

Title: String Theory Review-12

Date: Feb 10, 2015 10:15 AM

URL: <http://pirsa.org/15020022>

Abstract:

$$\partial_n T^{\mu\nu} = 0 \quad \partial_0 T^0 = -\partial_i T^i$$

$$Q = \int_{\text{SPACE}} T^0 d^3x$$

$$\partial_0 Q = \int_{\text{SPACE}} \partial_0 T^0 d^3x$$

$$T^0 = \partial_a j^a$$

$$\partial_0 \omega = \int_{\text{SPACE}} \mathcal{T}^{\perp} dx$$

$$\mathcal{T}^{\perp} |_{\perp} = \partial_a j^a$$

$a \in \parallel$

$$T^{\mu}_{\nu} = \sum_I \dot{R}_I \delta^{\mu}_{\nu}$$

$$t^{\mu\nu} = \sum_I \dot{r}_I \delta^{\mu\nu}$$

$$T_{zz} |_{\perp} = T_{zz} |_{\parallel}$$

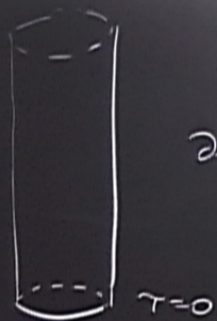
$$T_{zz} = -\frac{1}{2} \partial_z X \partial_z X$$

$$\partial X = \bar{\partial} X$$

$$\partial X = -\bar{\partial} X$$



CAUTION



$$\partial_\tau X|N\rangle = 0$$

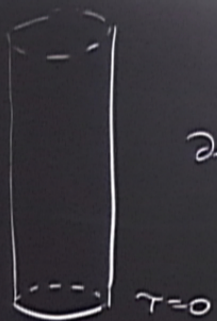
N

$$P|N\rangle = 0$$

$$(a_n - \bar{a}_{-n})|N\rangle = 0$$

$$|N\rangle = e^{\sum_{n>0} \frac{1}{n} a_n \bar{a}_{-n}} |0\rangle$$

$$X = x - 2ip\tau + \sum_{n \neq 0} \left[\frac{i}{n} a_n e^{in(\sigma + i\tau)} - \frac{i}{n} \bar{a}_n e^{-in(\sigma - i\tau)} \right]$$



$$\partial_\tau X|N\rangle = 0$$

N

$$P|N\rangle = 0$$

$$(a_n - \bar{a}_{-n})|N\rangle = 0$$

$$|N\rangle = e^{\sum_{n \neq 0} \frac{1}{n} a_{-n} \bar{a}_{-n}} |0\rangle = |0\rangle + a_{-1} \bar{a}_{-1} |0\rangle + \dots$$

$$X = x - 2ip\tau + \sum_{n \neq 0} \left[\frac{i}{n} a_n e^{in(\sigma + \tau)} - \frac{i}{n} \bar{a}_n e^{-in(\sigma - \tau)} \right]$$

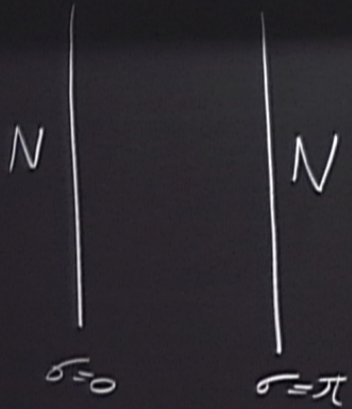
CAUTION

$$T = -\frac{1}{2} \partial X^\mu \partial X_\mu$$

$$\bar{T} = -\frac{1}{2} \bar{\partial} X^\mu \bar{\partial} X_\mu$$

$$\bar{\partial} X^\mu = g^{\mu\nu} \partial X_\nu$$

$$\partial_\perp X^\mu = \left(\frac{1-g}{1+g} \right)^{\mu\nu} \partial_\parallel X_\nu$$



$$X(\sigma, \tau) = x - 4ip\tau + \sum_{n=0}^{\infty} \frac{i}{n} a_n \left(e^{in(\sigma+\tau)} + e^{-in(\sigma+\tau)} \right)$$

$$p^2 = -\frac{1}{2}$$

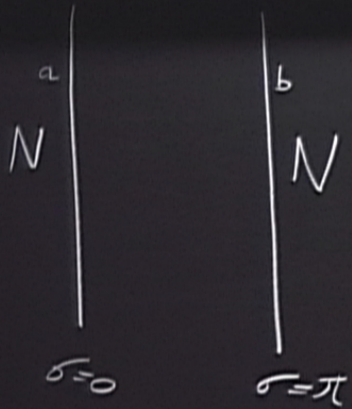
$$p^2 = 0$$

$$p^2 = \frac{3}{2}$$

$$|p\rangle$$

$$\epsilon_{\mu}(p) a_{-1}^{\mu} |p\rangle \dots$$

$$L_0 |p\rangle = 2p^2 |p\rangle$$



$$X(\sigma, \tau) = x - 4ip\tau + \sum_{n=0}^{\infty} \frac{i}{n} a_n \left(e^{in(\sigma+\tau)} + e^{-in(\sigma+\tau)} \right)$$

$$p^2 = -\frac{1}{2}$$

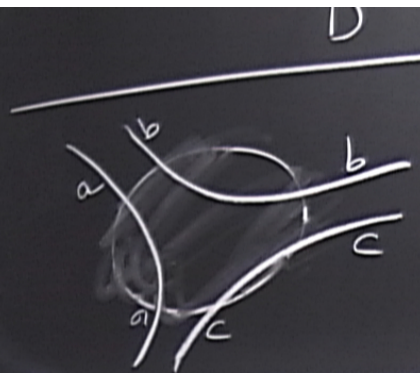
$$p^2 = 0$$

$$p^2 = \frac{3}{2}$$

$$|P\rangle_a^b$$

$$\in \langle P| a_{-1}^{\mu} |P\rangle_a^b \dots$$

$$L_0 |P\rangle = 2p^2 |P\rangle$$



$$\alpha |D\rangle = \alpha_0 |D\rangle$$

$$(a_n + \bar{a}_{-n}) |D\rangle = 0$$

$$|D\rangle = \int d\phi e^{i p \phi} e^{-\frac{1}{2} \phi^2}$$

$$N \quad \sigma=0$$

$$N \quad \sigma=\pi$$

$$p^2 = -\frac{1}{2}$$

$$|P\rangle_a^b$$

$$p^2 = 0$$

$$\sum_n (P) a_{-n} |P\rangle_a^b \dots$$

$$p^2 = \frac{1}{2}$$

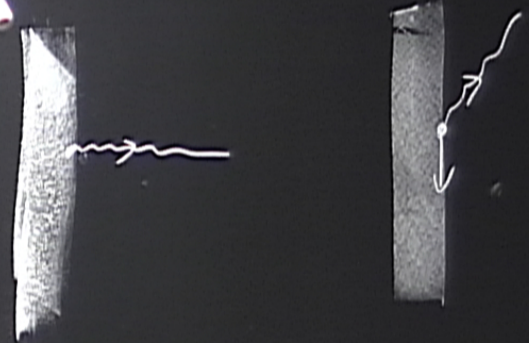
$$L_0 |P\rangle = 2P^2 |P\rangle$$

$$\begin{pmatrix} 1 & & & & & \\ & 1 & & & & \\ & & 1 & & & \\ & & & 1 & & \\ & & & & -1 & \\ & & & & & -1 \\ & & & & & & -1 \\ & & & & & & & -1 \end{pmatrix} = \eta_{\mu\nu}$$

$\eta_{\mu\nu}$

$$= \int e^{i\alpha \cdot p_{\perp}} |0, p_{\perp}\rangle + \int e^{i\alpha \cdot p_{\perp}} (a_{-1}^{\mu} \cdot \bar{a}_{-1}^{\mu} - a_{-1}^{\perp} \cdot a_{-1}^{\perp}) |0, p_{\perp}\rangle$$

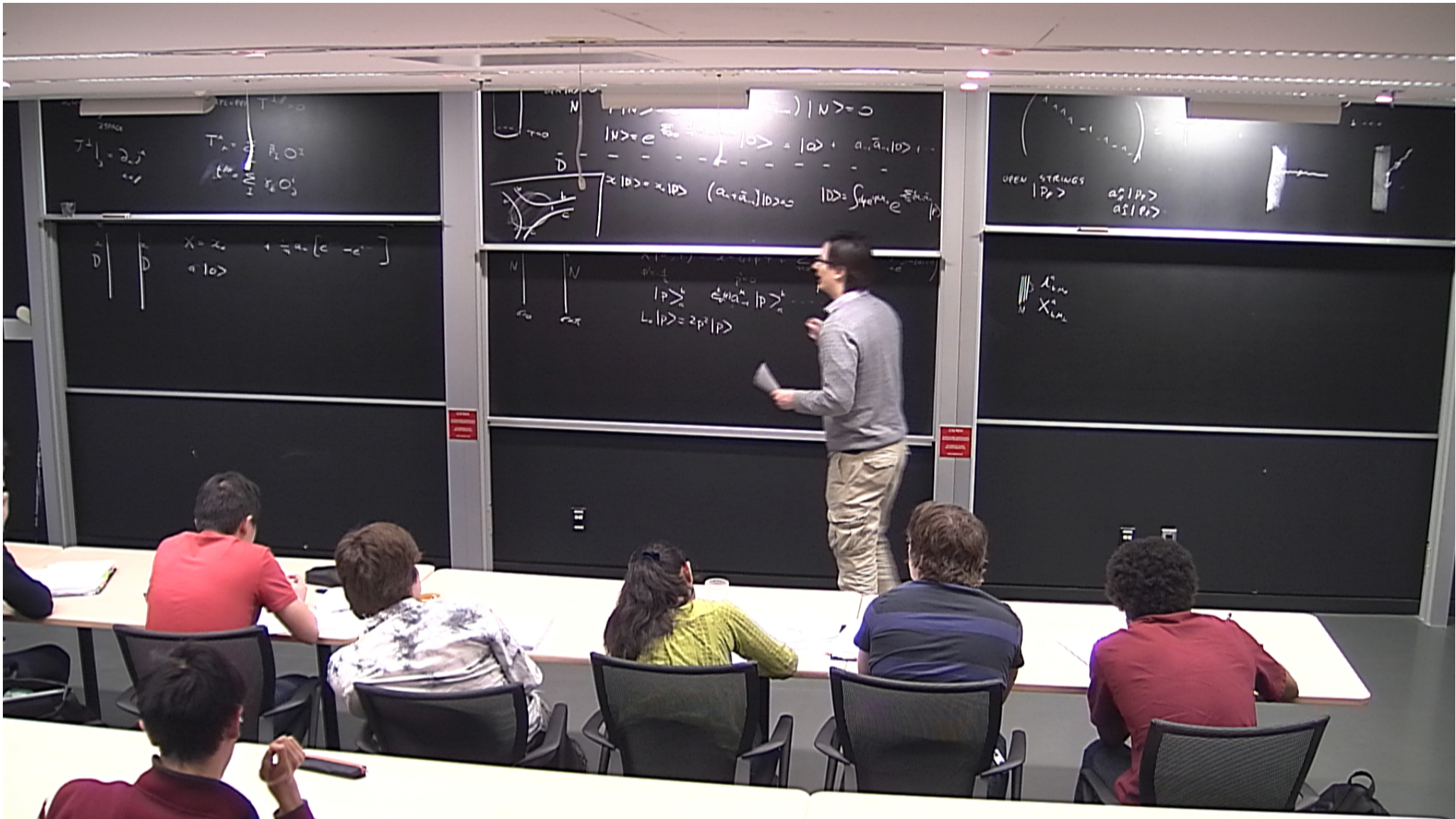
$\perp \dots$



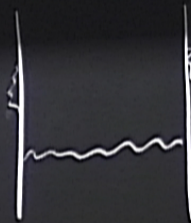
OPEN STRINGS
 $|P_{\parallel}\rangle$

$a_{\parallel}^{\mu} |P_{\parallel}\rangle$
 $a_{\perp}^{\mu} |P_{\parallel}\rangle$

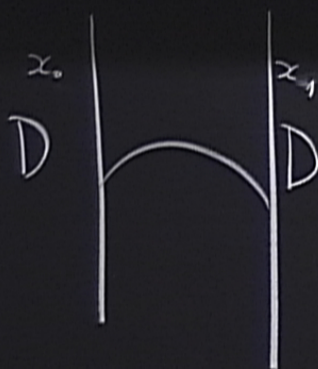
$$T = -\frac{1}{2} \partial X^{\mu} \cdot \partial X_{\mu} \quad \bar{T} = -\frac{1}{2} \bar{\partial} X^{\mu} \bar{\partial} X_{\mu}$$



$$\begin{array}{l}
 \left. \begin{array}{l} \text{||||} \\ \text{N} \end{array} \right\} \begin{array}{l} \mathcal{A}_{b\mu}^a \\ \mathcal{X}_{b\mu}^a \end{array} = \begin{pmatrix} \chi_0 & & & \\ & \chi_1 & & \\ & & \chi_2 & \\ & & & \chi_3 \end{pmatrix}
 \end{array}$$



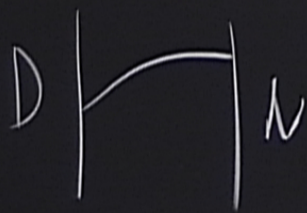
$\frac{1}{I} \delta \epsilon \circ$



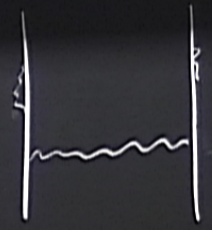
$$X = x_0 + \frac{x_1 - x_0}{\pi} \sigma + \frac{L}{\pi} a_n [e^{i\sigma} - e^{-i\sigma}]$$

$$a \cdot |0\rangle$$

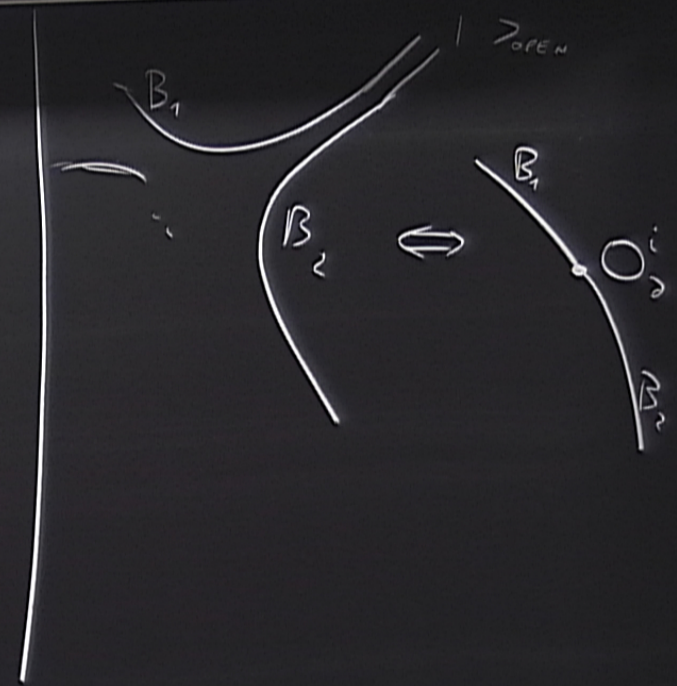
$$L_0 |0\rangle_{x_1}^{x_0} = \frac{(x_1 - x_0)^2}{8\pi} |0\rangle_{x_1}^{x_0}$$



$$\begin{array}{l}
 \left. \begin{array}{c} \text{||||} \\ \text{N} \end{array} \right\} \begin{array}{l} \mathcal{A}_{b\mu}^a \\ \mathcal{X}_{b\mu}^a \end{array} = \begin{pmatrix} \chi_0 & & & \\ & \chi_1 & & \\ & & \chi_2 & \\ & & & \chi_3 \end{pmatrix}
 \end{array}$$



a) / c



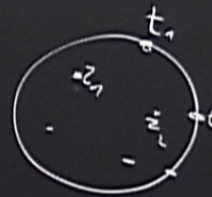
$$\frac{1}{I} \delta_{\alpha\beta} \delta_{\gamma\delta}$$

$$T_{zz} \Big|_0 = T_{\bar{z}\bar{z}} \Big|_0$$

$$T_{zz} = -\frac{1}{2} \partial_z X \partial_z X$$

$$\begin{aligned} \partial X &= \bar{\partial} X \\ \partial X &= -\bar{\partial} X \end{aligned}$$

$$N : \partial_{\perp} X = 0$$



$$\prod |z_0 - z_j| \prod |z_0 - t_j| \prod |t_i - t_j|^{-1}$$

$$\begin{aligned} \partial_{\parallel} X & \\ e^{i p X} & \end{aligned}$$

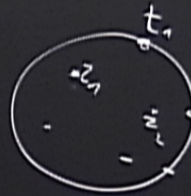
$$T_{zz} \Big|_D = T_{\bar{z}\bar{z}} \Big|_D$$

$$\partial X = \bar{\partial} X$$

$$\partial X = -\bar{\partial} X$$

$$T_{zz} = -\frac{1}{2} \partial X \partial X$$

$$N: \partial_+ X = 0$$



$$= \prod |z_0 - z_j| \prod |z_0 - t_j|^{-1}$$

$$D: \partial_- X$$

$$\partial_- X = e^{i p X}$$

$$X|_{\partial \Omega} \in \mathcal{L}$$

$$\partial_{\perp} X|_{\partial \Omega} \in N\mathcal{L}$$

$$\int_{\mathcal{L}} \sqrt{\det \frac{\partial X^{\mu}}{\partial u^{\alpha}} \frac{\partial X^{\nu}}{\partial u^{\beta}} G_{\mu\nu}} \, dX$$

$$\mathcal{L} \in \mathbb{R}^{25,1}$$