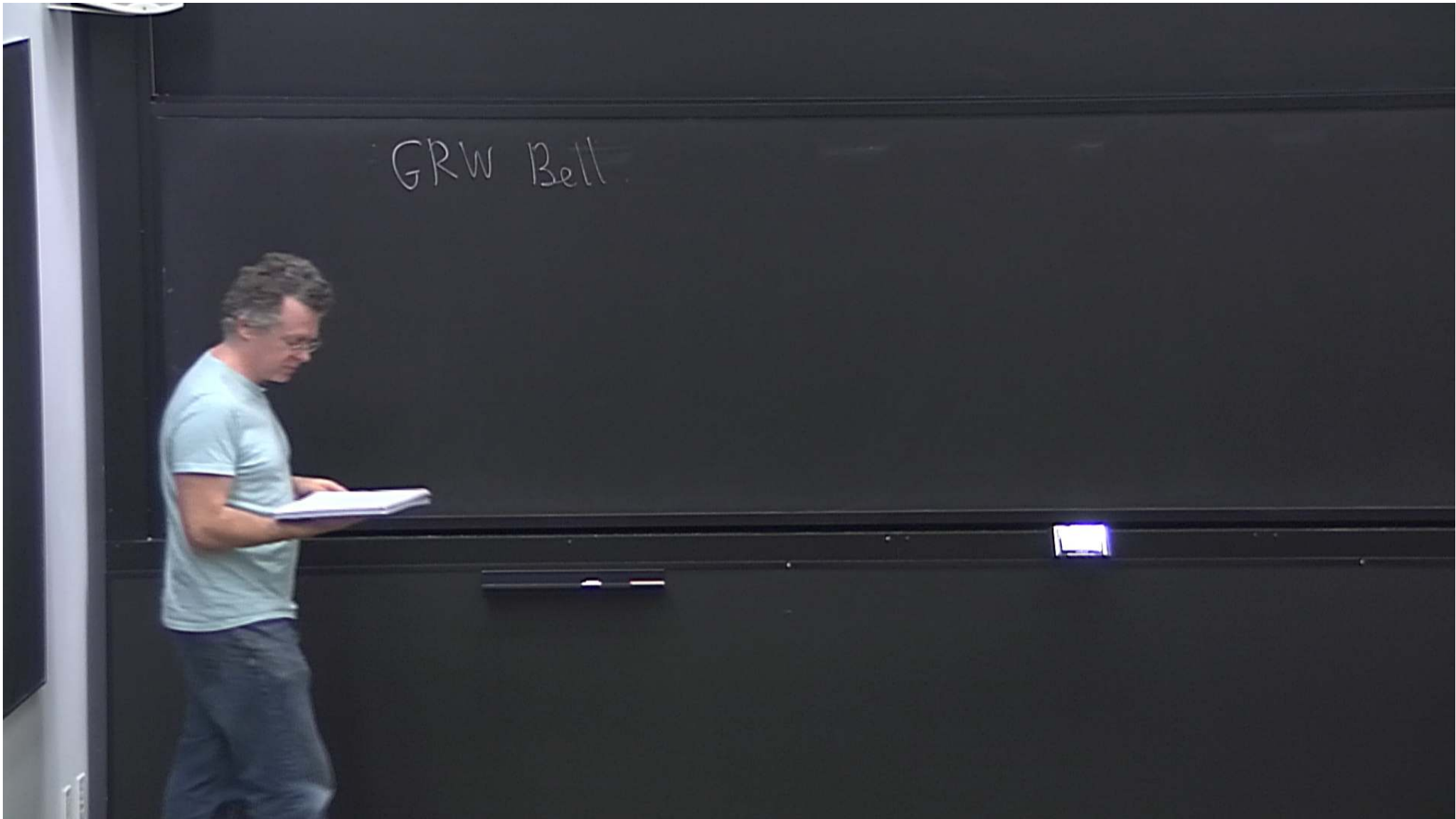


Title: Foundations of Quantum Mechanics-9

Date: Jan 15, 2015 11:30 AM

URL: <http://pirsa.org/15010048>

Abstract:



# GRW Bell

ontology

(a)  $\Psi(\vec{r}_1, \vec{r}_2, \dots, \vec{r}_N, t)$

(b) a way to get local beables  
Dynamics. Schrödinger evolution.

# GRW Bell

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(a)  $\Psi(\vec{\Gamma}_1, \vec{\Gamma}_2, \dots, \vec{\Gamma}_N, t)$

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Dynamics. (a) Schrödinger evolution.

(b) jumps.



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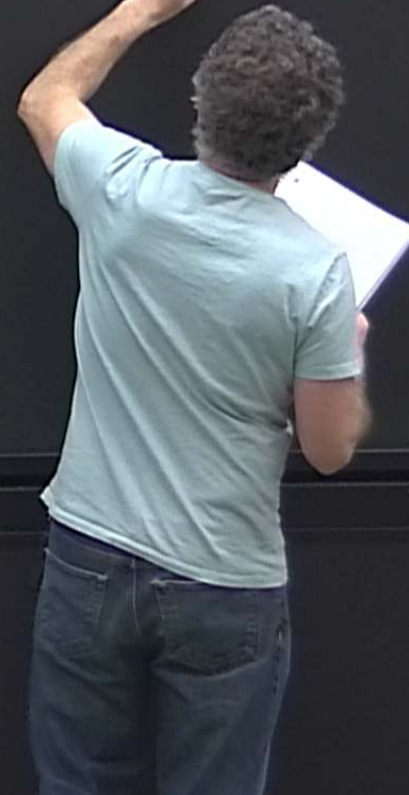
(b) a way to get local beables

Dynamics. (a) Schrödinger evolution.

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More details on jump process.

(i) The



# GRW Bell

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More details on jump process.

- (i) The probability per unit time for a jump is  $\frac{N}{T}$  where

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More details on jump process.

(i) The probability per unit time for a jump  
is  $\frac{N}{\tau}$  where  $N$  is the number of particles  
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- (i) The probability per unit time for a jump is  $\frac{N}{\tau}$  where  $N$  is the number of particles and  $\tau$  is a new constant of nature.

$$\text{prob} \left( \begin{array}{l} m \text{ evals} \\ \text{in time } T \end{array} \right) = \frac{e^{-\left(\frac{N}{\tau}T\right)} \left(\frac{N}{\tau}T\right)^m}{m!}$$

(b) jumps.

(ii) The jump is

$$\psi \rightarrow \frac{j(\vec{x} - \vec{r}_n) \psi(\vec{r}_1, \dots, \vec{r}_N, t)}{R_n(\vec{x})}$$

where  $n$  is chosen randomly from 1 to  $N$

and

$$\int d^3\vec{x} |j(\vec{x})|^2 = 1$$

and

$$|R_n(x)|^2 = \int d^3\vec{r}_1 d^3\vec{r}_2 \dots d^3\vec{r}_n |j(x-\vec{r}_n) \Psi|^2$$

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(iii) The collapse centre,  $\vec{x}$ , is chosen with probability,

$$d^3\vec{x} |R_n(x)|^2$$

and  $|R_n(x)|^2 = \int d^3\vec{r}_1 d^3\vec{r}_2 \dots d^3\vec{r}_n |j(x - \vec{r}_n) \Psi|^2$

(iii) The collapse centre,  $\vec{x}$ , is chosen with probability,

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(iii) usual choice is

$$j(x) = k \exp\left(-\frac{x^2}{2a^2}\right)$$

where  $a$  is another constant of nature.

and

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(v) GRW suggested

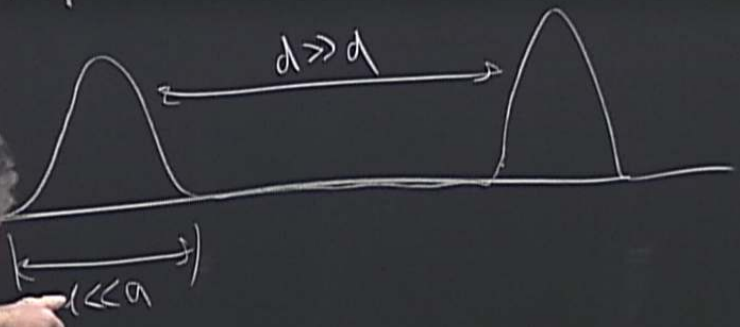
$$\tau = 10^{15} \text{ sec} \approx 10^8 \text{ years}$$

$$a = 10^{-5} \text{ cm}$$

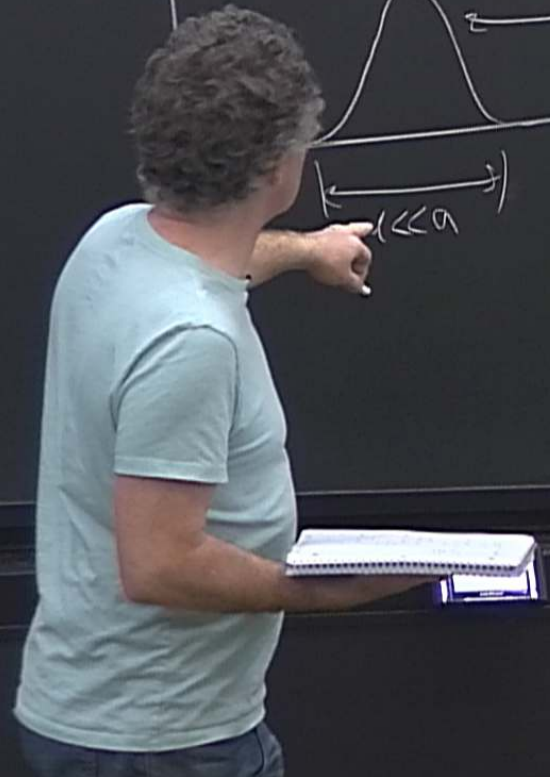
$$j(x) = K e^{-x/2a^2}$$

Superposition for a particle

$10^8$  years



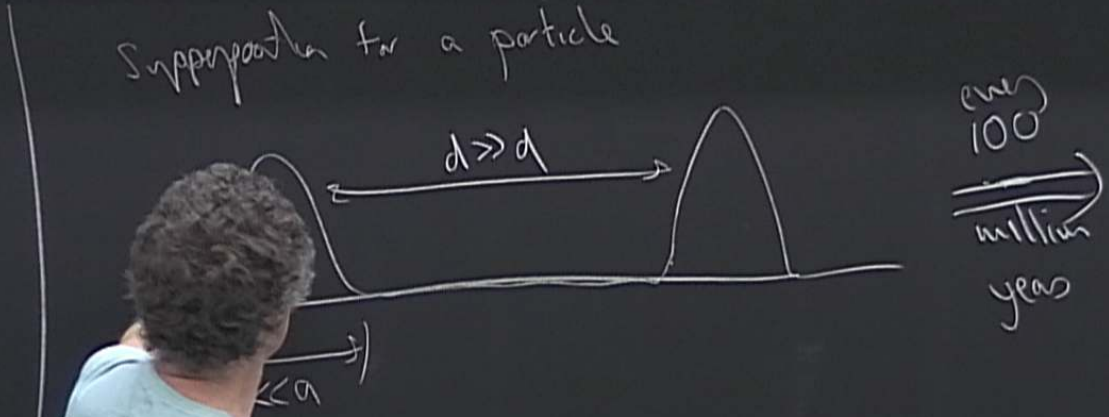
over  
100  
million  
years



$$j(x) = K e^{-\lambda(x - \frac{1}{2a^2})}$$

Superposition for a particle

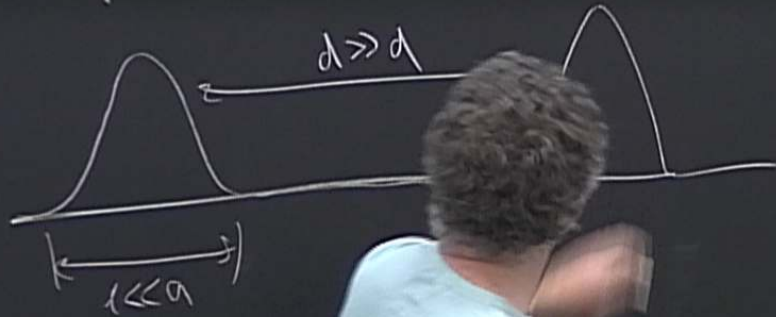
$10^8$  years



over  
100  
million  
years

$$j(x) = K e^{-x/a} (1/2a^2)$$

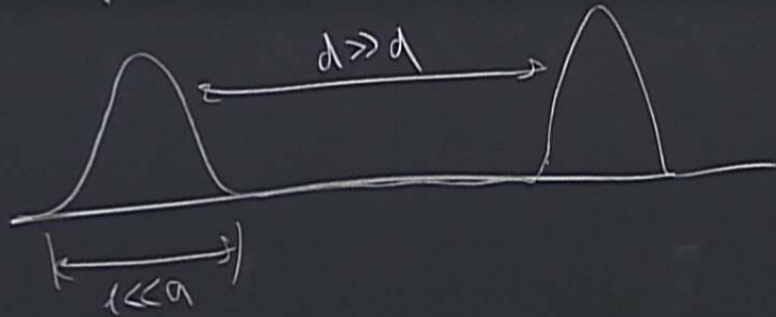
Superposition for a particle



every  
100  
million  
years

$$j(x) = K e^{-x^2/2a^2}$$

Superposition for a particle



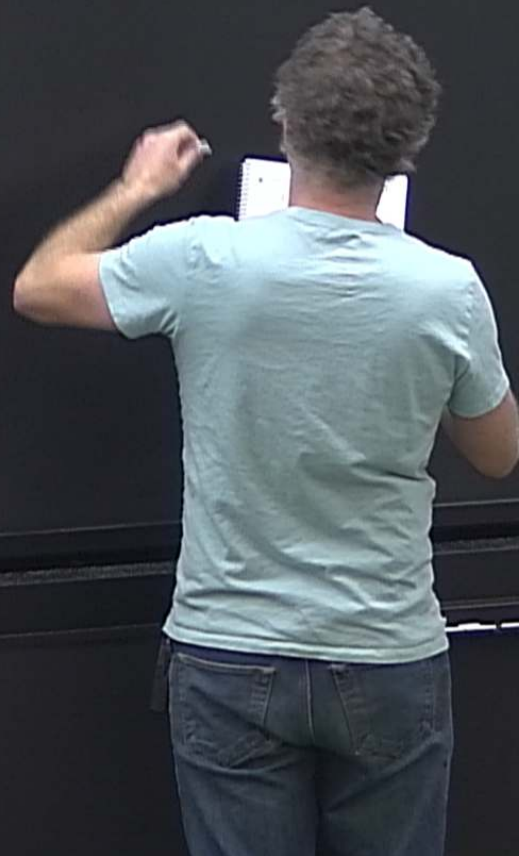
every  
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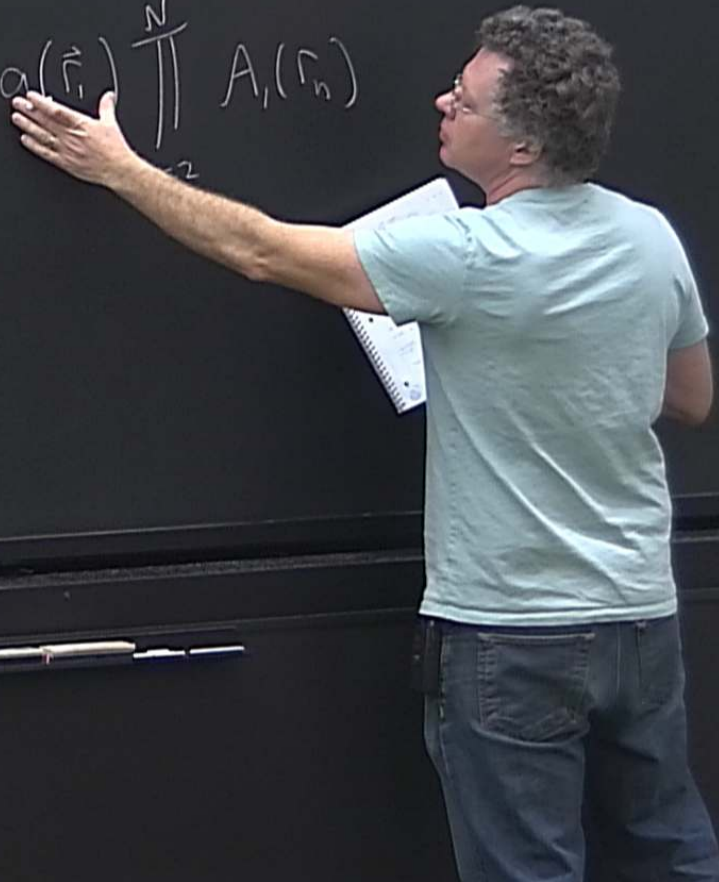
Consider a measurement

$$|\begin{array}{|c|} \hline \uparrow \\ \hline \end{array}\rangle = \alpha |\begin{array}{|c|} \hline \uparrow \\ \hline \end{array}\rangle + \beta |\begin{array}{|c|} \hline \nearrow \\ \hline \end{array}\rangle$$

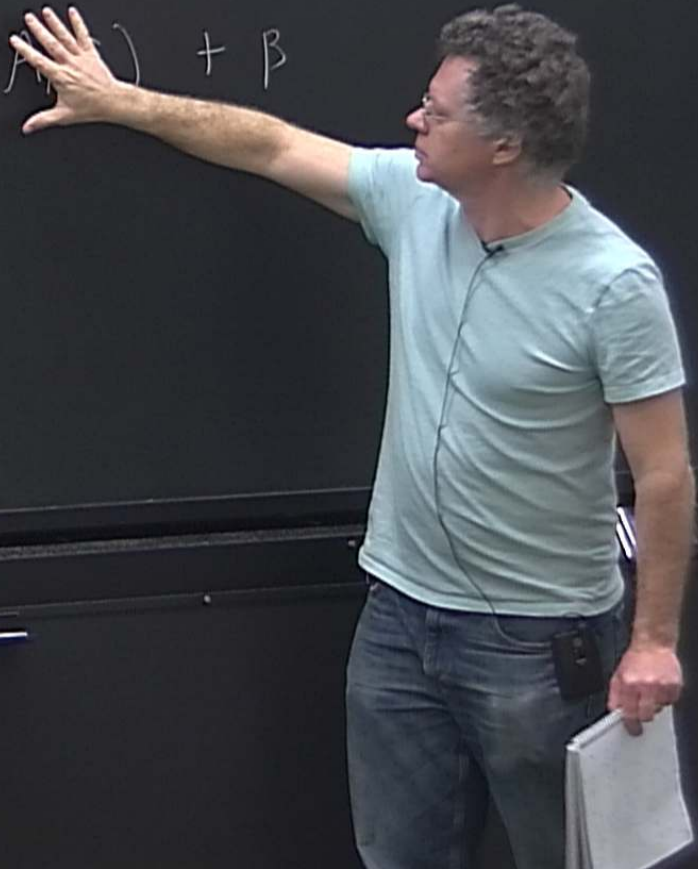
$$|\psi\rangle|A_0\rangle \rightarrow \alpha|a_1\rangle|A_1\rangle + \alpha|a_2\rangle|A_2\rangle$$



$$|\psi\rangle|A_0\rangle \rightarrow |a_1\rangle|A_1\rangle + \alpha|a_2\rangle|A_2\rangle$$
$$\approx \alpha(\vec{r}_1) \prod_{n=2}^N A_n(\vec{r}_n)$$



$$|\psi\rangle|A_0\rangle \rightarrow \alpha|a_1\rangle|A_1\rangle + \beta|a_2\rangle|A_2\rangle$$
$$\simeq \alpha a(\vec{r}_i) \prod_{n=2}^N \psi(\vec{r}_n) + \beta$$



$$|\psi\rangle|A_0\rangle \rightarrow \alpha|a_1\rangle|A_1\rangle + \beta|a_2\rangle|A_2\rangle$$

$$\simeq \alpha a(\vec{r}_1) \prod_{n=2}^N A_1(\vec{r}_n) + \beta a(\vec{r}_2) \prod_{n=2}^N A_2(\vec{r}_n)$$

$$|\psi\rangle|A_0\rangle \rightarrow \alpha|a_1\rangle|A_1\rangle + \beta|a_2\rangle|A_2\rangle$$

$$\simeq \alpha a(\vec{r}_1) \prod_{n=2}^N A_1(\vec{r}_n) + \beta a_2(\vec{r}_1) \prod_{n=2}^N A_2(\vec{r}_n)$$



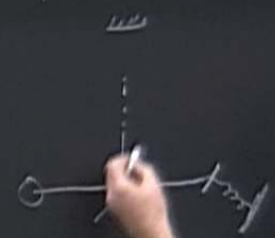
$$\prod_{n=2}^N A_2(\vec{r}_n)$$
$$A_2(\vec{r}_n) \approx 0$$

(non-overlapping)

$\frac{N}{T}$  is prob of hit (per unit time)  
so this will eventually "kill" other term.

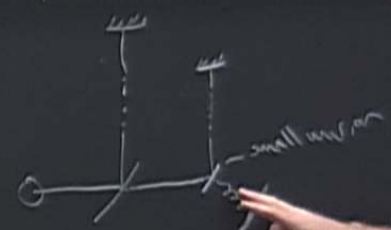
Empirical predictions distinct from standard (unitary) QT

- ① Interference is reduced for large objects  
Penrose proposal



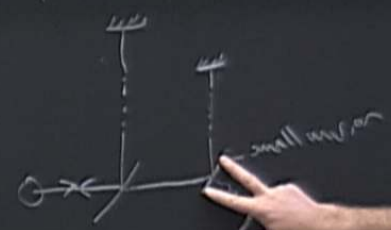
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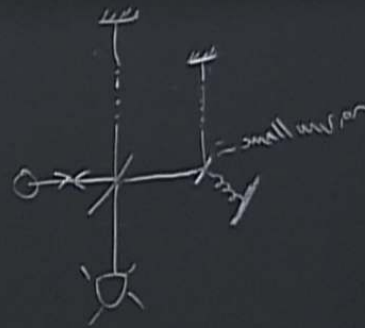
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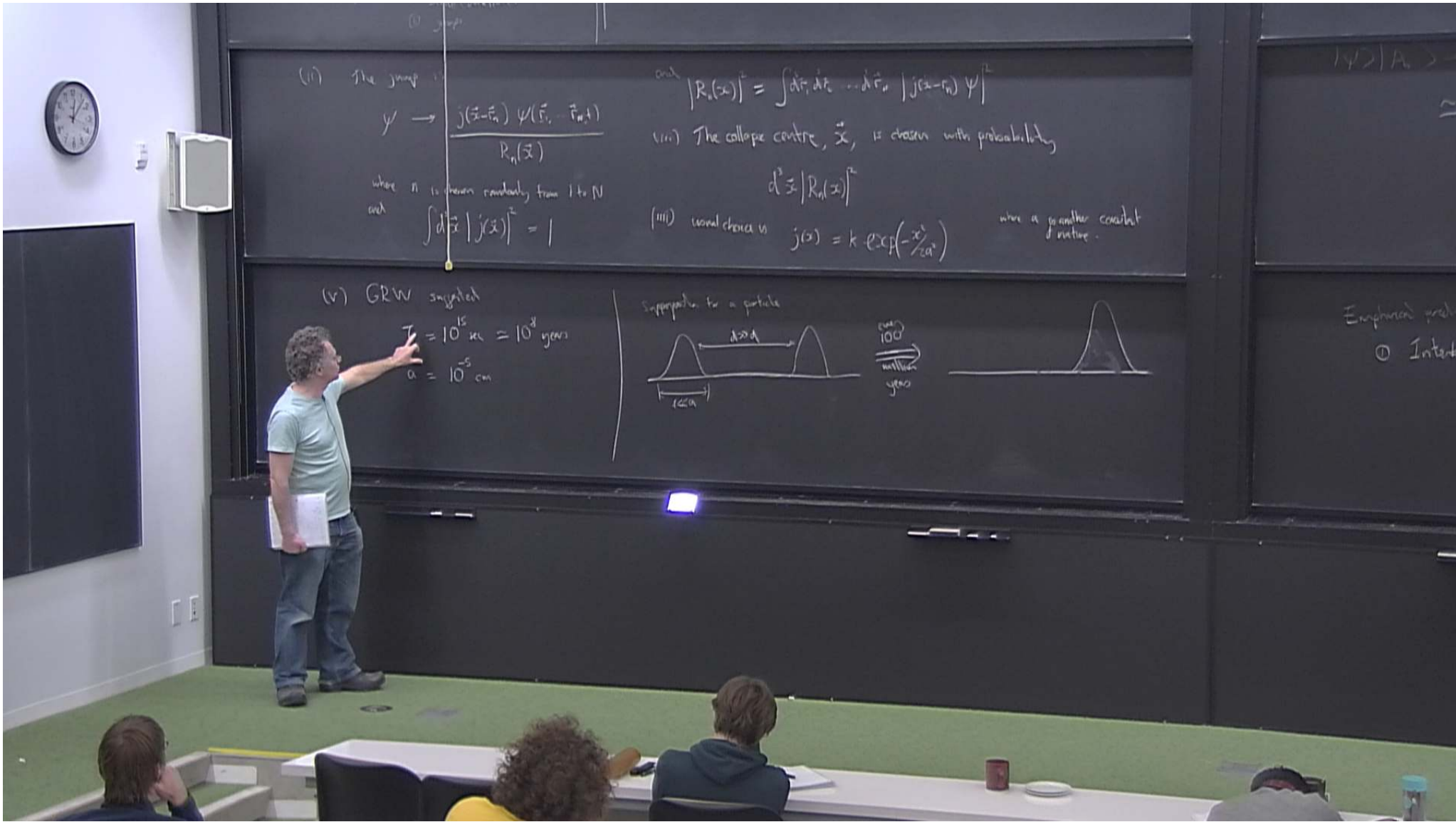
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Empirical predictions distinct from standard (unitary) QM

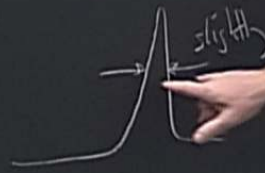
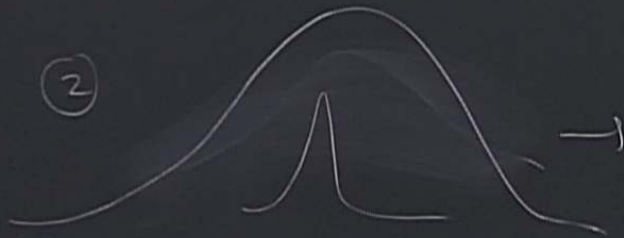
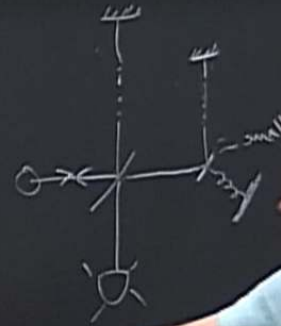
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$$\int d\vec{x} |j(\vec{x})| = | \dots \text{choice of } j(x) = k$$

local beables - that aspect of ontology that is responsible for 3D appearance

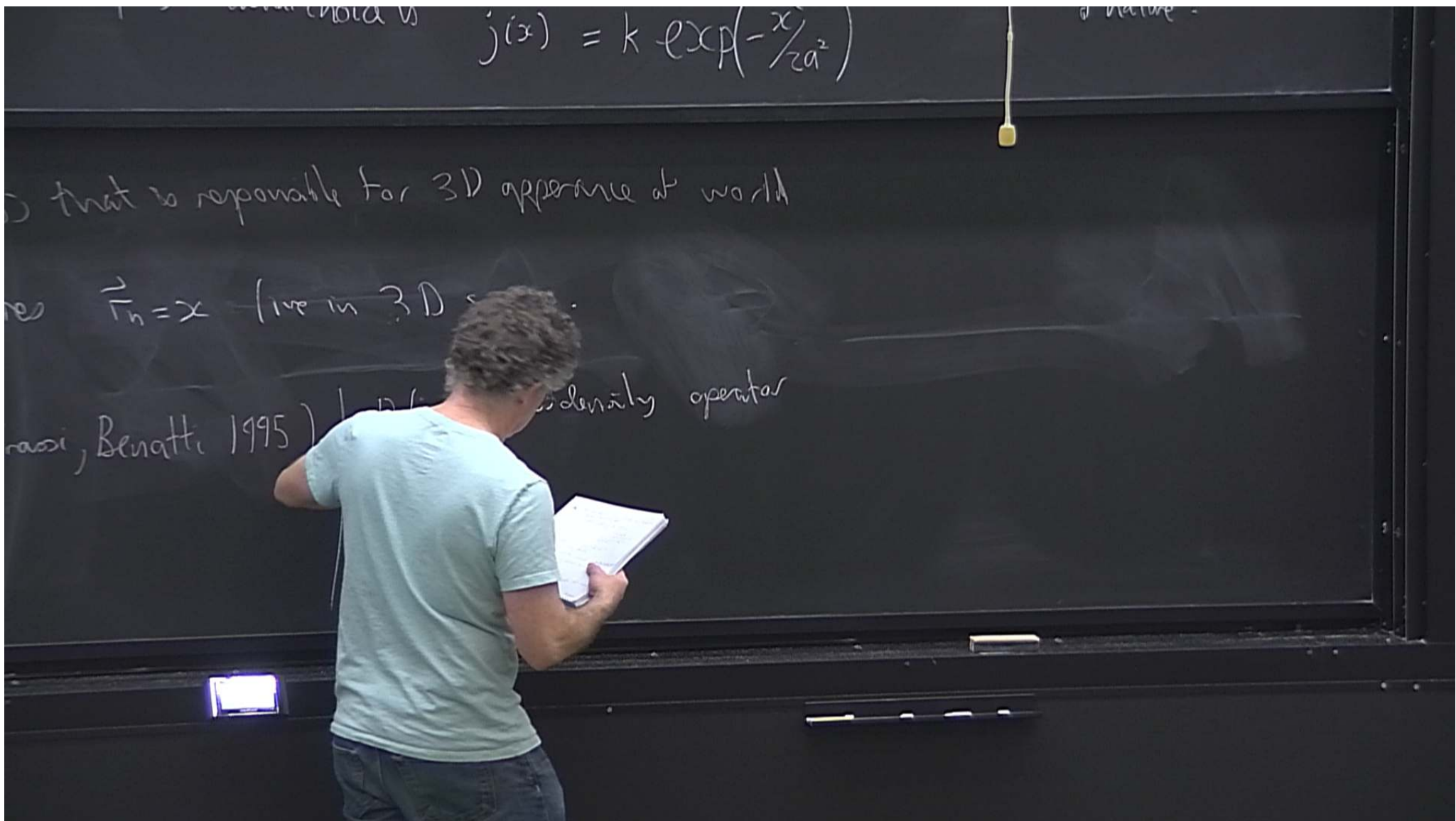
"flash" ontology      The jump centres  $\vec{\Gamma}_n = x$  live in 3D space.

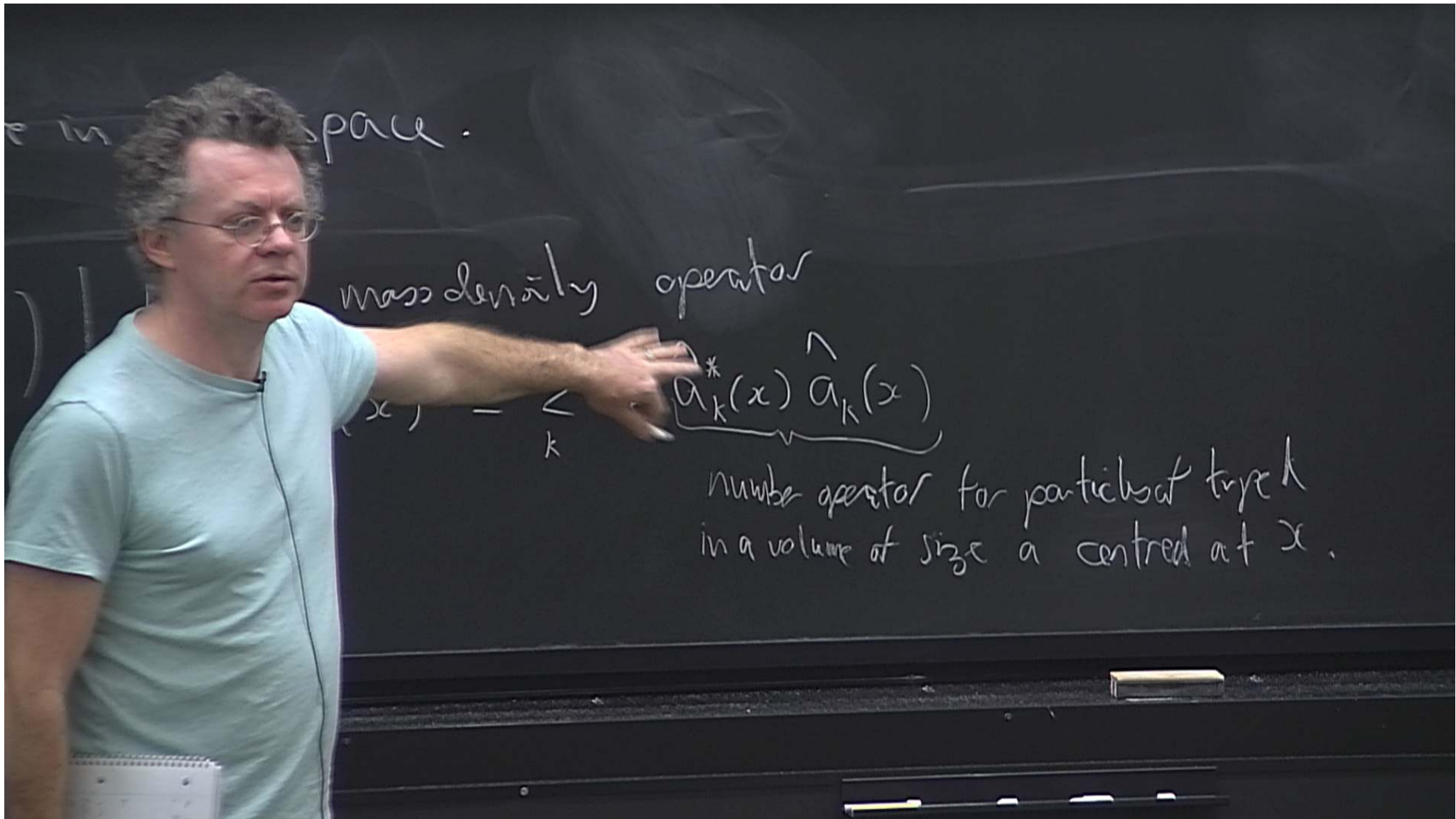
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local beables - that aspect of ontology that is responsible for 3D appearance

The "flash" ontology (Bell 1987)      The jump centres  $\vec{r}_n = x$  live in 3D space.

The mass density ontology (Ghirardi, Grassi, Benatti 1995)





mass density operator

$$\hat{n}_k(x) = \underbrace{a_k^*(x) a_k(x)}_{\text{number operator}}$$

number operator for particles of type  $k$  in a volume of size  $v$  centered at  $x$ .

in 3D space.

Define mass density operator

$$\hat{M}(x) = \sum_k m_k \underbrace{\hat{a}_k^*(x) \hat{a}_k(x)}_{\text{number operator for particles of type } k \text{ in a volume of size } a \text{ centered at } x.}$$

number operator for particles of type  $k$   
in a volume of size  $a$  centered at  $x$ .

presence of world

define

$$n(x,t) = \langle \psi | \hat{n} | \psi \rangle$$

density operator

$$\hat{n} = \sum_k m_k \hat{a}_k^*(x) \hat{a}_k(x)$$

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or 3D appearance of world

3D space.

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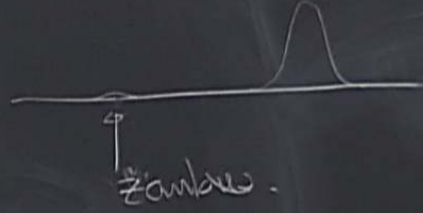
$$m(x,t) = \langle \psi | \hat{M} | \psi \rangle$$

gives a mass density

→ the local beable.

Criticisms

① Have tails

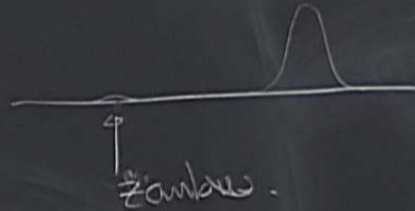


②



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② Hard to make it relativistic.

③ Not really fundamental physics.



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$$\simeq \alpha \prod_{i=1}^N A_1(\vec{r}_i) + \beta \prod_{i=1}^N A_2(\vec{r}_i)$$



$$|A_1(\vec{r}_i)| |A_2(\vec{r}_i)| \simeq 0$$

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$$N \simeq 10^{33}$$

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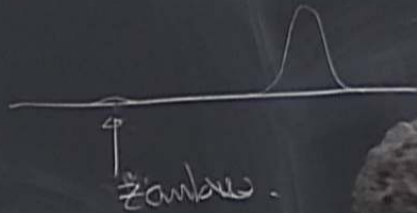
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