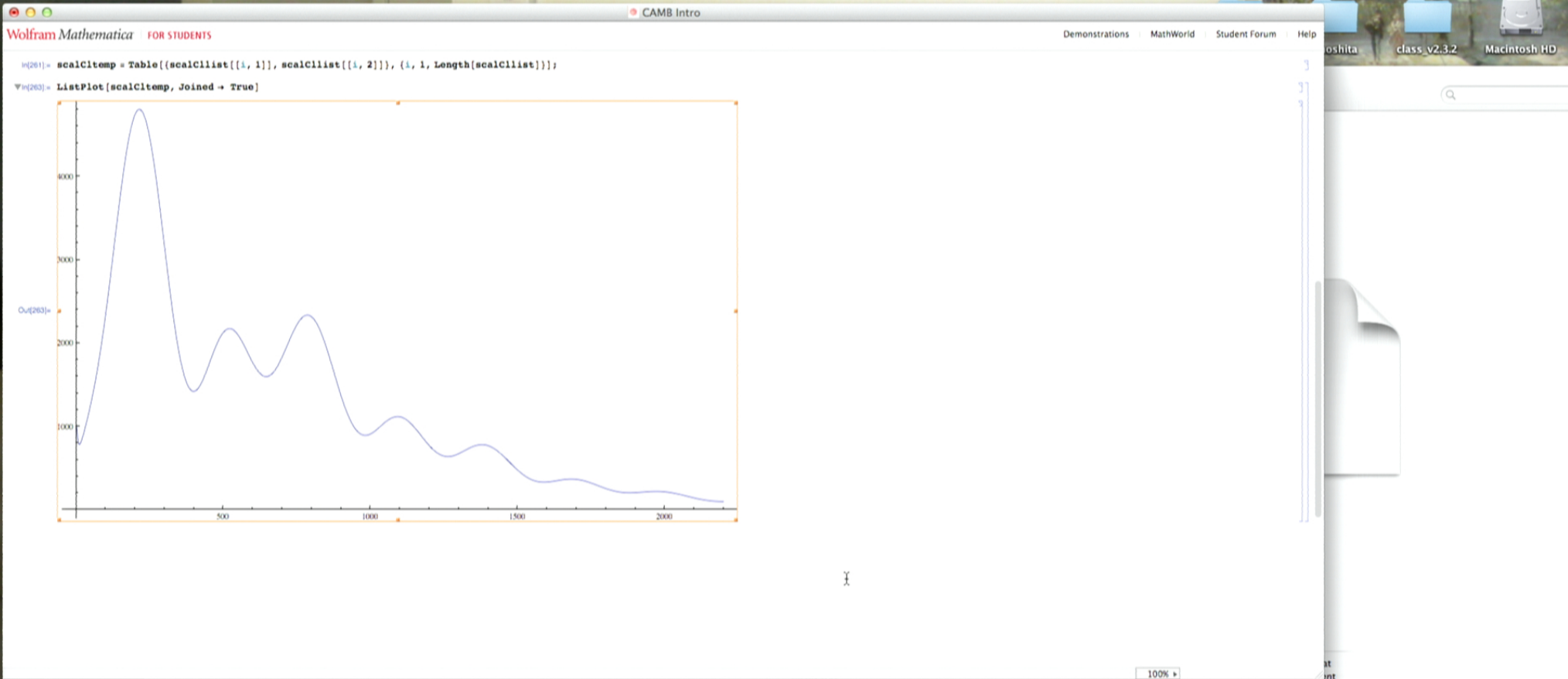
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```
#varying w is not supported by default
#w_a = 0
#if use_tabulated_w read (a,w) from file
#use_tabulated_w = F
#w_afile = wa.dat
#if use_omega
```

r\_s(zdrag)/Mpc = 139.63  
k\_D(zstar) Mpc = 0.1495

Size 141 KB  
Created Wednesday, February 11, 2015 at 8:58 PM  
Modified Today, 12:07 PM  
Last opened Today, 12:07 PM

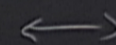
# Matter Power Spectrum:

Sc

# Matter Power Spectrum:

Scale of maximum

Horizon size at matter-rad equality



$\omega_m, z_{eq}$

## Matter Power Spectrum:

- Scale of maximum

Horizon size at matter-radiation equal



$\omega_m, z_{eq}$

- Wiggles at smaller scales

Baryon-acoustic oscillations



## Matter Power Spectrum:

- Scale of maximum

Horizon size at matter-rad equality



$\omega_m, z_{eq}$

- Wiggles at smaller scales

Baryon-acoustic oscillations (BAOs)



$\omega_b$  compared to  $\omega_{dm}$

# Matter Power Spectrum

- Scale of maximum  $\longleftrightarrow$  Horizon size at matter-rad equality  $\longleftrightarrow \omega_m, Z_{eq}$
- Wiggles at smaller scales  $\longleftrightarrow$  Baryon-acoustic oscillations (BAOs)  $\longleftrightarrow \omega_b$  compared to  $\omega_{cdm}$
- Amplitude  $\longleftrightarrow$  Primordial amplitude, length of  $\Lambda$  domination  $\longleftrightarrow A_s, \Omega_m$
- Tilt  $\longleftrightarrow$  Primordial tilt  $\longleftrightarrow n_s$



# CMB Power Spectrum

• scale

amplitude

$$\Theta_{\text{peak}} \sim \frac{\pi}{\Omega_{\text{peak}}} = \frac{ds}{D_A}$$

Time of matter-rad equality

$\omega_b, \omega_m$

$\omega_m, \Omega_n$

$\omega_m$