

Title: Motion of disc-shaped colloids and pairs of colloidal discs in a nematic liquid crystal

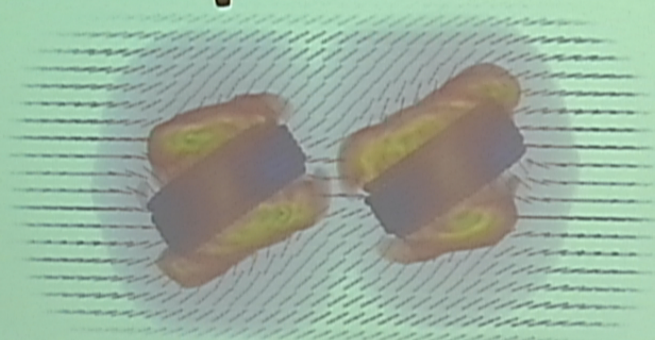
Date: May 07, 2014 04:05 PM

URL: <http://pirsa.org/14050057>

Abstract: <span>In the present work the motion of disc-shaped particles in a nematic liquid crystal was simulated via a Lattice Boltzmann algorithm. Under the action of a rotating magnetic field the colloidal disc with perpendicular surface anchoring immersed in a nematic liquid crystal experiences a torque and continues turning following the field. However when the disc reaches some critical position when the director field around it is highly distorted the disc suddenly flips to minimize the free energy. Analyzing this motion and consequently the behaviour of two discs placed close together we examine the possible uses of this peculiar flip behaviour.</span>

# Motion of disc-shaped colloids and pairs of colloidal discs in a nematic liquid crystal

Alena Antipova



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May 7, 2014

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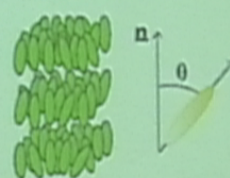
## Properties of the LC



Arrangement of molecules in solids



Arrangement of molecules in liquids

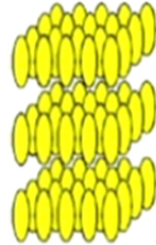


Arrangement of molecules in LC

$$\text{Scalar order parameter } S = \frac{1}{2} \langle 3 \cos^2 \theta - 1 \rangle, 0 < S < 1$$

$$\text{Tensor order parameter } Q_{\alpha\beta} = \langle n_{\alpha} n_{\beta} - \frac{1}{3} \delta_{\alpha\beta} \rangle$$

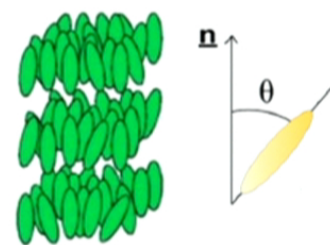
# Properties of the LC



Arrangement of  
molecules in  
solids



Arrangement of  
molecules  
in liquids



Arrangement of  
molecules  
in LC

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## Equations of motion

1) Continuity equation

$$(\partial_t \rho + \partial_\alpha \rho u_\alpha) = 0$$

2) Navier - Stokes equation

$$\rho \partial_t u_\alpha + \rho u_\beta \partial_\beta u_\alpha = \partial_\beta \tau_{\alpha\beta} + \partial_\beta \sigma_{\alpha\beta} + \frac{\rho \tau_f}{3} (\partial_\beta (\delta_{\alpha\beta} - 3a_0) \partial_\gamma u_\gamma + \partial_\alpha u_\beta + \partial_\beta u_\alpha)$$

3) Tensor order parameter evaluated by

$$(\partial_t + \mathbf{u} \cdot \nabla) \mathbf{Q} - \mathbf{S}(\mathbf{W}, \mathbf{Q}) = \Gamma \mathbf{H}$$

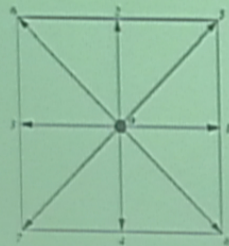
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## Lattice Boltzmann Algorithm

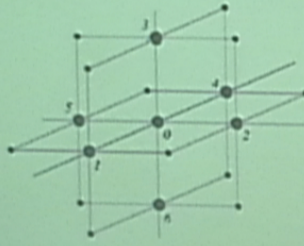
LB algorithm uses partial velocity distribution functions  $f_i = f_i(\vec{x}, t)$  and symmetric traceless tensors  $\mathbf{G}_i(\vec{x})$ .

$$\rho = \sum_i f_i, \rho u_\alpha = \sum_i f_i e_{i\alpha}, \mathbf{Q} = \sum_i \mathbf{G}_i$$

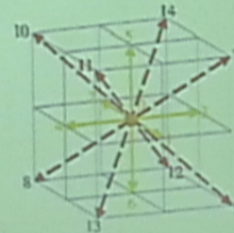
Velocity models: D1Q3, D1Q5, D2Q9, D3Q7, D3Q19, ...



D2Q9



D3Q7



D3Q15

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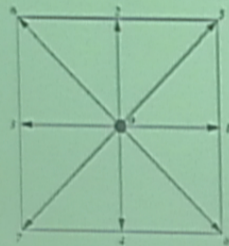
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## Lattice Boltzmann Algorithm

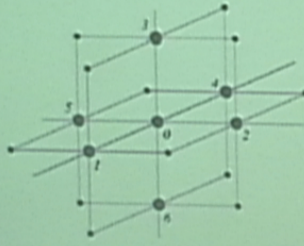
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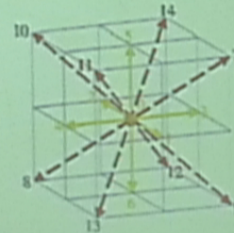
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D2Q9



D3Q7



D3Q15

more

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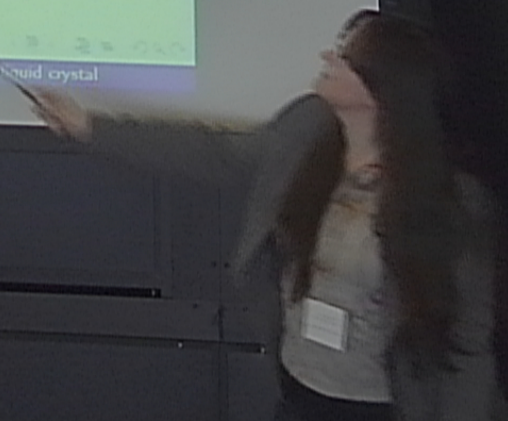
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# The problem

No external forces       $\theta = \frac{\pi}{2}$       Before flip,  $\theta > \frac{\pi}{2}$       After flip

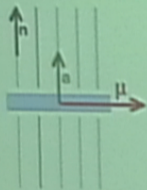
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# The problem

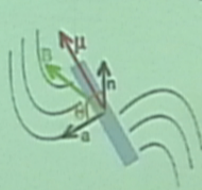
No external forces



$\theta = \frac{\pi}{2}$



Before flip,  $\theta > \frac{\pi}{2}$

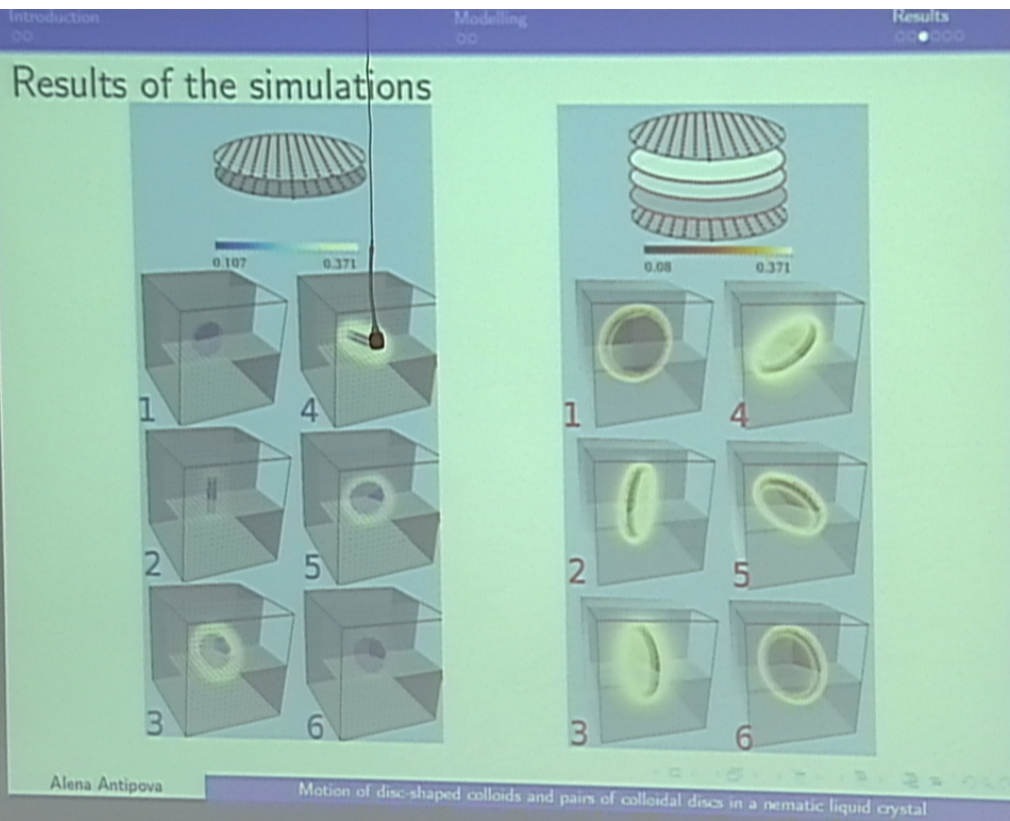


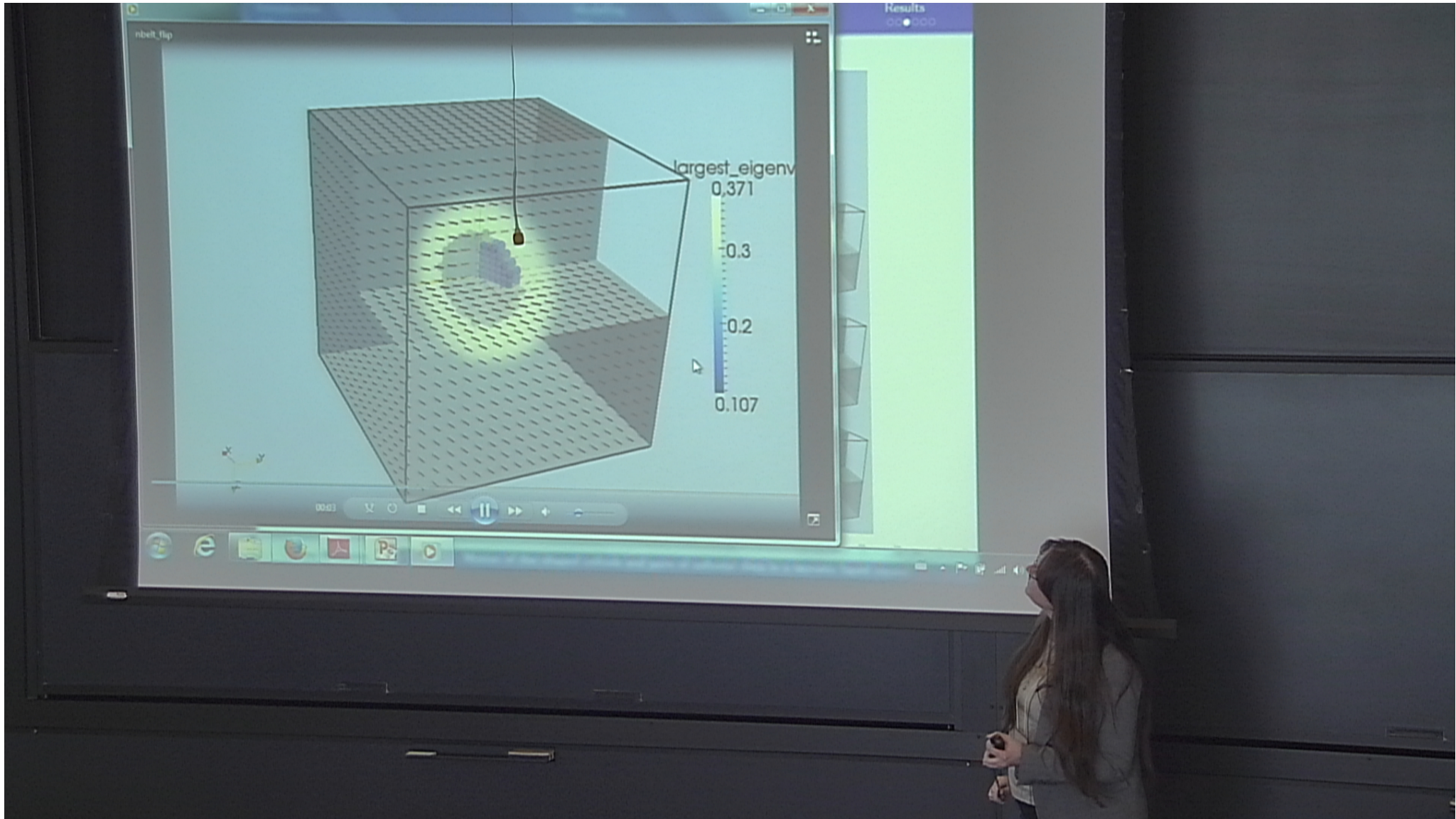
After flip



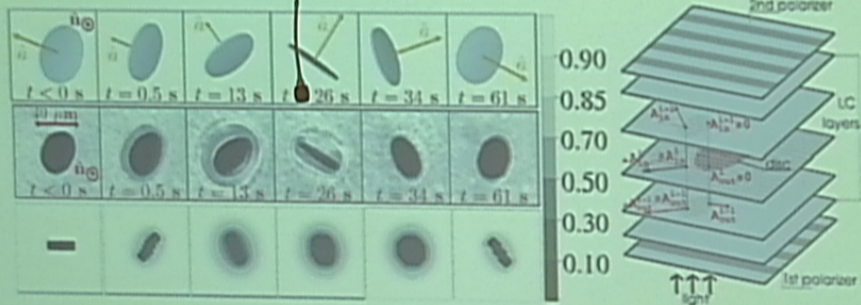
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# Light transmission



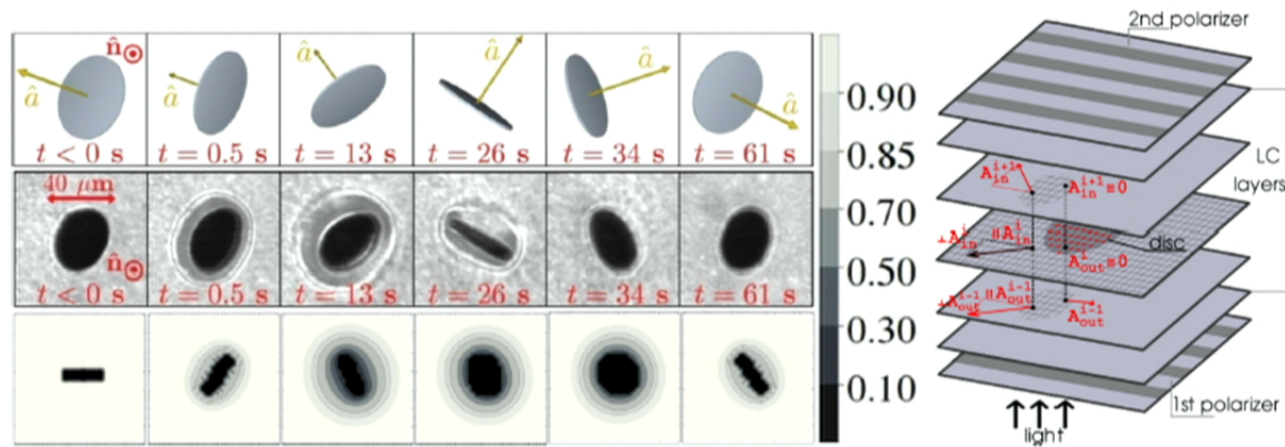
Elastic and hydrodynamic torques on a colloidal disk within a nematic liquid crystal  
J. Rovner, D. Bergnia, D. Reich, R. Lehny

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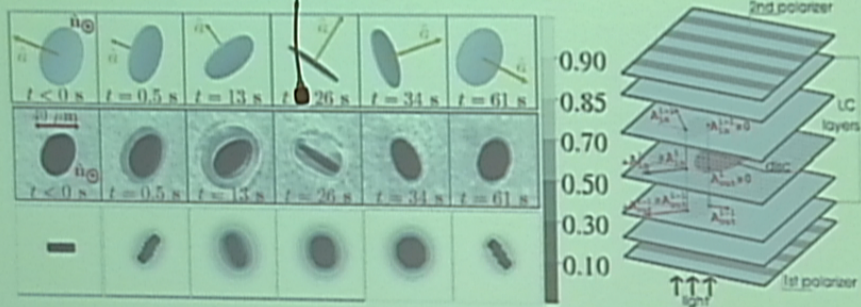
# Light transmission



Elastic and hydrodynamic torques on a colloidal disk within a nematic liquid crystal

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# Light transmission



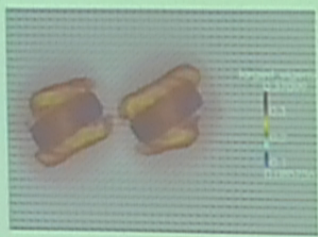
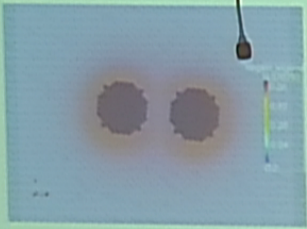
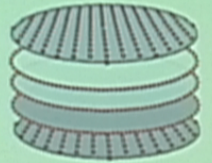
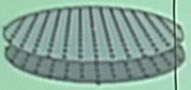
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# Two discs



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Motion of disc-shaped colloids and pairs of colloidal discs in a nematic liquid crystal



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# Two discs

The slide illustrates the interaction of two disc-shaped colloids in a nematic liquid crystal. It features two columns of images. The left column shows a single disc with a grid of lines on its surface, and below it, a simulation of two dark, circular discs with a color scale ranging from 0.00 to 0.20. The right column shows a stack of three discs with a grid of lines, and below it, a simulation of two orange, elongated discs with a color scale ranging from 0.00 to 0.20. A vertical line with a small black dot at the bottom is positioned between the two columns.

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## References

1. Elastic and hydrodynamic torques on a colloidal disk within a nematic liquid crystal, J. Rovner, D. Borgnia, D. Reich, R. Leheny. *Physical Review E Stat. Nonlin. Soft. Matter. Phys.* (2012)
2. Lattice Boltzmann simulations of Liquid Crystal Hydrodynamics, C. Denniston, E. Orlandini, J. M. Yeomans *Physical Review E* 63, (2001)
3. Lattice Boltzmann algorithm for three-dimensional liquid-crystal hydrodynamics, C. Denniston, D. Marenduzzo, E. Orlandini, and J.M. Yeomans *Phil. Trans. R. Soc. Lond. A* 362, 1745—1754, (2004)
4. Coupling MD particles to a Lattice-Boltzmann fluid through the use of conservative forces, F. E. Mackay, C. Denniston, *Journal of Computational Physics* 237, 289 (2013)
5. Elastic response of a nematic liquid crystal to an immersed nanowire, C. J. Smith, C. Denniston, *Journal of Applied Physics* 125
6. Deformable vesicles interacting in a nematic liquid crystal, F. E. Mackay, C. Denniston, *Soft Matter* 9, 5285—5292, (2013)
7. Lattice Boltzmann method for fluid flows, Chen, S. Doolen, G. D., *A. Rev. fluid Mech.* 30, 329—364, (1998)
8. de Gennes, P.-G. Prost, J. 1993 *The physics of liquid crystals*, 2nd edn. Oxford: Clarendon.

Thank you!