

Title: Visualizing Quantum Matter

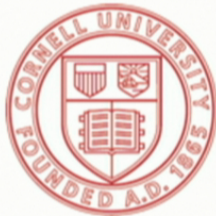
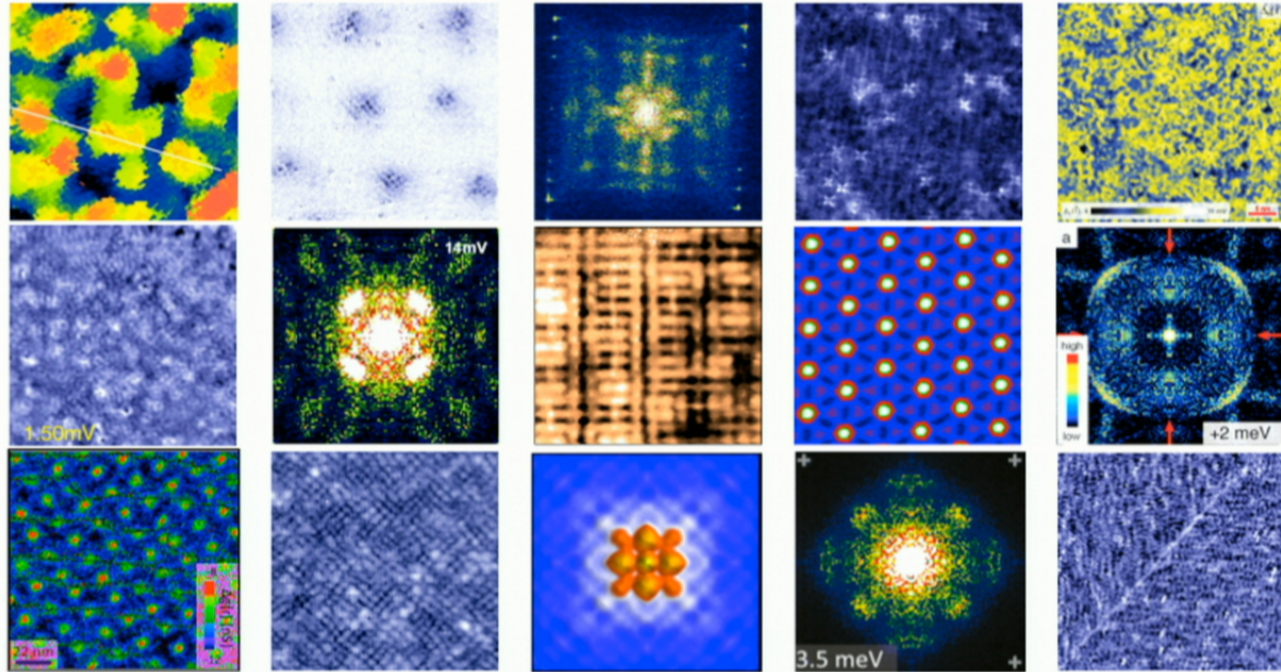
Date: Jan 14, 2015 02:00 PM

URL: <http://pirsa.org/15010080>

Abstract: <p>Everything around us, everything each of us has ever experienced, and virtually everything underpinning our technological society and economy is governed by quantum mechanics. Yet this most fundamental physical theory of nature often feels as if it is a set of somewhat eerie and counterintuitive ideas of no direct relevance to our lives. Why is this? One reason is that we cannot perceive the strangeness (and astonishing beauty) of the quantum mechanical phenomena all around us by using our own senses. I will describe the recent development of techniques that allow us to image electronic quantum matter directly at the atomic scale. As examples, we will visually explore the previously unseen and very beautiful forms of quantum matter making up electronic liquid crystals [1,2]; hybridized heavy-fermions [3,4]; topological-insulator surface states [5]; and high temperature superconductors [6,7]. We will discuss the implications for fundamental research, and also for advanced materials and new technologies, arising from the development and application of these novel techniques .</p>

VISUALIZING QUANTUM MATTER

PERIMETER INSTITUTE COLLOQUIUM / LAZARIDIS / Wednesday Jan. 14, 2015 at 2:00 PM



Cornell University

J.C. Séamus Davis

BROOKHAVEN
NATIONAL LABORATORY

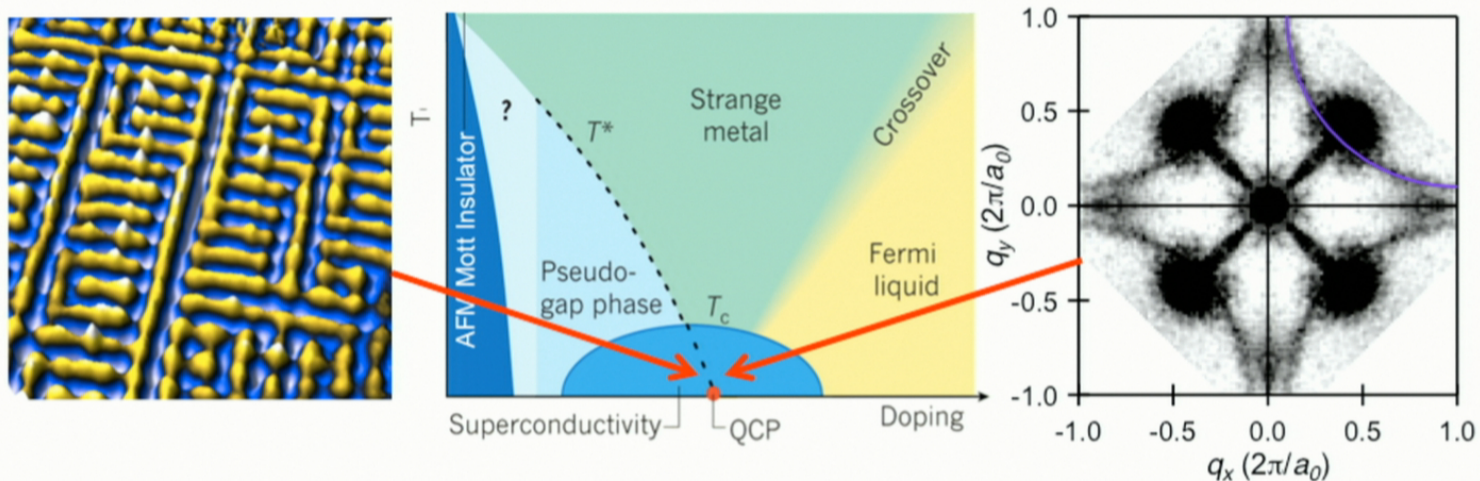


University
of
St Andrews



Atomic-scale Antagonism between d-Symmetry Cooper Pairs and d-Symmetry Density Waves in Underdoped Cuprates

QUANTUM MATTERS SEMINAR / UW PHY 308 / Tuesday Jan. 13, 2015 at 10:30 am



Nature **466**, 374 (2010)

PNAS **111**, E3026 (2014)

Science **344**, 612 (2014)



Cornell University

J.C. Séamus Davis

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NATIONAL LABORATORY

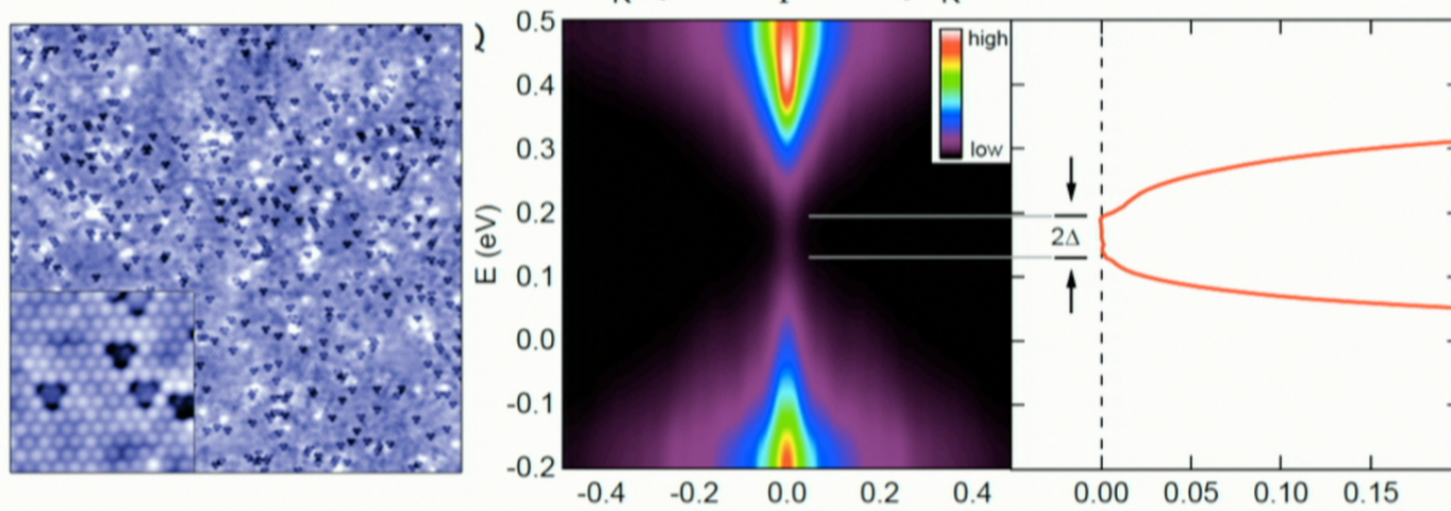


University
of
St Andrews

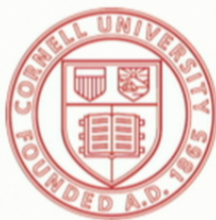


Atomic-scale Imaging of Dirac-Mass Configurations in Ferromagnetic Topological Insulators

PHYSICS COLLOQUIUM / UW-PHY 150 / Thursday Jan. 15, 2015 at 4:00 PM



arXiv 1412.2718 ; *PNAS* 112 (2015)



Cornell University

J.C. Séamus Davis

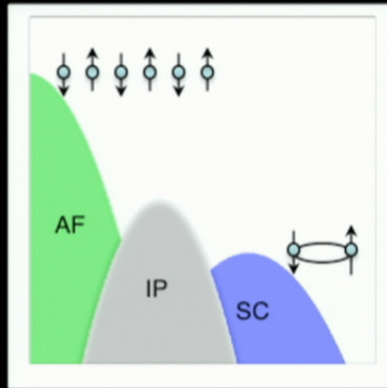
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NATIONAL LABORATORY



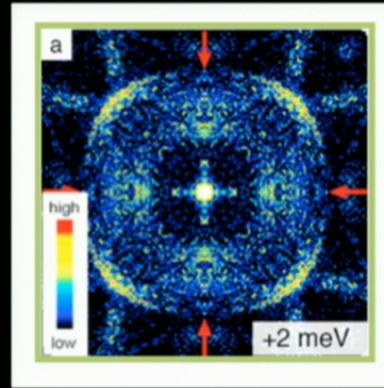
University
of
St Andrews



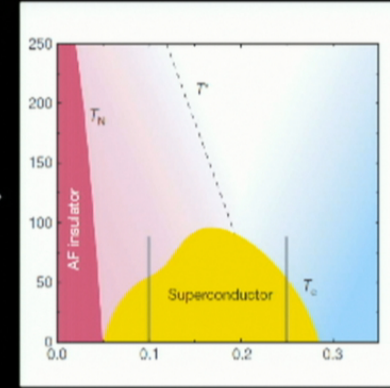
ANTIFERROMAGNETISM
& SUPERCONDUCTIVITY



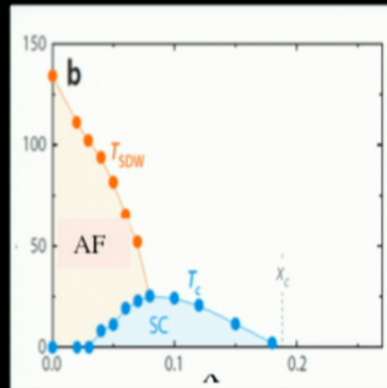
VISUALIZING ELECTRONIC
QUANTUM MATTER



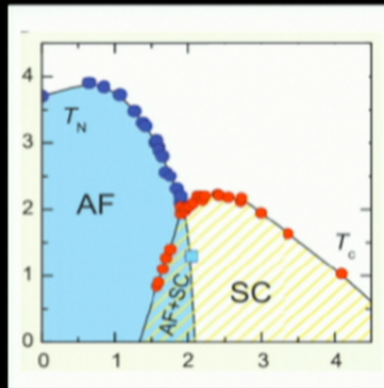
COPPER-BASED
SUPERCONDUCTIVITY
& INTERTWINED PHASES



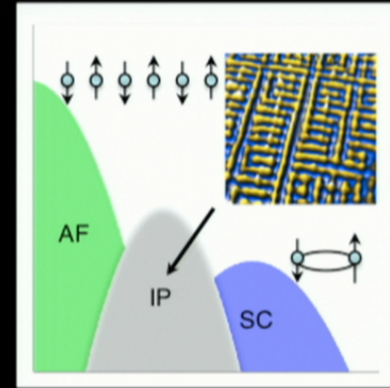
IRON-BASED
SUPERCONDUCTIVITY
& INTERTWINED PHASES



HEAVY-FERMION
SUPERCONDUCTIVITY
& INTERTWINED PHASES



'UNIFIED' MODEL
OF AF INTERACTIONS
INTERTWINED PHASES & HT SC

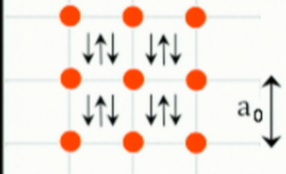
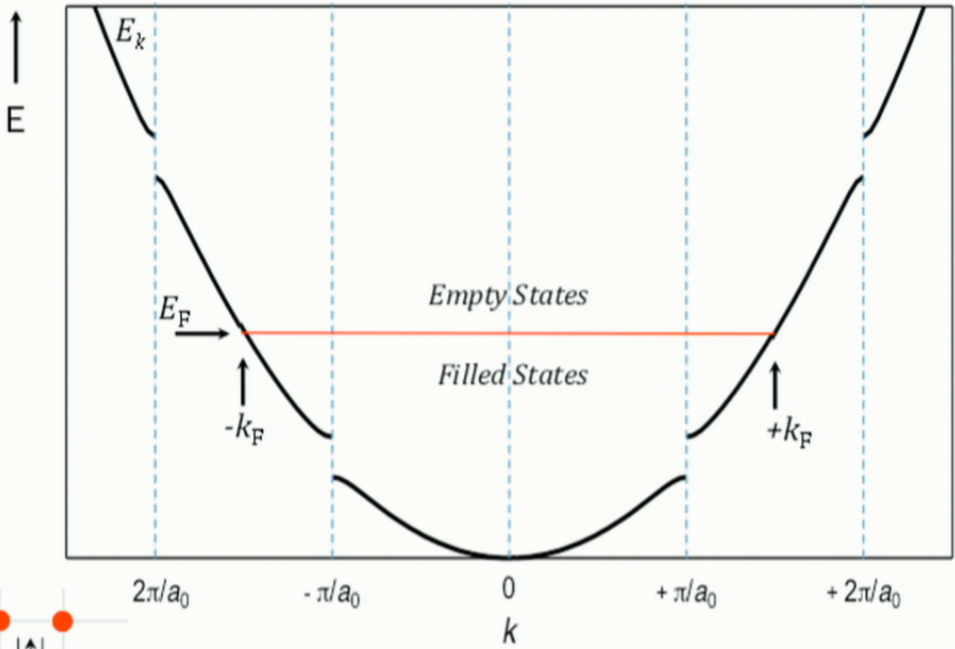


Fermi Energy E_F and Wavevector k_F

Degenerate electron gas

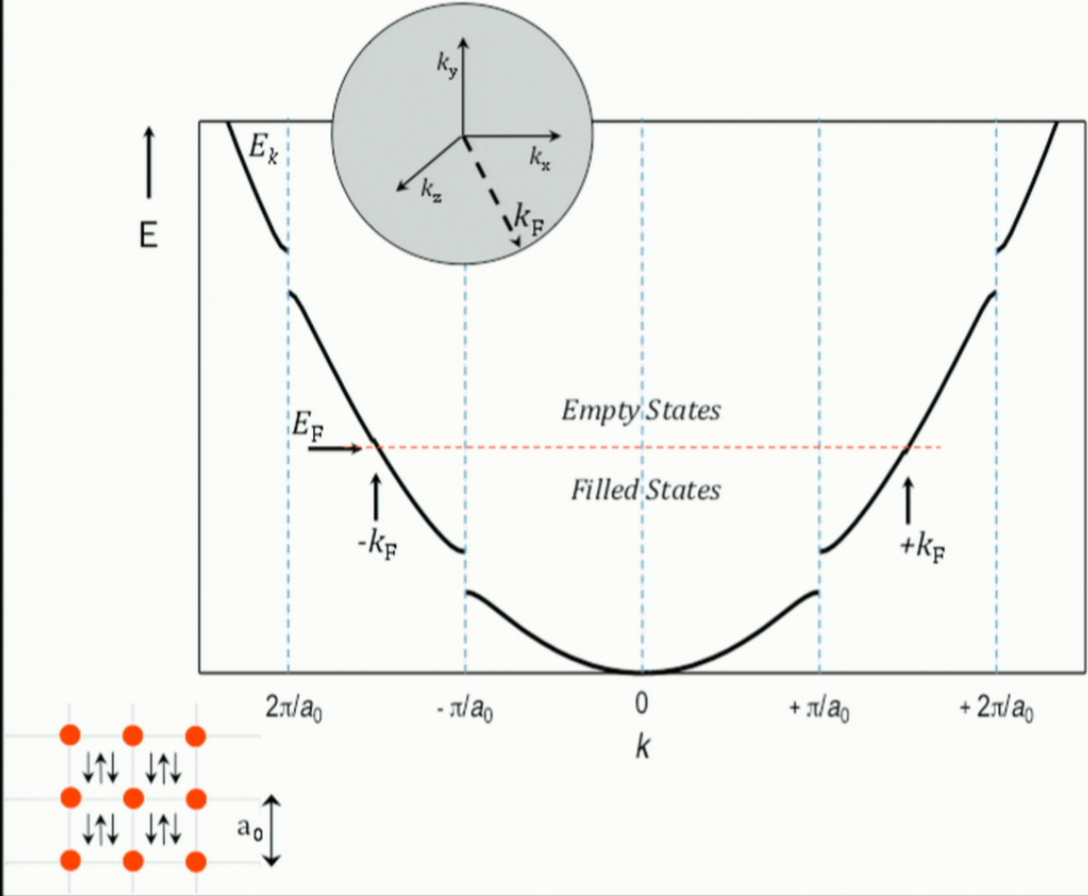


$$2\pi / \lambda \equiv k = p / \hbar$$

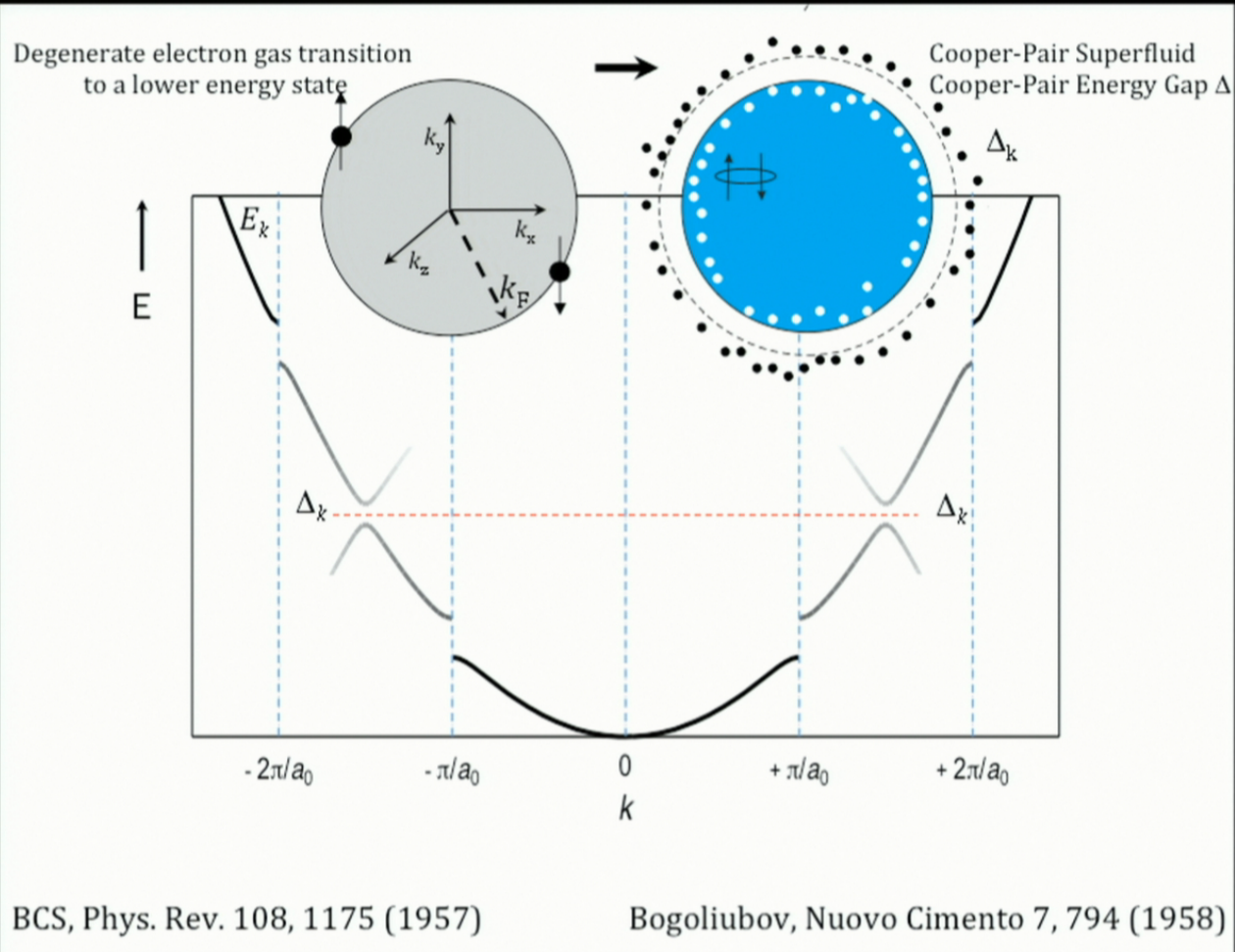


Fermi Energy E_F and Wavevector k_F

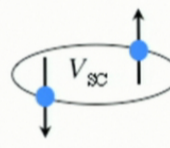
Degenerate electron gas

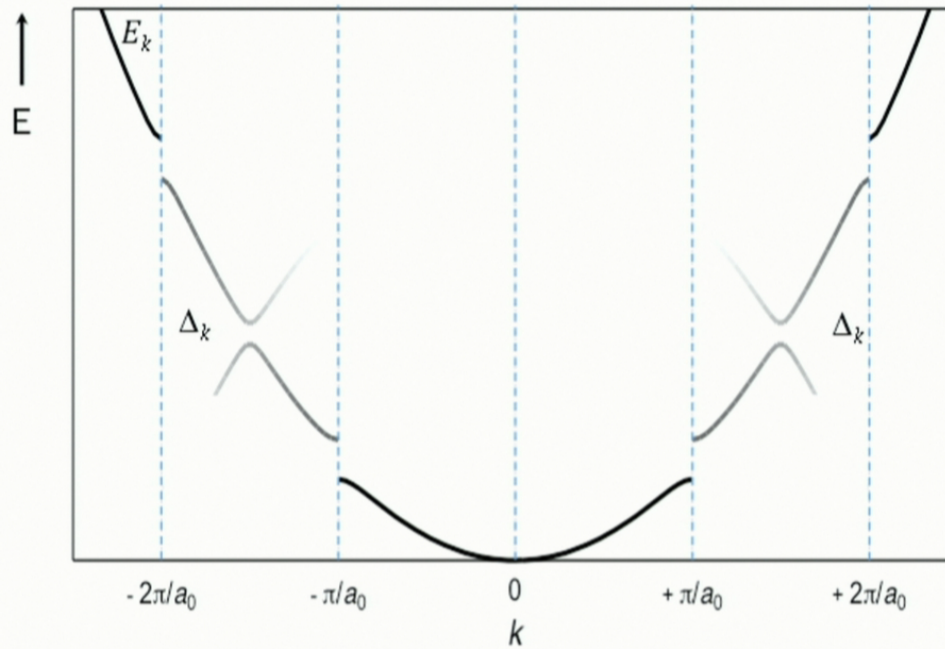


Bosonic Superfluid of Cooper Pairs



SC Energy Gap $\Delta(k) \longleftrightarrow$ Cooper Pairing Mechanism

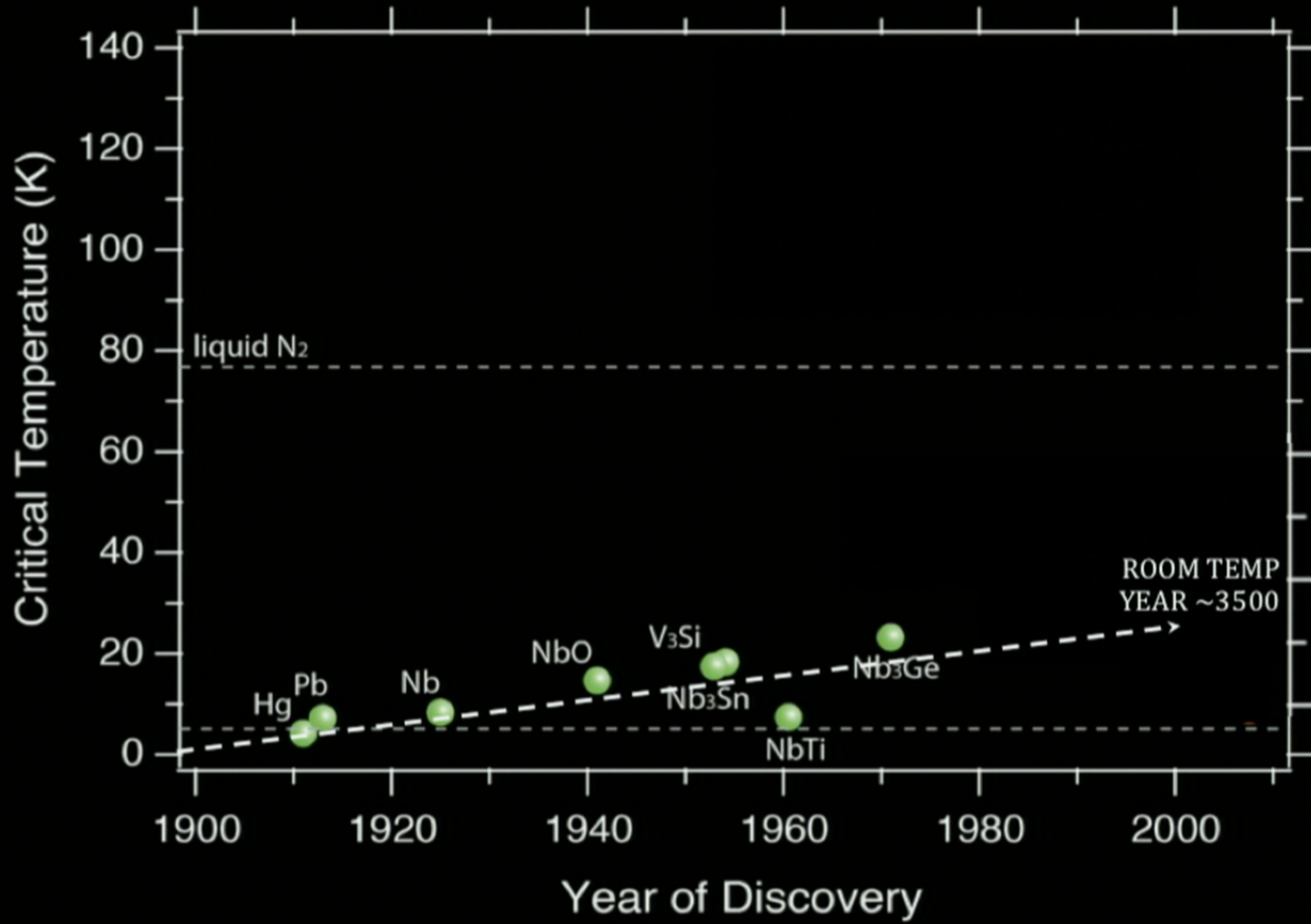
$$\Delta_k = - \sum_p V_{SC}(p-k) \left[\frac{\Delta_p}{2\sqrt{E_p^2 + \Delta_p^2}} \right] \longleftrightarrow \text{Cooper Pair Diagram}$$




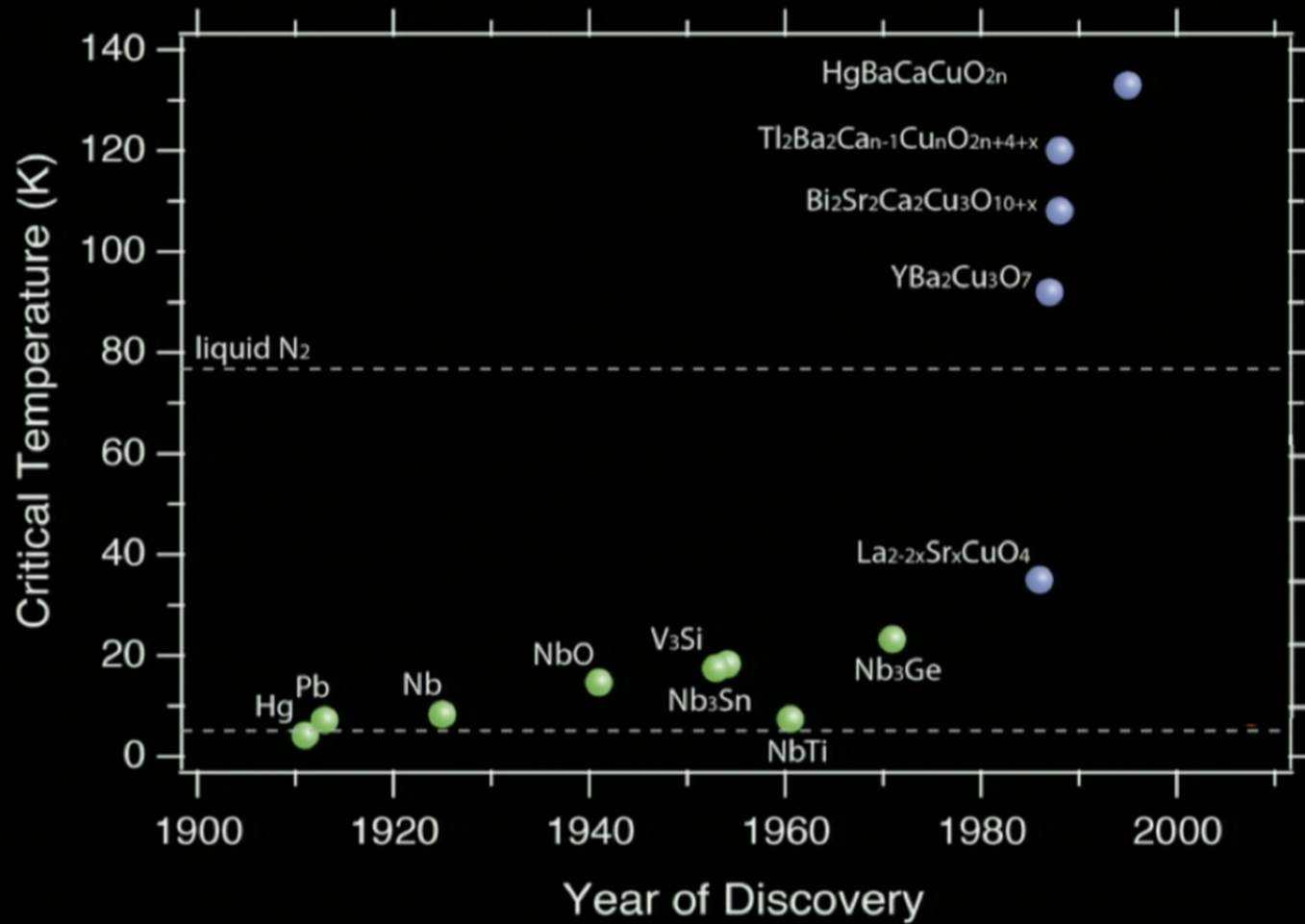
BCS, Phys. Rev. 108, 1175 (1957)

Bogoliubov, Nuovo Cimento 7, 794 (1958)

Conventional Superconductivity



Copper-based High- T_c SC





Power Efficiency/Capacity/Stability



Power Bottlenecks



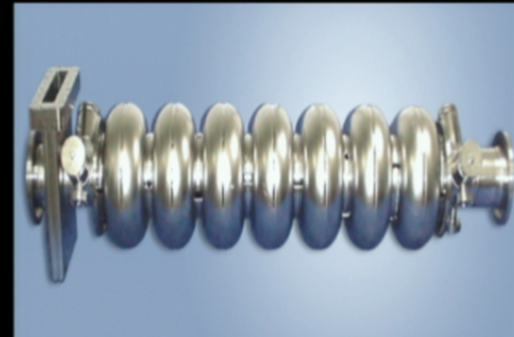
Accommodate Renewable Power



Efficient Rotating Machines



Information Technology



Next Generation HEP



Ultra-High Magnetic Fields



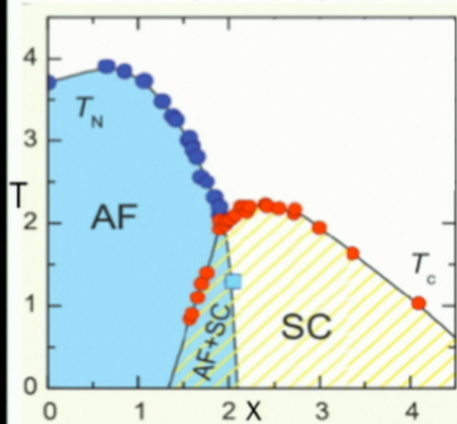
Medical



Transport

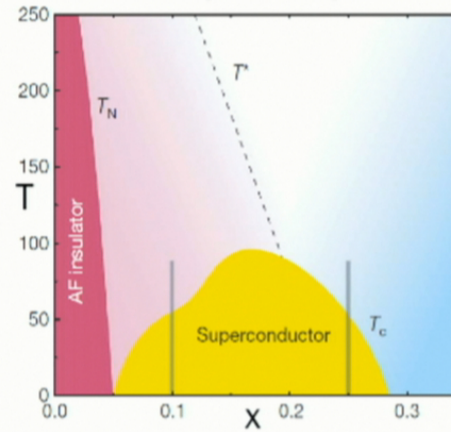
Physics of Unconventional HTS Superconductors

Heavy Fermion
(d-wave)



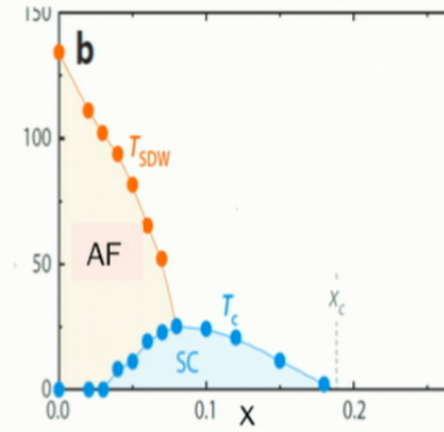
Steglich
PRL **43**, 1892 (1979)

Copper-oxide
(d-wave)



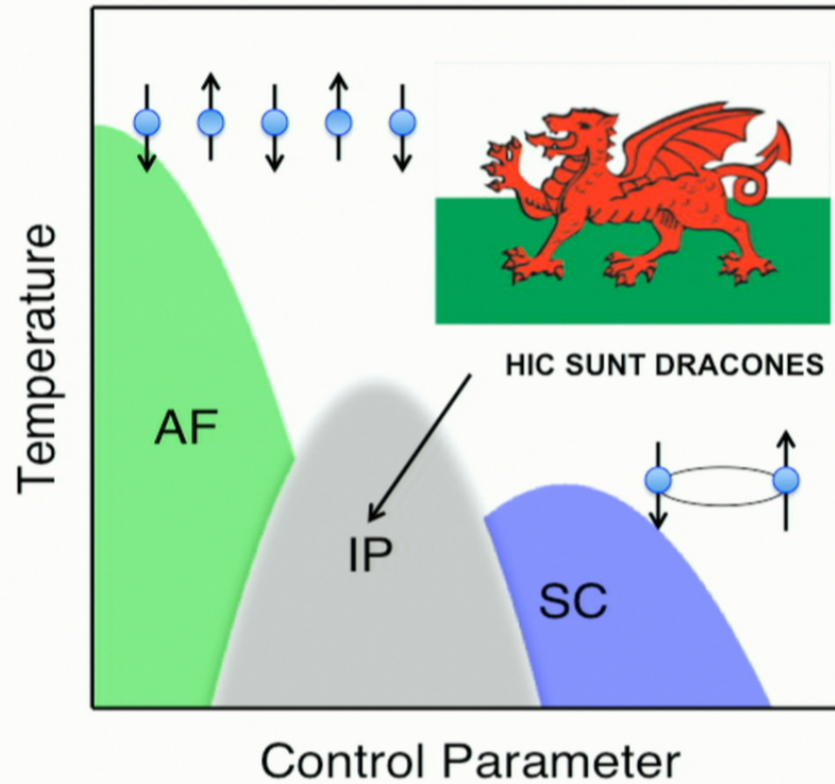
Müller
Z. Physic. **B 64** 189 (1986)

Iron-pnictide
(s_{\pm} -wave?)



Hosono
JACS. **130**, 3296 (2008)

Novel 'Intertwined' Phases of Electronic Matter ?



Gas → Fluid → Liquid Crystal

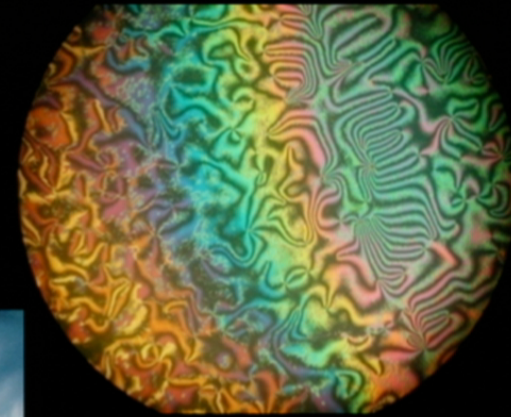
Increasing
interactions
& complexity



Vapour

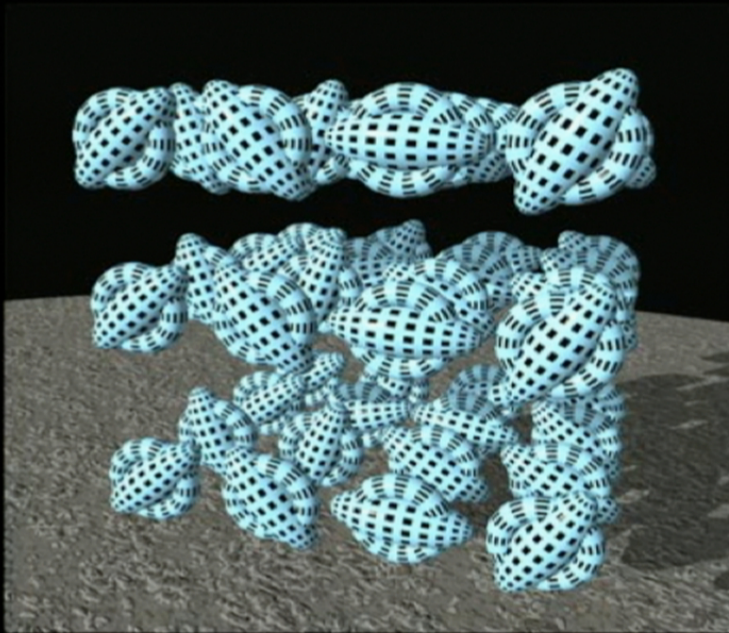


Liquid

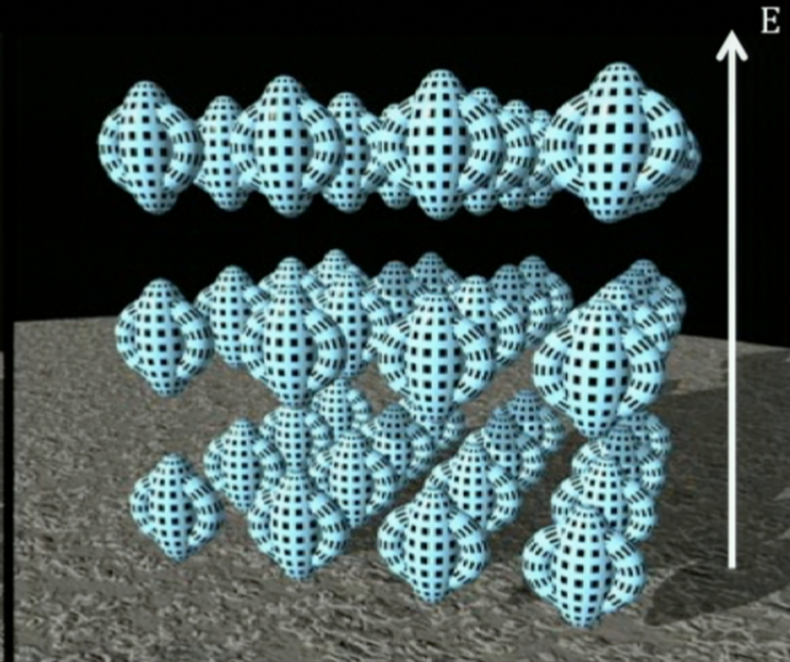


Liquid Crystal

Controllable Liquid Crystal States



Random molecular orientation



Molecules aligned by electric field

Controllable Liquid Crystal States



10¹\$ Industry

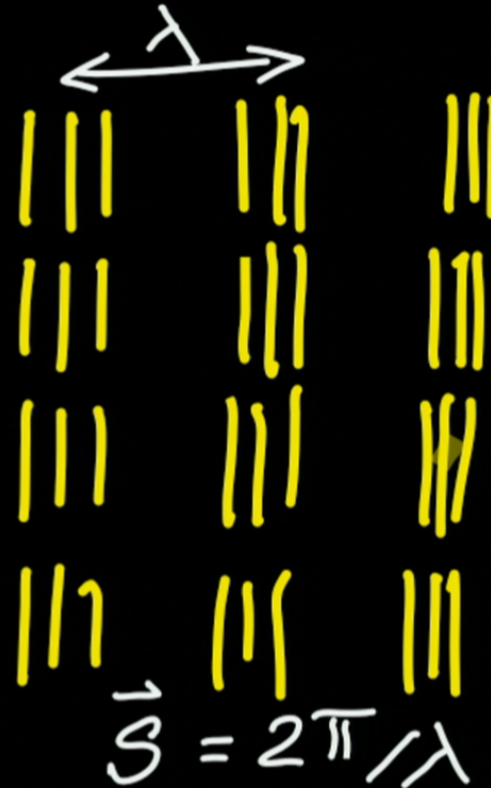
- Monitors
- LCD Displays
- LCD TVs
- 'Smart' Windows
- Much more.....



Two Key Types of Liquid Crystal States

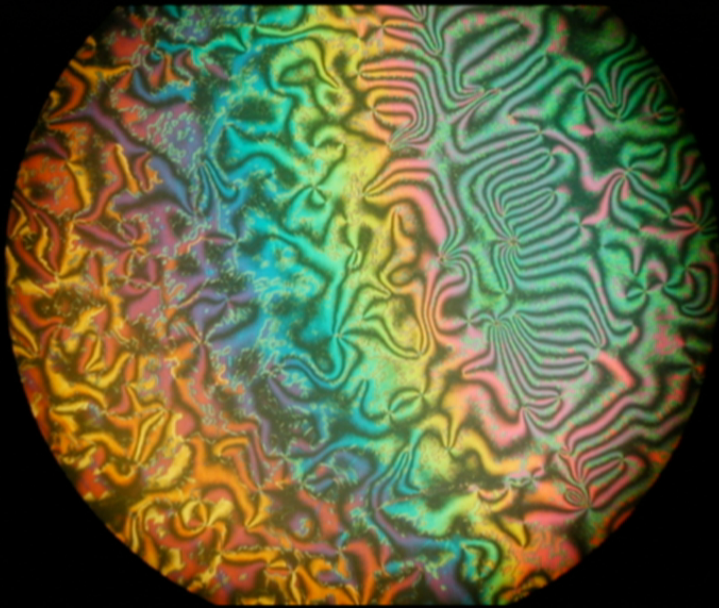


Nematic LC
breaks rotational
symmetry only



Smectic LC
breaks rotational &
translational symmetry

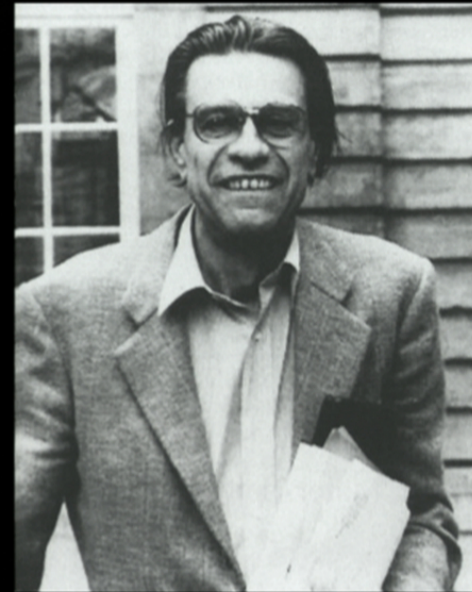
Understanding Liquid Crystals Required Visualization



Visualization



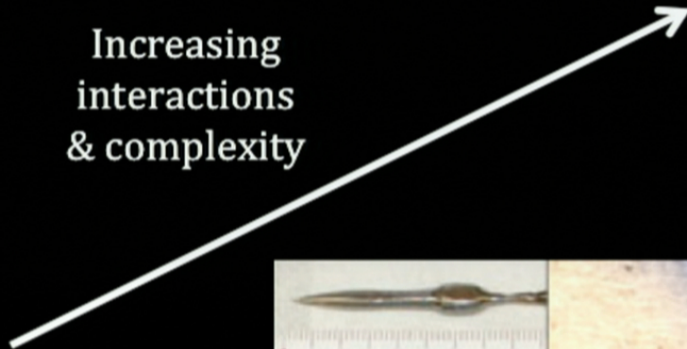
P.-G. de Gennes



Understanding

Electron Gas → Electronic Fluid → Electronic Liquid Crystal

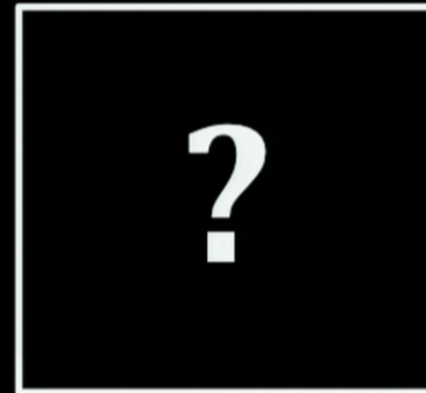
Increasing
interactions
& complexity



Electron Gas



Heavy Electron Fluid



Electronic Liquid Crystal

Electronic liquid-crystal phases of a doped Mott insulator

S. A. Kivelson*, E. Fradkin† & V. J. Emery‡

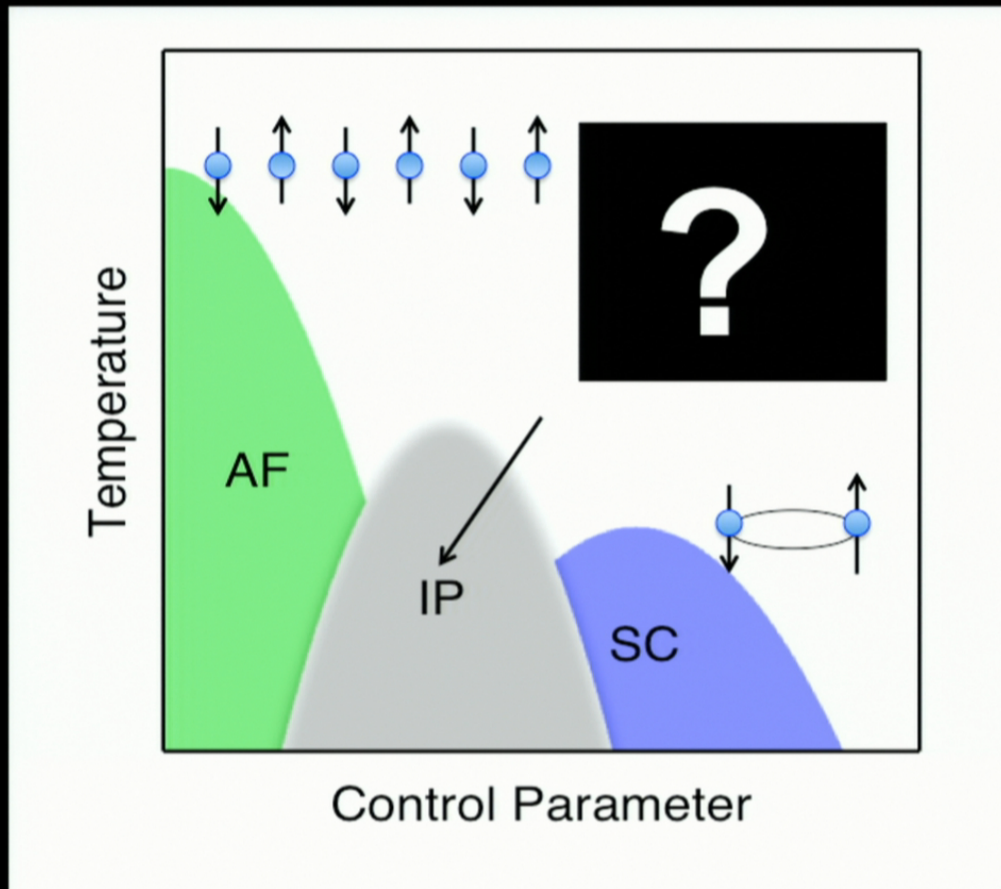
* Department of Physics, University of California Los Angeles, Los Angeles,
California 90095, USA

† Department of Physics, University of Illinois, Urbana, Illinois 61801-3080, USA

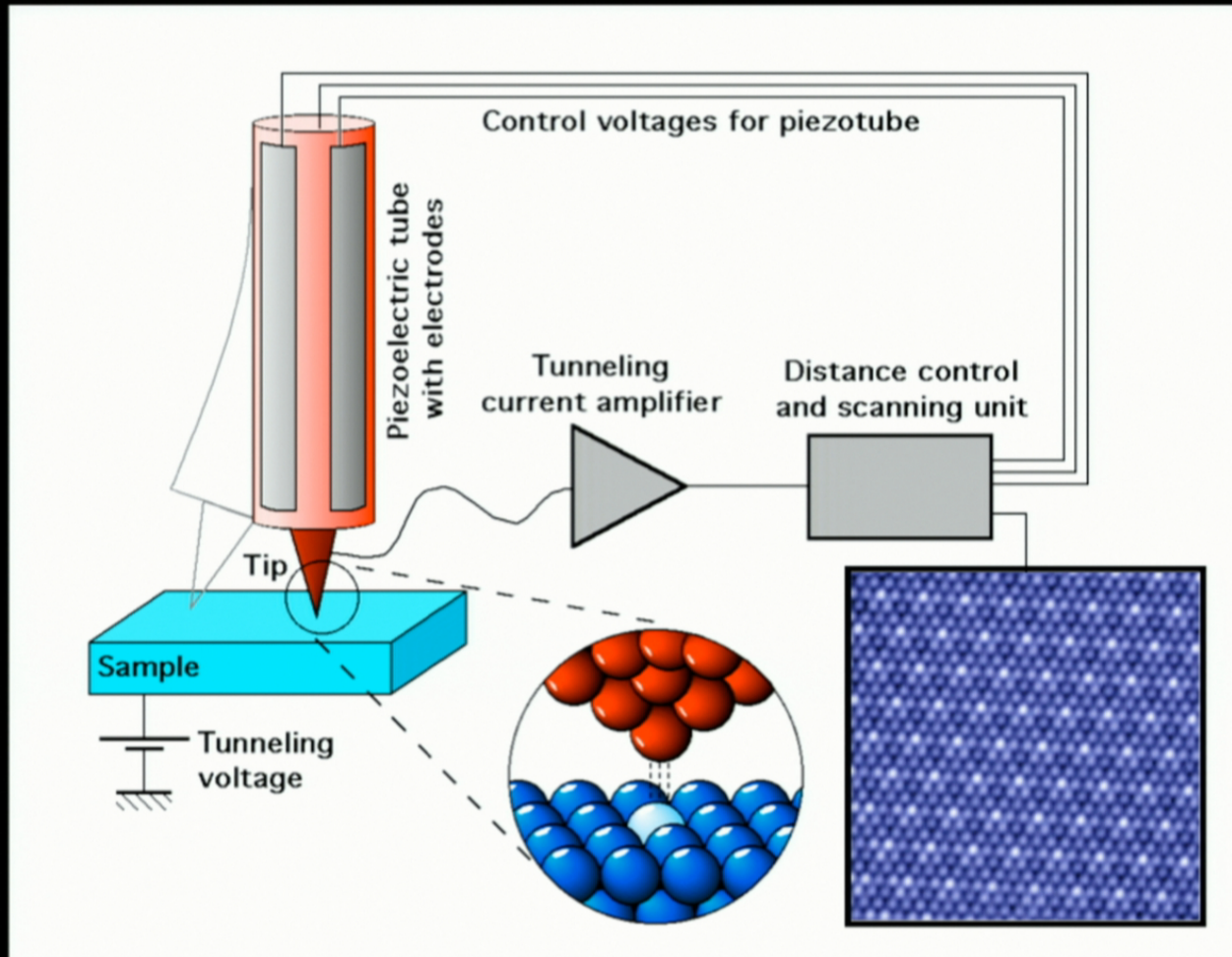
‡ Brookhaven National Laboratory, Upton, New York 11973-5000, USA

Nature 393, 550 (1998).

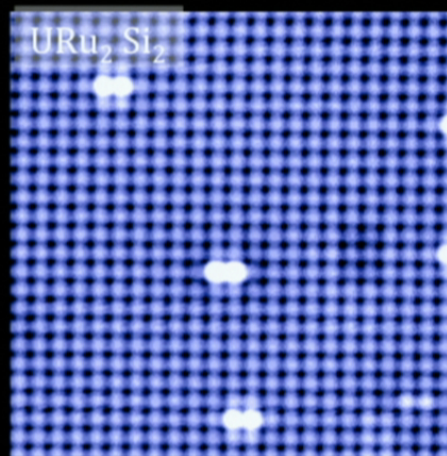
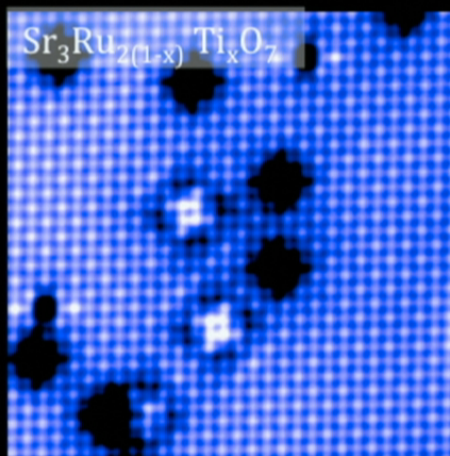
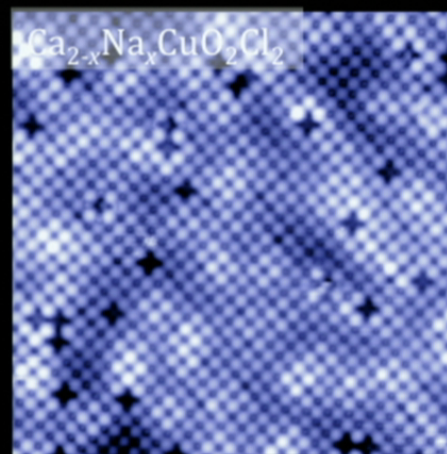
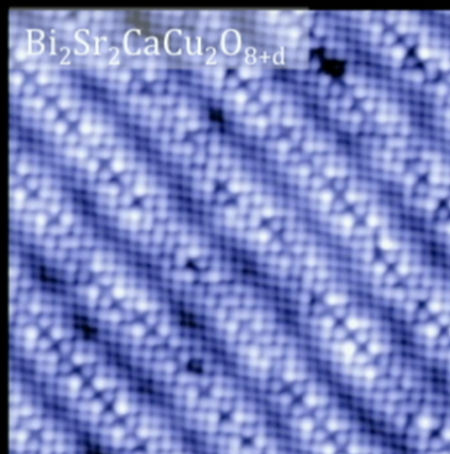
Electronic Liquid Crystals?



Scanning Electron-Tunneling Microscopy (STM)



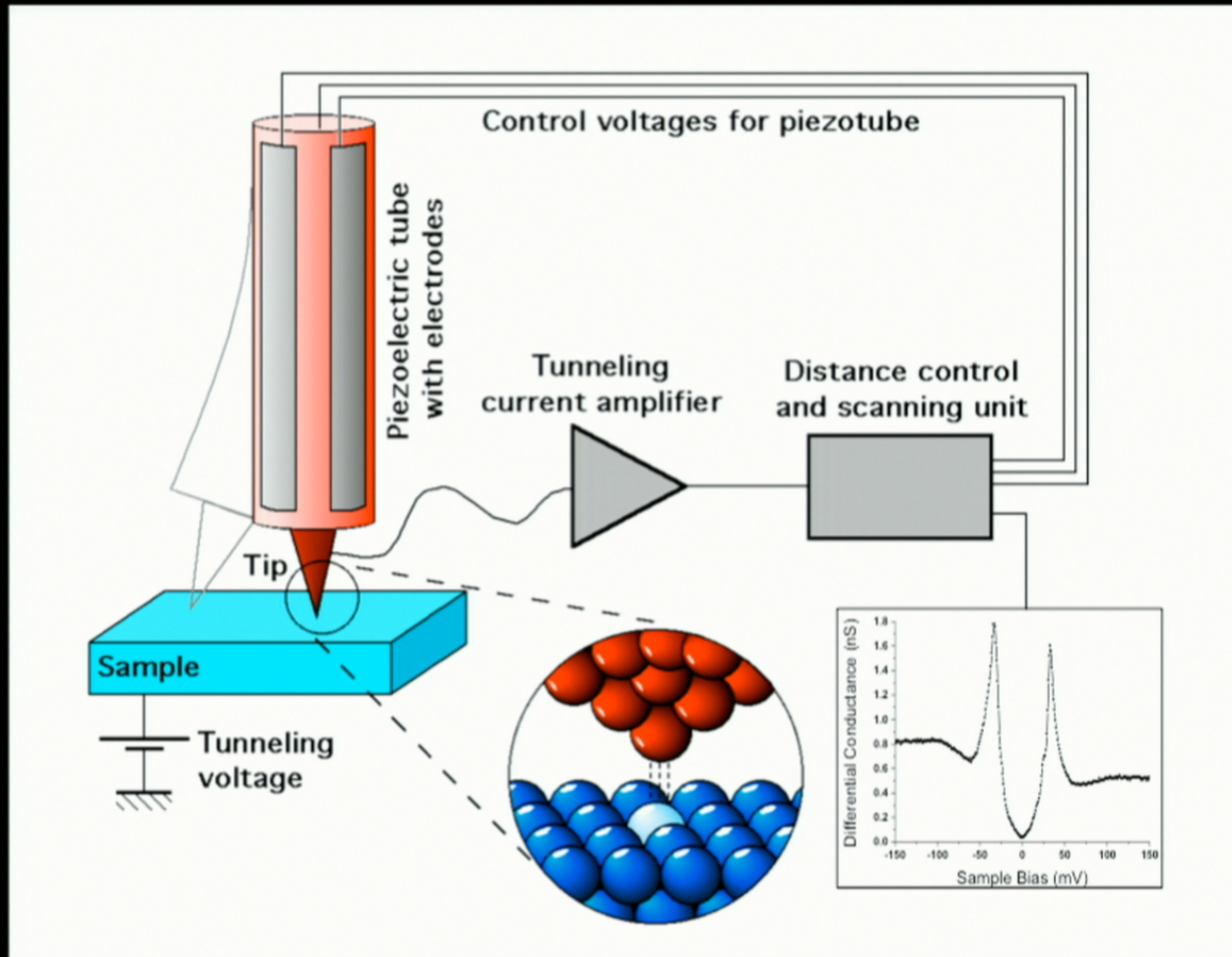
Images Atomic Locations Only



← ~100 Å →

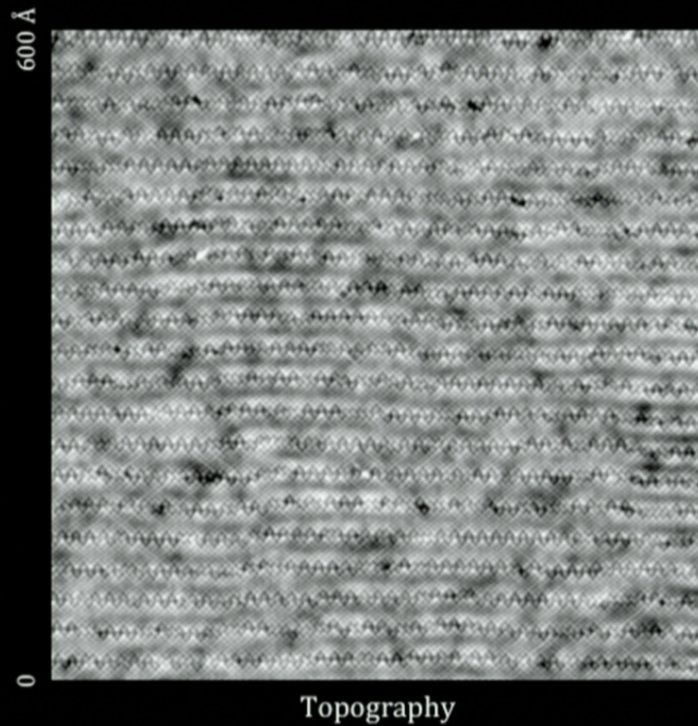
← ~100 Å →

Spectroscopic Imaging STM



Differential conductance $dI/dV @ V$ proportional to $N(E=eV)$

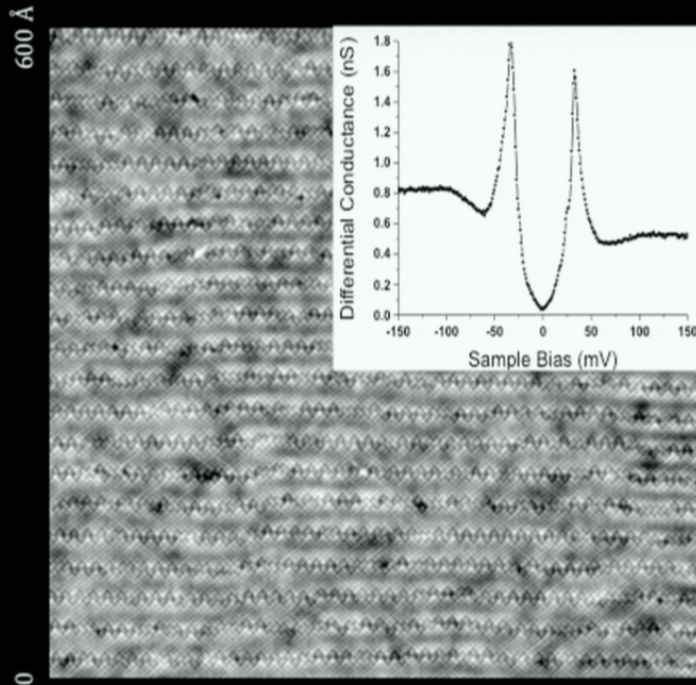
Spectroscopic Imaging STM



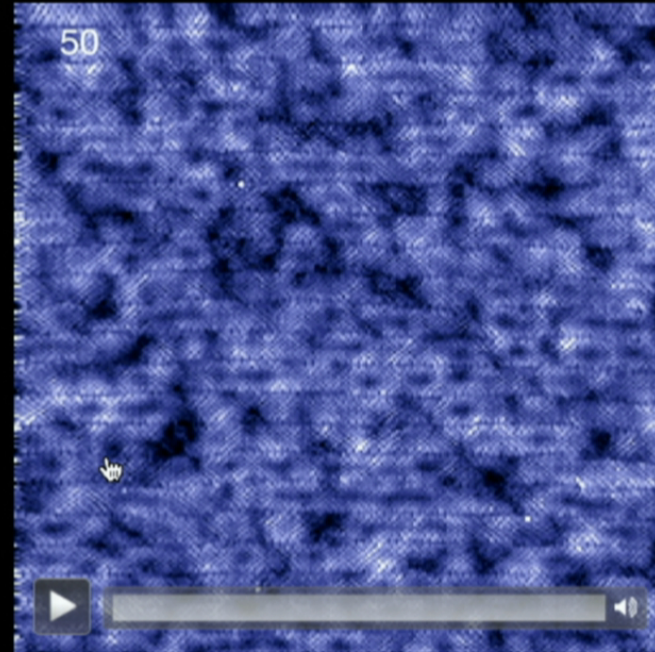
Rev. Sci. Inst. **70**, 1459 (1999).

Spectroscopic Imaging STM

dI/dV spectrum at every atom



Topography



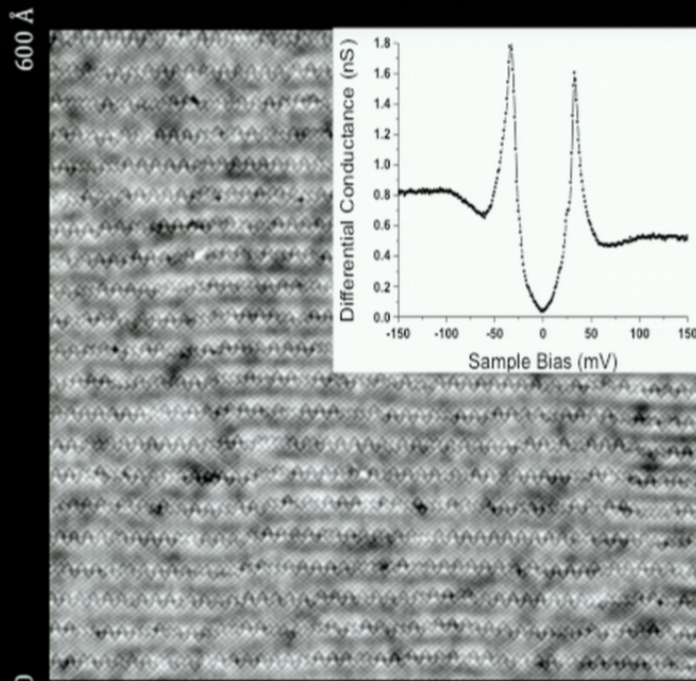
SI-STM



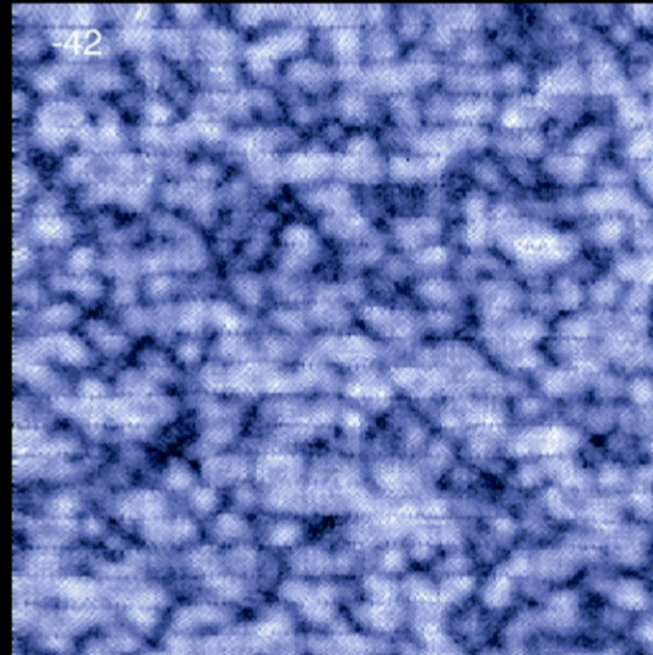
Rev. Sci. Inst. **70**, 1459 (1999).

Spectroscopic Imaging STM

dI/dV spectrum at every atom \rightarrow



Topography



SI-STM

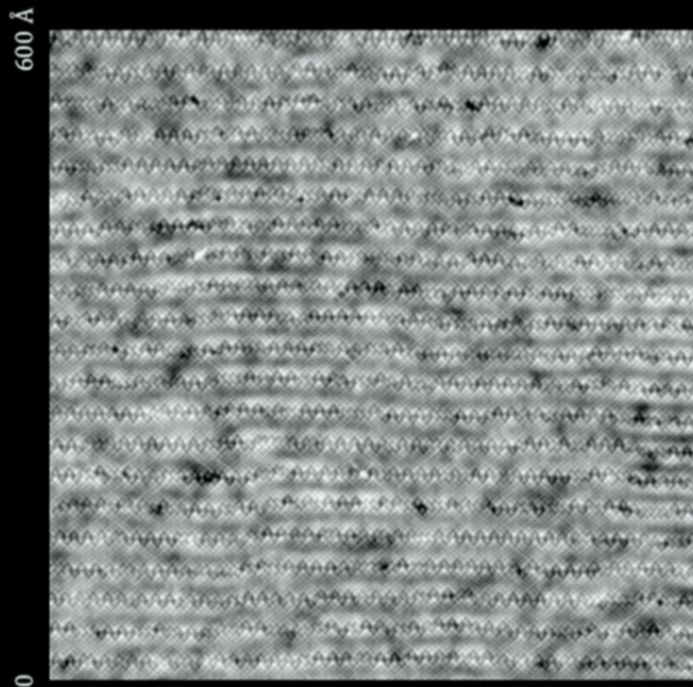
Rev. Sci. Inst. **70**, 1459 (1999).

Spectroscopic Imaging STM

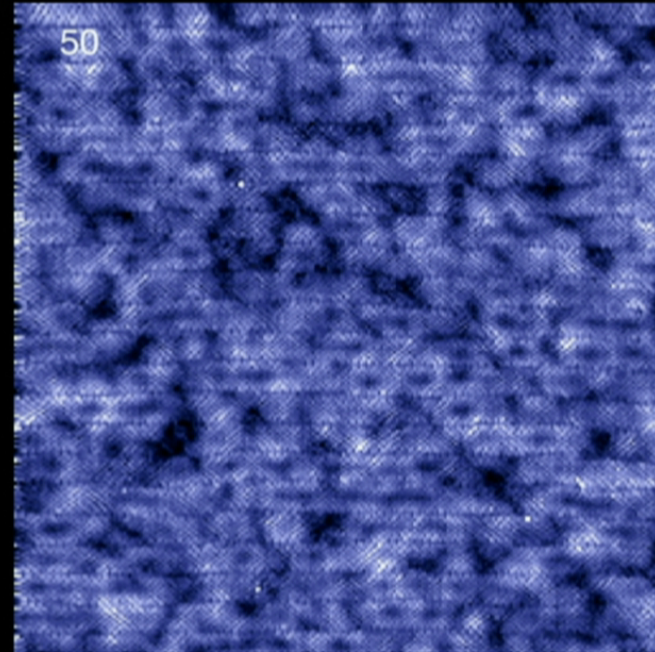
dI/dV spectrum at every atom



Atomic-resolution energy-resolved
 $N(r,E) \sim |\Psi(r,E)|^2$



Topography



SI-STM

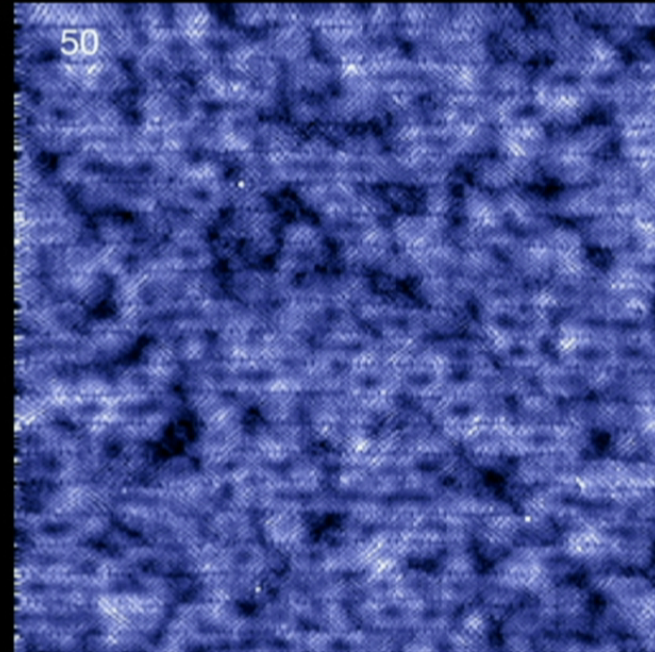
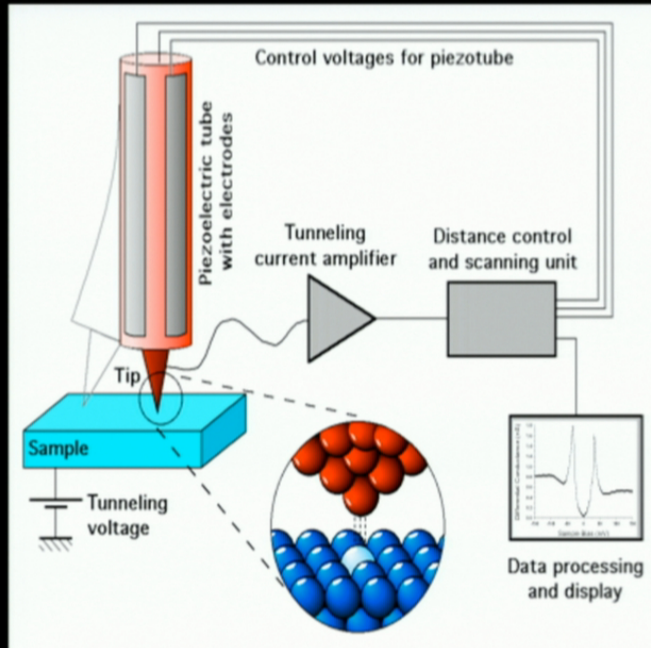
Rev. Sci. Inst. **70**, 1459 (1999).

Technically Challenging!

dI/dV spectrum at every atom



Atomic-resolution energy-resolved
 $N(r,E) \sim |\Psi(r,E)|^2$



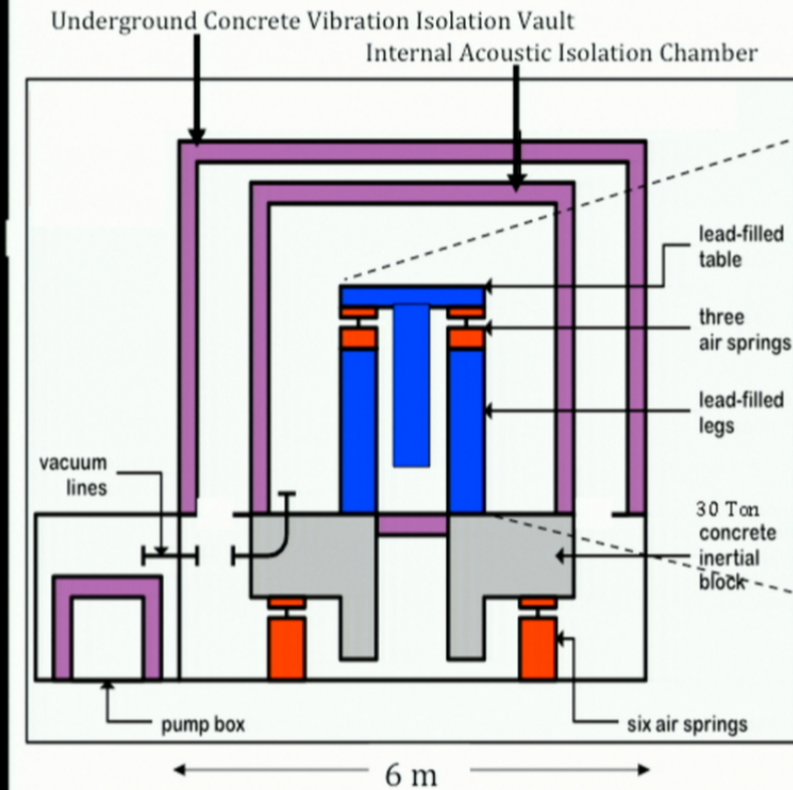
SI-STM

$512 \times 512 \times 200 = 5 \times 10^6$ measurements

Rev. Sci. Inst. **70**, 1459 (1999).

Ultra Low Vibration Cryostat & Laboratory

ULTRA LOW VIBRATION LAB



ULTRA LOW VIBRATION CRYOSTAT



Rev. Sci. Inst. **70**, 1459 (1999).

Ultra Low Vibration Cryostat & Laboratory

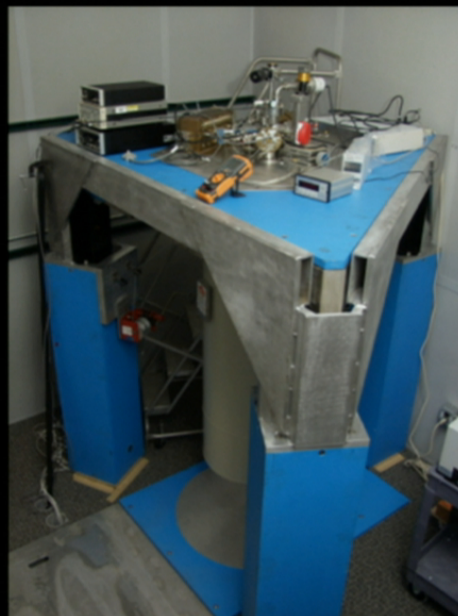


Rev. Sci. Inst. **70**, 1459 (1999).

Davis Group Spectroscopic Imaging STM Systems



STM1 (9T/250mK)
Iron-based HTS



STM3 (1K->100K)
Copper-based HTS



STM2 (9T/10mK)
Heavy Fermion SC

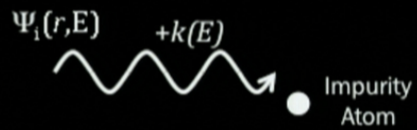
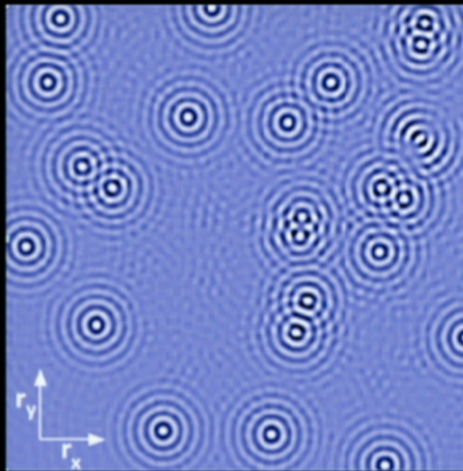
Visiting scientists from UK, Korea, Japan, Taiwan, Canada, Israel, France, Italy, Holland, Portugal, Germany, India, and several US Nat. Labs use our systems.

Rev. Sci. Inst. **70**, 1459 (1999).

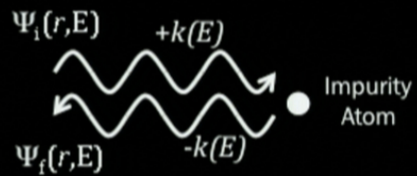
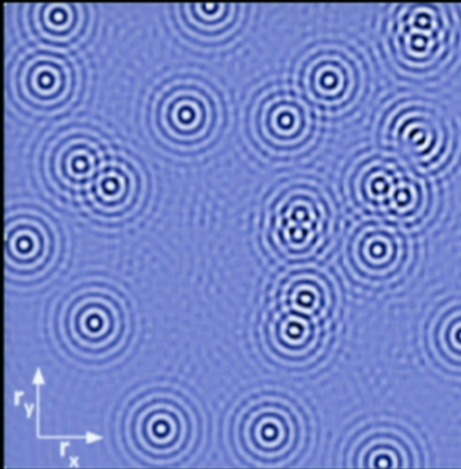
Quasiparticle Scattering Interference (QPI) Imaging



Quasiparticle Scattering Interference (QPI) Imaging

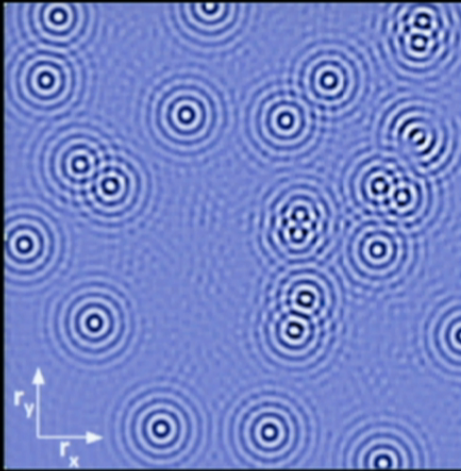


Quasiparticle Scattering Interference (QPI) Imaging

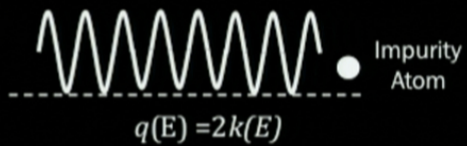


Quasiparticle Scattering Interference (QPI) Imaging

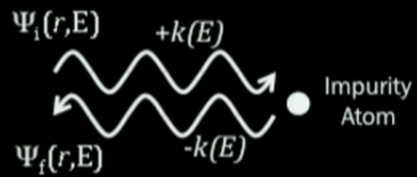
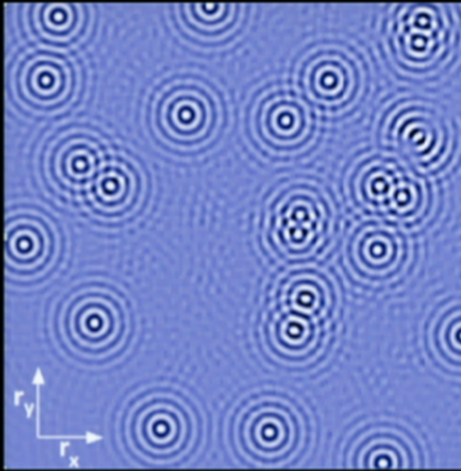
Interference Pattern



$$|\Psi(r,E)|^2$$

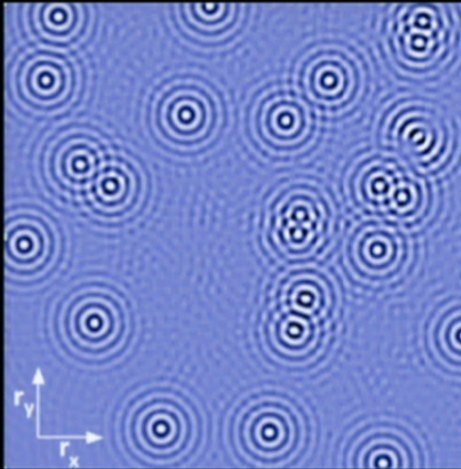


Quasiparticle Scattering Interference (QPI) Imaging

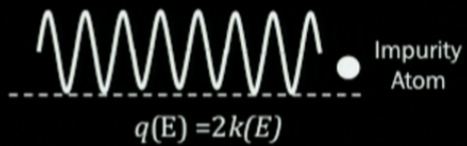


Quasiparticle Scattering Interference (QPI) Imaging

Interference Pattern



$$|\Psi(r,E)|^2$$



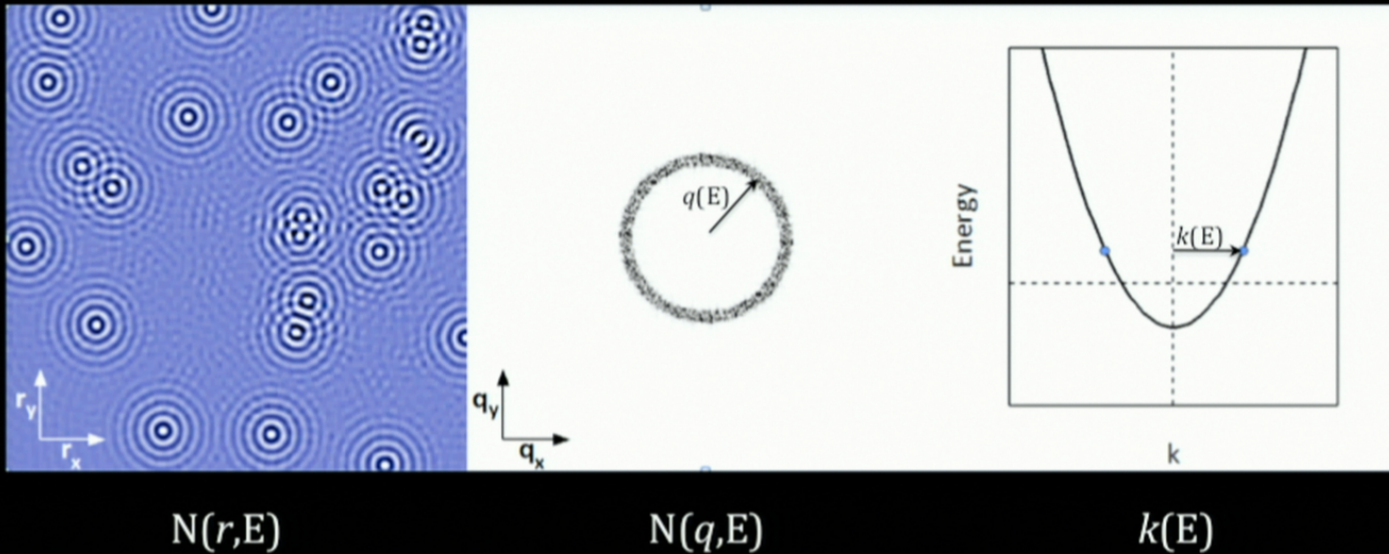
Quasiparticle Scattering Interference (QPI) Imaging

Interference Pattern
 $q(E)=2k(E)$

=>

Maxima $N(q,E)$
 $q(E)=2k(E)$

=> $k(E)=\pm q(E)/2$



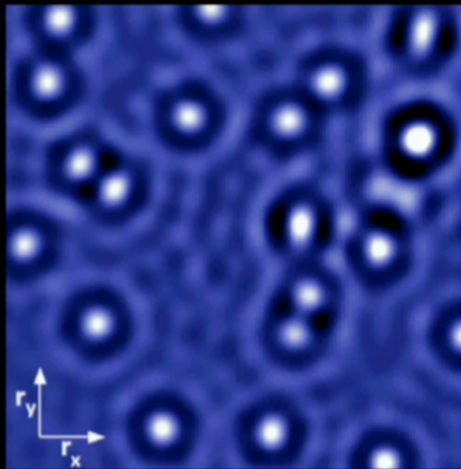
Quasiparticle Scattering Interference (QPI) Imaging

Interference Pattern
 $q(E)=2k(E)$

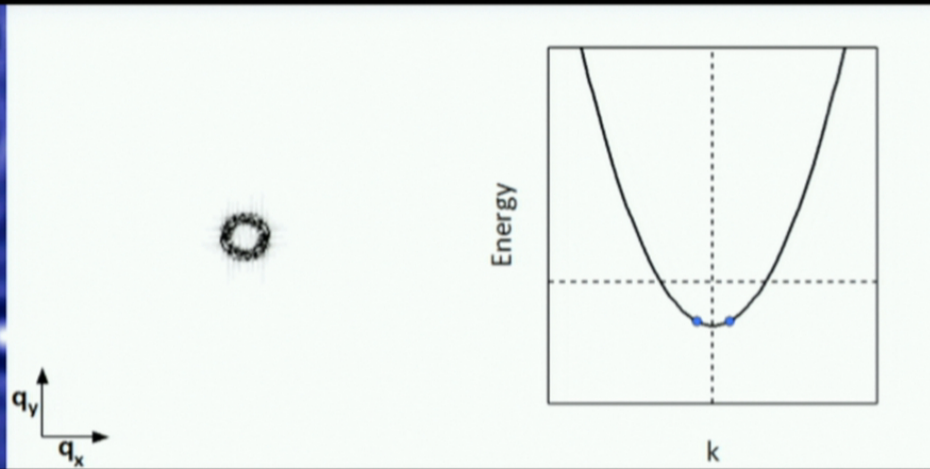
=>

Maxima $N(q,E)$
 $q(E)=2k(E)$

=> $k(E)=\pm q(E)/2$



$N(r,E)$



$N(q,E)$

$k(E)$

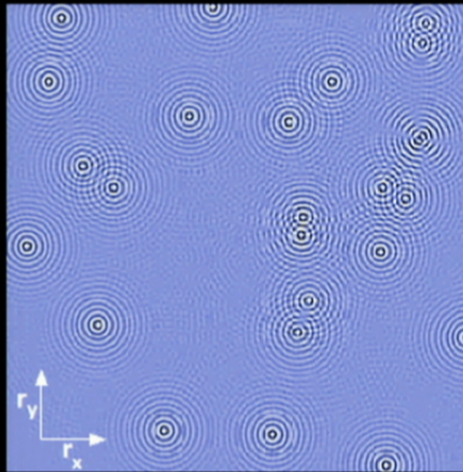
Quasiparticle Scattering Interference (QPI) Imaging

Interference Pattern
 $q(E)=2k(E)$

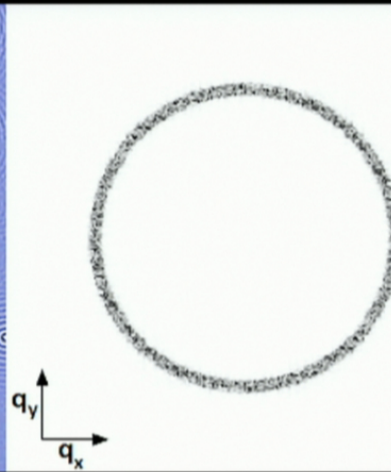
=>

Maxima $N(q,E)$
 $q(E)=2k(E)$

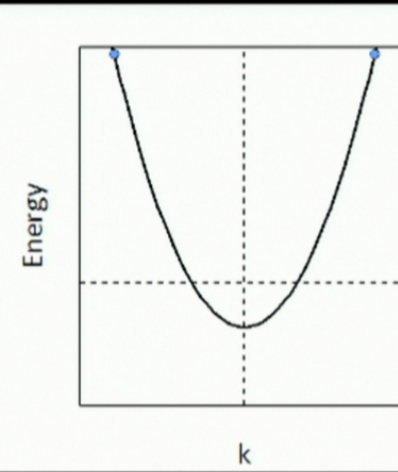
=> $k(E)=\pm q(E)/2$



$N(r,E)$



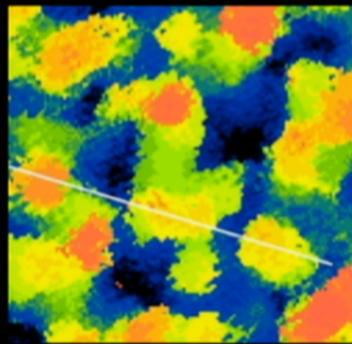
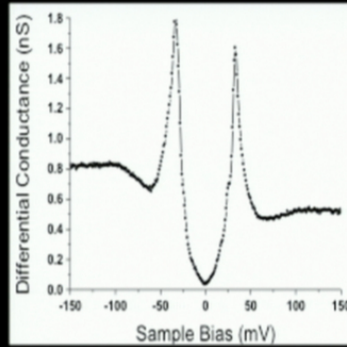
$N(q,E)$



$k(E)$

Direct Visualization of Electronic Quantum Matter

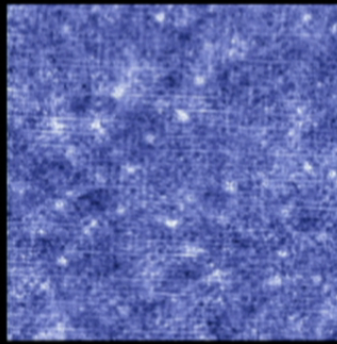
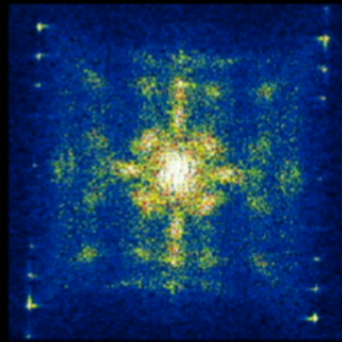
Nanoscale e-disorder



15 nm
Gapmap, B=0

Nature 414 282 (2001)
Nature 415 412 (2002)

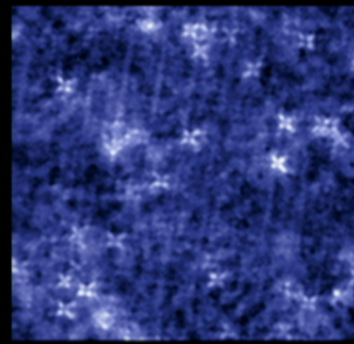
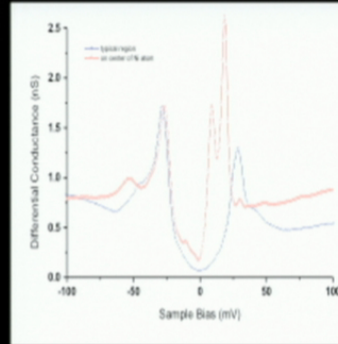
Q. Interference



56 nm
0-12mV LDOS, B=5T

Science 297, 1148 (2002)
Nature 422, 520 (2003)

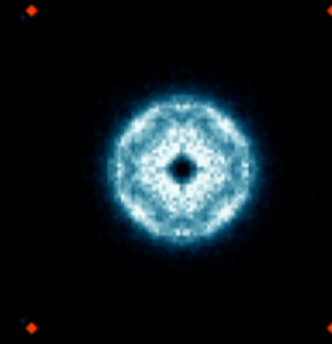
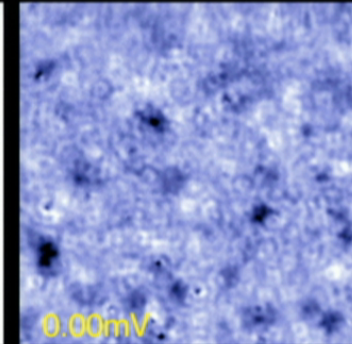
Impurity Atoms



64 nm
12 mV LDOS, B=0

Nature 411, 920 (2001)
Nature 403, 746 (2000)

Heavy Fermion SC

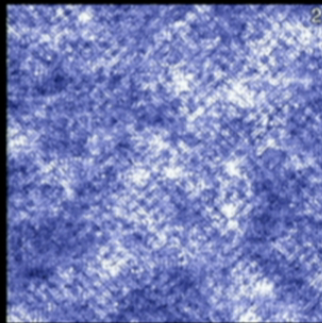
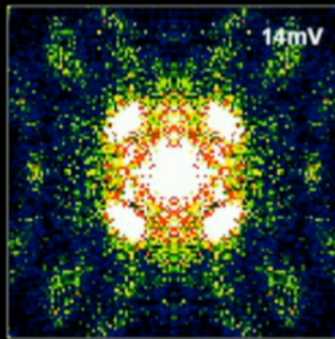


26 nm
250 mV

Nature 465, 570 (2010)
Nat. Phys. 9, 458 (2013)

Direct Visualization of Electronic Quantum Matter

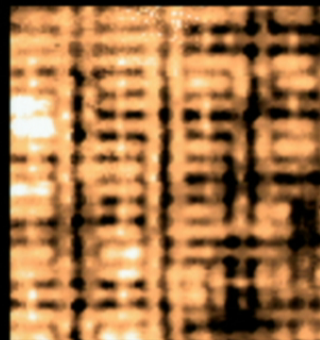
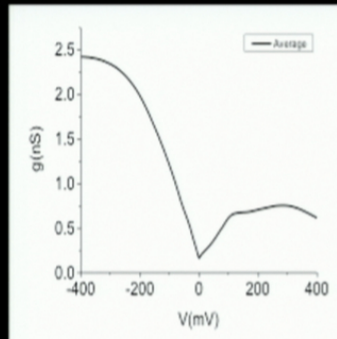
Phase Fluctuations



45 nm
dI/dV

Science 325, 1099 (2009)
Science 296 455 (2002)

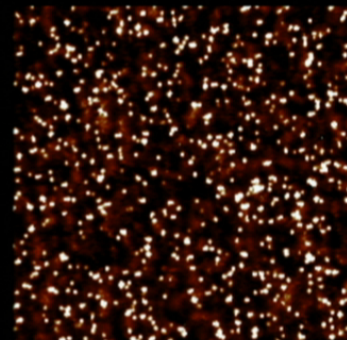
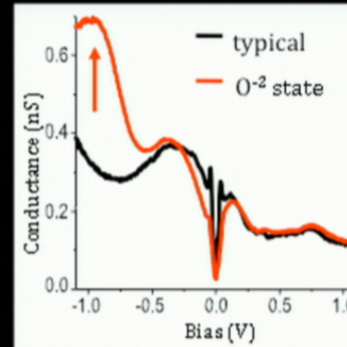
Exotic Density Waves



6.4 nm
R=I+/I-

Science 315, 1380 (2007)
Science, 333, 426 (2011)

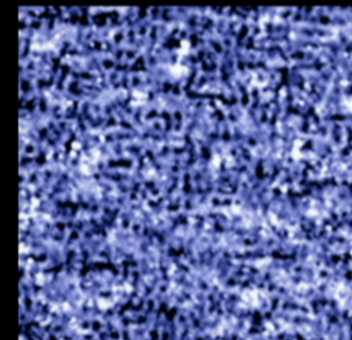
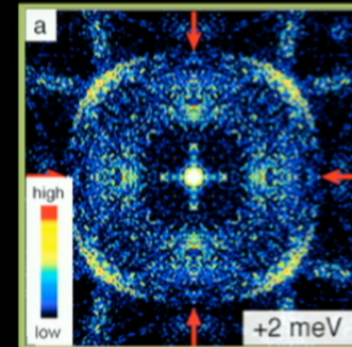
Dopant Atoms



40nm
-1V LDOS, B=0

Science 309, 1048 (2005)
Nature 442, 546 (2006)

FeAs Intertwined Phases



26 nm
-9mV LDOS, B=0

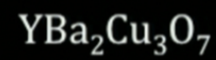
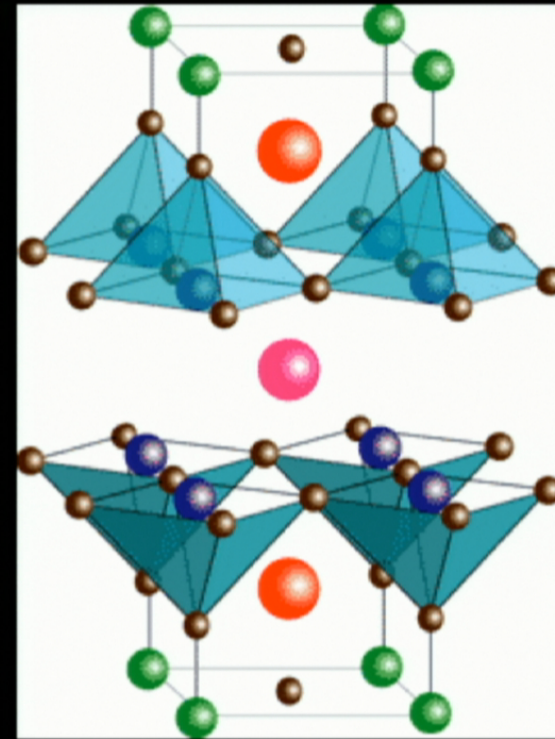
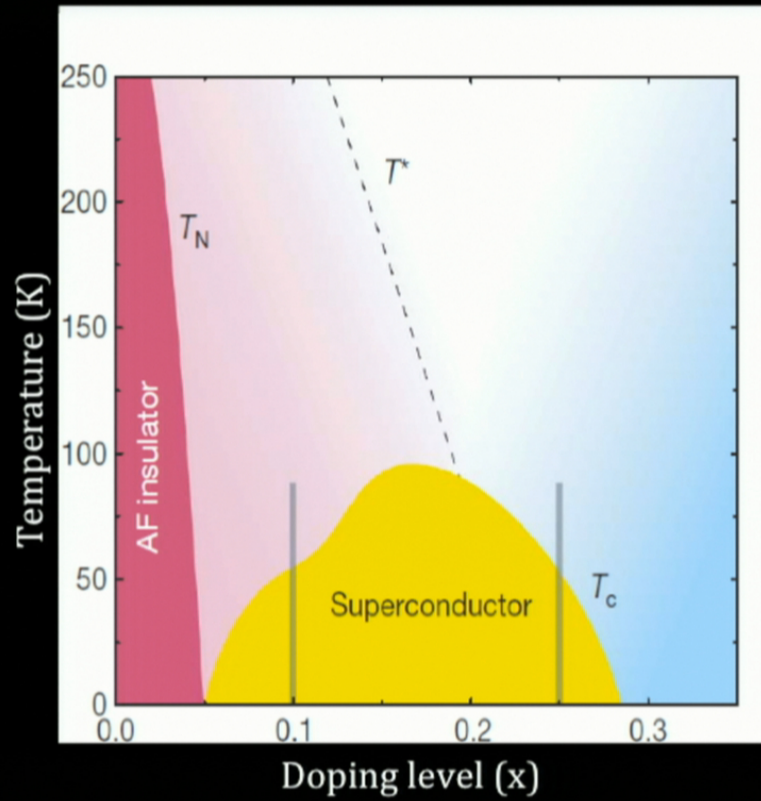
Science 327, 181 (2010)
Science 336, 563 (2012)

Ultra Low Vibration Cryostat & Laboratory

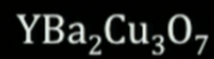
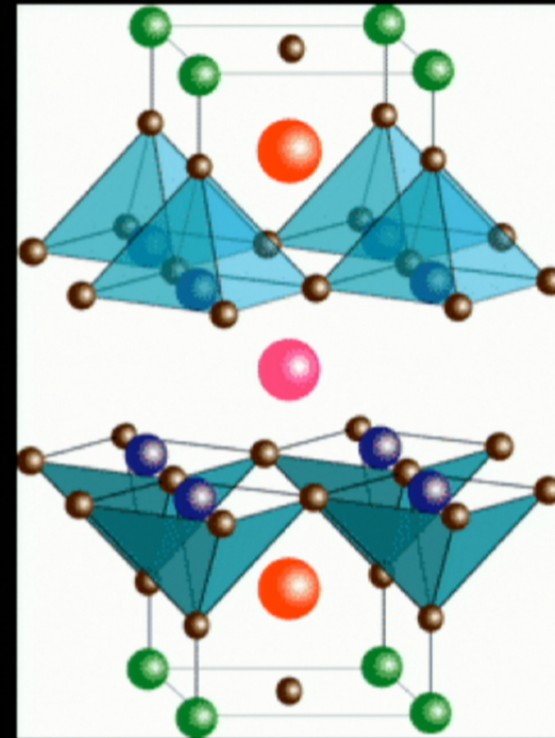
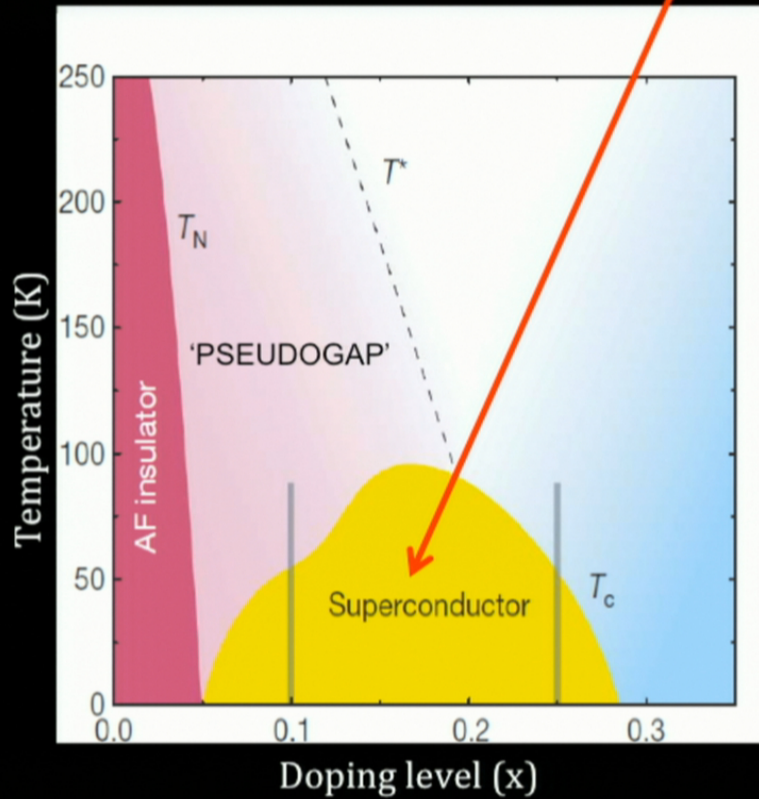


Institute for Quantum Computing , U. of Waterloo (2015)

Typical CuO_2 Phase Diagram

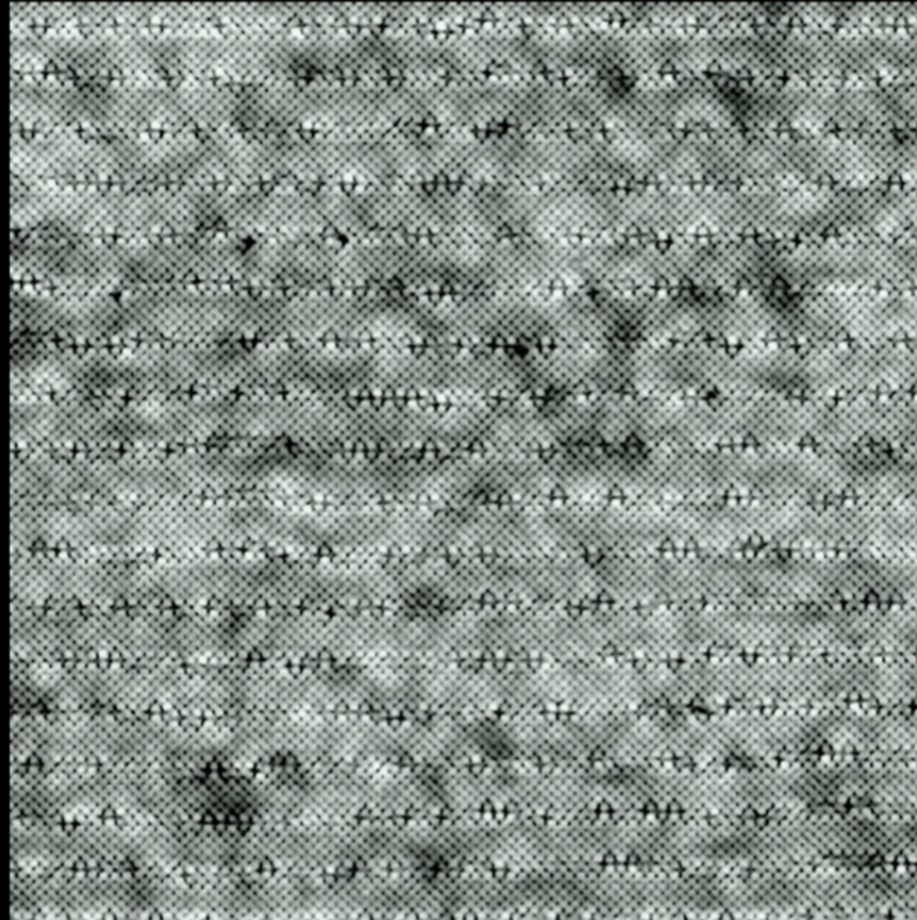


Mechanism of High-Tc Superconductivity?



Topograph

$T(r)$



45 nm

Nature **466**, 374 (2010)

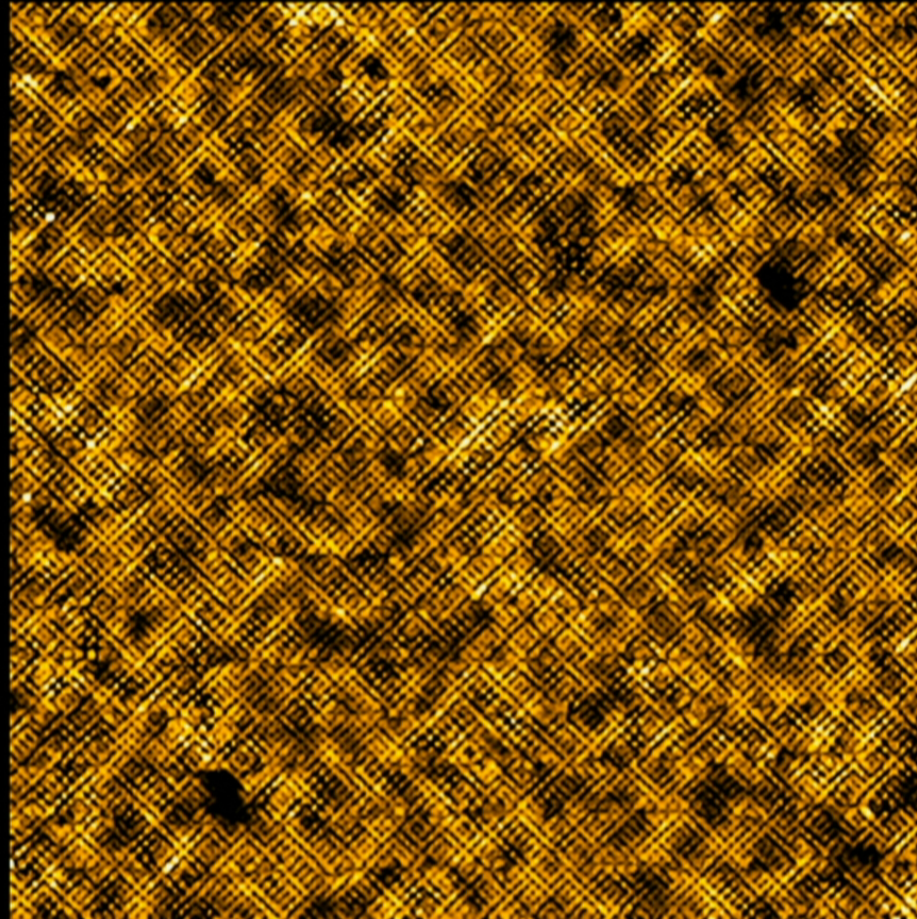
Science **333**, 4526 (2011)

Science **344**, 612 (2014)

'Pseudogap' Electronic Structure

$R(r)$

$p \sim 10\%$



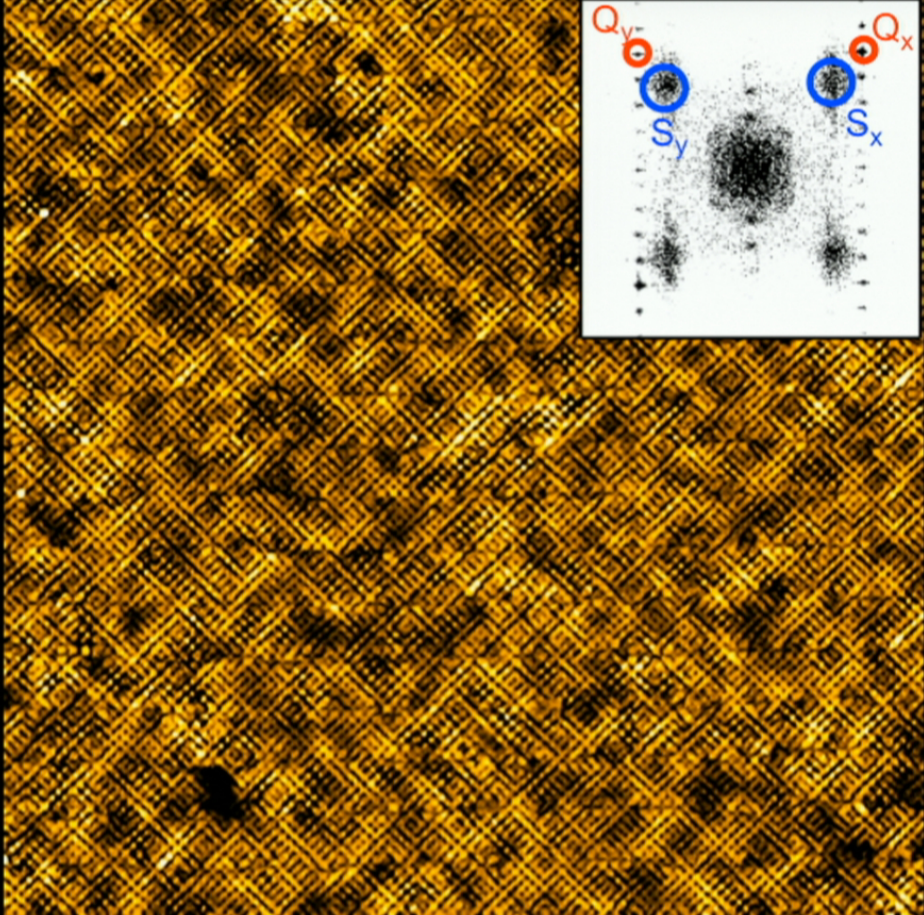
45 nm

Nature **466**, 374 (2010)

Science **333**, 4526 (2011)

Science **344**, 612 (2014)

Incommensurate Density Wave

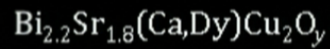
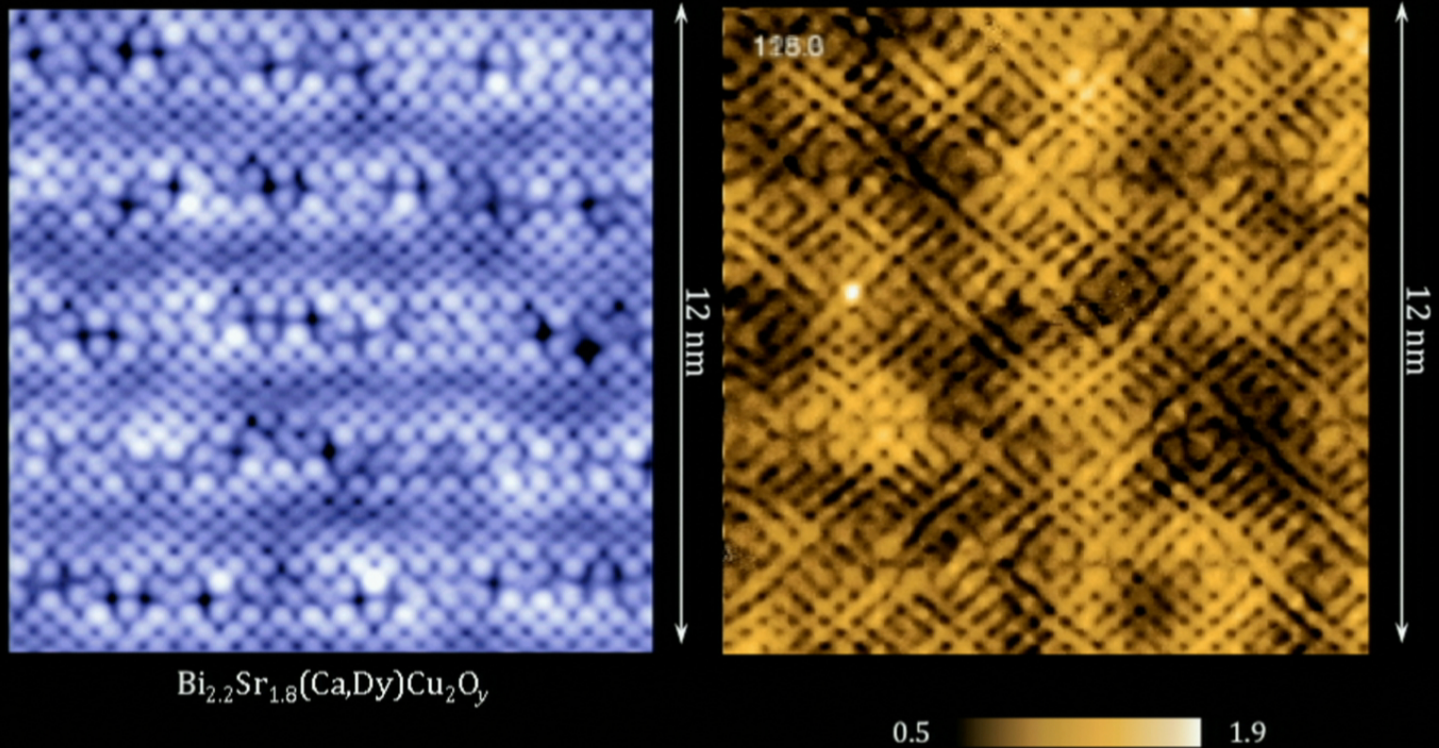


Nature 466, 374 (2010)

Science 333, 4526 (2011)

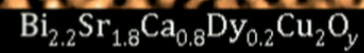
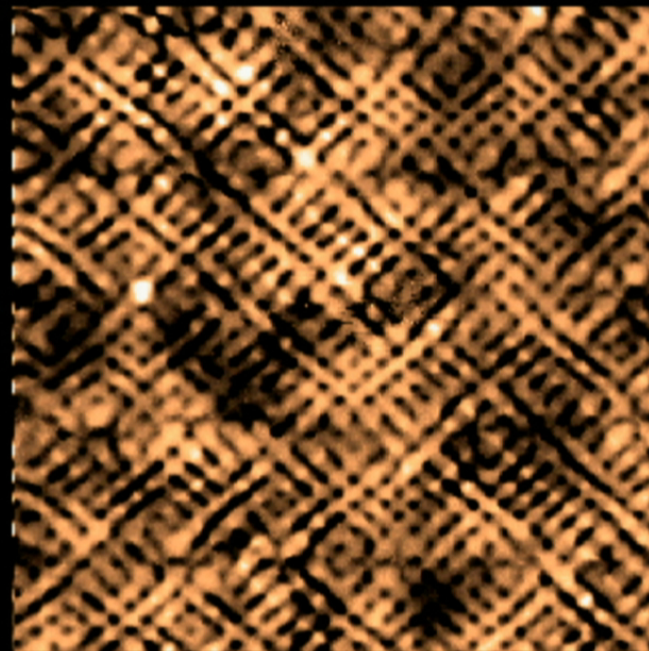
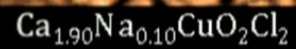
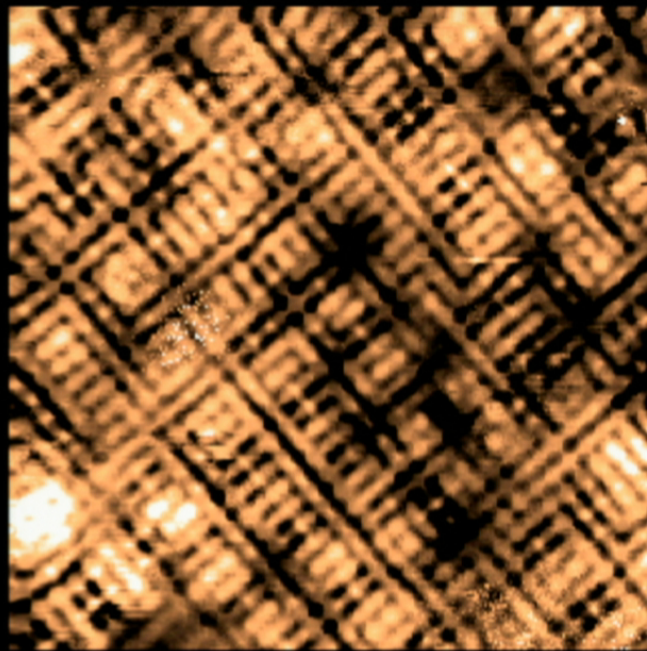
Science 344, 612 (2014)

High-resolution Imaging Cuprate Broken-Symmetry States



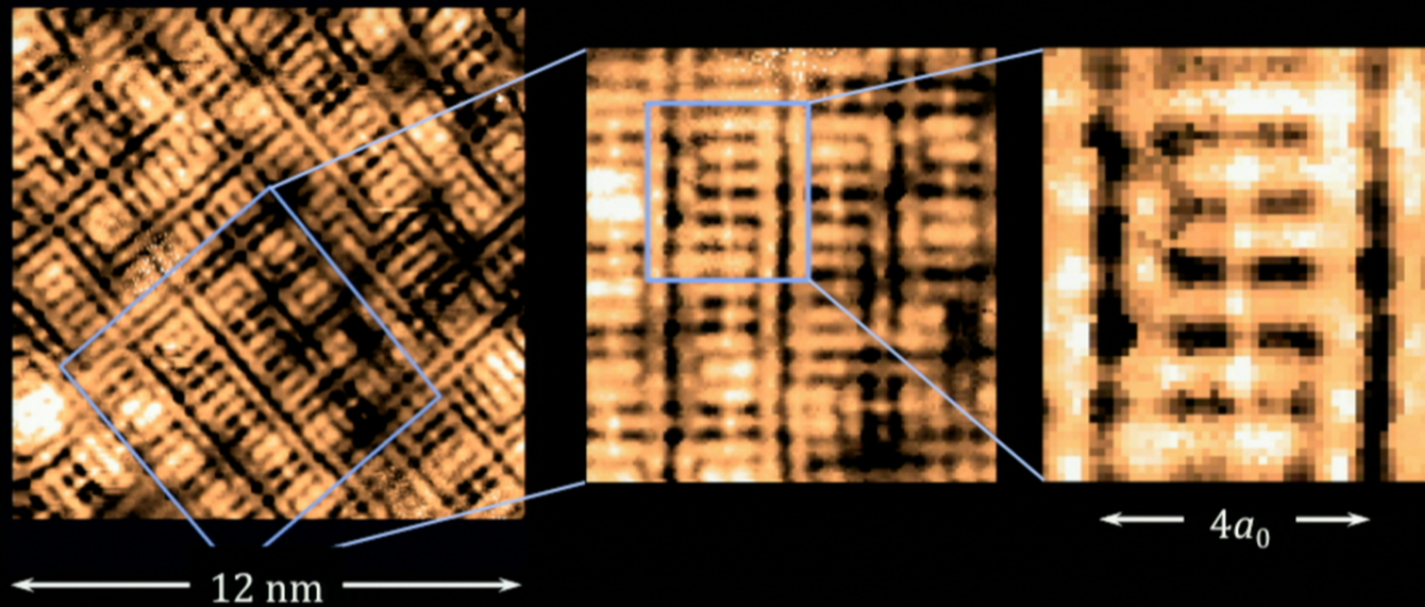
Nature 430, 1001 (2004) *Science* 315, 1380 (2007) *Nature* 466, 374 (2010) *Science* 344, 612 (2014)

High-resolution Imaging Cuprate Broken-Symmetry States



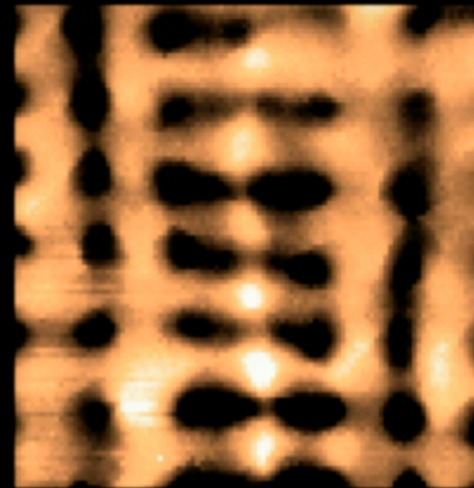
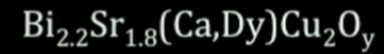
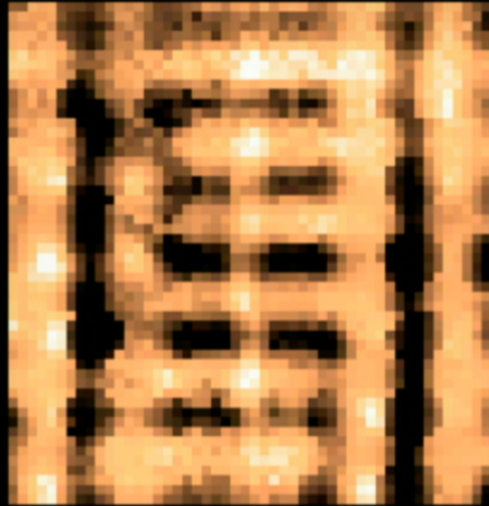
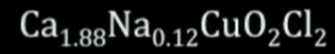
Nature 430, 1001 (2004) *Science* 315, 1380 (2007) *Nature* 466, 374 (2010) *Science* 344, 612 (2014)

Rotational Symmetry Breaking within CuO_2 Unit Cell



Nature 430, 1001 (2004) *Science* 315, 1380 (2007) *Nature* 466, 374 (2010) *Science* 344, 612 (2014)

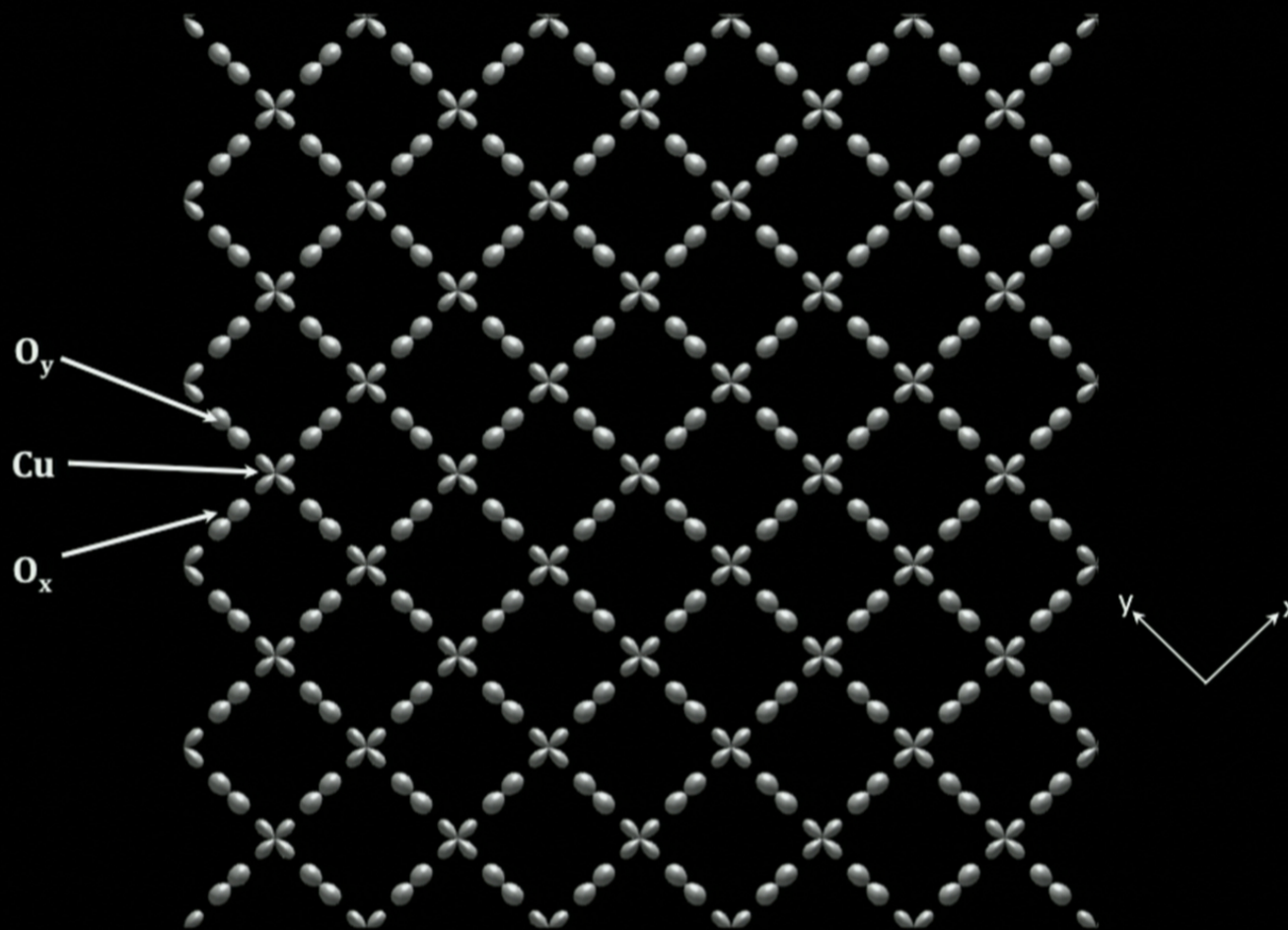
Complex / Repeatable Patterns of IUC C_4 Breaking



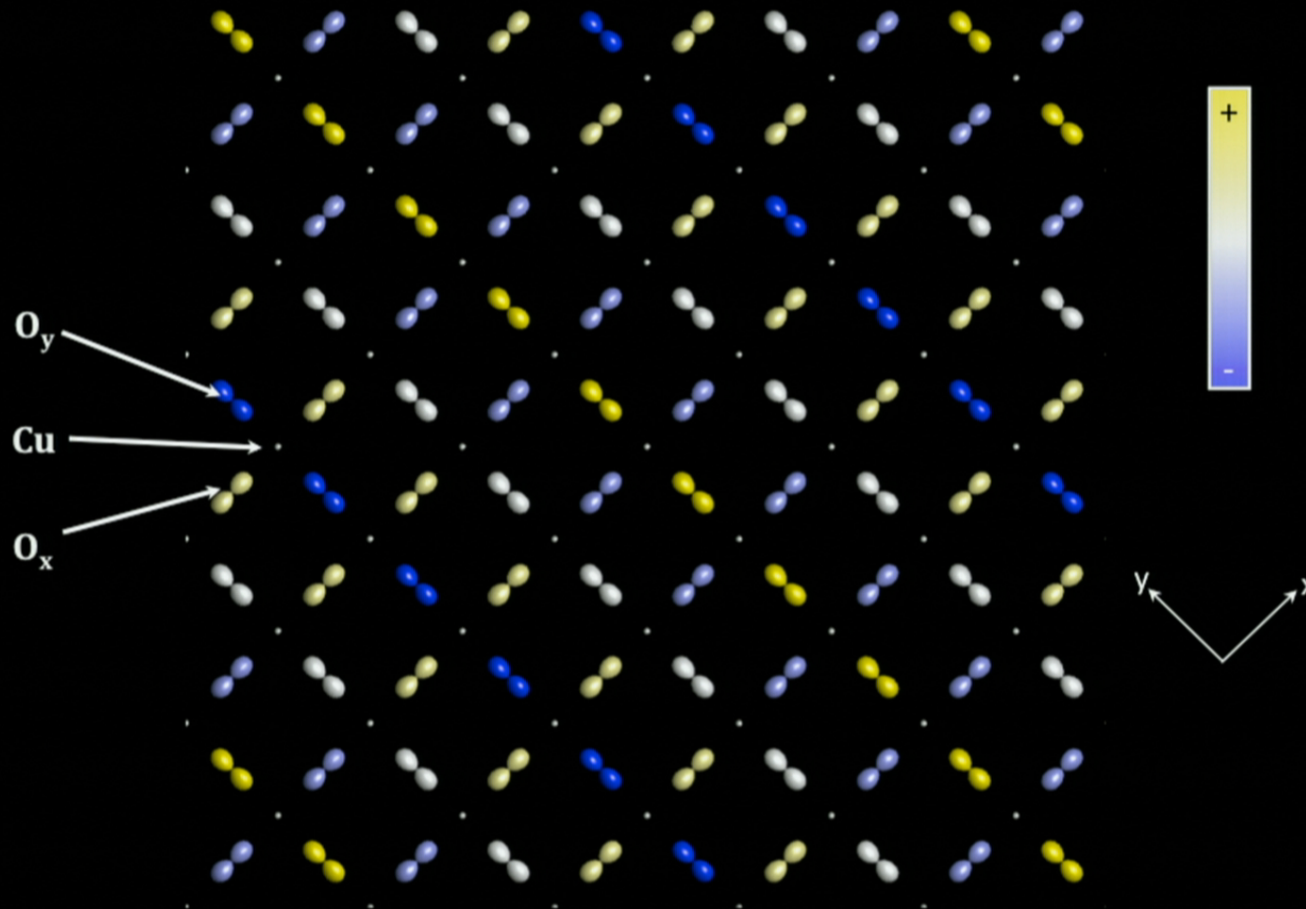
150 mV, 4.2 K

Nature **430**, 1001 (2004) *Science* **315**, 1380 (2007) *Nature* **466**, 374 (2010) *Science* **344**, 612 (2014)

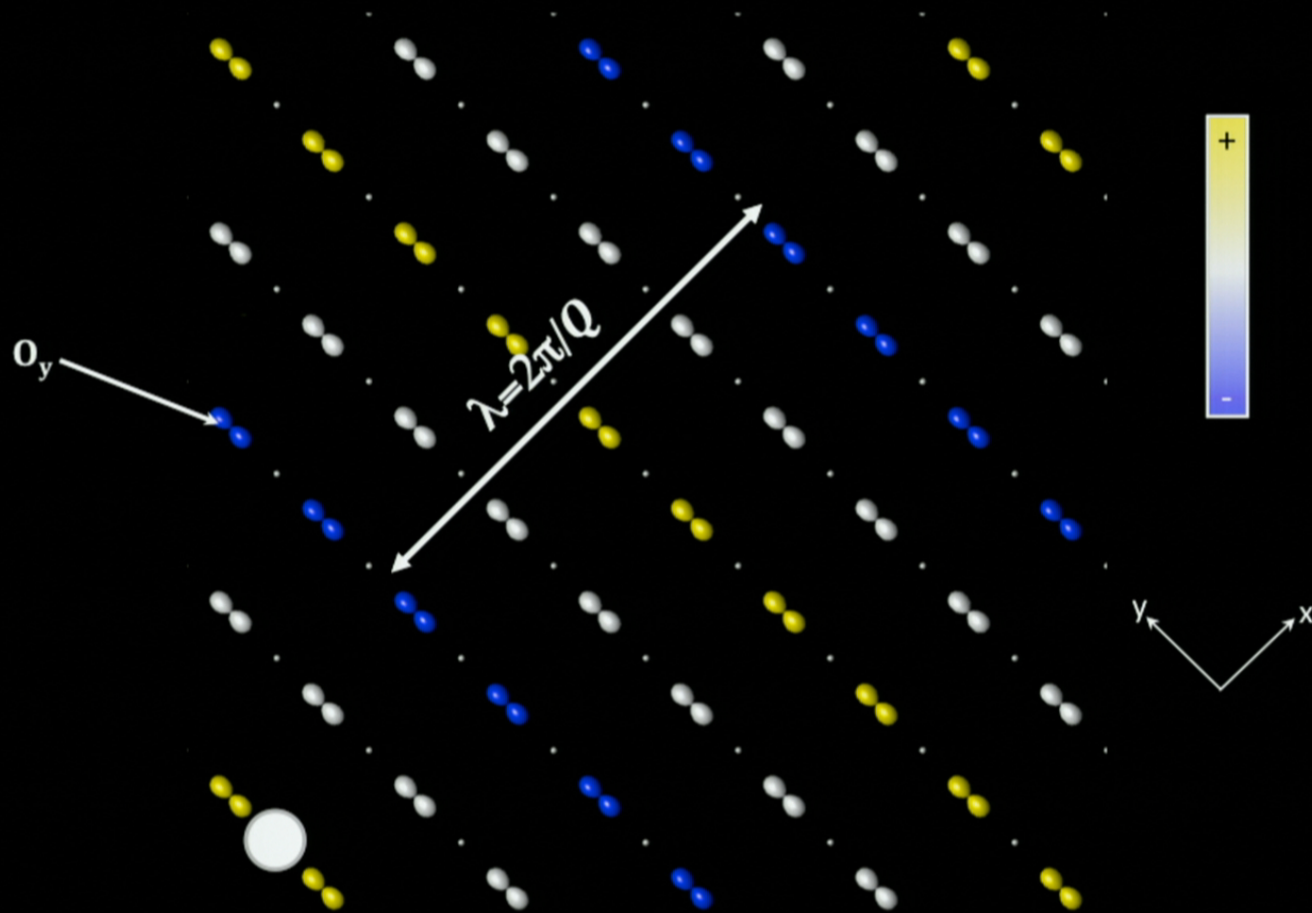
CuO₂ Lattice



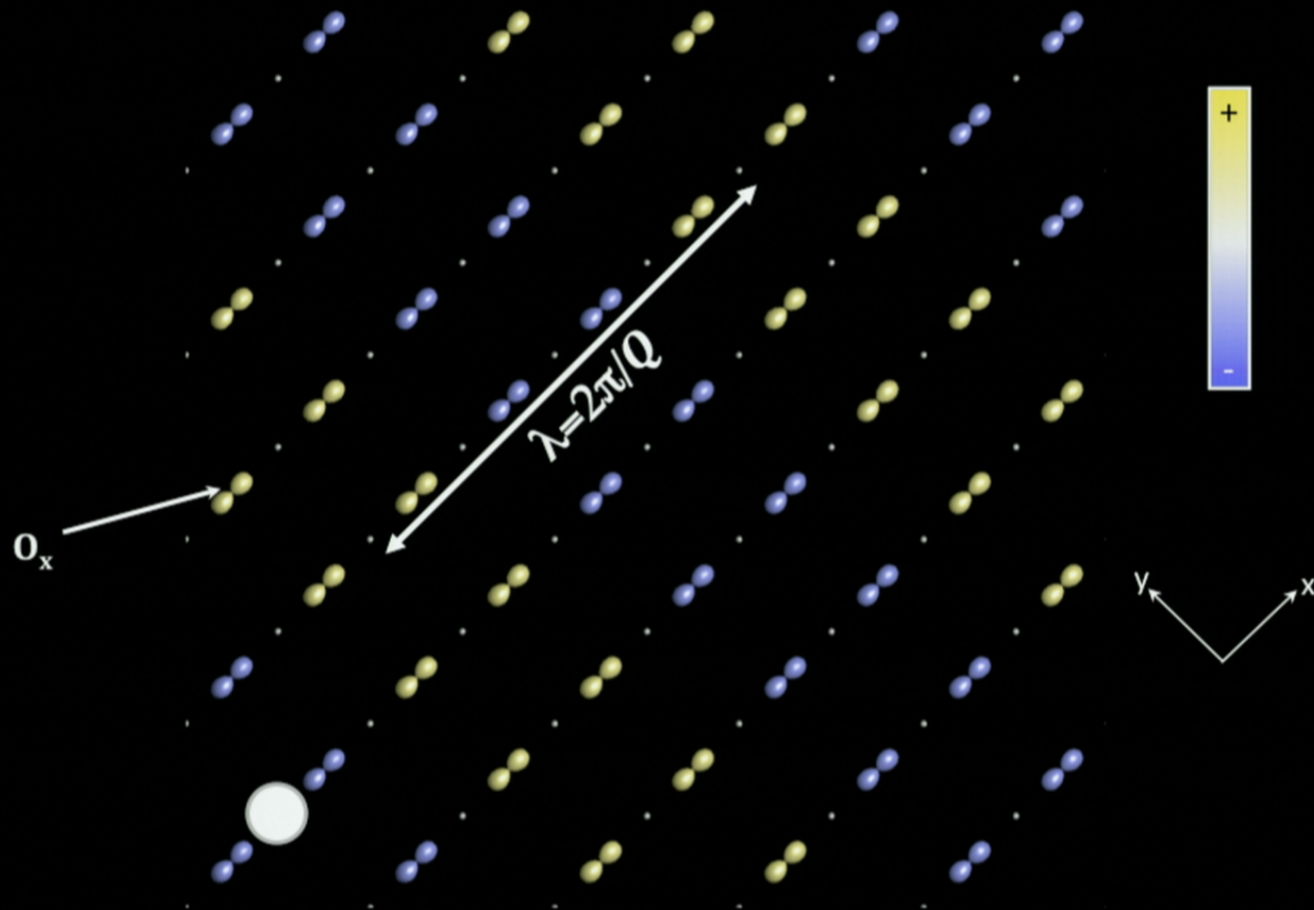
d-Symmetry Form Factor Density Wave



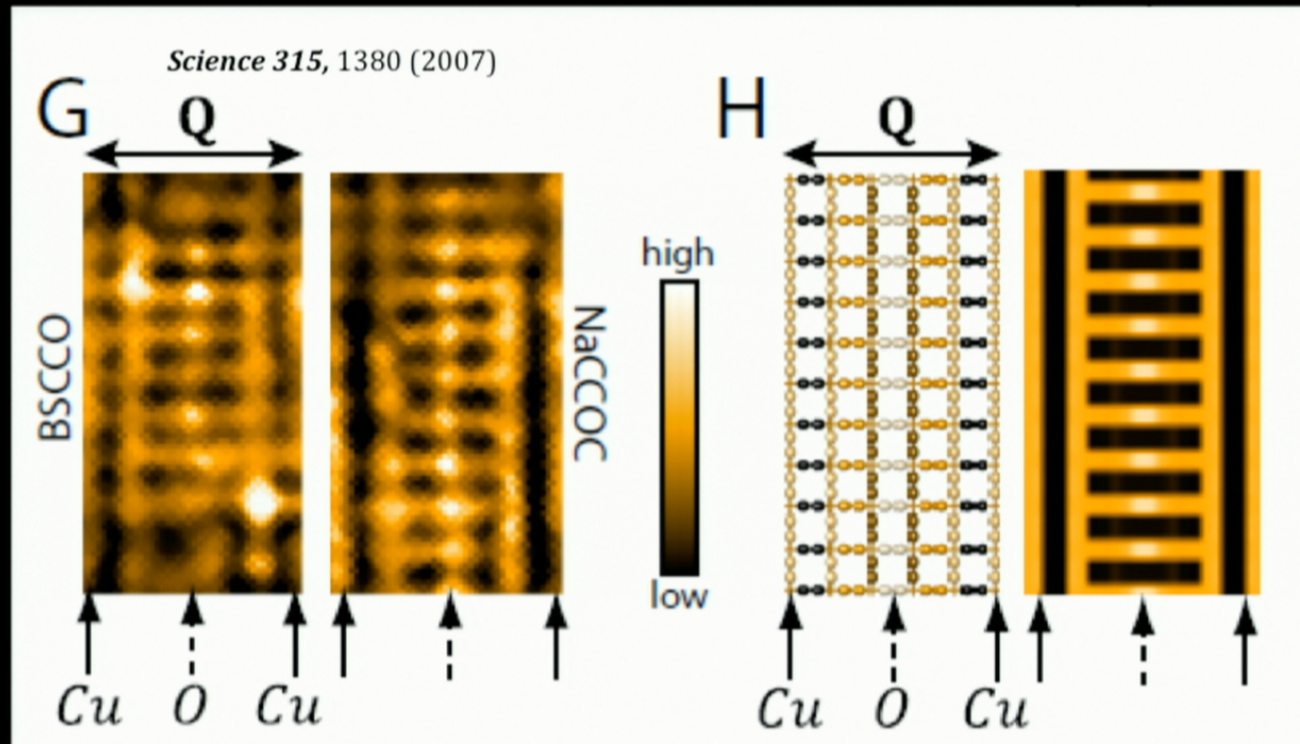
O_y Modulates at Q_x



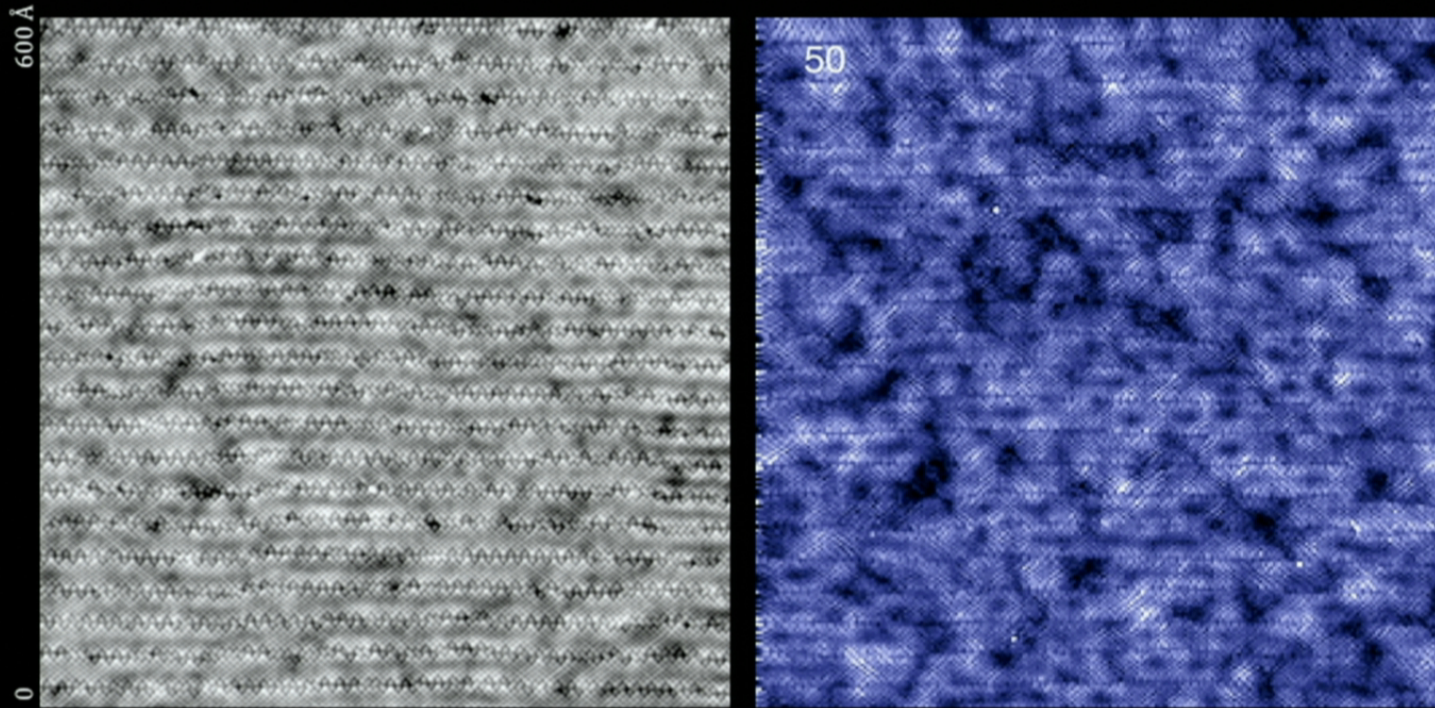
O_x Modulates at Q_x



Unidirectional d -Symmetry FF Density Wave



Copper-based HTS: Band/Gap Structure from QPI

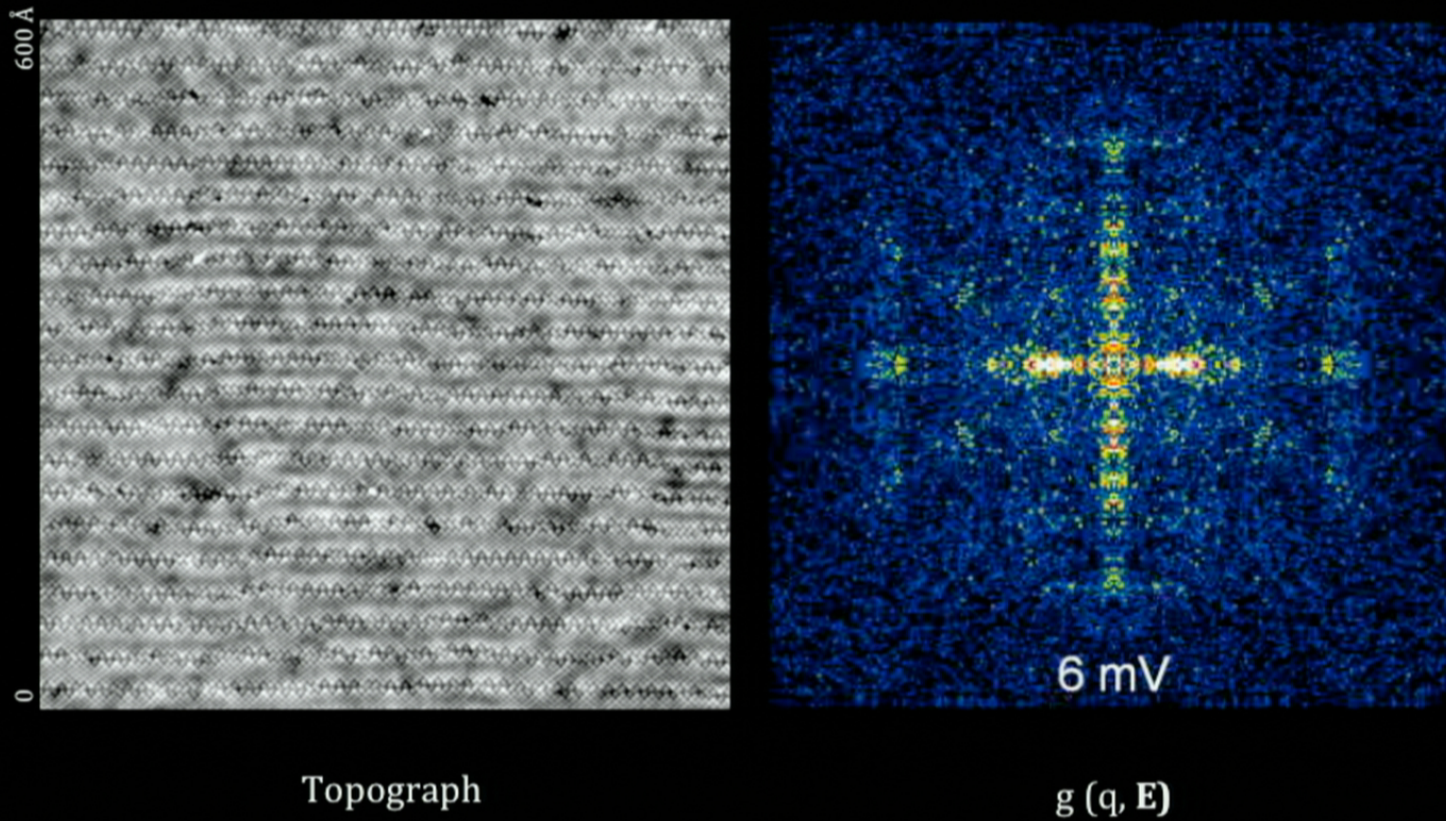


Topograph

$g(r,V)$

Nature 454, 1072, (2008)

Copper-based HTS: Band/Gap Structure from QPI

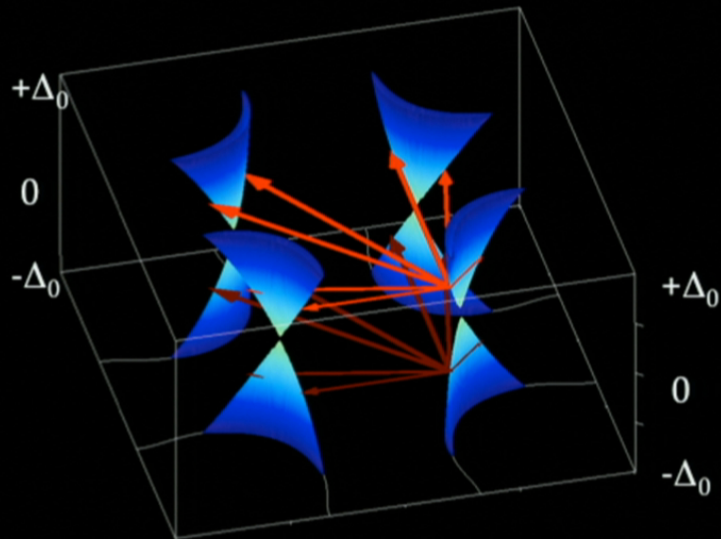


Topograph

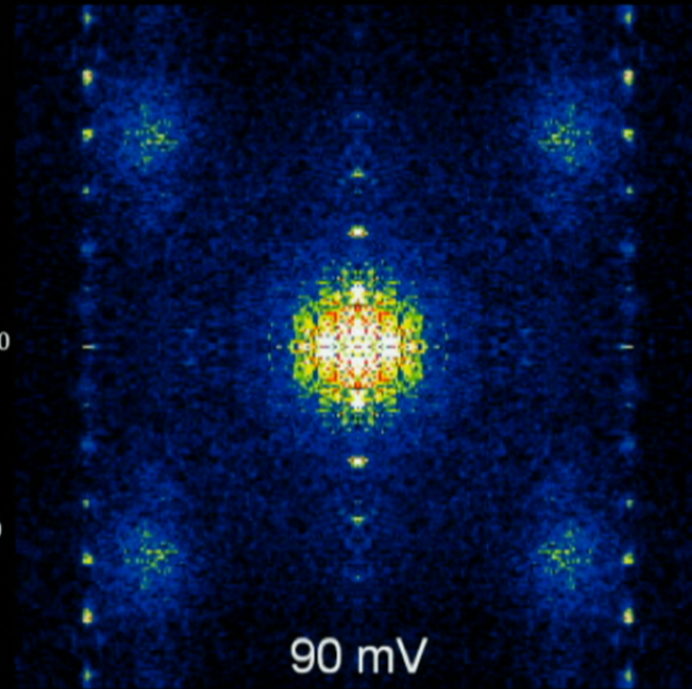
$g(q, E)$

Nature 454, 1072, (2008)

Copper-based HTS: Band/Gap Structure from QPI



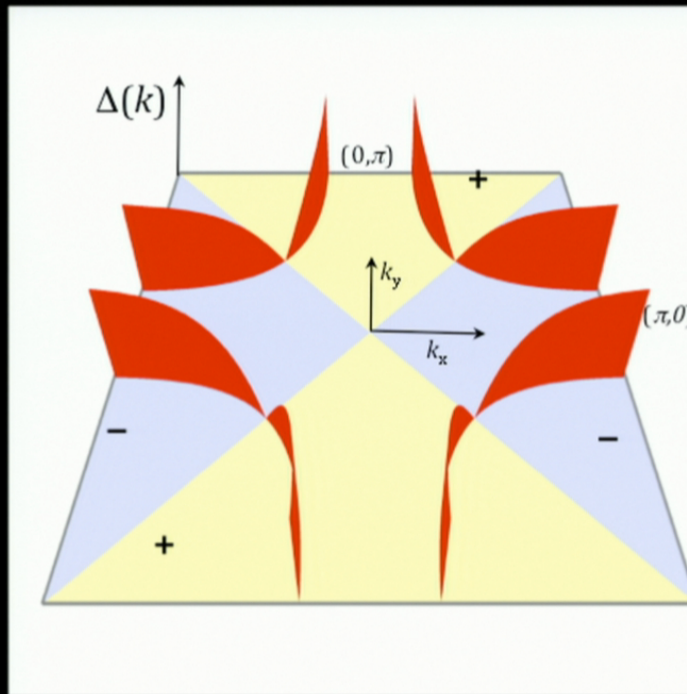
Particle-hole symmetric
 $i=1,..7$ Bogoliubov QPI



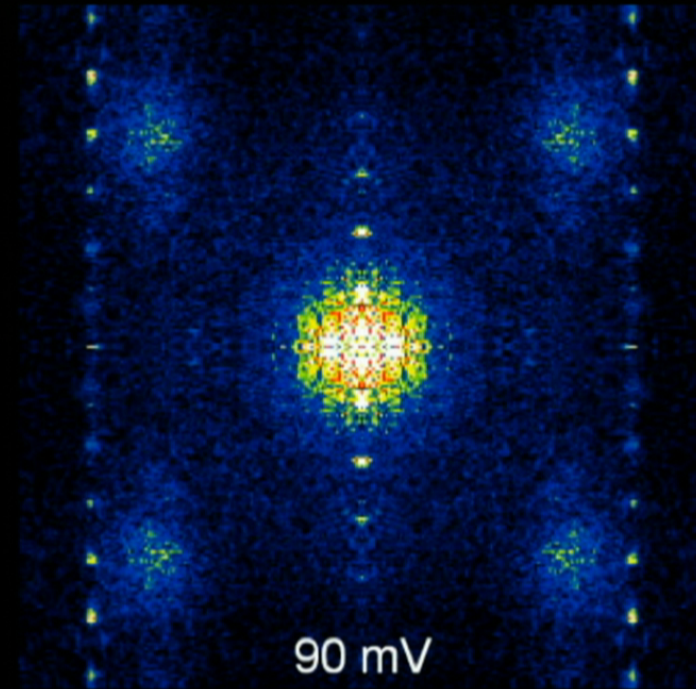
$g(q, E)$

Nature 454, 1072, (2008)

Copper-based HTS: Band/Gap Structure from QPI



$\Delta(k)$

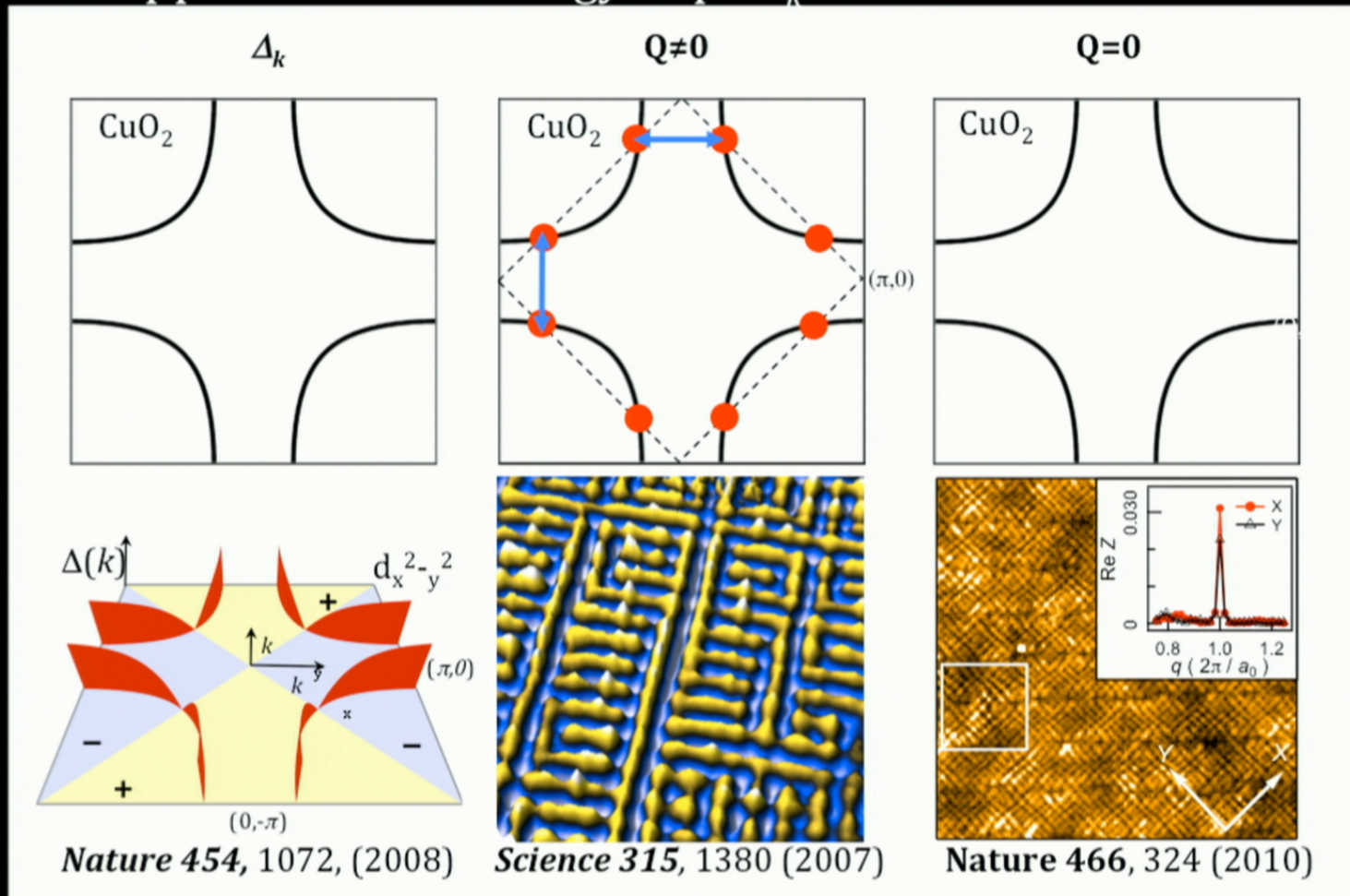


90 mV

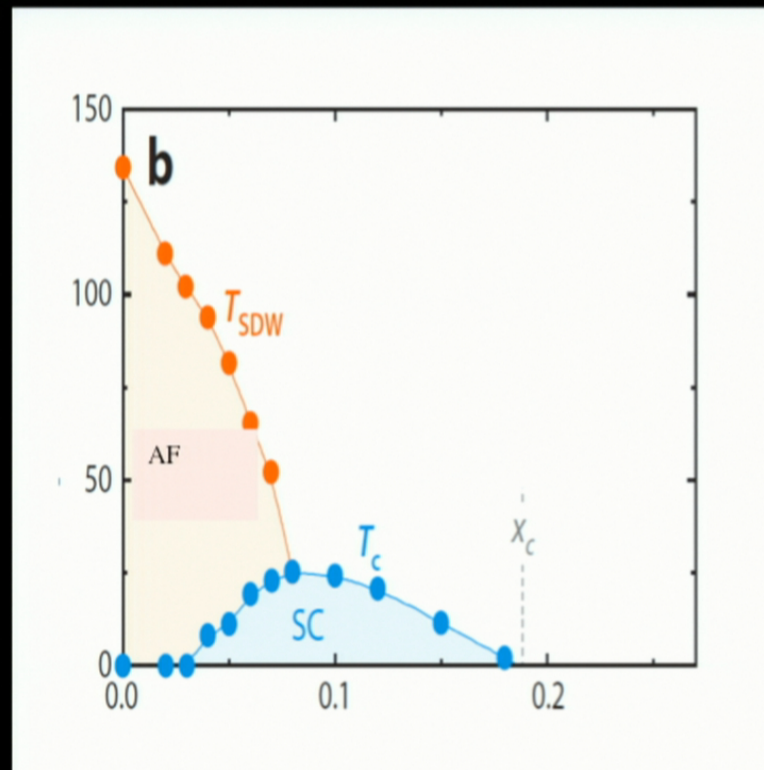
$g(q, E)$

Nature 454, 1072, (2008)

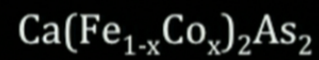
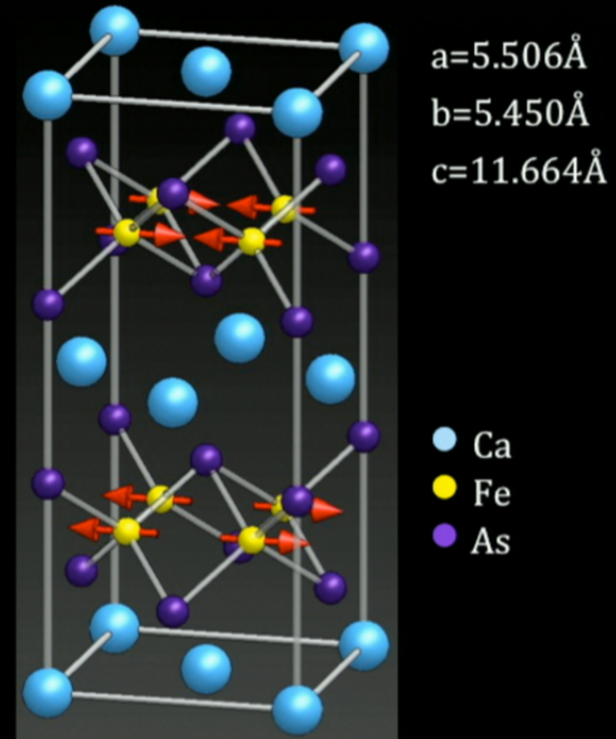
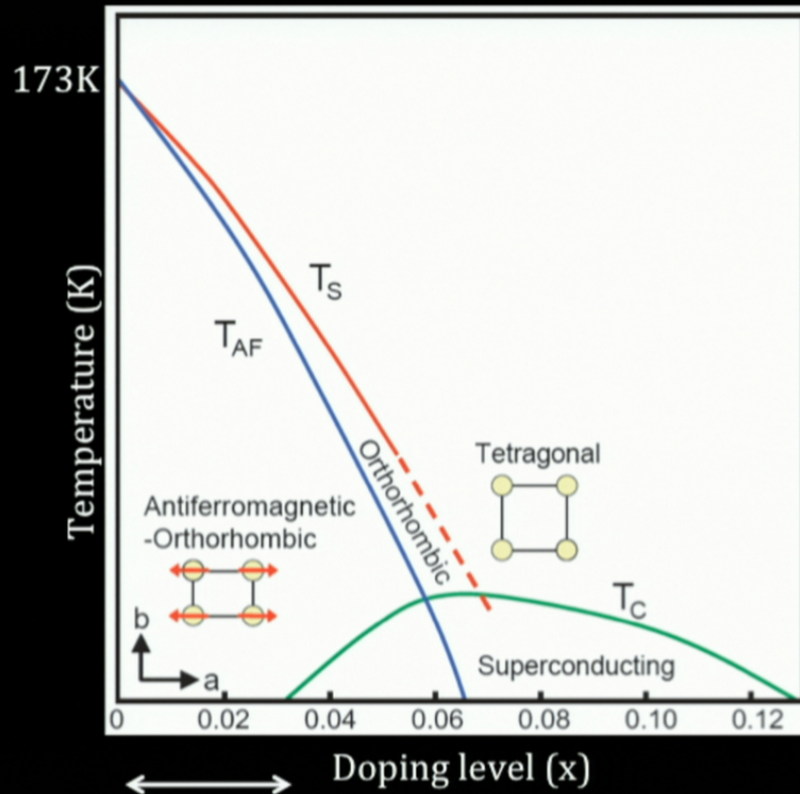
Copper-based SC Energy Gaps Δ_k & Intertwined Phases



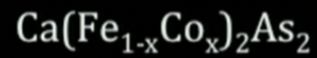
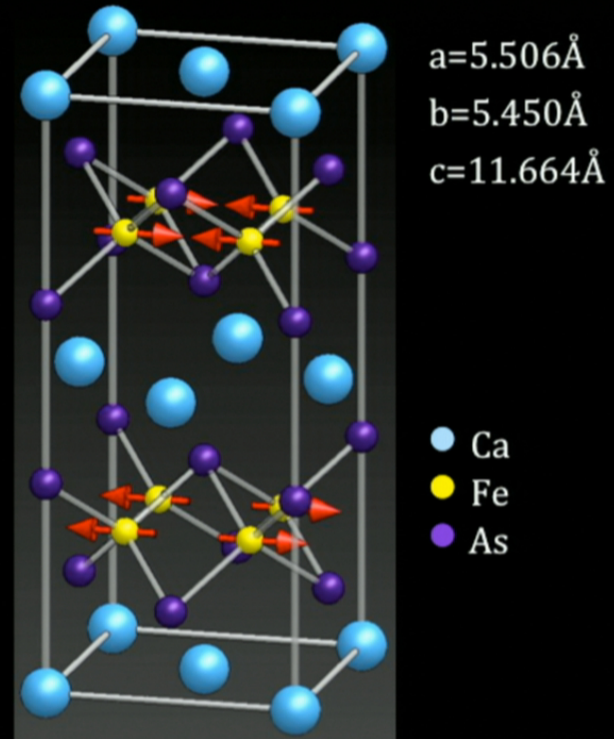
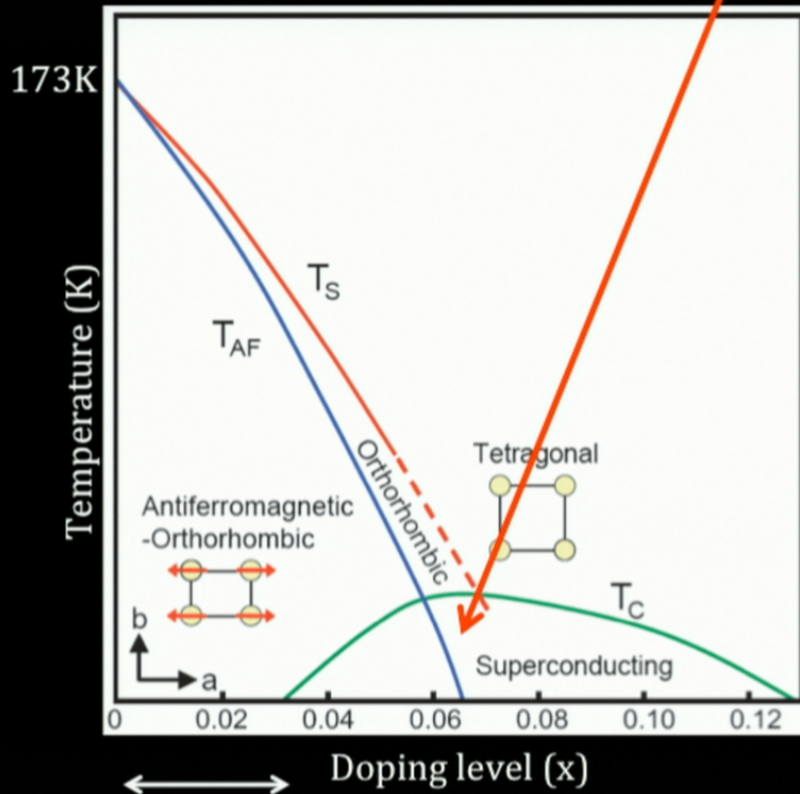
IRON-BASED SUPERCONDUCTIVITY & INTERTWINED PHASES



Typical FeAs Phase Diagram

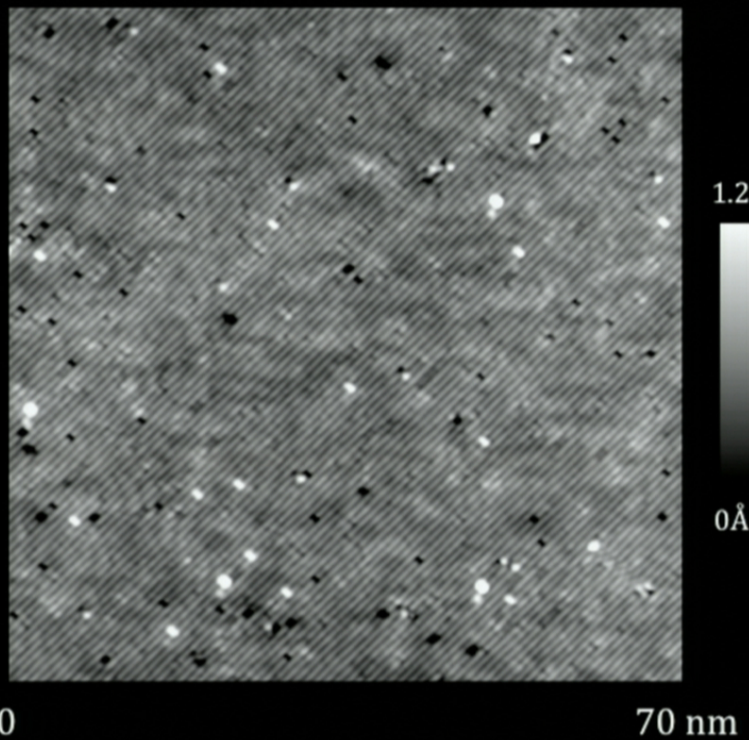


Mechanism of High-Tc Superconductivity?

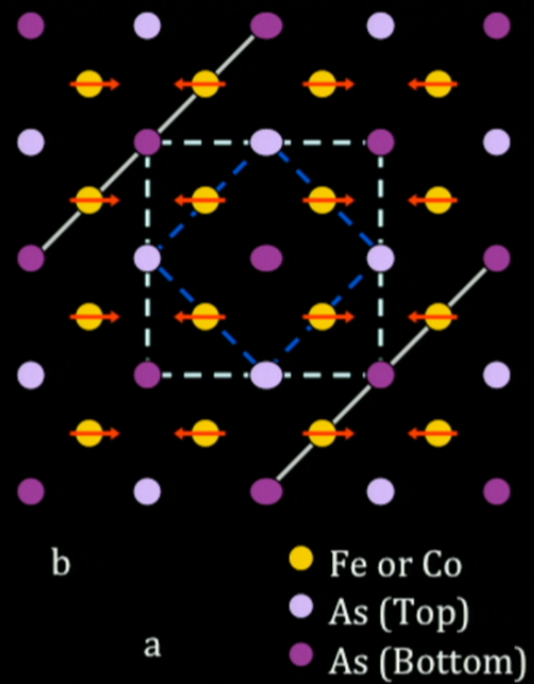


$\text{Ca}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$ -- Excellent cryo-cleave surface

Topography

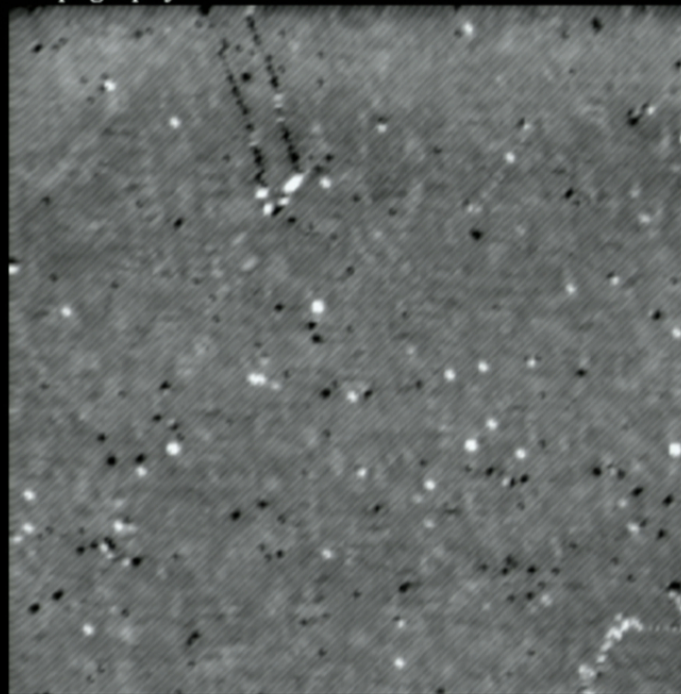


FeAs-layer Reconstruction



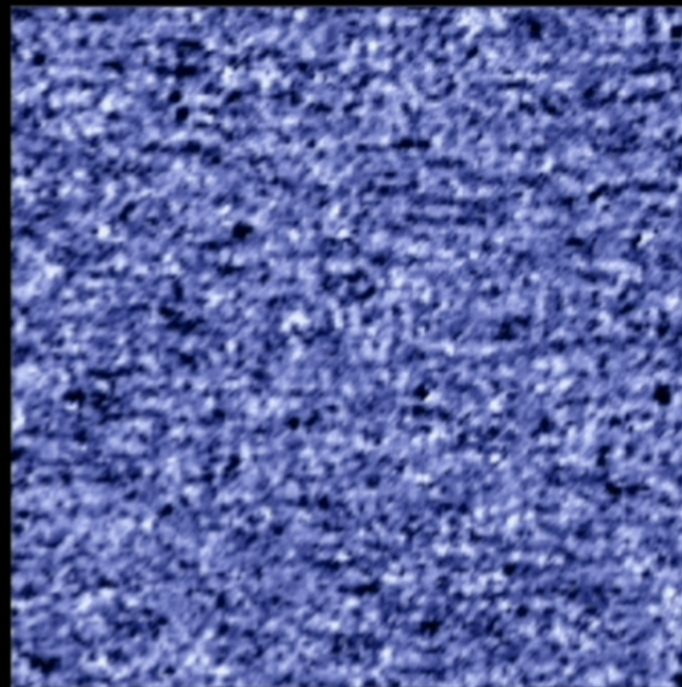
Quasiparticle Interference in 'Parent' State CaFe_2As_2

Topography



0

94nm 0

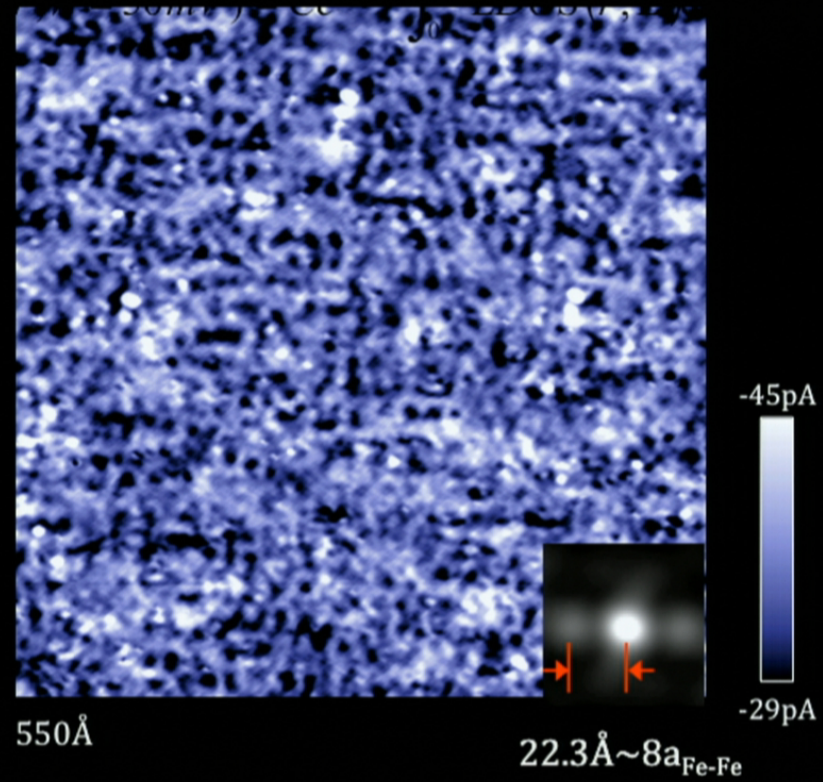


0

94nm

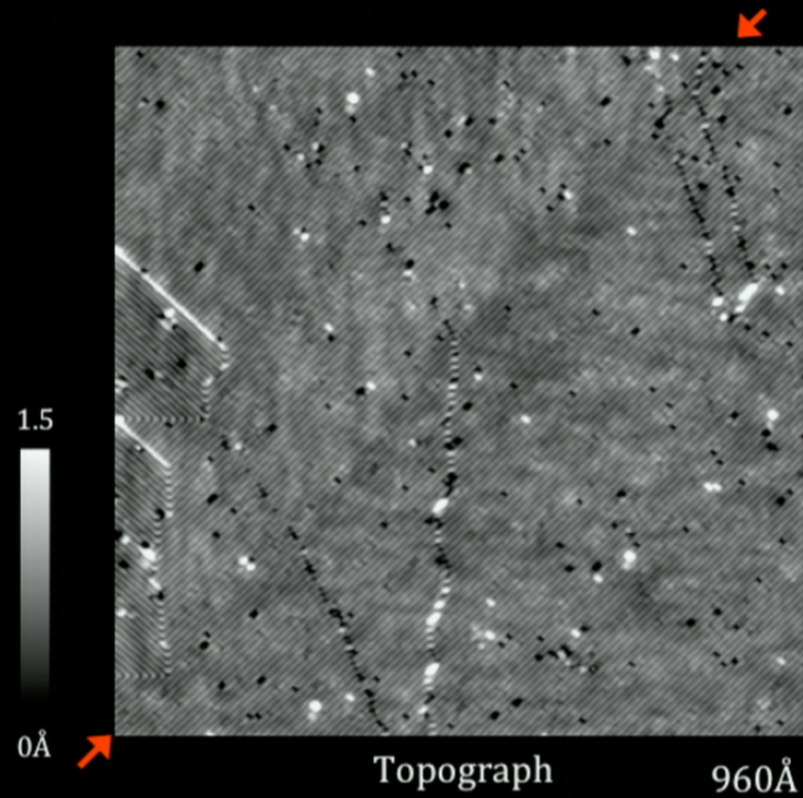
Science **327**, 181 (2010)

Static electronic nanostructures $\sim 8a_{\text{FeFe}}$ along a-axis



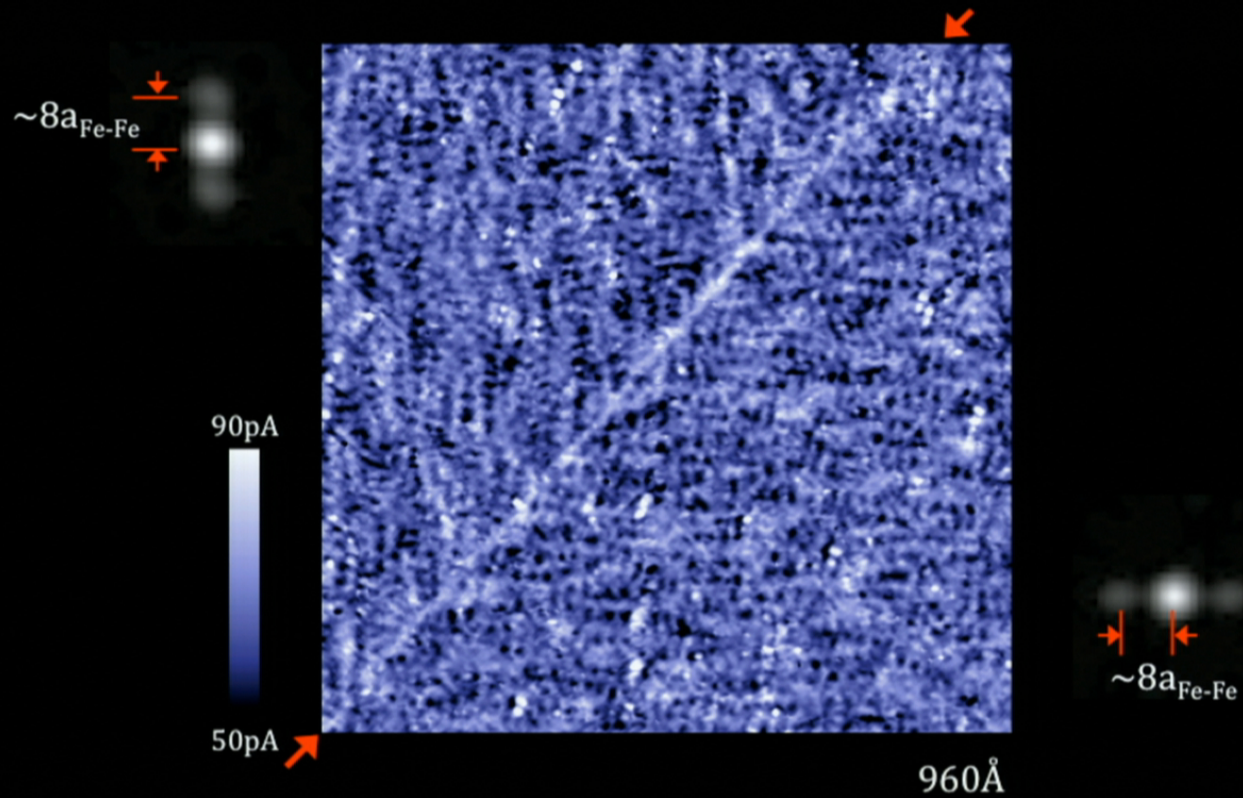
Science 327, 181 (2010)

Effect of orthorhombic twin boundary



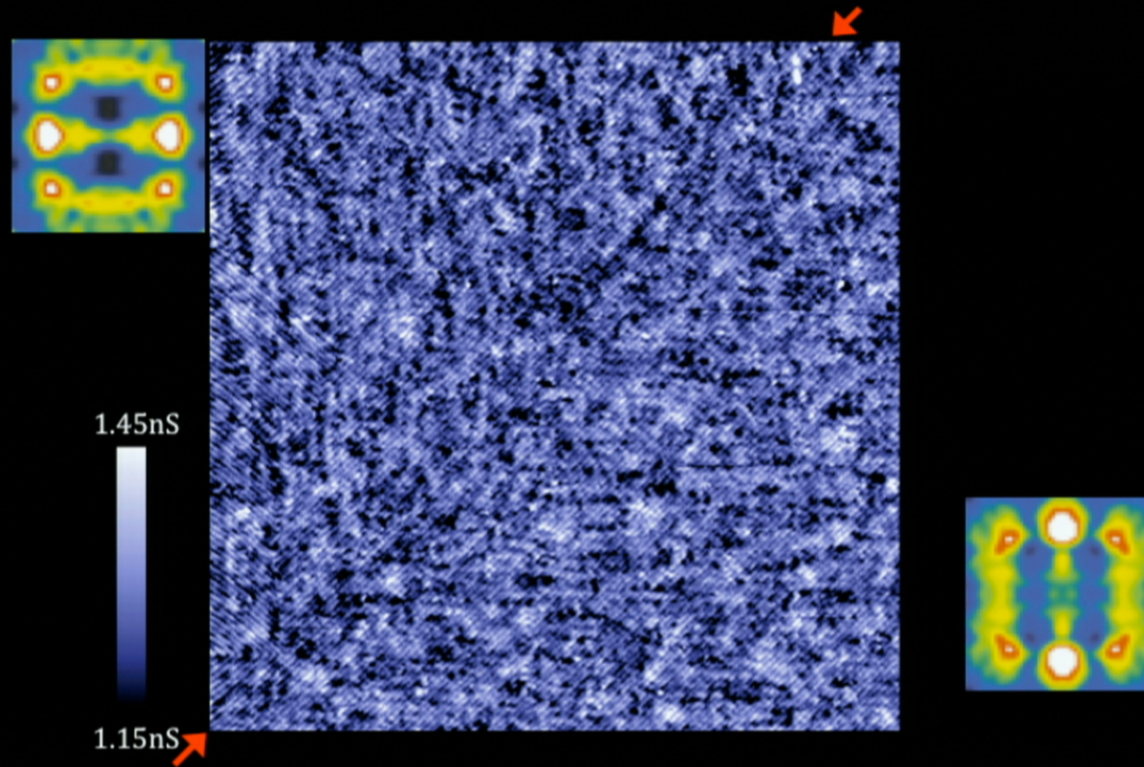
Science 327, 181 (2010)

Static $8a_0$ electronic nanostructures rotate by 90 degrees



Science 327, 181 (2010)

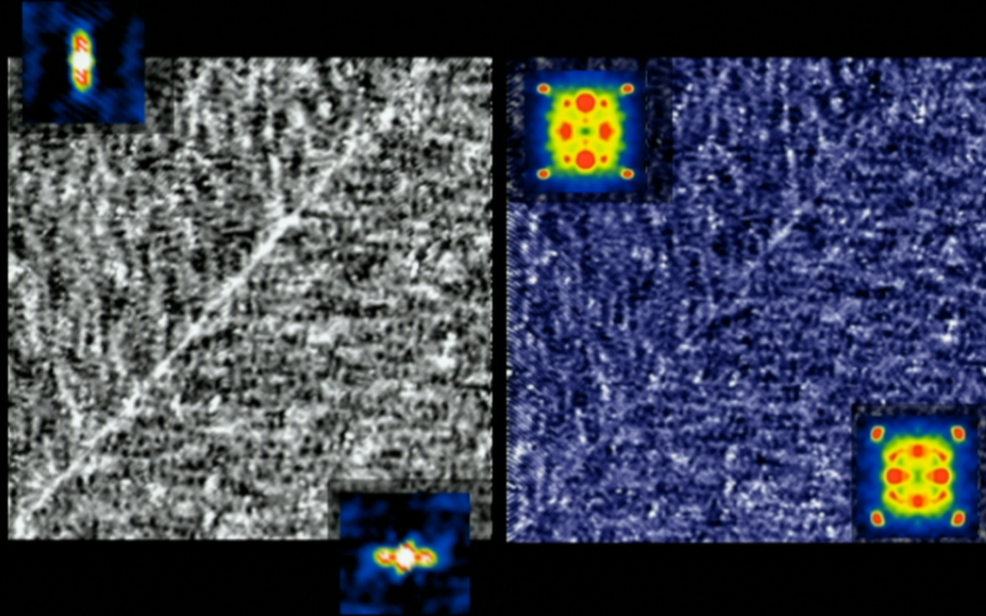
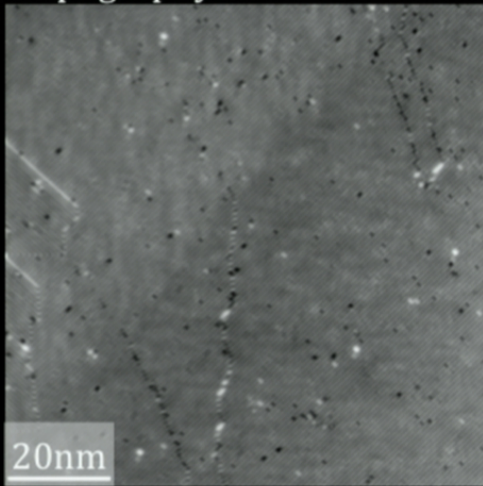
QPI modulation wavevectors rotate by 90 degrees



Science 327, 181 (2010)

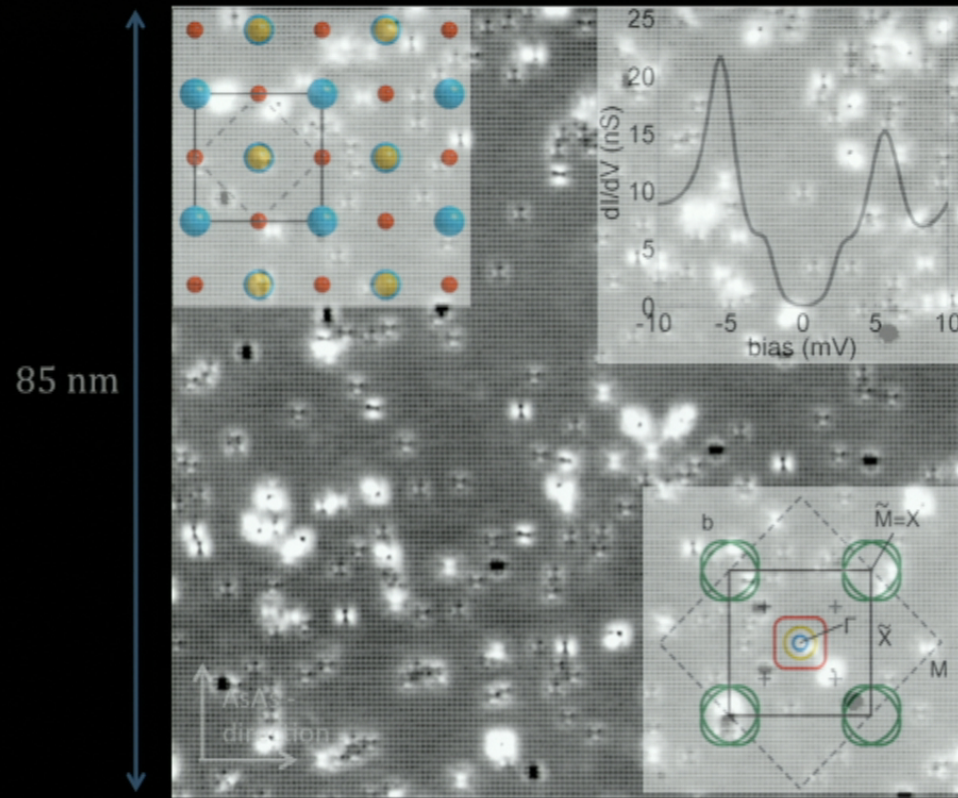
Discovery of Electronic Nematic Phase in Iron-Pnictides

Topography




Science **327**, 181 (2010)

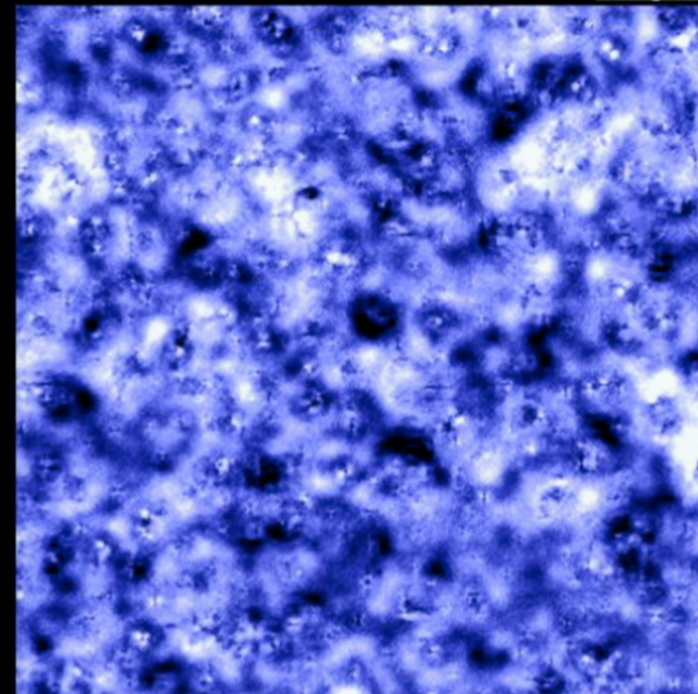
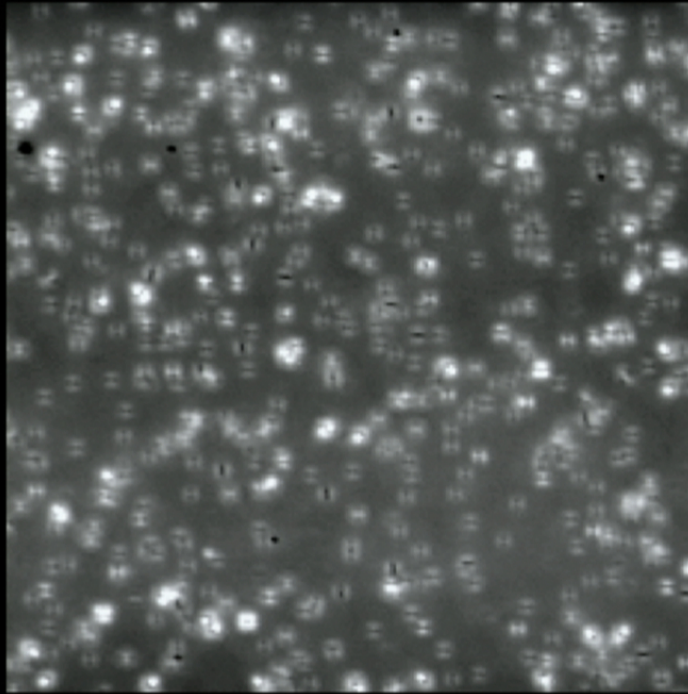
Energy Gaps, Surface & Tunneling



Science 336, 563, (2012)

LiFeAs Bogoliubov QPI $g(\mathbf{r}, E)$

-7.67 meV 



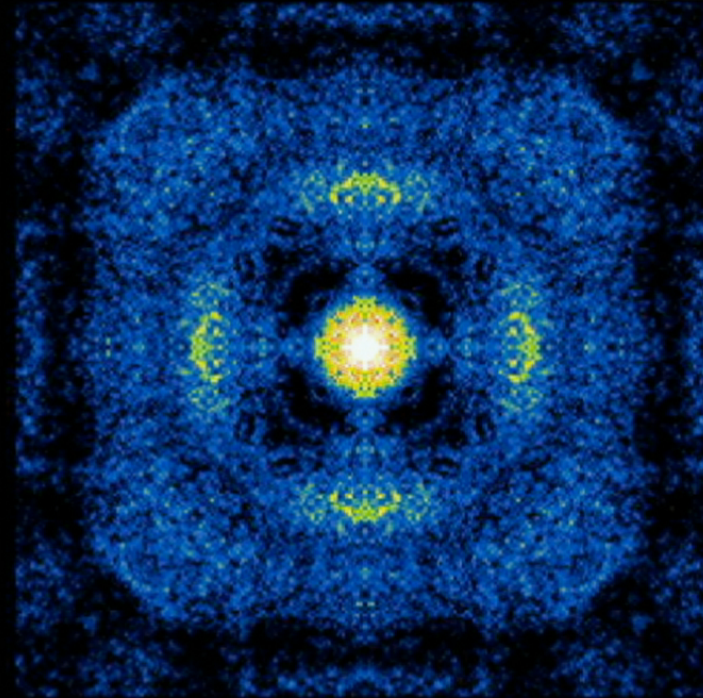
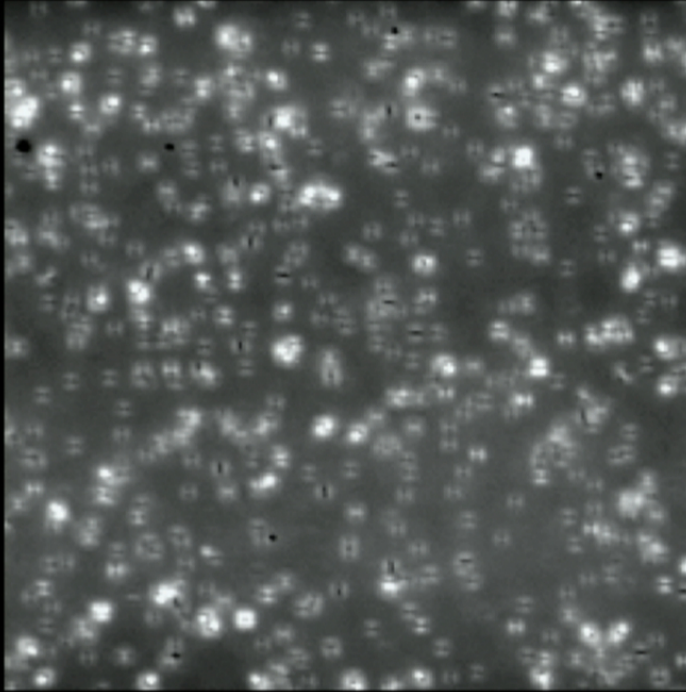
82 x 82 nm²

↑
AsAs -
direction
→

Science 336, 563, (2012)

LiFeAs Bogoliubov QPI $g(\mathbf{q}, E)$

-5.67 meV

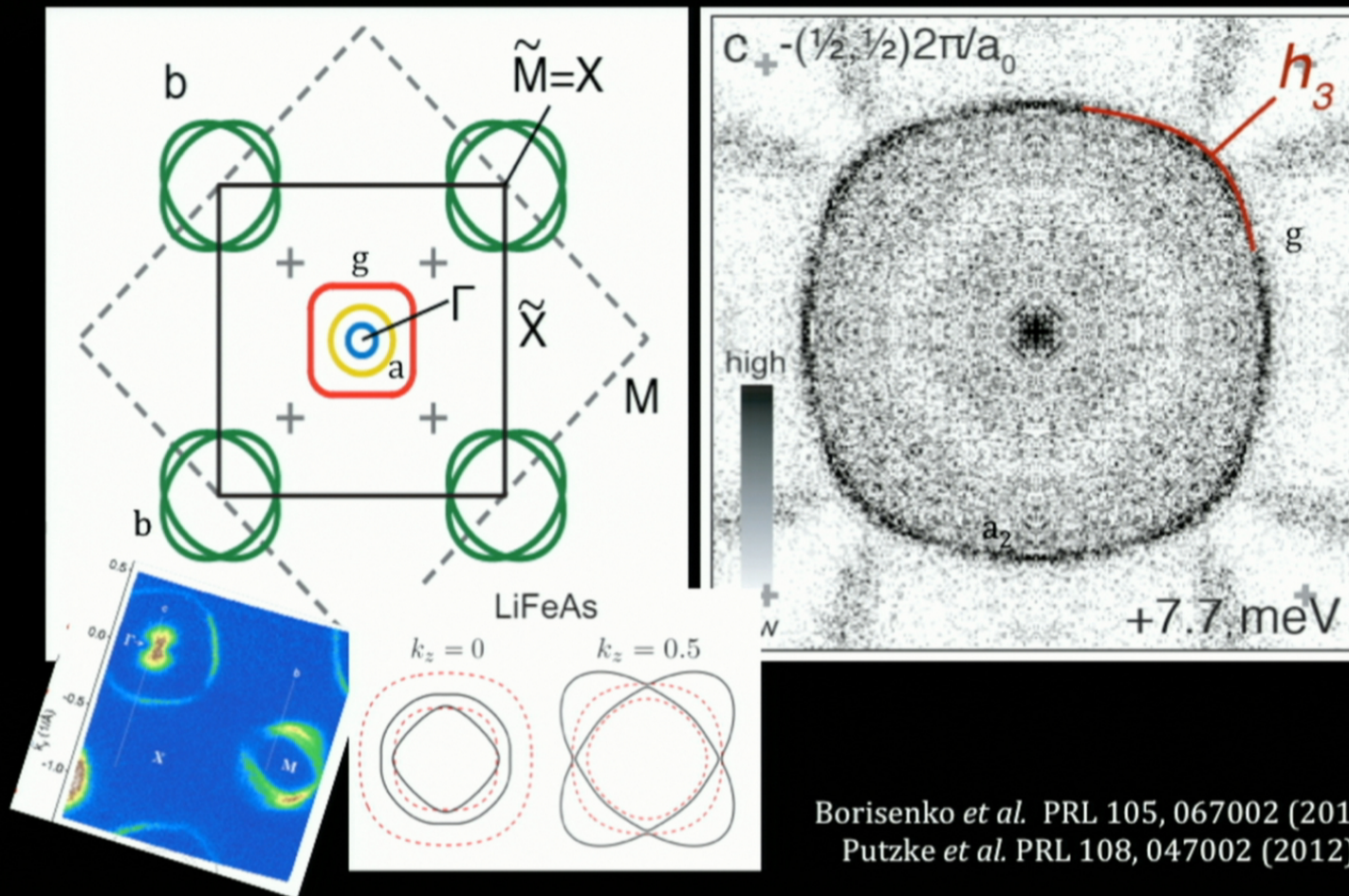


↑
AsAs -
direction
→

Science 336, 563, (2012)

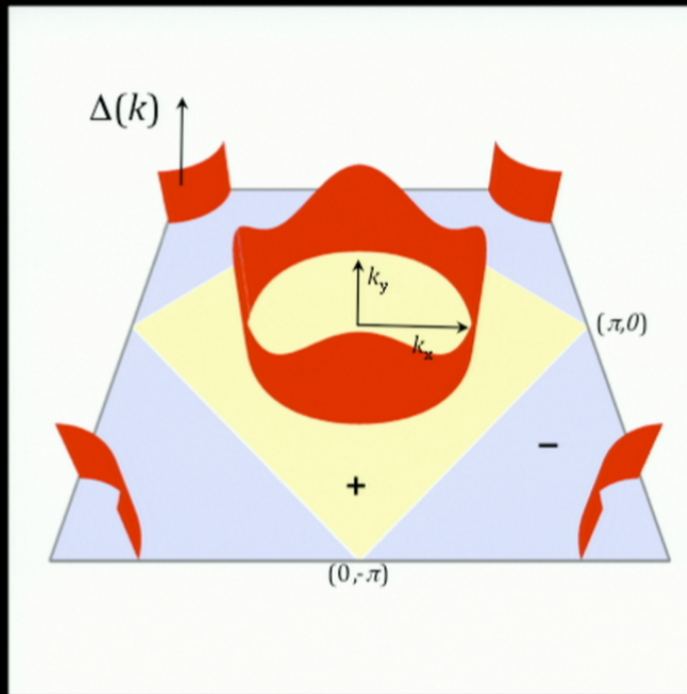


Band Identification : Correspondence to ARPES and Quantum Oscillations



Borisenko *et al.* PRL 105, 067002 (2010)
 Putzke *et al.* PRL 108, 047002 (2012)

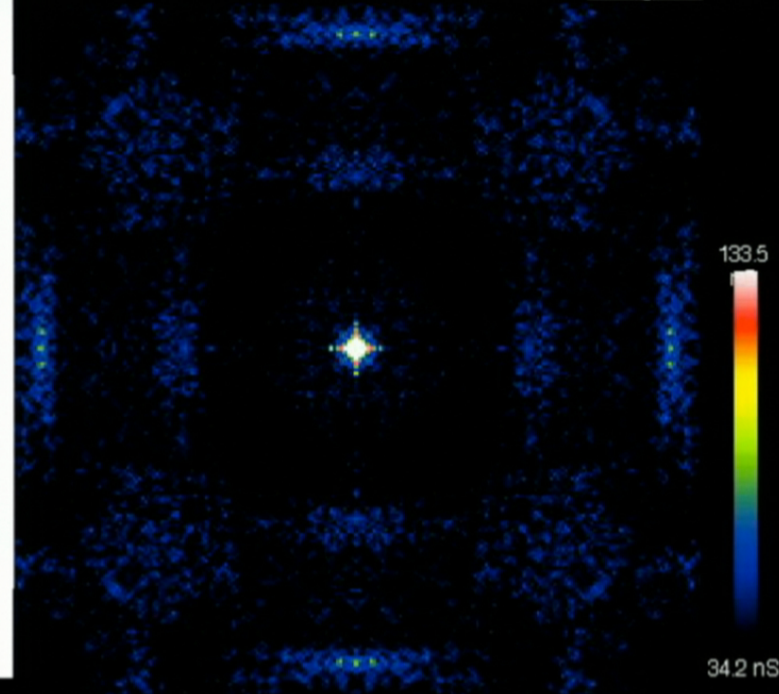
Iron-based HTS: Band/Gap Structure from QPI



$\Delta(k)$

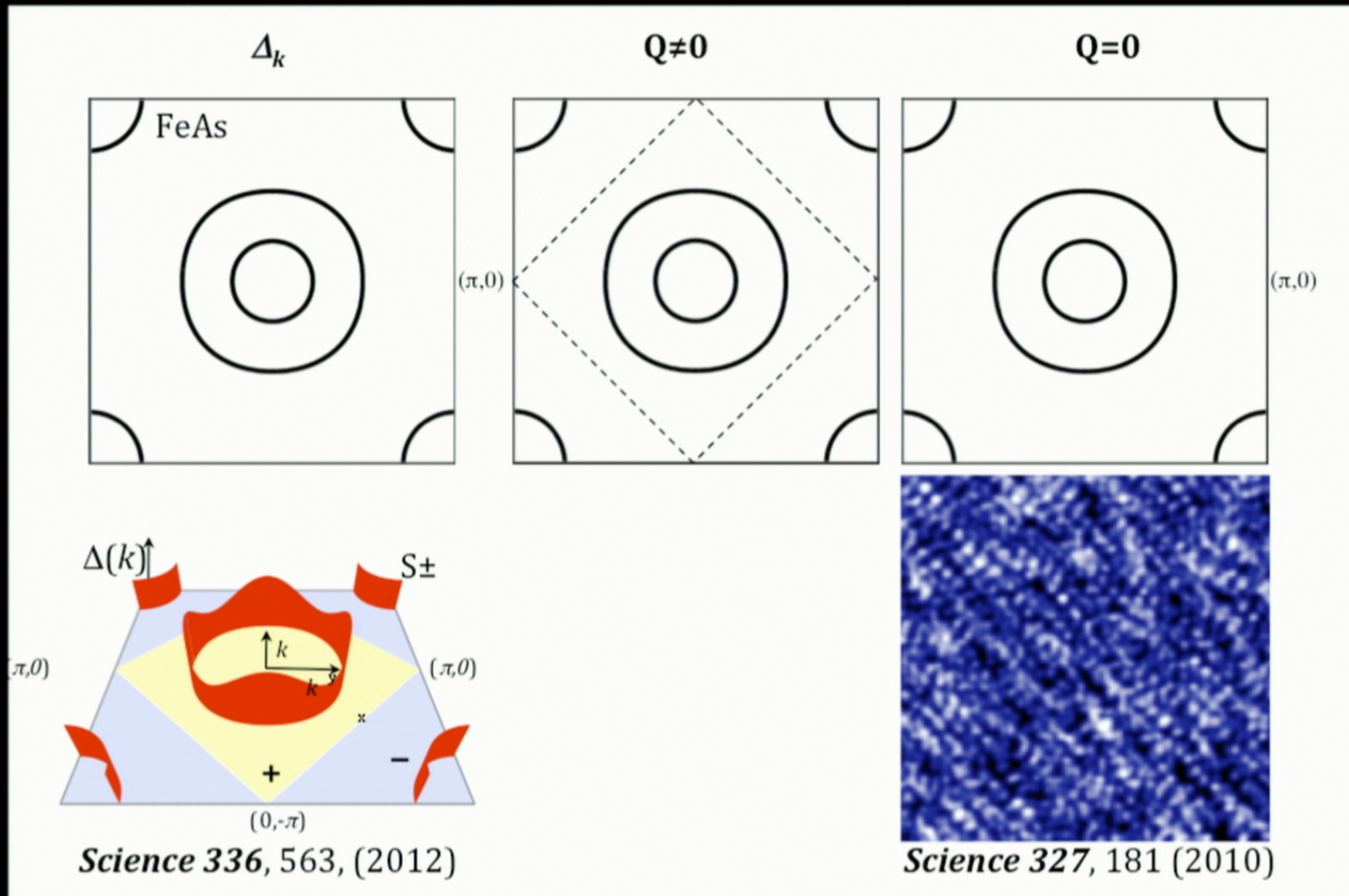
Science 336, 563, (2012)

-7.67 meV

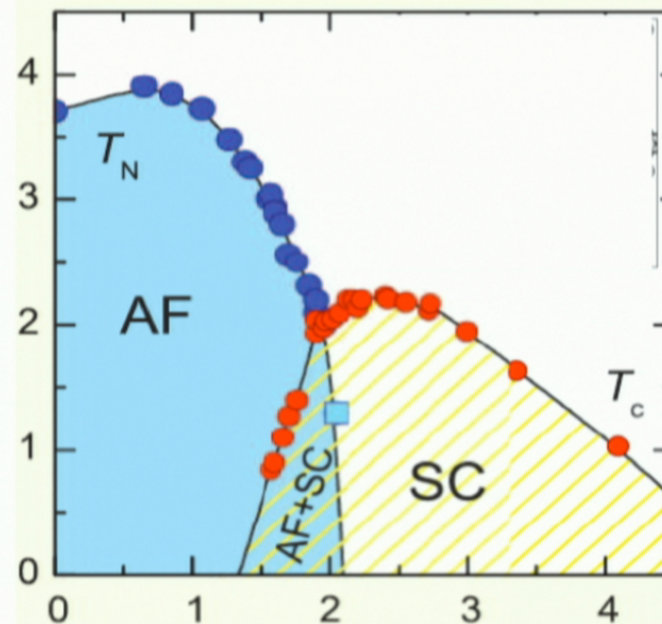


$g(q, E)$

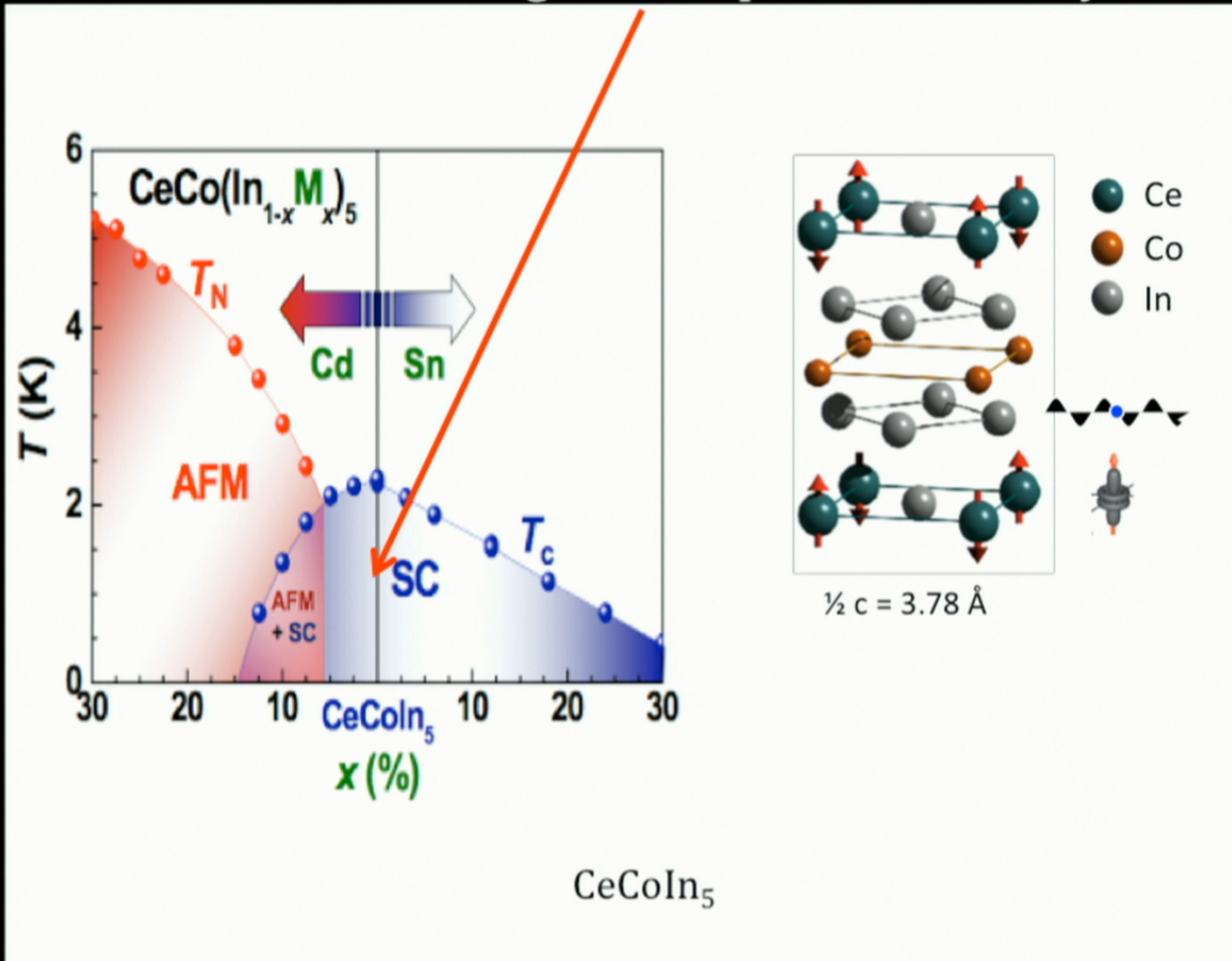
Iron-based Energy Gaps Δ_k & Intertwined Phases



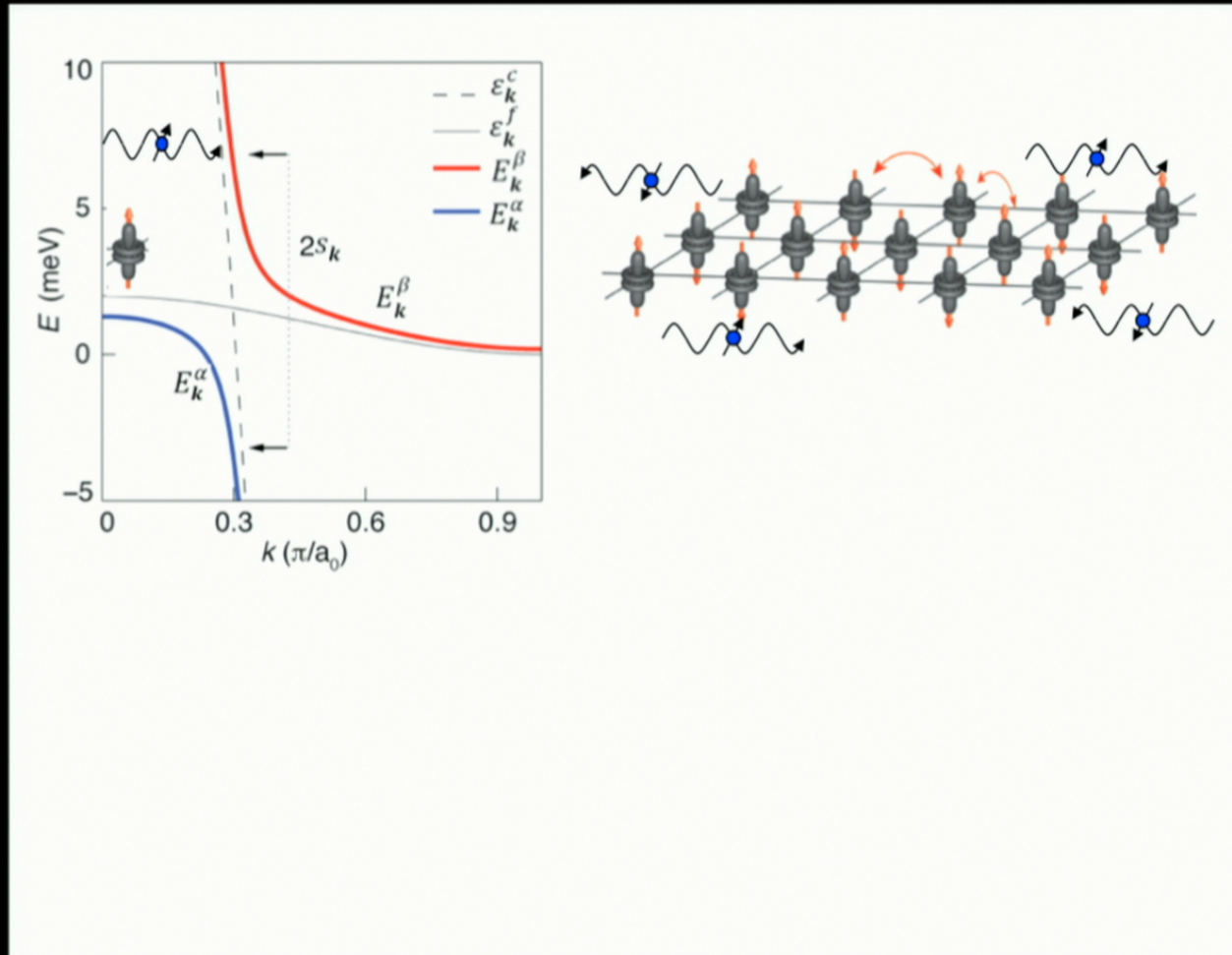
HEAVY FERMION SUPERCONDUCTIVITY & INTERTWINED PHASES



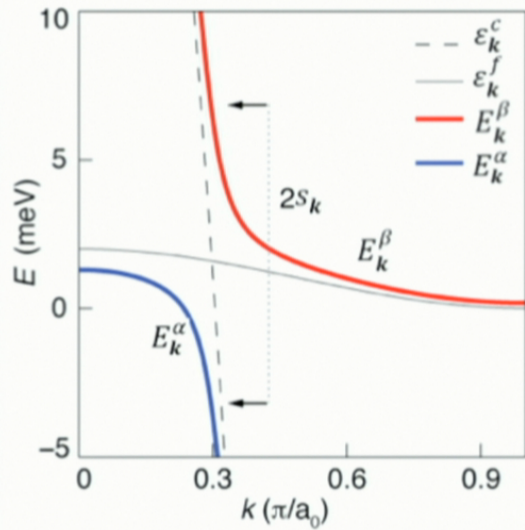
Mechanism of 'High-T_c' Superconductivity?



Heavy-Fermion Formation (f -electron Hybridization)



Heavy-Fermion Band Structure $E^{\alpha,\beta}$



$$H = \sum_{k,\sigma} \epsilon_k^c c_{k,\sigma}^\dagger c_{k,\sigma} + \epsilon_k^f f_{k,\sigma}^\dagger f_{k,\sigma} - S_k^* f_{k,\sigma}^\dagger c_{k,\sigma} - S_k c_{k,\sigma}^\dagger f_{k,\sigma}$$

$$H = \sum_{k,\sigma} \begin{pmatrix} c_{k,\sigma}^\dagger & f_{k,\sigma}^\dagger \end{pmatrix} \begin{pmatrix} \epsilon_k^c & -S_k \\ -S_k^* & \epsilon_k^f \end{pmatrix} \begin{pmatrix} c_{k,\sigma} \\ f_{k,\sigma} \end{pmatrix}$$

Diagonalize:

$$\det \begin{vmatrix} \epsilon_k^c - E & -S_k \\ -S_k^* & \epsilon_k^f - E \end{vmatrix} = 0$$

$$0 = (\epsilon_k^c - E)(\epsilon_k^f - E) - S_k^2 = E^2 - E(\epsilon_k^c + \epsilon_k^f) + \epsilon_k^c \epsilon_k^f - S_k^2$$

$$E_{\mathbf{k}}^{\alpha,\beta} = \frac{\epsilon_{\mathbf{k}}^c + \epsilon_{\mathbf{k}}^f}{2} \pm \sqrt{\left(\frac{\epsilon_{\mathbf{k}}^c - \epsilon_{\mathbf{k}}^f}{2}\right)^2 + S_{\mathbf{k}}^2}$$

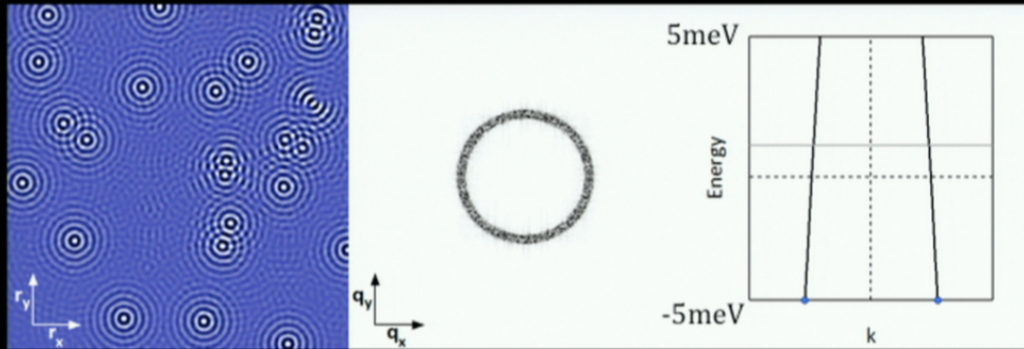
Measure $E_k^{\alpha,\beta}$ for Heavy-Fermion Bands ?



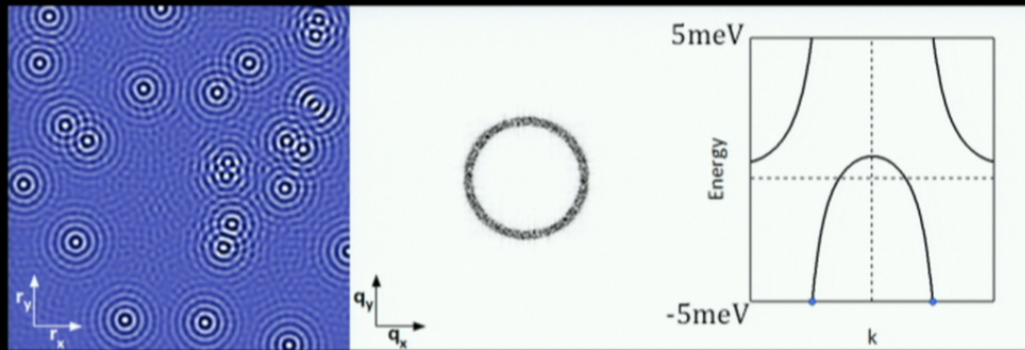
Heavy-Fermion Scattering Interference Imaging with Millikelvin SI-STM

Measure $E_k^{\alpha,\beta}$ for Heavy-Fermion Bands ?

Scattering interference within 'light' band

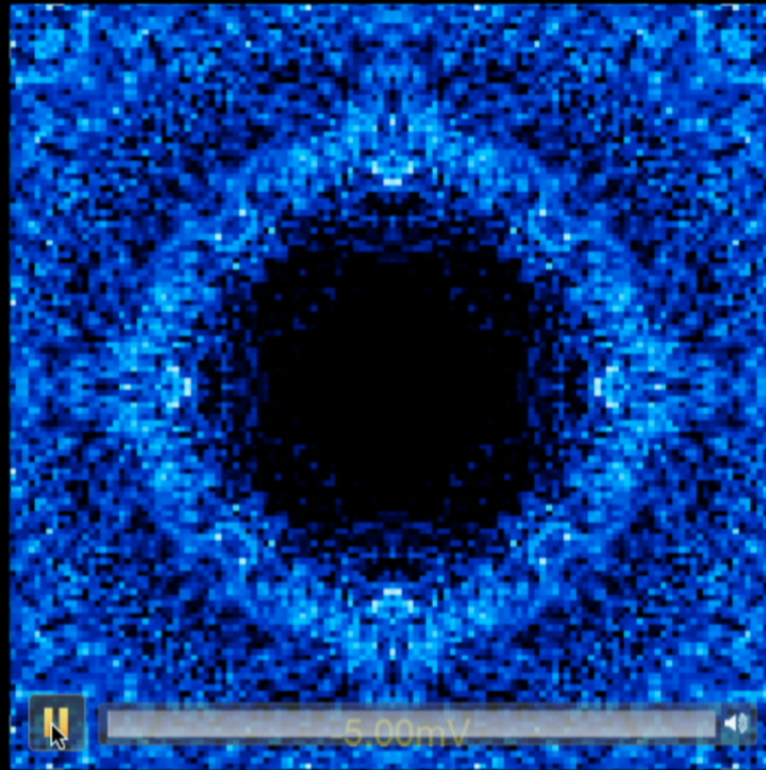
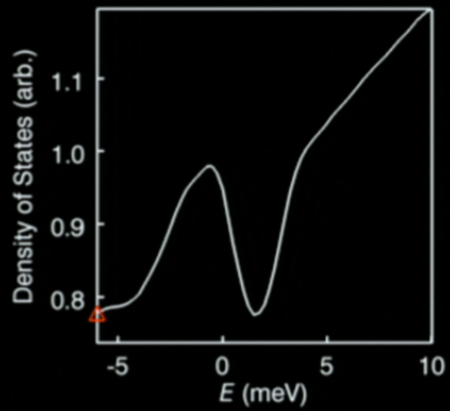


Scattering interference within two 'heavy-fermion' bands



$g(q,E) \rightarrow$ Heavy-Fermion QPI

$(0,\pi/a_0)$

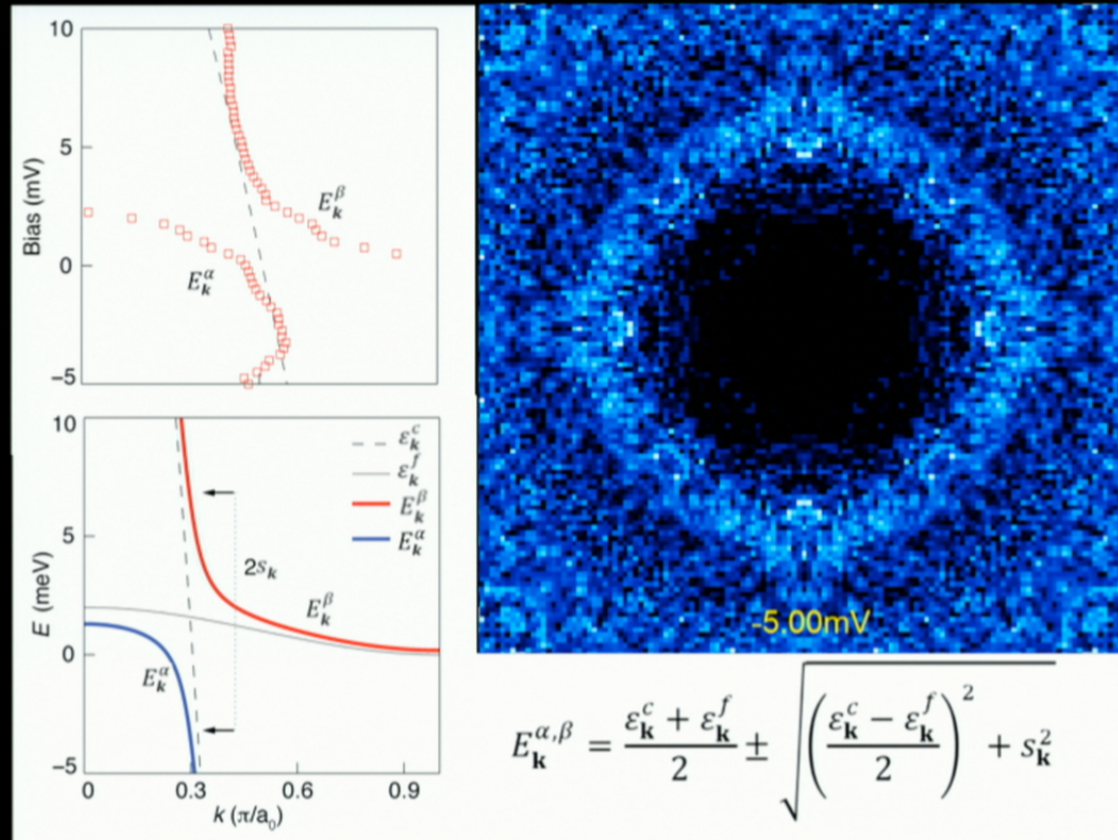


$(\pi/a_0,0)$

Nature 465, 570 (2010)



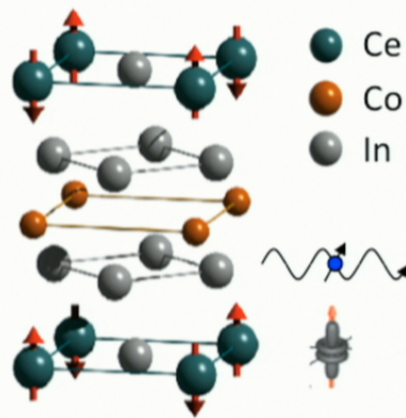
New technique → Measure Heavy-Fermion $E_k^{\alpha,\beta}$



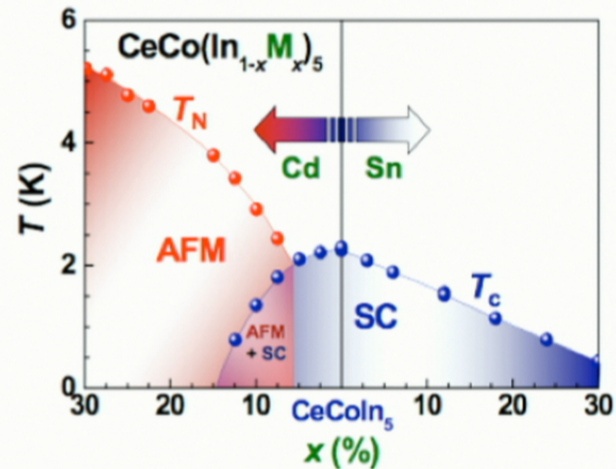
$$E_{\mathbf{k}}^{\alpha,\beta} = \frac{\varepsilon_{\mathbf{k}}^c + \varepsilon_{\mathbf{k}}^f}{2} \pm \sqrt{\left(\frac{\varepsilon_{\mathbf{k}}^c - \varepsilon_{\mathbf{k}}^f}{2}\right)^2 + S_{\mathbf{k}}^2}$$

Nature 465, 570 (2010)

CeCoIn₅ : Canonical Heavy-Fermion Superconductor



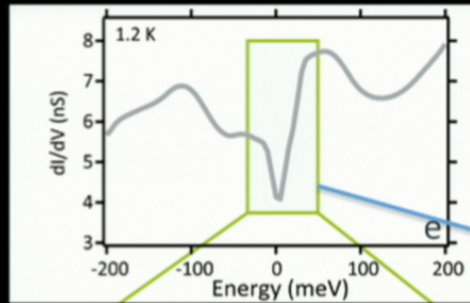
$$\frac{1}{2}c = 3.78 \text{ \AA}$$



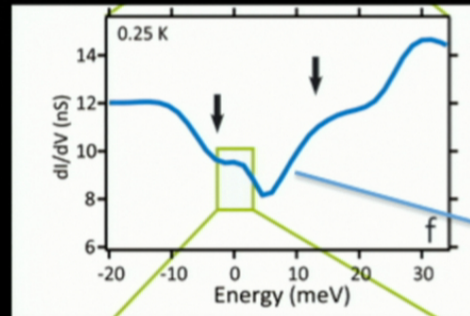
- Antiferromagnetic spin-fluctuations with $q=(\frac{1}{2} \frac{1}{2} \frac{1}{2})$
- $T_c = 2.3\text{K}$ one of highest for any heavy-fermion SC
- Strong evidence for anisotropic gap + nodes
- But $E_k^{\alpha,\beta}$ and $\Delta_k^{\alpha,\beta}$ unknown \Rightarrow pairing mechanism unknown

CeCoIn₅ : Three Energy Scales : ϵ_k^c / $E_k^{\alpha,\beta}$ / $\Delta_k^{\alpha,\beta}$

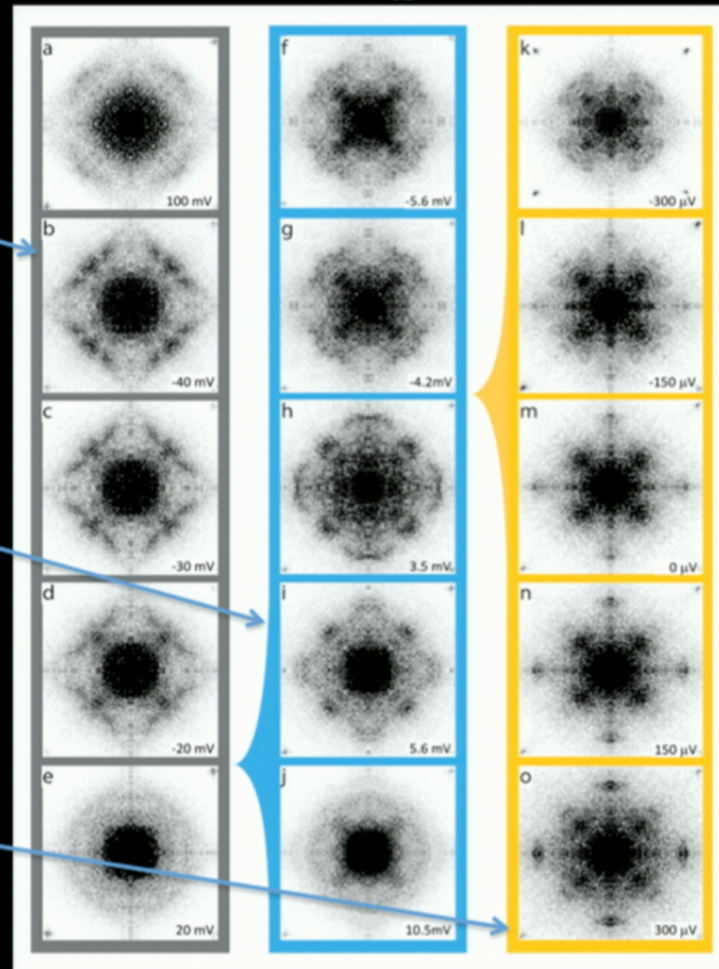
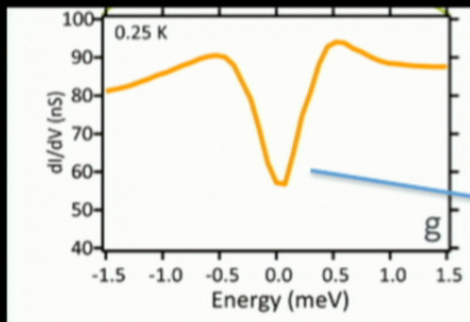
Light Band



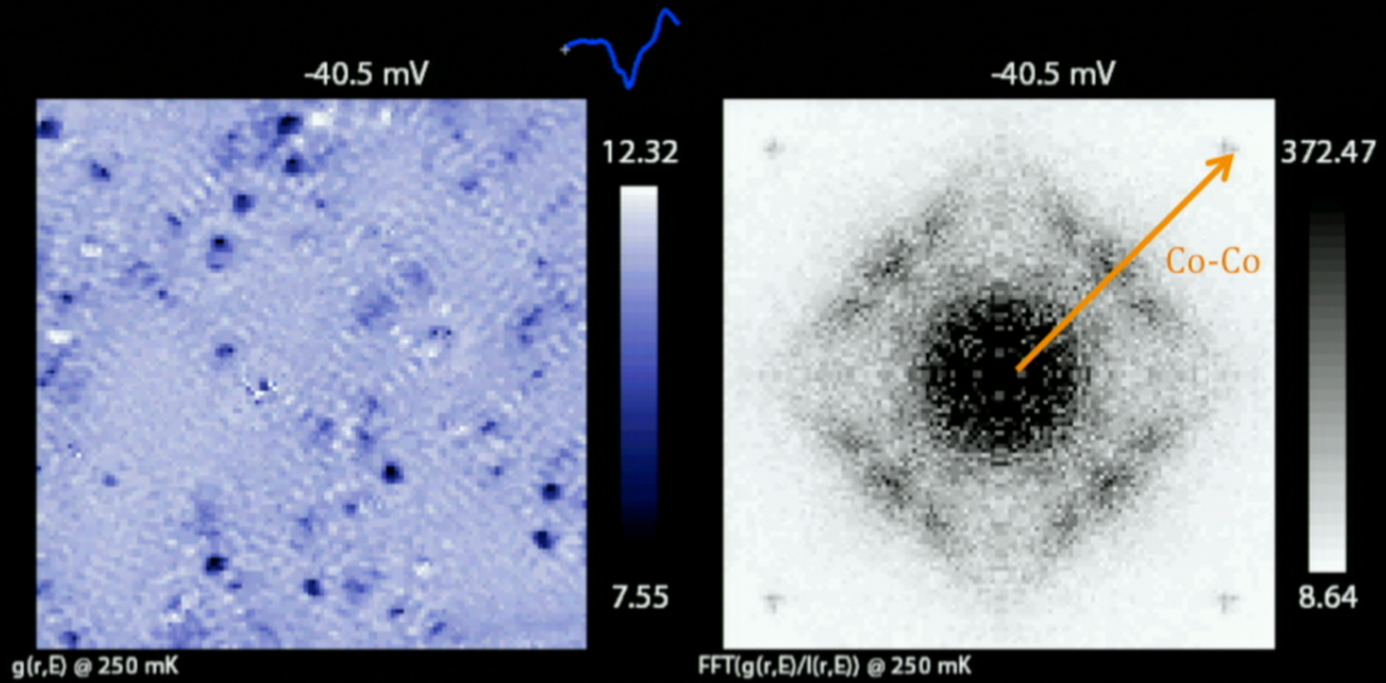
Heavy Bands



SC Gap

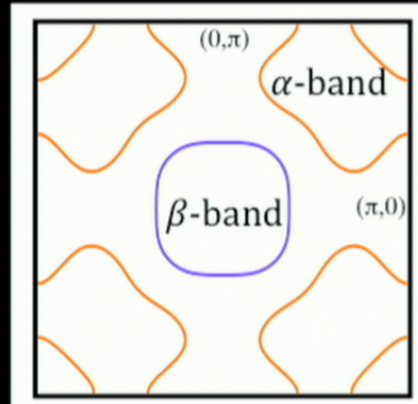
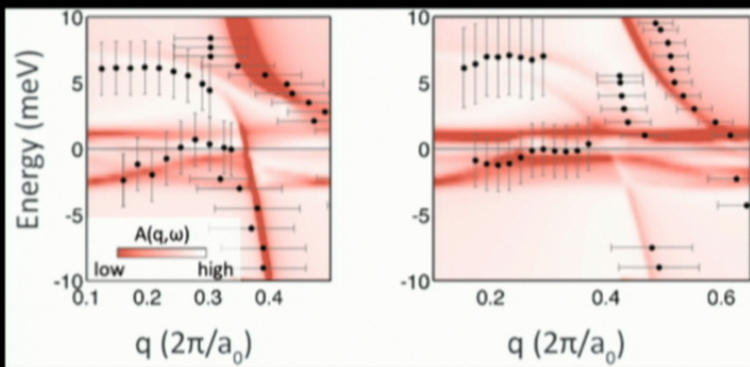
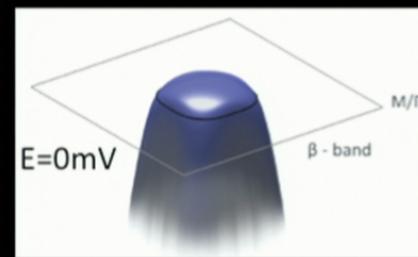
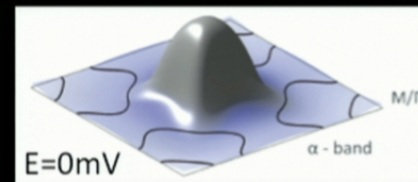
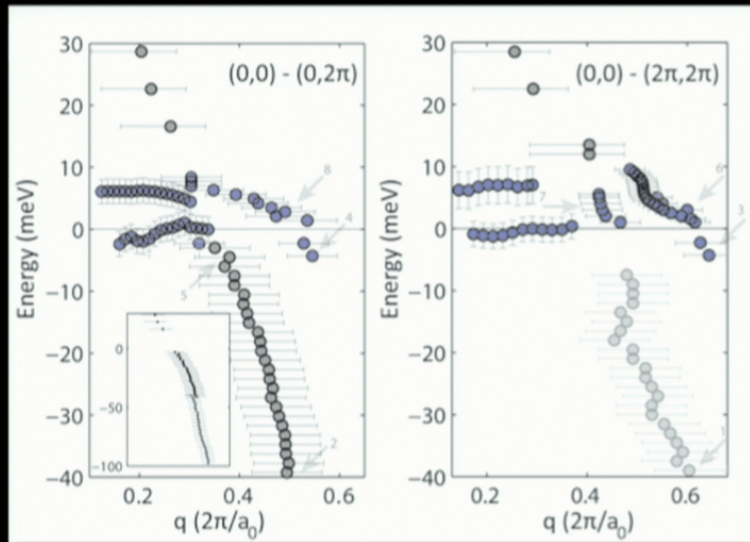
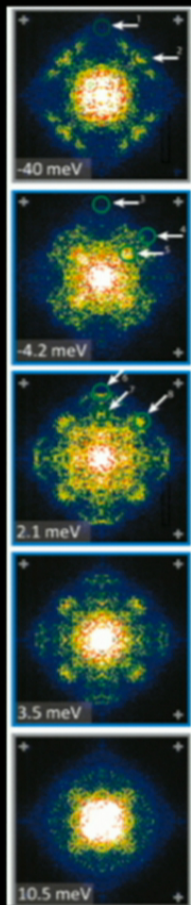


Measure : $\epsilon_k^c / E_k^{\alpha,\beta}$



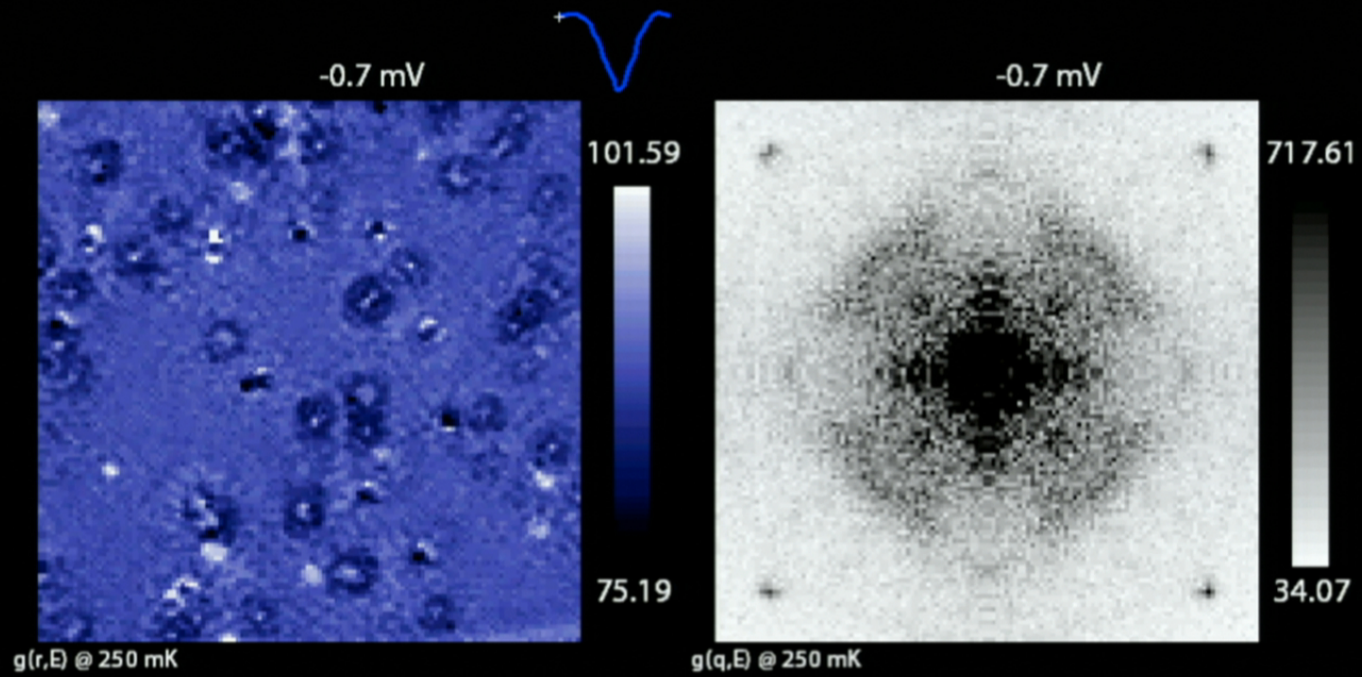
Nature Physics 9, 468 (2013)

Measure : $\epsilon_k^c / E_k^{\alpha,\beta}$



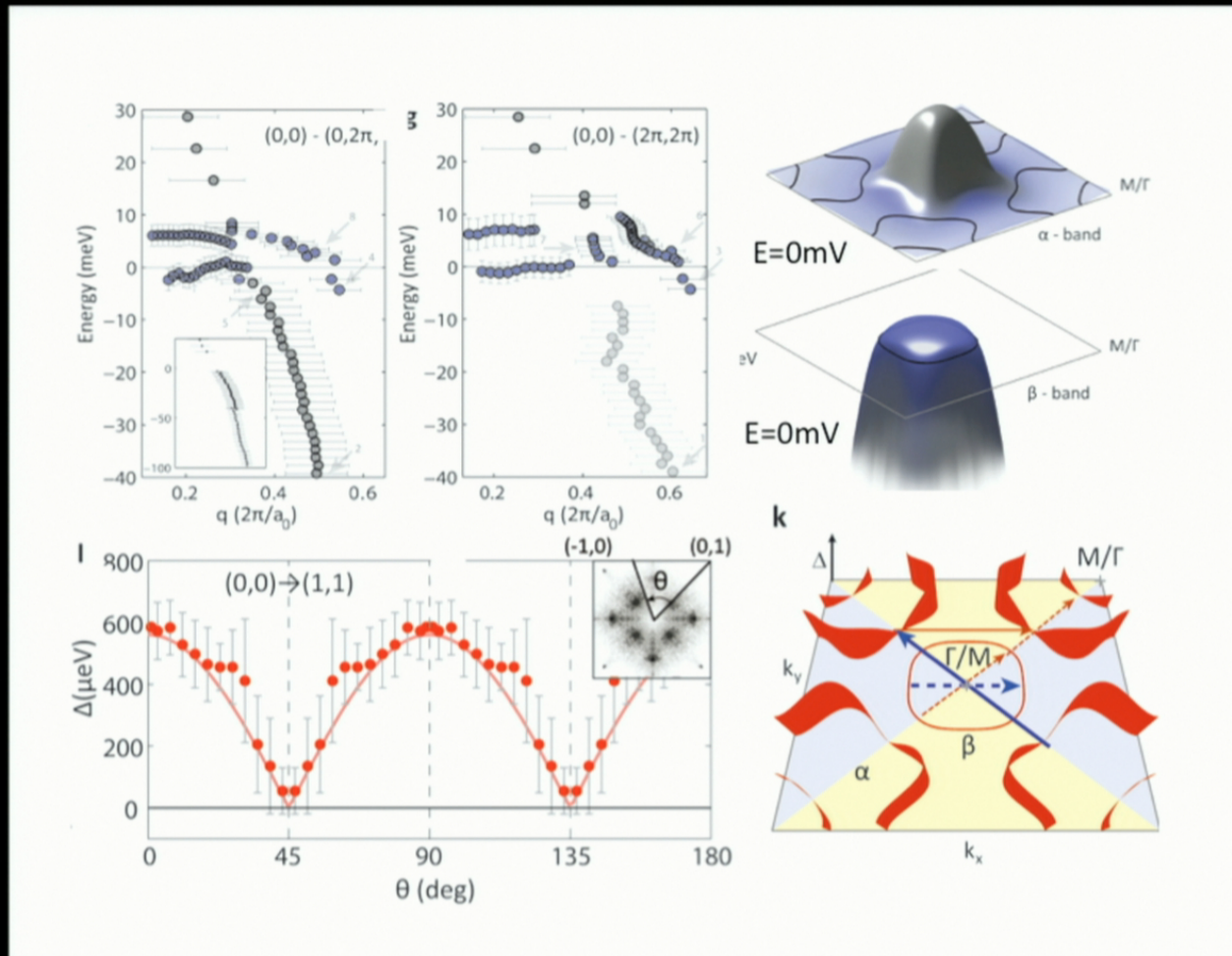
Nature Physics 9, 468 (2013)

Measure : $\epsilon_k^c / E_k^{\alpha,\beta} / \Delta_k^{\alpha,\beta}$



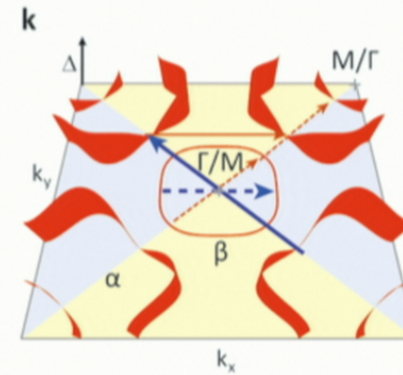
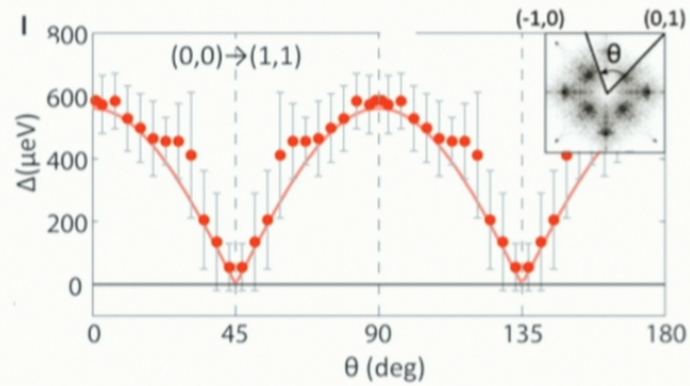
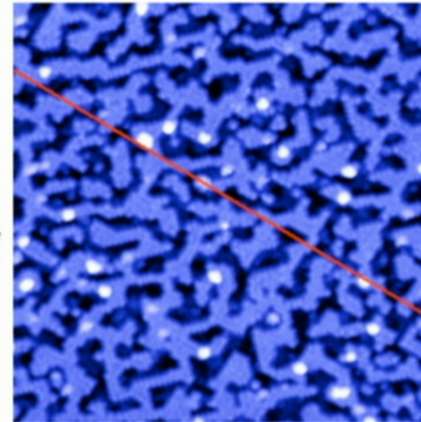
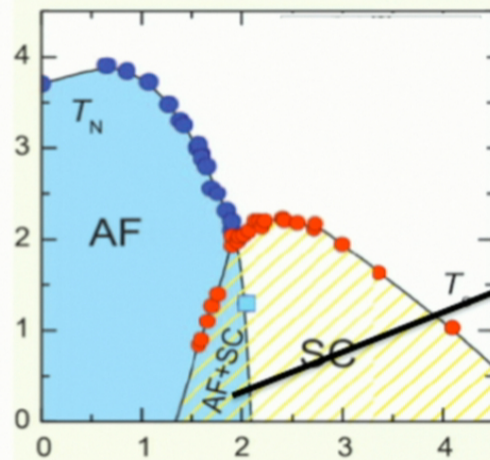
Nature Physics 9, 468 (2013)

Heavy-Fermion Superconductor : ϵ_k^c / $E_k^{\alpha,\beta}$ / $\Delta_k^{\alpha,\beta}$

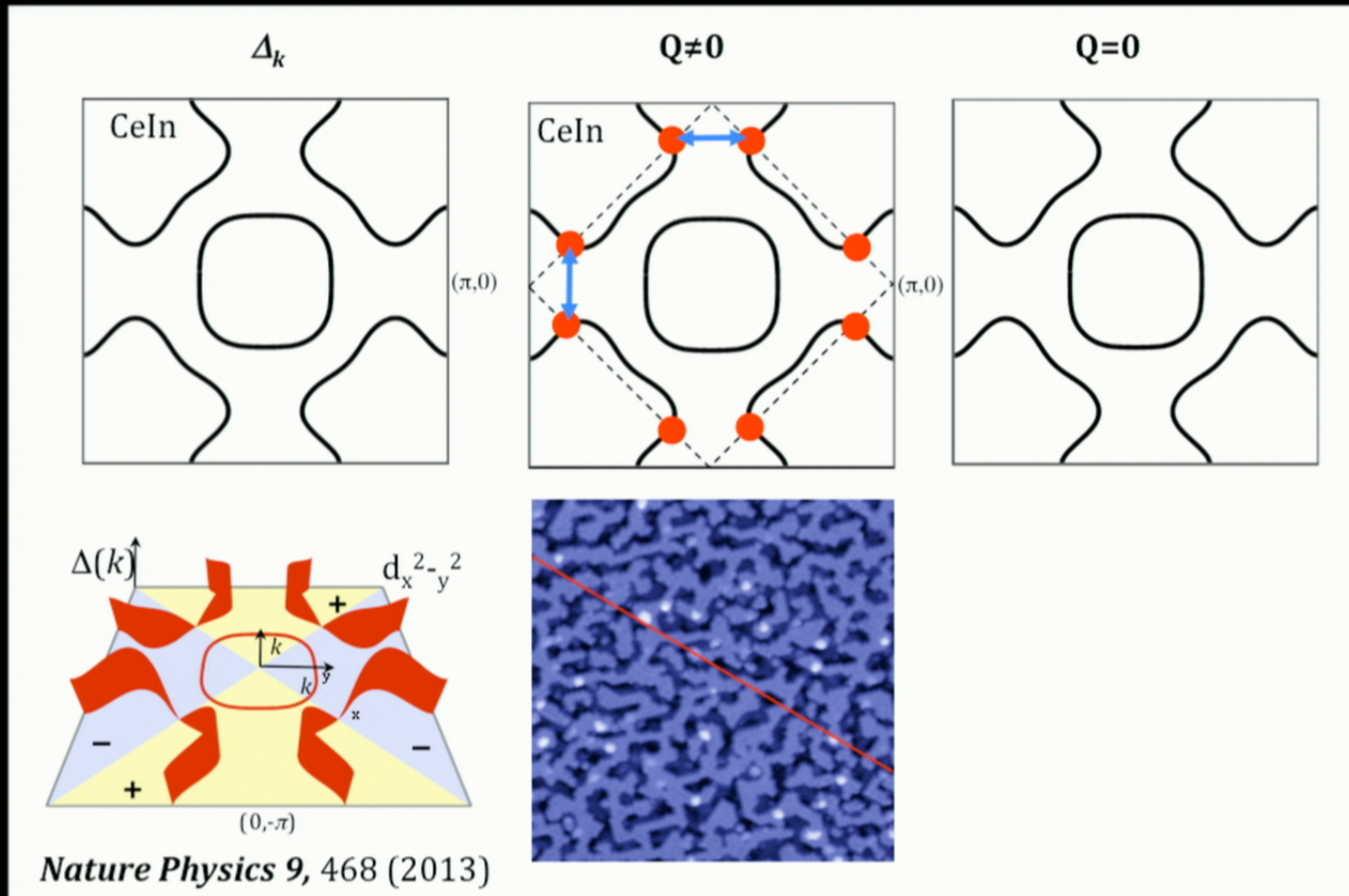


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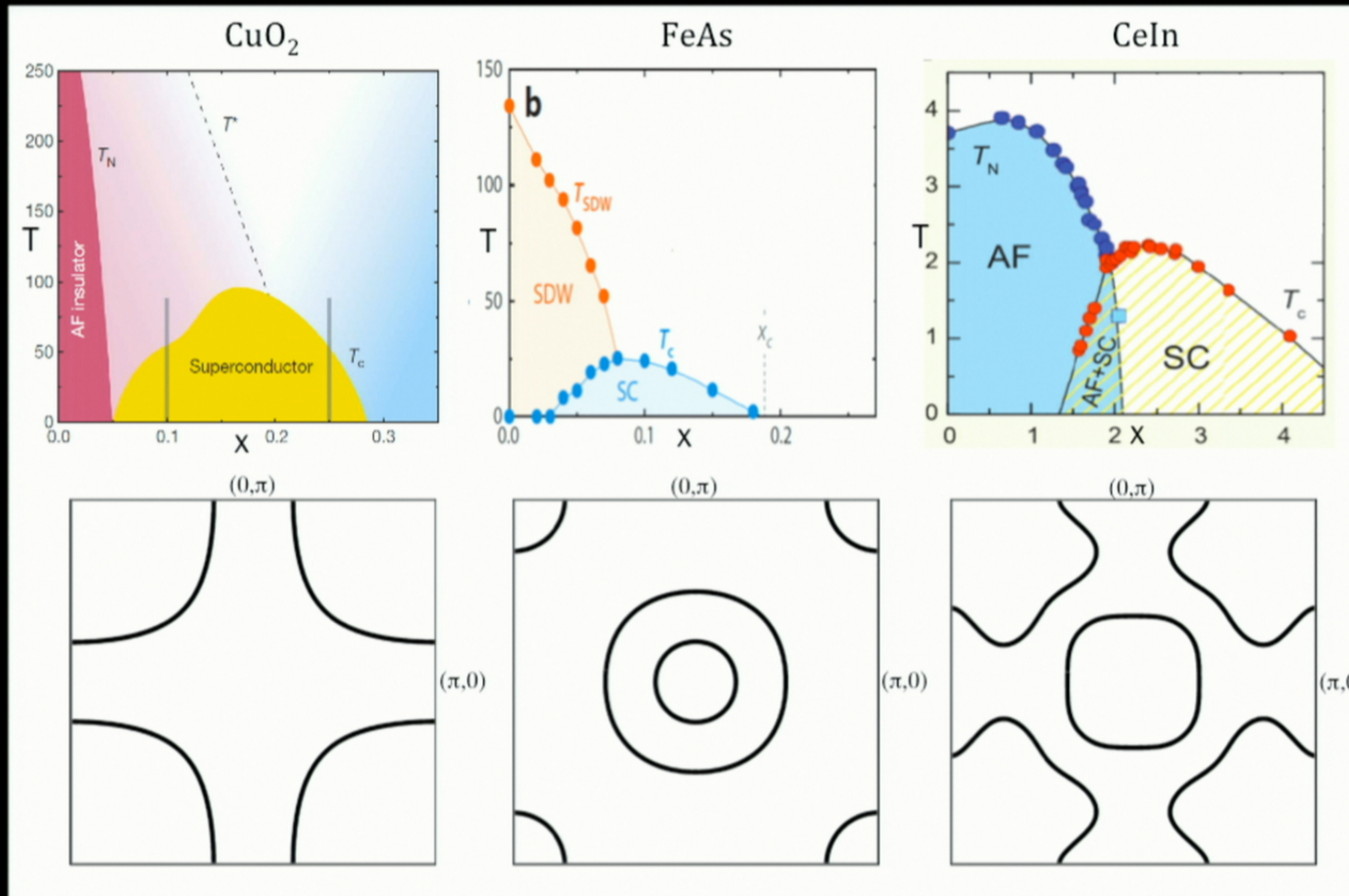
Heavy-Fermion Intertwined Electronic Phases ?



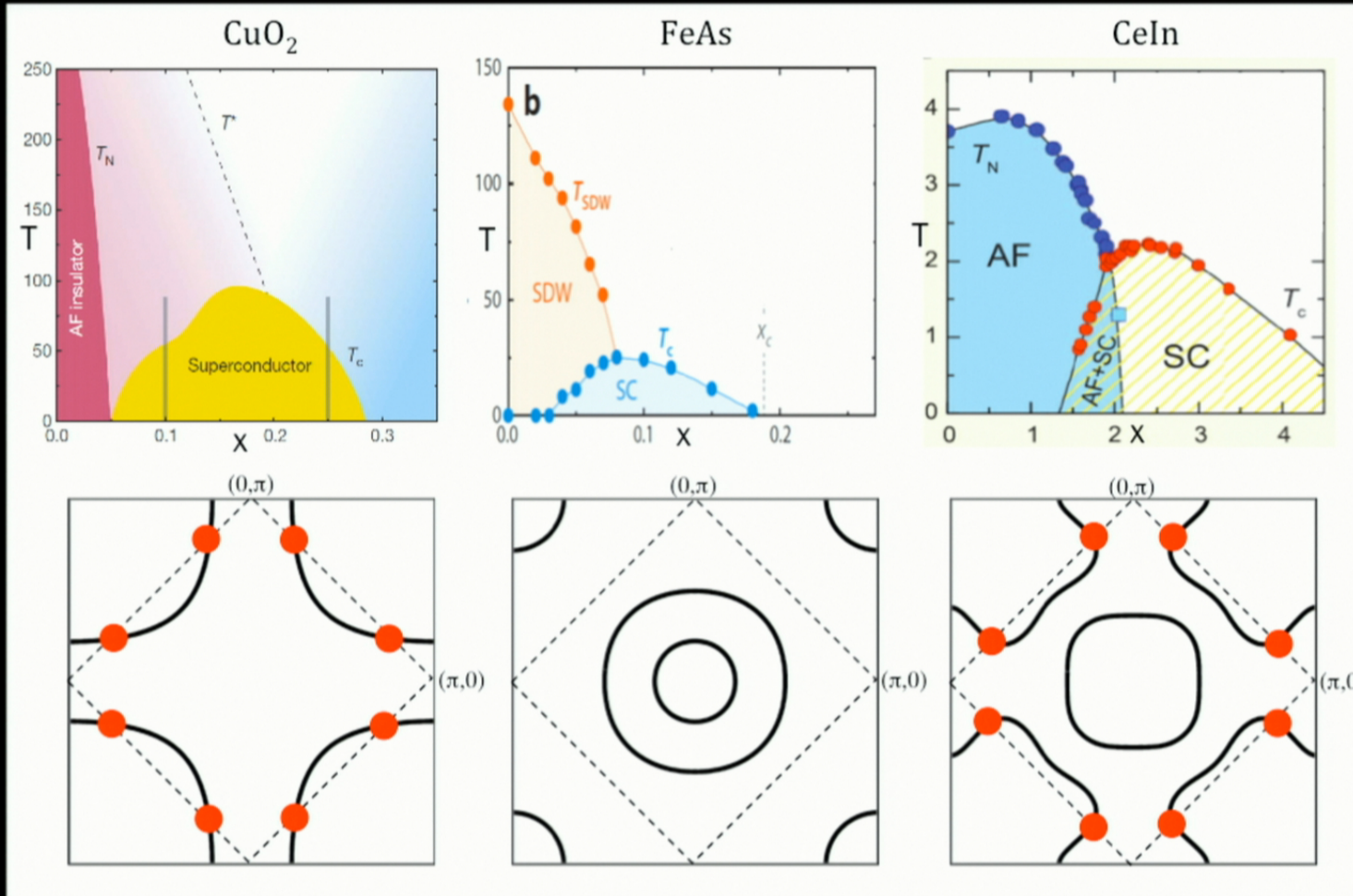
Heavy-fermion Energy Gaps Δ_k & Intertwined Phases



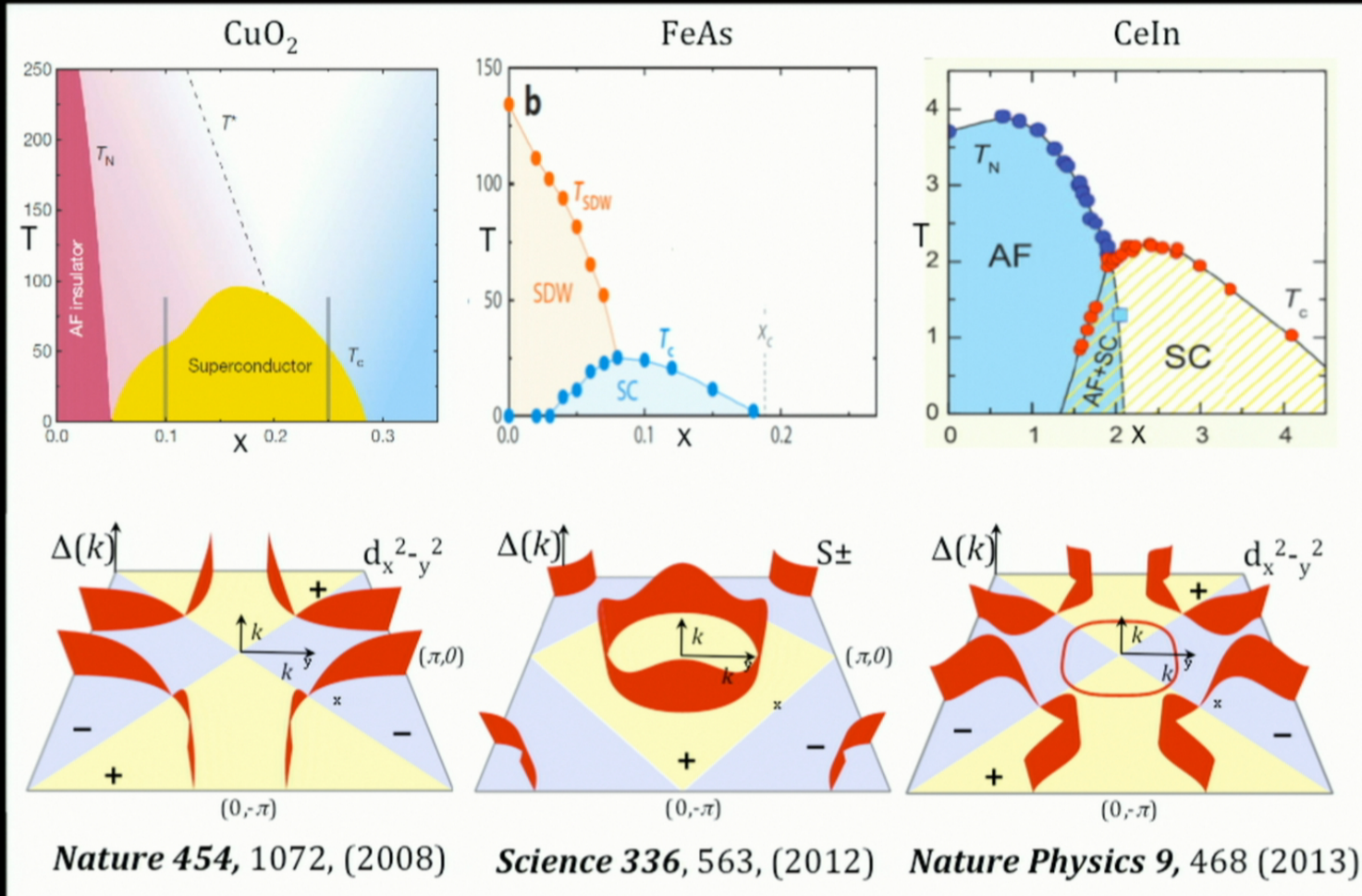
Distinct Fermi Surfaces



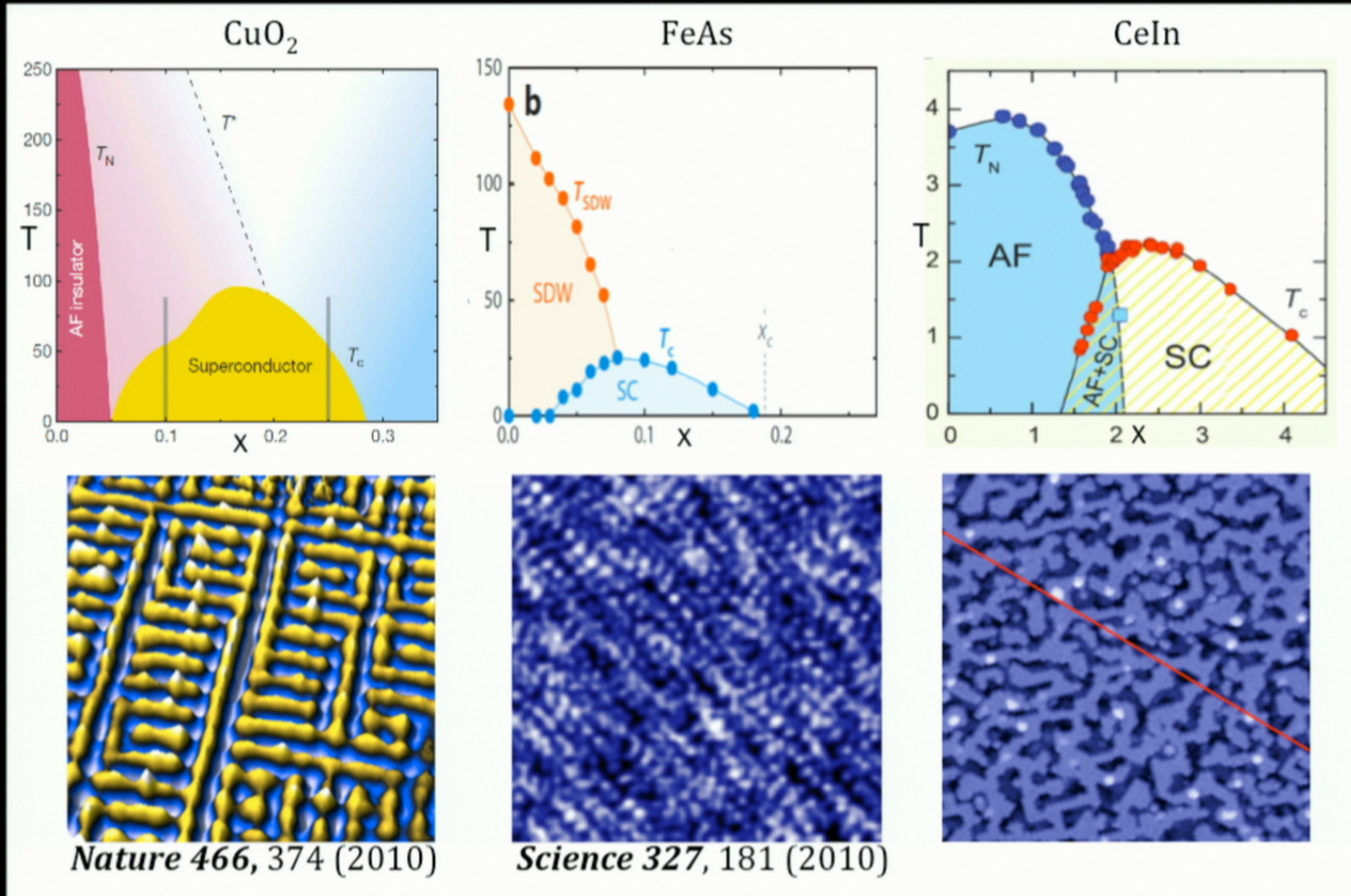
Distinct Antiferromagnetic 'Hot Spots'



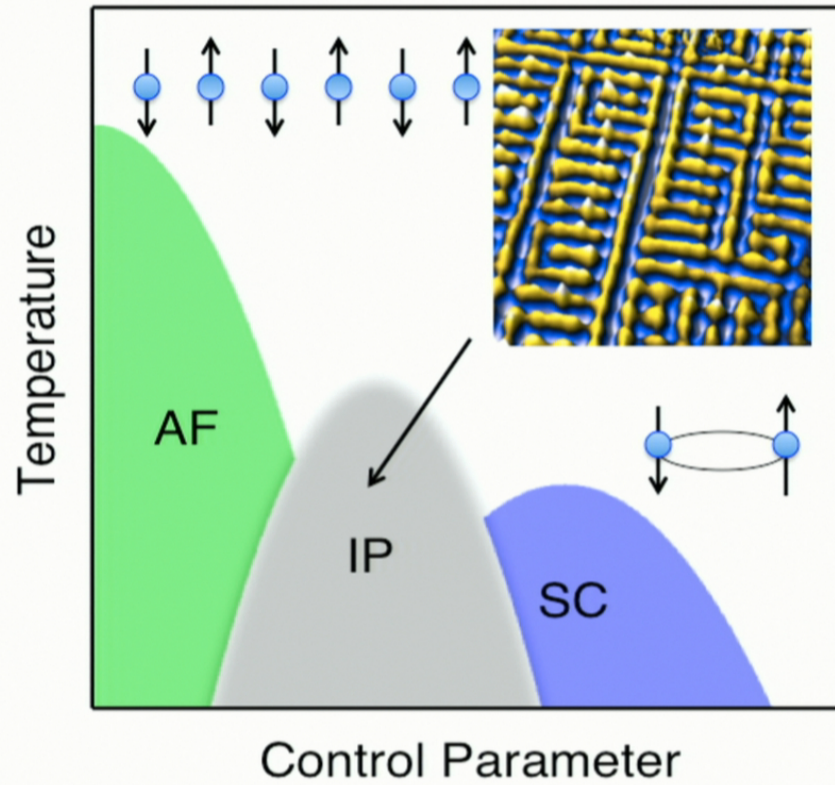
Distinct SC Gap Structure



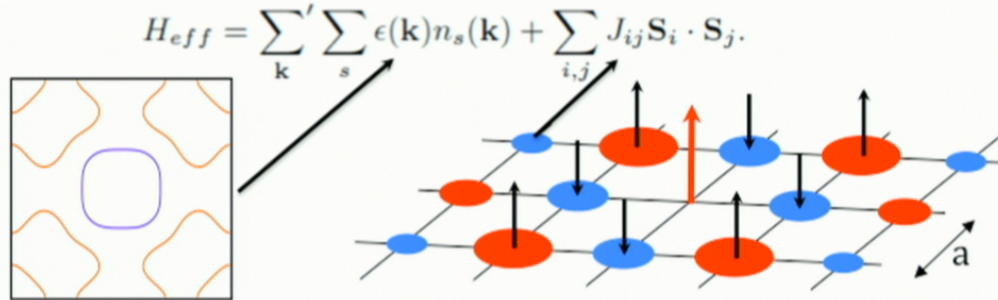
Distinct SC Intertwined Phases



Single Simple Explanation Possible?



CONCEPTUAL FRAMEWORK LINKING AF, IP and SC



$$\sum_{i,j} J_{ij} \vec{S}_i \cdot \vec{S}_j = \frac{1}{A} \sum_{\mathbf{k}, \mathbf{p}, \mathbf{q}} \sum_{s_1, 2, 3, 4} V_{\mathbf{q}}(\mathbf{k}; \mathbf{p}) \psi_{\mathbf{k}+\mathbf{q}, s_1}^\dagger \vec{\sigma}_{s_1, s_2} \psi_{\mathbf{k}, s_2} \cdot \psi_{\mathbf{p}-\mathbf{q}, s_3}^\dagger \vec{\sigma}_{s_3, s_4} \psi_{\mathbf{p}, s_4}; \quad [3]$$

where

$$V_{\mathbf{q}}(\mathbf{k}; \mathbf{p}) = J(\mathbf{q}) \{ \phi_{\alpha(\mathbf{k}+\mathbf{q})}^*(\mathbf{k} + \mathbf{q}) \cdot \phi_{\alpha(\mathbf{k})}(\mathbf{k}) \} \times \{ \phi_{\alpha(\mathbf{p}-\mathbf{q})}^*(\mathbf{p} - \mathbf{q}) \cdot \phi_{\alpha(\mathbf{p})}(\mathbf{p}) \}.$$

Here A is the total area, ϕ is the band eigen wavefunctions in the orbital basis, and $J(\mathbf{q})$ is the Fourier transform of J_{ij} . For the copper-based, iron-based, and heavy fermion superconductors $J(\mathbf{q})$ is taken to be an over all coupling strength J_{eff} times the following form factors:

$$\begin{aligned} & \cos k_x + \cos k_y \text{ (copper - based)} \\ & \cos \theta (\cos k_x + \cos k_y) + \sin \theta (2 \cos k_x \cos k_y) \text{ (iron - based)} \\ & \cos k_x + \cos k_y \text{ (heavy - fermion),} \end{aligned} \quad [4]$$

The next step is to decouple Eq. (3) in the particle-particle (for Cooper pairing) and particle-hole (for charge and spin density wave and Pomeranchuk). The “first-instability-mode analysis” described in section I-III allows us to determine the functional form of the order parameter. However it does not fix the overall magnitude. Once the functional form is determined we use the mean-field Hamiltonians described in section I-III to determine the energy gaps, fermi surface distortions,

- Determine using a single Hamiltonian (but different Fermiology)

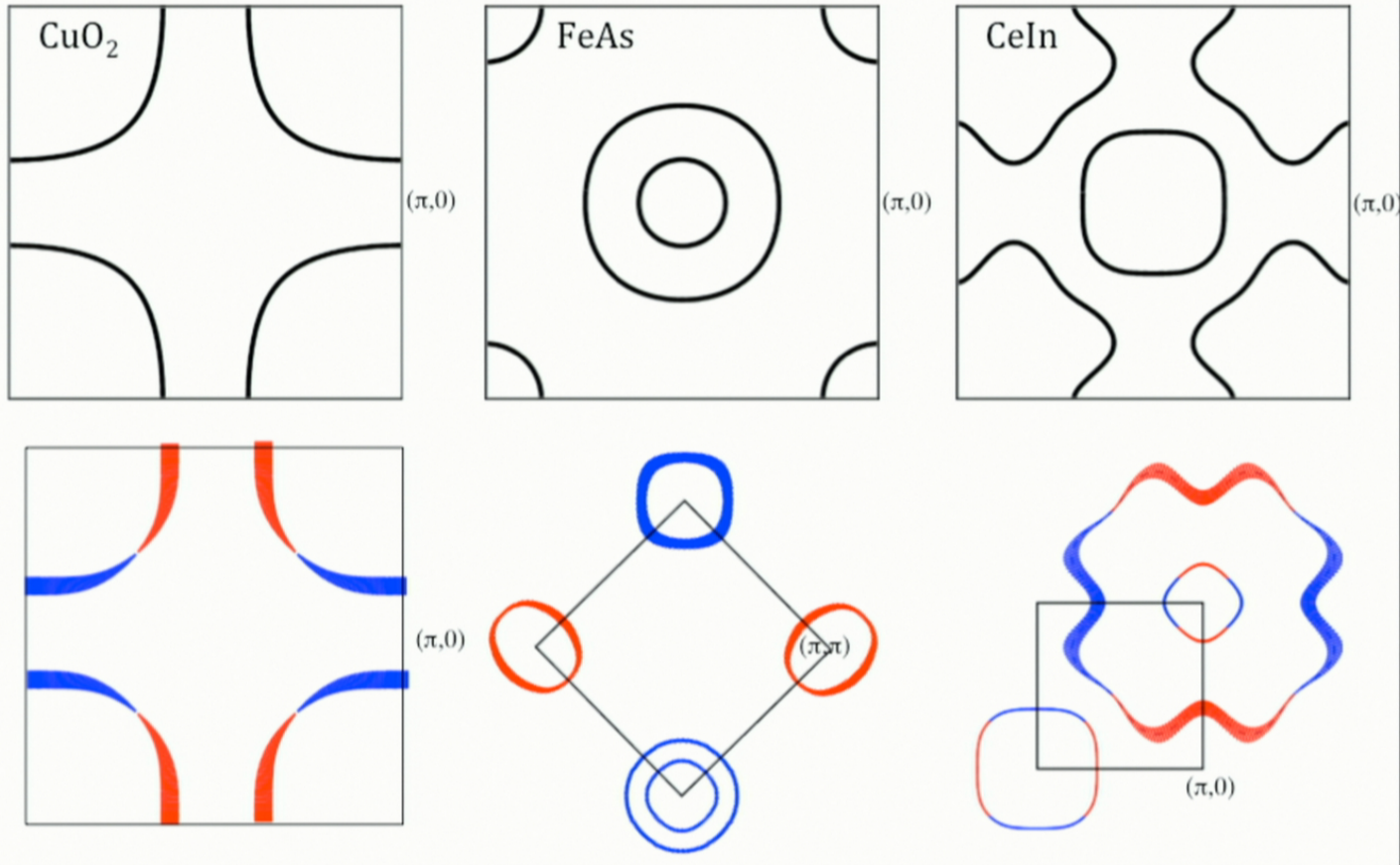
 - I SC Order Parameters
 - II $Q=0$ IUC Order Parameters
 - III $Q \neq 0$ CDW Order Parameters
 - IV $Q \neq 0$ SDW Order Parameters

for cuprates/pnictides/heavy fermions.

Concepts Relating Magnetic Interactions, Intertwined Electronic Orders and Strongly Correlated Superconductivity, J.C. Davis & D.-H. Lee, *PNAS* **110**, 17623 (2013)

Predict Δ_k Energy Gaps

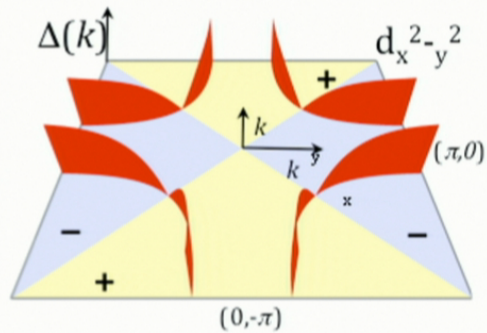
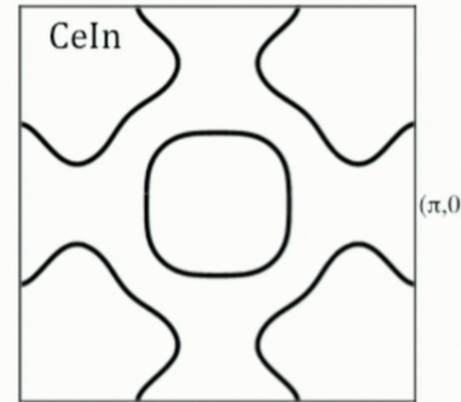
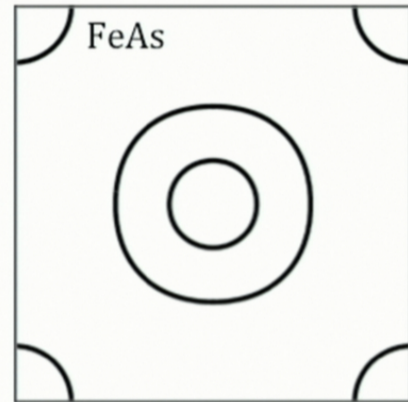
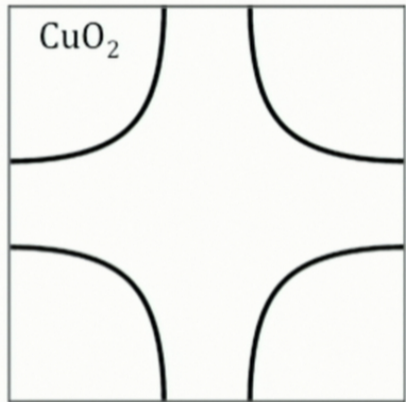
$$H_{eff} = \sum_{\mathbf{k}} \sum_s \epsilon(\mathbf{k}) n_s(\mathbf{k}) + \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j.$$



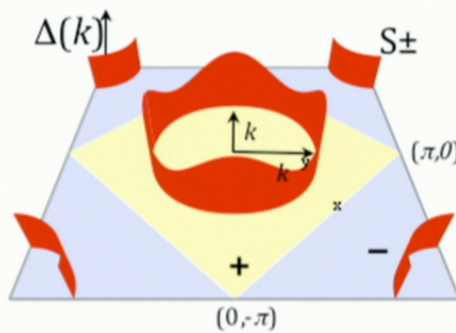
*Concepts Relating Magnetic Interactions, Intertwined Electronic Orders and Strongly Correlated Superconductivity, J.C. Davis & D.-H. Lee, **PNAS** **110**, 17623 (2013)*

Measured Δ_k Energy Gaps

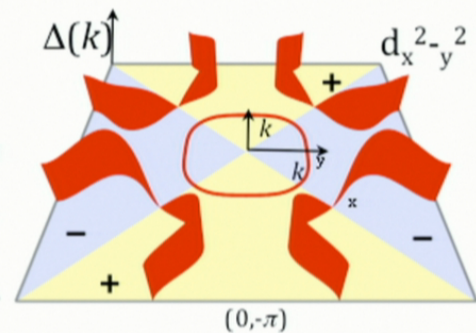
$$H_{eff} = \sum_{\mathbf{k}} \sum_s \epsilon(\mathbf{k}) n_s(\mathbf{k}) + \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j.$$



Nature **454**, 1072, (2008)



Science **336**, 563, (2012)

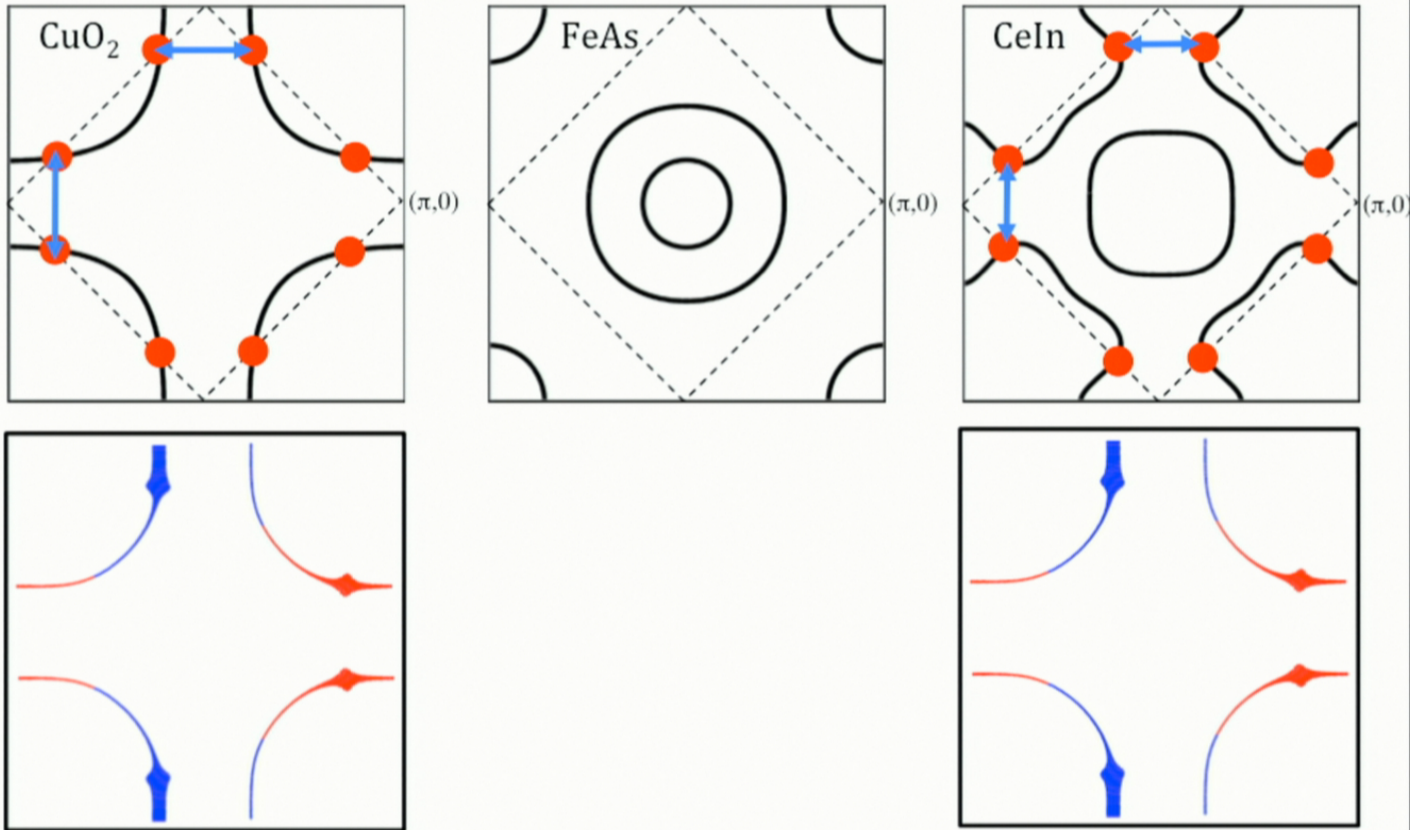


Nature Physics **9**, 468 (2013)

Concepts Relating Magnetic Interactions, Intertwined Electronic Orders and Strongly Correlated Superconductivity, J.C. Davis & D.-H. Lee, *PNAS* **110**, 17623 (2013)

Predicted Q≠0 Broken Symmetry (Density Wave) Phases

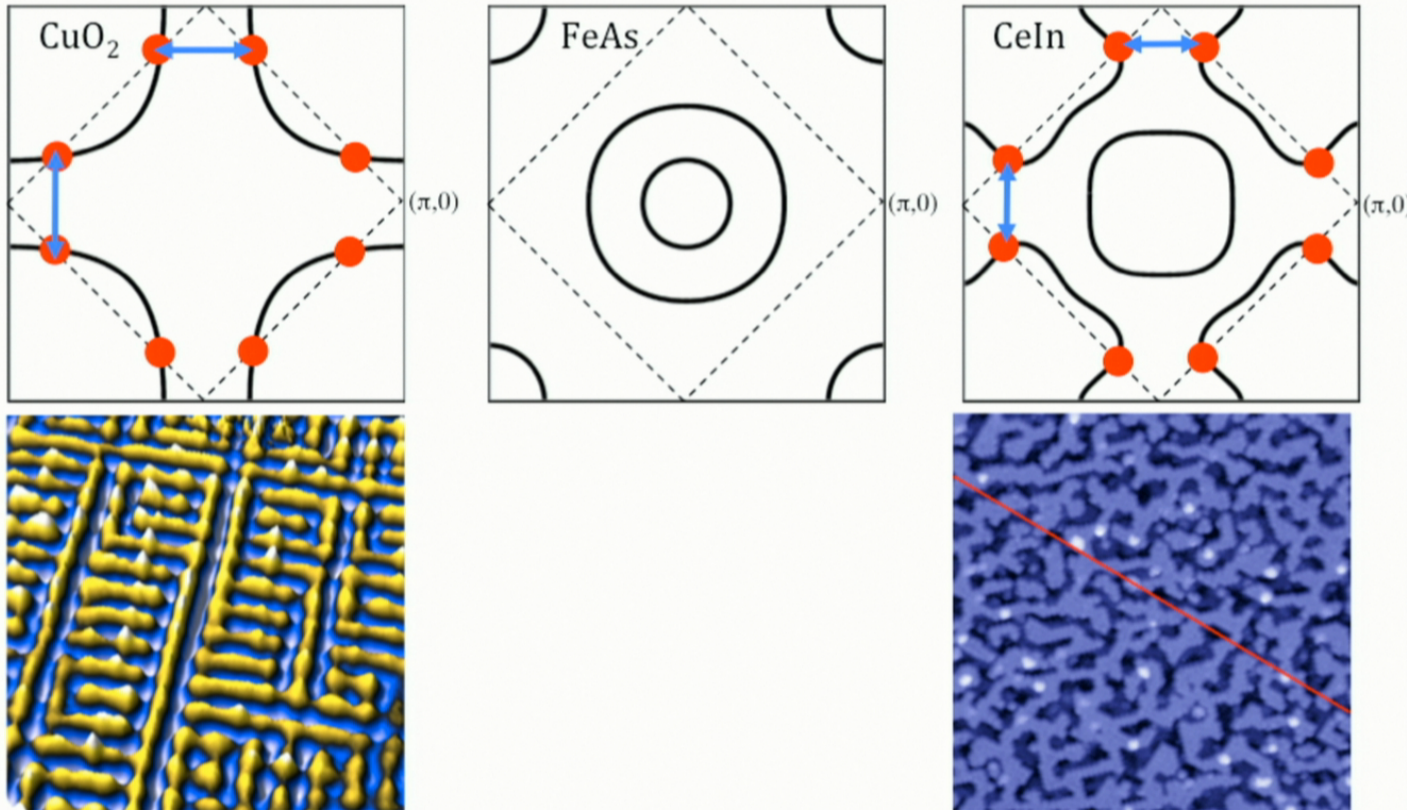
$$H_{eff} = \sum_{\mathbf{k}} \sum_s \epsilon(\mathbf{k}) n_s(\mathbf{k}) + \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j.$$



Concepts Relating Magnetic Interactions, Intertwined Electronic Orders and Strongly Correlated Superconductivity, J.C. Davis & D.-H. Lee, PNAS 110, 17623 (2013)

Measured $Q \neq 0$ Broken d-Form Factor Density Waves

$$H_{eff} = \sum_{\mathbf{k}} \sum_s \epsilon(\mathbf{k}) n_s(\mathbf{k}) + \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j.$$

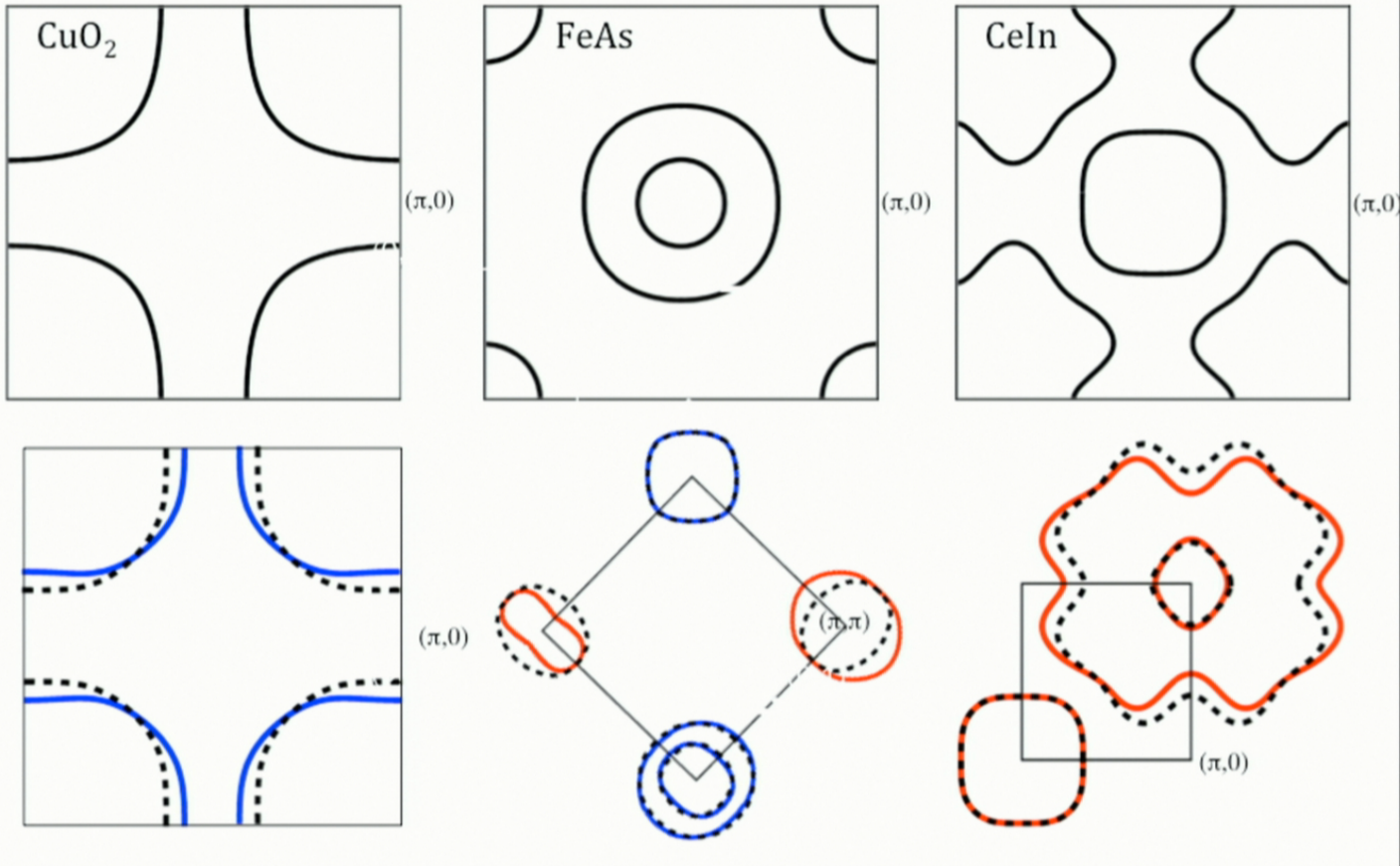


Science **315**, 1380 (2007)

Concepts Relating Magnetic Interactions, Intertwined Electronic Orders and Strongly Correlated Superconductivity, J.C. Davis & D.-H. Lee, *PNAS* **110**, 17623 (2013)

Predicted Q=0 Broken Symmetry (Nematic) Phases

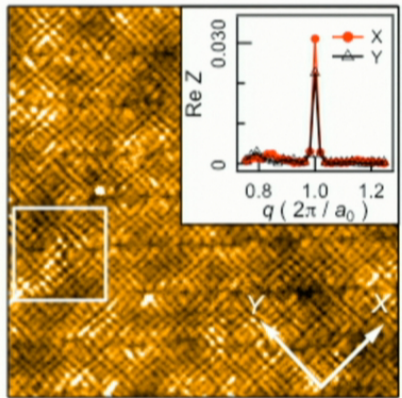
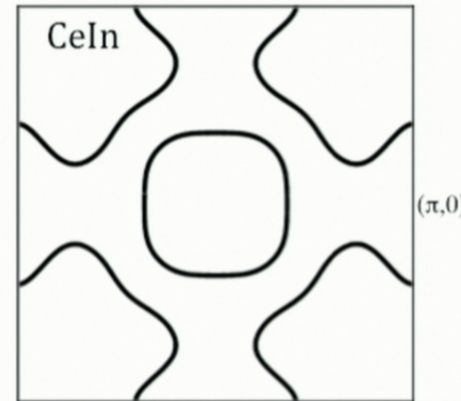
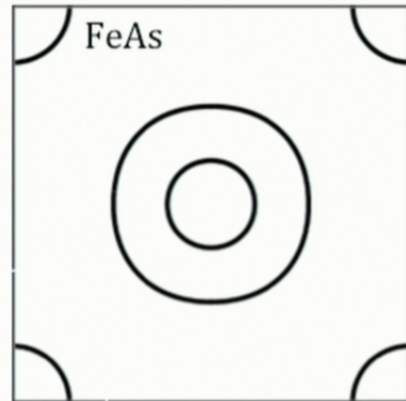
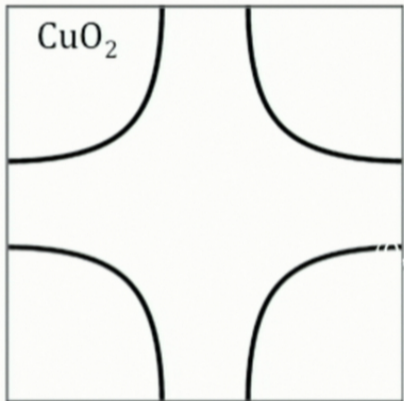
$$H_{eff} = \sum_{\mathbf{k}} \sum_s \epsilon(\mathbf{k}) n_s(\mathbf{k}) + \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j.$$



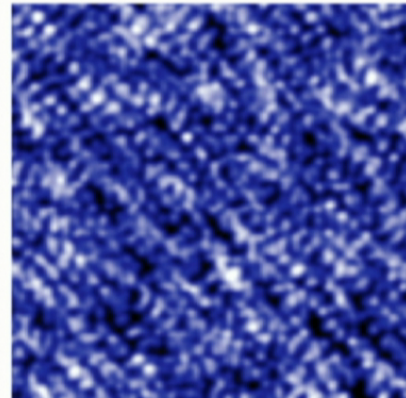
Concepts Relating Magnetic Interactions, Intertwined Electronic Orders and Strongly Correlated Superconductivity, J.C. Davis & D.-H. Lee, PNAS 110, 17623 (2013)

Measured Q=0 Broken Symmetry (Nematic) Phases

$$H_{eff} = \sum_{\mathbf{k}} \sum_s \epsilon(\mathbf{k}) n_s(\mathbf{k}) + \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j.$$



Nature 466, 324 (2010)



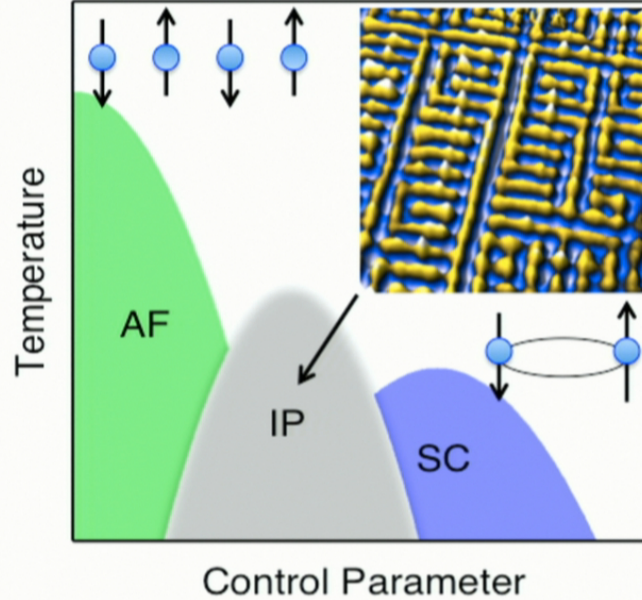
Science 327, 181 (2010)

Concepts Relating Magnetic Interactions, Intertwined Electronic Orders and Strongly Correlated Superconductivity, J.C. Davis & D.-H. Lee, PNAS 110, 17623 (2013)

'Unified' Model Linking AF, IP and SC across HTS Materials

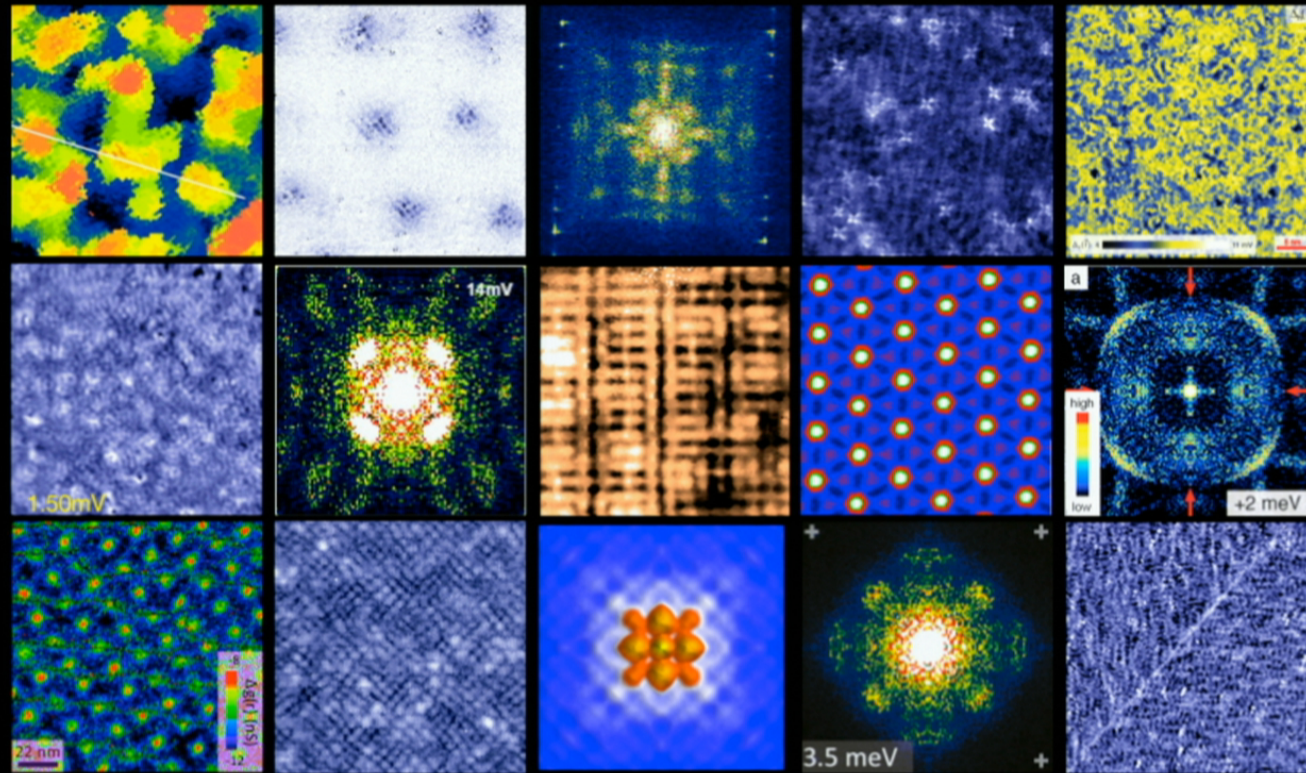


$$H_{eff} = \sum_{\mathbf{k}} \sum_s \epsilon(\mathbf{k}) n_s(\mathbf{k}) + \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j.$$



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THANKS!



Cornell University

J.C. Séamus Davis

BROOKHAVEN
NATIONAL LABORATORY



St. Andrews