

Title: Generic Spin Model for Honeycomb Iridates Beyond the Kitaev Limit

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Abstract: Recently, realizations of Kitaev physics have been sought in the $A_2\text{IrO}_3$ family of honeycomb iridates, originating from oxygen-mediated exchange through edge-shared octahedra. However, for the $J=1/2$ Mott insulator in these materials exchange from direct d-orbital overlap is relevant, and it was proposed that a Heisenberg term should be added to the Kitaev model. Here we provide the generic nearest-neighbour spin Hamiltonian when both oxygen-mediated and direct overlap are present, containing a bond dependent off-diagonal exchange in addition to Heisenberg and Kitaev terms. We analyze this complete model using a combination of classical techniques and exact diagonalization. Near the Kitaev limit, we find new magnetic phases, 120 degree and incommensurate spiral order, as well as extended regions of zigzag and stripy order. Possible applications to Na_2IrO_3 and Li_2IrO_3 are discussed.

Generic spin model for the honeycomb iridates beyond the Kitaev limit

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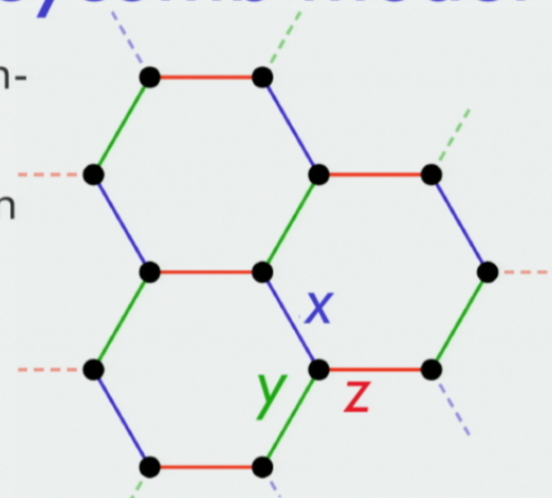
University of Toronto



Four Corners Meeting, May 2014

Kitaev's honeycomb model

- Exactly solvable spin- $\frac{1}{2}$ model
- Highly **anisotropic** in spin and space
- Ground state is Z_2 spin liquid
- Gapless Majorana fermions

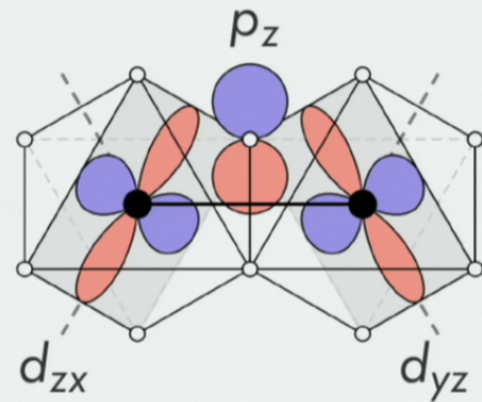


Can it be realized in a solid-state system?

Kitaev exchange $K \sum_{\langle ij \rangle \in \gamma} S_i^\gamma S_j^\gamma$

A. Kitaev, Ann. Phys. (2005)

Spin-orbit Mott insulators



- Edge-shared oxygen octahedra
- Effective $j=1/2$ spin model
- Considers **only** oxygen mediated exchange

Ferromagnetic

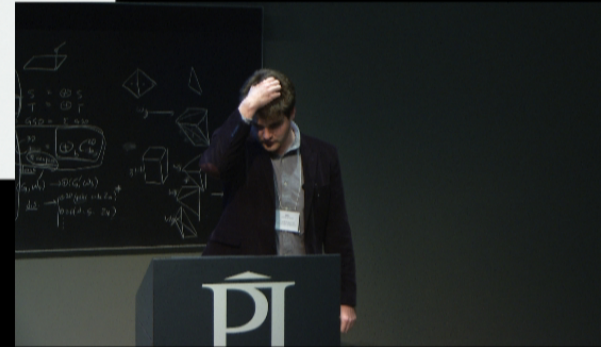
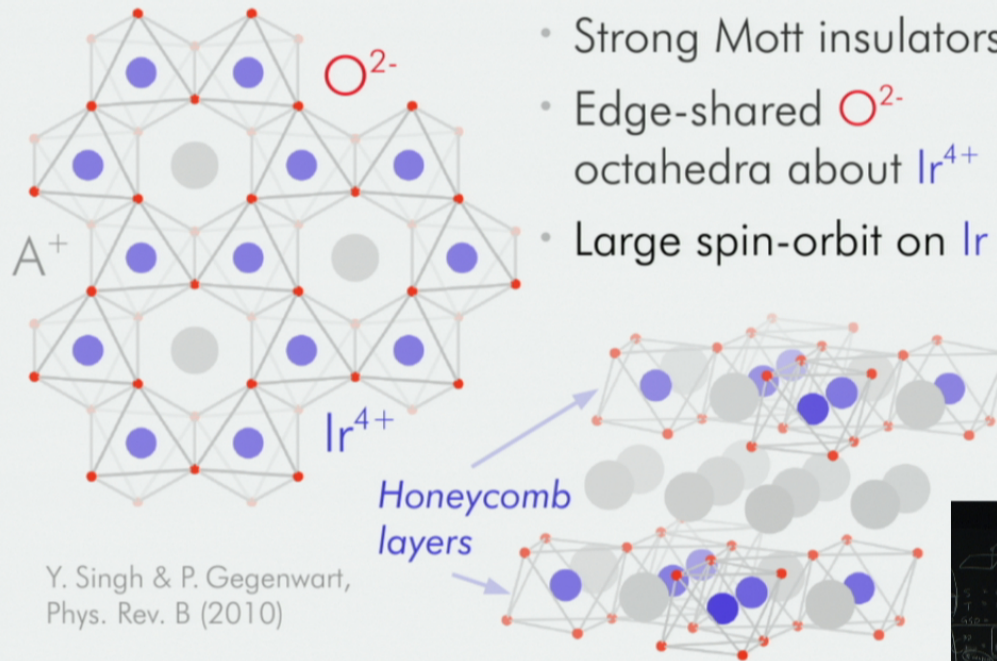
$$K \sim -\frac{8J_H}{3U^2} \left(\frac{t_{pd\pi}^2}{\Delta_{pd}} \right)^2$$

Hund's coupling

Candidate materials?

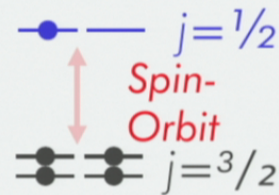
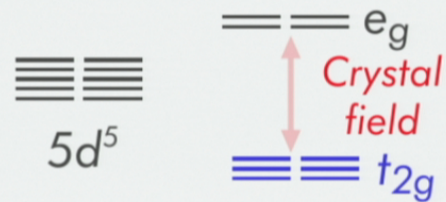
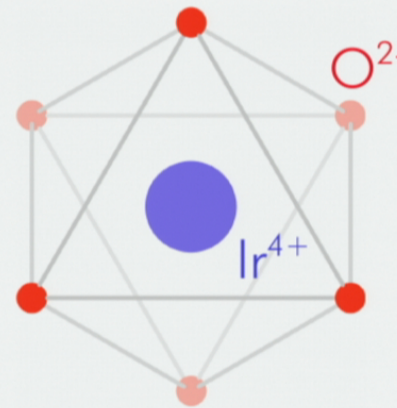
G. Jackeli & G. Khalliliuin, Phys. Rev. Lett. (2009)

Materials: Na_2IrO_3 & Li_2IrO_3

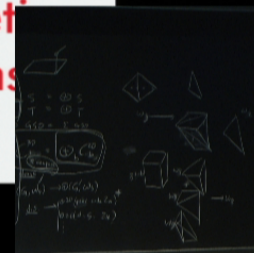


Atomic Physics

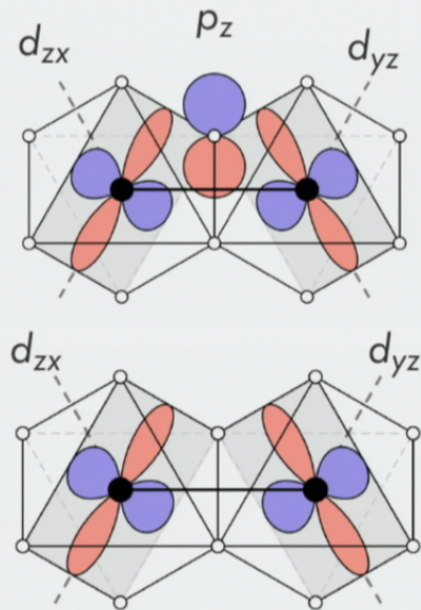
- Crystal field and spin-orbit give half-filled $j=1/2$ band
- Atomic interactions in t_{2g} include Hubbard U and Hund's coupling J_H



Kinetic terms



Inter-orbital hopping terms



- Focus on a **z** bond of the lattice
- Large 5d orbitals
- Inter-orbital **yz-zx** hopping from oxygen and dd

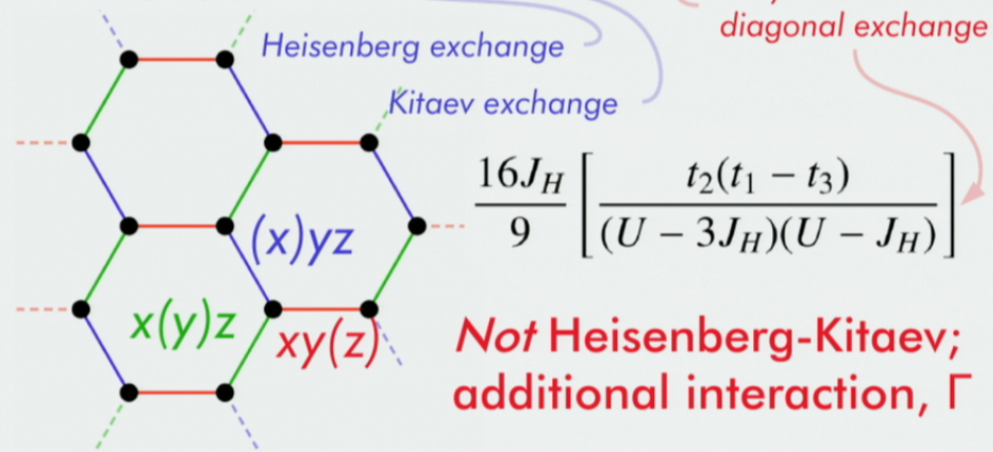
$$t_2 = \frac{1}{2} (t_{dd\pi} - t_{dd\delta}) + \frac{t_{pd\pi}^2}{\Delta_{pd}}$$



Heisenberg-Kitaev- Γ Model

- Strong coupling expansion $U, J_H \gg \lambda \gg t$

$$H = \sum_{\langle ij \rangle \in \alpha\beta(\gamma)} \left[J \vec{S}_i \cdot \vec{S}_j + K S_i^\gamma S_j^\gamma + \Gamma (S_i^\alpha S_j^\beta + S_i^\beta S_j^\alpha) \right]$$



HK Γ Model: cont.

- In previous work only the Heisenberg and Kitaev terms were derived – no Γ term

Problem #1: Zigzag hard to find in HK model – if oxygen mediated hopping dominates K has wrong sign

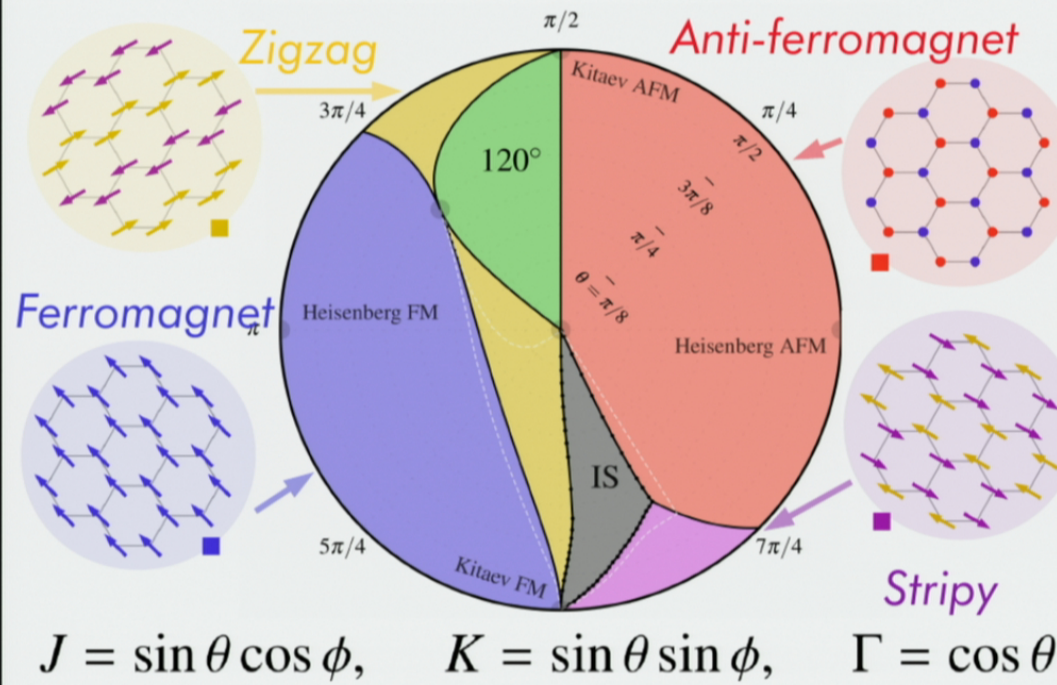
Problem #2: No incommensurate spiral

- Some proposed solutions: Strong e_g - t_{2g} contribution to K to change sign, further neighbour J_2 and J_3 , etc.

Chaloupka et al. Phys. Rev. Lett.(2010), (2013);
Kimchi & You, Phys. Rev. B (2011), etc

What happens
when is Γ finite?

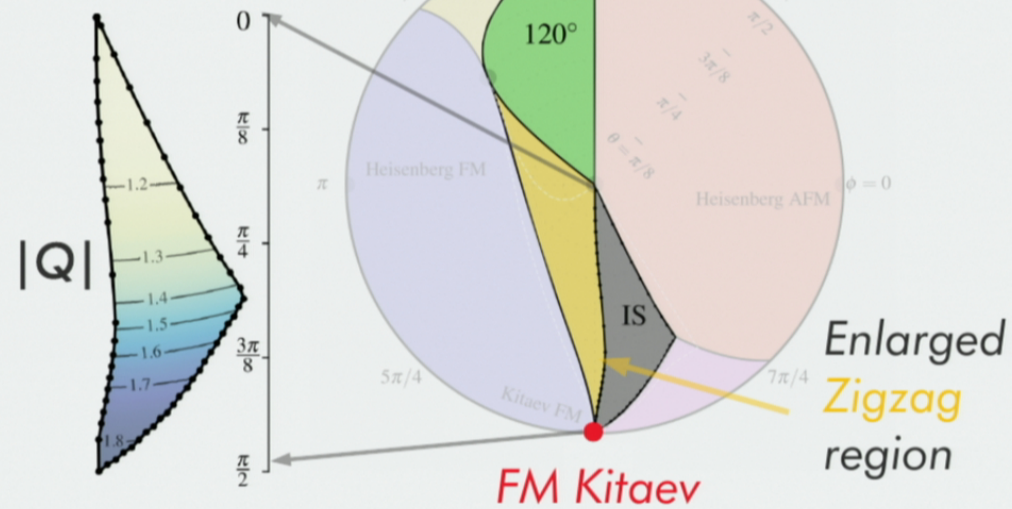
Classical Phase Diagram $\Gamma > 0$



New Phases

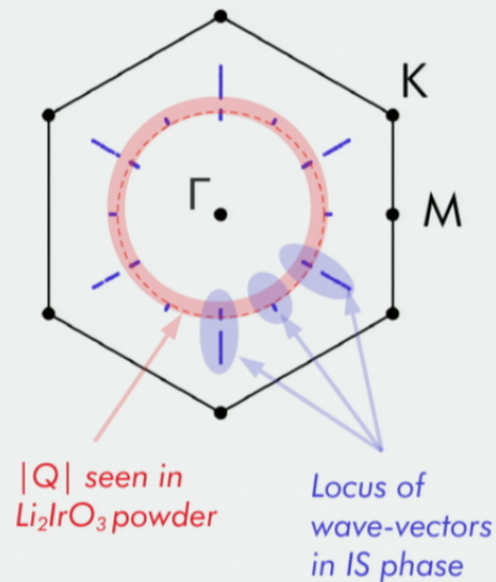
Incommensurate
spiral order

Three sublattice,
120° order



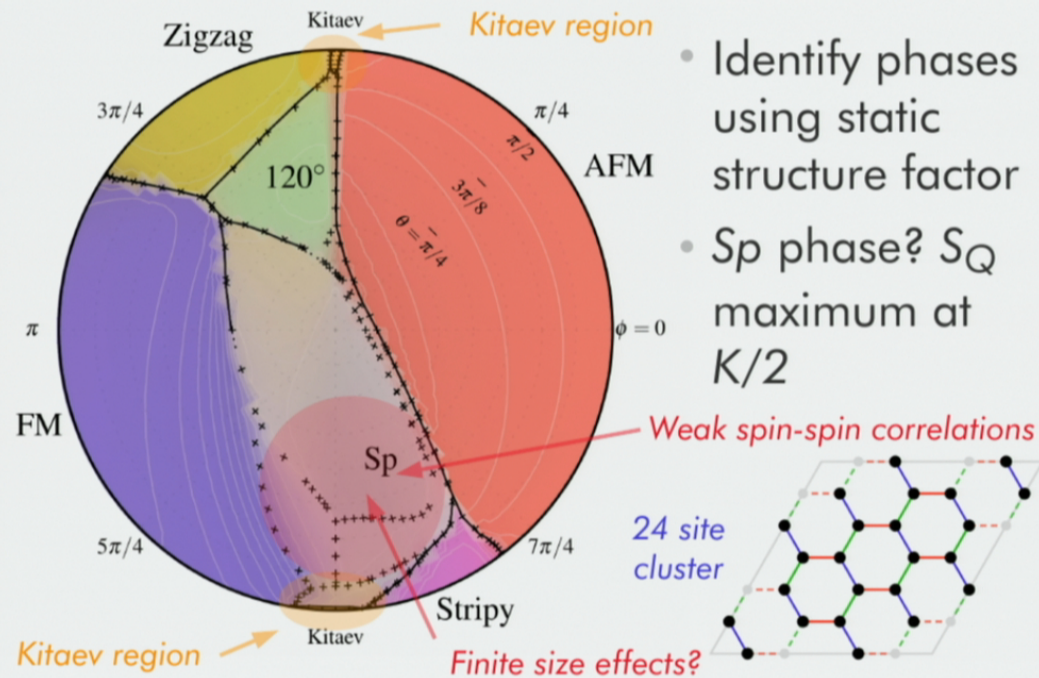
Incommensurate Spiral

- Appears near **FM** **Kitaev** limit
- Spiral wave-vector varies in phase
- Clusters with \sim fixed $|Q|$ and along Γ -K lines
- Near wave-vector reported in Li_2IrO_3



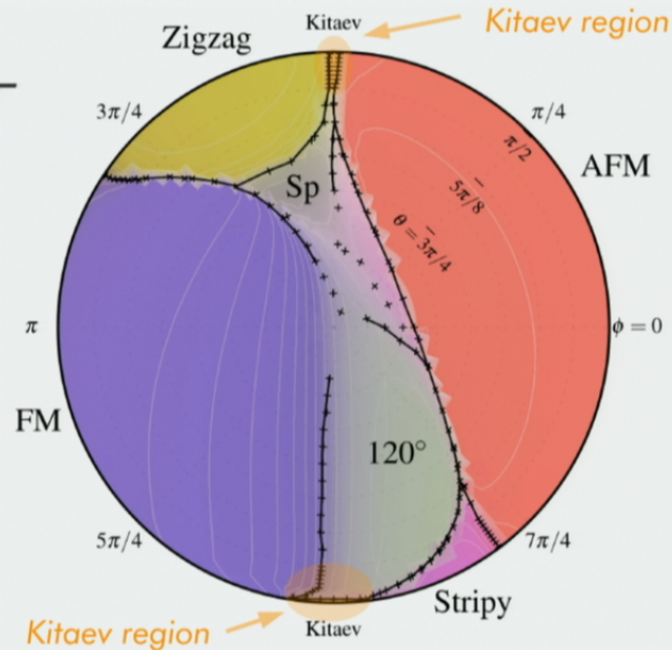
S.K. Choi, APS March Meeting Talk 2014

Exact Diagonalization: $\Gamma > 0$



Exact Diagonalization: $\Gamma < 0$


- Classical mapping Γ to $-\Gamma$ *not* valid
- Qualitatively similar to mapped $\Gamma > 0$ phase diagram
- Both $\Gamma > 0$ and $\Gamma < 0$ *consistent with classical results*



Conclusions

- Minimal $j=1/2$ spin model of edge-shared octahedra is

$$H = \sum_{\langle ij \rangle \in \alpha\beta(\gamma)} \left[J \vec{S}_i \cdot \vec{S}_j + K S_i^\gamma S_j^\gamma + \Gamma (S_i^\alpha S_j^\beta + S_i^\beta S_j^\alpha) \right]$$

Symmetric off-diagonal exchange 


- Finite Γ gives new phases; **120° order** and *incommensurate spiral* – relevant for Li_2IrO_3 ?
- New zigzag region** for $\Gamma > 0$ near the FM Kitaev limit – relevant for Na_2IrO_3 ?

Details in Phys. Rev. Lett. **112**, 077204 (2014)

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Symmetric off-diagonal exchange 

- Finite Γ gives **new** phases; **120° order** and *incommensurate spiral* – **relevant for Li₂IrO₃?**
- New zigzag region** for $\Gamma > 0$ near the FM Kitaev limit – **relevant for Na₂IrO₃?**

Details in Phys. Rev. Lett. **112**, 077204 (2014)