

Title: Measurements of Noise in Condensed Matter Systems Using Superconducting Qubits and Resonators

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Abstract: <span>Superconducting qubits based on Josephson junctions and resonators are presently leading candidates for the implementation of quantum computing. These systems couple strongly to their environment, which often makes preservation of coherence challenging. This strong coupling can be turned into an advantage: it enables the investigation of noise and loss at low temperatures. I will discuss two topics. The first topic is the use of superconducting flux qubits to measure magnetic flux noise. The second topic is the measurement of microwave loss in amorphous dielectric materials. Experiments with superconducting coherent systems can be used to extract new information on flux noise and dielectric loss, not accessible using other methods used in the past, providing useful input to theoretical developments.</span>



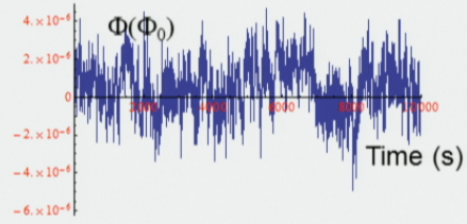
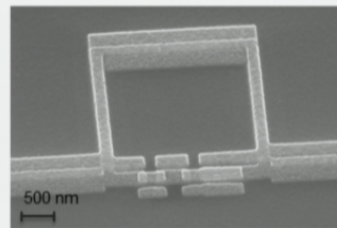
## Measurements of Noise in Condensed Matter Systems Using Superconducting Qubits and Resonators

*Adrian Lupascu*  
Institute for Quantum Computing, Department of Physics and Astronomy,  
University of Waterloo

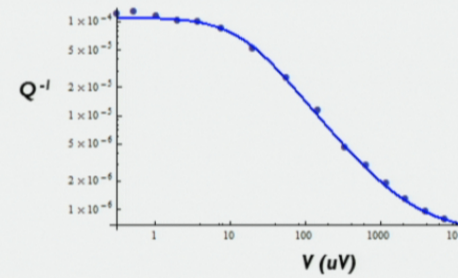
4 corners workshop, Waterloo, May 1<sup>st</sup>, 2014

# Outline

## Flux noise

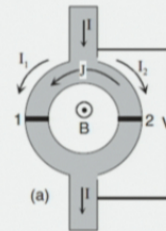


## Loss in amorphous dielectrics

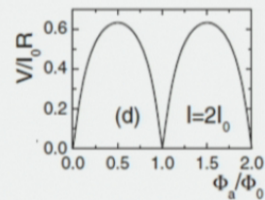


## Flux noise in SQUIDs

### ▶ DC-SQUIDS



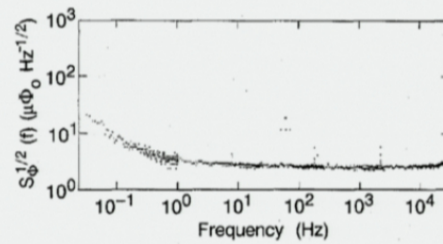
### ▶ Flux modulation



Clarke and Braginski, The squid handbook (2004)

## Flux noise in SQUIDs

- ▶ Intrinsic noise



Wellstood *et al.*,  
IEEE Trans Magn (1987)

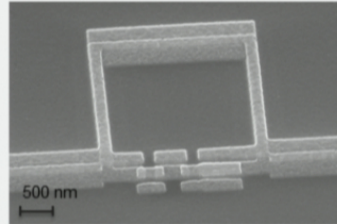
- ▶ Noise features

- ▶  $1/f^\alpha$  ( $\alpha \sim 1$ ), no low frequency cutoff
- ▶ “universal” magnitude (weak dependence of materials, size)
- ▶ local
- ▶ not due to vortices

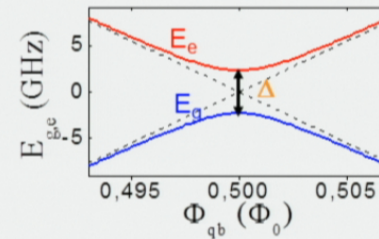
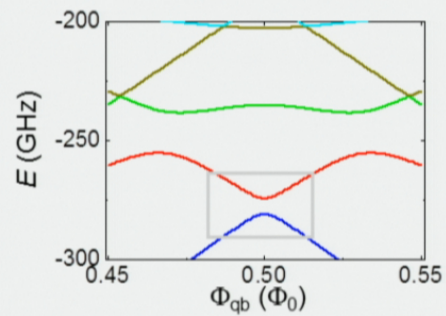
- ▶ Detrimental to magnetometry



## The flux qubit



Mooij et al., Science 285 1036 (1999)



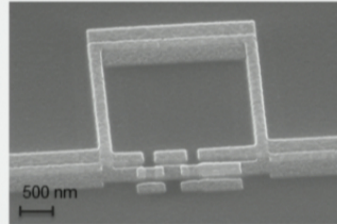
$$\hat{H} = \frac{h}{2} \left( 2I_p \left( \Phi_{qb} - \Phi_0/2 \right) \hat{\sigma}_z + \Delta \hat{\sigma}_x \right)$$

$I_p, \Delta$ : **design** parameters  
 $\Phi_{qb}$ : **control** parameter

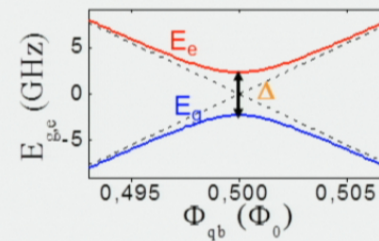
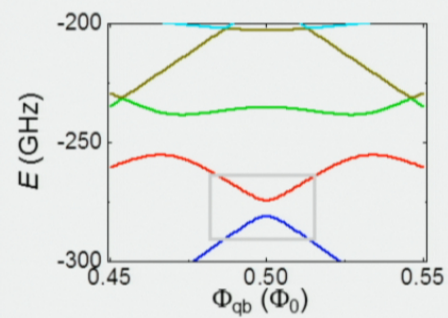
In basis:  $\{|\uparrow\rangle, |\downarrow\rangle\}$



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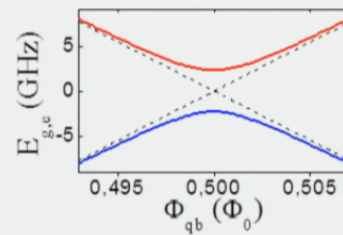
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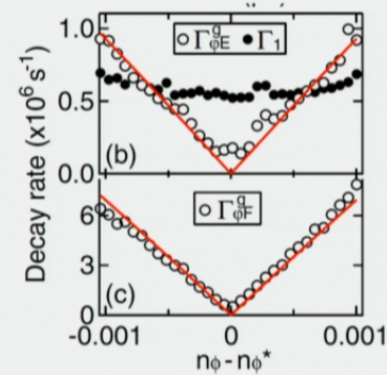


## The flux qubit – decoherence due to flux noise

- ▶ Sensitivity to flux fluctuations is minimum at the symmetry point



- ▶ Strong “pure dephasing” away from the symmetry point

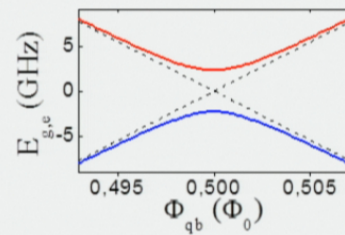


Yoshihara *et al.*, PRL **97**, 167001 (2006)

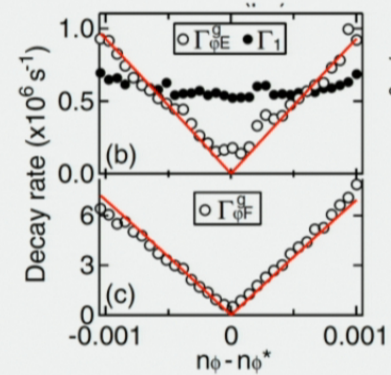


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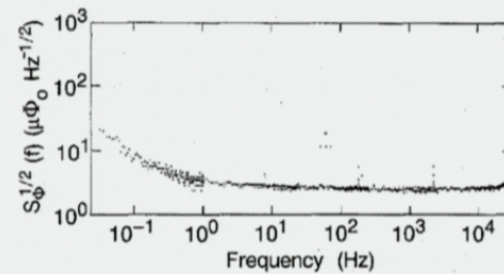
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Yoshihara *et al.*, PRL **97**, 167001 (2006)

## Measurements of flux noise using DC-SQUIDS

- ▶ Higher frequency limited by other sources of noise in SQUIDS, bandwidth



Wellstood *et al.*,  
IEEE Trans Magn (1987)

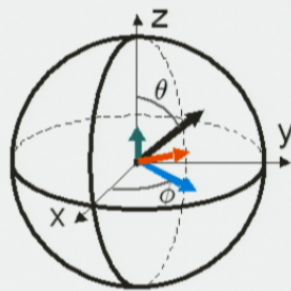


## Single-qubit control

- ▶ Microwave resonant driving

$$H = -\frac{\omega_{01}}{2}\sigma_z + \epsilon_0 \cos(\omega_d t + \phi)\sigma_x$$

- ▶ Dynamics in a rotating frame



$$|\psi(t)\rangle = \cos \frac{\theta(t)}{2} |0\rangle + \sin \frac{\theta(t)}{2} e^{i\phi(t)} |1\rangle$$

Dynamics in a rotating frame

- **Control**  $\epsilon(t) = \epsilon_0 \cos(\omega_d t + \phi)$
  - **Detuning**  $\omega_d - \omega_{01}$
- precession around **effective field** gives full control

- ▶ High fidelity control readily achievable (fast gates)

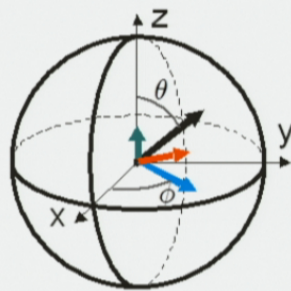


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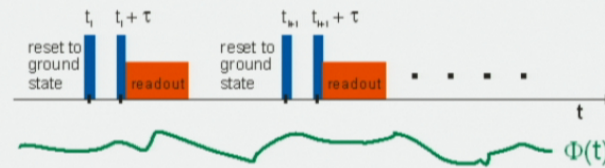
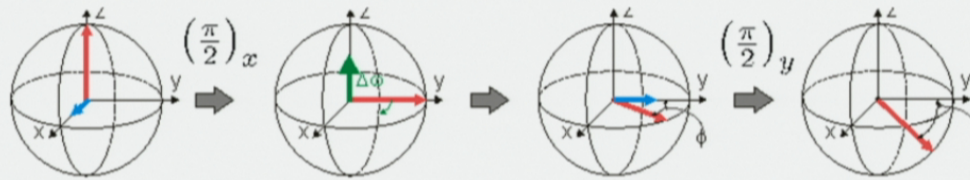
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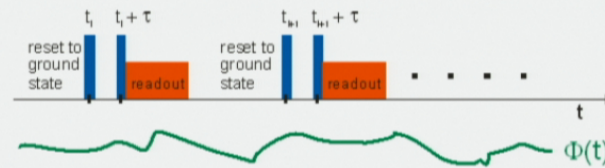
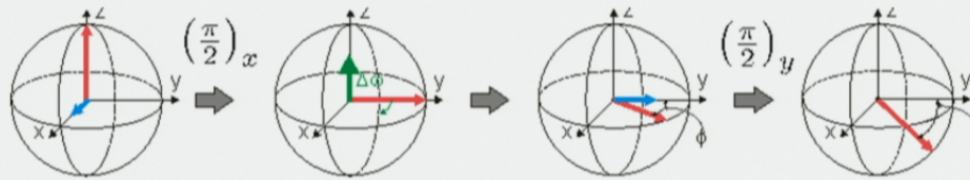
## Measurement of magnetic flux noise based on Ramsey interferometry



$$\phi_i = \int_{t_i}^{t_i + \tau} dt' \frac{\partial \omega_{01}}{\partial \Phi} \Phi(t')$$

A running average is needed (to overcome noise due to measurement)

## Measurement of magnetic flux noise based on Ramsey interferometry

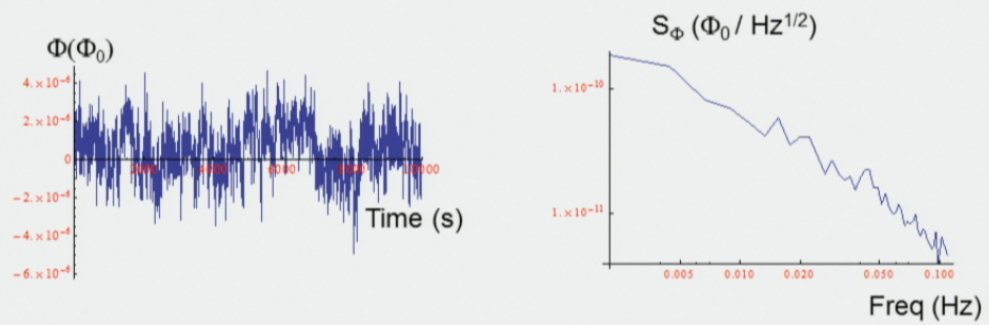


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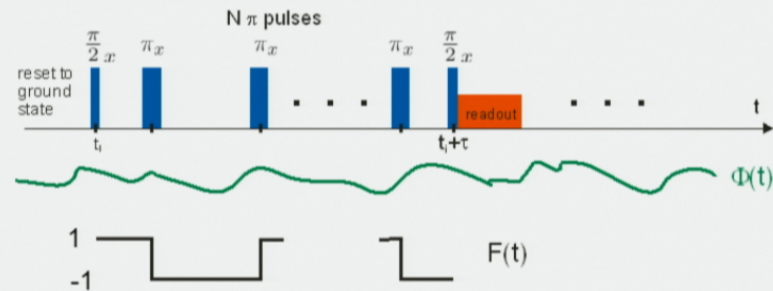
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## Measurement of magnetic flux based on Ramsey interferometry



## Measurement of magnetic flux noise based on pulse sequences



$$\phi_i = \int_{t_i}^{t_i + \tau} dt' \frac{\partial \omega_{01}}{\partial \Phi} F(t') \Phi(t')$$

An average over many repetitions gives  $\langle e^{i\phi(\tau)} \rangle$

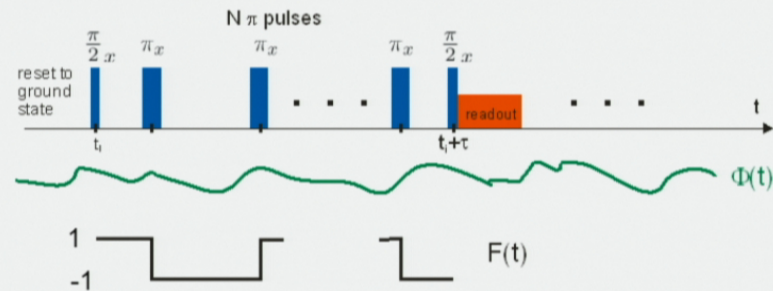
For Gaussian noise

$$\begin{aligned} \langle \exp(i\phi(\tau)) \rangle &= \\ &= \exp \left[ -\frac{1}{2} \left( \frac{\partial \omega_{01}}{\partial \Phi} \right)^2 \int_0^\tau dt_1 \int_0^\tau dt_2 \langle \delta \Phi(t_1) \delta \Phi(t_2) \rangle F(t_1) F(t_2) \right] \end{aligned}$$





## Measurement of magnetic flux noise based on pulse sequences



$$\phi_i = \int_{t_i}^{t_i + \tau} dt' \frac{\partial \omega_{01}}{\partial \Phi} F(t') \Phi(t')$$

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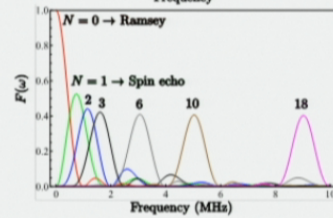
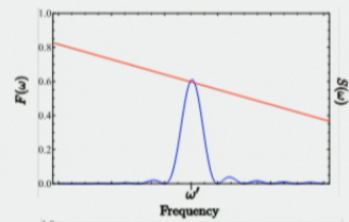
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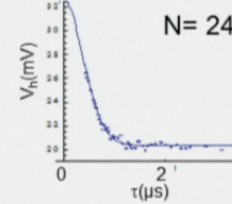
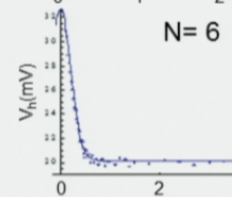
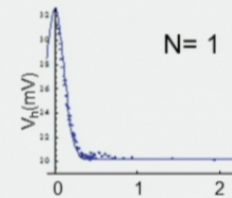


## Measurement of magnetic flux noise based on pulse sequences

$$\langle \exp(i\phi(\tau)) \rangle = \exp \left[ - \int_0^\infty d\omega S(\omega) \underbrace{F_{\tau, N}(\omega)}_{\text{filter function}} \right]$$

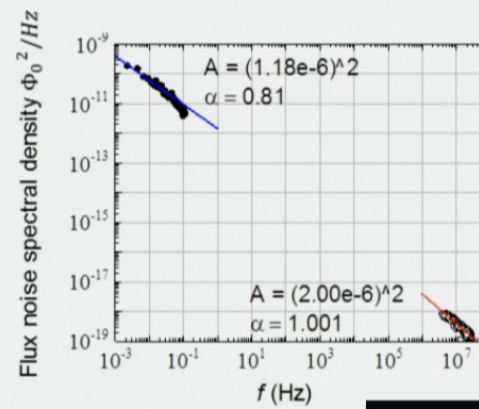
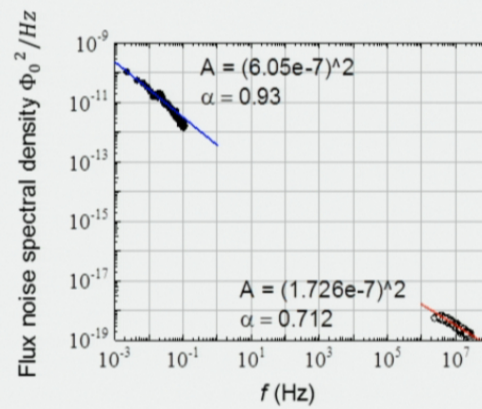


J. Bylander et al., Nat. Phys. 7, 565 (2011)



## Low and high frequency flux noise

Temperature: 40 mK



Orgiazzi *et al.*, in preparation



## Models for 1/f noise

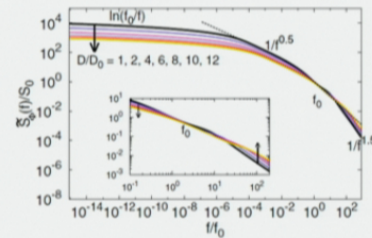
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- ▶ Main ingredients
  - ▶ Electron spins, at surfaces/interfaces
  - ▶ Dynamics of interacting spins or trapped states with random spin orientation
- ▶ Spins at surfaces/interfaces
  - ▶ Koch et al (2007) – electrons traps
  - ▶ De Sousa (2007) – dangling bonds
  - ▶ Choi et al (2009) – metal induced gap states

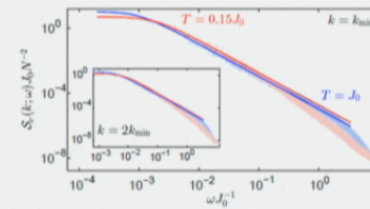


## Predictions for interacting spin models

Faoro and Ioffe, 2008  
Lanting et al, 2014



Atalaya et al, 2014



Some open questions

- Disagreement with the wide (>10 orders of magnitude)  $1/f$  noise behaviour
- No predictions for the temperature dependence



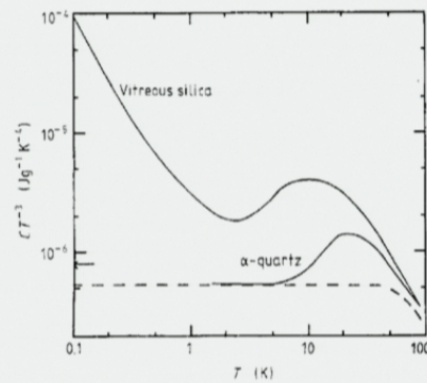
## Prospects

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- ▶ Measurements based on qubits give access to wider spectral information, better sensitivity; input to theory
  - ▶ Systematic experiments: verify scaling, dependence on materials
  - ▶ Reduction of magnetic field noise will have a major impact on quantum information and magnetic field detection
-

## Amorphous materials at low temperatures

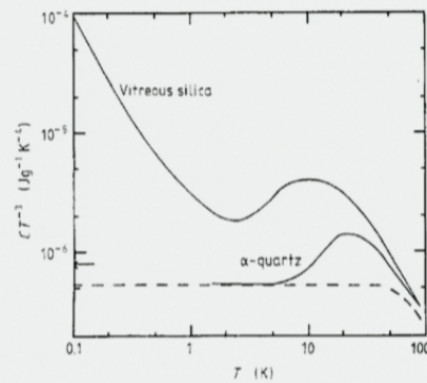
- ▶ Anomalies in specific heat and heat conductivity



Phillips, Rep. Prog. Phys. 50 1657 (1987)

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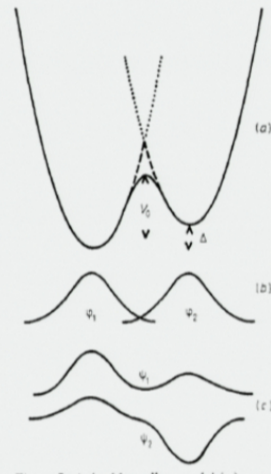


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## TTLS model

### ▶ Tunneling two level system (TTLS) model



Two parameters:

- $\Delta$  – asymmetry of the potential well
- $\Delta_0$  - tunneling

An electric field or strain can change the asymmetry  $\Delta$ , providing a mechanism for inducing transitions.

Distribution:

$$f(\Delta, \Delta_0) = \frac{P}{\Delta_0}$$

Phillips, Rep. Prog. Phys. 50 1657 (1987)



## Dielectric loss

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- TLS model predictions

- Temperature dependence:  $Q_i^{-1}(\omega, T) = Q_0^{-1} \tanh(\hbar\omega/k_B T)$

- Electric field dependence:  $Q^{-1}(E, \omega, T) = \frac{Q_i^{-1}(\omega, T)}{\sqrt{1 + (E/E_c)^2}}$

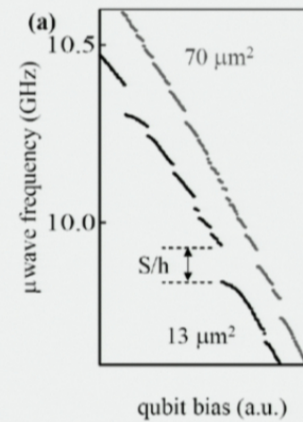
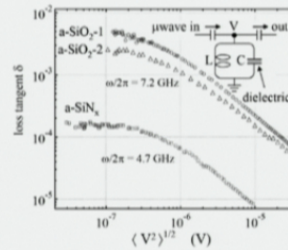
- Key points

- Energy of the field absorbed by TLSs and emitted via phonons
    - Large power leads to saturation – loss decreases
    - Increasing temperature – excited TLSs, less likely to absorb the energy from the field



## Dielectric loss in superconducting quantum devices

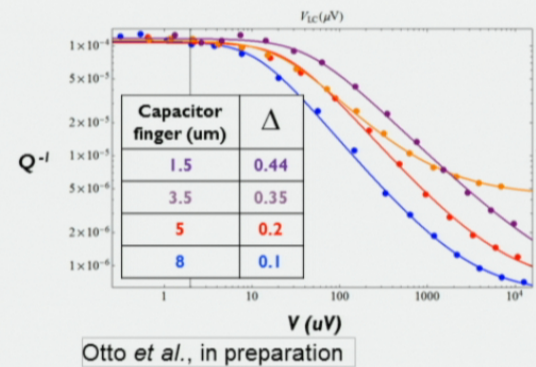
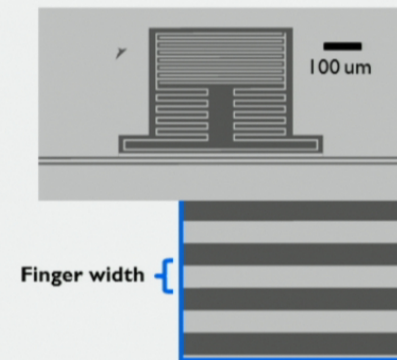
- ▶ Resonators: limits quality factor (at low powers – the important regime), leads to spectral diffusion
- ▶ Qubits: energy relaxation



Martinis et al, PRL 95, 210503 (2005)

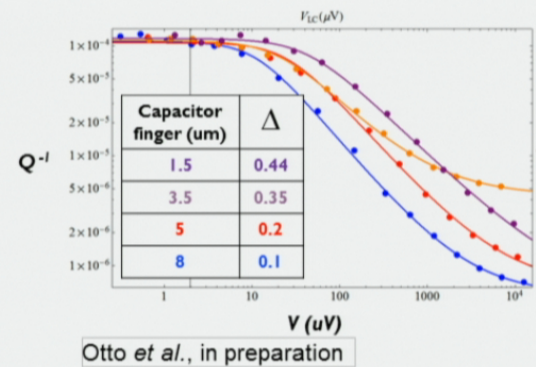
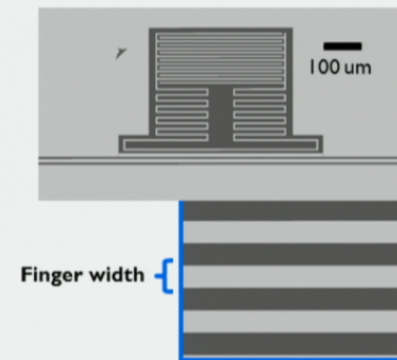
## Power dependence of loss

- ▶ TTLS prediction  $Q^{-1} = \frac{Q_0^{-1}}{\sqrt{1 + (\frac{E}{E_c})^2}}$
- ▶ Experimental results  $Q^{-1} = \frac{Q_0^{-1}}{\sqrt{1 + (\frac{E}{E_c})^{2-\Delta}}}$
- ▶ Systematic variation with geometry



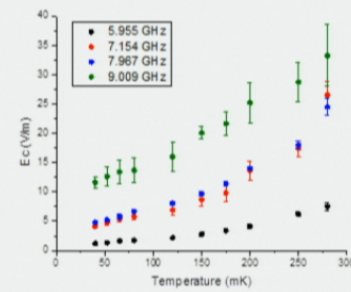
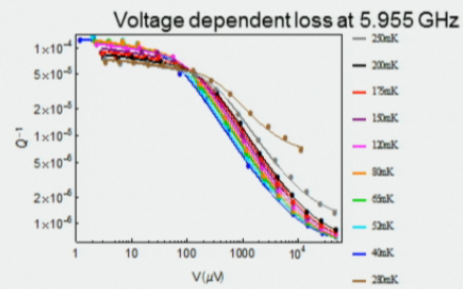
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## Critical field – temperature dependence

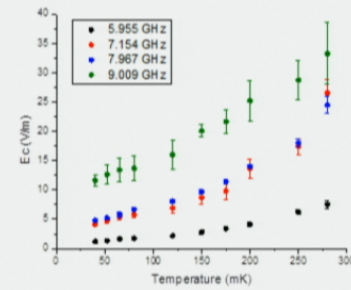
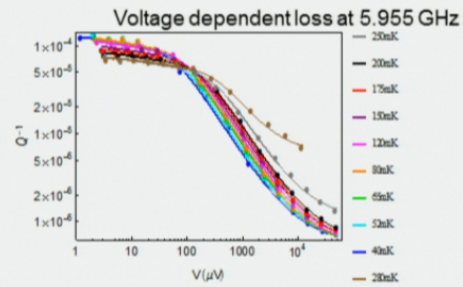
### ▶ 100 nm $\text{Al}_2\text{O}_3$



Otto *et al.*, in preparation

## Critical field – temperature dependence

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Otto *et al.*, in preparation

## Critical field – temperature dependence

- ▶ The critical field is a measure of coherence

$$E_c \sim \Gamma_1 \Gamma_2$$

$\Gamma_1/\Gamma_2$ : TLS energy relaxation / dephasing rates

- ▶ For TLS in the quantum regime ( $\hbar\omega \gg k_B T$ ),  $E_c$  is expected to be temperature independent
- ▶ Recent theory work (Faoro and Ioffe, 2014) predicts a temperature dependence in  $\Gamma_2$  due to TLS-TLS interactions
- ▶ Interactions may induce a temperature dependence in  $\Gamma_1$





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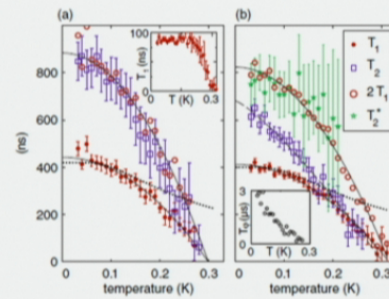
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## Measurements of TLS decoherence using qubits

### ▶ Measurements in thin AlOx layers



Lisenfeld et al, PRL 105, 230504 (2010).

### ▶ Temperature dependence is different of what we find (are measurements on individual TLSs biased?)

## Amorphous materials - prospects

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- ▶ Criticism of TTLS model
    - ▶ Microscopic model
    - ▶ Universality of loss constants
    - ▶ Alternate theories (Vural and Leggett, 2011)
  - ▶ Critical field measurements are important in further understanding the physics of amorphous materials
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## Acknowledgement

- ▶ SQD group
  - ▶ Jean-Luc Orgiazzi
  - ▶ Chunqing Deng
  - ▶ Marty Otto
  - ▶ Ali Yurtalan
  - ▶ Feiruo Shen
  - ▶ Nicolas David Gonzalez
  - ▶ Pol Forn Diaz



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