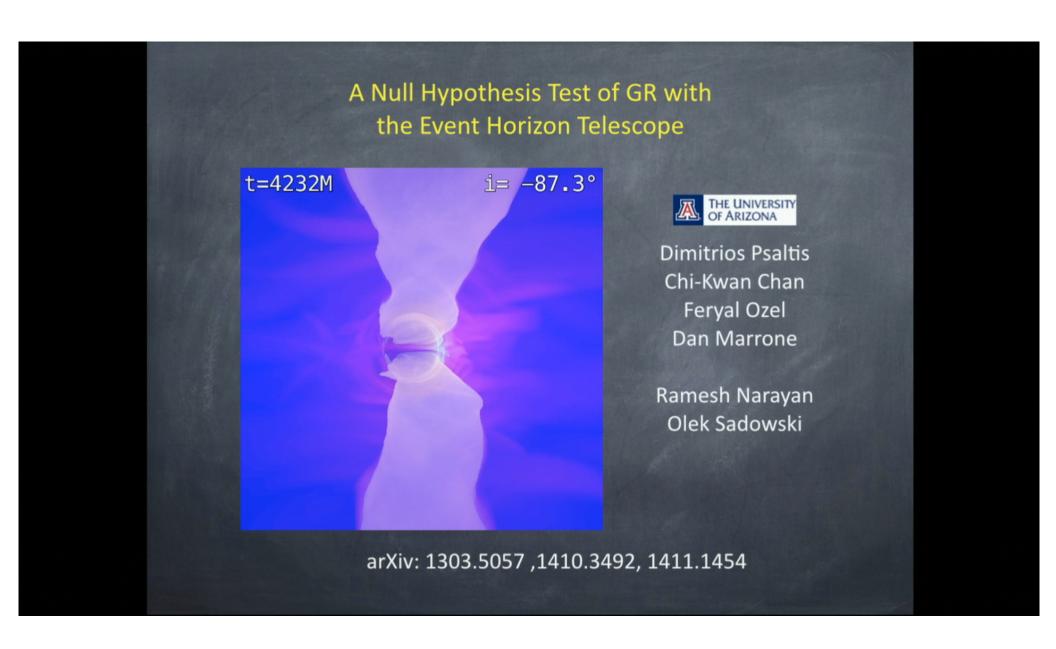
Title: GPU-accelerated Ray Tracing and a Null Hypothesis Test of GR with the EHT

Date: Nov 12, 2014 03:45 PM

URL: http://pirsa.org/14110121

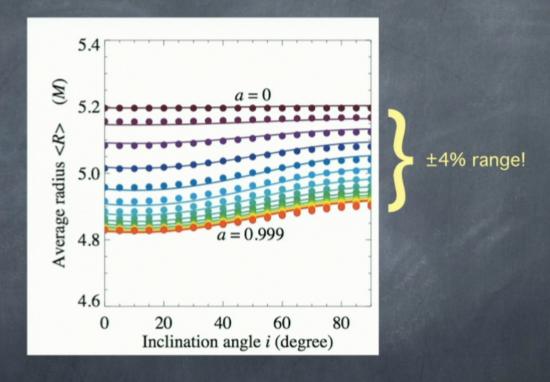
Abstract: The Event Horizon Telescope will generate the first images of the black-hole shadows in Sgr A* and in M87. The observed photons will have originated in one of the strongest gravitational fields found in the Universe, encoding during their travel to the Earth the properties of the black-hole spacetimes. In this talk, I will discuss the prospect of performing a new null hypothesis test of GR with EHT observations of Sgr A* that does not depend on a prior knowledge of the properties of the accretion flow. I will address a a small number of outstanding questions related to the scattering screen towards the galactic center that need to be answered in order for this null hypothesis test to be performed. I will then use results from recent GPU-accelerated ray tracing calculations in conjunction with GRMHD simulations to argue that upcoming observations of Sgr A* with the EHT will be able to confirm the GR predictions for the size and shape of the black-hole shadow to an accuracy of better than 10%, in a model independent way.

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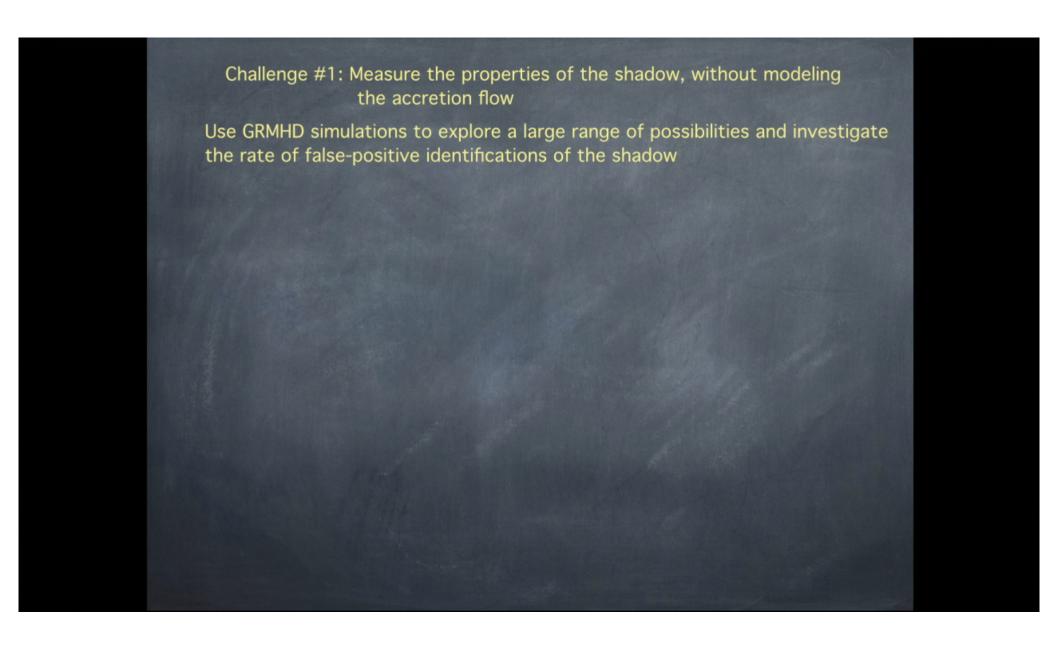
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The opening angle of the black-hole shadow has a very weak dependence on black-hole spin or inclination.

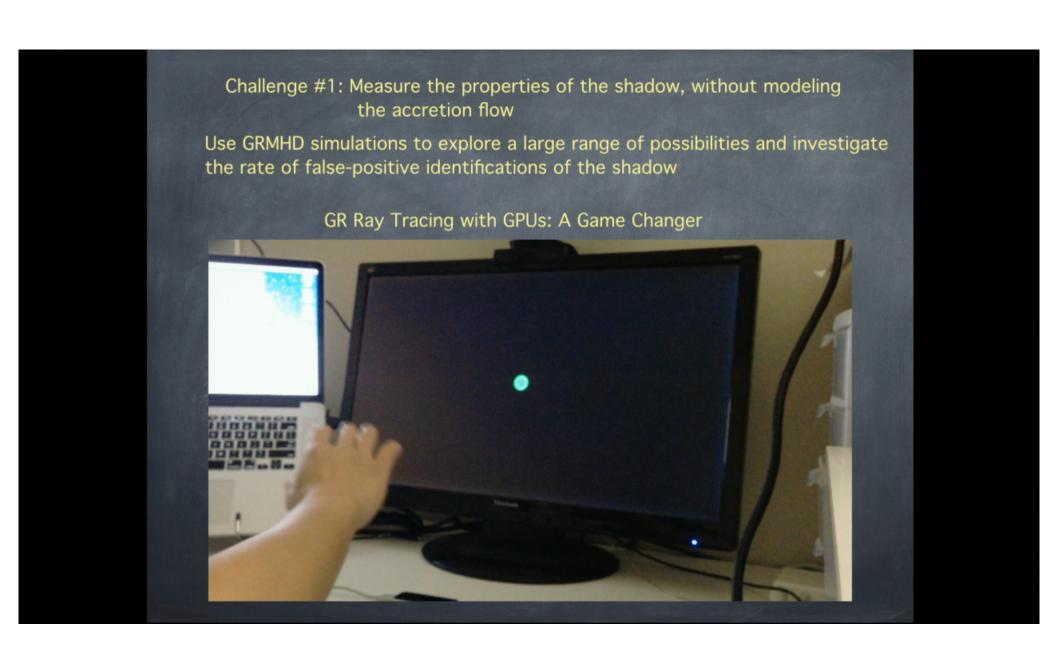


A null hypothesis test: Does the image of Sgr A* have a shadow of the shape and size expected in GR?

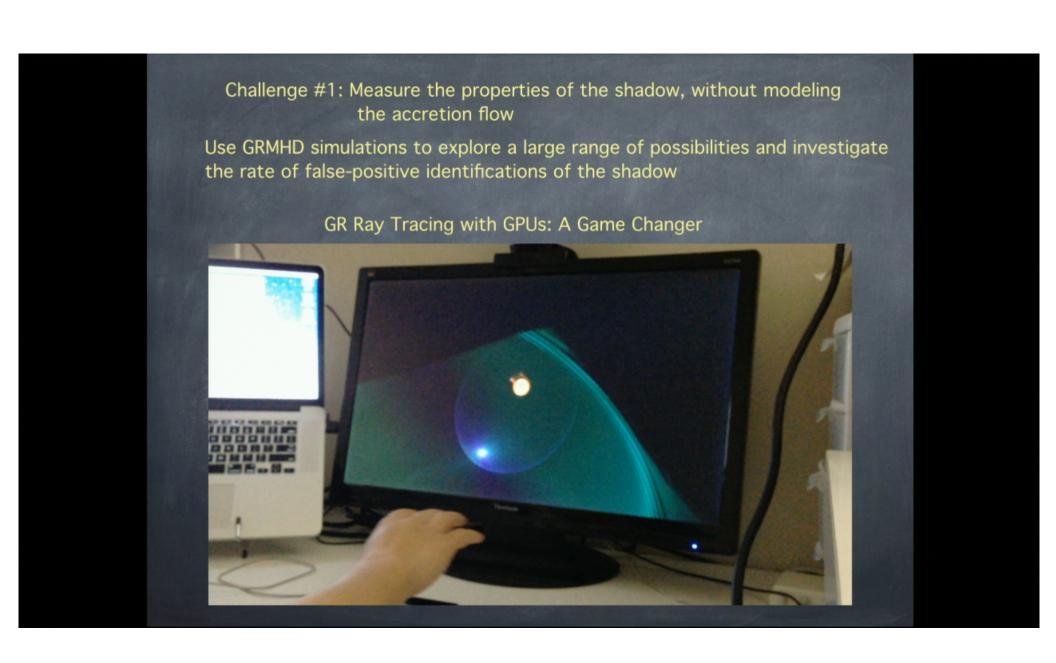
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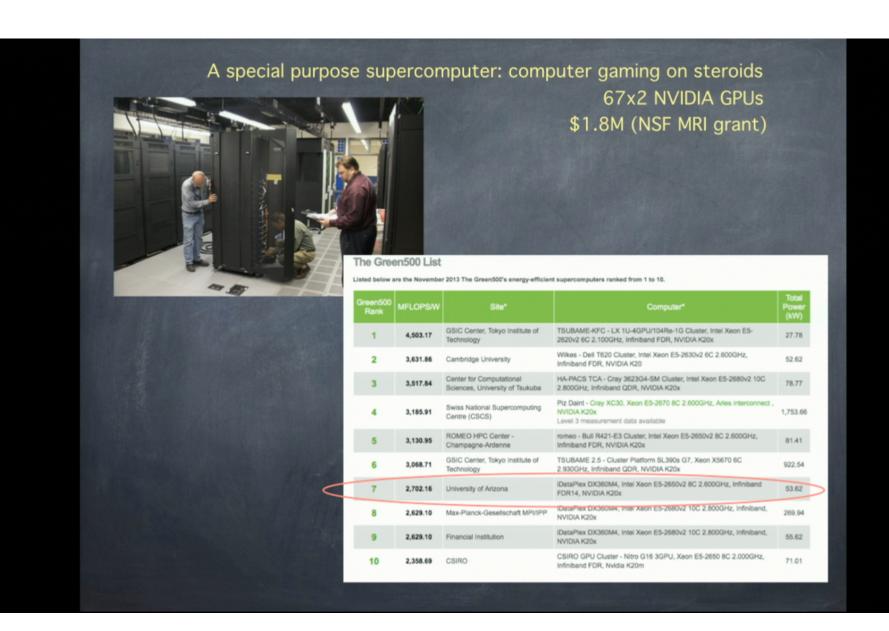
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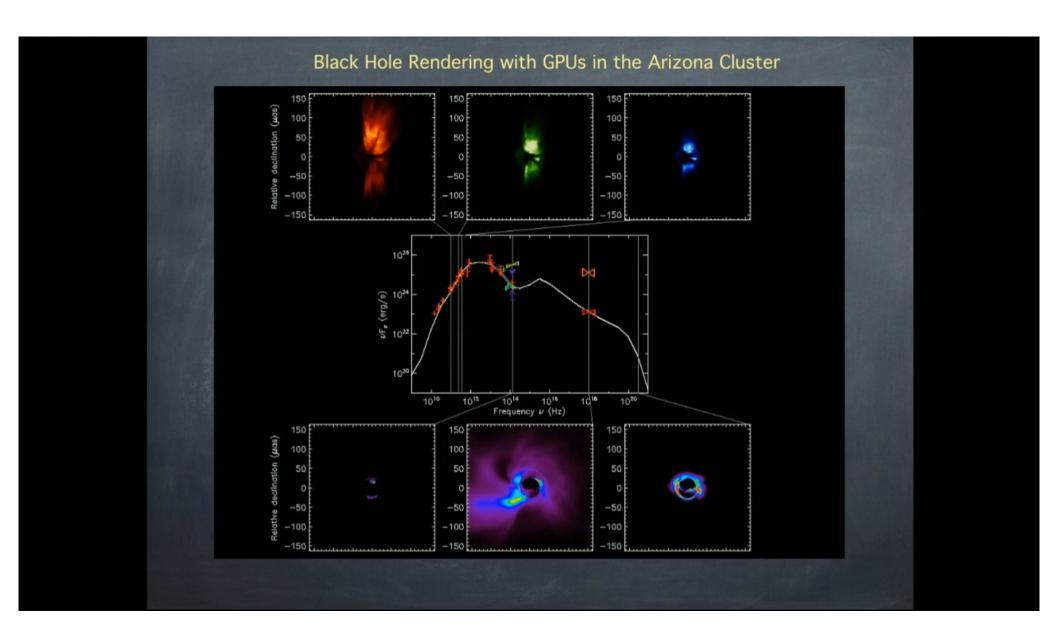
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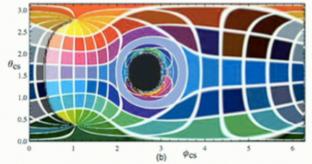


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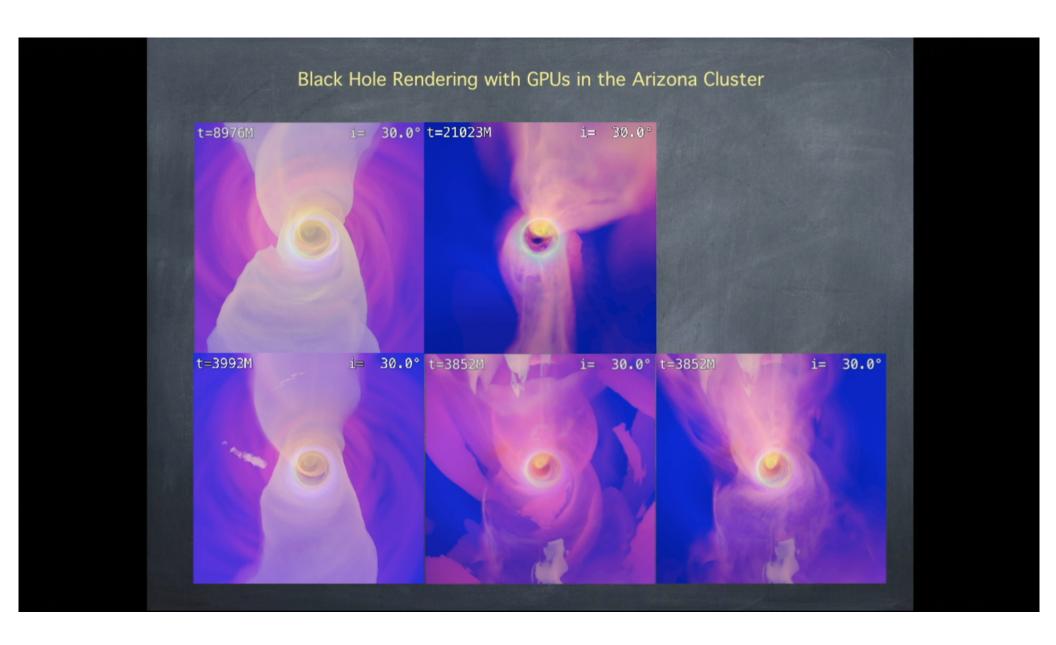
McConaughey explores another world in Interstellar (top). Thorne's diagram of how a black hole distorts light.

TO DIAGRAMS COURTESY OF KIP THORNE

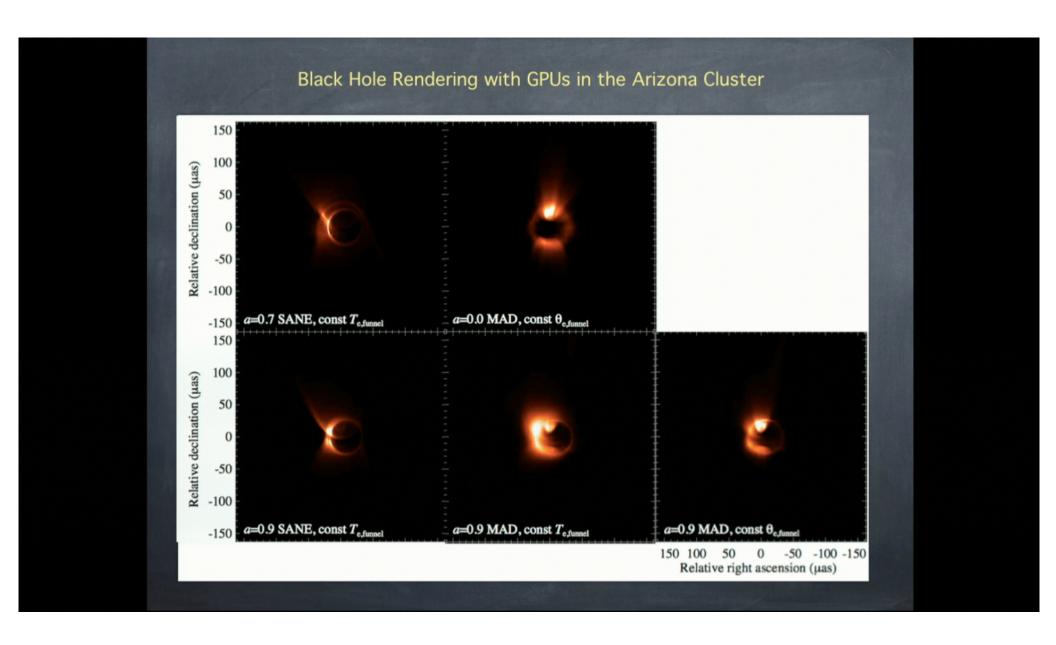
ray-tracing software makes the generally reasonable assumption that light is traveling along straight paths," says Eugénie von Tunzelmann, a CG supervisor at Double Negative. This was a whole other kind of physics. "We had to write a completely new renderer," she says.

Some individual frames took up to 100 hours to render, the computation overtaxed by the bendy bits of distortion caused by an Einsteinian effect called gravitational lensing. In the end the movie brushed up against 800 terabytes of data. "I thought we might cross the petabyte threshold on this one," von Tunzelmann says.

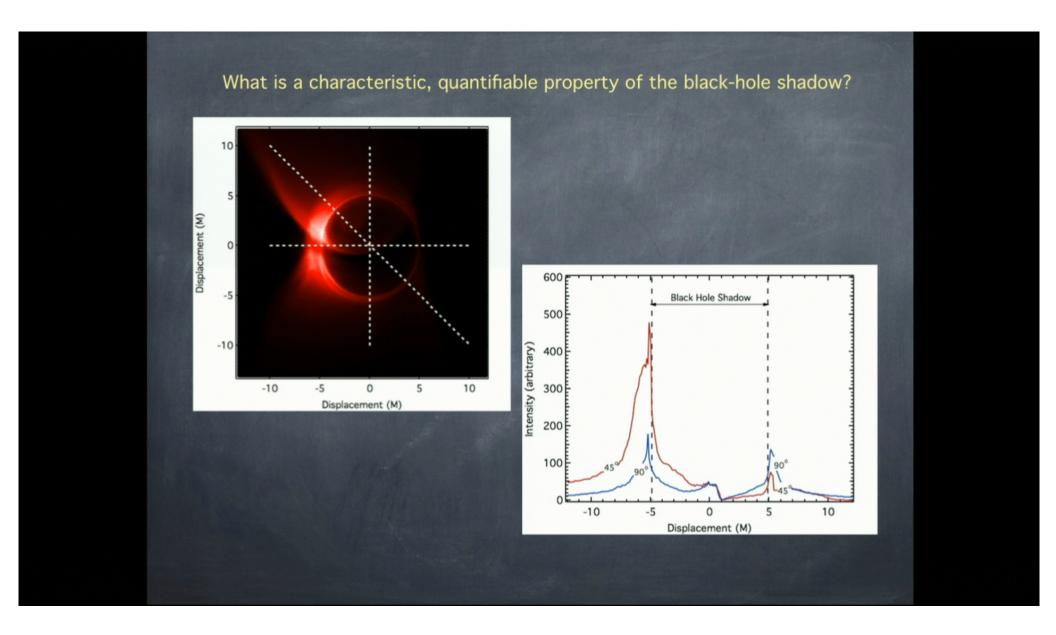
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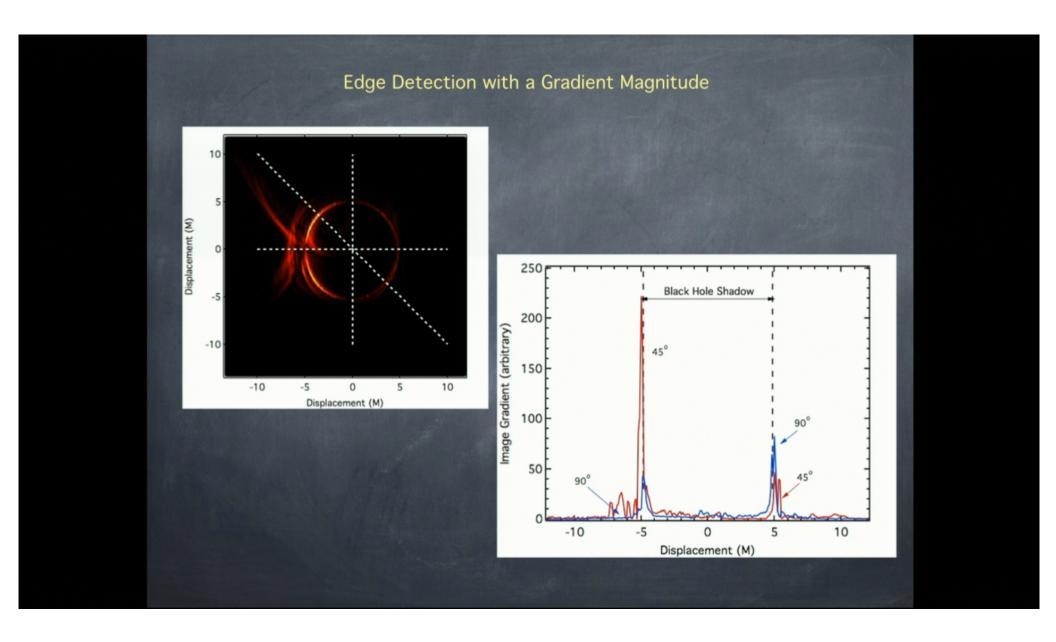
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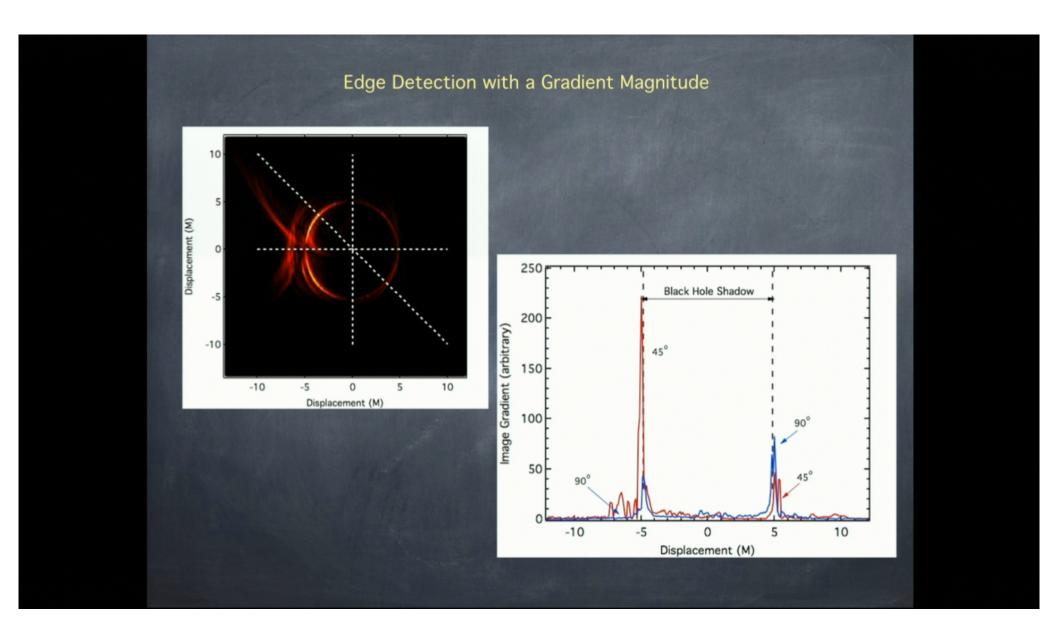
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A formal definition of the Radon Transform for a Kerr Black-Hole Shadow, with appropriate definition of posterior Likelihood measures

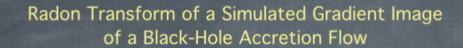
$$\alpha'(r) = -m \frac{\left[a^2(r+1) + (r-3)r^2\right] \csc \theta_o}{a(r-1)}$$

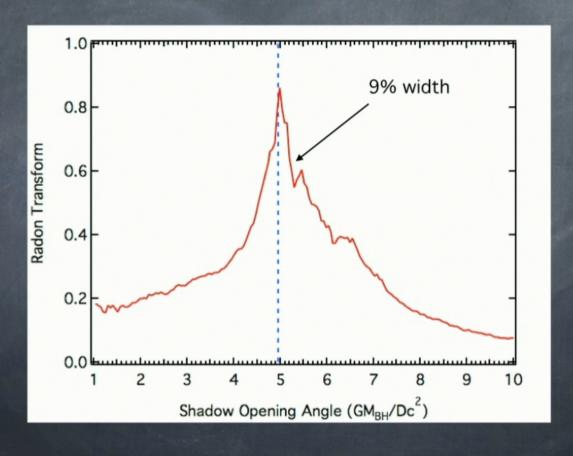
$$\beta'_{\pm}(r) = \pm m \frac{1}{a(r-1)} \left\{ a^4(r-1)^2 \cos^2 \theta_o + a(r-1) \left[a^2(r+1) + (r-3)r^2 \right] \cot^2 \theta_o - r^3 \left[(r-3)^2 r - 4a^2 \right] \right\}^{1/2}.$$

$$egin{align} \mathcal{R}(lpha_0,eta_0,\phi,m,a) &= C \int_{r_{
m ph-}}^{r_{
m ph+}} dr rac{ds}{dr} \ &\{ H \left[G(lpha,eta_+) - G_0
ight] + H \left[G(lpha,eta_-) - G_0
ight] \} \end{split}$$

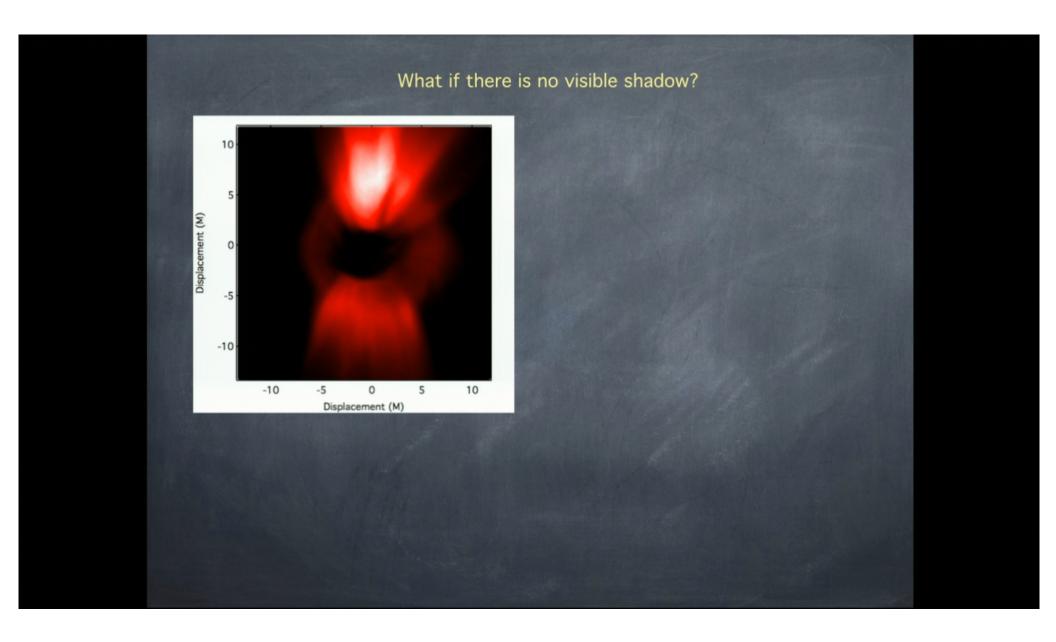
$$\begin{split} \frac{ds}{dr} &= \frac{r\left(r^2 - 3r + 3\right) - a^2}{a(r-1)^2} \\ &\left\{ \frac{\left[a(r-1)\cot^2\theta_{\text{o}} - 2(r-3)r^2\right]^2}{a^4(r-1)^2\cos^2\theta_{\text{o}} + a(r-1)\left[a^2(r+1) + (r-3)r^2\right]\cot^2\theta_{\text{o}} - r^3\left[(r-3)^2r - 4a^2\right]} + 4\csc^2\theta_{\text{o}} \right\}^{1/2} \end{split}$$

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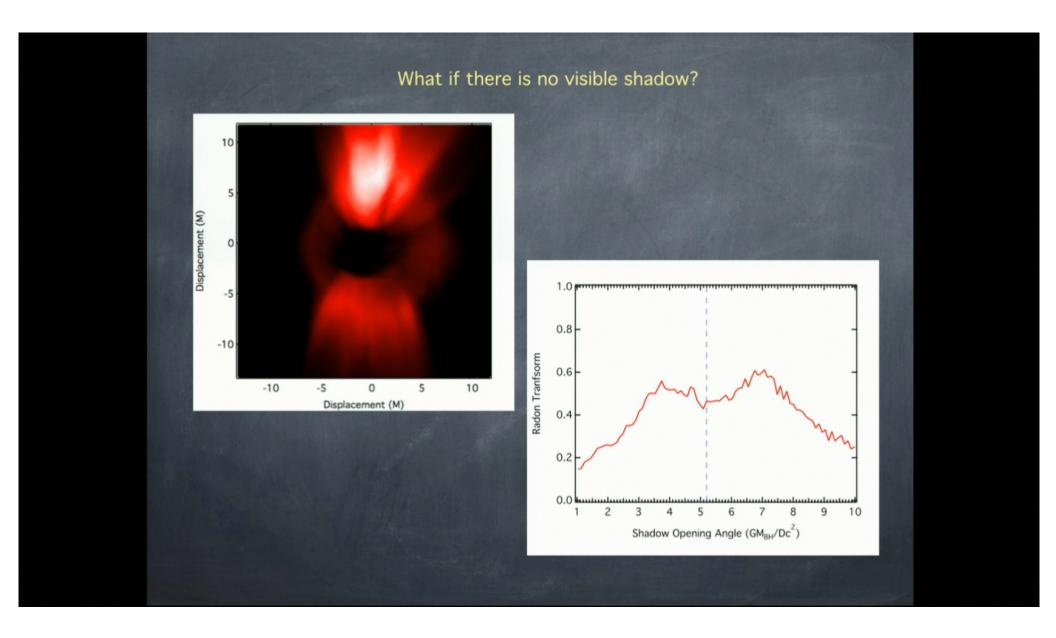




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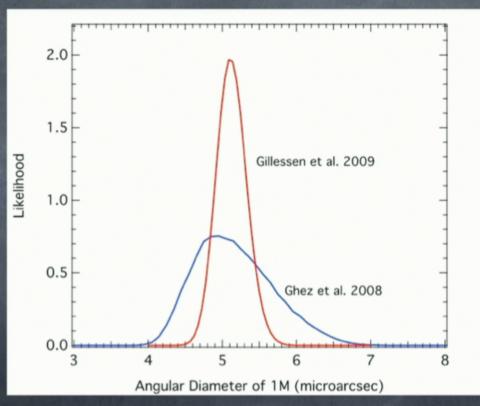


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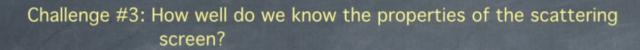
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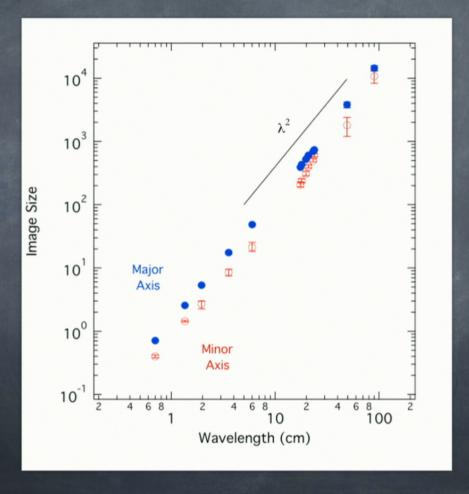
Challenge #2: What is the expected angular size of the black-hole shadow?



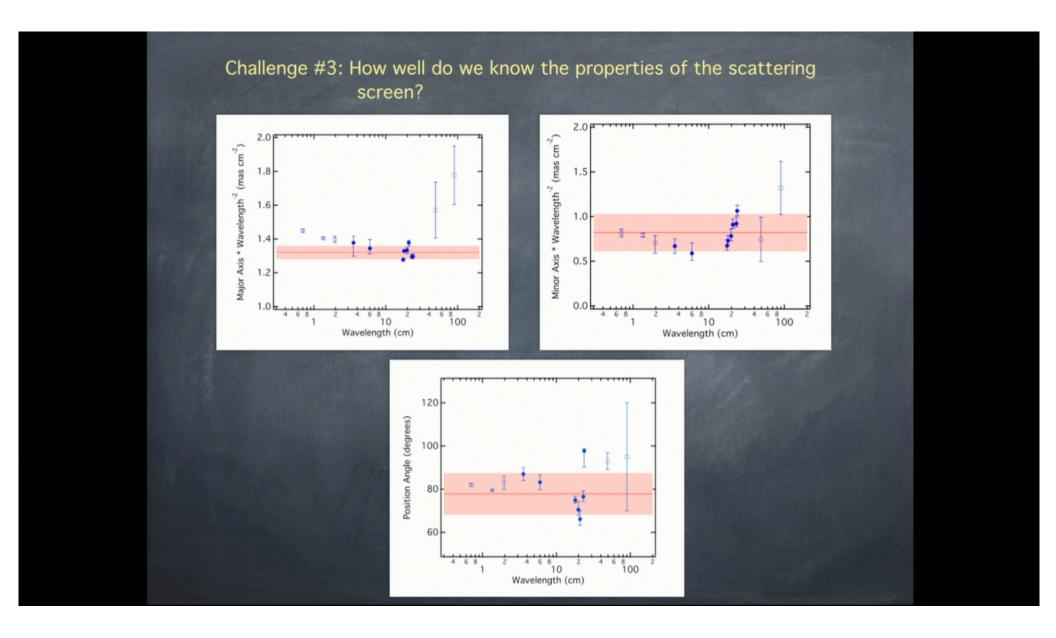
The angular size of the black-hole shadow is known to within 6% M/D=5.19+-0.29 microarcsec

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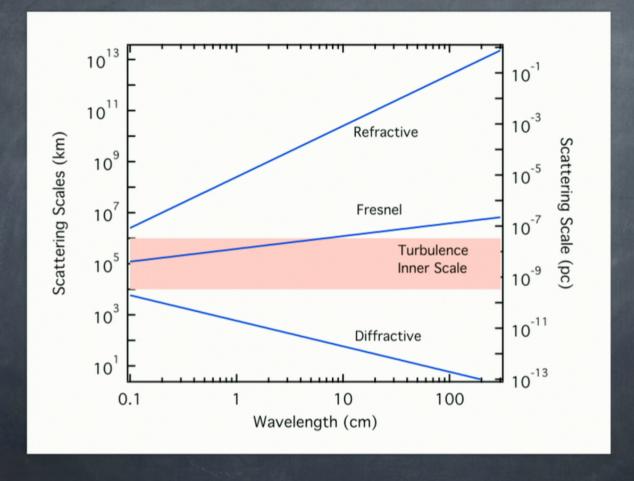


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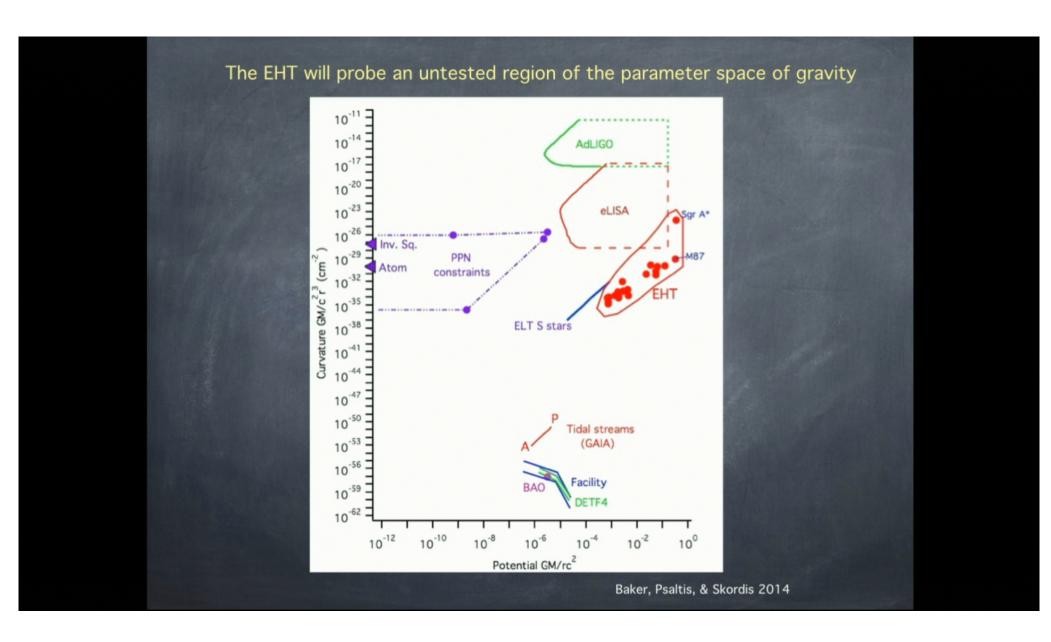


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