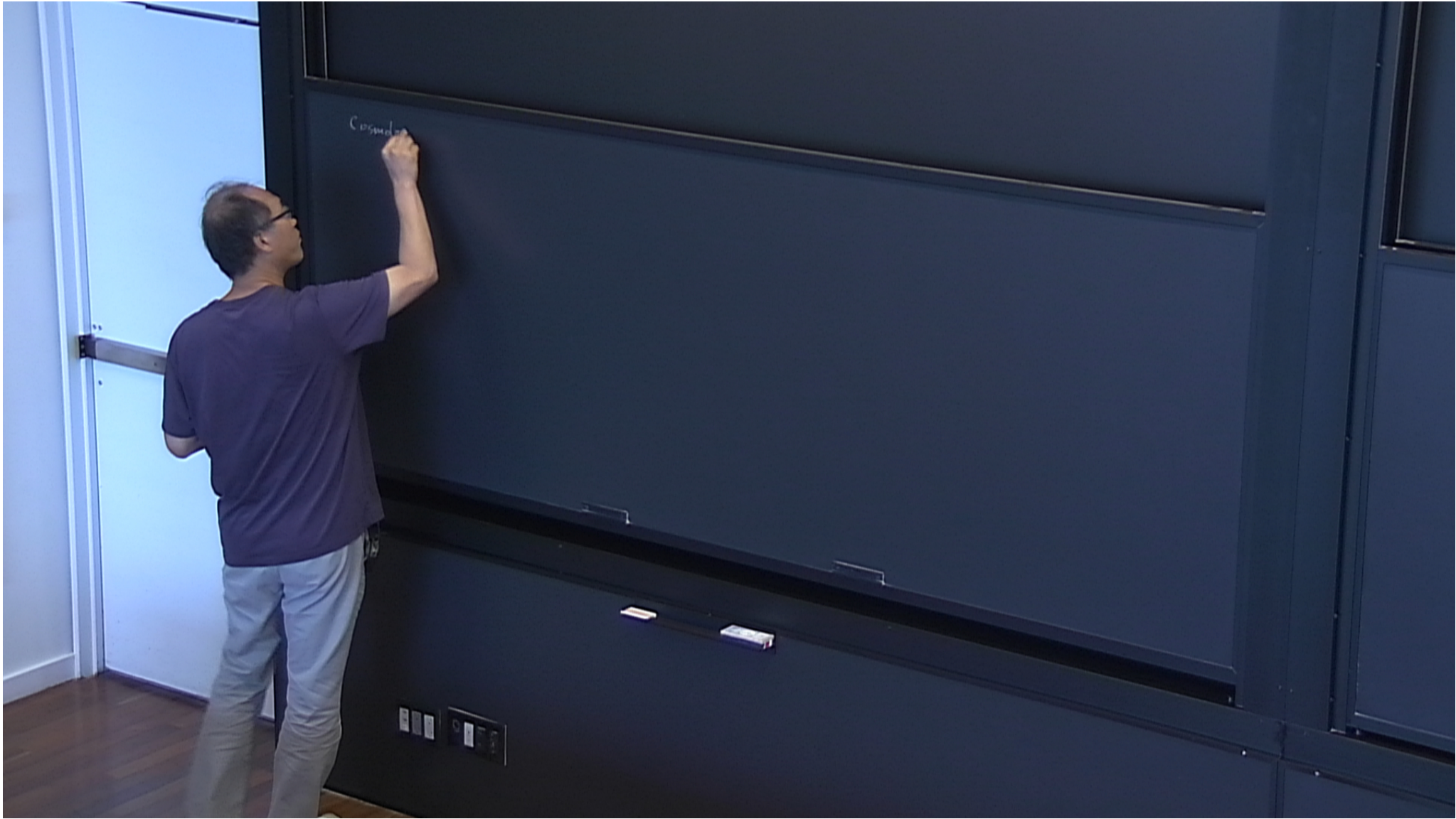


Title: Cosmological Coincidence Problem

Date: Jul 15, 2014 11:00 AM

URL: <http://pirsa.org/14070030>

Abstract: I will try to explain how cosmological coincidence of the two values, the matter energy density and the dark energy density, at the present epoch based on a single scalar field model with a quartic potential, non-minimally interacting with gravity. Dark energy in this model originates from the potential energy of the scalar field, which is sourced by the appearance of non-relativistic matter at the time $z \sim 10^{10}$. No fine tuning of parameters are necessary.



Cosmological Constant Problem

Cosmological Constant Problem

mechanism

J. Overduin
TH Lec. P 0h

Cosmological Coincidence Problem

J. Overduin
TH Lec. P. Oh

mechanism: p

Cosmological Coincidence Problem

J. Overduin
TH Lec. P 0h

mechanism: present value of dark energy

Cosmological Coincidence Problem

J. Overduin
TH Lec. P 0h

mechanism present value of dark energy

Ω

Cosmological Coincidence Problem

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TH Lec. P 0h

mechanism: present value of dark energy

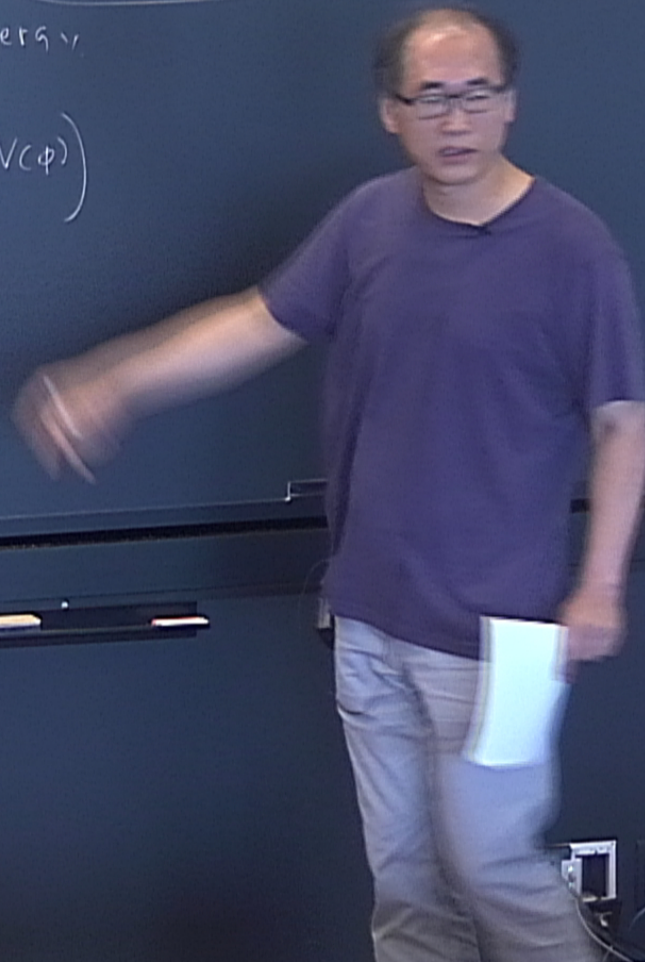
$$\mathcal{L} = F_3 \left(\frac{1}{2} \dot{\chi}^2(\phi) R - \frac{1}{2} k(\phi) (\partial\phi)^2 - V \right)$$

Cosmological Coincidence Problem

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mechanism: present value of dark energy,

$$\mathcal{L} = \int d^4x \left(\frac{1}{2} \underbrace{\dot{\chi}^2(\phi)}_{\text{kinetic}} - \frac{1}{2} k(\phi) (\partial\phi)^2 - V(\phi) \right)$$

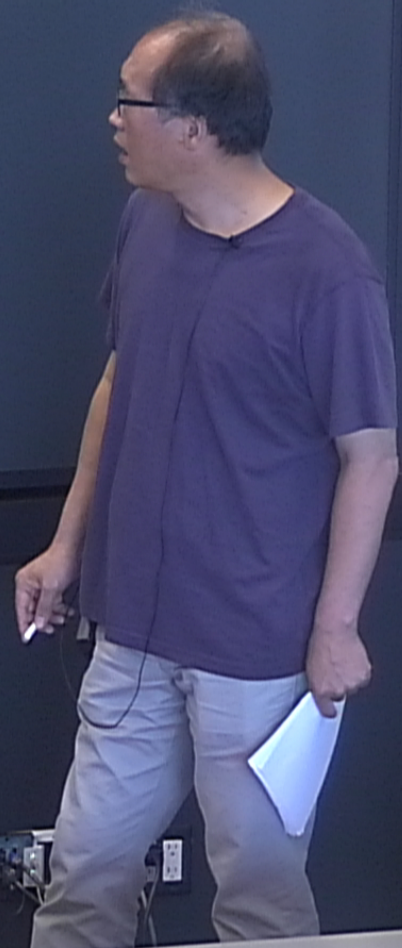


Cosmological Coincidence Problem

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mechanism: present value of dark energy

$$\mathcal{L} = \int d^4x \left(\frac{1}{2} \underline{\dot{\chi}^2} - \frac{1}{2} k(\phi) (\partial\phi)^2 - V(\phi) \right)$$



Cosmological Coincidence Problem

J. Overduin
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mechanism: present value of dark energy

$$\mathcal{L} = \int d^4x \left(\frac{1}{2} \underline{\dot{\chi}^2}(\phi) R - \frac{1}{2} k(\phi) (\partial\phi)^2 - V(\phi) \right)$$

G

Cosmological Coincidence Problem

J. Overduin
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mechanism: present value of dark energy

$$\mathcal{L} = F_3 \left(\frac{1}{2} \underline{\dot{\chi}^2}(\phi) R - \frac{1}{2} k(\phi) (\partial\phi)^2 - V(\phi) \right)$$

GR \Rightarrow

$$-2 \frac{\ddot{a}}{a} = \left(p + \frac{1}{3} \rho \right)$$

Cosmological Coincidence Problem

J. Overduin
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mechanism: present value of dark energy

$$\mathcal{L} = F \left(\frac{1}{2} \dot{\chi}^2 - \frac{1}{2} k(\phi) (\partial\phi)^2 - V(\phi) \right)$$

GR \Rightarrow

$$-2 \frac{\ddot{a}}{a} = \left(\rho + \frac{1}{3} p \right)$$

$$\ddot{a} > 0 \quad p < -\frac{1}{3} \rho < 0$$

Cosmological Coincidence Problem

J. Overduin
TH Lec. P 0h

mechanism: present value of dark energy

$$\mathcal{L} = \int d^4x \left(\frac{1}{2} \dot{\phi}^2 - \frac{1}{2} k(\phi) (\partial\phi)^2 - V(\phi) \right)$$

GR \Rightarrow

$$-\frac{\ddot{a}}{a} = \left(\rho + \frac{1}{3} p \right)$$

$$\ddot{a} > 0$$

$$p < -\frac{1}{3} \rho < 0$$

normal matter

Cosmological Coincidence Problem

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mechanism: present value of dark energy

$$\mathcal{L} = \int d^4x \left(\frac{1}{2} \dot{\phi}^2 - \frac{1}{2} k(\phi) (\partial\phi)^2 - V(\phi) \right)$$

$$= (p + \frac{1}{3}\rho)$$

$\ddot{a} > 0$
 $p < -\frac{1}{3}\rho < 0$
 $p > 0$ for normal matter.

$\ddot{a} > 0$
possible if $p < 0$

Cosmological Coincidence Problem

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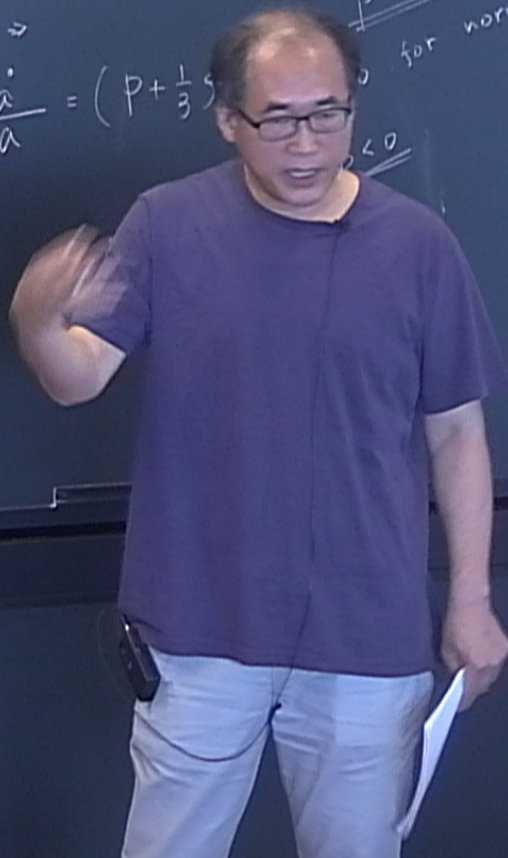
mechanism: present value of dark energy

$$\mathcal{L} = \int d^4x \left(\frac{1}{2} \dot{\phi}^2 - \frac{1}{2} k(\phi) (\partial\phi)^2 - V(\phi) \right)$$

GR \Rightarrow

$$-2 \frac{\ddot{a}}{a} = (\rho + \frac{1}{3} p)$$

$\ddot{a} > 0$
 $p < -\frac{1}{3} \rho < 0$
for normal matter.



Cosmological Coincidence Problem

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mechanism: present value of dark energy

$$\mathcal{L} = \Gamma \left(\frac{1}{2} \dot{\alpha}^2 R - \frac{1}{2} k(\phi) (\partial\phi)^2 - V(\phi) \right)$$



GR \Rightarrow

$$-2 \frac{\ddot{a}}{a} = \left(\rho + \frac{1}{3} p \right)$$

$\ddot{a} > 0$

$$p < -\frac{1}{3} \rho < 0$$

$p > 0$ for normal matter

$\ddot{a} > 0$ possible if $p < 0$
 $p = w \rho$
 $\Rightarrow \rho$ more slowly

Cosmological Coincidence Problem

J. Overduin
TH Lec P 0h

mechanism: present value of dark energy

$$\mathcal{L} = \sqrt{-g} \left(\frac{1}{2} \dot{\phi}^2 - \frac{1}{2} k(\phi) (\partial\phi)^2 - V(\phi) \right)$$

GR \Rightarrow

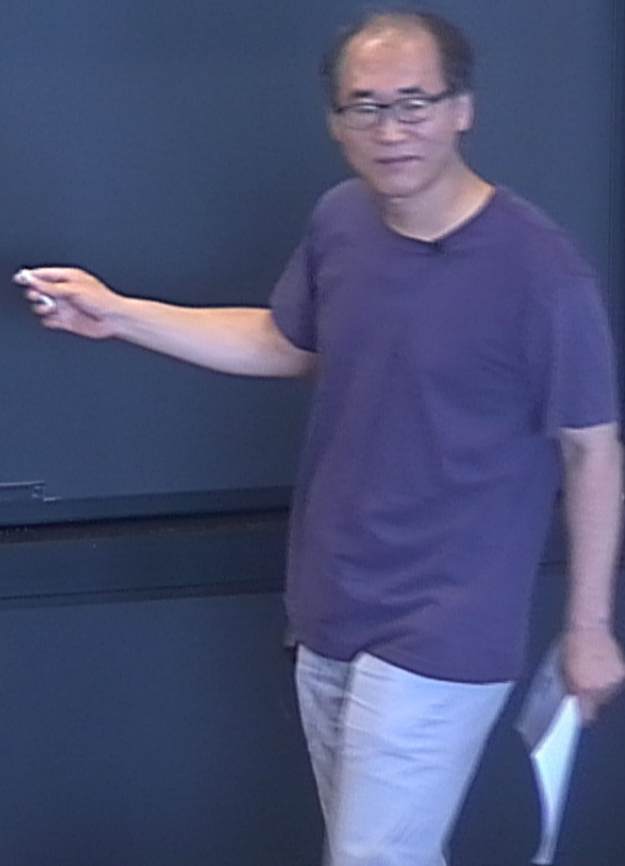
$$-2 \frac{\ddot{a}}{a} = \left(\rho + \frac{1}{3} p \right)$$

$\ddot{a} > 0$
 $p < -\frac{1}{3} \rho < 0$
for normal matter.

$\ddot{a} > 0$ possible if $p < 0$
 $p = w \rho$
 $\Rightarrow \rho$ more slowly than $\frac{1}{a^2}$

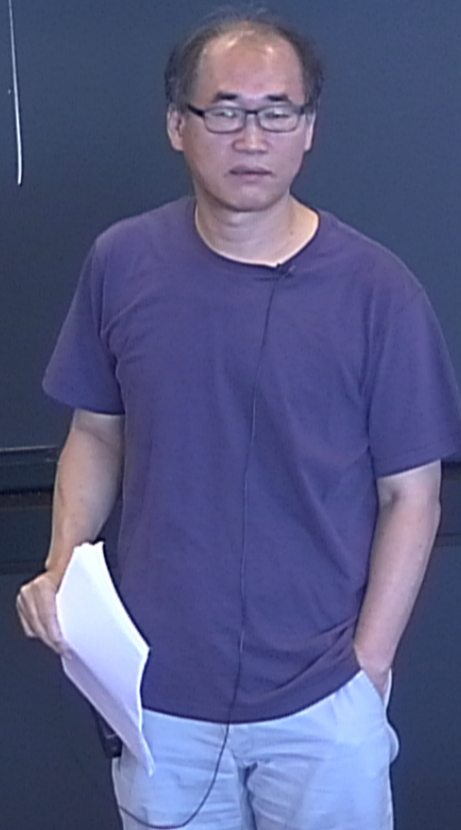
- ① our universe $\ddot{a} > 0$
- ② transition from $\ddot{a} < 0$ to $\ddot{a} > 0$ recently
- ③ P_{d_0}

- ① our universe $\ddot{a} > 0$
- ② transition from $\ddot{a} < 0$ to $\ddot{a} > 0$ recently
- ③ $\rho_{d0} \approx 3\rho_{m0}$, $\rho_{d0} \approx \text{constant}$ recent past

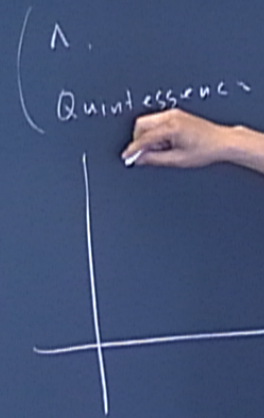


- ① our universe $\ddot{a} > 0$
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- ③ $\rho_{d0} \approx 3\rho_{m0}$, $\rho_{d0} \approx \text{constant}$ recent past
 $(z \sim \underline{5-10})$

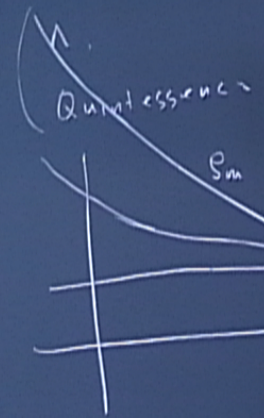
Λ
Quintessence



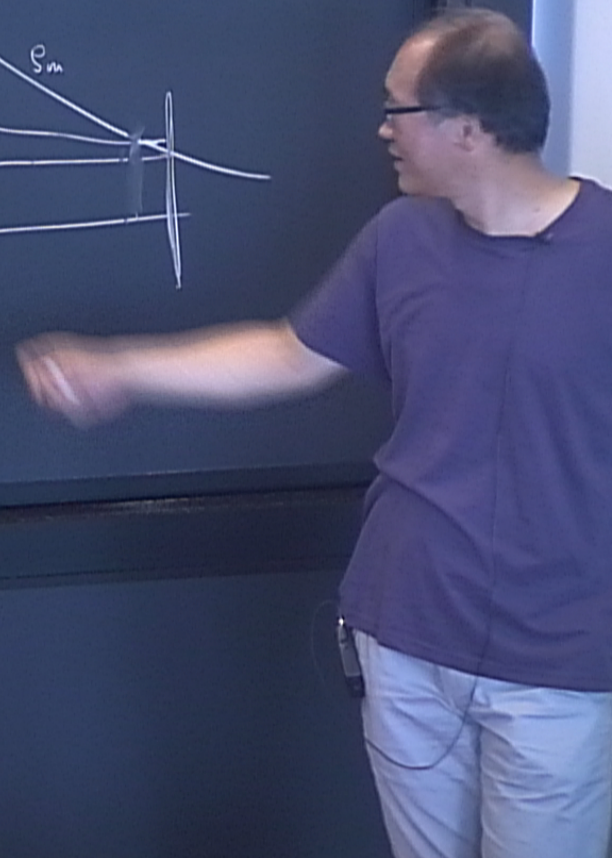
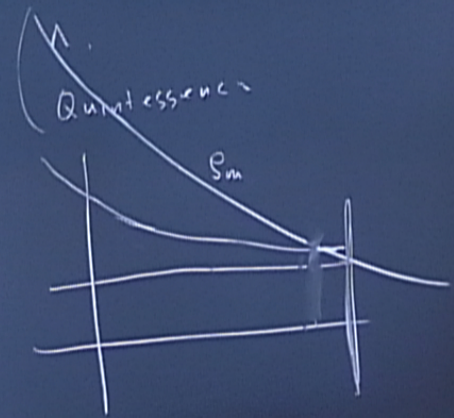
- ① our universe $\ddot{a} > 0$
- ② transition from $\ddot{a} < 0$ to $\ddot{a} > 0$ recently
- ③ $\rho_{d0} \approx 3 \rho_{m0}$, $\rho_{d0} \approx \text{constant}$ recent past
 $(z \sim 5 \sim 10)$



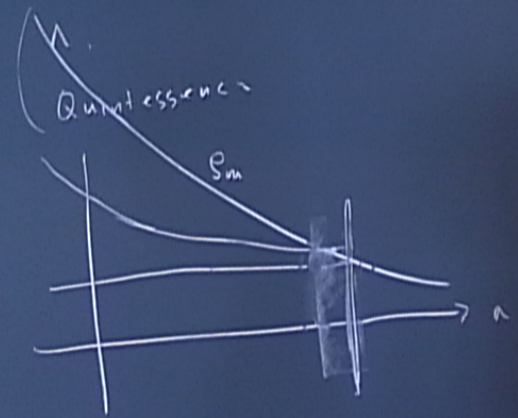
- ① our universe $\ddot{a} > 0$
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 $(z \sim 5 \sim 10)$



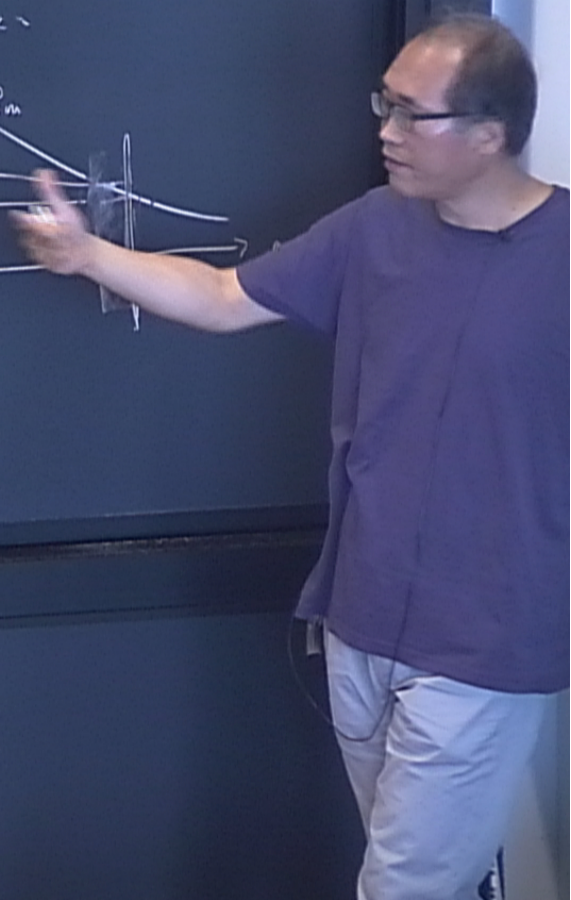
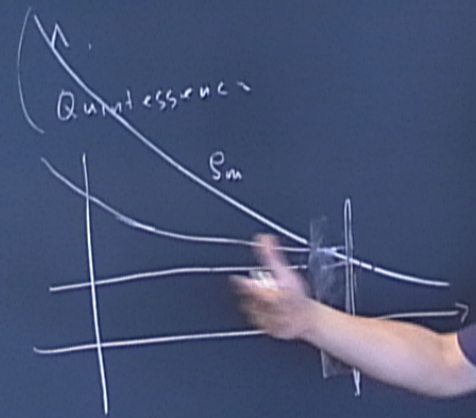
- ① our universe $\ddot{a} > 0$
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- ③ $\rho_{d0} \approx 3 \rho_{m0}$, $\rho_{d0} \approx \text{constant}$ recent past
 $(z \sim 5 \sim 10)$



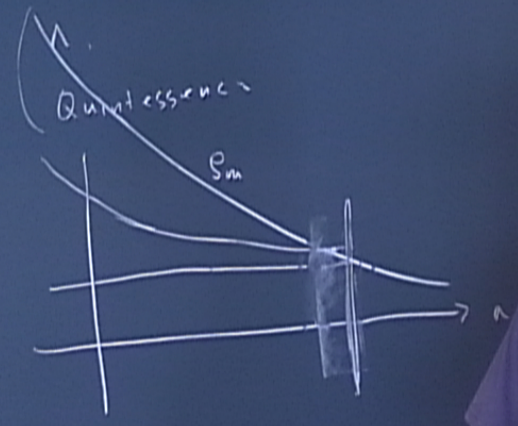
- ① our universe $\ddot{a} > 0$
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 $(z \sim 5 \sim 10)$



- ① our universe $\ddot{a} > 0$
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- ③ $\rho_{d0} \approx 3 \rho_{m0}$, $\rho_{d0} \approx \text{constant}$ recent past
 $(z < 10 \approx a)$
 $\frac{a_0}{a}$



- ① our universe $\ddot{a} > 0$
- ② transition from $\ddot{a} < 0$ to $\ddot{a} > 0$ recently
- ③ $\rho_{d0} \approx 3 \rho_{m0}$, $\rho_{d0} \approx \text{constant}$ recent past
 $(z < 10 \approx a)$
 $\frac{a_0}{a}$



Non-minimal coupling.

$$\mathcal{L} = \int -\frac{1}{2} \dot{\alpha}^2(\phi) R - \frac{1}{2} k_{10}$$

Non-minimal coupling

$$\mathcal{L} = \int -\frac{1}{2} \left(\frac{1}{2} k(\phi) (\partial\phi)^2 - V(\phi) \right) + \mathcal{L}_m$$



Non-minimal coupling.

$$\mathcal{L} = \int -g \left(\frac{1}{2} \alpha^2(\phi) R - \frac{1}{2} k(\phi) (\partial\phi)^2 - V(\phi) \right) + \mathcal{L}_m$$

$$\downarrow \quad g_{\mu\nu} \rightarrow \alpha^2(\phi) g_{\mu\nu}$$

$$\mathcal{L} = \int -g \left(\frac{1}{2} R - \frac{1}{2} k_E(\phi) (\partial\phi)^2 - V \right)$$

Non-minimal coupling.

$$\mathcal{L} = \int -\frac{1}{2} \alpha^2(\phi) R - \frac{1}{2} k(\phi) (\partial\phi)^2 - V_E(\phi) + \mathcal{L}_m(\dot{\chi}(\phi))$$

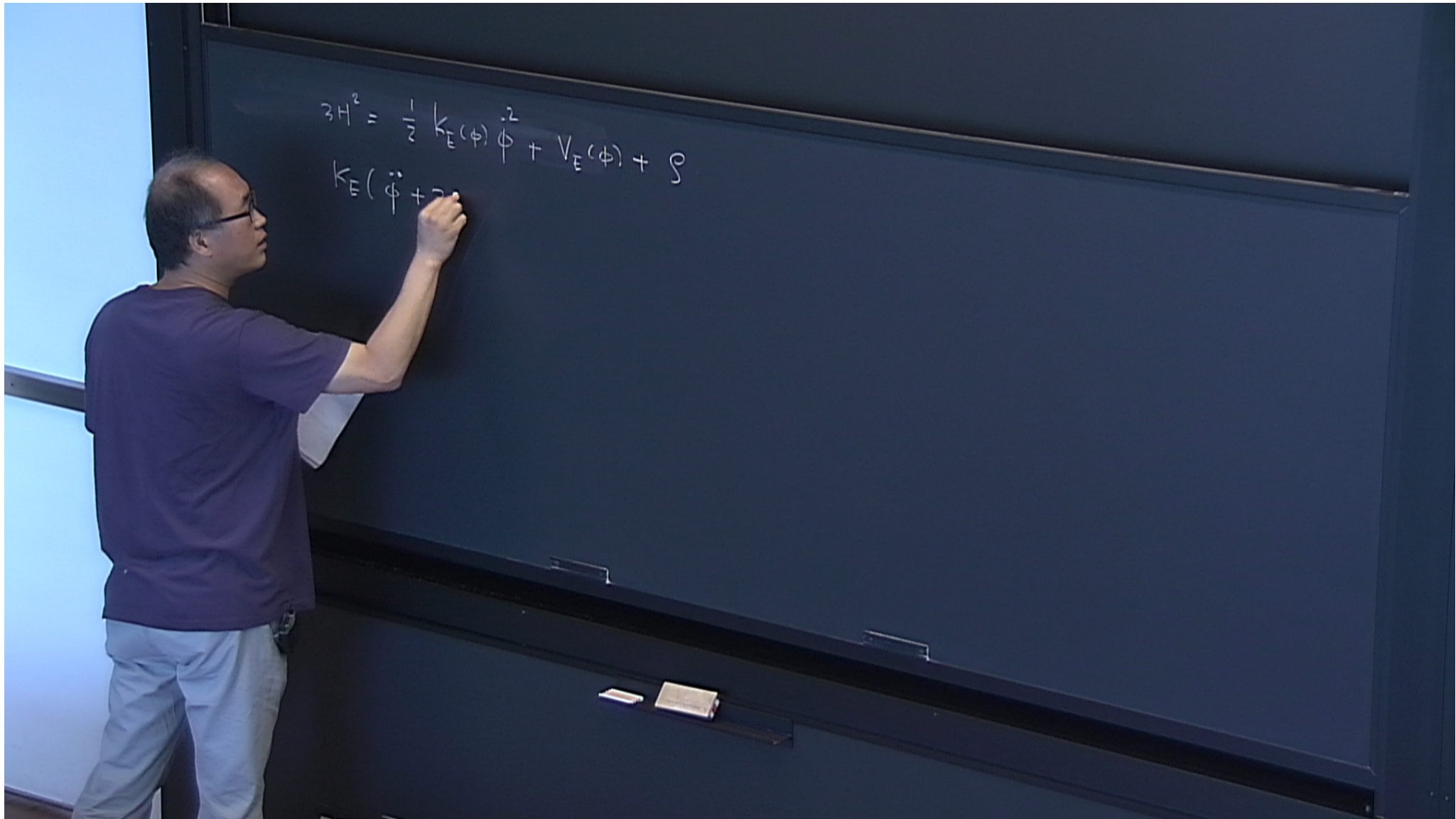
$$\downarrow \quad g_{\mu\nu} \rightarrow \alpha^2(\phi) g_{\mu\nu} \quad \mathcal{L} = \int$$

Non-minimal coupling.

$$\mathcal{L} = \int -g \left(\frac{1}{2} \alpha^2(\phi) R - \frac{1}{2} k(\phi) (\partial\phi)^2 - V(\phi) \right) + \mathcal{L}_m$$

$$\downarrow \quad g_{\mu\nu} \rightarrow \alpha^2(\phi) g_{\mu\nu}$$

$$\mathcal{L} = \int -g \left(\frac{1}{2} R - \frac{1}{2} k_E(\phi) (\partial\phi)^2 - V_E(\phi) \right) + \mathcal{L}_m(\alpha^2(\phi))$$



$$3H^2 = \frac{1}{2} k_E(\phi) \dot{\phi}^2 + V_E(\phi) + \rho$$

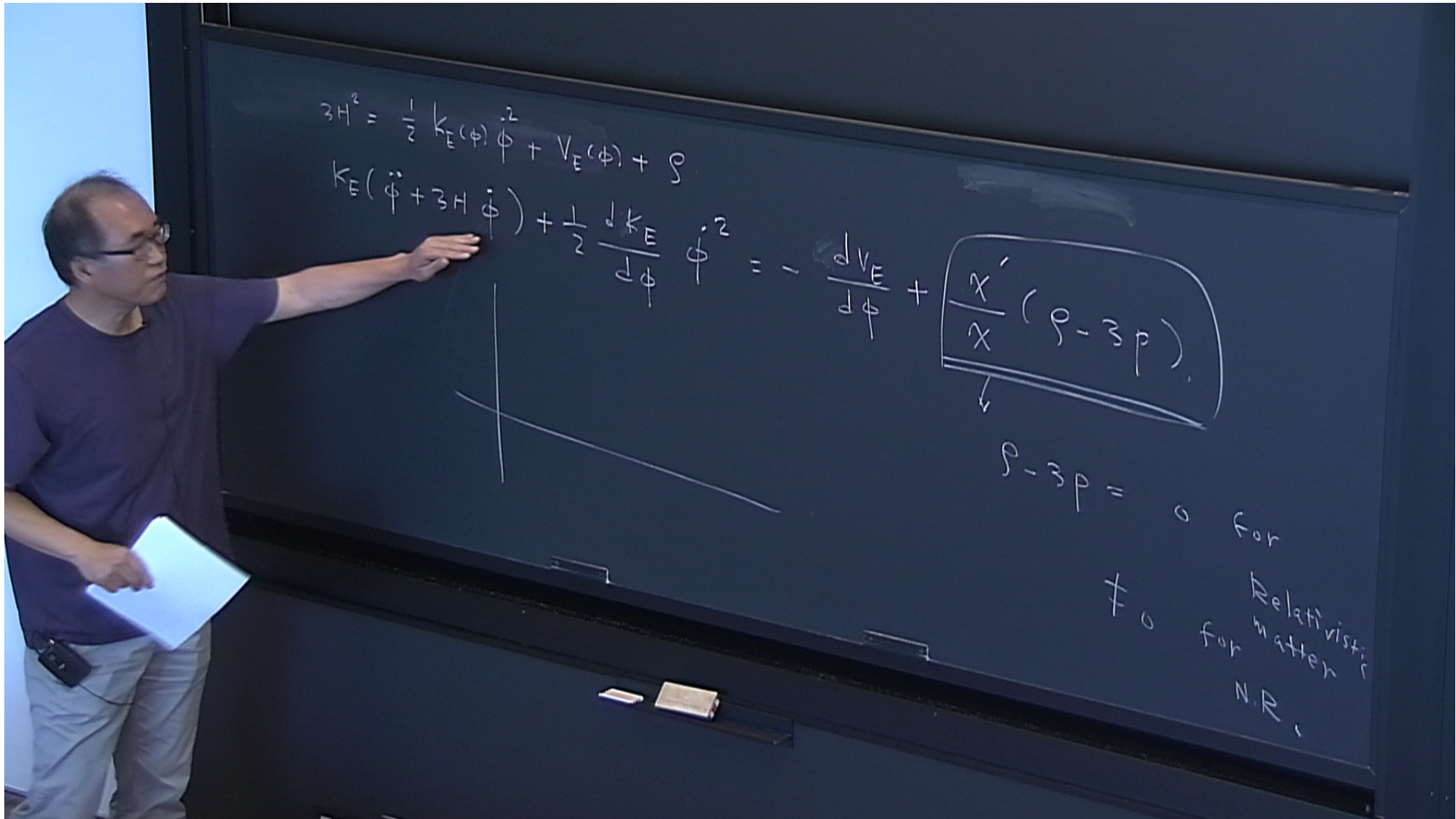
$$k_E(\ddot{\phi} + 3H\dot{\phi}) + \frac{1}{2} \frac{dk_E}{d\phi} \dot{\phi}^2 = - \frac{dV_E}{d\phi} + \frac{\rho'}{\rho} (\rho - 3p)$$

$$3H^2 = \frac{1}{2} K_E(\phi) \dot{\phi}^2 + V_E(\phi) + \rho$$

$$K_E(\ddot{\phi} + 3H\dot{\phi}) + \frac{1}{2} \frac{dK_E}{d\phi} \dot{\phi}^2 = - \frac{dV_E}{d\phi} + \frac{\rho'}{\rho} (\rho - 3p)$$

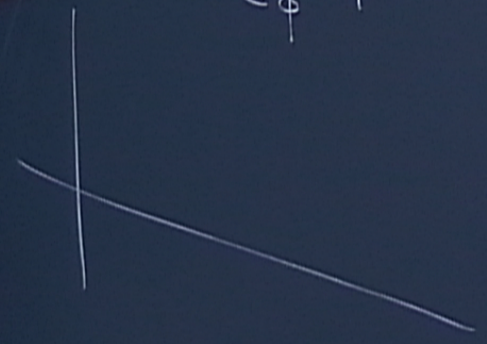
$$3H^2 = \frac{1}{2} K_E(\phi) \dot{\phi}^2 + V_E(\phi) + \rho$$

$$K_E(\ddot{\phi} + 3H\dot{\phi}) + \frac{1}{2} \frac{dK_E}{d\phi} \dot{\phi}^2 = - \frac{dV_E}{d\phi} + \frac{\dot{\chi}'}{\chi} (\rho - 3p)$$

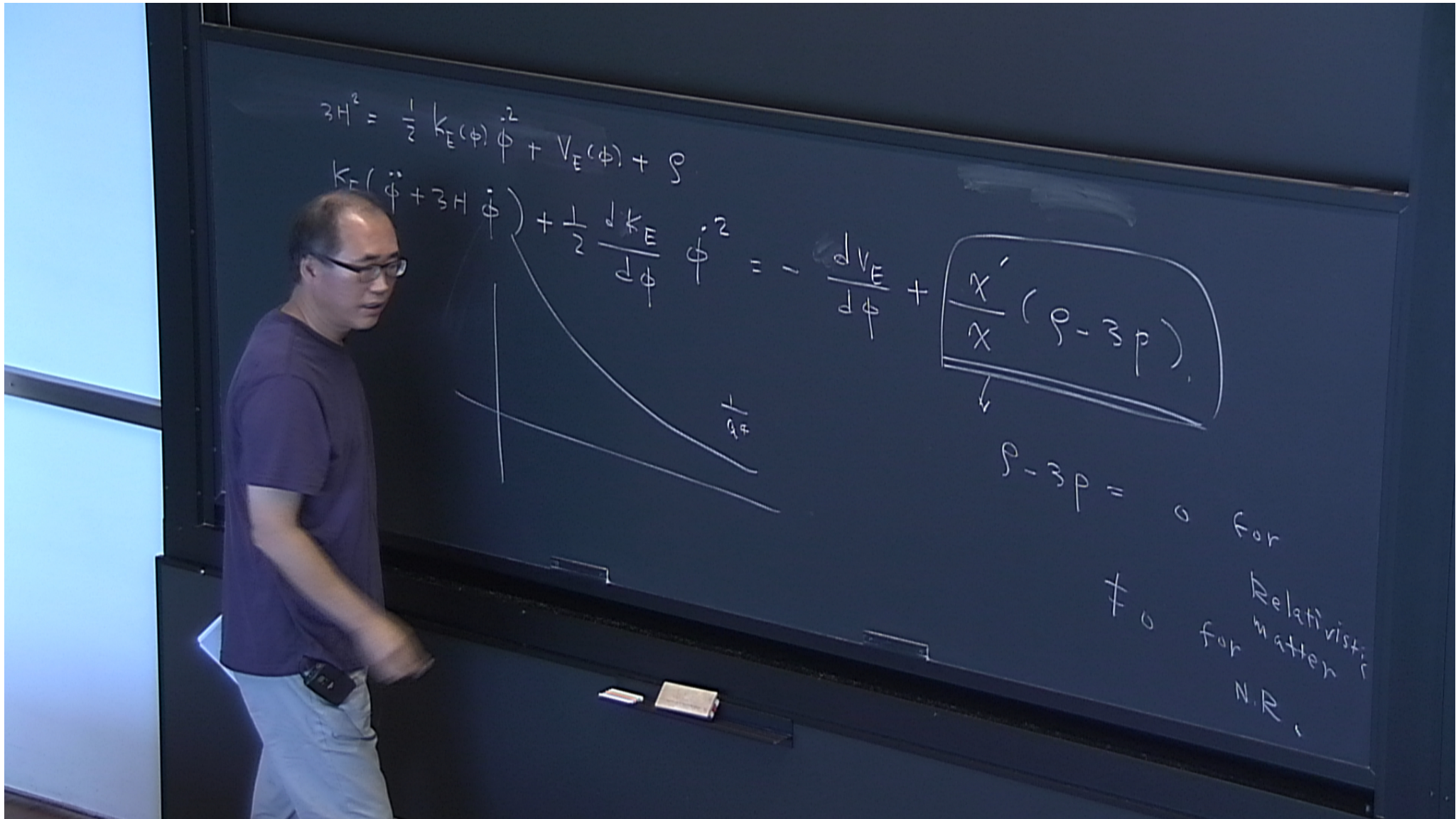


$$3H^2 = \frac{1}{2} K_E(\phi) \dot{\phi}^2 + V_E(\phi) + \rho$$

$$K_E(\phi)(\ddot{\phi} + 3H\dot{\phi}) + \frac{1}{2} \frac{dK_E}{d\phi} \dot{\phi}^2 = - \frac{dV_E}{d\phi} + \frac{X'}{X} (\rho - 3p)$$

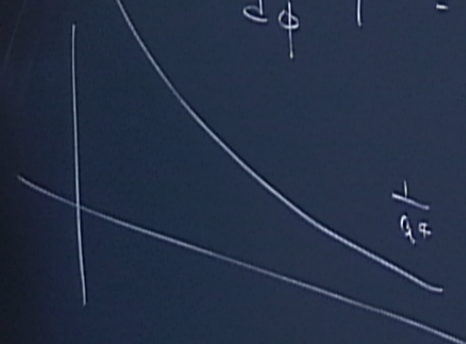


$\rho - 3p = 0$ for
 Relativistic
 matter
 $\neq 0$ for matter
 N.R.

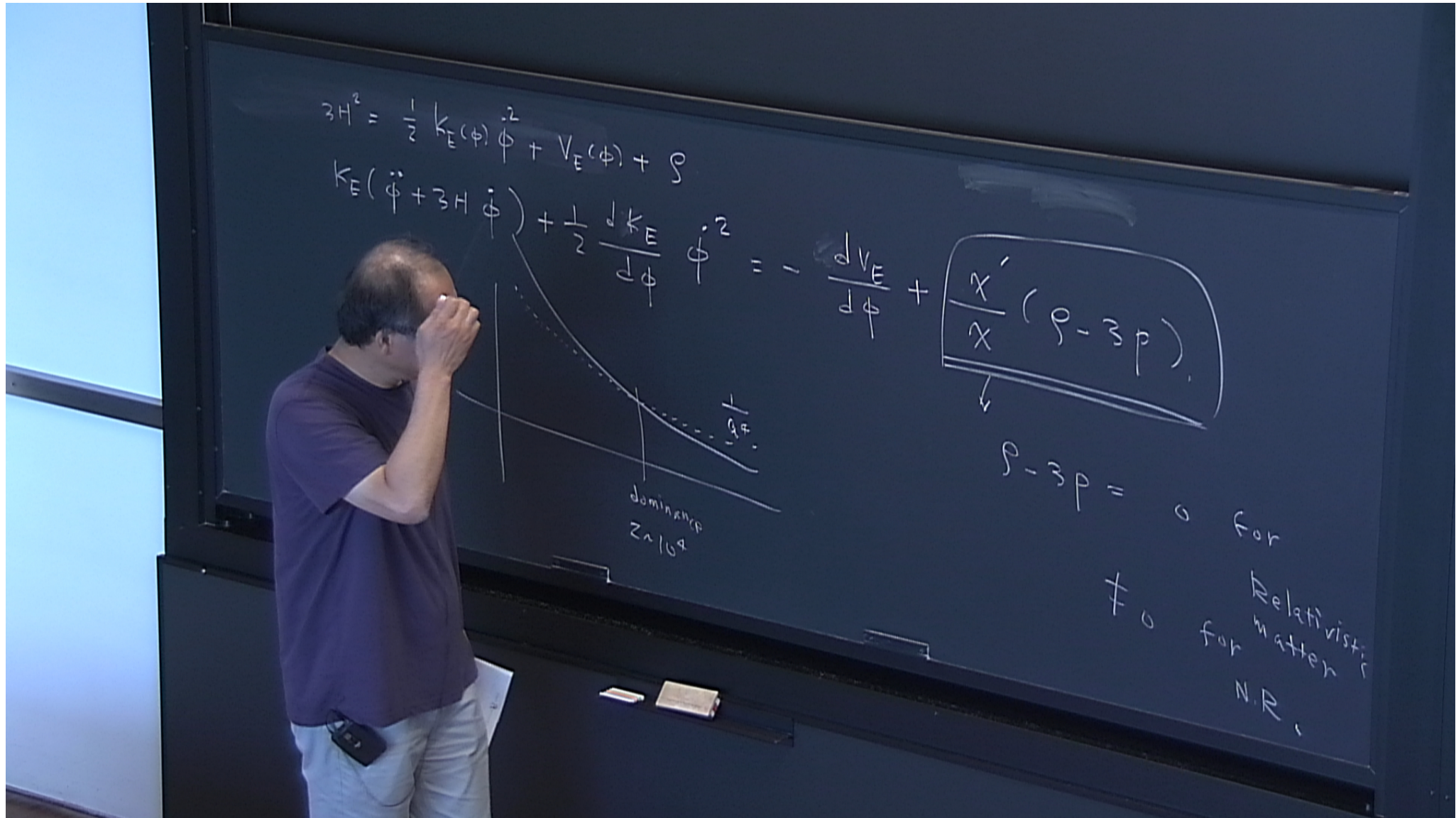


$$3H^2 = \frac{1}{2} \dot{\phi}^2 + V_E(\phi) + \rho$$

$$K_E(\ddot{\phi} + 3H\dot{\phi}) + \frac{1}{2} \frac{dK_E}{d\phi} \dot{\phi}^2 = - \frac{dV_E}{d\phi} + \frac{\dot{\chi}}{\chi} (\rho - 3p)$$

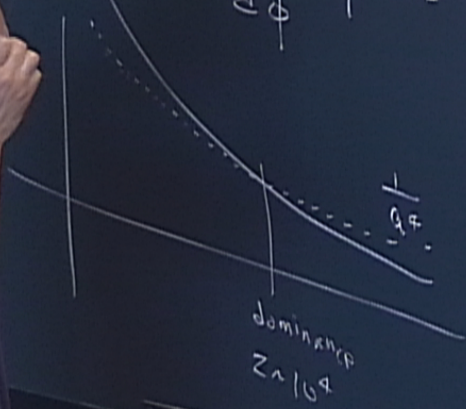


$\rho - 3p = 0$ for
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 N.R.

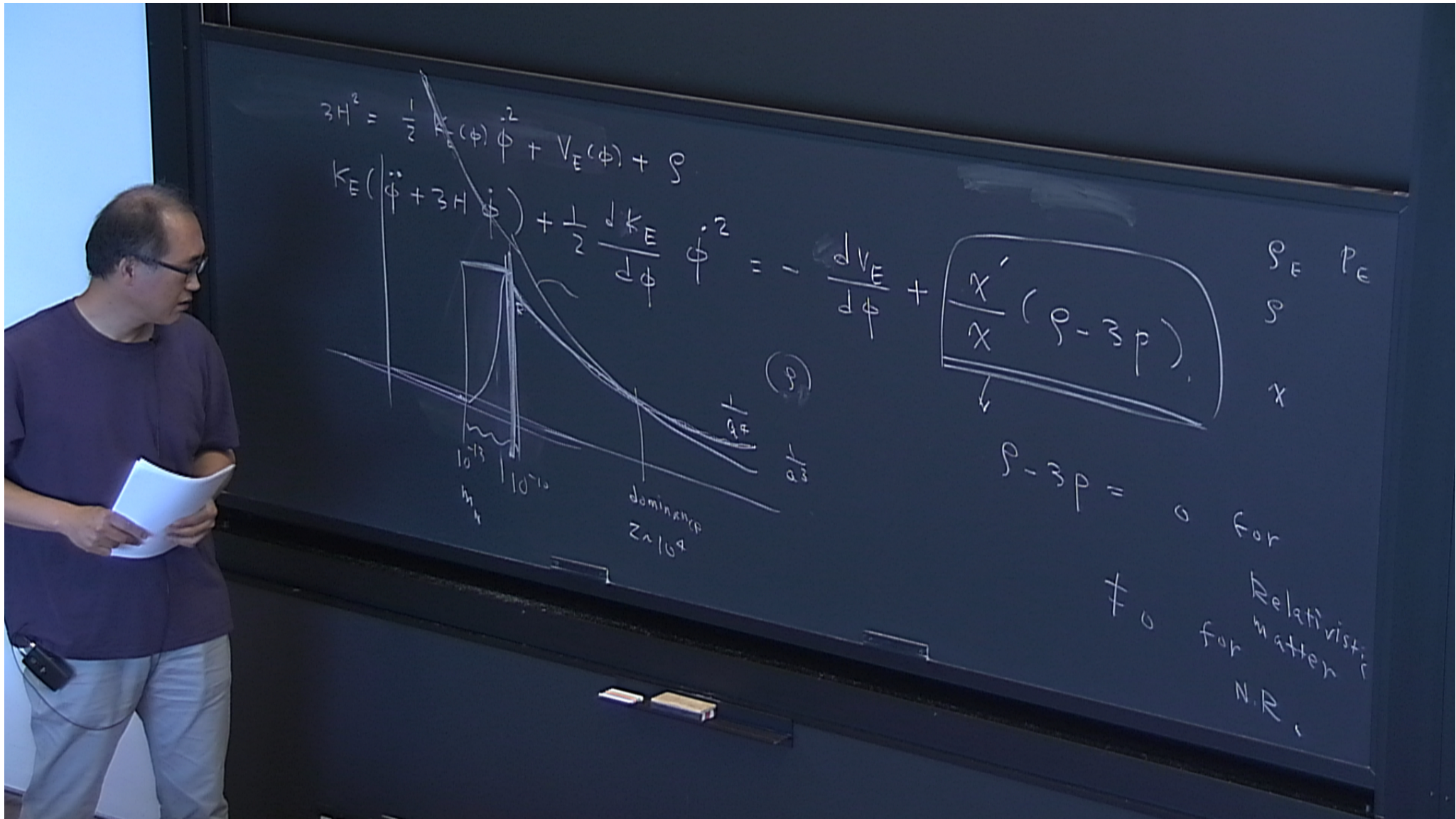


$$3H^2 = \frac{1}{2} K_E(\phi) \dot{\phi}^2 + V_E(\phi) + \rho$$

$$K_E(\ddot{\phi} + 3H\dot{\phi}) + \frac{1}{2} \frac{dK_E}{d\phi} \dot{\phi}^2 = - \frac{dV_E}{d\phi} + \frac{\rho'}{\rho} (\rho - 3p)$$

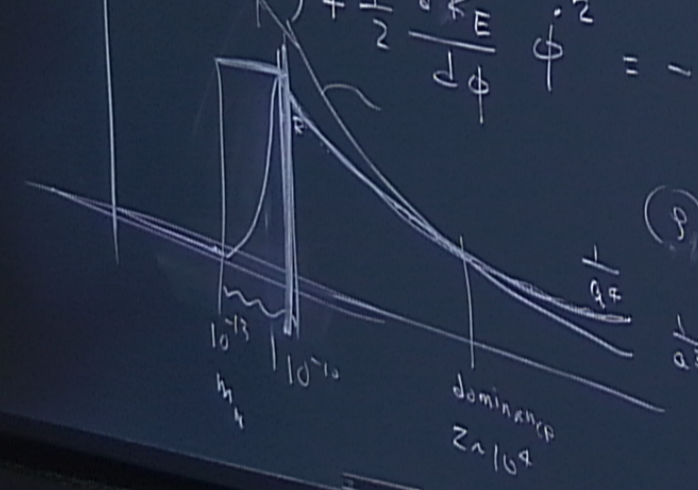


$\rho - 3p = 0$ for
 Relativistic
 $\neq 0$ for matter
 N.R.



$$3H^2 = \frac{1}{2} \dot{\phi}^2 + V_E(\phi) + \rho$$

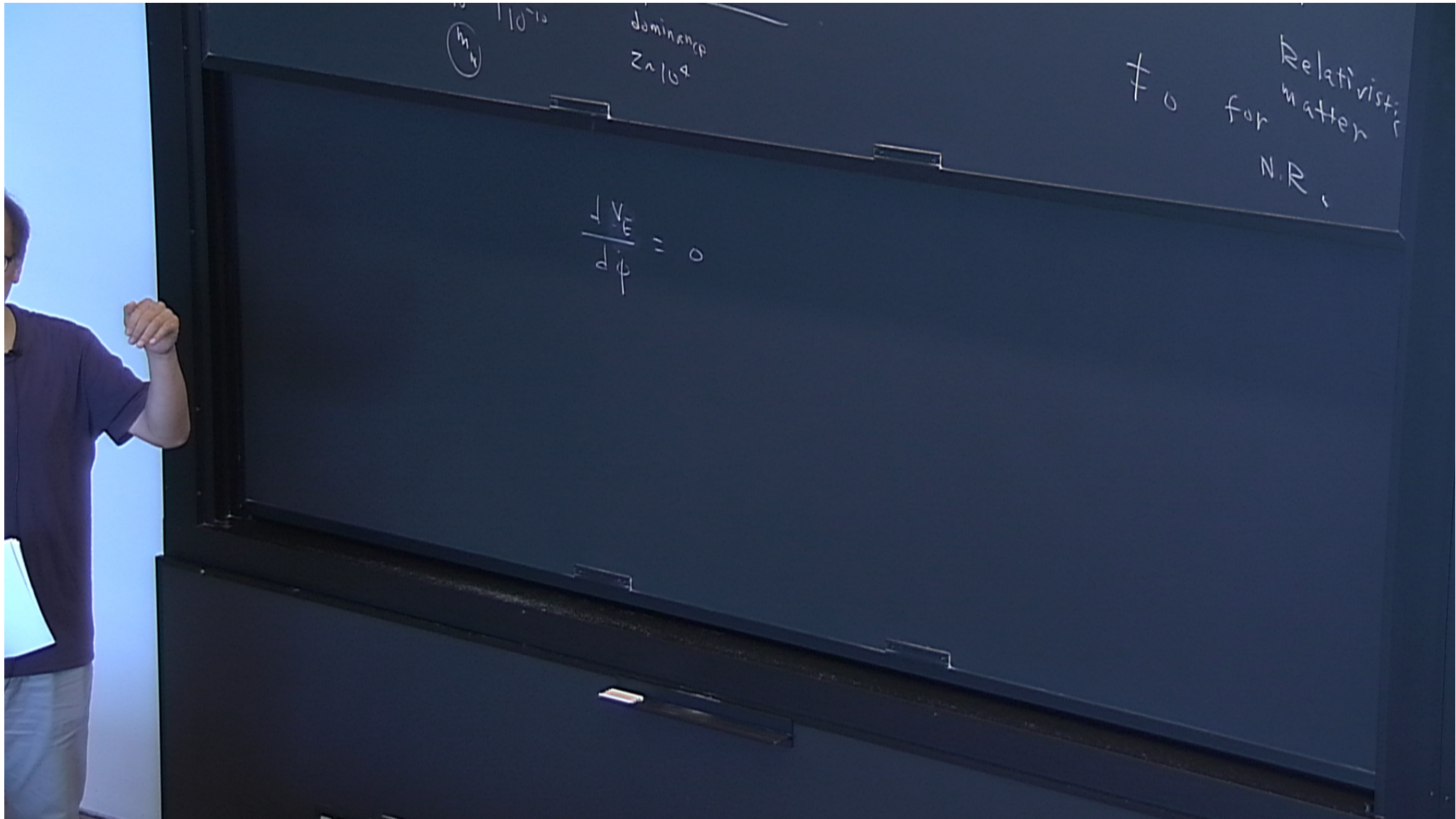
$$K_E(\ddot{\phi} + 3H\dot{\phi}) + \frac{1}{2} \frac{dK_E}{d\phi} \dot{\phi}^2 = - \frac{dV_E}{d\phi} + \frac{\rho - 3p}{\chi}$$

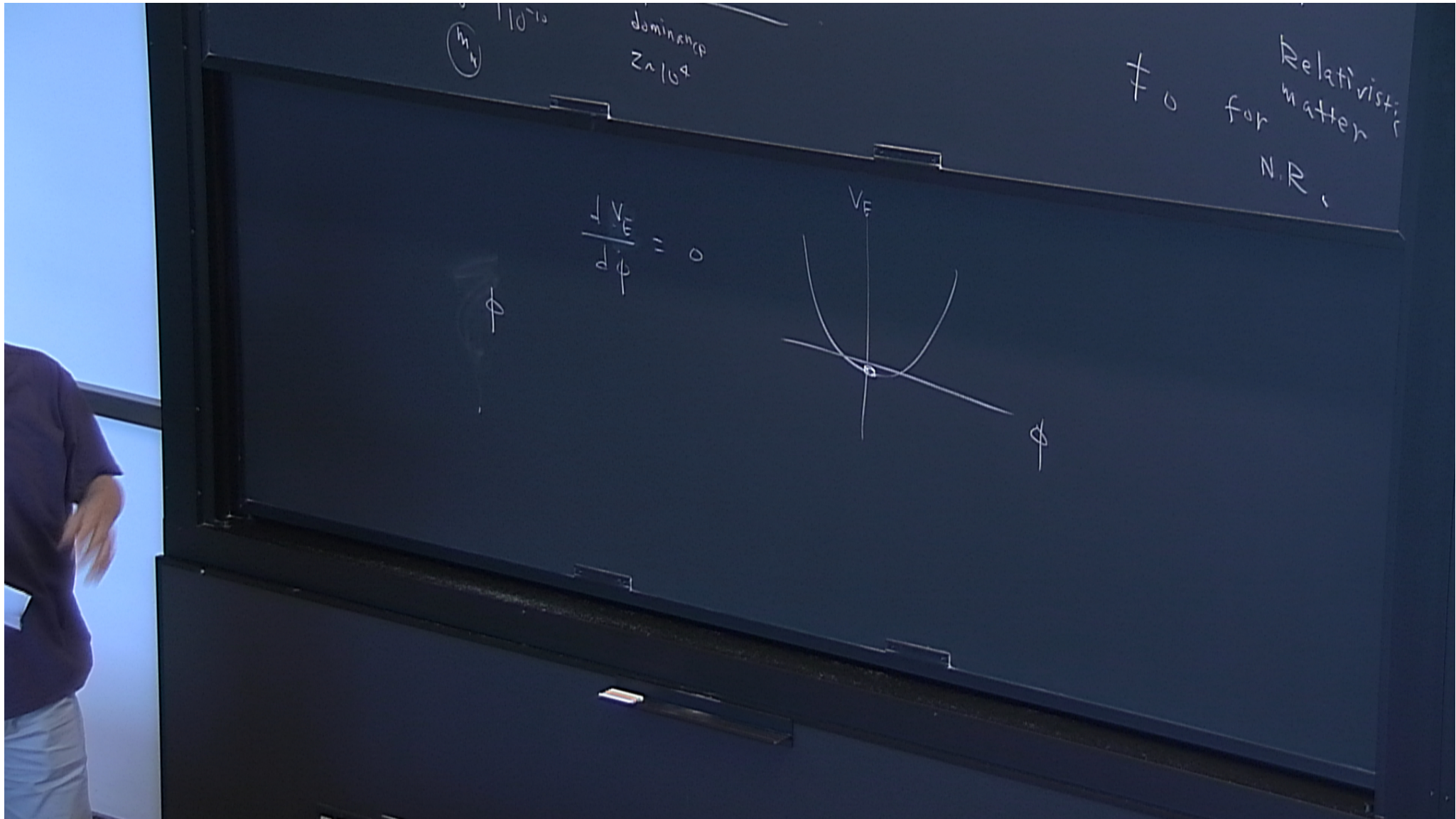


$$\frac{\rho - 3p}{\chi}$$

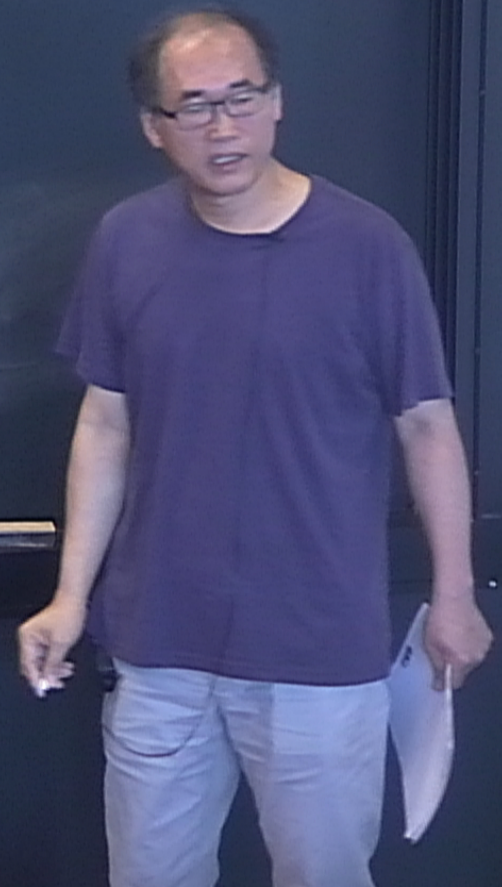
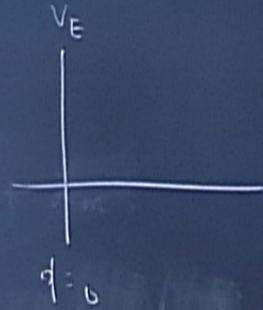
ρ_E p_E
 ρ
 χ

$\rho - 3p = 0$ for
 Relativistic
 $\neq 0$ for matter
 N.R.

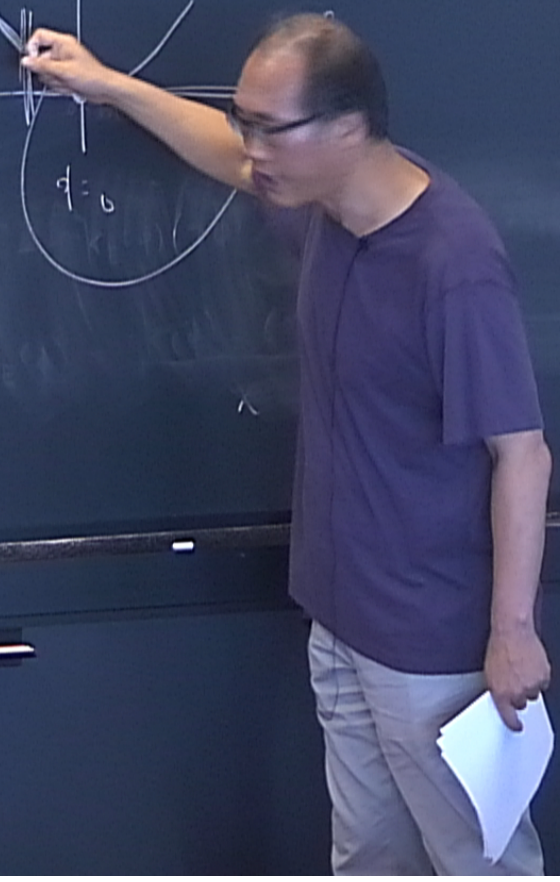
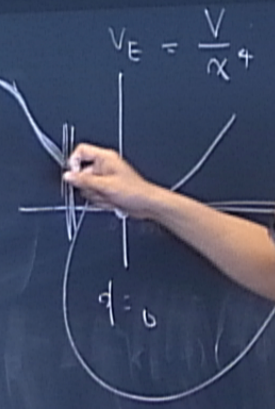




$$\chi^2(\phi) = \phi^2 - 2\alpha\phi + 1$$
$$V(\phi) = \frac{1}{4} \lambda \phi^4$$

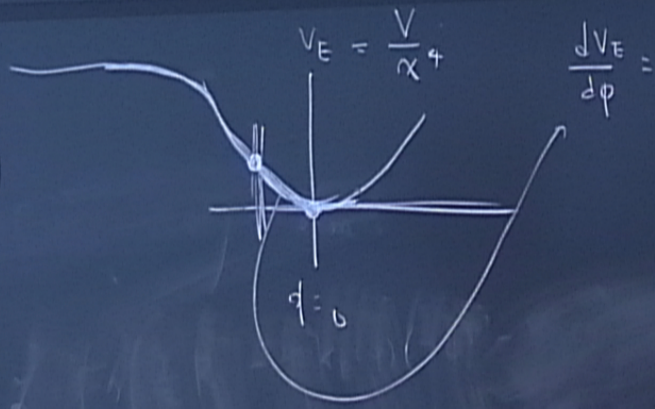


$$\chi^2(\phi) = \phi^2 - 2\alpha\phi + 1$$
$$V(\phi) = \frac{1}{4} \lambda \phi^4$$



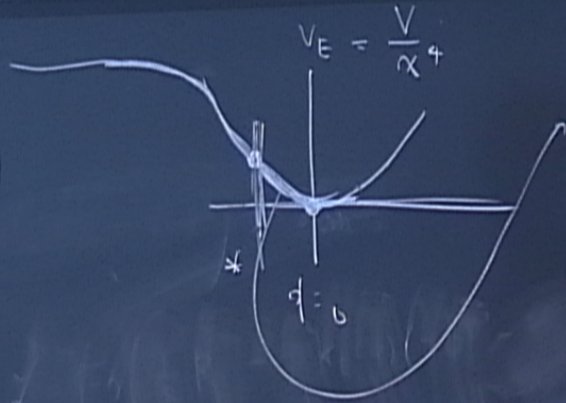
$$\chi^2(\phi) = \phi^2 - 2\alpha\phi + 1$$

$$V(\phi) = \frac{1}{4} \lambda \phi^4$$



$$\chi^2(\phi) = \phi^2 - 2\alpha\phi + 1$$

$$V(\phi) = \frac{1}{4}\lambda\phi^4$$



$$\frac{dV_E}{d\phi} = \frac{\chi'}{\chi} \rho_w$$

$$\chi \sim 1$$

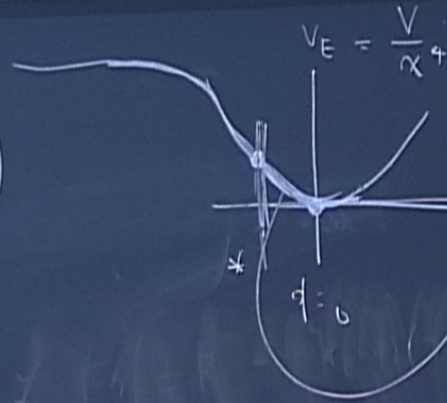
$$\chi' \sim -\alpha$$

V

$$x^2(\phi) = \phi^2 - 2\alpha\phi + 1$$

$$V(\phi) = \frac{1}{4} \lambda \phi^4$$

$$\lambda \phi^3$$



$$\frac{dV_E}{d\phi} = \frac{x'}{x} \rho_w$$

$$x \sim 1$$

$$x' \sim -\alpha$$

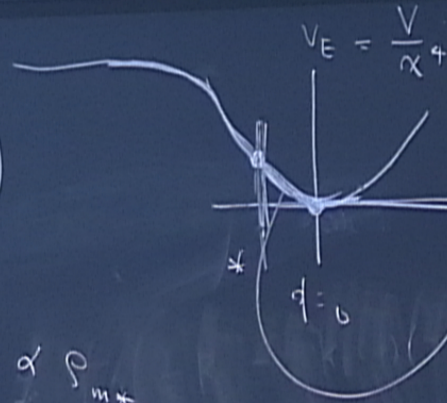
$$V_E \sim \frac{1}{4} \lambda \phi^4$$

$$x^2(\phi) = \phi^2 - 2\alpha\phi + 1$$

$$V(\phi) = \frac{\lambda}{4} \phi^4$$

$$\lambda \phi_*^3 = \alpha \rho_{m*}$$

$$= \alpha$$



$$\frac{dV_E}{d\phi} = \frac{x'}{x} \rho_m$$

$$x \sim 1$$

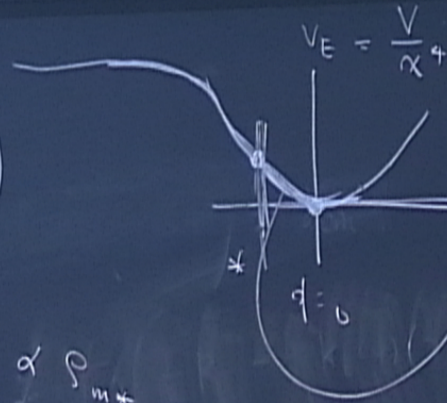
$$x' \sim -\alpha$$

$$V_E \sim \frac{\lambda}{4} \phi^4$$

$$\chi^2(\phi) = \phi^2 - 2\alpha\phi + 1$$

$$V(\phi) = \frac{1}{4}$$

$$\begin{aligned} \lambda \phi_*^3 &= \alpha \rho_{m*} \\ &= \alpha \rho_{m0} \left(\frac{a_0}{a_*} \right)^2 \end{aligned}$$

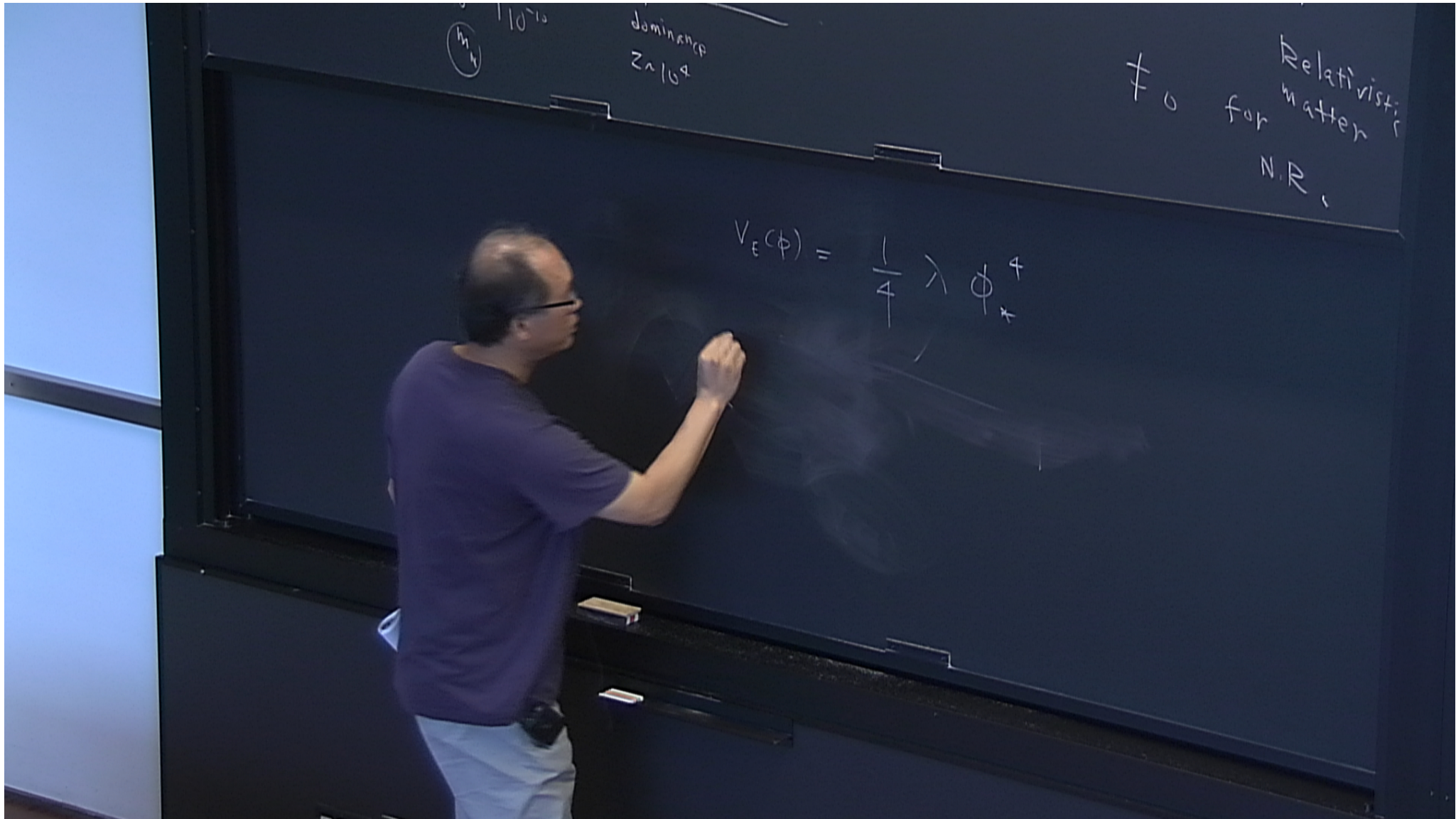


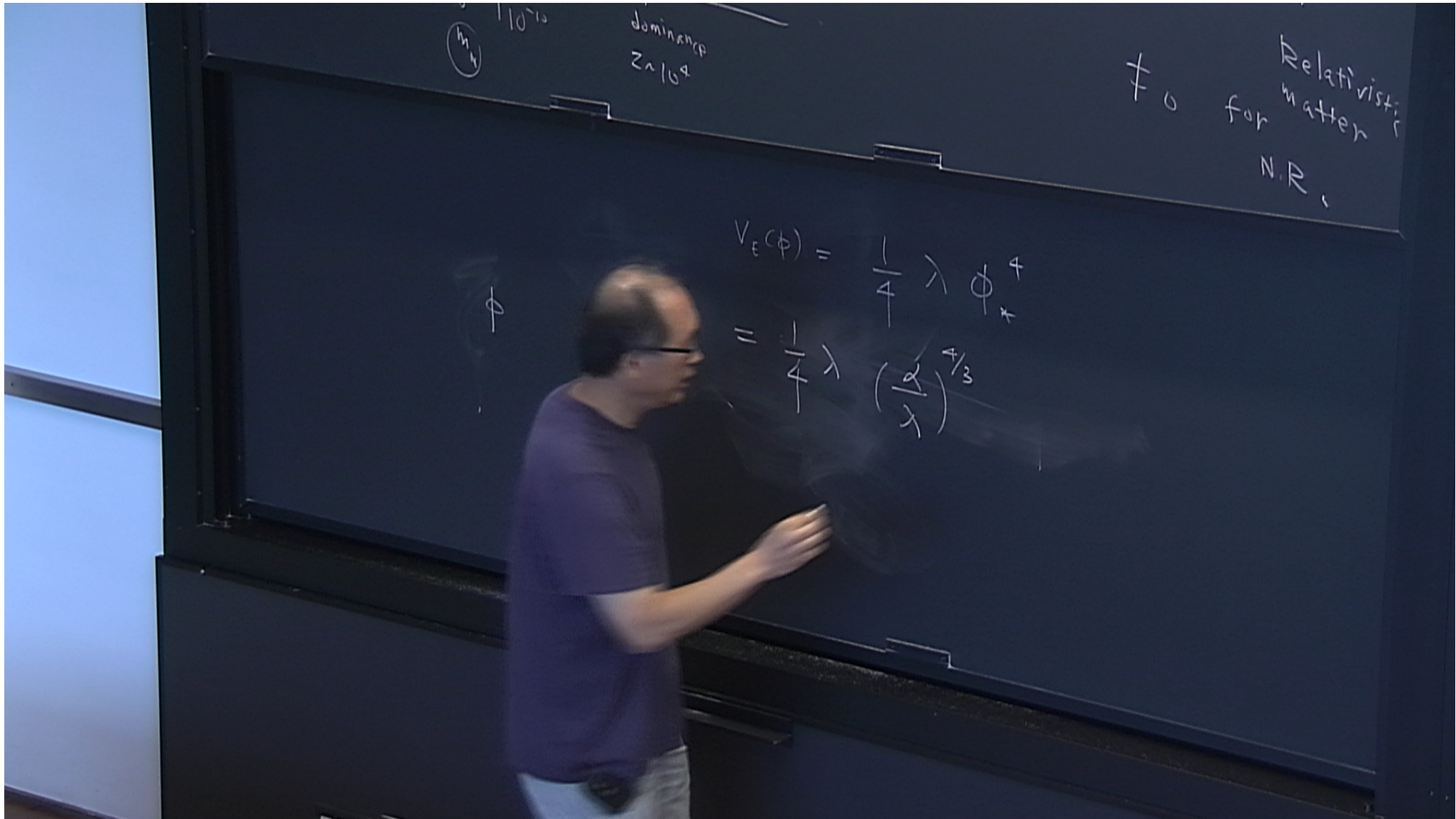
$$\frac{dV_E}{d\phi} = \frac{\chi'}{\chi} \rho_m$$

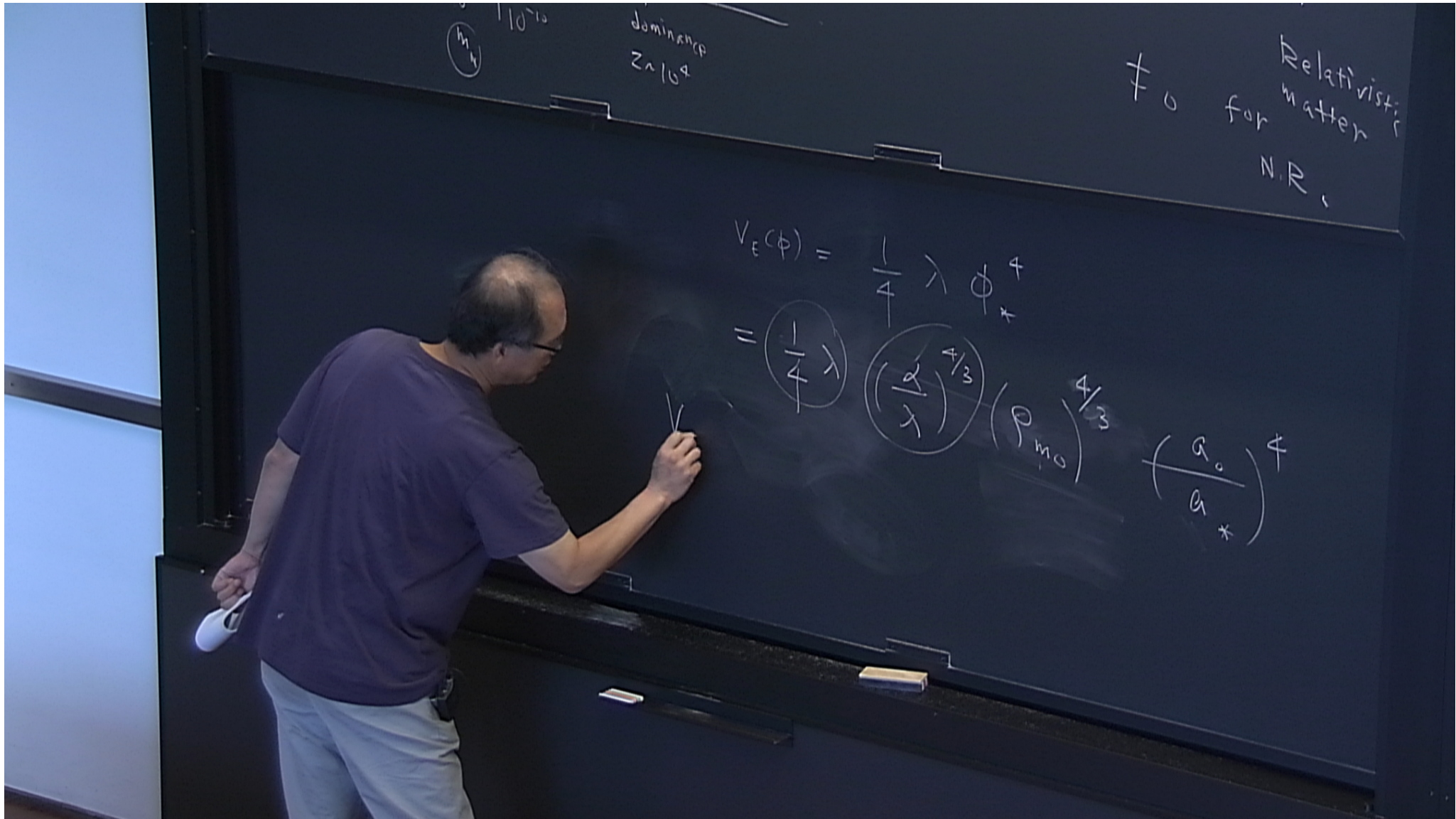
$$\chi \sim 1$$

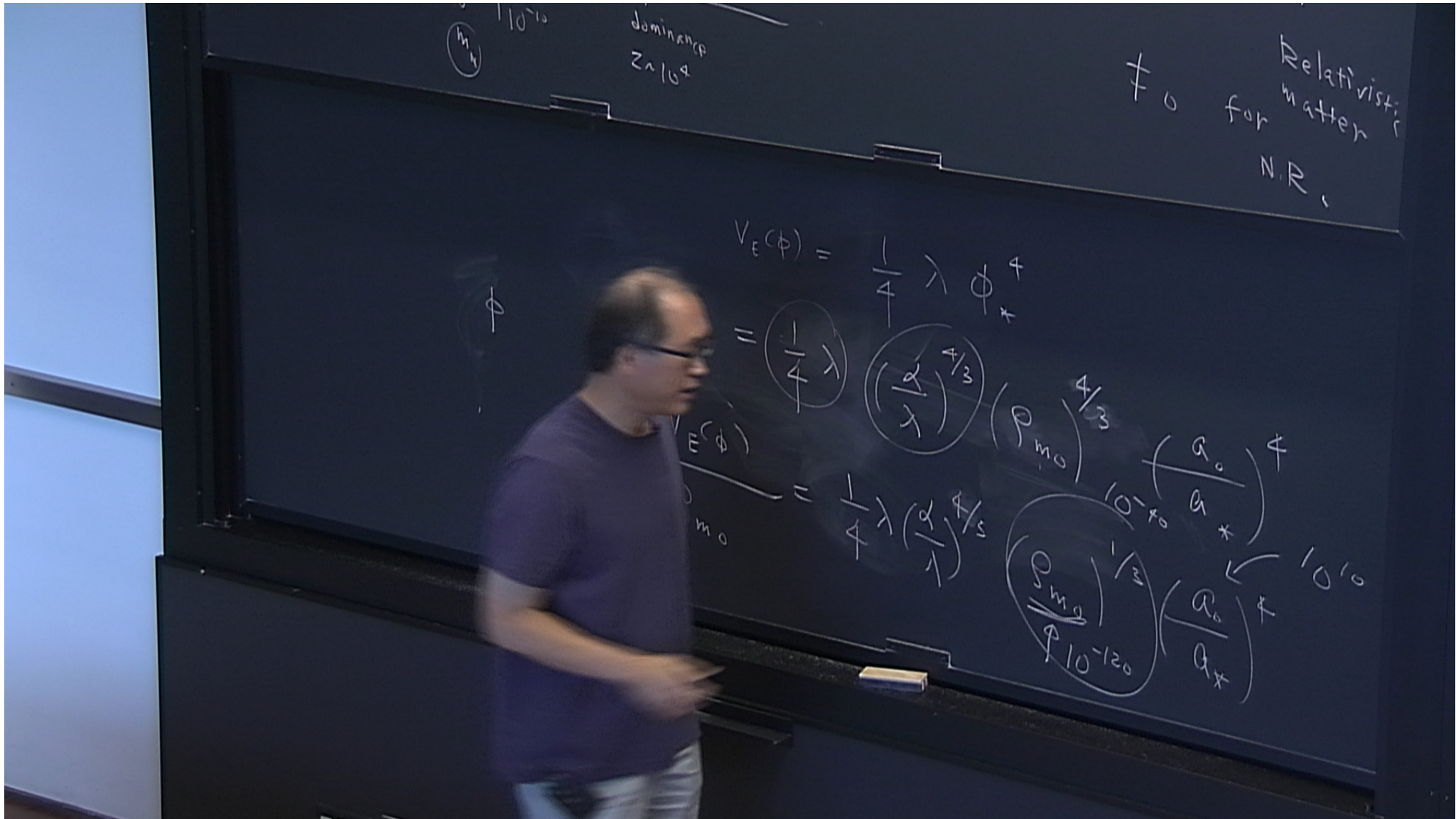
$$\chi' \sim -\alpha$$

$$V_E \sim \frac{1}{4} \lambda \phi^4$$









EXIT

$$\ddot{\phi} = -\frac{1}{2} K(\phi) \dot{\phi}^2 + V_E(\phi) + S$$

$$K_E(\dot{\phi}^2 + 3H\dot{\phi}) + \frac{1}{2} \frac{dK_E}{d\phi} \dot{\phi}^2 = -\frac{dV_E}{d\phi} + \frac{\alpha'}{\alpha} (\rho - 3p)$$

$\rho - 3p = 0$ for
radiation matter
NR

Cosmological Constant Problem (J Overduin, 2011, Lene P. DeWitt)

mechanism: present value of dark energy

$$\chi = \Gamma \left(\frac{1}{2} \frac{\alpha'}{\alpha} \rho - \frac{1}{2} k(\phi) (\dot{\phi}^2) - V(\phi) \right)$$

$\ln R = \dots$
 $\frac{d \ln R}{dt} = \dots$
 $\rho > 0$
 $\rho < -\frac{1}{3} \rho < 0$
 $\rho > 0$ for normal matter
 $\rho < 0$
 $\rho > 0$ for dark energy



$$V_E(\phi) = \frac{1}{4} \lambda \phi^4$$

$$= \left(\frac{1}{4} \lambda \right) \left(\frac{\rho_{min}}{\lambda} \right)^{4/3} \left(\frac{\rho_{min}}{\lambda} \right)^{4/3}$$

$$\frac{V_E(\phi)}{\rho_{min}} = \frac{1}{4} \lambda \left(\frac{\rho_{min}}{\lambda} \right)^{4/3}$$

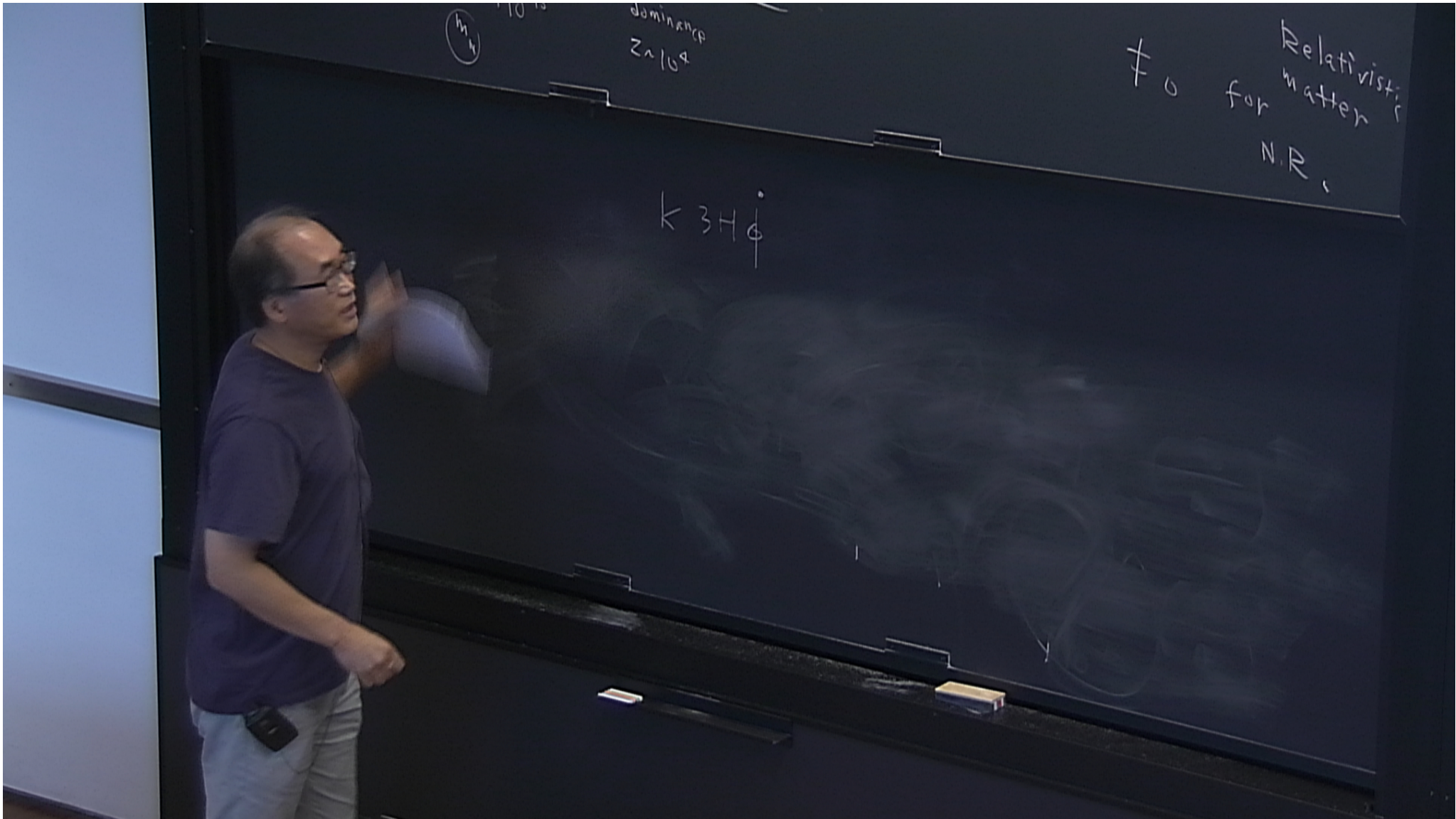
$\rho_{min} \sim 10^{-120}$
 $\frac{\rho_{min}}{\lambda} \sim 10^{120}$

$$\chi^2(\phi) = \dot{\phi}^2 - 2\lambda\phi + 1$$

$$V(\phi) = \frac{1}{4} \lambda \phi^4$$

$\lambda \phi_{min}^3 = \alpha \rho_{min}$
 $= \alpha \rho_{min} \left(\frac{\rho_{min}}{\lambda} \right)^{1/3}$





$$3H^2 = \frac{1}{2} K_E(\phi) \dot{\phi}^2 + V_E(\phi) + \rho$$

$$K_E(\ddot{\phi} + 3H\dot{\phi}) + \frac{1}{2} \frac{dK_E}{d\phi} \dot{\phi}^2 = - \frac{dV_E}{d\phi} + \frac{\rho'}{\rho} (\rho - 3p)$$

$$3H\dot{\phi}$$

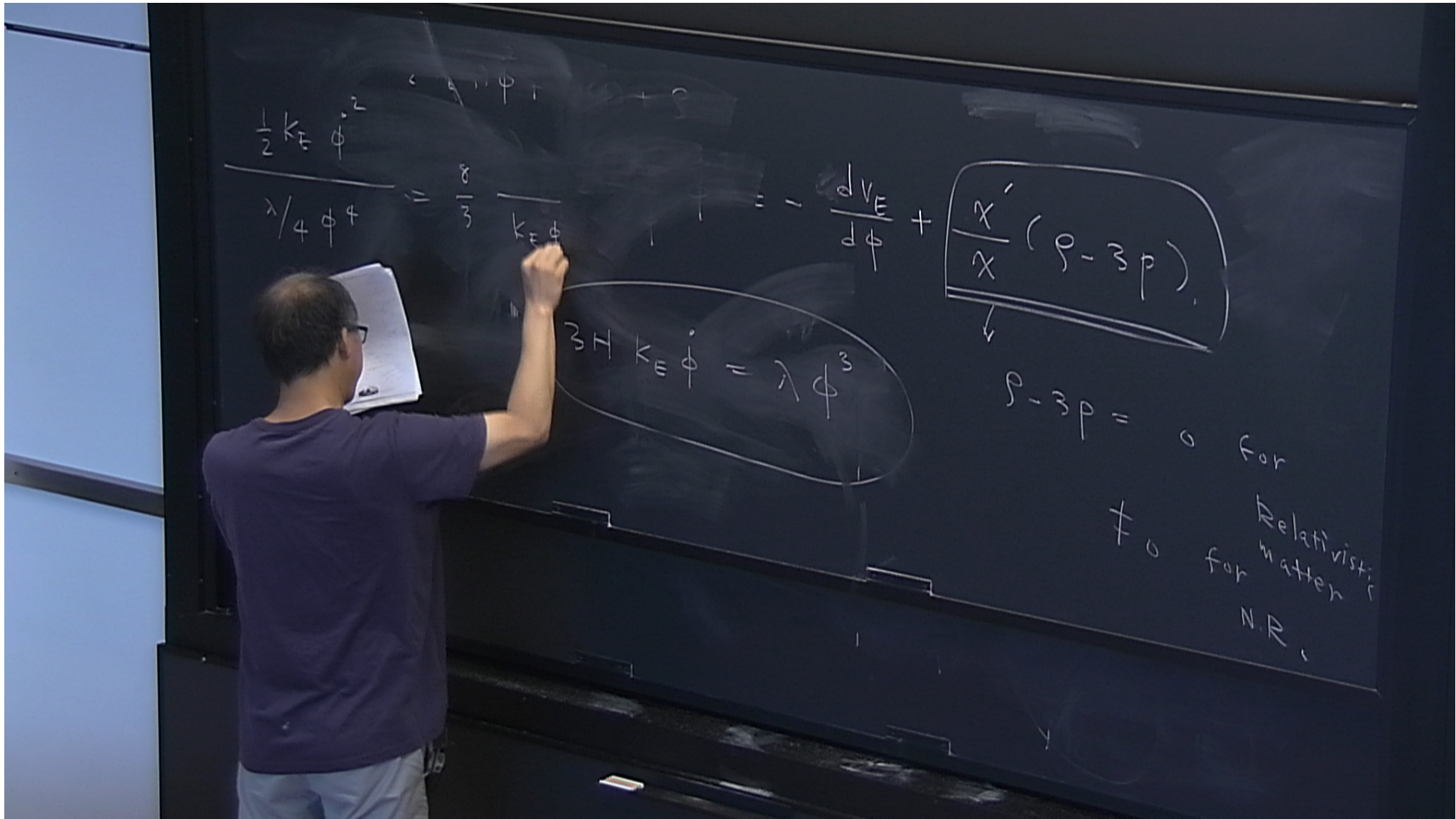
$\rho - 3p = 0$ for
 Relativistic
 $\neq 0$ for matter
 N.R.

$$3H^2 = \frac{1}{2} K_E(\phi) \dot{\phi}^2 + V_E(\phi) + \rho$$

$$K_E(\ddot{\phi} + 3H\dot{\phi}) + \frac{1}{2} \frac{dK_E}{d\phi} \dot{\phi}^2 = - \frac{dV_E}{d\phi} + \frac{\dot{\chi}}{\chi} (\rho - 3p)$$

$$3H K_E \dot{\phi} = - \frac{dV_E}{d\phi}$$

$\rho - 3p = 0$ for
 Relativistic
 $\neq 0$ for matter
 N.R.



$$\frac{\frac{1}{2} k_E \phi^2}{\lambda/4 \phi^4} = \frac{8}{3} \frac{k_E \phi}{\lambda \phi^3} = - \frac{dV_E}{d\phi} + \frac{\rho'}{\rho} (\rho - 3p)$$

$$3H^2 k_E \dot{\phi}^2 = \lambda \phi^3$$

$$\rho - 3p = 0 \text{ for Relativistic matter}$$

$$\neq 0 \text{ for N.R.}$$

