

Title: What Can We Learn from Precision Higgs

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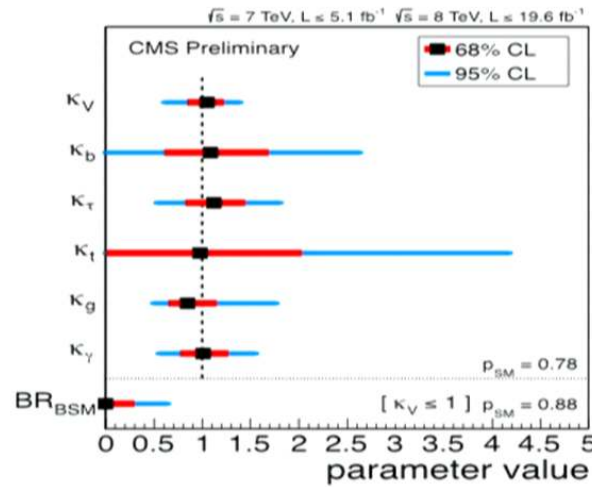
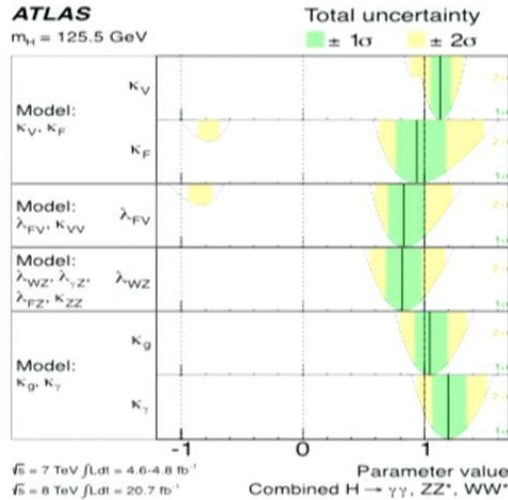
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Abstract: <span>In the coming years, LHC experiments will measure Higgs properties, such as its couplings, with increasing precision. Electron-positron Higgs factories, such as the ILC or TLEP, would be able to achieve even better precision. In this talk, I will discuss some of the physics questions that can be addressed by a precision Higgs coupling measurement program. First, the issue of naturalness of the electroweak scale can be addressed in a robust, model-independent manner. Second, the possibility of a first-order electroweak phase transition can be definitively probed, testing one of the necessary conditions of electroweak baryogenesis scenario.</span>

# What Can We Learn from Precision Higgs

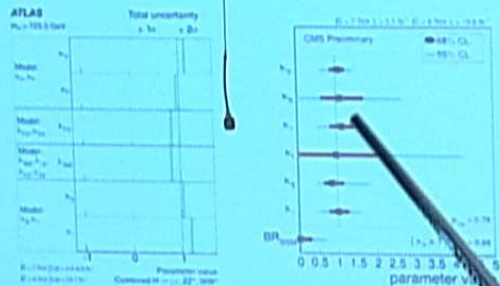
Maxim Perelstein, Cornell  
Perimeter Institute Seminar, June 13, 2014

# Higgs: Discovery to Precision



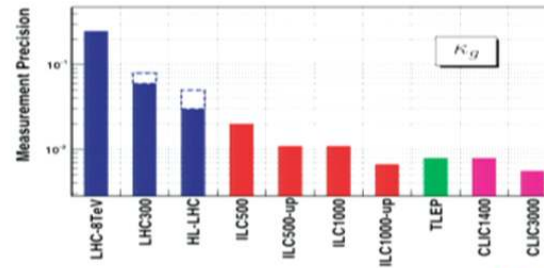
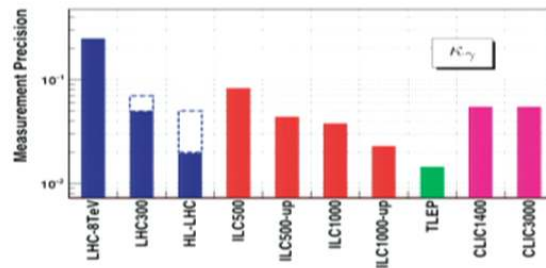
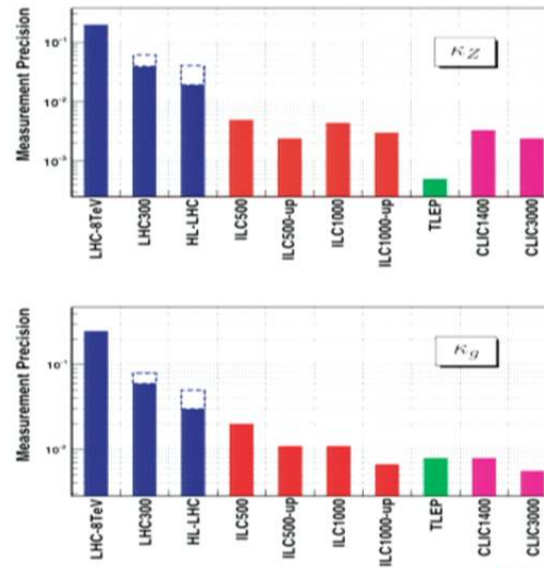
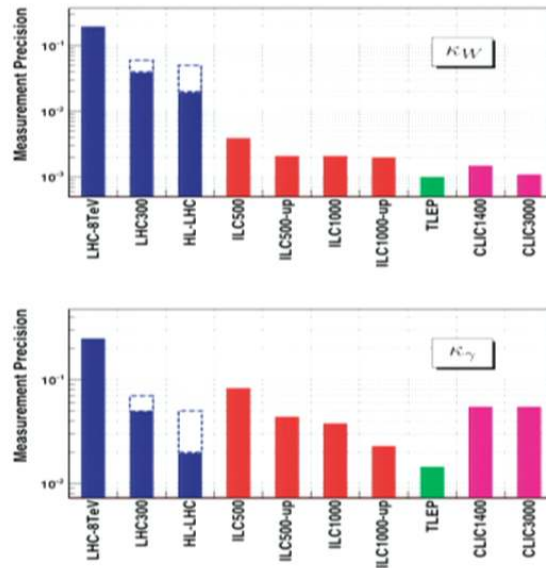
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# Higgs: Discovery to Precision



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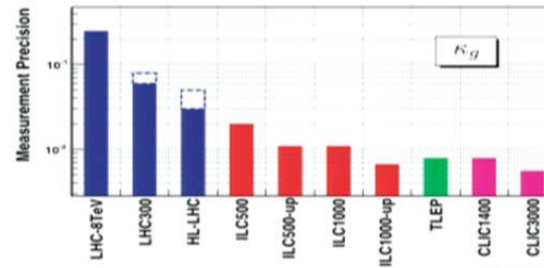
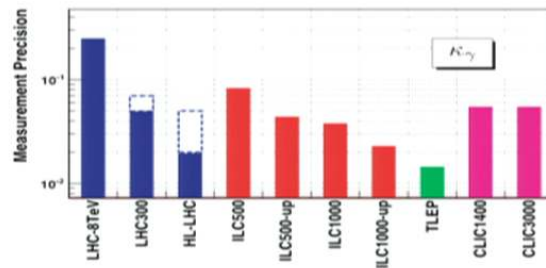
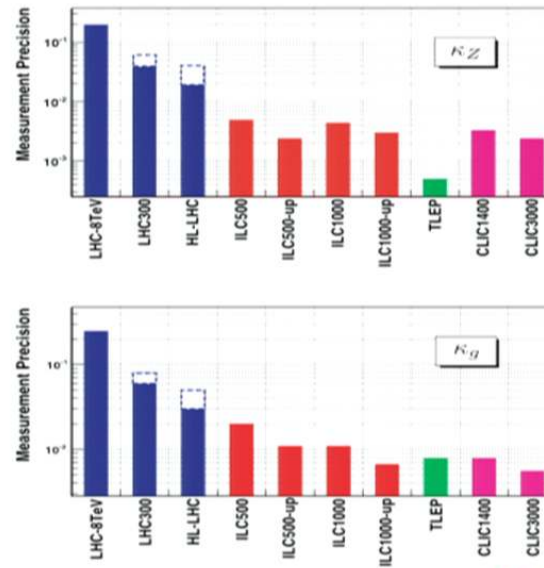
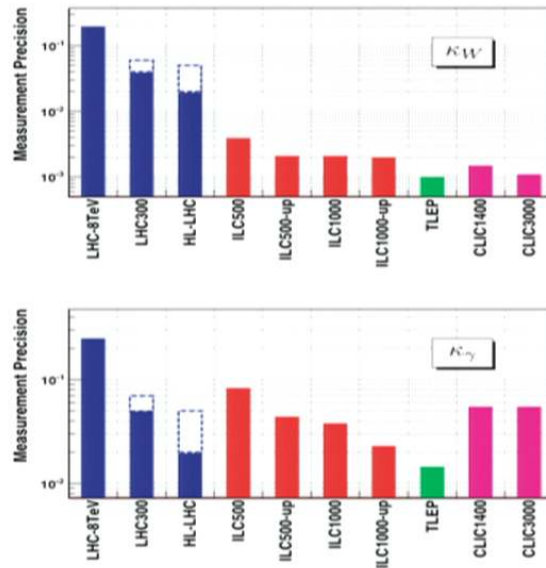
# Future: Higgs Precision Program



Snowmass Higgs Report

- 2-5% precision achievable at the **HL-LHC**
- 0.1% precision on  $V$ , 1% on  $g$  and  $\gamma$  at  **$e^+e^-$  Higgs factories**
- At or almost at precision electroweak levels!

# Future: Higgs Precision Program



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# Outline

- This talk is about potential **physics implications** of Higgs Coupling (HC) measurements at this level of precision
- Two parts:
  - HC and Naturalness: a model-independent connection [Farina, MP, Rey-Le Lorier, I 305.6068]
  - HC and Electroweak Phase Transition dynamics [A. Katz, MP, I 401.1827]

# Intro: Minimalist BSM

- Precision electroweak tests strongly suggest that physics remains weakly coupled until (at least)  $\sim 10$  TeV scale
- In this talk, I will take a modest attitude and only think about physics below 10 TeV (do not insist on perturbative gauge coupling unification etc.)
- If only SM until 10 TeV, the Higgs mass parameter needs to be fine tuned:

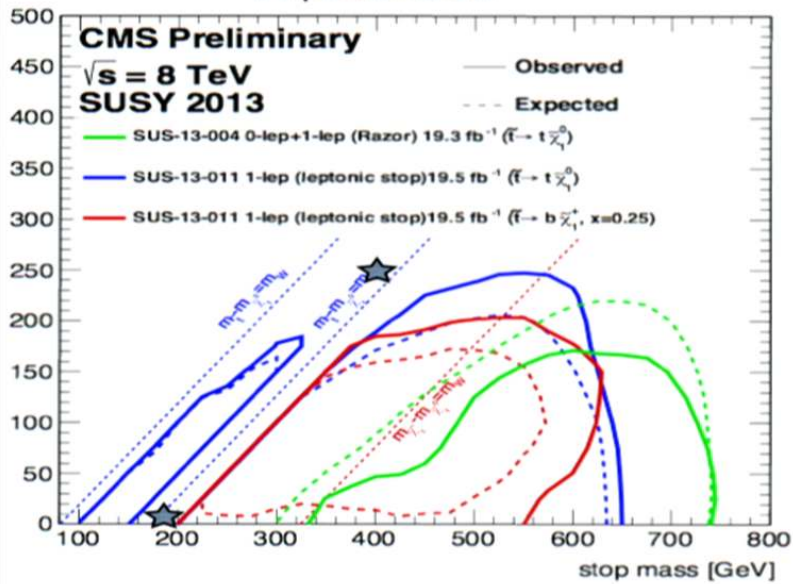
$$-m^2 = -m_{\text{tree}}^2 + \frac{c}{16\pi^2}\Lambda^2 \quad \Delta = \frac{\delta m^2}{m^2}$$

$$(v, m_h) \Rightarrow m \approx 90 \text{ GeV} \quad \delta m^2 \sim \frac{3y_t^2\Lambda^2}{8\pi^2} \Rightarrow \Delta_{\text{SM}} \gtrsim 500$$

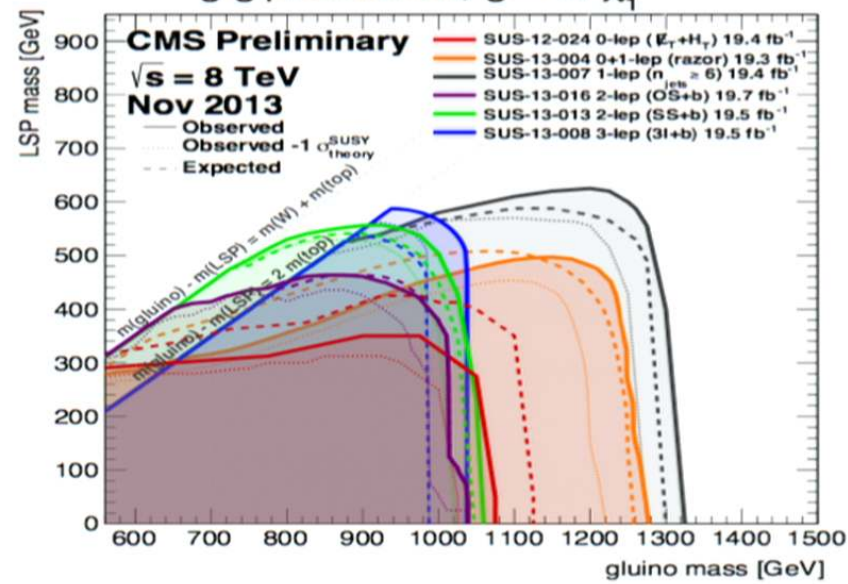
- Note: this assumes that the SM is an effective theory and new propagating d.o.f.'s coupled to the Higgs appear at some scale, possibly  $\gg 10$  TeV
- Avoiding this fine-tuning is the (only) motivation for new physics at the energy scale accessible to the LHC. Only a few mechanisms for doing so in a weakly-coupled theory are known (SUSY, Little Higgs, Gauge-Higgs Unification).

# Naturalness: Not Dead Yet

$\tilde{t}\text{-}\tilde{t}$  production



$\tilde{g}\text{-}\tilde{g}$  production,  $\tilde{g} \rightarrow t \bar{t} \tilde{\chi}_1^0$



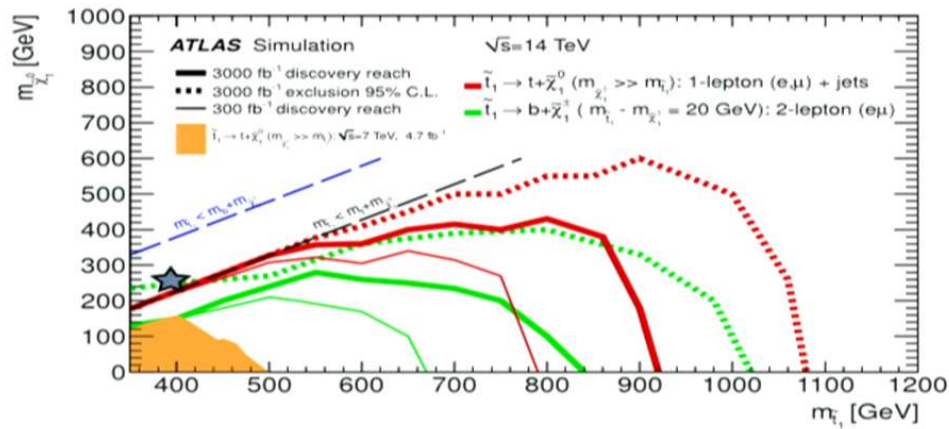
- Direct stop searches currently do not exclude big regions of parameter space with  $\Delta_{\text{EFT}} \sim 1/4$  or even  $\sim 1$  in the “stealthy” region  $m_{\tilde{t}} \approx m_t, m_{\tilde{\chi}} \approx 0$
- Gluino bounds OK too for now:  $m_{\tilde{g}} < 4m_{\tilde{t}}$  is 100% natural if gluino is Dirac

# Minimalist SUSY

- Consider an “effective” SUSY theory with a 10 TeV cutoff [e.g. Brust, Katz, Lawrence, Sundrum, I | 10.6670]
- Only superpartners canceling the largest contributions to  $m^2$  must appear. Stops and gluinos are especially important at the LHC.
- One-loop fine-tuning estimate in the effective theory is simply

$$\Delta \approx \frac{3y_t^2 m_{\tilde{t}}^2}{8\pi^2} \log \frac{\Lambda^2}{m_{\tilde{t}}^2} \approx \left( \frac{m_{\tilde{t}}}{200 \text{ GeV}} \right)^2$$

- In SUSY literature, fine-tuning is typically quantified by measuring the dependence of the Higgs mass on input parameters, usually at a high (GUT) scale
- The above estimate, “EFT FT”, should be thought of as a rough model-independent lower bound on FT
- Can physics at >10 TeV reduce tuning? Logically possible, but no concrete convincing example so far.



- Even at 14 TeV, probing compressed spectra, as well as stealthy and RPV scenarios, will remain non-trivial in direct searches based on current strategies
- Taylor-made searches for these regions (e.g. ISR-tags to search for compressed spectra) may be developed
- An alternative approach: indirect search by measuring **Higgs couplings**

# I. Higgs and Naturalness: General Argument

[Farina, MP, Rey Le-  
Lorier, I 305.6068]

- One-loop quantum corrections to Higgs potential are given by the **Coleman-Weinberg** formula:

$$V_{\text{CW}}(h) = \frac{1}{2} \sum_k g_k (-1)^{F_k} \int \frac{d^4 \ell}{(2\pi)^4} \log(\ell^2 + m_k^2(h))$$

- The only input is Higgs-dependent masses of all particles; focus on tops

- The famous mass renormalization is just  $\delta\mu^2 \equiv \frac{\delta^2 V_{\text{CW}}}{\delta h^2} \Big|_{h=0}$ .

- Top partner mass is  $m^2(T_i) = m_{0,i}^2 + c_i h^2 + \dots$

- Cancellation of quadratic divergence gives a **sum rule**:  $6y_t^2 = \sum_i g_i (-1)^{F_i} c_i$

- Potential **fine-tuning** comes from the next (log-divergent) term:

$$\Delta = \frac{\delta\mu^2}{\mu^2} \approx 0.78 \left( \sum_i g_i (-1)^{F_i} c_i \left( \frac{m_{0,i}}{1 \text{ TeV}} \right)^2 \log \frac{\Lambda^2}{m_{0,i}^2} - 6y_t^2 \left( \frac{m_t}{1 \text{ TeV}} \right)^2 \log \frac{\Lambda^2}{m_t^2} \right)$$

- Low-Energy Theorems give the top partner contributions to  $hgg$  and  $h\gamma\gamma$  in terms of the same object: Higgs-dependent top-partner mass

$$\mathcal{L}_{top} = \frac{m_t}{2} C_t H_{up} F^{top} \quad \mathcal{L}_{top} = \frac{m_t}{12\pi^2} C_t b G_{\mu\nu} G^{\mu\nu}$$

$$C_t = 1 + \frac{1}{16} \sum_{\tilde{t}_1, \tilde{t}_2} N_{\tilde{t}_i} g_{\tilde{t}_i}^2 \frac{d(\ln m_{\tilde{t}_i})}{d(\ln m_t)} + \frac{1}{32} \sum_{\tilde{t}_1, \tilde{t}_2} N_{\tilde{t}_i} g_{\tilde{t}_i}^2 \frac{d(\ln m_{\tilde{t}_i})}{d(\ln m_t)}$$

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- Plug in top partner masses:

$$C_t = 1 + \frac{1}{16} \sum_{\tilde{t}_1, \tilde{t}_2} \frac{N_{\tilde{t}_i} g_{\tilde{t}_i}^2 m_{\tilde{t}_i}^2}{m_{\tilde{t}_i}^2 - m_t^2} + \frac{1}{32} \sum_{\tilde{t}_1, \tilde{t}_2} \frac{N_{\tilde{t}_i} g_{\tilde{t}_i}^2}{m_{\tilde{t}_i}^2 - m_t^2}$$

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- Very general, robust result: inverse correlation between fine-tuning and top SM contributions to  $hgg$  and  $h\gamma\gamma$
- Exception: non-colored, non-charged partners. Come back to these later in the talk.
- Benchmark example: a single top partner, spin 0, with quantum numbers of the SM top (e.g.: MSSM with degenerate stops)

- Low-Energy Theorems give the top partner contributions to  $h\eta\eta$  and  $h\gamma\gamma$  in terms of the same object: Higgs-dependent top-partner mass

$$\mathcal{L}_{\text{top}} = \frac{m_t}{2t} C_t h F^{\mu\nu} F^{\mu\nu}, \quad \mathcal{L}_{\text{top}} = \frac{m_t}{12t^2} C_t h G_{\mu\nu} G^{\mu\nu}$$

$$C_t = 1 + \frac{1}{2} \sum_f \frac{N_f Q_f^2}{m_{T_f}^2} = \frac{3}{16} \sum_f \frac{N_f Q_f^2}{m_{T_f}^2}$$

$$C_t = 1 + \sum_f \frac{C_f y_f^2}{m_{T_f}^2} = \frac{1}{2} \sum_f \frac{C_f y_f^2}{m_{T_f}^2}$$

- Plug in top partner masses:

$$C_t \approx 1 + \frac{3}{4} \sum_f \frac{N_f Q_f^2 y_f^2}{m_{T_f}^2} = \frac{3}{16} \sum_f \frac{N_f Q_f^2 y_f^2}{m_{T_f}^2}$$

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$$\mathcal{L}_{top} = \frac{1}{2} C_t h F_{\mu\nu} F^{\mu\nu} \quad \mathcal{L}_{top} = \frac{1}{128\pi^2} C_t h G_{\mu\nu} G^{\mu\nu}$$

$$C_t = 1 + \frac{1}{4} \sum_{\text{top partners}} N_c Q_t^2 \frac{\partial \ln m_t^2}{\partial \ln m_{\text{top}}^2} = \frac{3}{4} \sum_{\text{top partners}} N_c Q_t^2 \frac{\partial \ln m_t^2}{\partial \ln m_{\text{top}}^2}$$

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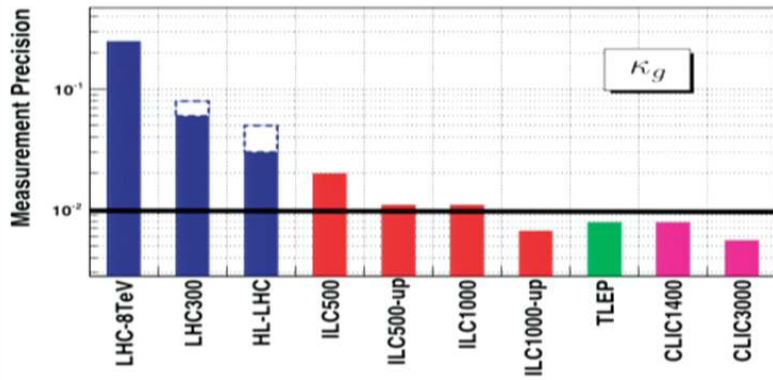
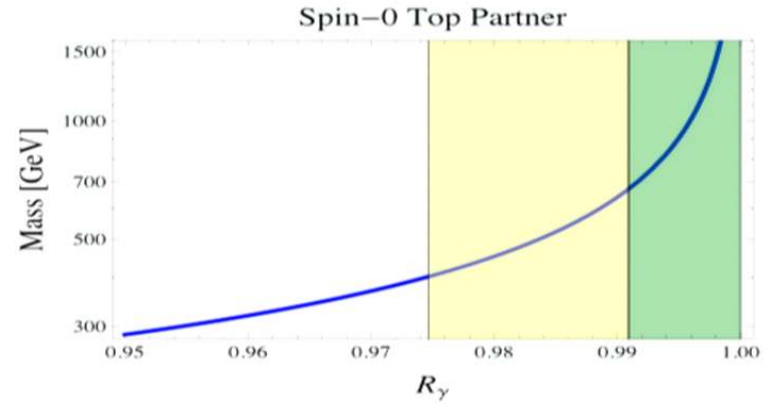
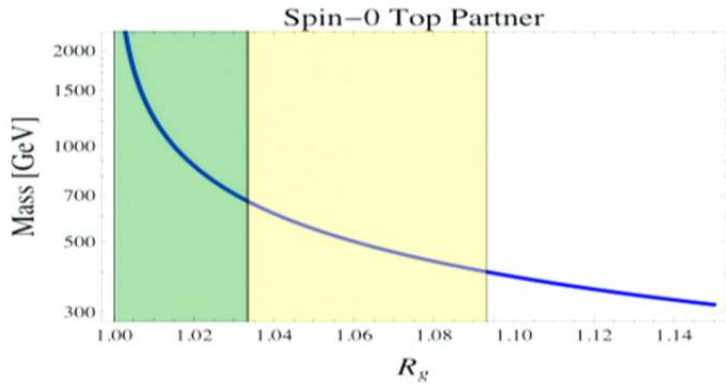
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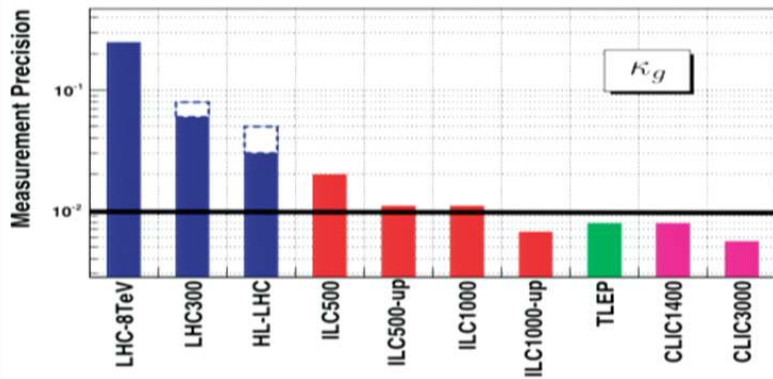
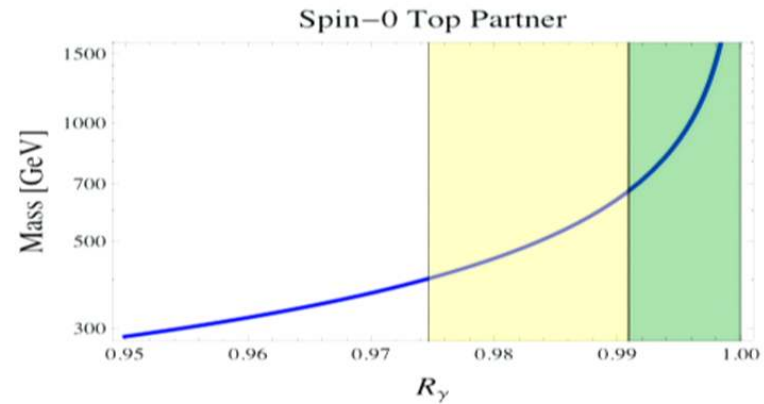
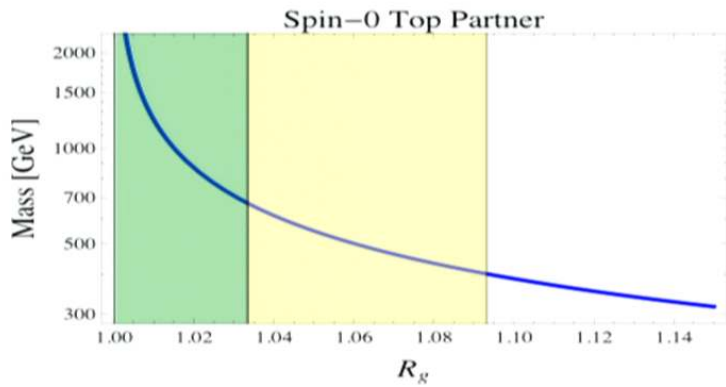
$$C_\gamma = C_g = 1 + \frac{1}{4} \frac{y_t^2 v^2}{m_{0,1}^2 + y_t^2 v^2}$$



A 1% measurement of  $R_g$  would probe the top partner mass of  $\sim 1.2$  TeV...

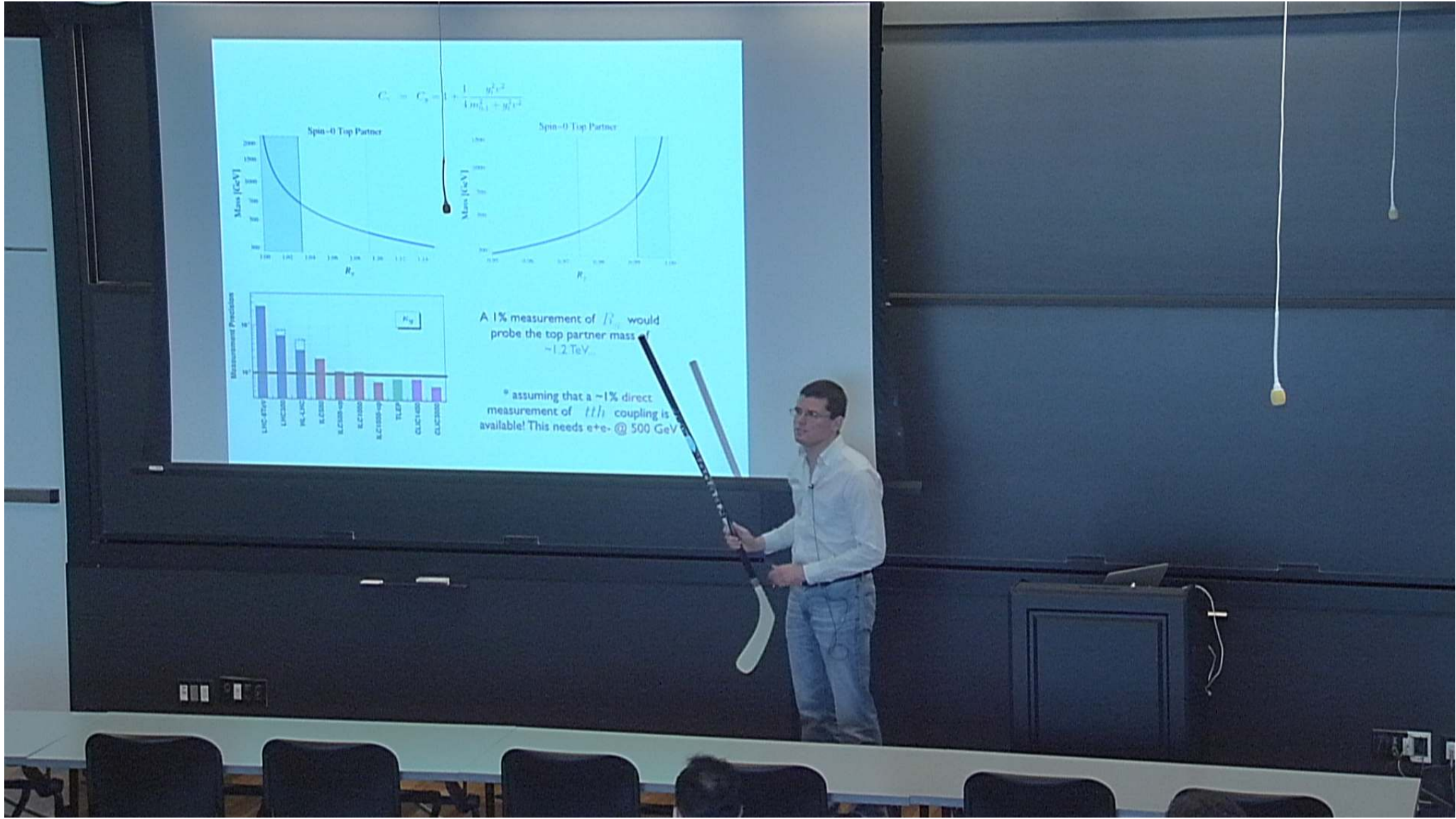
\* assuming that a  $\sim 1\%$  direct measurement of  $t\bar{t}h$  coupling is available! This needs  $e^+e^- @ 500$  GeV

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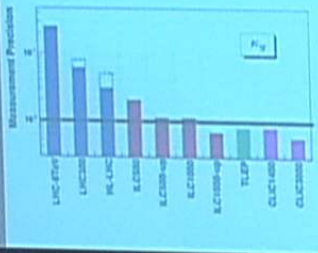
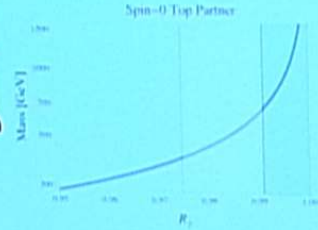
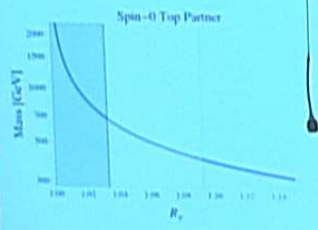


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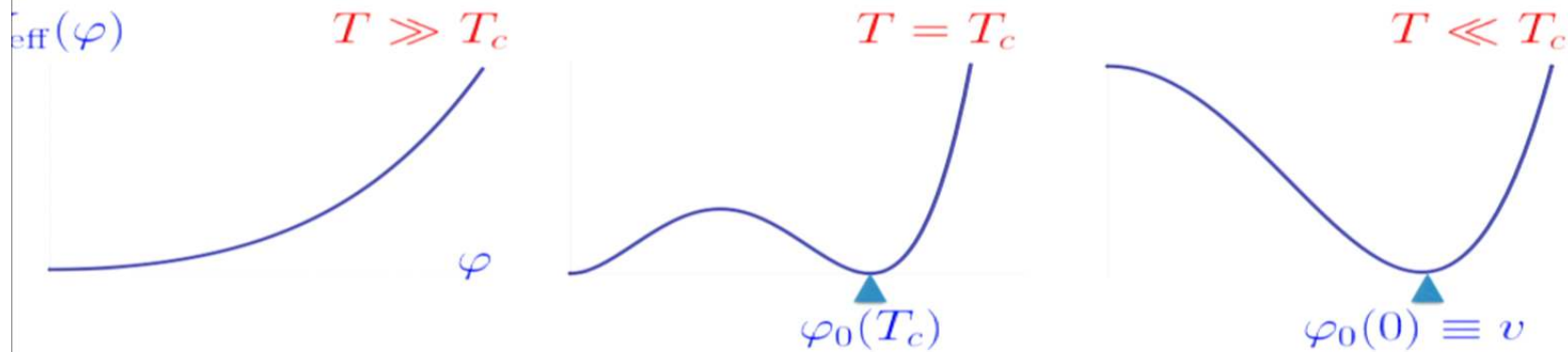
$$C_{\tau} = C_{\sigma} = 1 + \frac{1}{4} \frac{y_t^2 v^2}{4m_{\tilde{t}_1}^2 + y_t^2 v^2}$$



A 1% measurement of  $R_{\tau}$  would probe the top partner mass of  $\sim 1.2$  TeV...

\* assuming that a  $\sim 1\%$  direct measurement of  $t\bar{t}$  coupling is available! This needs  $e^+e^- @ 500$  GeV

# First-Order EWPT in Cartoons



- “Transition strength”  $\sim$  entropy release  $\xi = \varphi_0(T_c)/T_c$
- Numerical studies: EW Baryogenesis possible if  $\xi \geq 0.9$

# HC and EWPT

- No possibility of producing “plasma” with restored EW symmetry (T-RHIC?) so no direct experimental probe
- However, hard to induce large modifications of the finite-T potential without also modifying T=0 Higgs potential and couplings
- Can precise measurements of Higgs couplings conclusively probe the nature of EWPT?
- Two basic mechanisms for first-order EWPT: **tree-level mixing** with other scalars; and **loop-induced** corrections (the famous  $T^3$  term)
- We will focus on **loop-y models** since they seem harder to probe

# HC and EWPT: Setup

- The cubic term at high-T is induced by loops of scalars, not fermions

- Add a single complex scalar  $\Phi$ , with  $V_\Phi = m_0^2|\Phi|^2 + \kappa|\Phi|^2|H|^2 + \eta|\Phi|^4$ .

- One-loop corrections to the potential at both T=0 and finite-T are well known:

$$V_1(\varphi) = \frac{g_i(-1)^{F_i}}{64\pi^2} \left[ m_i^4(\varphi) \log \frac{m_i^2(\varphi)}{m_i^2(v)} - \frac{3}{2}m_i^4(\varphi) + 2m_i^2(\varphi)m_i^2(v) \right];$$

$$V_T(\varphi; T) = \frac{g_i T^4 (-1)^{F_i}}{2\pi^2} \int_0^\infty dx x^2 \log \left[ 1 - (-1)^{F_i} \exp \left( \sqrt{x^2 + \frac{m_i^2(\varphi)}{T^2}} \right) \right],$$

- Again, the key object is the Higgs-dependent  $\Phi$  mass! But recall:

$$\mathcal{L}_{h\gamma\gamma} = \frac{2\alpha}{9\pi v} C_\gamma h F_{\mu\nu} F^{\mu\nu}, \quad \mathcal{L}_{hgg} = \frac{\alpha_s}{12\pi v} C_g h G_{\mu\nu} G^{\mu\nu}$$

$$C_\gamma = 1 + \frac{3}{8} \sum_f^{\text{Dirac fermions}} N_{c,f} Q_f^2 \frac{\partial \ln m_f^2(v)}{\partial \ln v} + \frac{3}{32} \sum_s^{\text{scalars}} N_{c,s} Q_s^2 \frac{\partial \ln m_s^2(v)}{\partial \ln v}$$

$$C_g = 1 + \sum_f^{\text{Dirac fermions}} C(r_f) \frac{\partial \ln m_f^2(v)}{\partial \ln v} + \frac{1}{4} \sum_s^{\text{scalars}} C(r_s) \frac{\partial \ln m_s^2(v)}{\partial \ln v},$$

- Expect **direct correlation** between the size of the cubic coupling induced at finite-T and non-SM contributions to  $hgg$  and  $h\gamma\gamma$  (unless  $\Phi$  is color and EM-neutral)

# Analytic Example

- A special case can be studied analytically\*:  $m_0 = 0$

- High-temperature expansion of the thermal potential:

$$V_{\text{eff}}(\varphi; T) = V_0(\varphi) + V_T(\varphi; T) \approx \frac{1}{2} \left( -\mu^2 + \frac{g_\Phi \kappa T^2}{24} \right) \varphi^2 - \frac{g_\Phi \kappa^{3/2} T}{24\sqrt{2}\pi} \varphi^3 + \frac{\lambda}{4} \varphi^4$$

- Location of the broken-symmetry minimum at finite T:  $\frac{\partial V_{\text{eff}}}{\partial \varphi} = 0 \rightarrow \varphi_0(T)$

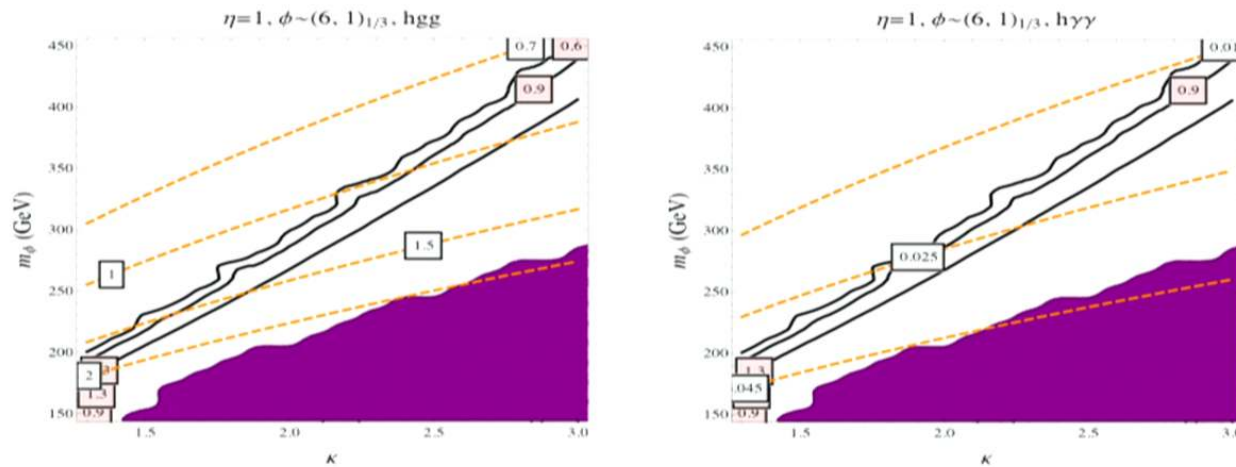
- Critical temperature:  $V_{\text{eff}}(0, T_c) = V_{\text{eff}}(\varphi_0(T_c), T_c)$

- Solve together:  $T_c^2 = \frac{24\mu^2}{g_\Phi \kappa \left( 1 - \frac{g_\Phi \kappa^2}{24\pi^2 \lambda} \right)}, \quad \varphi_+(T_c) = \frac{g_\Phi \kappa^{3/2} T_c}{12\sqrt{2}\pi \lambda}$

- Strongly 1-st order if  $\kappa > 3.6 g_\Phi^{-2/3}$

- Gluon-Higgs coupling:  $R_g = \frac{1}{8} \frac{\kappa v^2}{m_0^2 + \kappa v^2} \approx 0.12$

# Results: "Sextet"

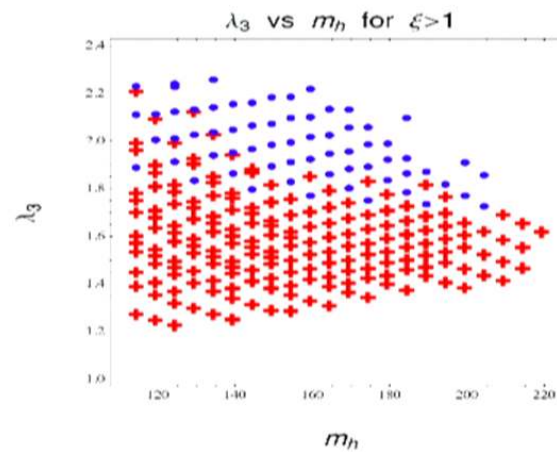
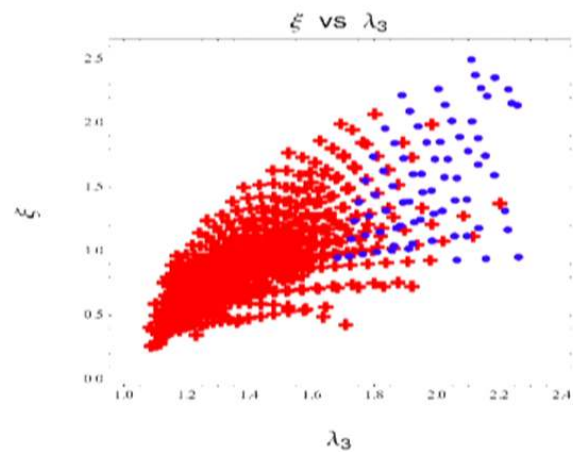


ATLAS:  $R_g = 1.08 \pm 0.14,$   $R_\gamma = 1.23^{+0.16}_{-0.13}.$   $\rightarrow$  ruled out!\*

[\* usual caveat: SM total width assumed]

# Higgs Self-Coupling

[Noble, MP, 0711.3018]



same correlation for Higgs self-coupling: deviations of **20% or more** in a broad range of models with first-order EWPT

Measure it at a 100 TeV collider?

# Conclusions: EWPT

- Strongly first-order EWPT, and with it Electroweak Baryogenesis, remains a **viable possibility** in a general BSM context
- We focused on the models where first-order EWPT is induced by **loops** of a BSM scalar, with various SM quantum numbers
- In the case of colored scalar, **LHC-14** measurement of  $hgg$  will be able to conclusively probe the full parameter space with 1-st order EWPT
- For non-colored scalars, **e+e- Higgs factories** will be necessary
- **TLEP** would be able to conclusively probe the full parameter space with 1-st order EWPT in **all models**, even if induced by a SM-singlet scalar