

Title: New insights into polymer-induced drag reduction in turbulent flows

Date: May 07, 2014 10:35 AM

URL: <http://pirsa.org/14050041>

Abstract: Polymer additives are known to cause significant reduction in turbulent friction drag and reduce the energy dissipation rate of fluid transport. This effect is however bounded by a universal upper limit the maximum drag reduction (MDR) asymptote that does not change with polymer properties. Understanding MDR remains an important unsolved problem in the areas of turbulence and non-Newtonian fluid mechanics. Dynamical trajectories on the boundary in state space between laminar and turbulent plane channel flow - edge states - are computed for Newtonian and viscoelastic fluids. Viscoelasticity has a negligible effect on the properties of these solutions and at least at a low Reynolds number their mean velocity profiles correspond closely to experimental observations for polymer solutions in the MDR regime. These results confirm the existence of weak turbulence states that cannot be suppressed by polymer additives explaining the fact that there is an upper limit for polymer-induced drag reduction.

New insights into polymer-induced drag reduction in turbulent flows

Li Xi

*Department of Chemical Engineering
McMaster University*

Compute Ontario Research Day
Waterloo, ON, May 7, 2014



1

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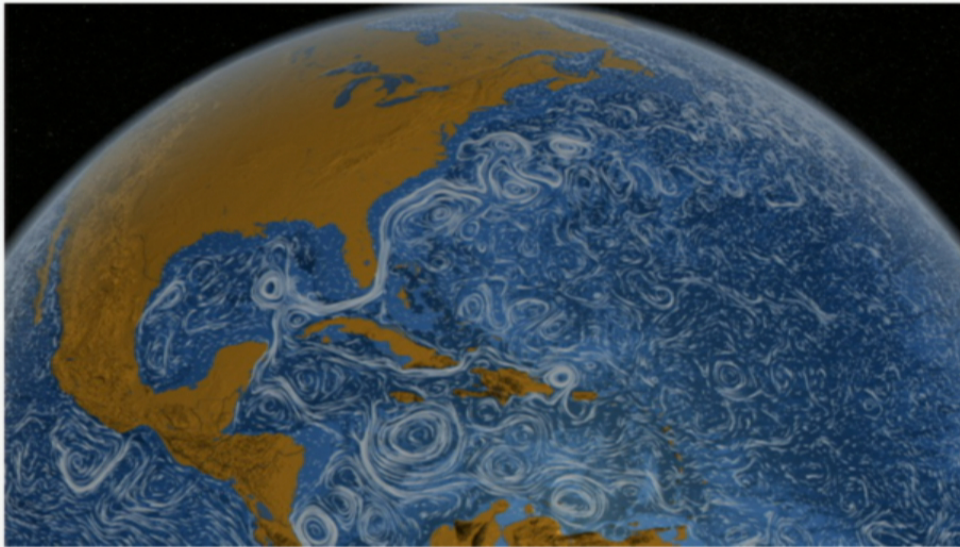
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1

What is turbulence?



nasa.gov

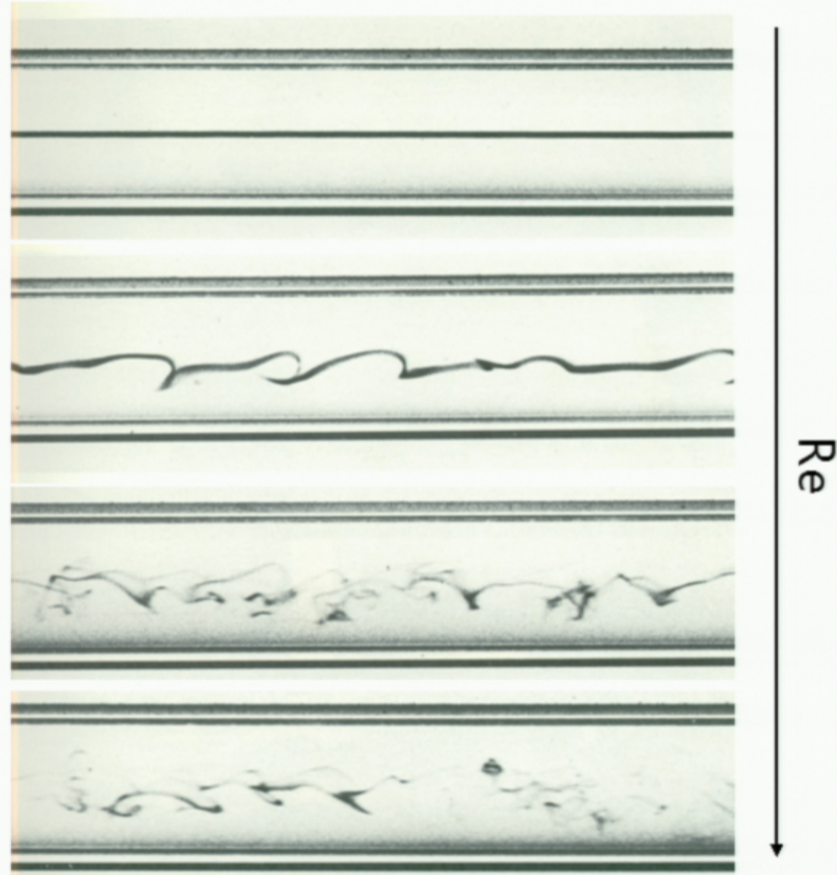


Hu D. L. and Bush J. W. M., *Phys. Fluids*, 2005

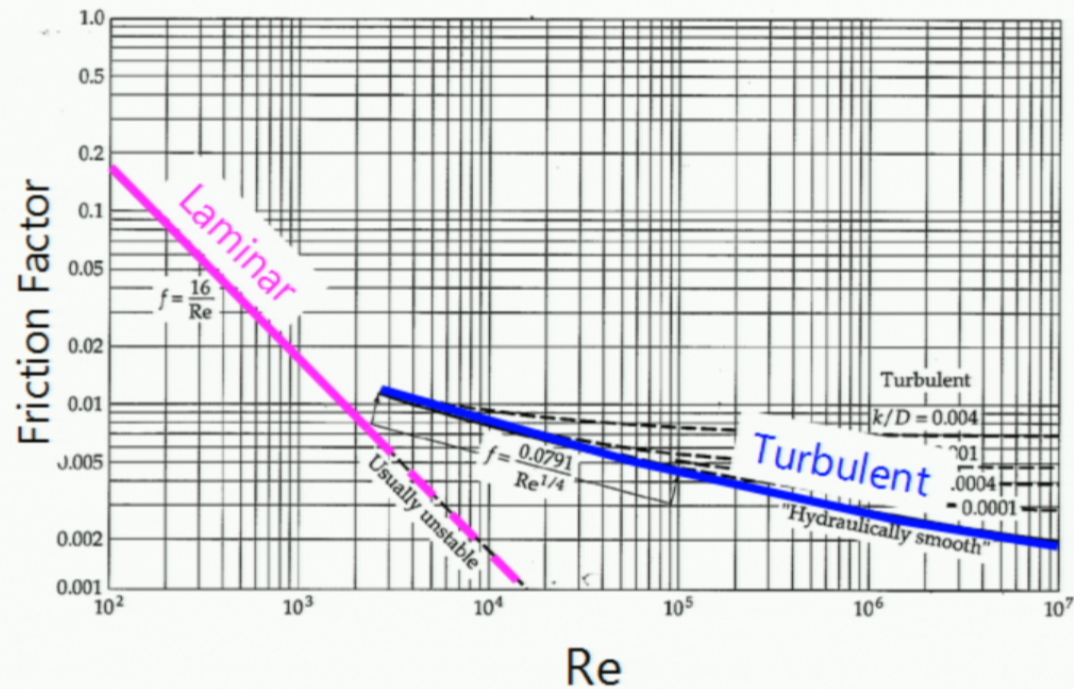


Hiuchi H, *Phys. Fluids*, 1993

Laminar-Turbulent Transition in Pipe Flow



Why do we care?



Bird, Stewart and Lightfoot, *Transport Phenomena*, 2nd ed., 2002



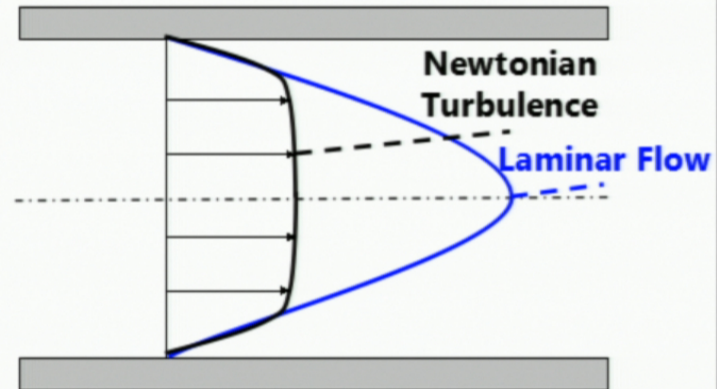
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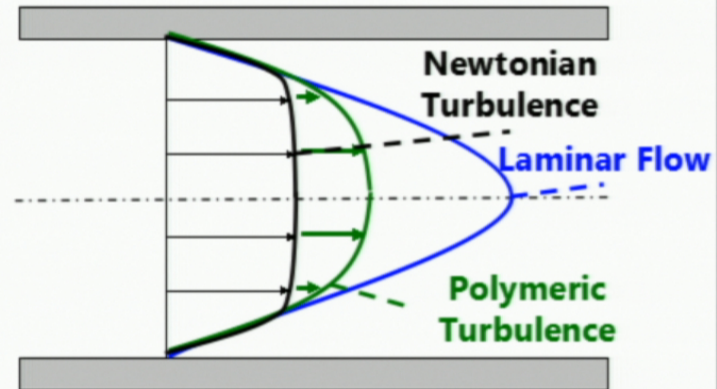
Turbulence of polymer solutions: drag reduction effects

- Very low polymer concentration
 - O(10)-O(100) wppm
- DR% up to 80%.
- Energy saving in fluid transportation.
- Theoretical significance:
 - Turbulence & polymer physics.



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Trans-Alaska Pipeline System



picture credit: <http://www.alyeska-pipe.com/>

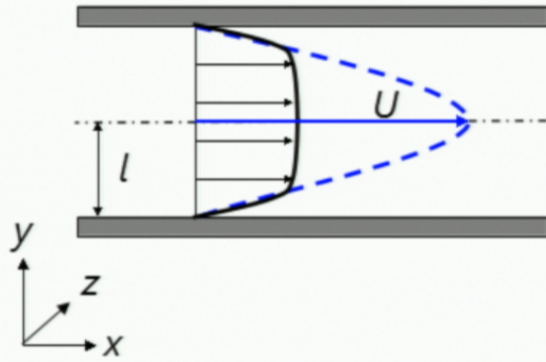
Simulation of viscoelastic turbulence

Physical Systems

PDEs

Fields

Parameters



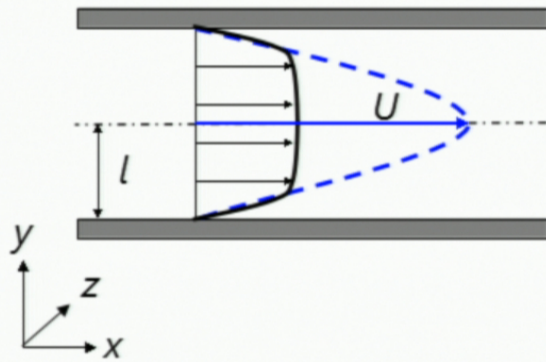
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Navier-Stokes Eq.

↓
velocity (\mathbf{v}) &
pressure (p)

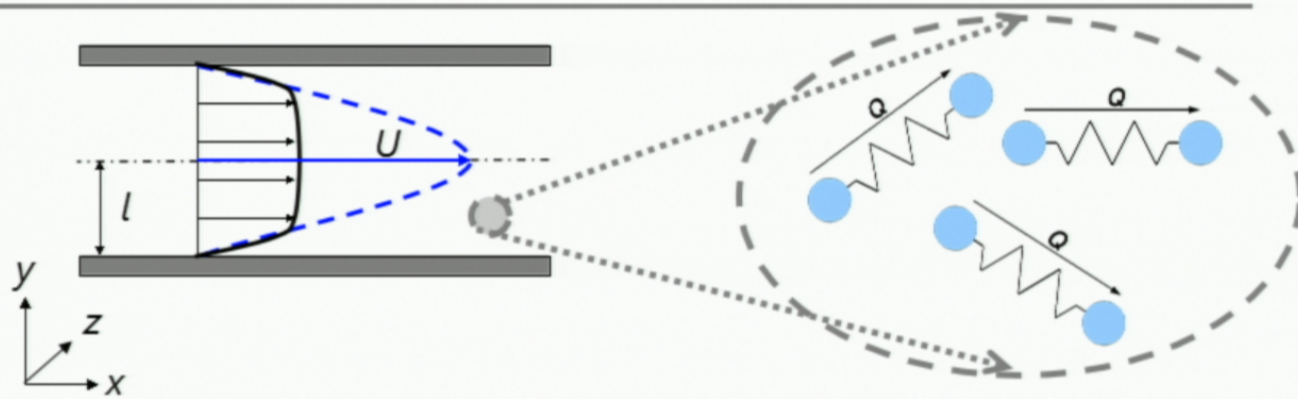
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FENE-P Constitutive Eq.

velocity (\mathbf{v}) &
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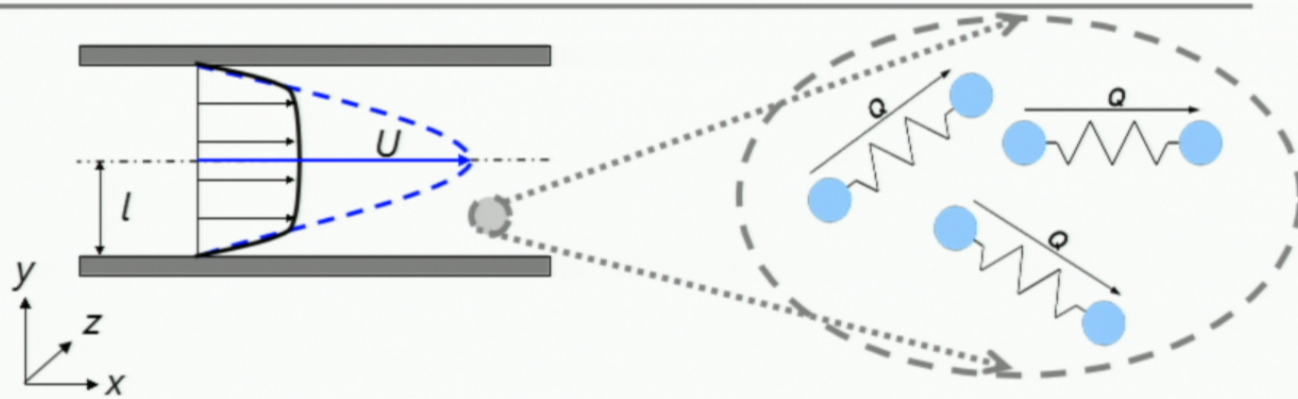
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polymer
conformation tensor: $\alpha \equiv \frac{H\langle \mathbf{Q}\mathbf{Q} \rangle}{kT}$

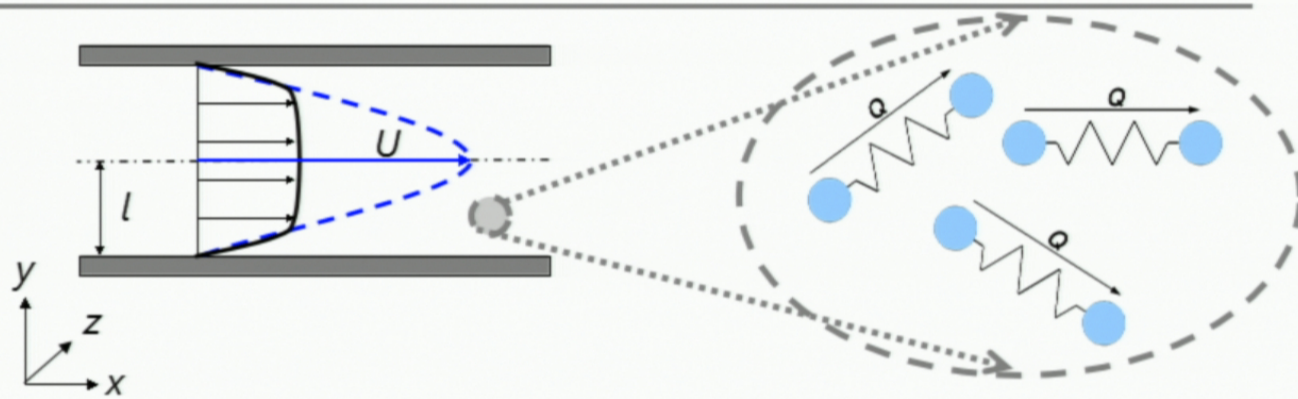
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$$\alpha \equiv \frac{H \langle \mathbf{Q}\mathbf{Q} \rangle}{kT}$$

$$\text{Re} \equiv \frac{\rho U l}{\eta_s + \eta_p} \quad \beta \equiv \frac{\eta_s}{\eta_s + \eta_p} \quad b \equiv \max(\text{tr}(\alpha)) \quad \text{Wi} \equiv \lambda \frac{2U}{l}$$

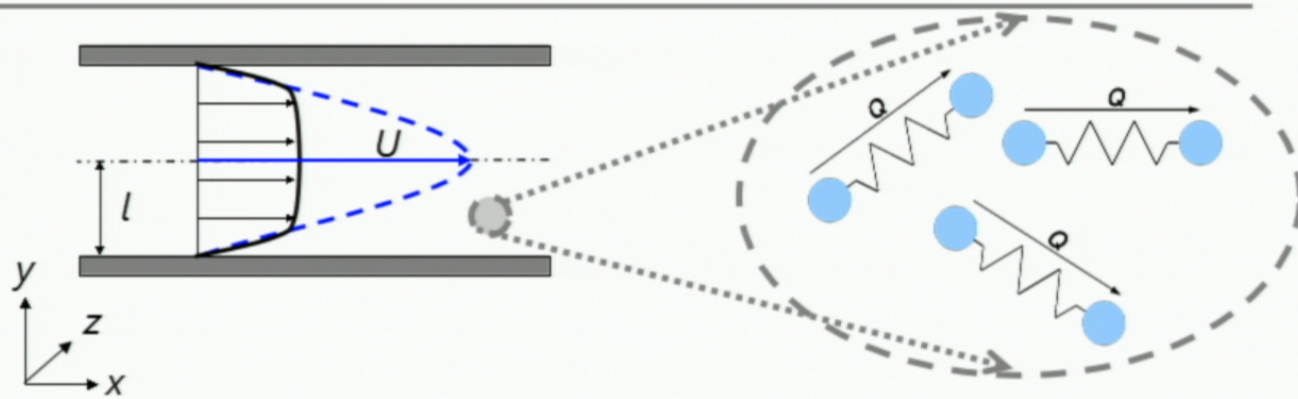
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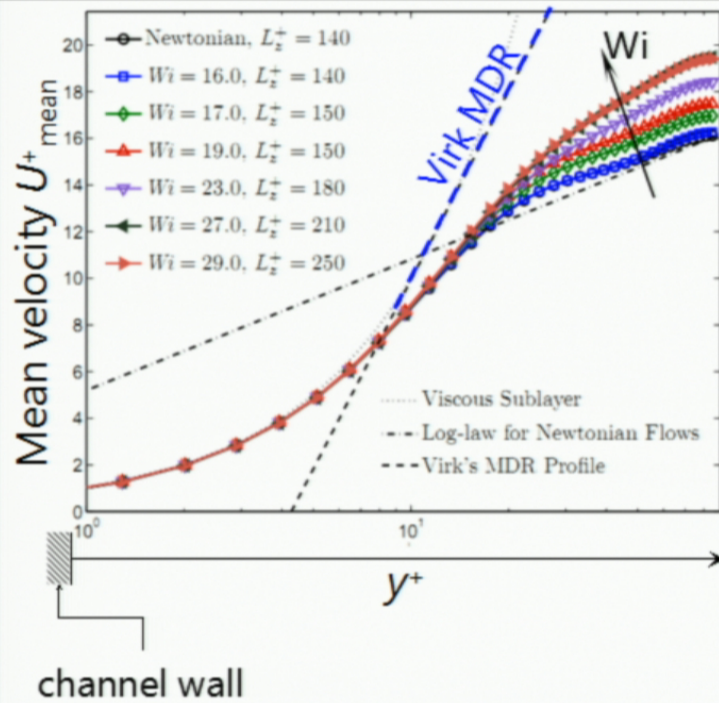
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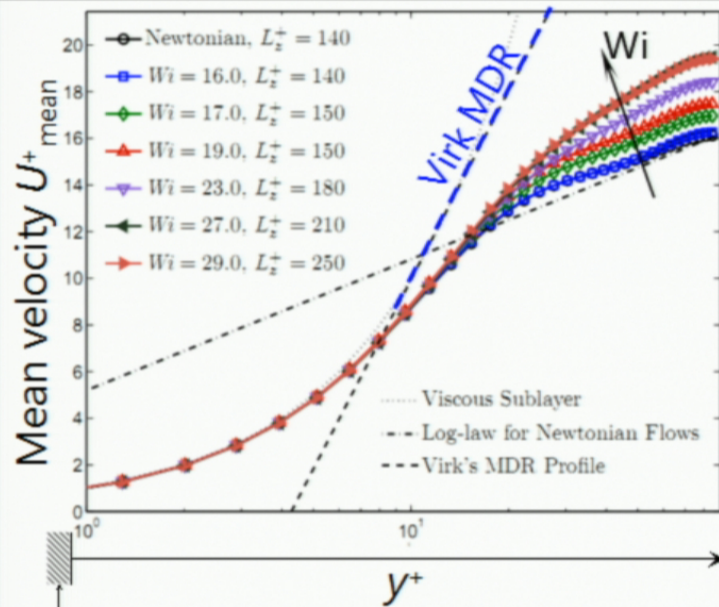
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DNS observation of drag reduction



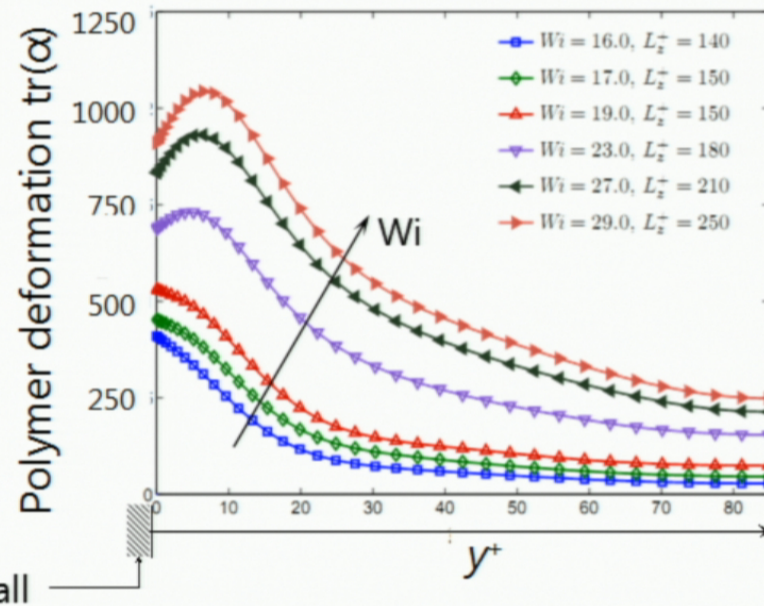
Xi & Graham, *J. Fluid Mech.* 2010

DNS observation of drag reduction



channel wall

Xi & Graham, *J. Fluid Mech.* 2010



channel wall

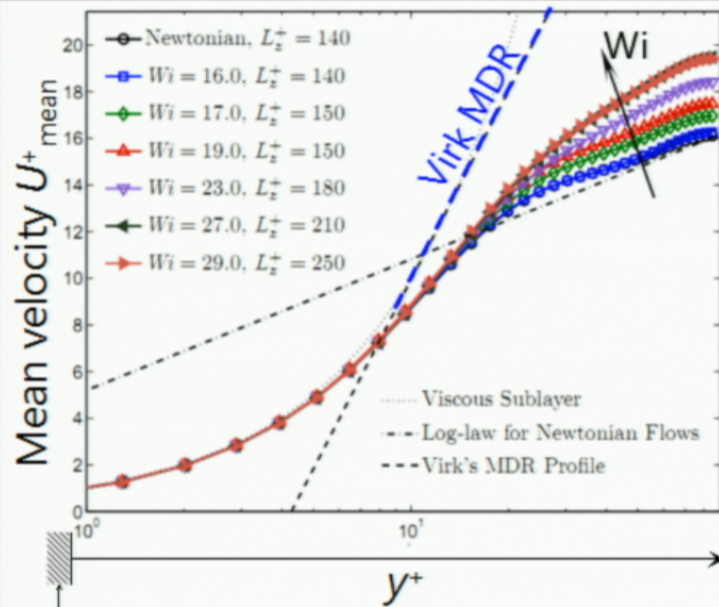


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DNS observation of drag reduction

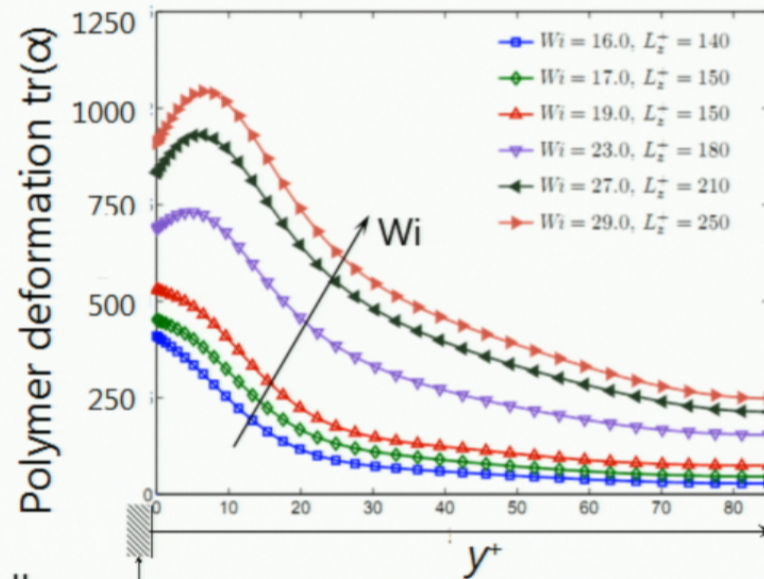


channel wall

Xi & Graham, *J. Fluid Mech.* 2010



polymer extension ->
 polymer stress ->
 turbulence suppression



channel wall

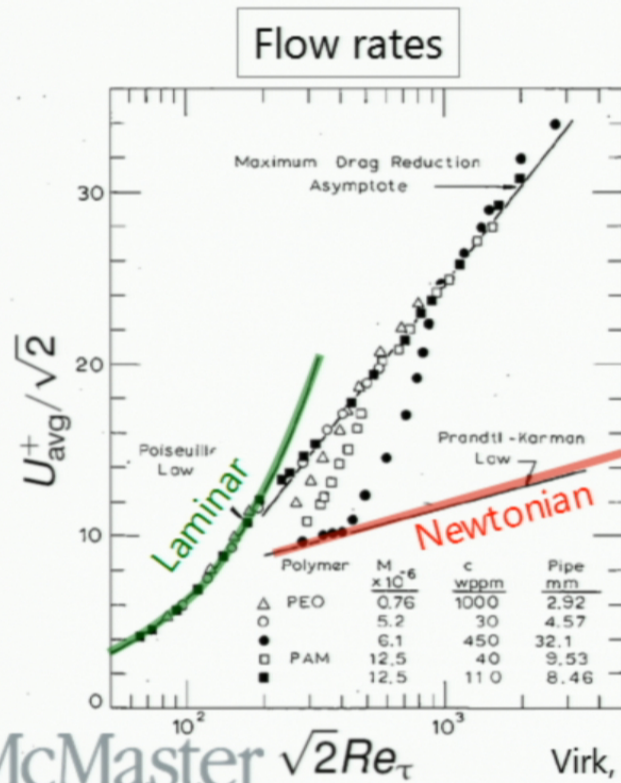
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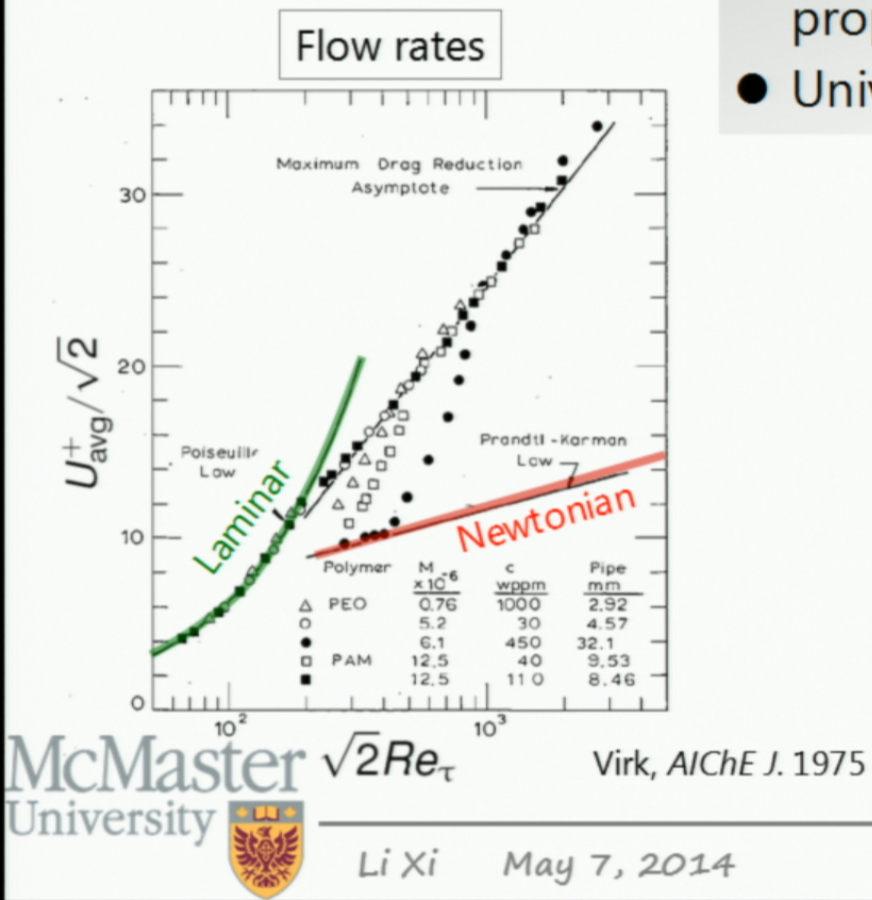
MDR: A universal upper limit of polymer drag reduction

- MDR** (maximum drag reduction):
- Insensitive to polymer-related properties.
 - Universal mean velocity profile.



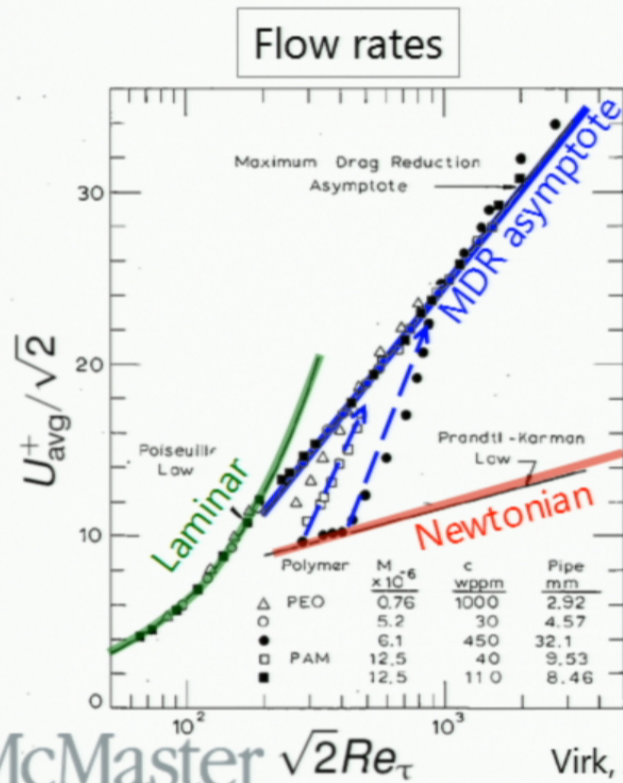
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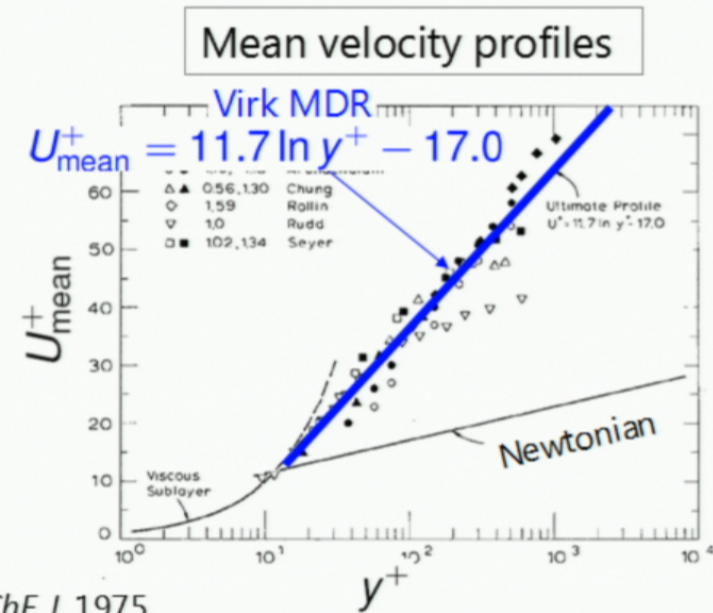
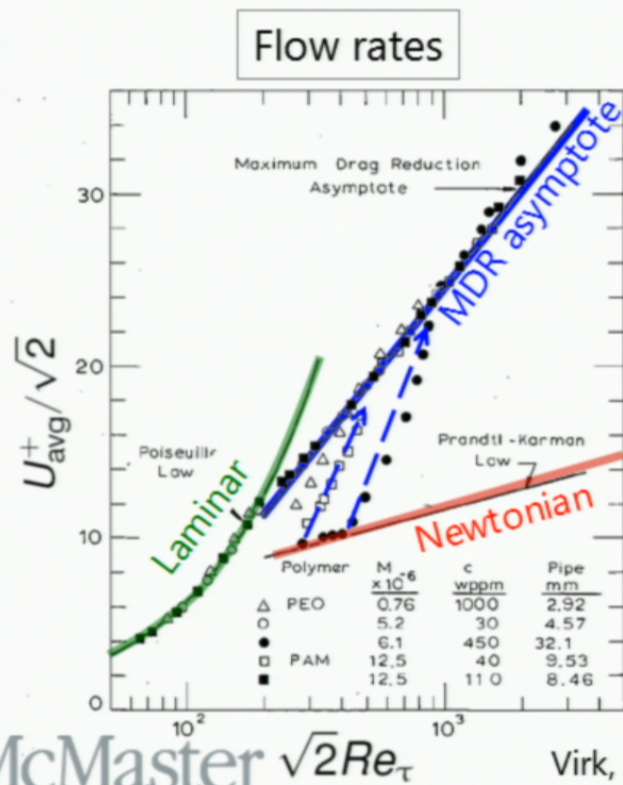
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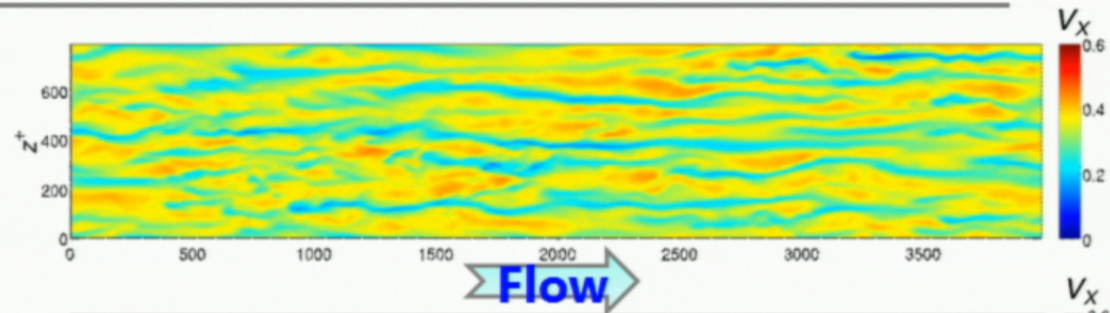
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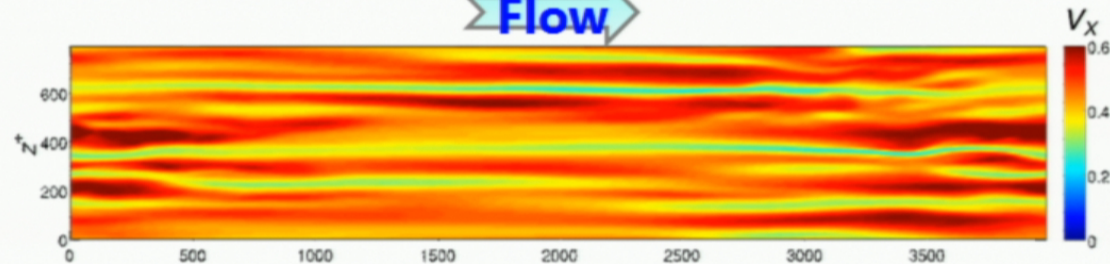


MDR: A universal upper limit of polymer drag reduction

Newtonian



$DR\% = 57\%$



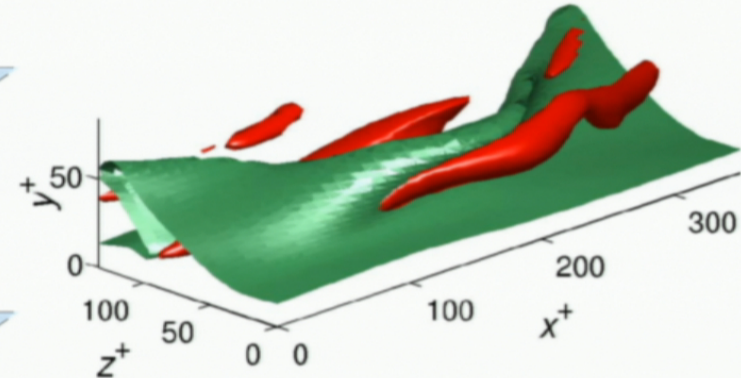
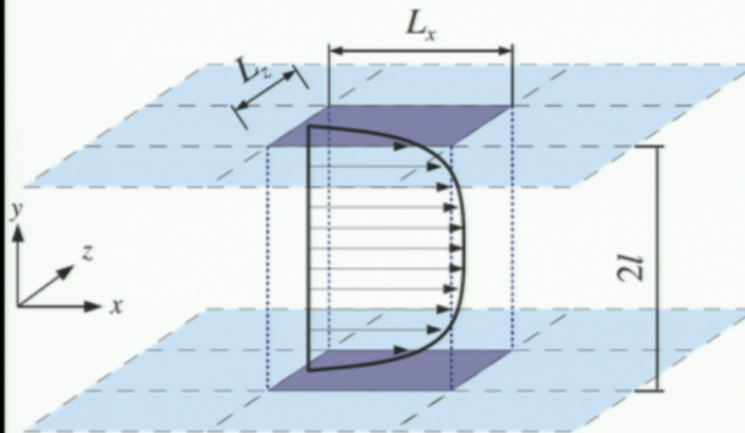
Xi, Ph.D. Dissertation, UW-Madison, 2009

Important questions:

- What sustains turbulence at MDR?
- Why is MDR universal (w.r.t. polymer properties)?
- What is the origin of the flow structures at MDR?

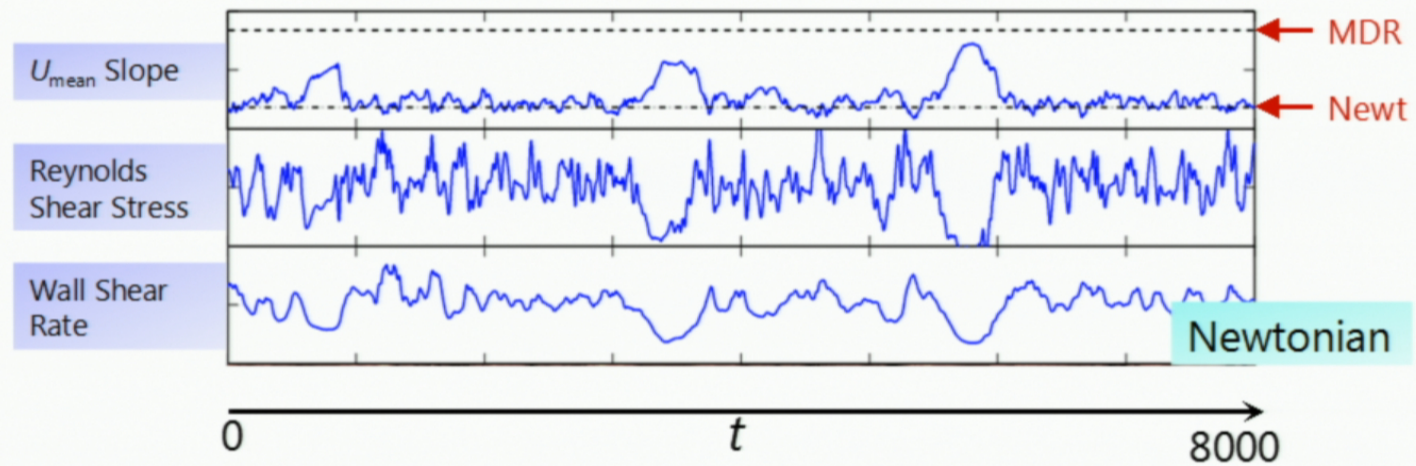
Method: minimal flow units (MFU)

- Isolate the essential flow structure for self-sustaining turbulence.
- Track the time evolution of the most important flow motions.

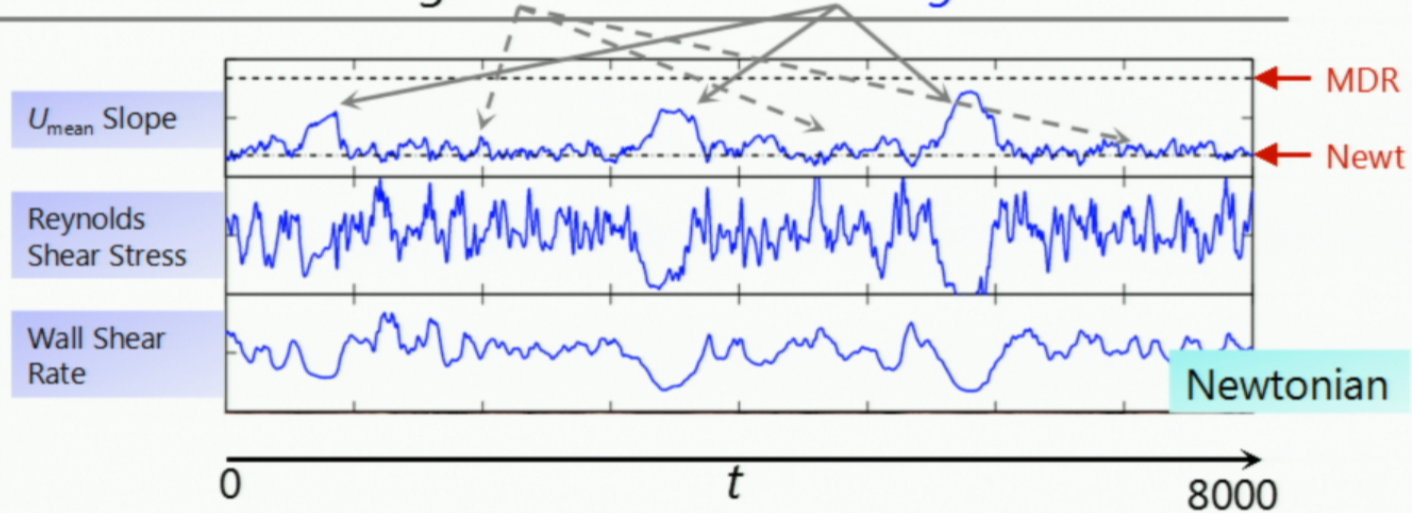


Red: streamwise vortices
Green: velocity isosurface
(upward pleat: low-speed streak)

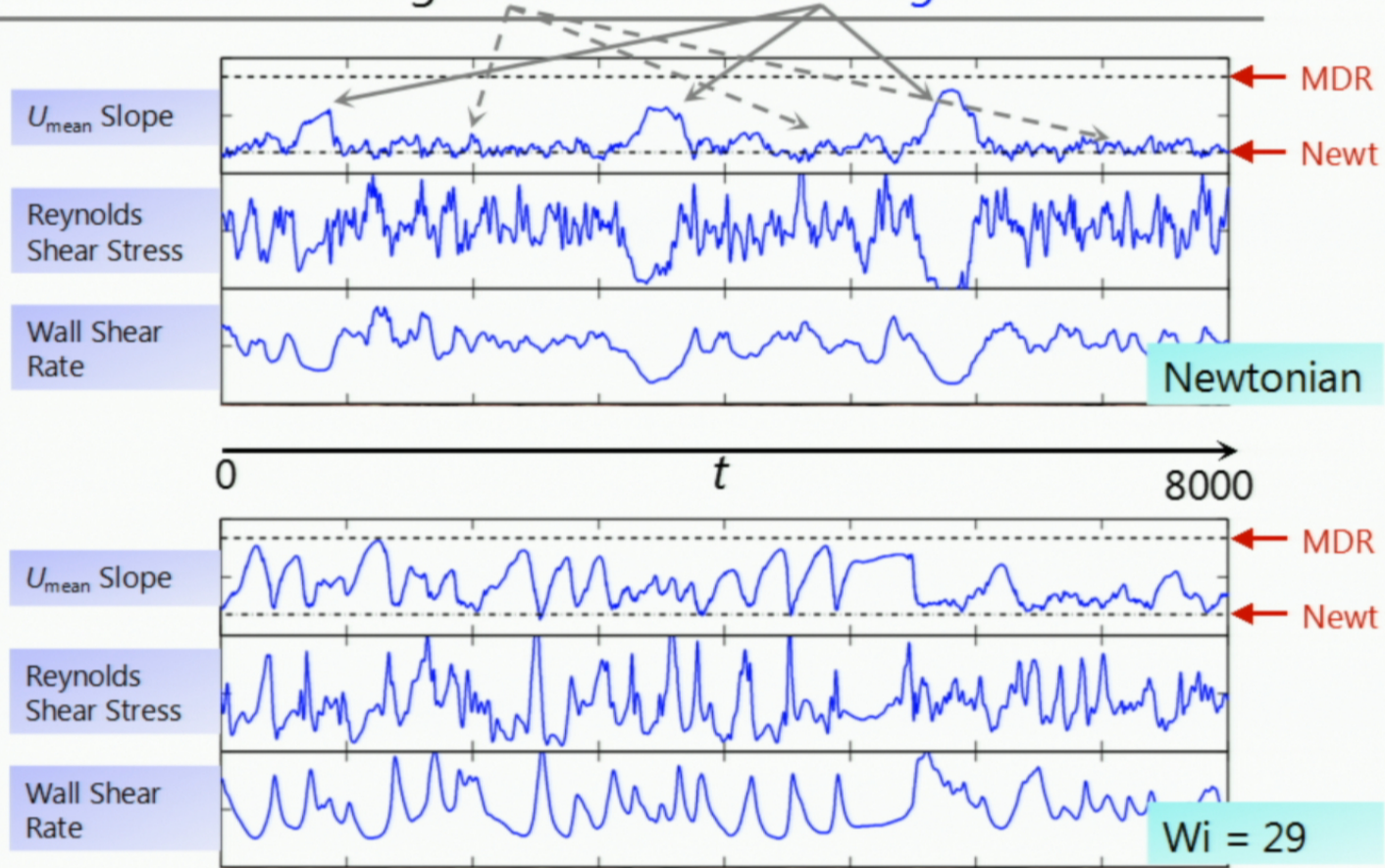
Time series: introducing *active* and *hibernating* turbulence



Time series: introducing *active* and *hibernating* turbulence



Time series: introducing *active* and *hibernating* turbulence



Xi & Graham, *Phys. Rev. Lett.*, 2010
 Xi & Graham, *J. Fluid Mech.*, 2012

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WPS 演示 开始 插入 设计 动画 幻灯片放映 审阅 视图 办公空间 未登录

从头开始 从当前开始 自定义放映

开始放映幻灯片

大纲 幻灯片

9 MDR: A universal upper limit of polymer drag reduction

Newtonian
DR% = 57%

Important questions:

- What sustains turbulence at MDR?
- Why is MDR universal (or is polymer-propagated)?
- What is the origin of the hair structures at MDR?

10 Method: minimal flow units (MFU)

- Isolate the essential flow structure for self-sustaining turbulence
- Track the time evolution of the most important flow features

Red streamwise vortices
Green velocity surfaces
Upward (blue) / downward (orange) streaks

11 Time series introducing color and naming turbulence

12 Dynamics during a typical hairaming period

幻灯片 11 / 17

bottom top

$\langle \partial v_x / \partial y \rangle_t$

U_{bulk}

t

x^+ z^+

U^*_{mean}

y^+

top bottom

y^+ z^+ x^+

60%

EN 10:58 AM 5/7/2014

WPS 演示 开始 插入 设计 动画 幻灯片放映 审阅 视图 办公空间 未登录

从头开始 从当前开始 自定义放映 开始放映幻灯片

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Red streamwise vortices
Green velocity structures
Upward streamlines (downward streamlines)

11 Time series: introducing noise and damping turbulence

12 Dynamics during a typical hairaming period

幻灯片 11 / 17

movie_r16

bottom top

$\langle \partial v_x / \partial y \rangle$

U_{bulk}

$\langle \partial v_x / \partial y \rangle_b$

t

U^*_{mean}

top
bottom

300
200
100
0

0 100 200

z^+

85
0
-85

200 100 0 100 300

z^+

y

x^+

00:42

60%

EN 10:59 AM 5/7/2014

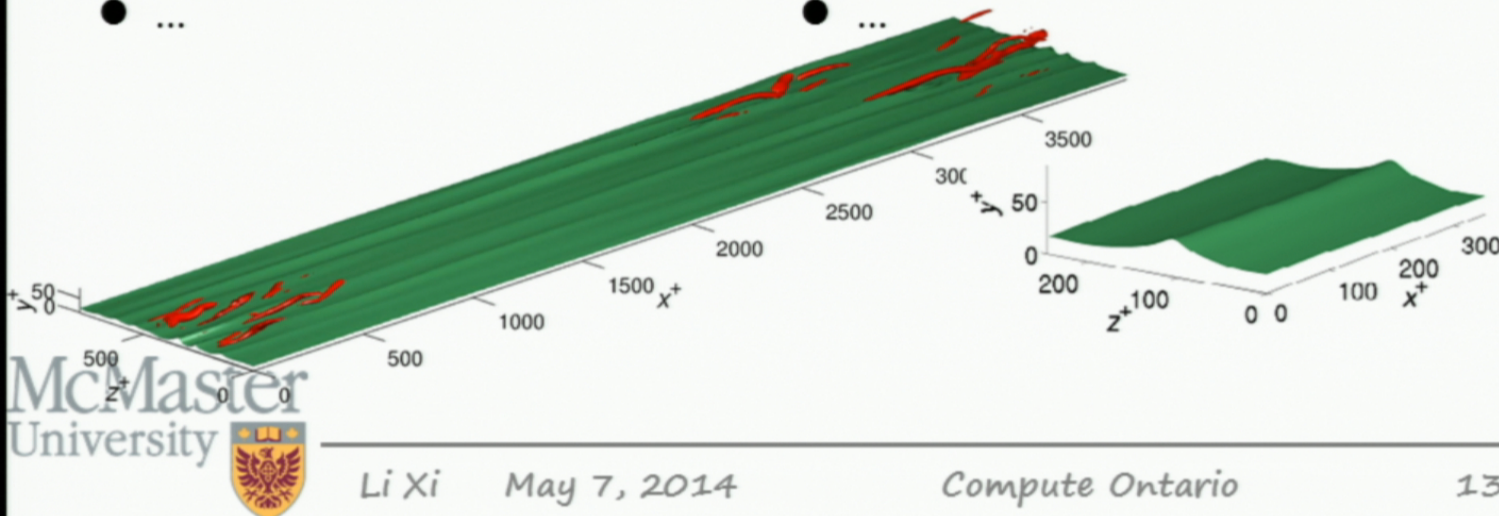
Hibernating turbulence vs. MDR: similarities

MDR

- Umean slope: $A = 11.7$.
- Weak streamwise vortices.
- Extended, mostly straight low-speed streaks.
- Lower transverse velocity fluctuations and Reynolds shear stress.
- ...

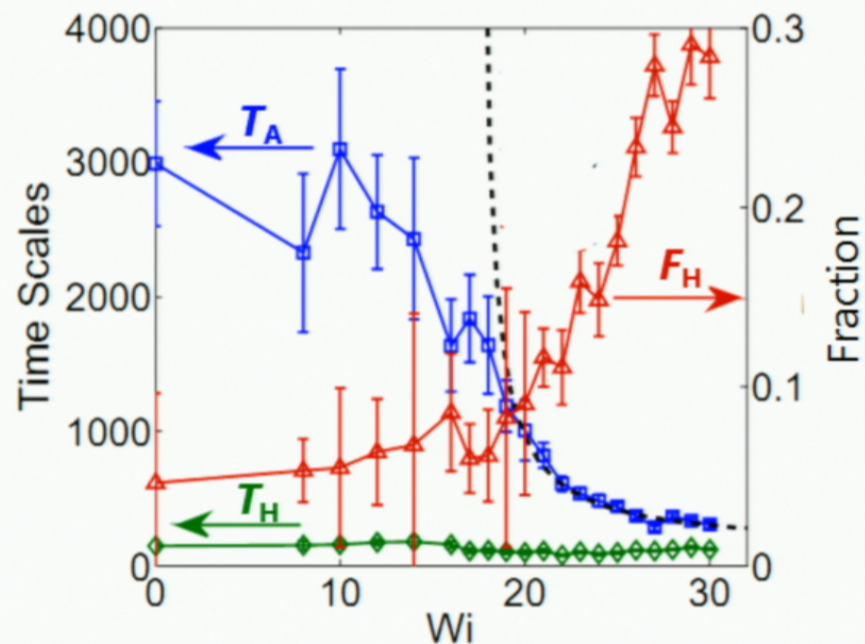
Hibernating Turbulence

- Umean slope: $A \rightarrow 11.7$
- Weak streamwise vortices.
- Almost streamwise-independent streaks.
- Lower transverse velocity fluctuations and Reynolds shear stress.
- ...



Frequency and duration of hibernating intervals

- T_{Active} decreases with Wi .
- $T_{Hibernating}$ approximately constant.
- Hibernation takes up a larger **fraction** in statistics at high Wi .



Xi & Graham, *Phys. Rev. Lett.*, 2010
Xi & Graham, *J. Fluid Mech.*, 2012



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14

Frequency and duration of hibernating intervals

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- Hibernation takes up a larger **fraction** in statistics at high Wi .

Hibernation is *Newtonian*.

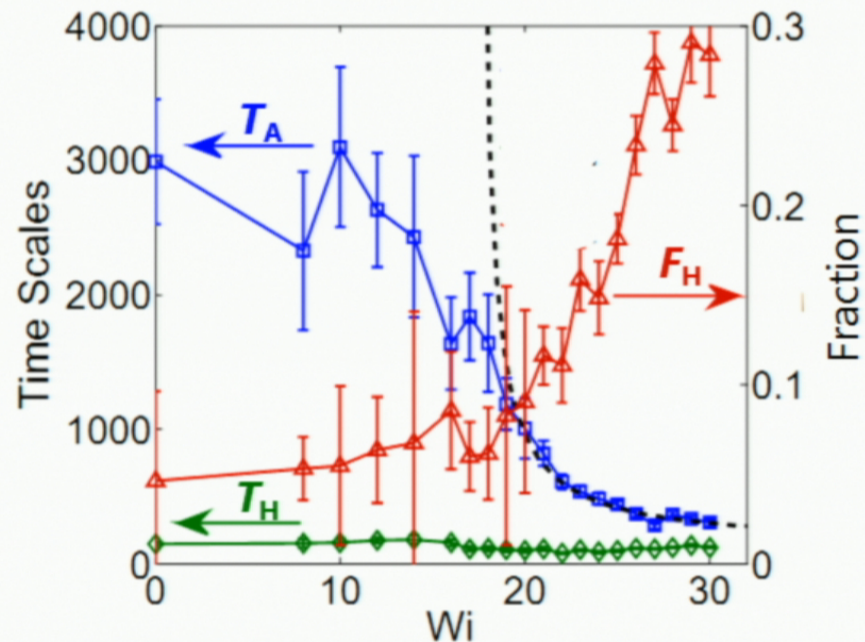
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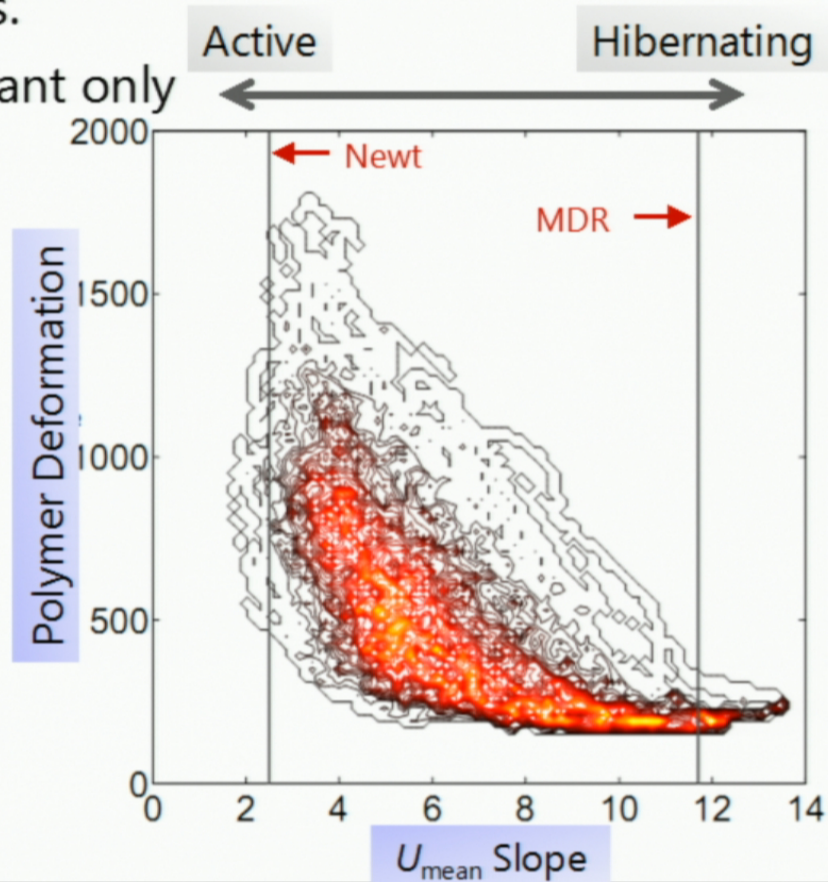
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14



Polymer conformation statistics

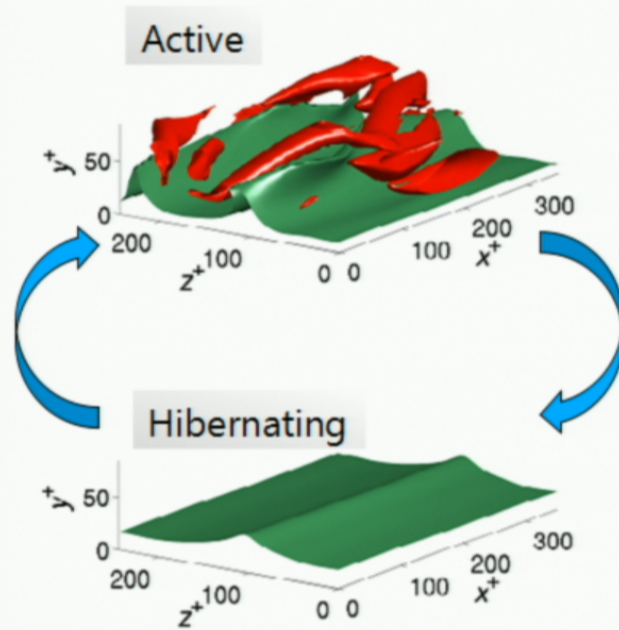
- Anti-correlation between the mean velocity and polymer stress.
- Polymer effects are important only within active intervals.



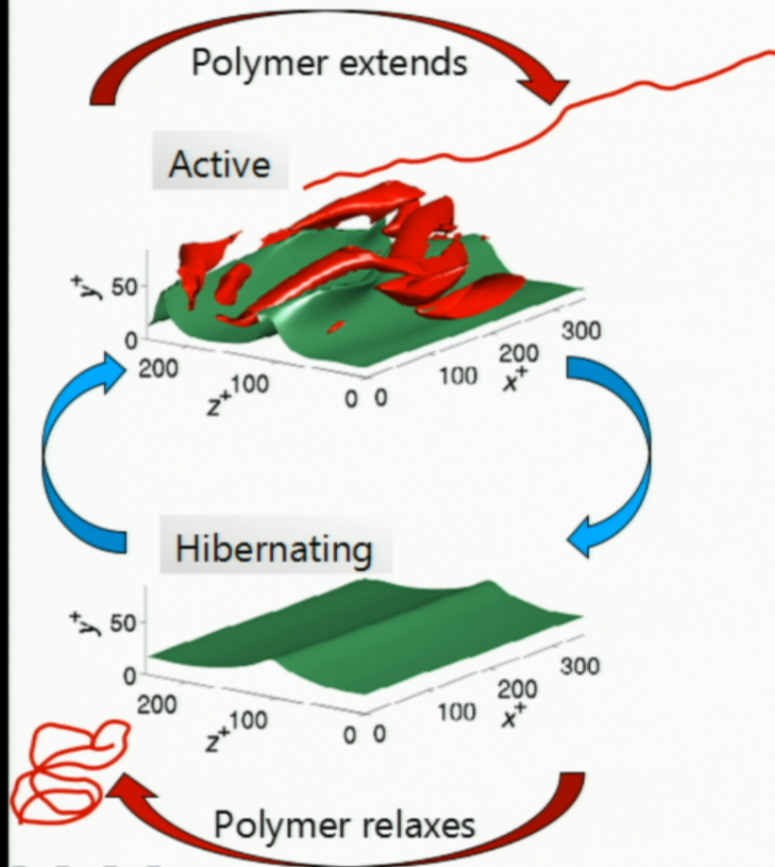
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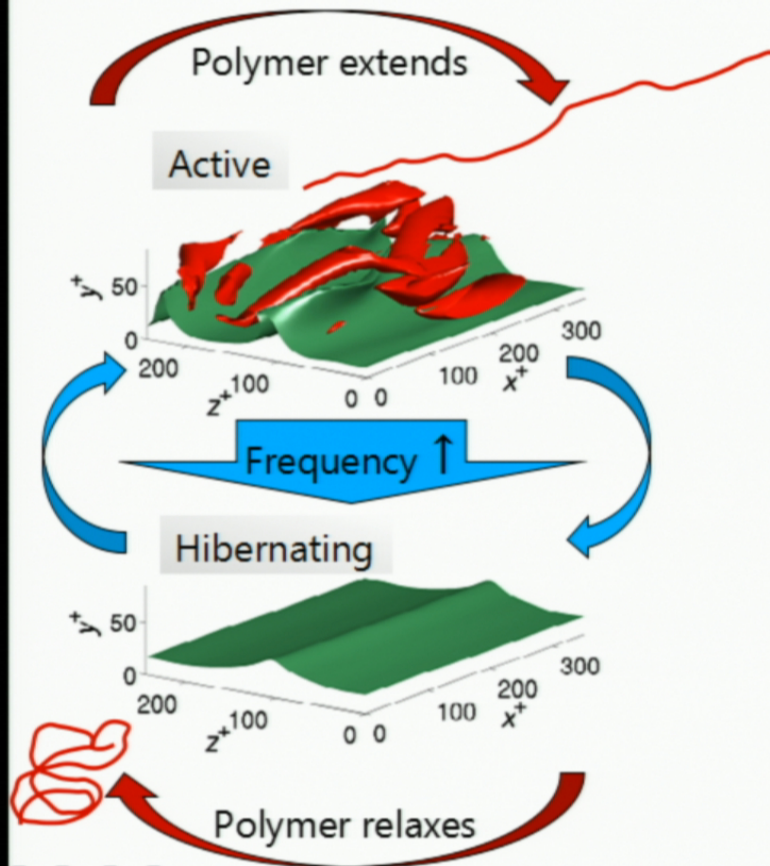
Physical picture and a simple model



Physical picture and a simple model



Physical picture and a simple model



Summary

- Hibernating turbulence:
 - Newtonian in nature.
 - MDR-like.
- Polymer suppresses active turbulence only.
- As $Wi \uparrow$, hibernation becomes more dominant, the flow appears more like MDR.
- A framework consistently explaining all major observations of MDR.

Acknowledgment:



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CRSNG**

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17