

Title: Foundations of Quantum Mechanics-7

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Abstract:

The many worlds interpretation (Everett 1957)

The axioms

① The ontic state at time  $t$  is  $|\psi(t)\rangle$

## The many worlds interpretation (Everett 1957)

and that's it!!

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- ② The wavefunction  $|\psi(t)\rangle$  evolves according to
$$i\hbar \frac{\partial |\psi(t)\rangle}{\partial t} = \hat{H} |\psi(t)\rangle$$

many worlds interpretation (Everett 1957)

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The claim is that this recovers the appearances (tables, chairs, ...)  
and the empirical content of quantum theory (probs)

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and the empirical content

Will follow David Wallace's approach.

Two problems

① where does the "world" structure come from?  
And in what basis? } influenced by

Simon Saunders

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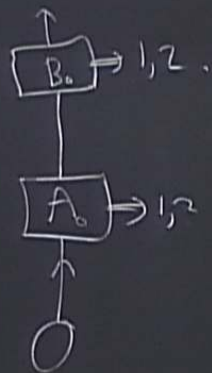
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at macroscopic level using decoherence.

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$$|\psi\rangle_S |A_0\rangle_A |B_0\rangle_B \rightarrow \alpha |a_1\rangle_S |A_1\rangle_A |B_0\rangle_B + \beta |a_2\rangle_S |A_2\rangle_A |B_0\rangle_B$$

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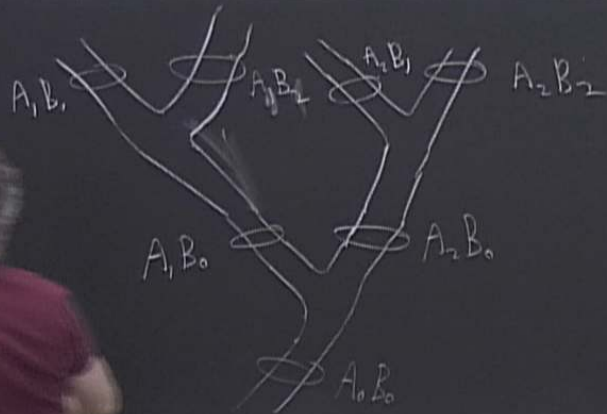
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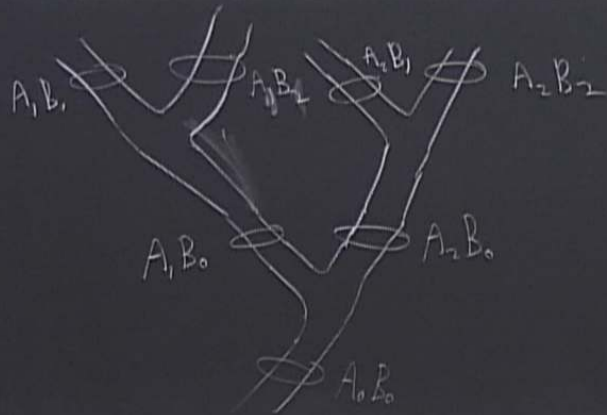
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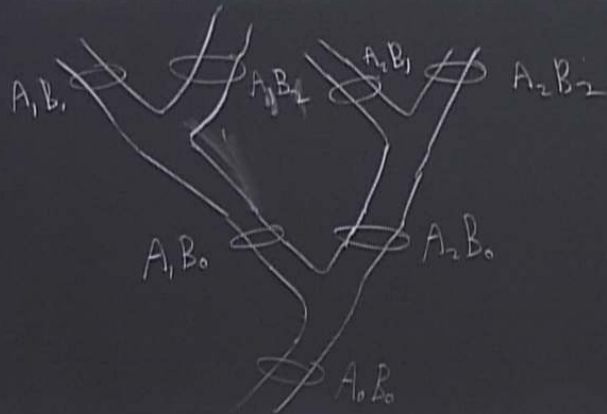


What picks out a particular basis?  
 Have various environmental degrees of freedom  
 which will decohere in this basis ( $A_i B_j$  basis)  
 These branches are emergent (approximate) structure



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certainly happens.

$$|\psi\rangle|A\rangle \rightarrow \alpha|a_1\rangle|A_1\rangle + \beta|a_2\rangle|A_2\rangle$$

and  $\beta = 10^{-100}$

but this world is just as real (colours just as bright...)

but in MW it definitely happens

why don't we put

$$\text{prob}_2 = 1$$

even if we have a probability,

why not

$$\text{prob}_2 = \frac{1}{2}$$

The idea

Probability is a measure of agents' subjective belief and so influences how agents act

⇒ Decision theory



can prove that

Normally we would say that  
 $\text{prob}_z = 10^{-200}$

but in MW it definitely happens  
why don't we put  
 $\text{prob}_z = 1$

can prove a theorem. The theorem says, basically,  
rational agents behave as if there are probabilities.

①  $\exists$  a unique  $P_r(s)$  s.t.  $\sum_{s \in S} P_r(s) = 1$

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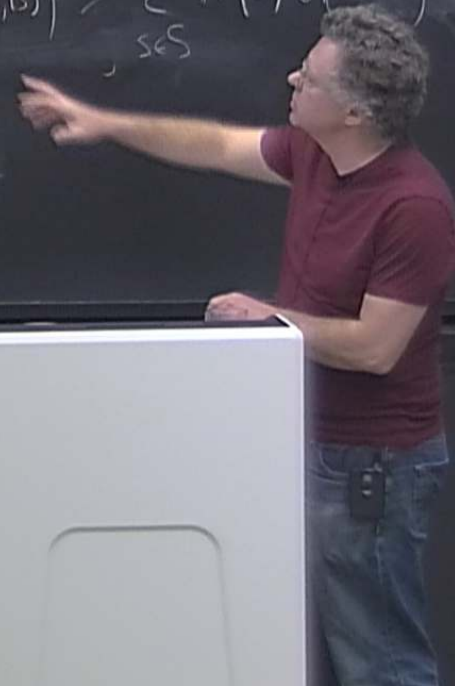
s.t.  $b_1 > b_2$

$$\text{iff } \sum_{s \in S} P_r(s) U(b_r(s)) > \sum_{s \in S} P_c(s) U(b_c(s))$$

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And in what basis?

Simon Saunders

at macroscopic level using d

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want to show that these probs are  $1/d^2$

The Principle Principle

A rational agent



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The Principle Principle.

A rational agent who knows that the objective probability  
for  $s$  is  $P$  is required to choose this as his  
subjective probability.

And in what basis?

Where does the Born rule (prob = |amplitude|<sup>2</sup>) come from?

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at macroscopic level using decoherence.

to show that these probs are 1/4?

Principle Principle -

rational agent who knows that the objective probability is  $P$  is required to choose this as his subjective probability.

Wallace has a set of axioms that apply decision theoretic ideas to the branching structure

- Ⓐ - proves that if two events have same <sup>subjective</sup> ID then agents must give same probs (equivalence rule)
- Ⓑ Then uses equiv. rule to prove Born rule.