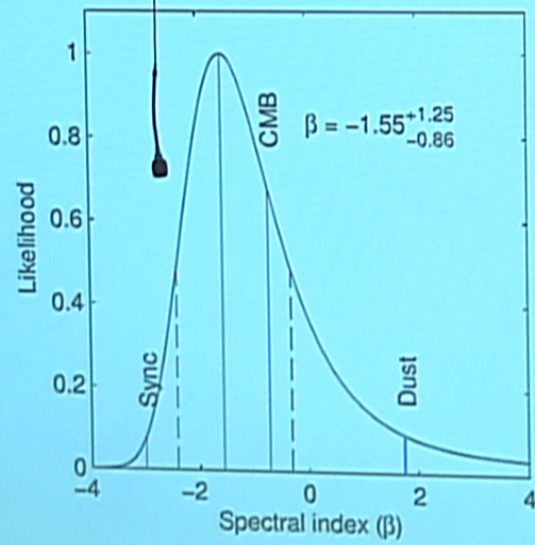


Title: CMB anomalies from primordial gravitational waves

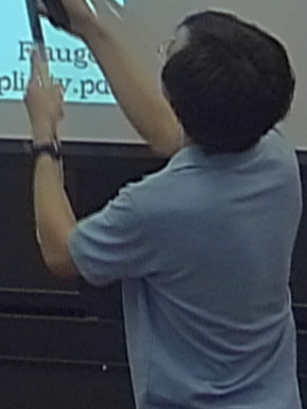
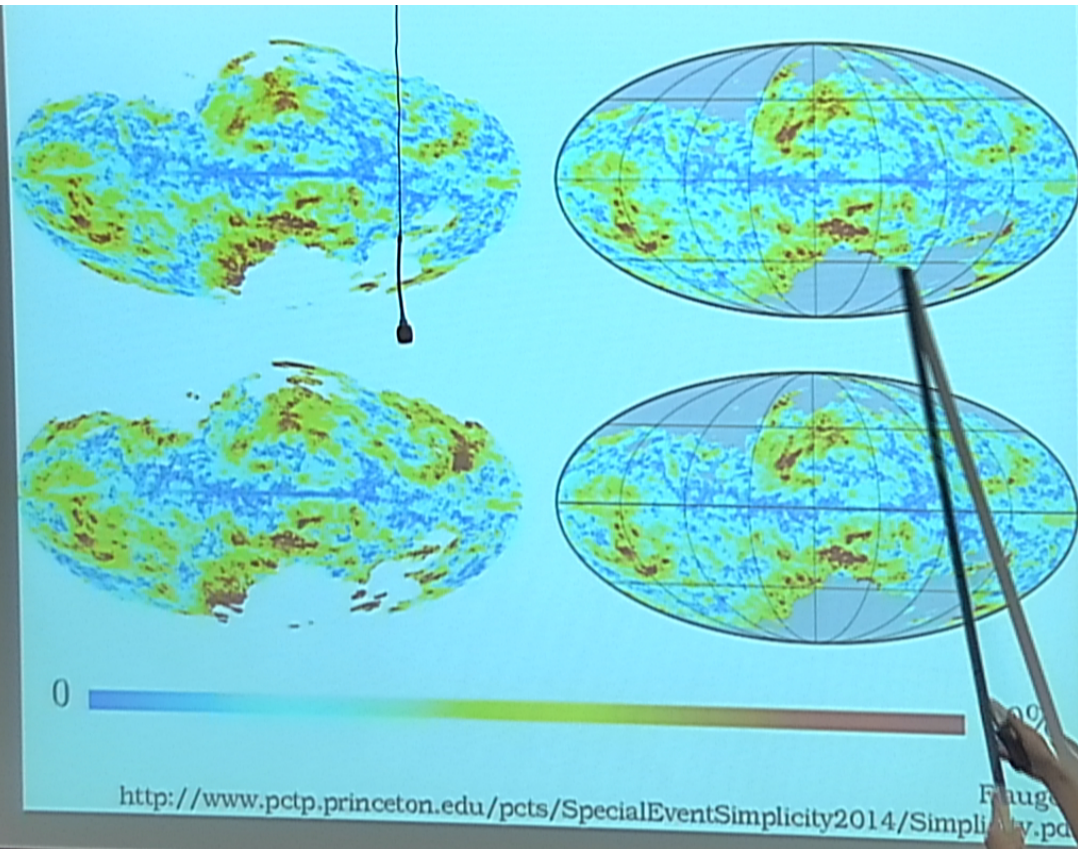
Date: Aug 13, 2014 01:00 PM

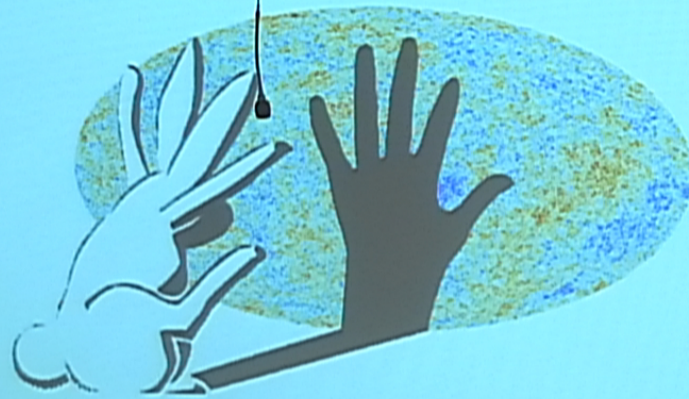
URL: <http://pirsa.org/14080019>

Abstract: We relate CMB anomalies and the recent observational evidence of primordial gravitational waves. Two aspects are investigated: (a) Several anomalies are spotted on the low l temperature map of the WMAP and Planck experiments. However, those anomalies disappear at high l . We propose that those low l temperature anomalies may come from nearly scale invariant anomalies of the tensor sector. Those anomalies on the temperature map naturally decay towards small scales, characterized by the tensor-to-temperature radiation transfer function. (b) The anomalies introduced by the gravitational waves discovery. Strong tension is noticed between the BICEP2 and Planck data. We study in detail how blue tilt of the tensor spectrum reconciles the tension between those datasets.



BICEP2

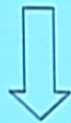




For primordial: $B_1 \times B_2$, shape, most dust models
For dust: DDM2 autocorrelation, tension
We need to be patient

Inflation before BICEP2

η -problem: η is unnaturally small



Inflation after BICEP2

ϵ -problem: ϵ is unnaturally large

Two topics concerning anomalies

- New proposals for existing anomalies
- New anomalies brought by BICEP2

WMAP/Planck anomalies (at low ℓ)

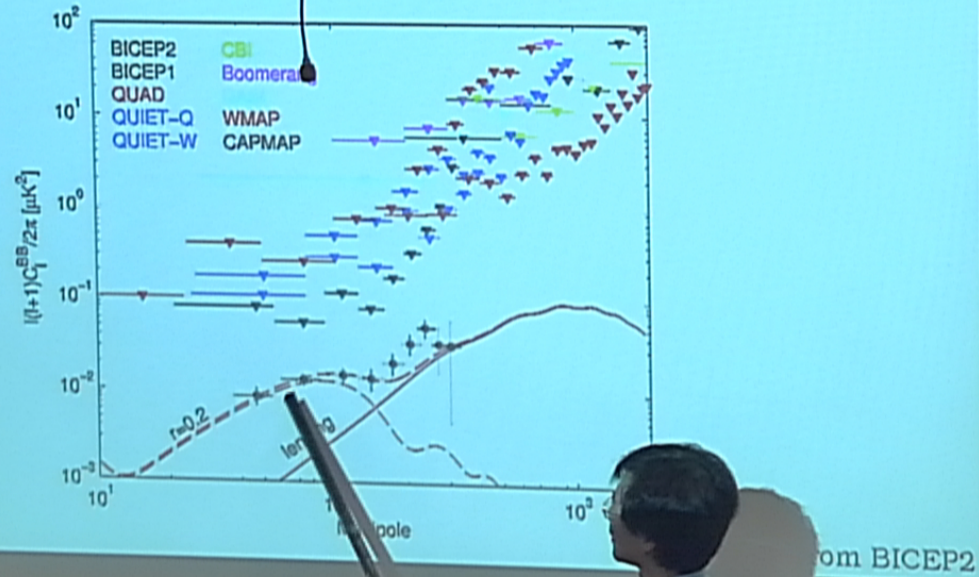
(CMB is much less anomalous at high ℓ)

Possibility:

- Cosmic variance
- Introduce scale dependent features

Scale invariant physics \Rightarrow scale dep. anomalies?

Now $r=0.2$ provides such a mechanism.



Scale invariant physics \Rightarrow scale dep. anomalies

Decay: the tensor-to-temperature transfer function

Example: Anisotropy

- Case 1: anisotropic inflation
- Case 2: solid inflation

Scalar (relatively) isotropic, tensor anisotropic

Charged anisotropic inflation, $V = m^2 \phi^2$

$$S = \int d^4x \sqrt{-g} \left[\frac{M_P^2}{2} R - \frac{1}{2} D_\mu \varphi \overline{D^\mu \varphi} - \frac{f^2(\varphi)}{4} F_{\mu\nu} F^{\mu\nu} - V(\varphi, \overline{\varphi}) \right]$$

$$g^{\mu\nu} \mathcal{D}_\mu \phi \mathcal{D}_\nu \phi \rightarrow -e^2 g^{ij} \phi^2 A_i A_j$$

$$g^{ij} \phi^2 A_i A_j \rightarrow g^{ij} \delta \phi^2 A_i A_j \rightarrow P^\zeta(\mathbf{k}) = P_0^\zeta(k) (1 + g_*^\zeta \cos^2 \theta)$$

$$g^{ij} \phi^2 A_i A_j \rightarrow h^{ij} \phi^2 A_i A_j \rightarrow P^h(\mathbf{k}) = P_0^h(k) (1 + g_*^h \cos^2 \theta)$$

Tensor-tensor \rightarrow TT dominates

X. Chen, R. Emami, H. Firouzjahi, YW, 1404.0818

Charged anisotropic inflation, $V = m^2 \phi^2$

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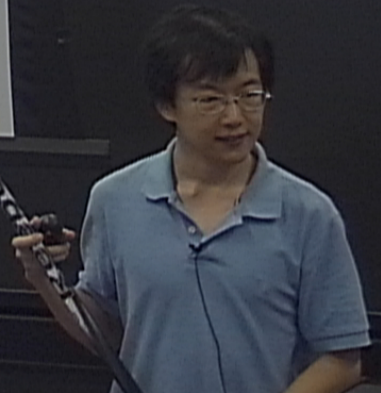
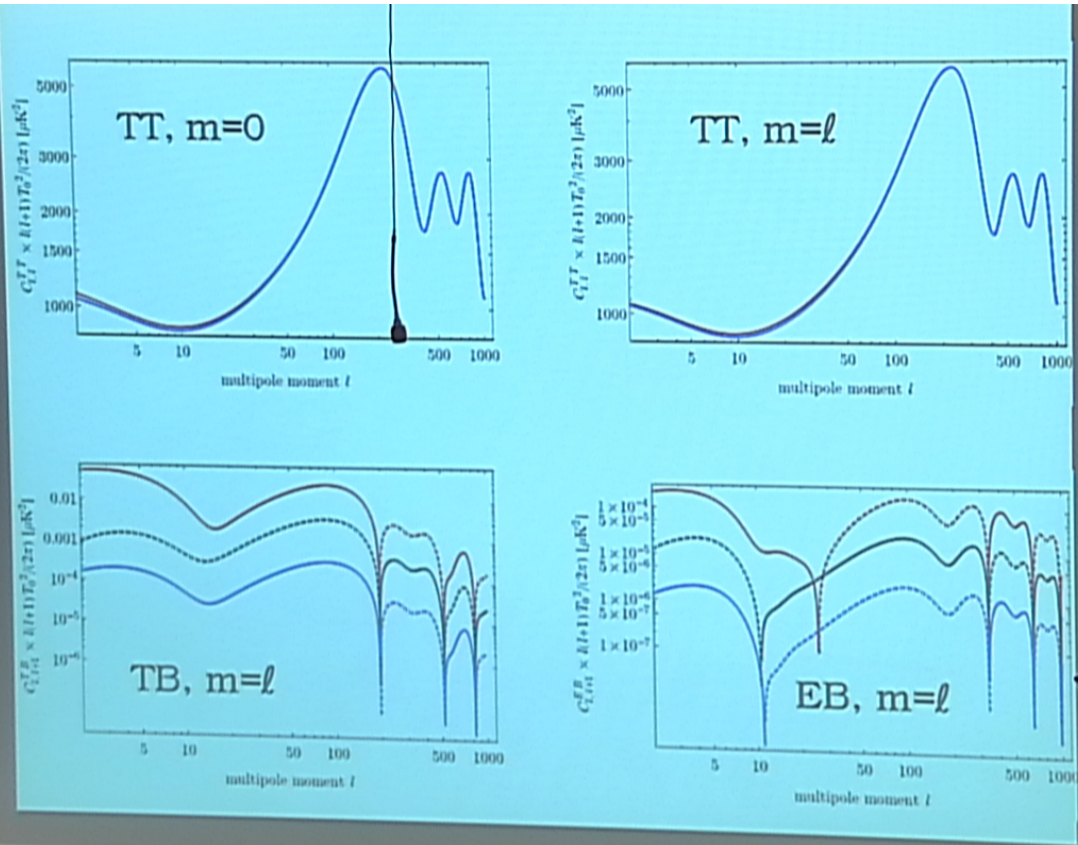
$$g^{\mu\nu} \mathcal{D}_\mu \phi \mathcal{D}_\nu \phi \rightarrow -e^2 g^{ij} \phi^2 A_i A_j$$

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X. Chen, R. Emami, H. Firouzjahi, YW, 1404.4083



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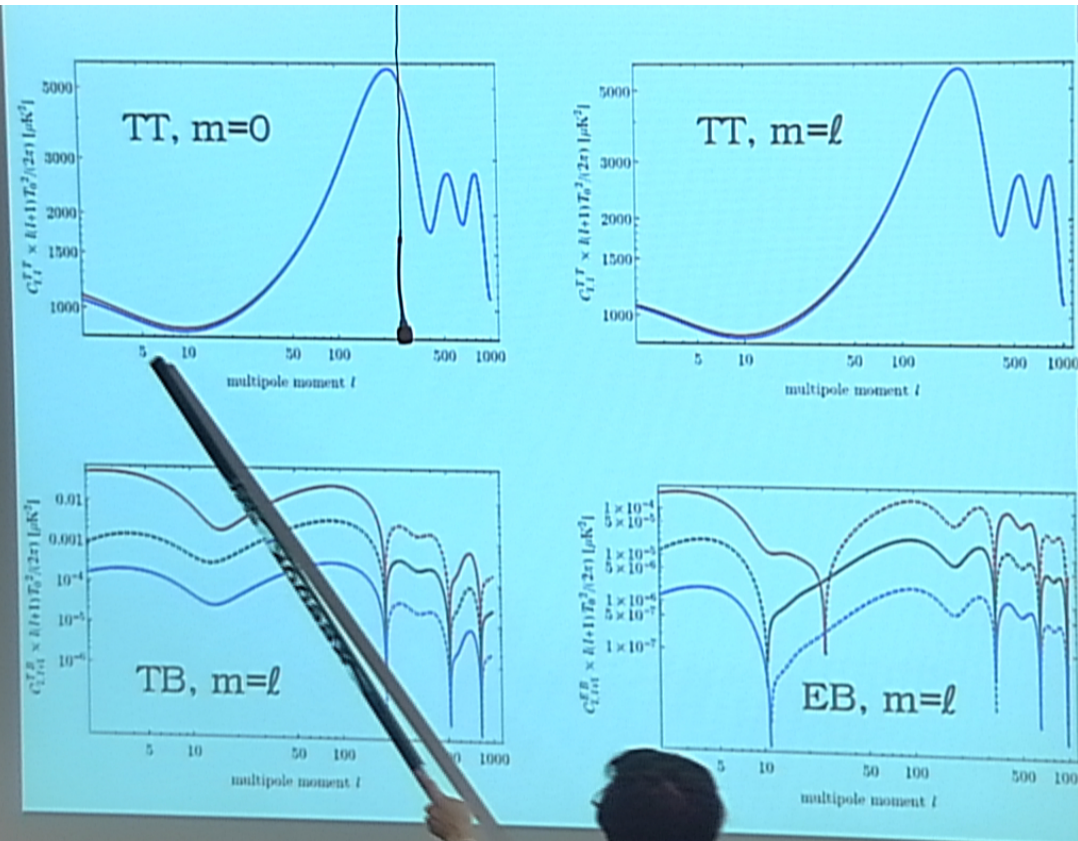
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Tensor-tensor \rightarrow TT dominates

X. Chen, R. Emami, H. Firouzjahi, YW, 1404.4083



Solid inflation,

$$\delta P_\zeta: \text{---} \zeta \text{---} \ast \text{---} \zeta \text{---}$$

$$\delta_{(1)} P_h: \text{---} h_+, h_x \text{---} \bullet \text{---} h_-, h_x \text{---}$$

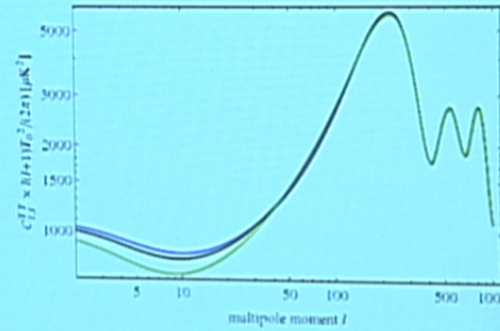
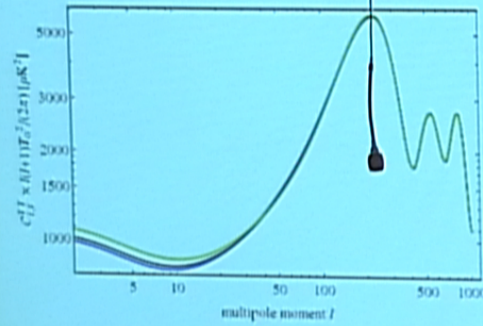
$$\delta_{(2)} P_h: \text{---} h_+ \text{---} \zeta \text{---} h_- \text{---}$$

$$P_{\zeta h}: \text{---} \zeta \text{---} \text{---} h_- \text{---}$$

Scalar-tensor \rightarrow TT dominates

M. Akhshik, R. Emami, H. Firouzjan, YV 1405-179

About low ℓ suppression

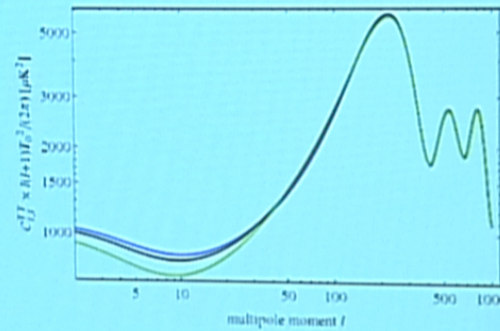
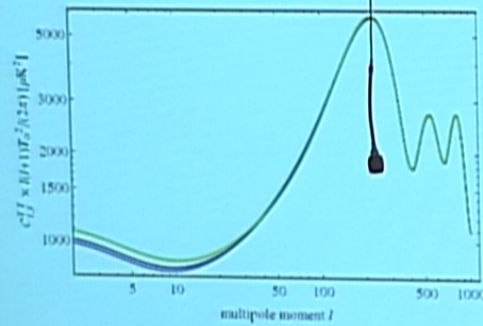


Here is a debate:

(with Contaldi, Peloso, Sorbo)

(average over l ? mask effect?)

About low ℓ suppression



Here is a debate:

(with Contaldi, Peloso, Sorbo)

(average over l ? mask effect?)

$$\mathcal{L}_3^{(K)} \supset M_K \frac{3\partial_a \pi \partial_b \pi \partial^2 \dot{\gamma}_{ab}}{2a}$$

$$\langle \gamma_{ij}(\mathbf{p}_1) \pi(\mathbf{p}_2) \pi(\mathbf{p}_3) \rangle = (2\pi)^3 \delta^3(\mathbf{p}_1 + \mathbf{p}_2 + \mathbf{p}_3) \frac{3M_K H^3 p_1 p_2 p_3 [P^2 + 12p_2 p_3 + 3P(p_2 + p_3)]}{4M_p^9 \epsilon^2 p_2^3 p_3^3 P^5} \Pi_{ijab}(\hat{\mathbf{p}}_1)$$

However, contribution from beyond decoupling

$$\delta \mathcal{L}_3^{(K)} = -\frac{6}{a} \epsilon M_K H^2 \pi (\partial_a \partial_b \pi \partial_a \partial_b \pi - \partial^2 \pi \partial^2 \pi) + \mathcal{O}(\epsilon^2) = -\frac{9}{a} M_K \epsilon H^2 \partial_a \pi \partial_a \pi \partial^2 \pi + \mathcal{O}(\epsilon^2)$$

$$\langle \pi_{\mathbf{p}_1} \pi_{\mathbf{p}_2} \pi_{\mathbf{p}_3} \rangle = (2\pi)^3 \delta^3(\mathbf{p}_1 + \mathbf{p}_2 + \mathbf{p}_3) \frac{9}{16} \frac{M_K H^2 (p_1^2 + p_2^2 - p_3^2) [P^3 + 3p_1 p_2 p_3 + P(p_1 p_2 + p_2 p_3 + p_3 p_1)]}{M_p^9 \epsilon^2 p_1^3 p_2^3 p_3^3 P^4} + (\mathbf{p}_1 \leftrightarrow \mathbf{p}_3) + (\mathbf{p}_2 \leftrightarrow \mathbf{p}_3) .$$

$$\langle T^\zeta T^\zeta T^\zeta \rangle \sim \langle \zeta \zeta \zeta \rangle, \quad \langle T^\gamma T^\zeta T^\zeta \rangle \sim \langle \gamma \zeta \zeta \rangle \sim \langle T^\zeta T^\zeta T^\zeta \rangle$$

Lesson: gravity cannot be ignored when comparing

How precise do we know about n_t ?

need to know k -space vs l -space

How precise do we know about n_t ?

$$\Delta n_t \sim \Delta \ln k / \Delta \ln r \sim (0.003/0.01) / (0.06/0.2) \sim 1$$

$$\Delta k \sim 0.003/\text{Mpc at } k \sim 0.01/\text{Mpc}$$

$$\Delta r \sim 0.06 \text{ at } r \sim 0.2$$

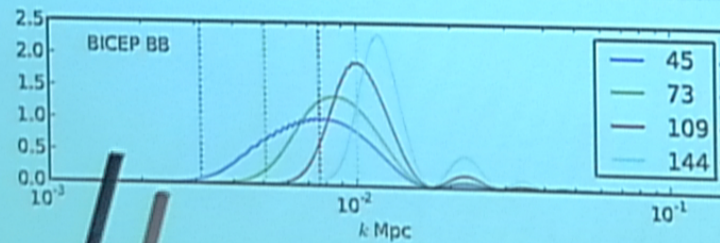


Figure by Lewis (CosmoCoffee)

Why positive n_t better fits data?

The BICEP2 side:

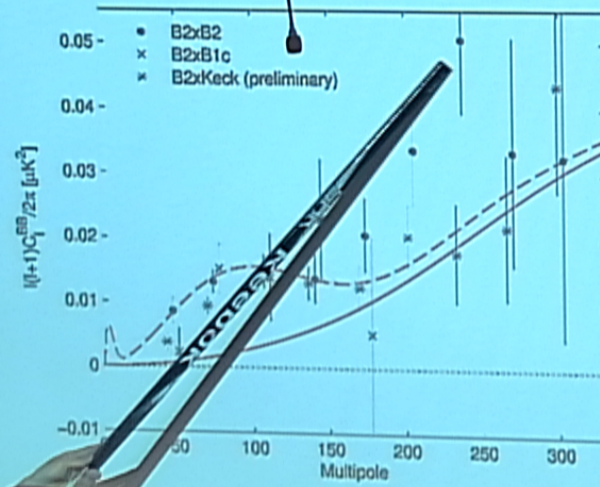
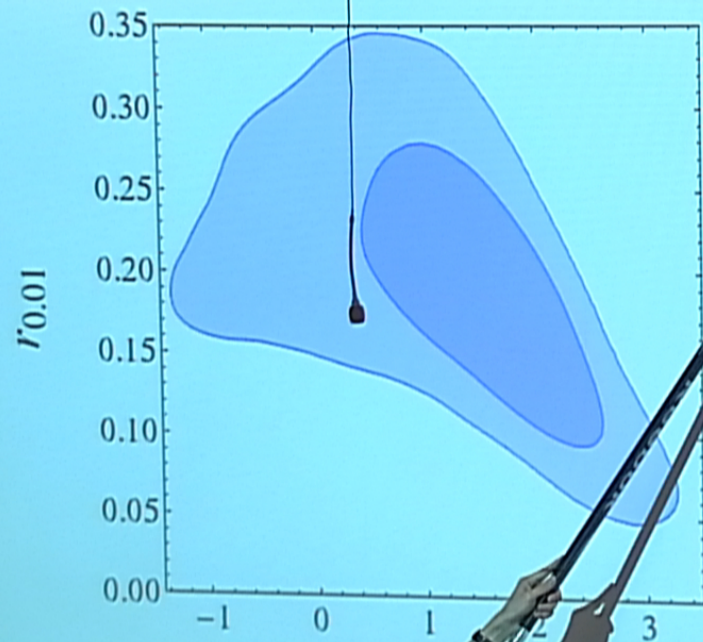


Figure: BICEP2



BICEP2 only:
blue $n_t \sim 1.5\sigma$

M. Gerbino, A. M... Di Valentino, A. Melchiorri, 1403.5732
YW, W. Xue, 1403.5817

Why positive n_t better fits data?

The Planck side:

power deficit @ $l \leq 40$
@ 5%~10% @ $2.5 \sim 3\sigma$

Another enhancement by
5% ($r=0.1$) ~10% ($r=0.2$)
would be another $2.5 \sim 3\sigma$

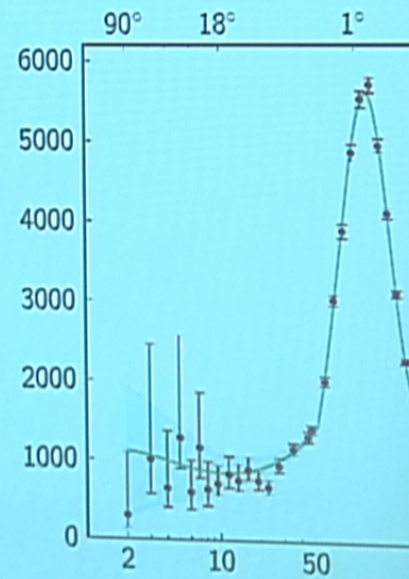


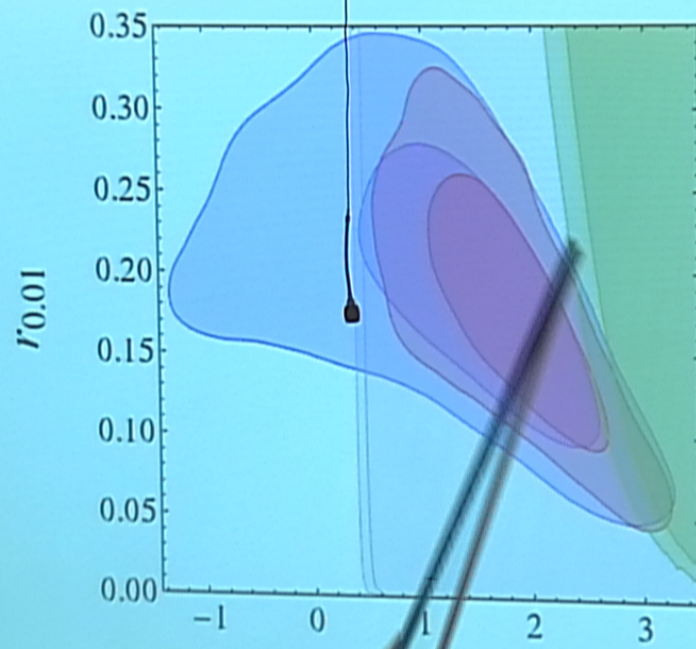
Figure: Planck XV

But n_t cannot be too blue

When $n_t > 2$,
primordial B-mode dominates over lensing

So the POLARBEAR signal of lensing B-mode
starts to constraint n_t

(need direct detection)
(cross correlation does not help)



Assuming
constant n_t for
50~60 e-folds

Implications:

~~$n_t > 0$ at more than 3.5σ ?~~

$n_t > 0$ at more than 3.5σ
compared with the minimal model

Implications:

$n_t > 0$ at more than 3.5σ
compared with the minimal model

But there may also be
foreground, running, isocurvature, neutrinos...

Advantage of n_t :

- Higher confidence level
- Can be tested soon (Planck)

Disadvantage of n_t :

- Smaller theoretical prior (read: challenge)

Tension between BICEP2 and Planck:

Not in tension? *et al.*, Audren, D. G. Figueroa, T. Tram, 1405.1390

Dangerous to measure tension of huge data sets
by one number!

Need to define null/alternative hypothesis

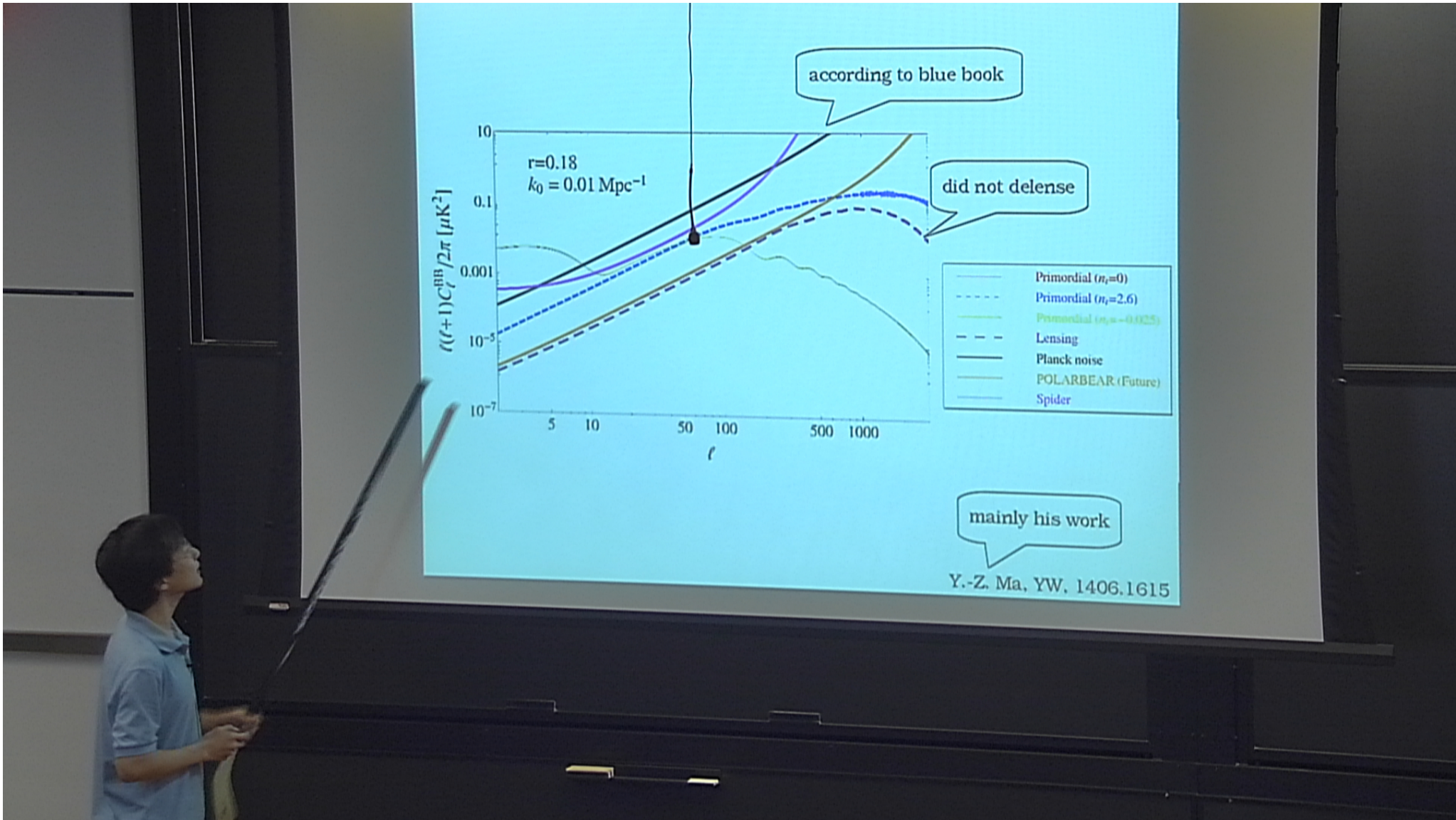
$n_t=0$ /blue n_t : Tension is at about $2\sim 3\sigma$

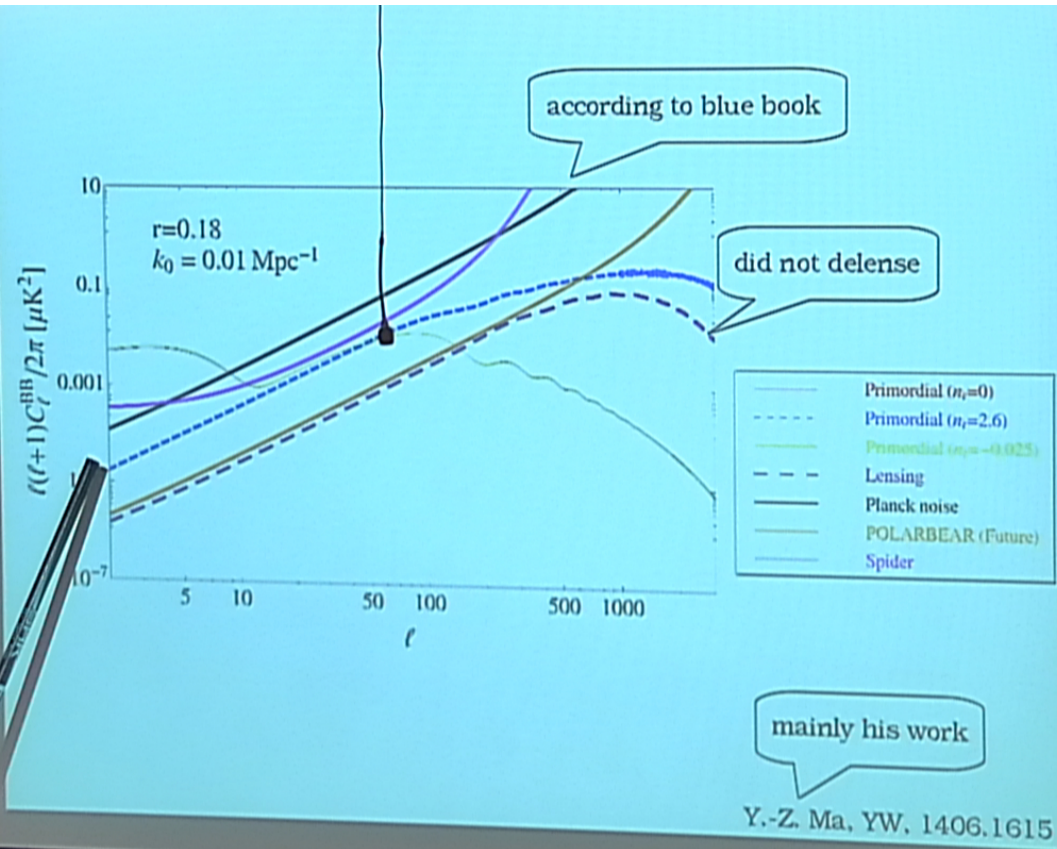
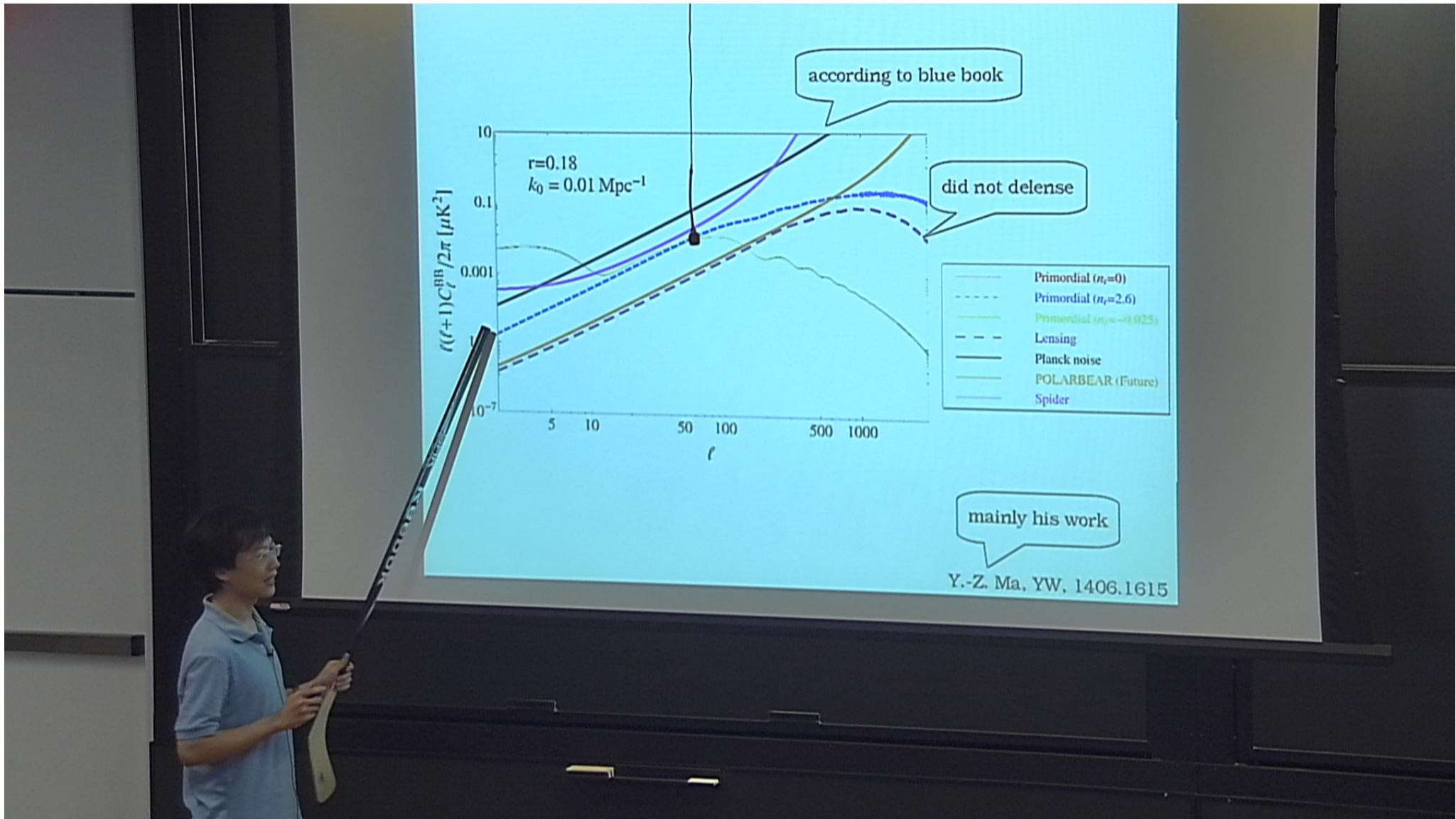
et al., Aslaksen, K. Dimopoulos, M. M. Sheikh-Jabbari, G. Shiu, 1403.6099

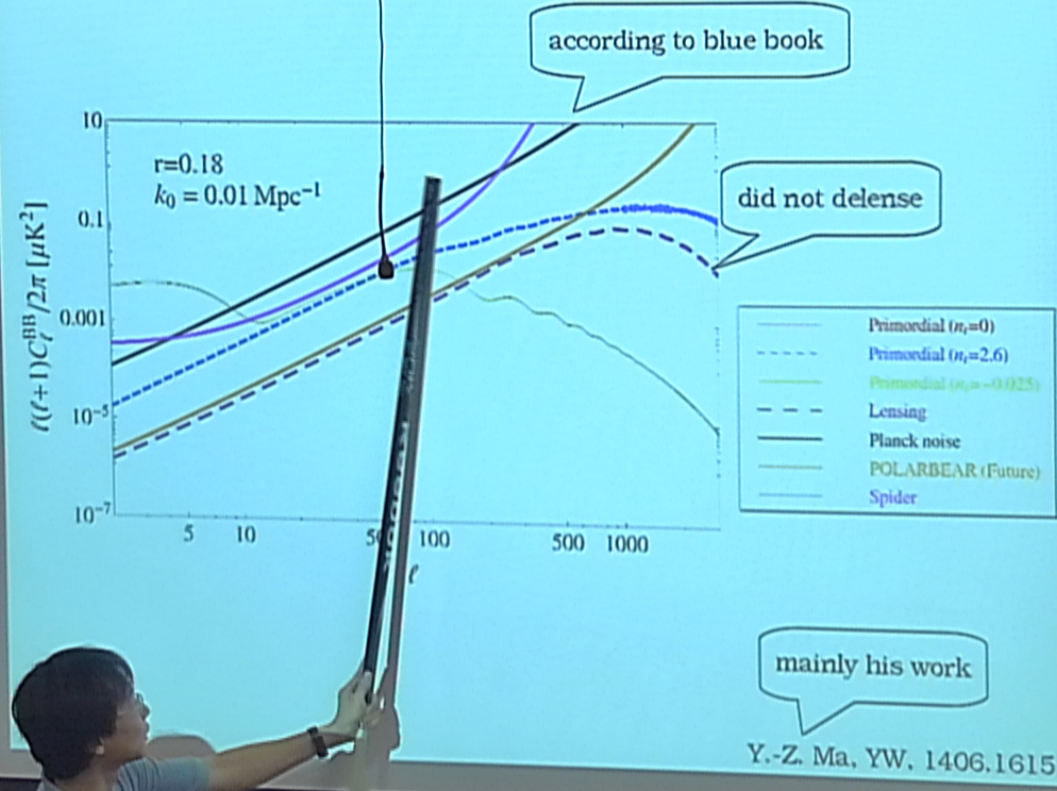
YW, W. Xue, 1403.5817

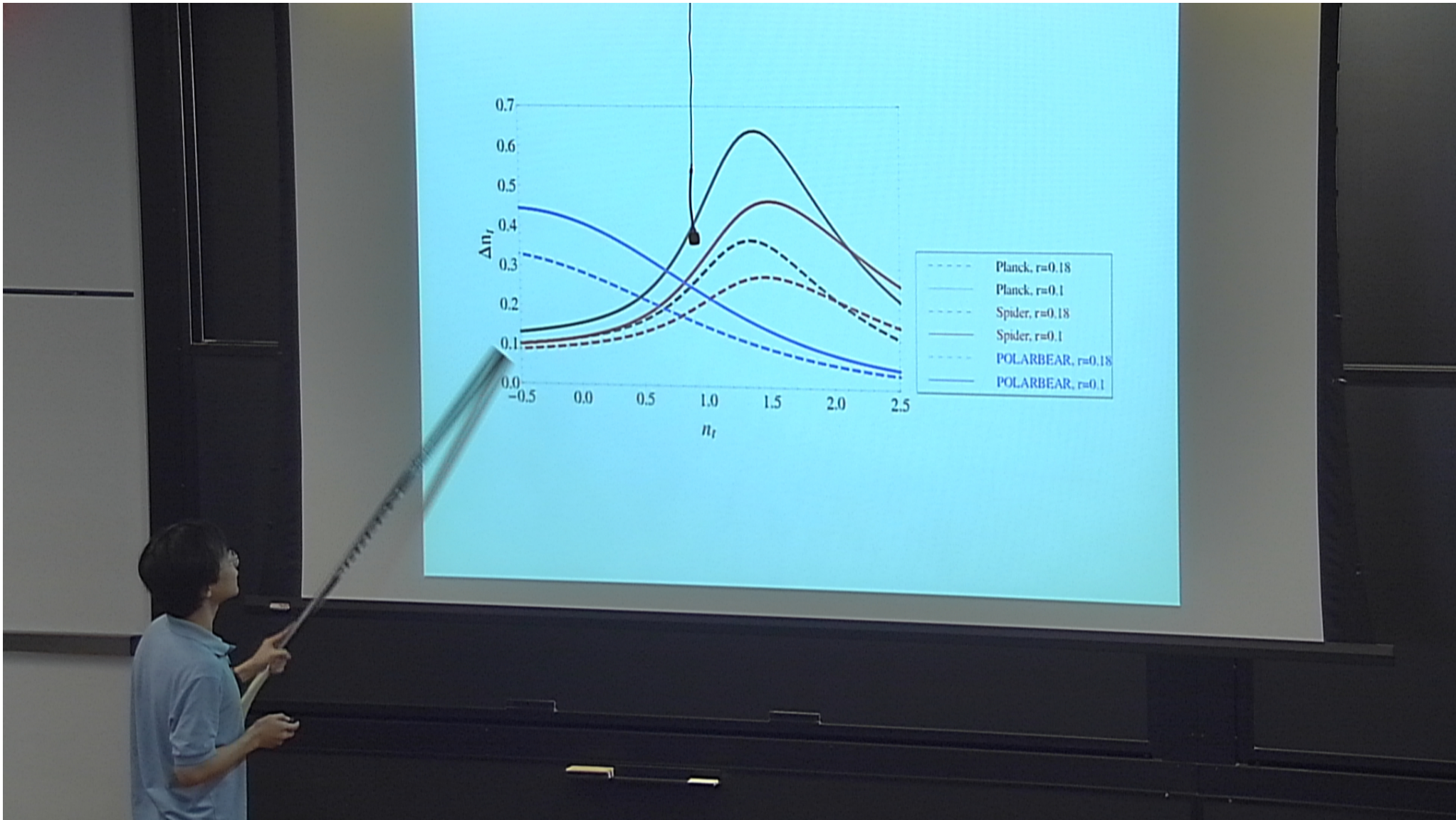
et al., M. S. ... C. ... kin, L. Boyle, N. Turok, M. Halpern, G. Hinshaw, B. Gold, 1404.0373

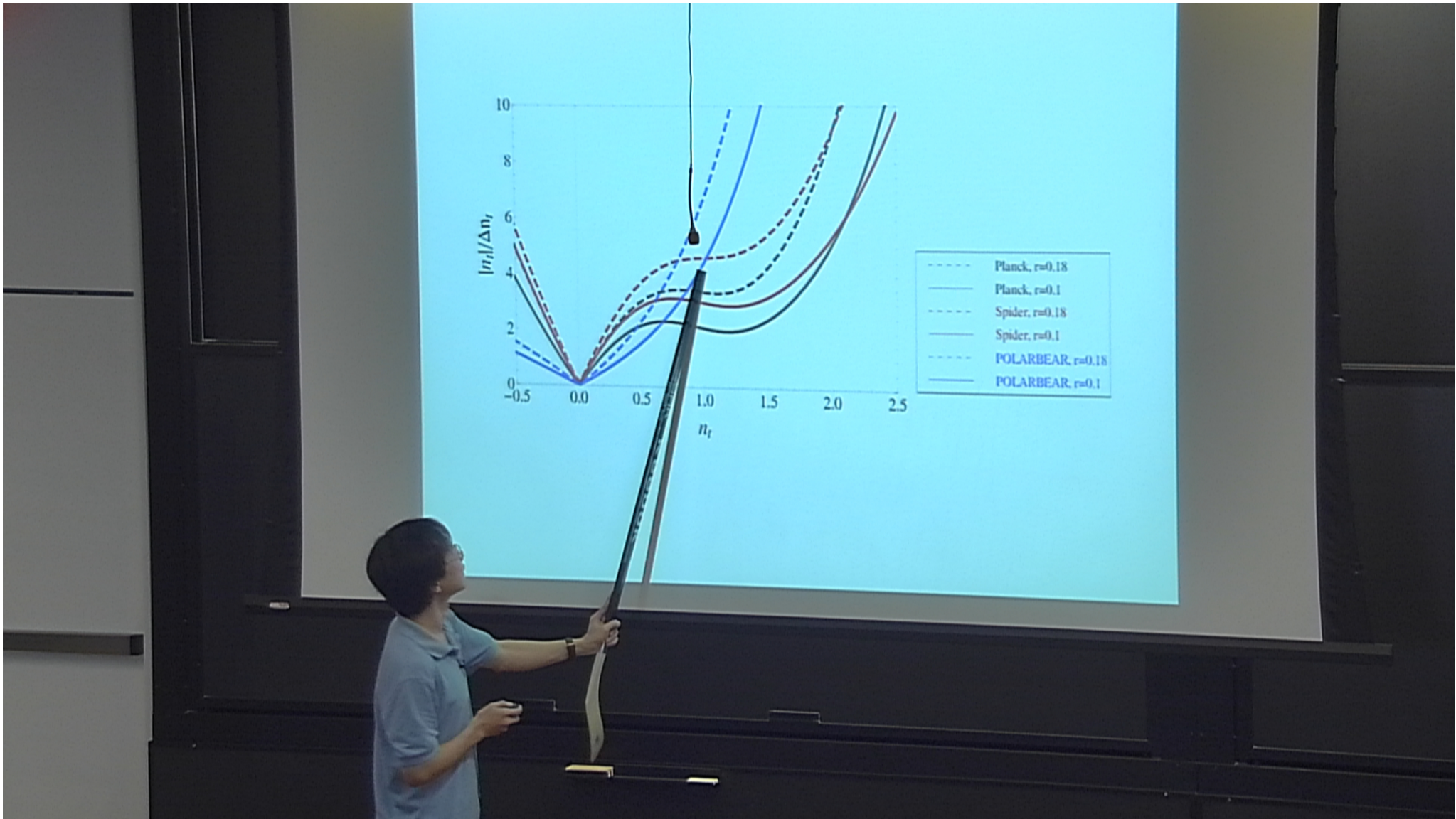
Y.-Z. Ma, YW, 1406.1615











Theories with blue n_t :

Inflation:

- Modified vacuum
- Particle production
- Modified tensor dispersion relation
- Galileons
- Solid inflation

Alternative to inflation:

- String gas cosmology (prediction)
- Matter bounce

YW, W. Xue, 1403.5817

A. Ashoorioon, K. Dimopoulos, M. M. Sheikh-Jabbari, G. Shiu, 1403.6099

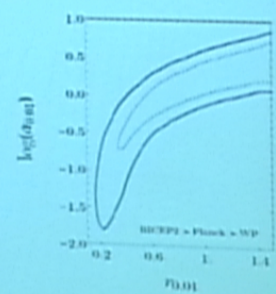
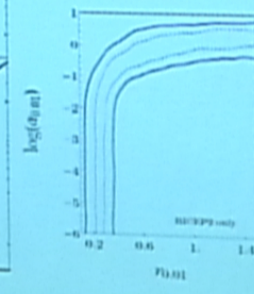
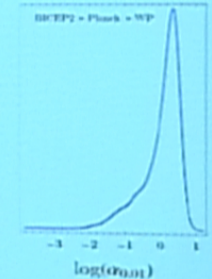
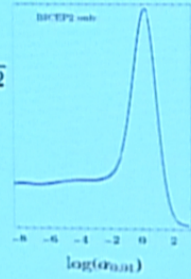
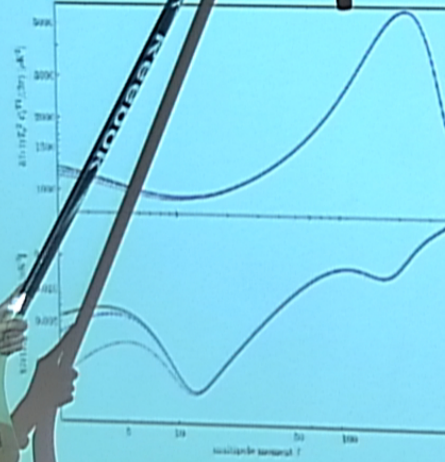
Y.-F. Cai, YW, 1404.6672

S. Mukohyama, R. Namba, M. Peloso, G. Shiu, 1405.0346

Example: modified tensor dispersion relation

$$[\pi_{ij}(\tau, \mathbf{k}), \pi_{kl}(\tau, \mathbf{k}')] = \alpha_{ijkl} \delta^{(3)}(\mathbf{k} - \mathbf{k}') \quad (\text{see also mass gravity})$$

$$P_T(k) = A_T \left(\frac{k}{k_{\text{pivot}}} \right)^{n_t} \frac{k^3}{(k^2 + \alpha^2 k_{\text{pivot}}^2)^{3/2}}$$

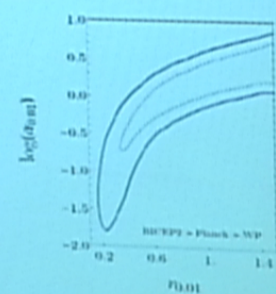
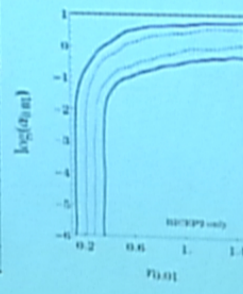
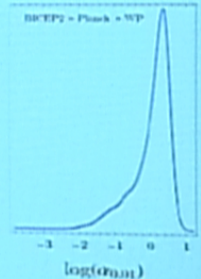
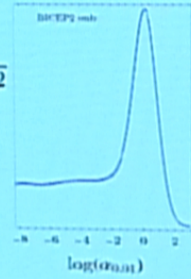
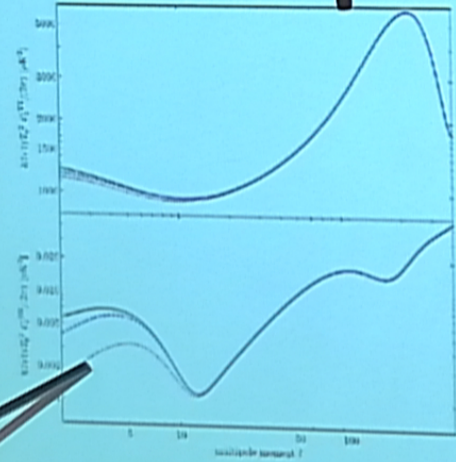


Y. Cai, YW

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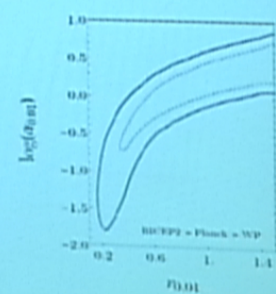
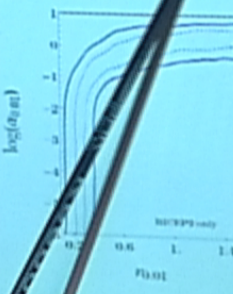
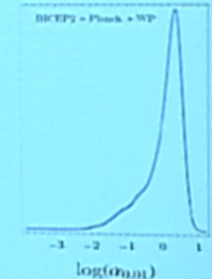
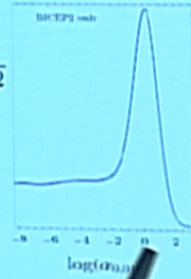
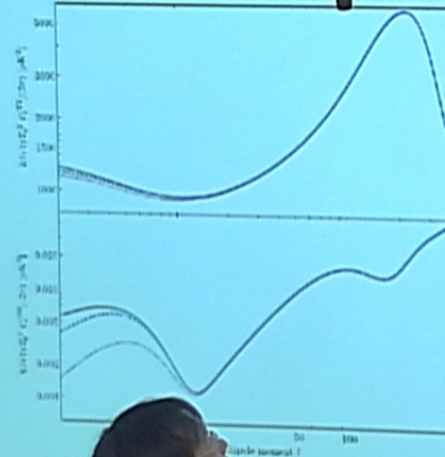


Y. Cai, YW

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Y. Cai, YW

Example: Galileons

existing Galileon models:

same color for scalar and tensor

But there can be exceptions, e.g.

$$\mathcal{L} = K(\phi, X) + G(\phi, X)\square\phi$$

$$K(\phi, X) = M_p^2 X - V(\phi) - M_p^3 g(\phi)(2X)^{\frac{1}{2}}$$

$$G(\phi, X) = M_p^2 \gamma(\phi) \left(\frac{2X}{M_p^2}\right)^p$$

Equilateral f_{NL} is at least $\mathcal{O}(10)$

With Y. Cai, J. Gong, S. Pi

Two topics concerning anomalies

- New proposals for existing anomalies
- New anomalies brought by BICEP2

Thank you!