

Title: Black Holes- the Harmonic Oscillators of the 21st Century

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Abstract: In the twentieth century, many problems across all of physics were solved by perturbative methods which reduced them to harmonic oscillators. Black holes are poised to play a similar role for the problems of twenty-first century physics. They are at once the simplest and most complex objects in the physical universe. They are maximally complex in that the number of possible microstates, or entropy, of a black hole is believed to saturate a universal bound. They are maximally simple in that, according to Einstein's theory, they are featureless holes in space characterized only by their mass, charge and angular momentum. This dual relation between simplicity and complexity, as expressed in black holes, has recently been successfully applied to problems in a disparate variety of physical systems. I will give an introduction to the subject intended for a general audience.

BLACK HOLES:

the Harmonic Oscillators
of the 21st Century

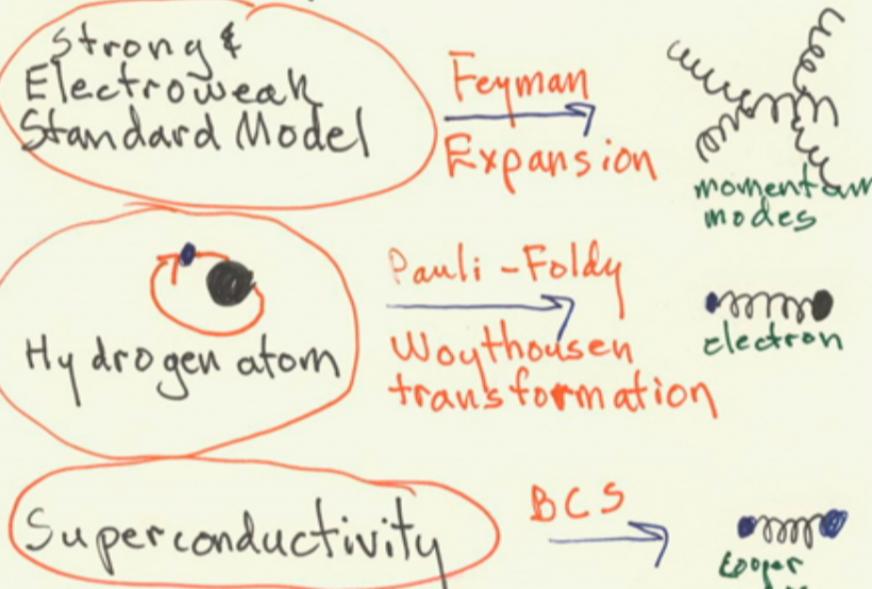
Andy Strominger
Harvard University

PERIMETER INSTITUTE COLLOQUIUM, MARCH 2014

a wide array of problems across physics were solved by mapping them to the harmonic oscillator:



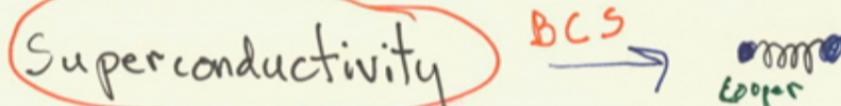
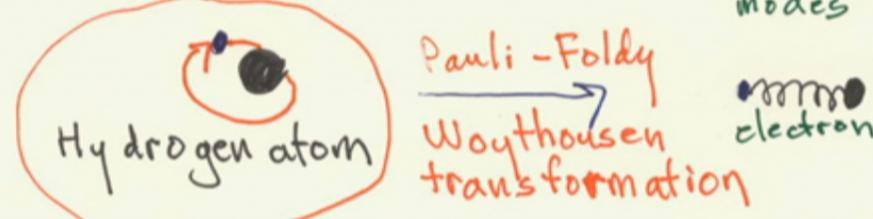
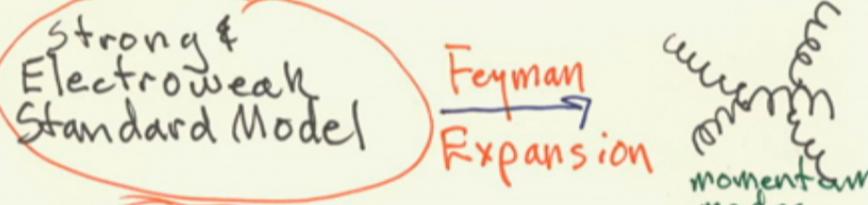
For example:



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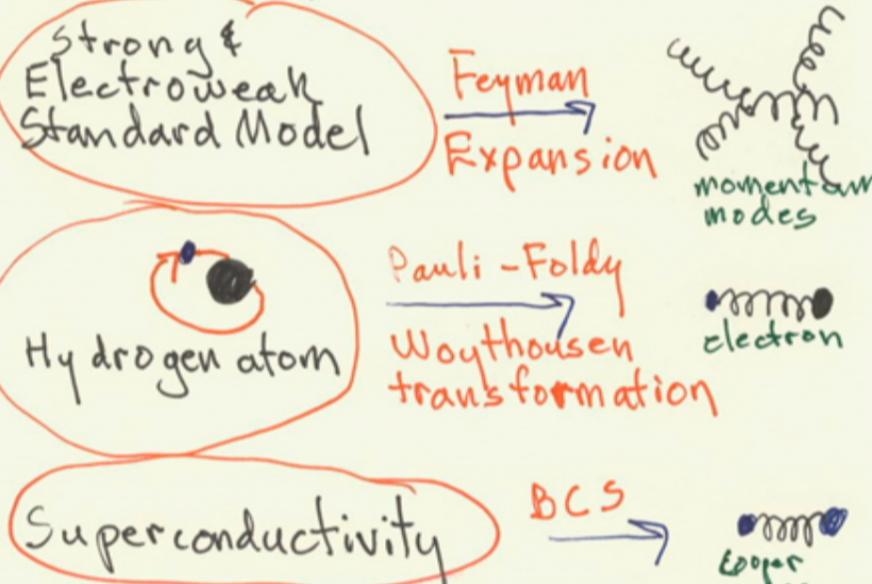
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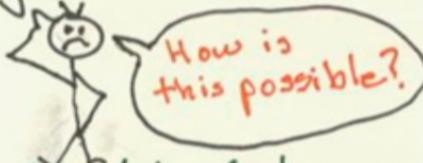
a wide array of problems across physics were solved by mapping them to the harmonic oscillator:



For example:



They are at once both the ^{simplest}
and most ^{complex} objects in the
physical universe.



SIMPLE



According to Einstein-Schwarzchild.. they are empty, featureless holes in space characterized only by M, Q and J.

COMPLEX



According to Bekenstein-Hawking... the number of possible microstates $e^{S_{BH}}$ saturates a universal bound $S_{BH} = \frac{1}{4} \text{Area}(\text{Horizon})$

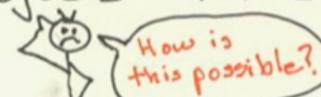
Progress over the last decade in the dual quantum relation ^{understanding} simplicity ^{complexity} has been successfully.

Black holes are poised to play a similar role in the 21st century. They are at once both the **simplest** and most **complex** objects in the physical universe.

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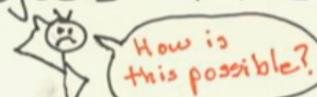
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PROGRESS IN PHYSICS

3

20th CENTURY



21st CENTURY



OUTLINE

- I. Brief Bio of the Black Hole 1915- [redacted], and What We Have Learned
- II. Applications
- III. Role of string theory
- IV. Current status & future prospects

Birth of the Black Hole

Nov 25, 1915

Einstein discovers the Einstein equation. Believes exact solution will never be found.

★ Jan 16, 1916

Exact solution announced by Einstein to Prussian academy. "It is always pleasant to have an exact solution in simple form at your disposal
— Karl Schwarzschild

May 11 1916

Schwarzschild dies. ■ Russian front

$$\begin{aligned} ds^2 = & - \left(1 - \frac{2GM}{r}\right) dt^2 \\ & + \frac{dr^2}{\left(1 - \frac{2GM}{r}\right)} \\ & + d\theta^2 + \sin^2 \theta d\phi^2 \end{aligned}$$

Nobody knows what it means!

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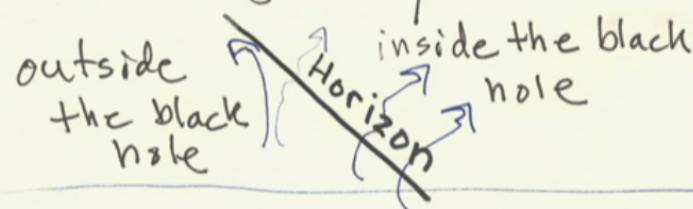
Childhood (confused)

1930's

Chandrasekhar, Oppenheimer
Snyder: stars with mass
 $M > 3M_{\odot}$ collapse into black
holes. Einstein disagrees!

1950's

Finkelstein, Kruskal.
Horizon $\stackrel{\text{surface of black hole}}{=}$ $r = 2GM$
is a one-way membrane
not a singularity



1963

Kerr discovers rotating
Kerr solution

1960s

Penrose, Hawking, Carter
singularities, can say structure

1967 Wheeler coins "BLACK HOLE"

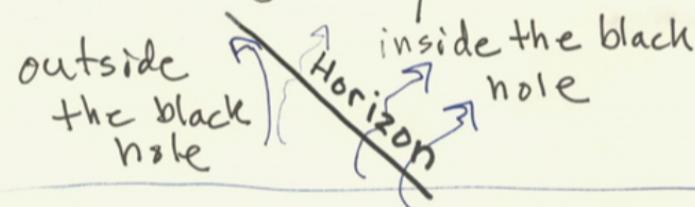
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FIRST LAW

Thermodynamics:

$$TdS = dE - \Phi dQ - \Sigma dJ + \dots$$

Classical Black Hole Dynamics:

$$\frac{K}{8\pi}dA = dE - \Phi dQ - \Sigma dJ + \dots$$

$K \equiv$ surface gravity
 $A \equiv$ area of horizon

The first BH law is related to the "no-hair" theorem: a static BH is characterized by conserved quantities E , Q and J .

Analogy:

$$S \leftrightarrow A$$

$$T \leftrightarrow K$$

SECOND LAW

Thermodynamics:

$$\Delta S \geq 0$$

Classical Black Hole Dynamics:

$$\Delta A \geq 0$$

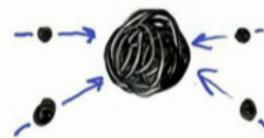
Classical black holes only
grow in size.

Analogy:

$$S \leftrightarrow A$$

Penrose Christodoulou Hawking Bardeen
Carter Bekenstein ...

The Area only increases because matter can go into, but not out of, a black hole: ¹⁰



As Boltzmann explained, Entropy only increases because it measures molecular disorder - hard to prove



but easy to understand. The surprise is that these are in disguise the same phenomena!

Hawking '74 completes the circle: Black holes radiate blackbody radiation at

$$T_{BH} = \frac{K}{2\pi}$$

Observed
in the
sky?

Planck Units

$\Rightarrow S_{BH} = \frac{1}{4} \text{Area}$ Bekenstein-Hawking Entropy

\Rightarrow Unified Laws of BHs + Thermodynamics

Generalized 1st law

$$T(dS_{out} + dS_{BH}) = dE - \cancel{\oint} dQ - \cancel{\int} dJ + \dots$$

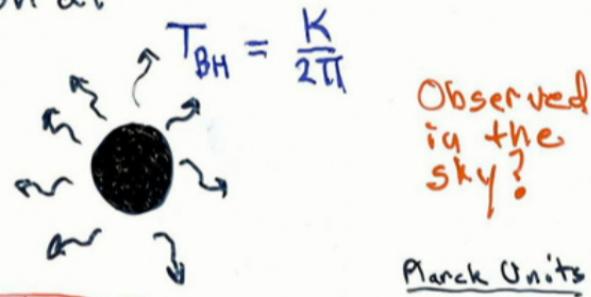
Generalized 2nd law

$$\Delta S_{out} + \Delta S_{BH} \geq 0$$

S_{out} ≡ entropy outside
the black hole

Troubled Quantum Adolescence

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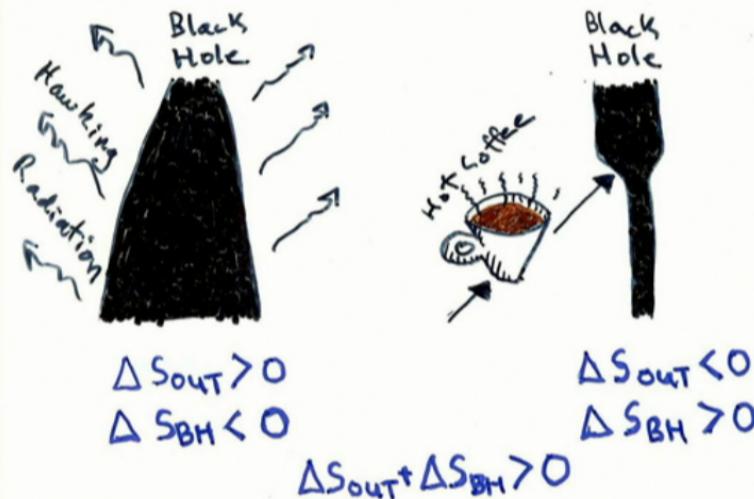
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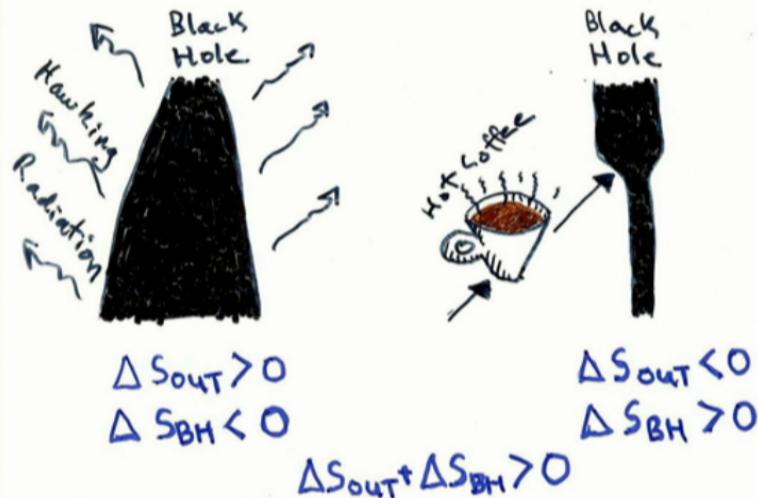
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A series of ingenious gedanken experiments has failed to find violations of the generalized 2nd law $\Delta S_{\text{out}} + \Delta S_{\text{BH}} \geq 0$.

$S_{\text{BH}} \sim$ ignorance about black hole interior?
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We seek a single, unified derivation of the unified laws of BH thermodynamics: to microscopically derive those laws-as Boltzmann did for ordinary thermodynamics by counting BH microstates. We need to show

$$S_{BH} = \frac{\text{Area}}{4 G_N \hbar} = \log [\# \text{of BH states}]$$
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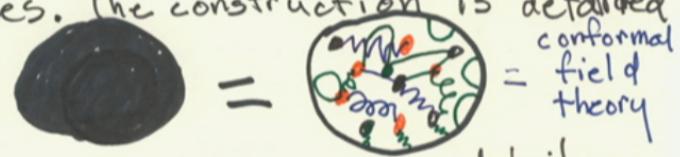
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20 years later... .

14

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String theory is used by A.S. and Vafa to microscopically compute S_{BH} for certain unphysical black holes. Perfect agreement is found in many cases. The construction is detailed



and appears to use many details of string theory. It is the first stringy example of what is now known as the AdS/CFT correspondence. Much light is shed on string theory.

~~TOPIC FOR A DIFFERENT LECTURE~~

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It is shown that string theory was not needed! The construction is boiled down to its key ingredients and found to apply to any consistent quantum gravity containing the black hole solutions.

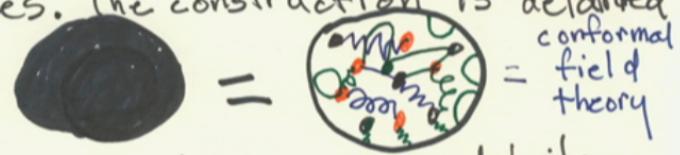
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The statistical mechanics of continuous fluids ^{gases} has an ultraviolet catastrophe. Boltzmann needed a consistent ultraviolet cutoff - the theory of molecules to derive the universal laws of thermodynamics from stat mech. He did not need the exact periodic table.

Quantum gravity also has an ultraviolet catastrophe - non renormalizability. (Pauli) A consistent ultraviolet cutoff of some kind is needed to derive the universal laws of black hole thermodynamics. But just as Boltzmann did not need the periodic table, we should not need all the details of string theory.

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10 years later

2008

we have obtained a statistical understanding of the thermodynamic behavior of special black holes seen in the sky without using or assuming string theory - but drawing lessons from our experience. Guica, Hartman, Song & Taylor These special black holes are called extreme Kerr the horizon rotates at (nearly) the speed of light.

An extreme 4D

Kerr black hole
has angular momentum
 $J = GM^2$,
Hawking temperature
 $T_H = 0$,
and Bekenstein-Hawking
entropy

$$S_{BH} = \frac{2\pi J}{\hbar} .$$

GRS 1915+105 has

$$M \approx 14 M_\odot$$

$$\frac{J}{GM^2} > 0.98$$

McClintock, Shafee, Narayan,
Remillard, Davis & Li (2008)
Recently reported:

Seyfert 1.2 galaxy MCG-6-30-15 has million solar mass BH
with $(J/GM^2) > 0.989$!!! Brenneman & Reynolds

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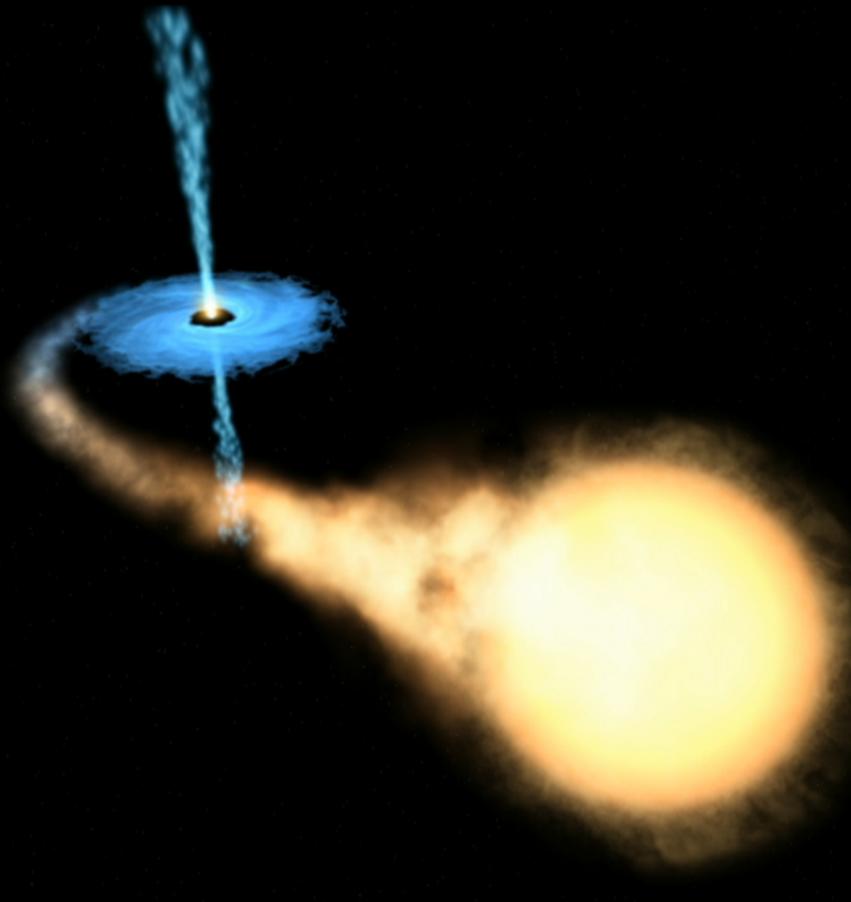
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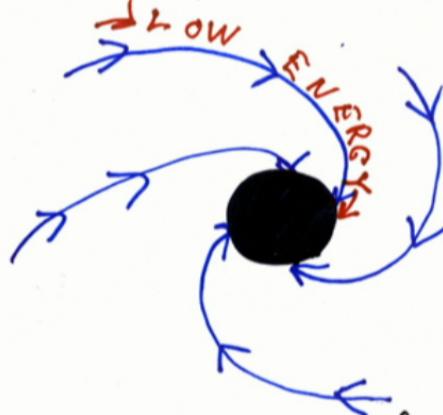


The near-horizon region
of extreme Kerr¹⁹



all excitations must move
counter-clockwise at the
speed of light!

In this very-near horizon
region, quantum gravitational



dynamics simplify dramatically
much as is the case for e.g.
dynamics of Cooper pairs in
a superconductor or quantum
Hall edge states at low
energies. Critical behavior
& powerful new symmetries—
offspring of diffeomorphisms—
arise in the limit.

The fixed point at the near-horizon limit is a 1+1 dimensional conformal field theory with a $(\phi, +)$ Virasoro algebra

$$[L_m, L_n] = (m-n)L_{m+n} + \frac{c}{12}(m^3-m)\delta_{m+n}$$

and central charge

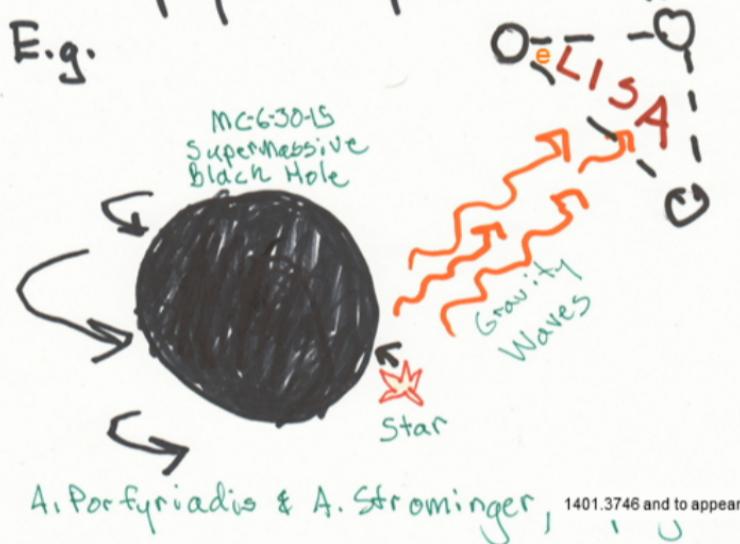
$$c = \frac{12J}{\hbar}$$

at temperature $T = \frac{1}{2\pi l}$.

These facts follow simply from a careful analysis of the properties of general coordinate transformations very near the horizon.

We hope to use this
newly-discovered conformal
symmetry to explain, organize
or even predict some
astrophysical phenomena.

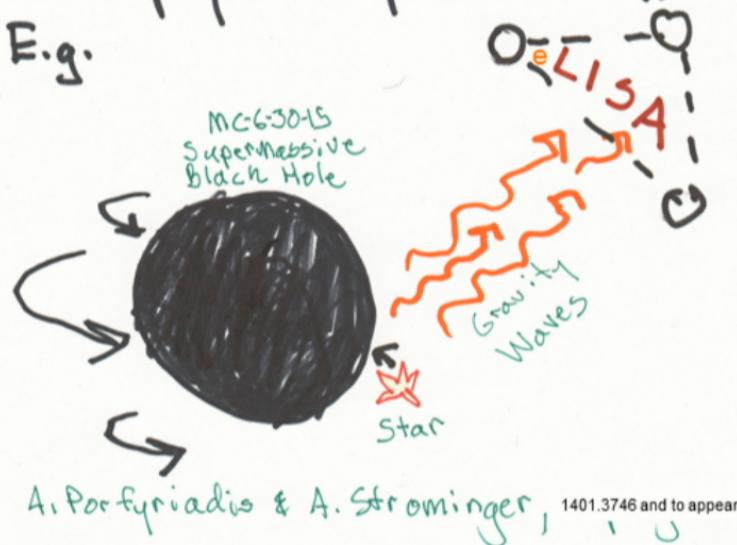
E.g.



A. Portyriadis & A. Strominger, 1401.3746 and to appear

many systems to consider, much
data .!.

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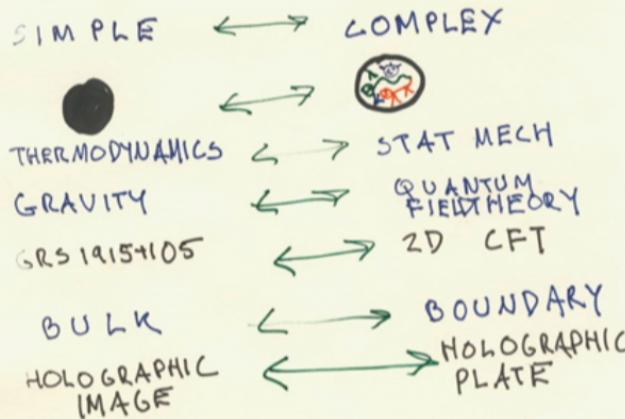
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many systems to consider, much
data...!

This is known as a

HOLOGRAPHIC DUALITY

SUMMARY



These dualities, whose quintessential realization is the macro/micro description of blackholes, are ubiquitous. They are both conceptually deep and computationally effective. Our current understanding is very limited, yet there are already many applications...
* Simplifications of this talk may be misleading!

Nuclear Physics

Long-lived states in the QCD plasma produced at the Relativistic Heavy Ion Collider

are black holes!

SIMPLE ↔ COMPLEX
BLACK HOLES ↔ QCD PLASMA

Kovtun, Son, Starinets...
Yaffe, Pollicastro...
de Wolfe, Gubser, Losen, Teaney



Surprise appearance of the black hole!

Algebraic Geometry

The Gromov-Witten invariants, which count holomorphic genus g curves in a Calabi-Yau space,



are equivalent to the

Donaldson-Thomas invariants, which count gauge field configurations. Ooguri, As Vafa.



This equivalence can not be seen by standard algebraic geometric methods! Many other pure math examples... wall crossing Moore Dench Kostovitch Stoibelman ...

High T_c Superconductivity

The quantum critical behavior of certain high- T_c cuprates has been mapped to the near-horizon of a black hole and then solved in a suitable approximation. This postdicted the anomalous Nernst effect, and has made further predictions awaiting experimental verification.

Mueller Hartnoll Kortun Herzog Son

HEY!
SURPRISE!

Graphene

The magnetohydrodynamic electron plasma has been mapped to a black hole and a cyclotron resonance predicted.

Sachdev Kortun Hartnoll Mueller



FLUID MECHANICS

It has been clear since the 70's that the black hole horizon closely resembles a fluid

Damour
Price
Thorne



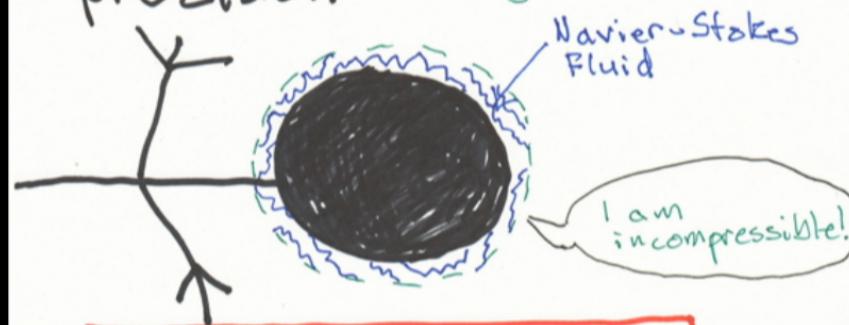
Navier Stokes ? = Einstein

Recently, once again using lessons learned from string theory, good progress has been made on this problem

Battacharya Minwalla Wadia
Hoogenboom Mandal Sharma Hubeny
Rangamani....

Recently this relation
has been elevated to
full mathematical
precision

Bredberg Keeler Lysouz AS



$$\text{Einstein } G_{ab} = 0$$

$$\text{Navier } \nabla^i v_i + \nu \times \partial_n v_i - \partial^i v_i = \partial^i p$$

and Kolmogorov exponent computed
with numerical GR!!! Adams Chester
Liu

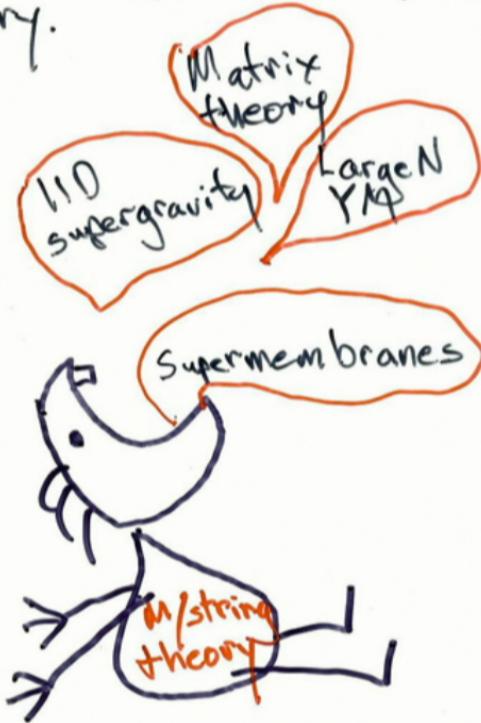
COSMIC CENSORSHIP \Leftrightarrow GLOBAL EXISTENCE
???. \Leftrightarrow TURBULENCE

There are more examples of surprise black hole appearances, and undoubtedly many more to come.  Before concluding, I will say a few words on the current status and ^{fundamental} role of string theory, about which there has been much public confusion.

String Theory

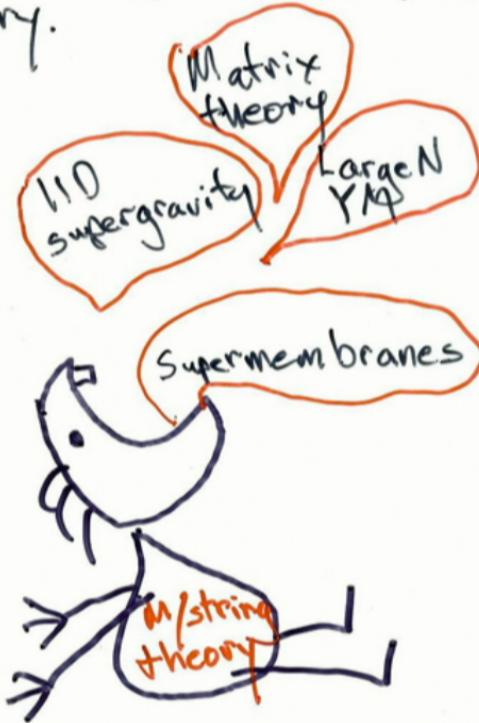
- Was discovered forty years ago as a highly nontrivial perturbative solution to the problem of reconciling quantum mechanics and general relativity. Later it was understood to also include matter and gauge interactions and became a promising candidate for a unified theory of all the forces and particles of nature. Over the decades it has grown into a large and highly cohesive web incorporating many ideas from disparate investigations.

In the last decade we have learned that strings are but one of many equivalent "dual" descriptions of a much larger structure still called M or string theory.



M/string theory has no competitors because it eats them all up.

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FLOW CHART OF VIEWS ON STRING THEORY

29

STRING THEORY
IS EVERYTHING

make prediction
testable
with current
experiments

Anthropic
Landscape

or

STRING THEORY
IS NOTHING



or

STRING THEORY
IS SOMETHING

it solves some
problems but not
others. more
yet to understand,
DON'T HAVE TO GO HOME! ONTO NEXT
PAGE!

WHEEE!!!



STRING THEORY REPORT CARD

Issued by 33
A. Strominger
Spring Semester
2014

	A	B	C	D	F
Not being ruled out as theory of nature	✓				
Unambiguous testable prediction					✓
Potential for LHC signal				✓	
Solving black hole puzzles		✓			
Applications/inspirations for pure math	✓				
Applications/inspirations other areas of physics		✓			
Unification	✓				
Uniqueness			✓		
Solving the cosmological constant problem					✓
Understanding the Big Bang/Origin of Universe				✓	
Solving Pauli's renormalizability problem	✓				

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