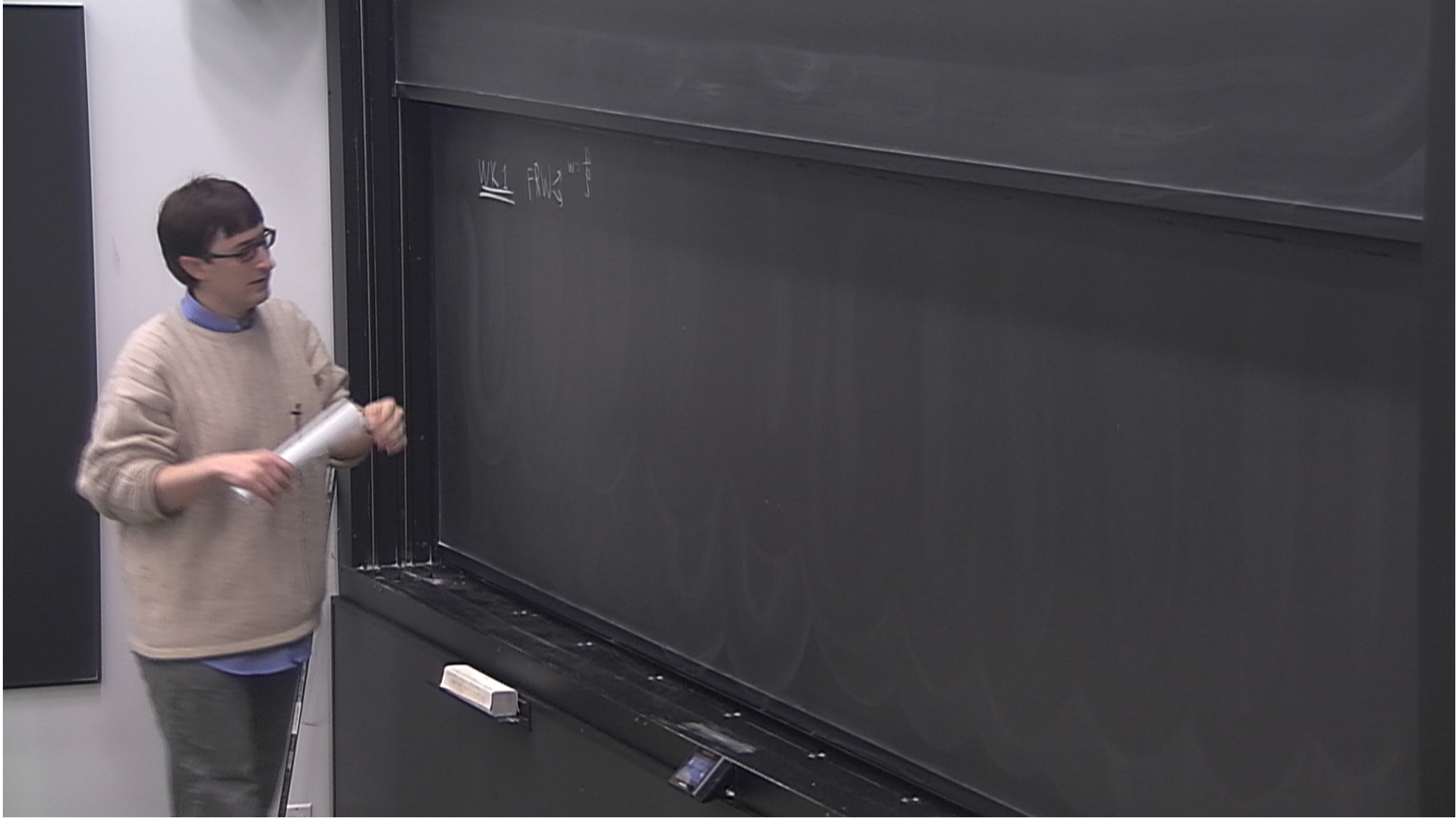


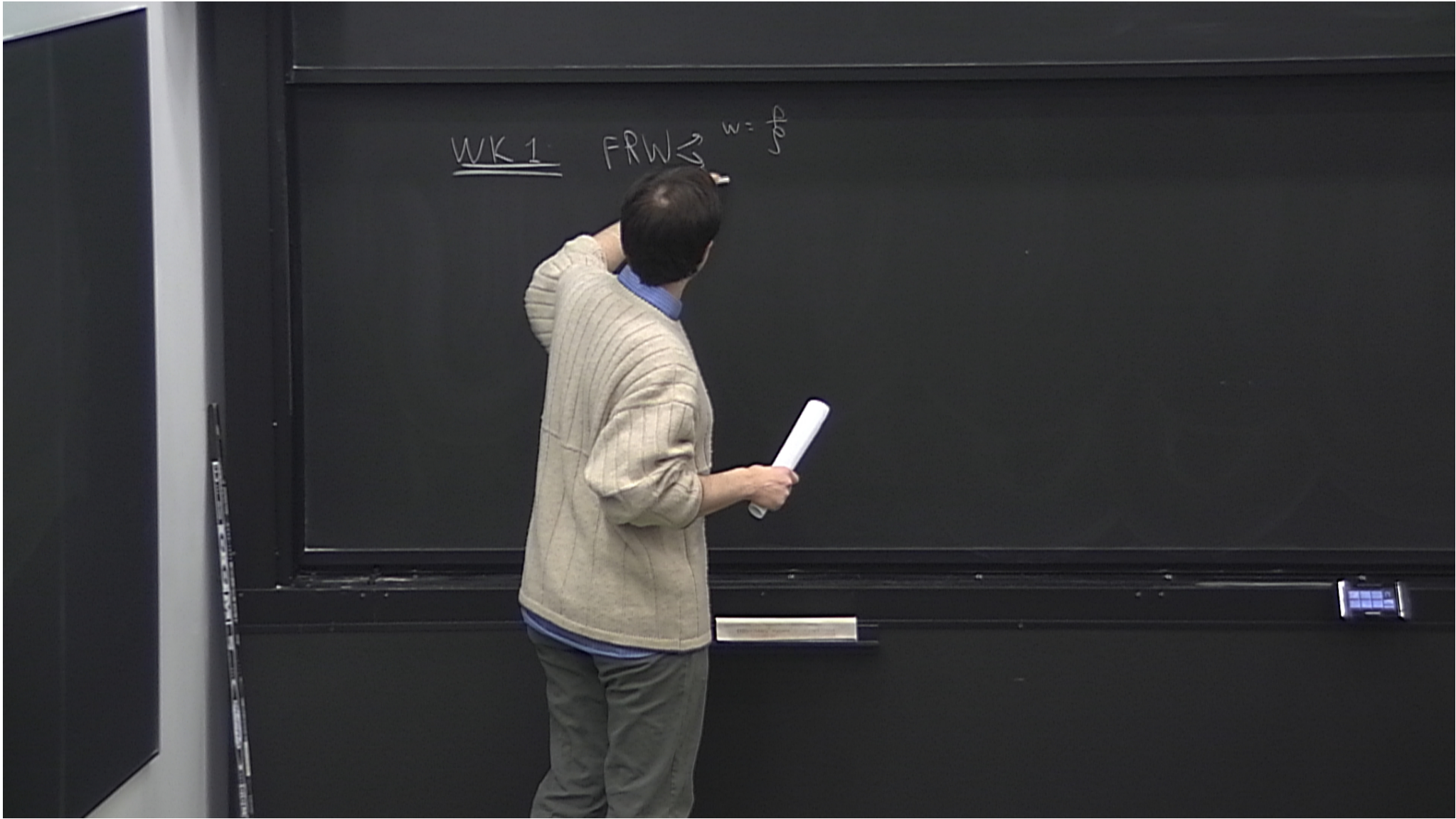
Title: 13/14 PSI - Cosmology Review - Lecture 9

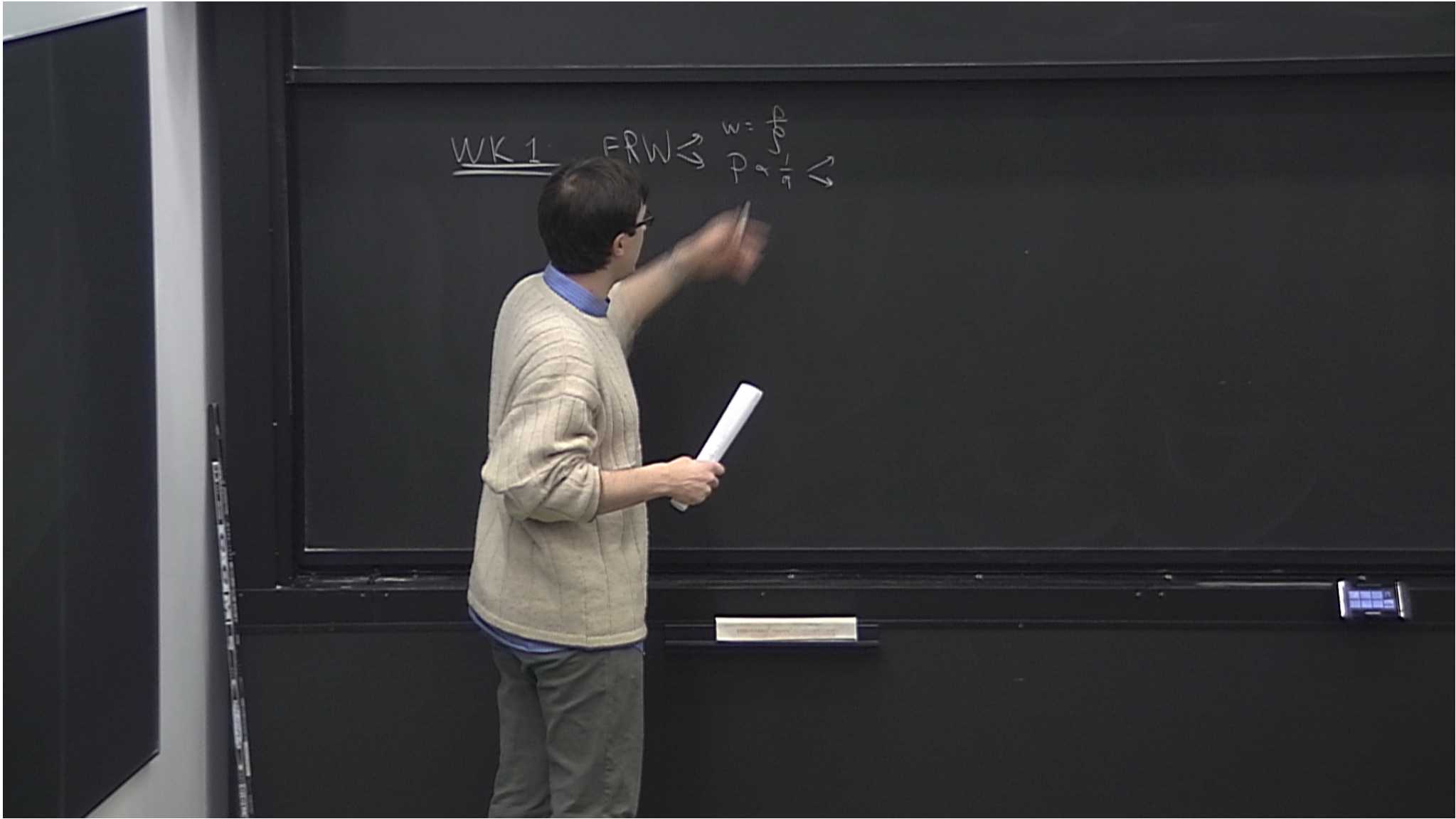
Date: Feb 10, 2014 11:30 AM

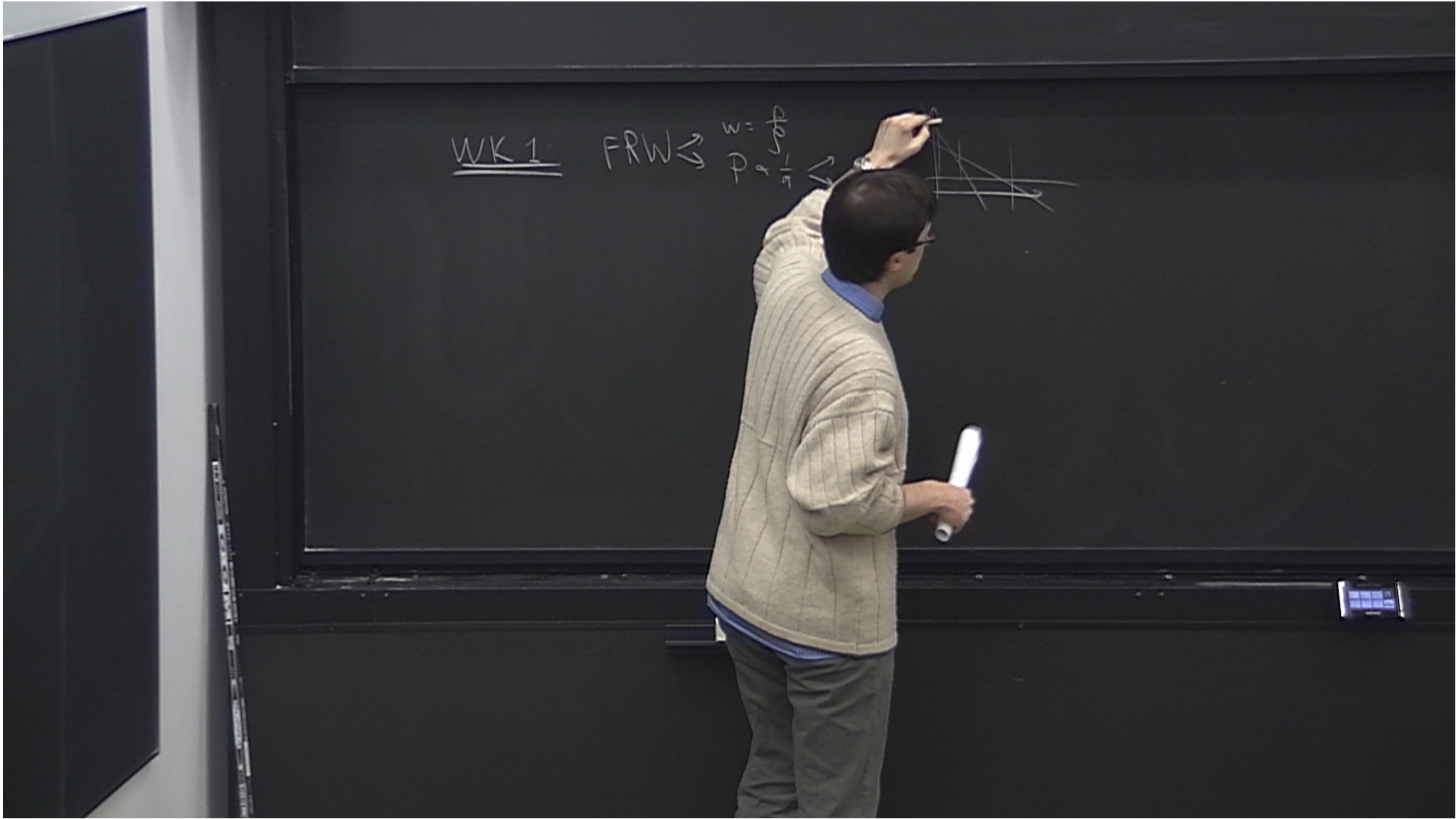
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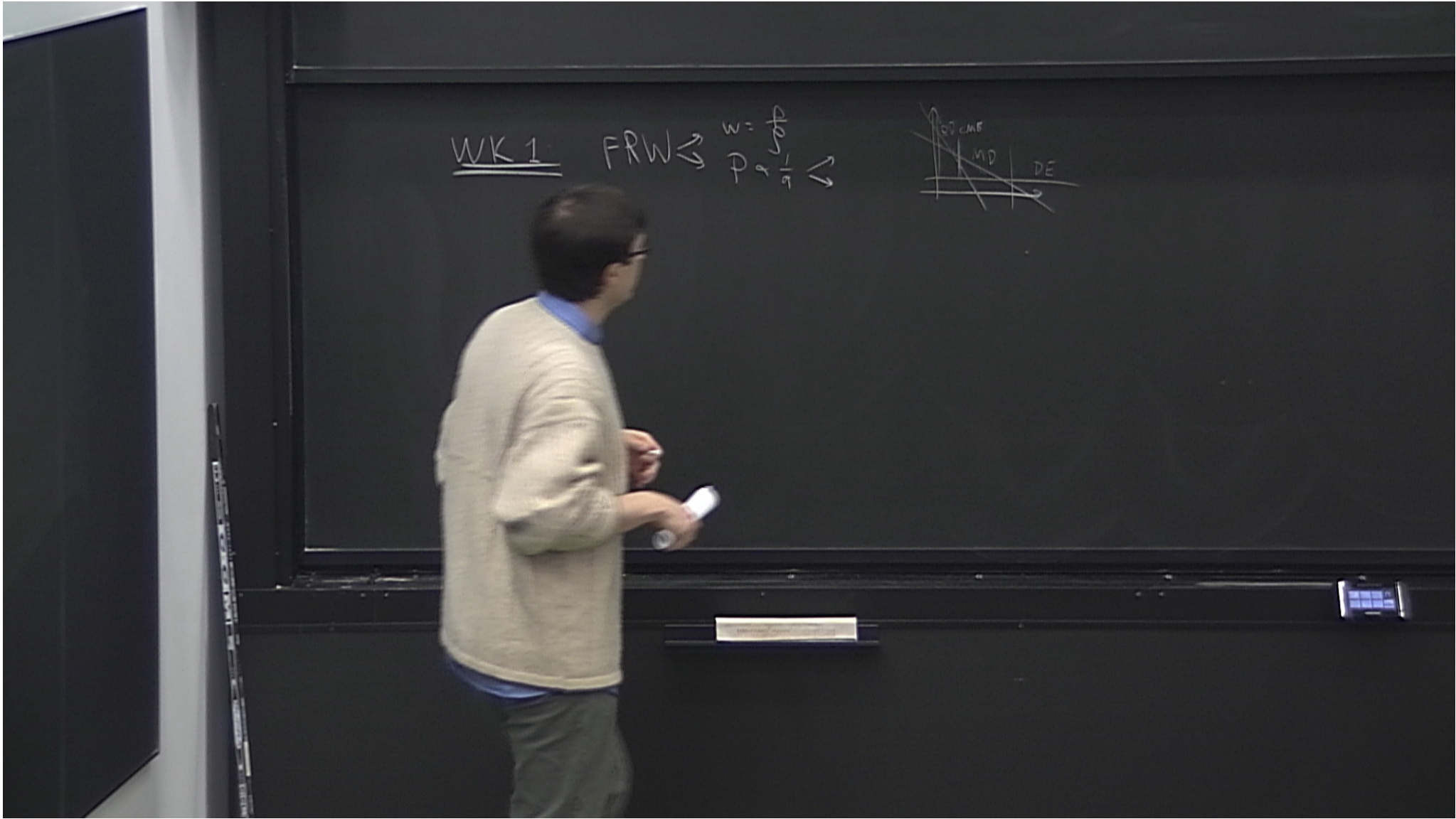
Abstract:



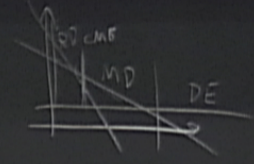


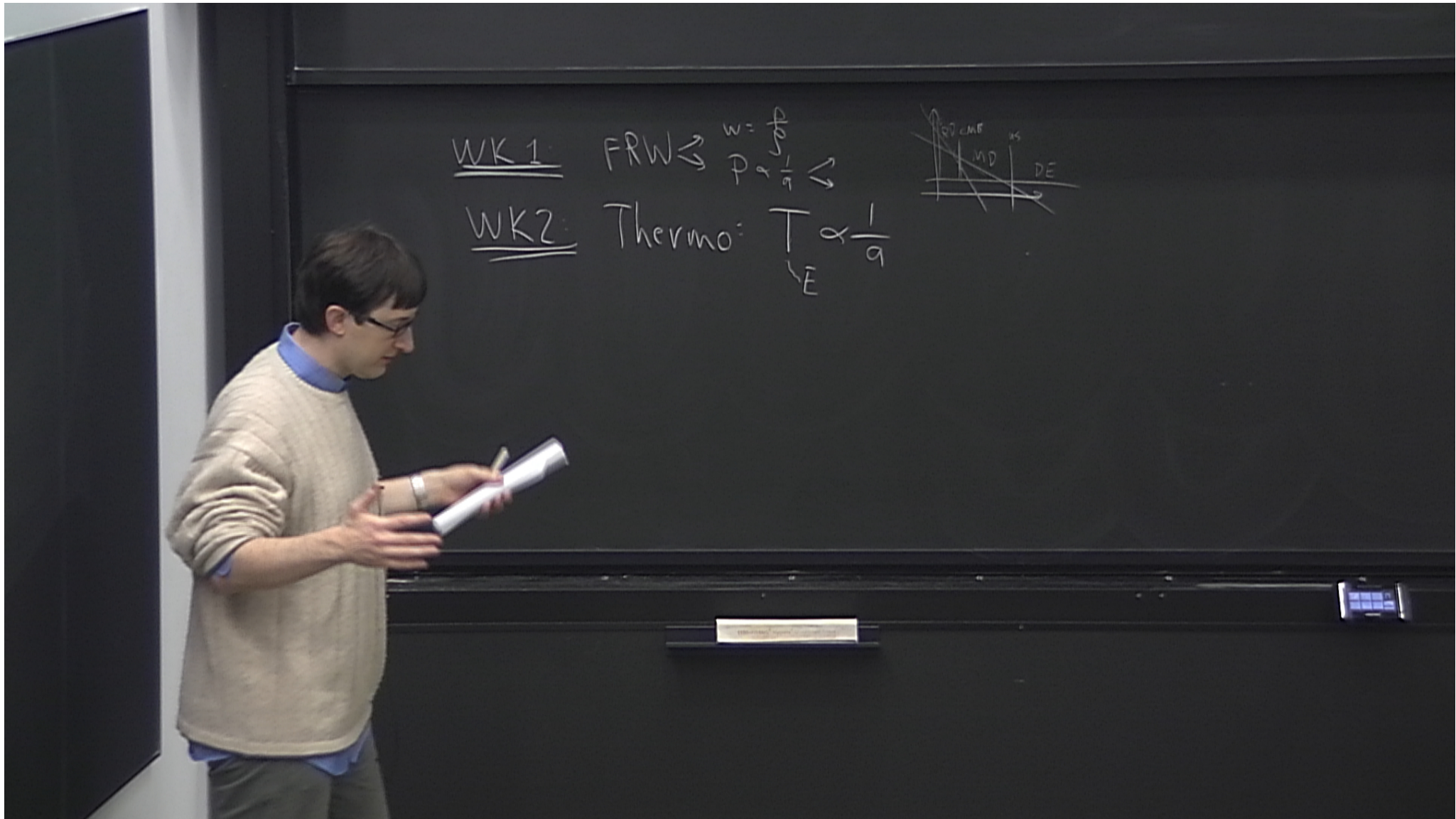


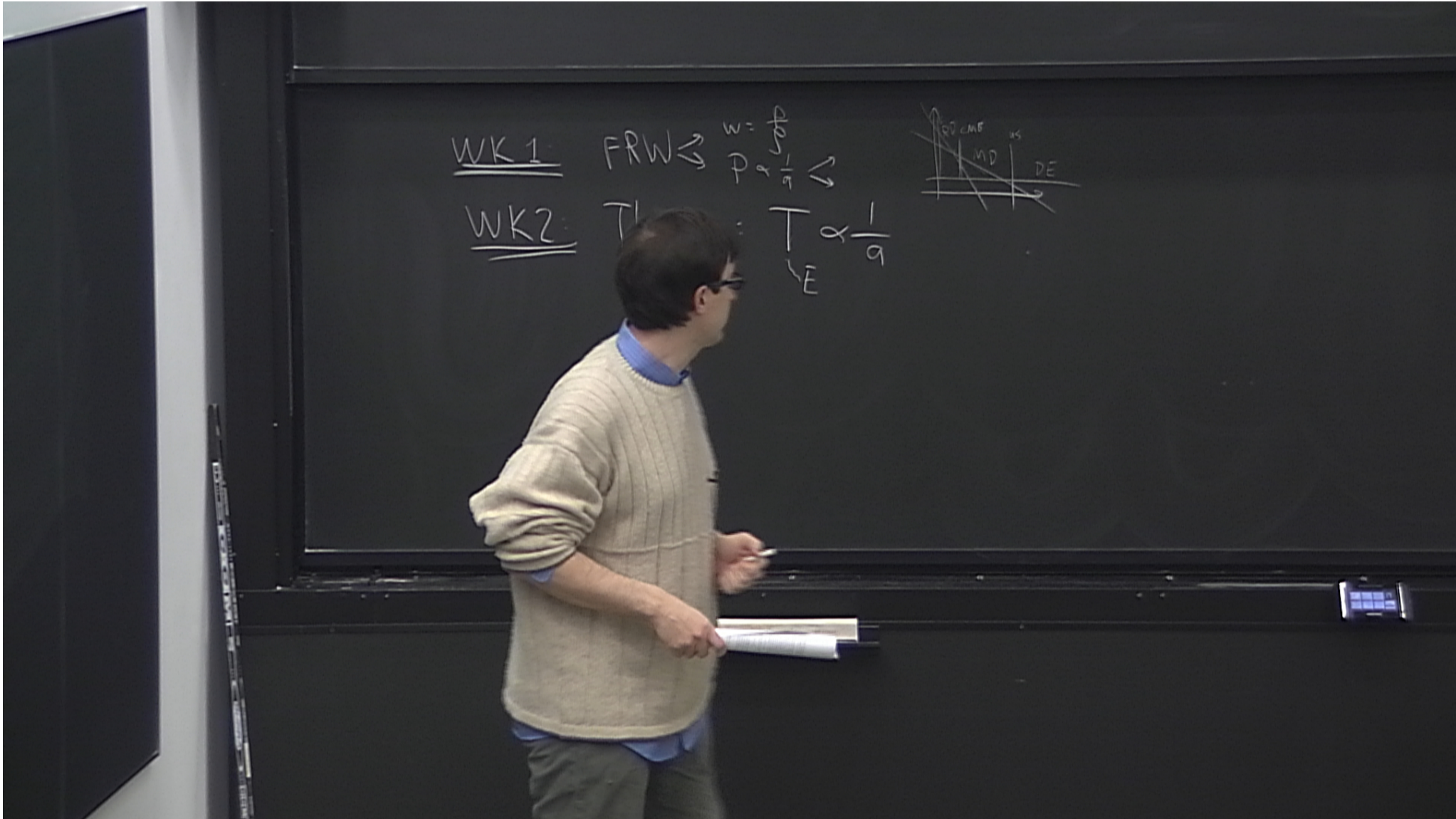




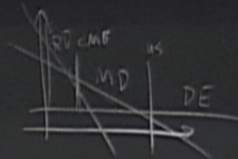
WK 1 FRW $\Leftrightarrow w = \frac{p}{q-1}$



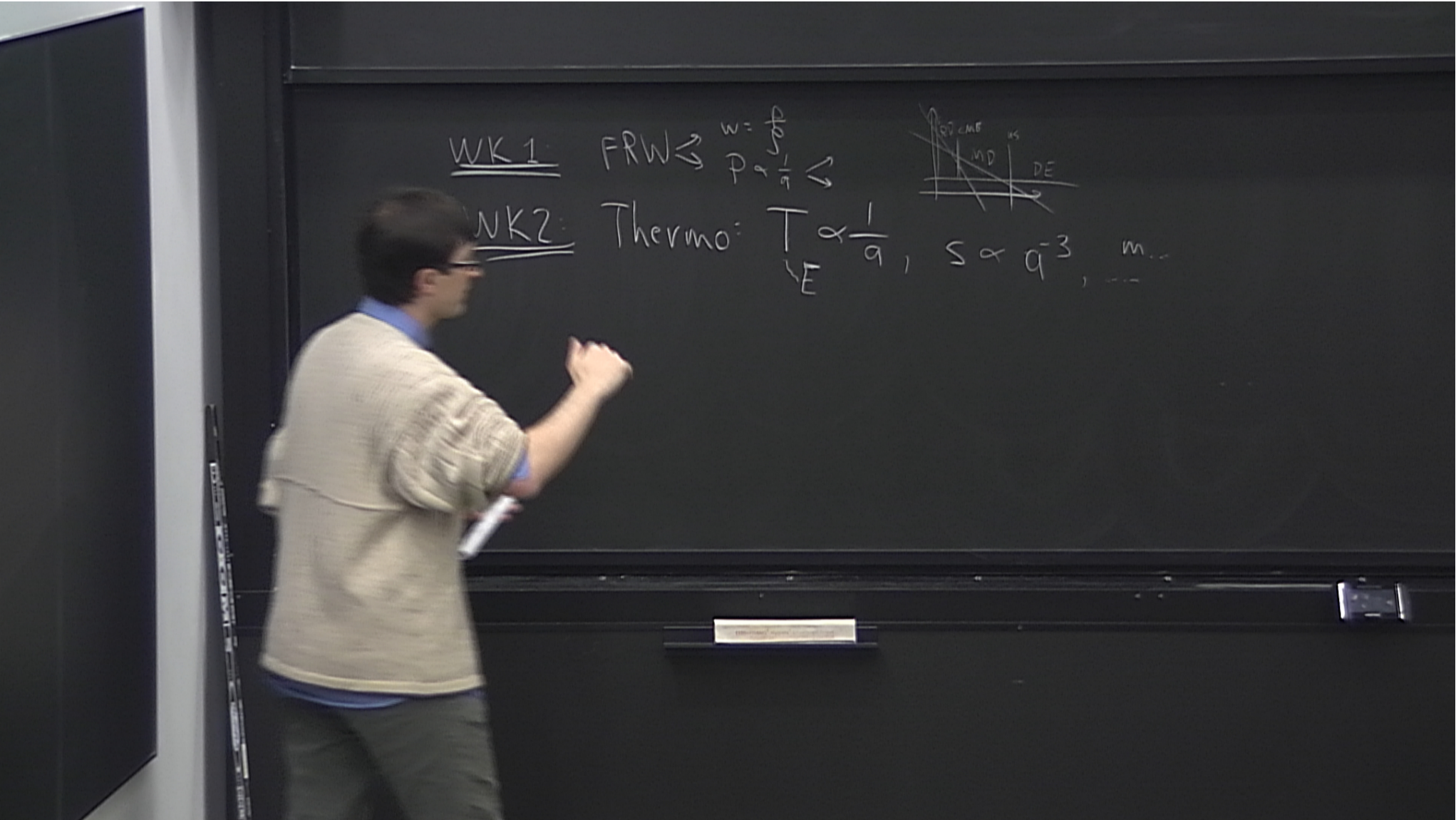




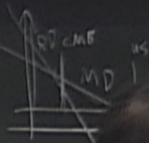
WK 1 FRW $\rightarrow w = \frac{\dot{p}}{p}$



WK 2 Thermo: $\frac{1}{a}, s \propto a^{-3}$



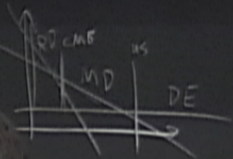
WK 1 FRW \rightarrow $w = \frac{p}{a}$
 $p \propto \frac{1}{a}$



WK 2 Thermo: $T \propto \frac{1}{a}$, $S \propto$

$$m \dots e^{-w/T}$$

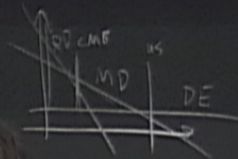
WK 1 FRW \Rightarrow $w = \frac{\rho}{3}$
 $p = \frac{1}{3} \rho$



WK 2 Thermo: T

$$s \propto a^{-3}, \quad m \dots e^{-m/T}$$
$$n \propto a^{-3}$$

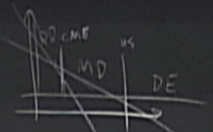
WK 1 FRW \Rightarrow $w = \frac{p}{a}$
 $p \propto \frac{1}{a} \Rightarrow$



WK 2 Thermo: T

$$S \propto a^{-3}, \quad m \dots e^{-m/T}$$
$$n \propto a^{-3}$$

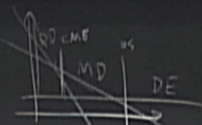
WK 1 FRW \rightarrow $w = \frac{f}{a}$
 $p \propto \frac{1}{a}$



WK 2 Thermo: $T \propto \frac{1}{a}$, $S \propto a^3$, $m \dots e^{-m/T}$
 E , $n \propto a^{-3}$

$\frac{S_F}{n}$

WK 1 FRW \rightarrow $w = \frac{f}{a}$
 $p \propto \frac{1}{a}$

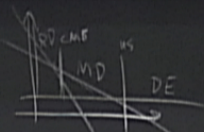


WK 2 Thermo: $T \propto \frac{1}{a}$, $S \propto a^3$, $m \dots e^{-m/T}$
 $E \propto a^3$, $n \propto a^{-3}$

$$\frac{S_F}{n_F} = \frac{S_0}{n_0}$$

$$p_0 = m n_0 > p_0$$

WK 1 FRW $\rightarrow w = \frac{\rho}{\rho + p}$
 $\rho \propto \frac{1}{a^3}$



WK 2

rmo: $T \propto \frac{1}{a}$, $S \propto a^{-3}$, $m \dots e^{-m/T}$

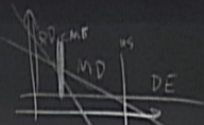
BBN ~ He ~ 25%
H ~ 75%

$\bar{n} \propto a^{-3}$

$\frac{S_f}{n_f} = \frac{S_0}{n_0}$

$\rho_0 = m n_0 > \rho_{cr} = \frac{3H_0^2}{8\pi G}$

WK 1 FRW $\rightarrow w = \frac{p}{\rho} \rightarrow$



WK 2

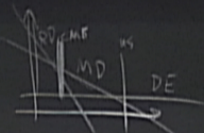
Thermo: $T \propto \frac{1}{a}$, $S \propto a^{-3}$, $m \dots e^{-m/T}$

BBN \sim He $\sim 25\%$
H $\sim 75\%$

CMB $\sim z \sim 1000$

$$\frac{S_f}{n_f} = \frac{S_0}{n_0} \quad \rho_0 = m n_0 > \rho_{cr} = \frac{3H_0^2}{8\pi G}$$

WK 1 FRW $\rightarrow w = \frac{p}{\rho}$
 $\rho \propto \frac{1}{a^3}$



WK 2

Thermo: $T \propto \frac{1}{a}$

$$S \propto a^{-3}, \quad \bar{n} \propto a^{-3}$$

$m \dots e^{-m/T}$

$$\frac{S_F}{n_F} = \frac{S_0}{n_0}$$

$$\rho_0 = m n_0 > \rho_{cr} = \frac{3H_0^2}{8\pi G}$$

BBN \sim He $\sim 25\%$
H $\sim 75\%$

CMB $\sim z \sim 1000$

Dark Matter

Dark E

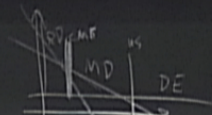
WK 1 FRW $\rightarrow w = \frac{p}{\rho}$

WK 2 Thermo: $T \propto \frac{1}{a}$

BBN \sim He $\sim 25\%$
H $\sim 75\%$

CMB $\sim z \sim 1000$

- \rightarrow Dark Matter \leftarrow
- \rightarrow Dark E \leftarrow



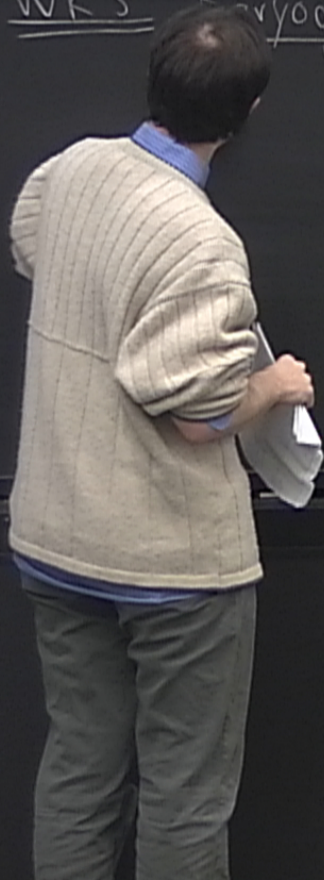
$$\rho \propto a^{-3}$$
$$\bar{n} \propto a^{-3}$$

$$m \dots e^{-m/T}$$

$$\frac{S_f}{n_f} = \frac{S_0}{n_0}$$

$$\rho_0 = m n_0 > \rho_{cr} = \frac{3H_0^2}{8\pi G}$$

WK 3 Parvogenesis



WK 3 Baryogenesis

Inflation \rightarrow cosmo conundra

Q

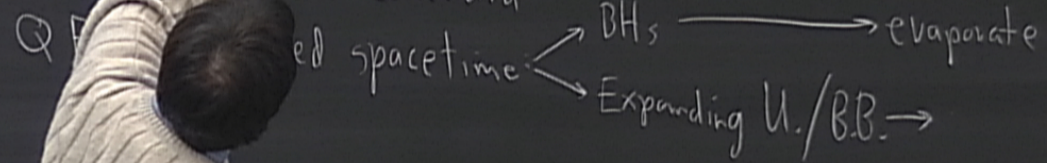
WK 3 Barogenesis
ation → cosmo conundra

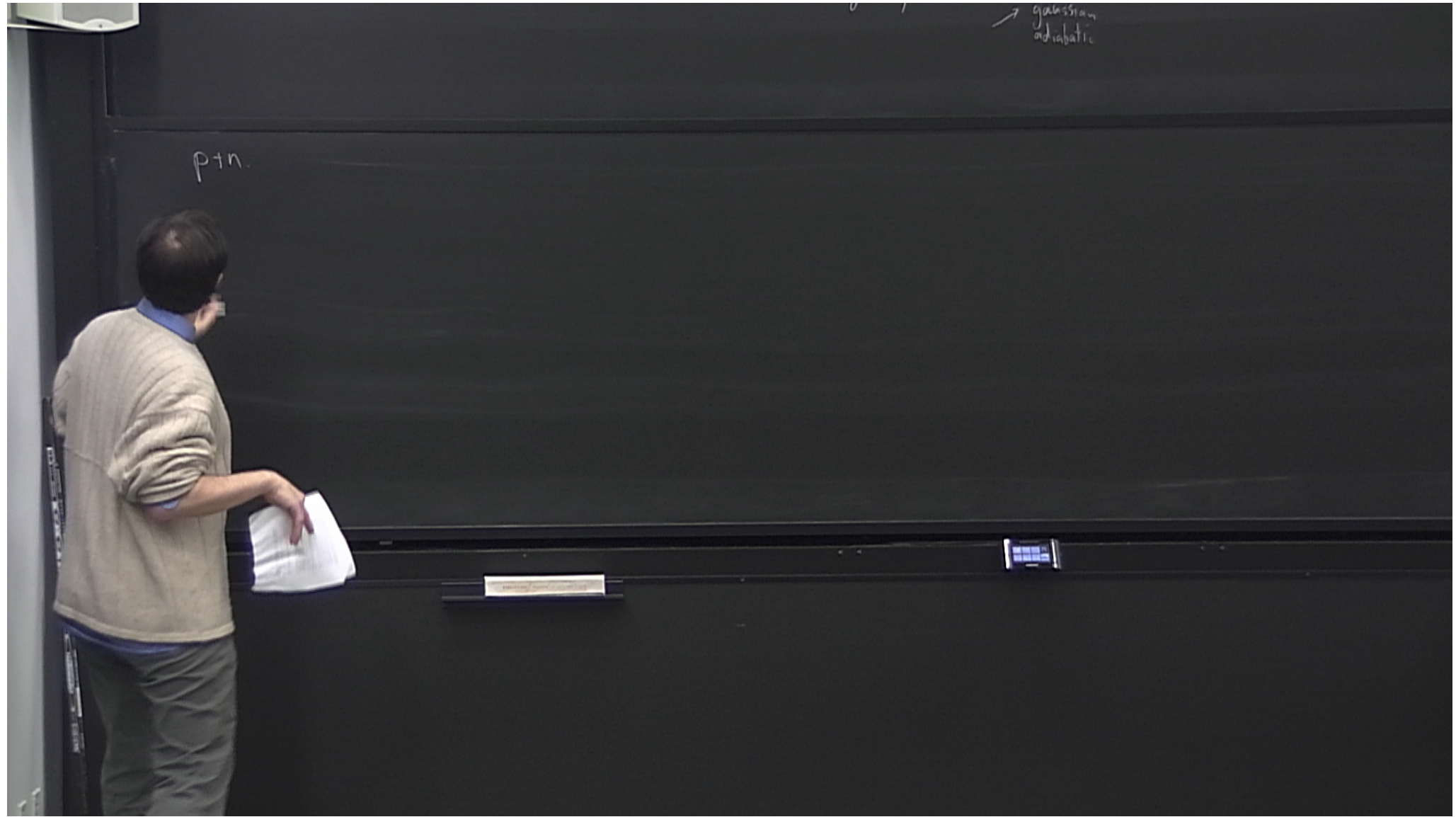
WK 3: Baryogenesis

Inflation \rightarrow cosmo conundrum
QFT in curved spacetime, BHs

WK 3 Baryogenesis

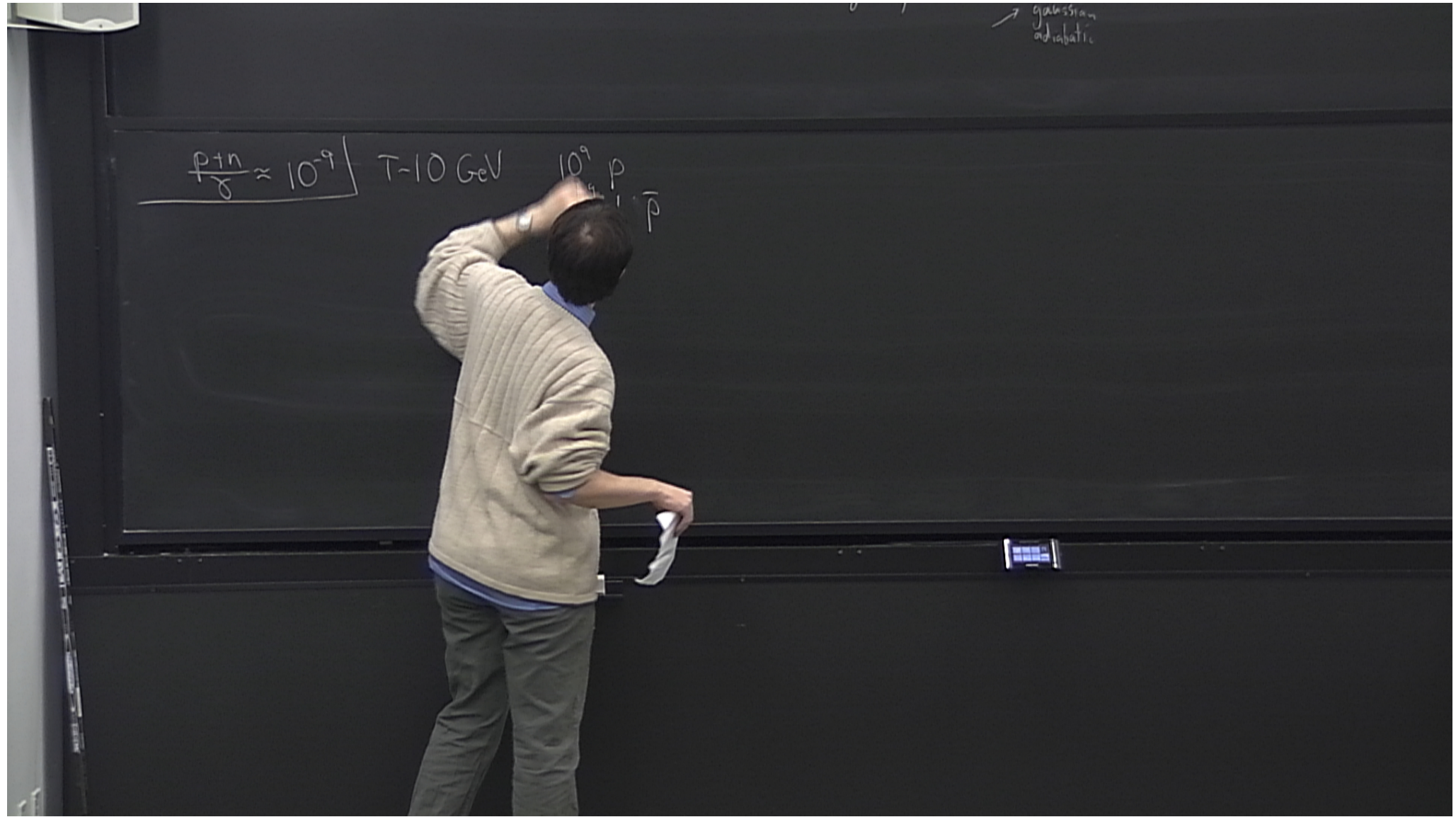
Inflation → cosmo conundra





$$\frac{p+n}{\gamma} \approx$$

→ gaussian
adiabatic



$$\frac{p+n}{g} \approx 10^{-9} \quad T=10 \text{ GeV}$$

$$\begin{matrix} 10^9 \bar{p} \\ 10^9+1 p \end{matrix}$$

B

→ gaussian
adiabatic

$$\frac{p+n}{\gamma} \approx 10^{-9} \quad T=10 \text{ GeV}$$

$$\begin{matrix} 10^9 \bar{p} \\ 10^9+1 p \end{matrix}$$

→ gaussian
adiabatic

$$\frac{p+n}{\gamma} \approx 10^{-9} \quad T=10 \text{ GeV}$$

$$\begin{array}{l} 10^9 \bar{p} \\ 10^9 + 1 p \end{array}$$

→ gaussian
adiabatic

B P

→ gaussian
adiabatic

$$\frac{\mu + n}{\gamma} \approx 10^{-9} \quad T = 10 \text{ GeV}$$

$10^9 \bar{p}$
 $10^9 + 1 p$

$B_1 \rightarrow$ "Sphaleron"

→ gaussian
adiabatic

$$\frac{\rho+n}{\gamma} \approx 10^{-9} \quad T=10 \text{ GeV} \quad \boxed{\begin{matrix} 10^9 \bar{p} \\ 10^9+1 p \end{matrix}}$$

B $B \rightarrow$ "Sphaleron"
inflation $\rightarrow a \propto e^{60} \quad B \propto a^{-3+60}$

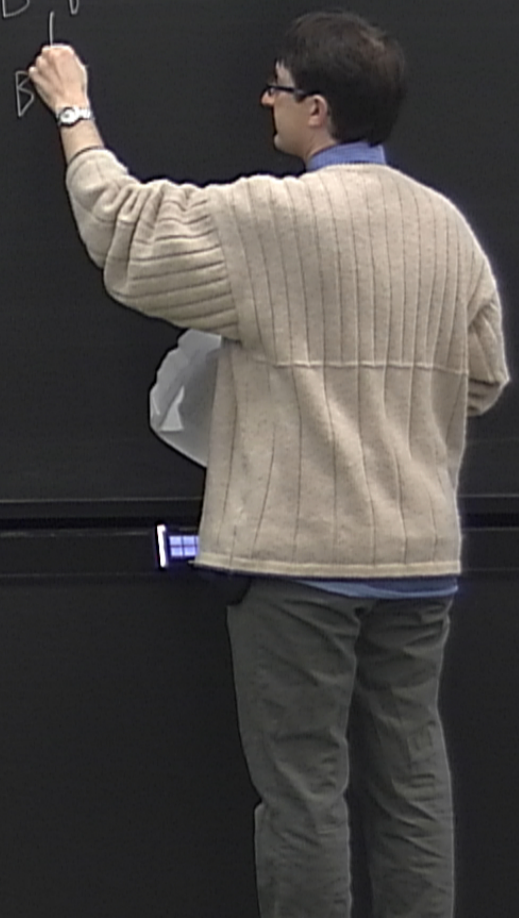
→ gaussian
adiabatic

$$\frac{p+n}{\rho} \approx 10^{-9} \quad T \sim 10 \text{ GeV} \quad \boxed{\begin{matrix} 10^9 \bar{p} \\ 10^9 + 1 \rho \end{matrix}}$$

B $B \rightarrow$ "Sphaleron"
inflation $\rightarrow a \propto e^{60} \quad B \propto a^{-3 \cdot 60} \quad 10^{-9}$

Sakharov

$$B = \bar{B}$$



→ gaussian
adiabatic

$$\frac{p+n}{g} \approx 10^{-9} \quad T \sim 10 \text{ GeV}$$

$$\boxed{\begin{matrix} 10^9 \bar{p} \\ 10^9 + 1 p \end{matrix}}$$

$B \rightarrow$ "Sphaleron"

inflation $\rightarrow a \sim e^{60} \quad B \sim g^{-3 \cdot 60} \quad 10^{-9}$

Sakharov

$$B = \bar{B} \\ \downarrow \\ B \neq \bar{B}$$

- 1) \cancel{B}
- 2) \cancel{C}, \cancel{P}
- 3) $\cancel{T.E.}$

$$X_{B_1} \rightarrow \dots - B_2$$

...ing U./B.B. → scale invariant
→ gaussian
→ adiabatic

$$\bar{p} + 1 \cdot p$$

Sakharov

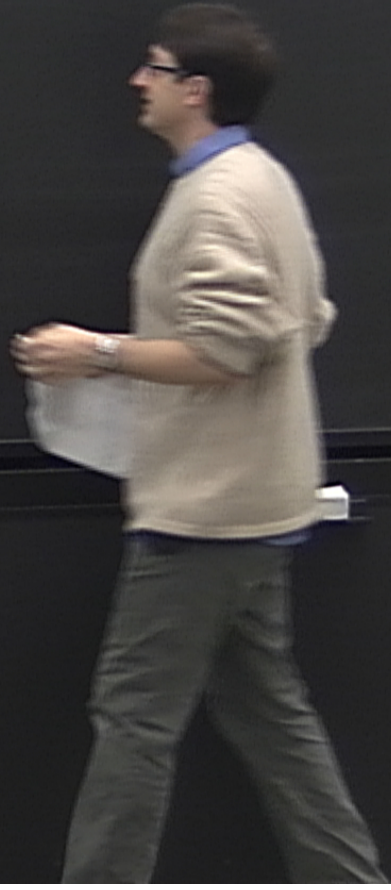
$$B = \bar{B} \\ \downarrow \\ B \neq \bar{B}$$

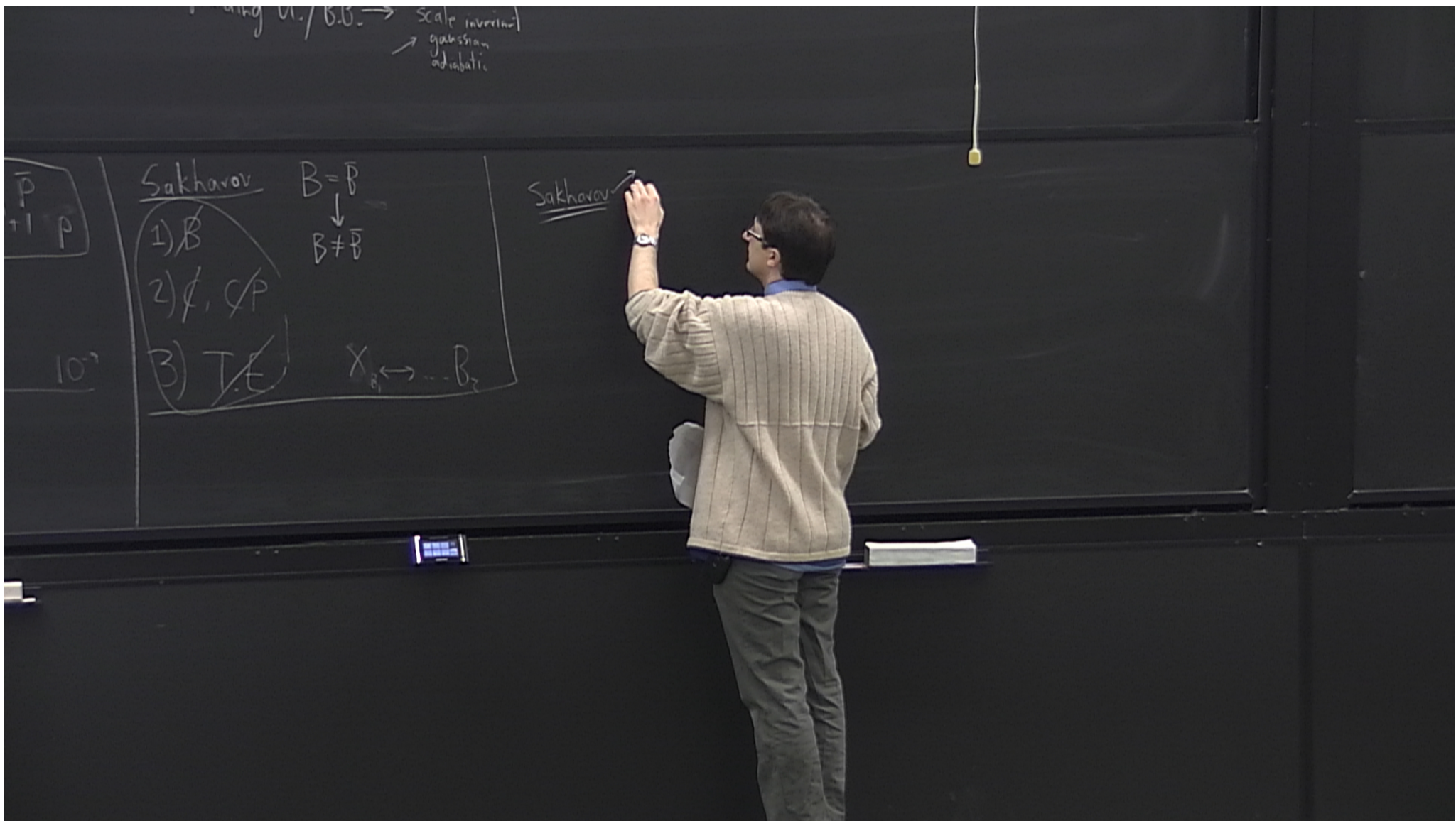
Sakharov

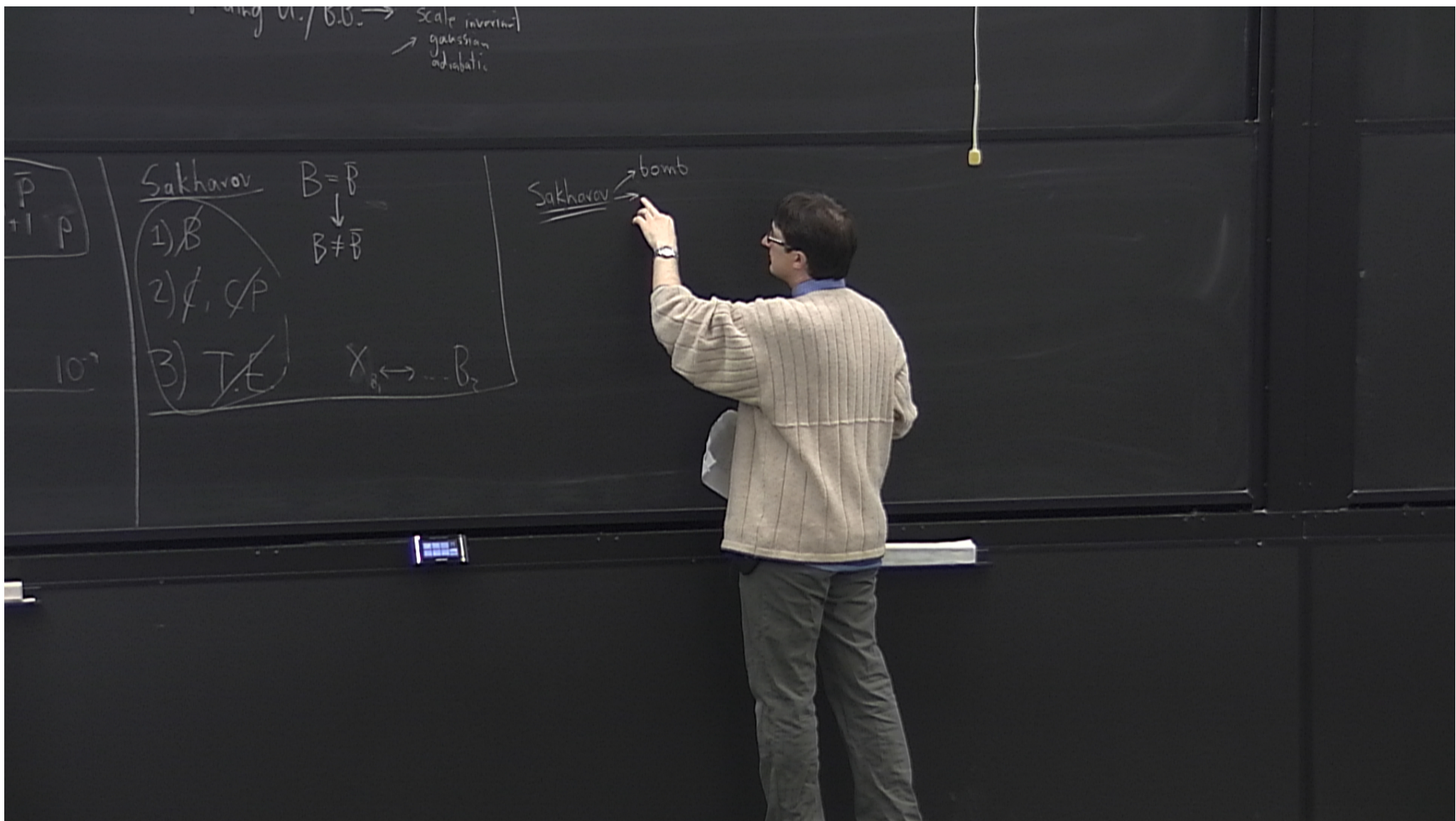
- 1) \bar{B}
- 2) \not{C}, \not{CP}
- 3) $\not{T, E}$

$$X_{a_1} \leftrightarrow \dots \leftrightarrow B_2$$

10^{-9}







...ing $U./B.B.$ → scale invariant
→ gaussian
→ adiabatic

\bar{p}
 $+1 p$

Sakharov

$B = \bar{P}$

↓
 $B \neq \bar{P}$

1) \bar{B}

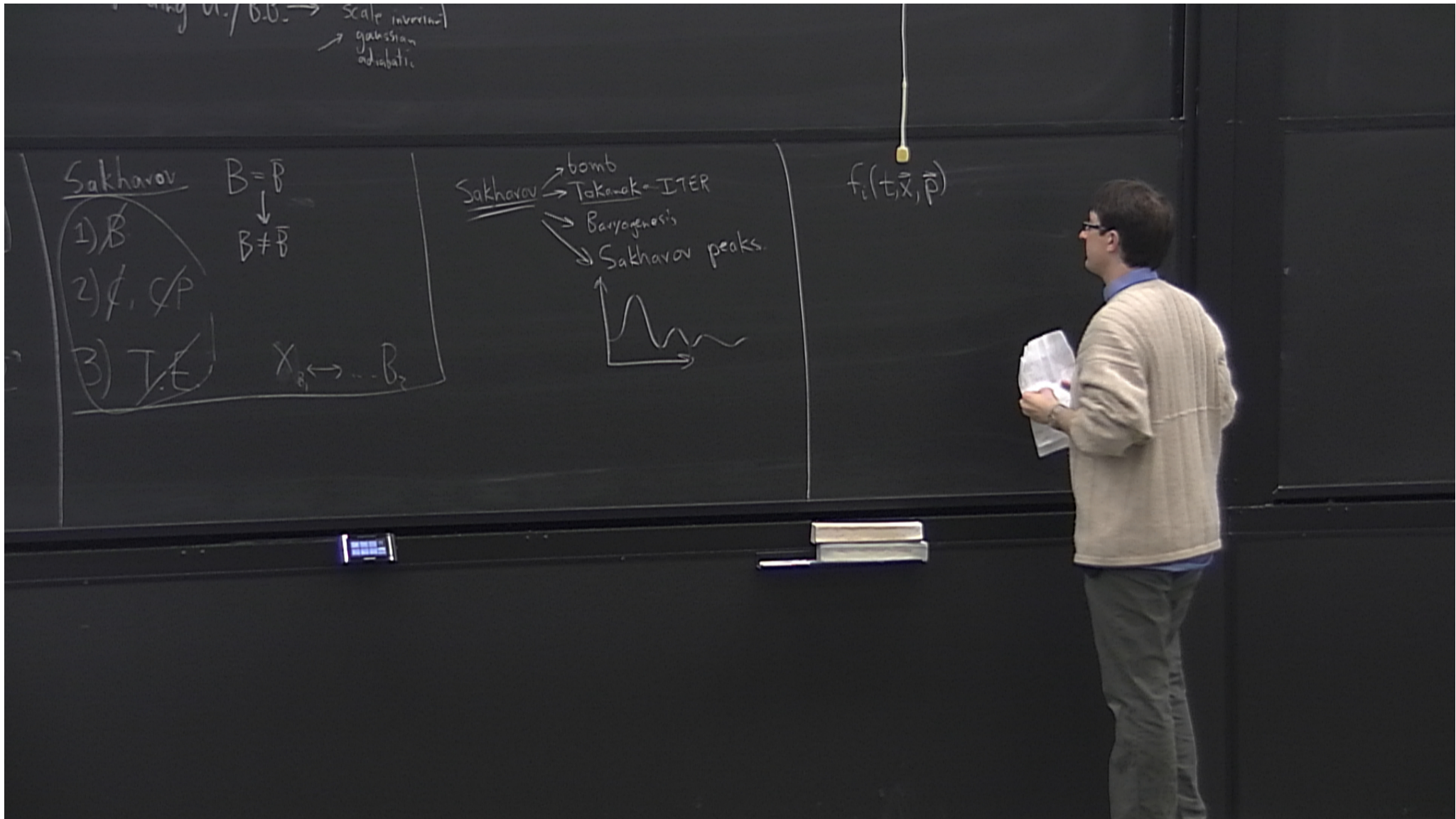
2) \not{C}, \not{P}

3) T, E

$X_i \leftrightarrow \dots B_j$

Sakharov → bomb

10^{17}



scale invariant
gaussian
adiabatic

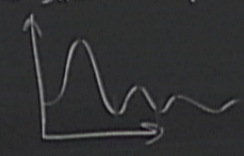
Sakharov

$B = \bar{B}$
 \downarrow
 $B \neq \bar{B}$

- 1) B
- 2) C, CP
- 3) T, E

$X_1 \leftrightarrow \dots \leftrightarrow B_2$

Sakharov → bomb
Taka-ack-ITER
→ Baryogenesis
→ Sakharov peaks.



$f_i(t, \vec{x}, \vec{p})$

...ing $U./B.D.$ → scale invariant
 → gaussian
 adiabatic

Sakharov

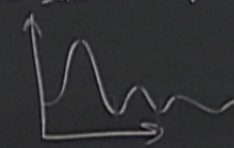
$B = \bar{B}$
 \downarrow
 $B \neq \bar{B}$

- 1) B
- 2) C, CP
- 3) T, E

$X_1 \leftrightarrow \dots B_2$

Sakharov

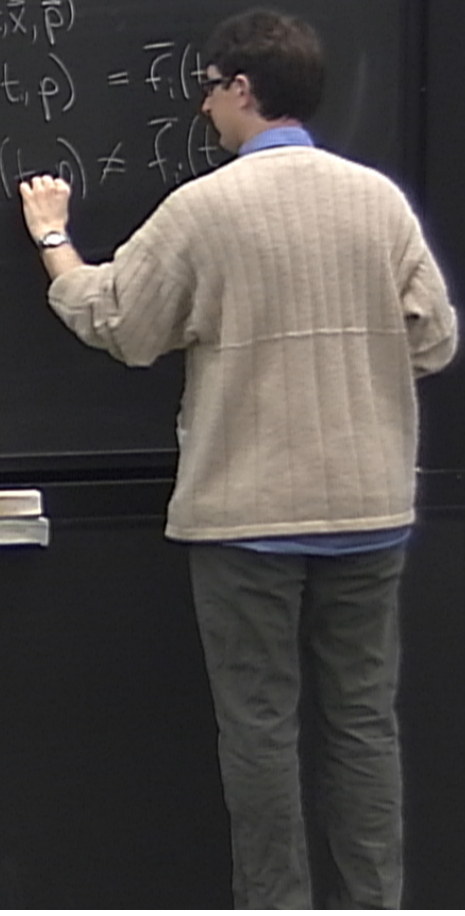
- bomb
- Tokamak-ITER
- Baryogenesis
- Sakharov peaks.

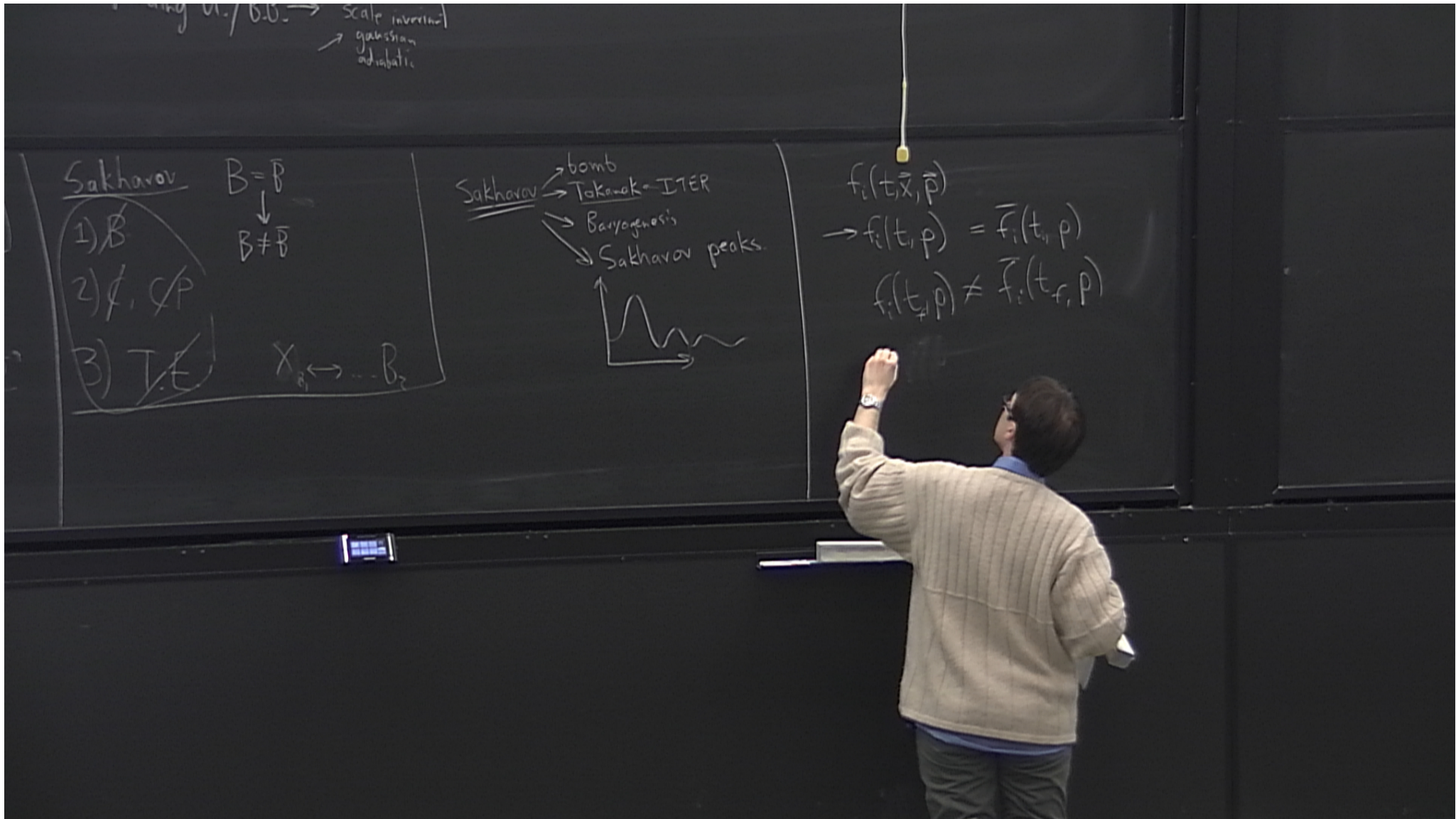


$$f_i(t, \vec{x}, \vec{p})$$

$$\rightarrow f_i(t, p) = \bar{f}_i(t)$$

$$f_i(t, p) \neq \bar{f}_i(t)$$





...ing $U./B.B.$ → scale invariant
 → gaussian
 adiabatic

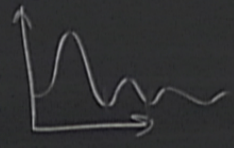
Sakharov

$B = \bar{B}$
 ↓
 $B \neq \bar{B}$

- 1) B
- 2) C, CP
- 3) T, E

$X_1 \leftrightarrow \dots B_2$

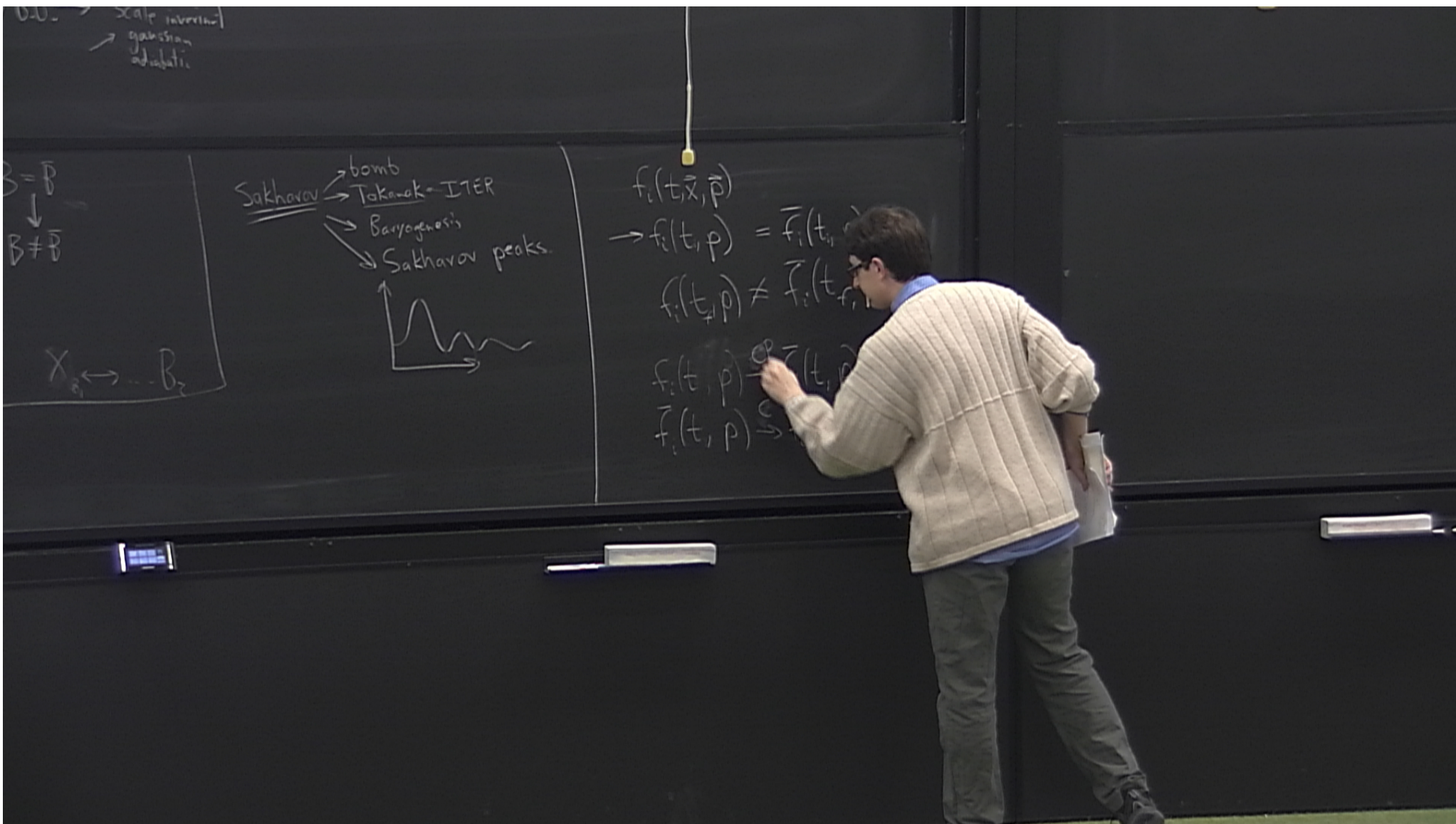
Sakharov → bomb
 → Tokamak-ITER
 → Baryogenesis
 → Sakharov peaks.

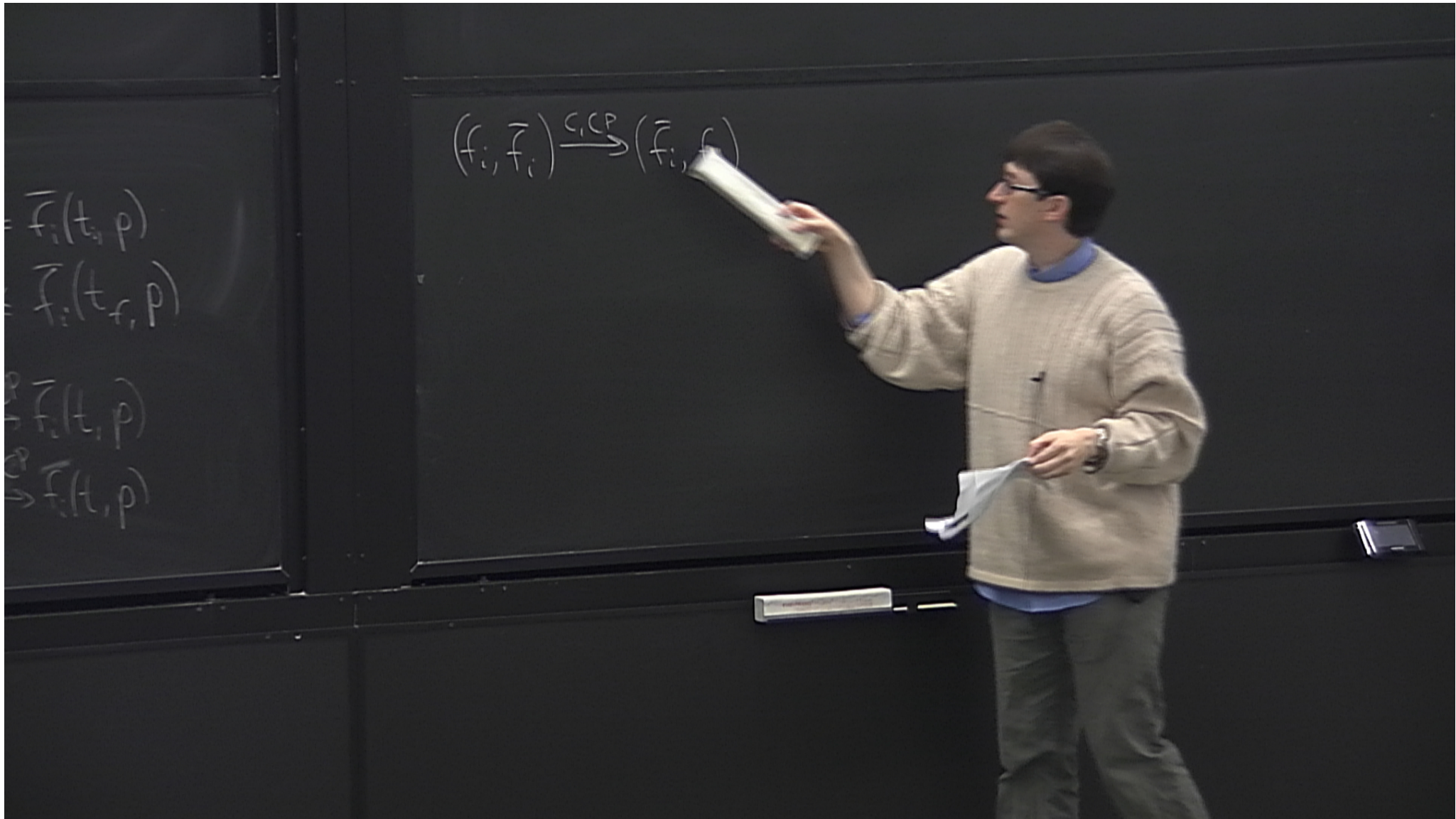


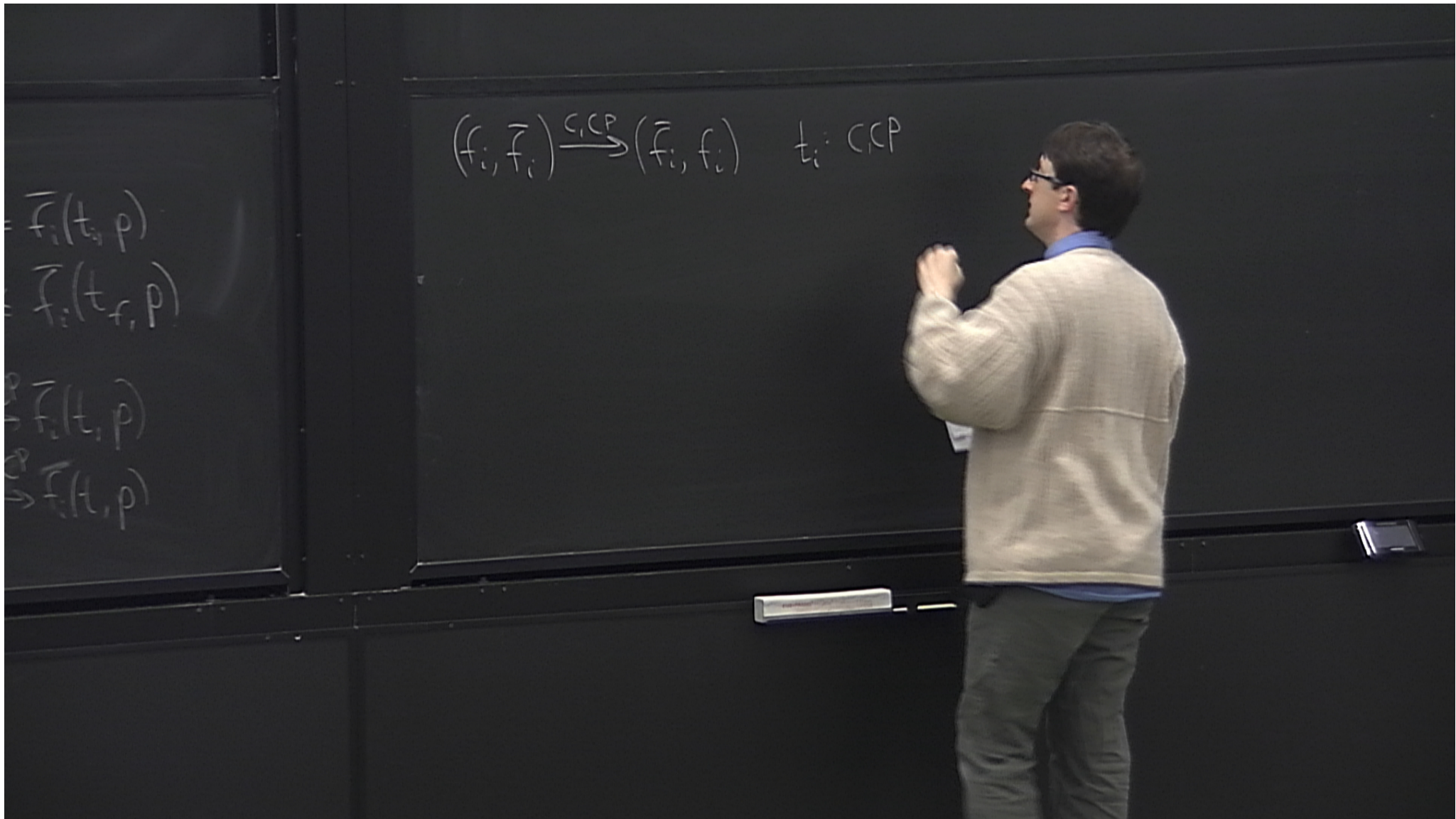
$$f_i(t, \vec{x}, \vec{p})$$

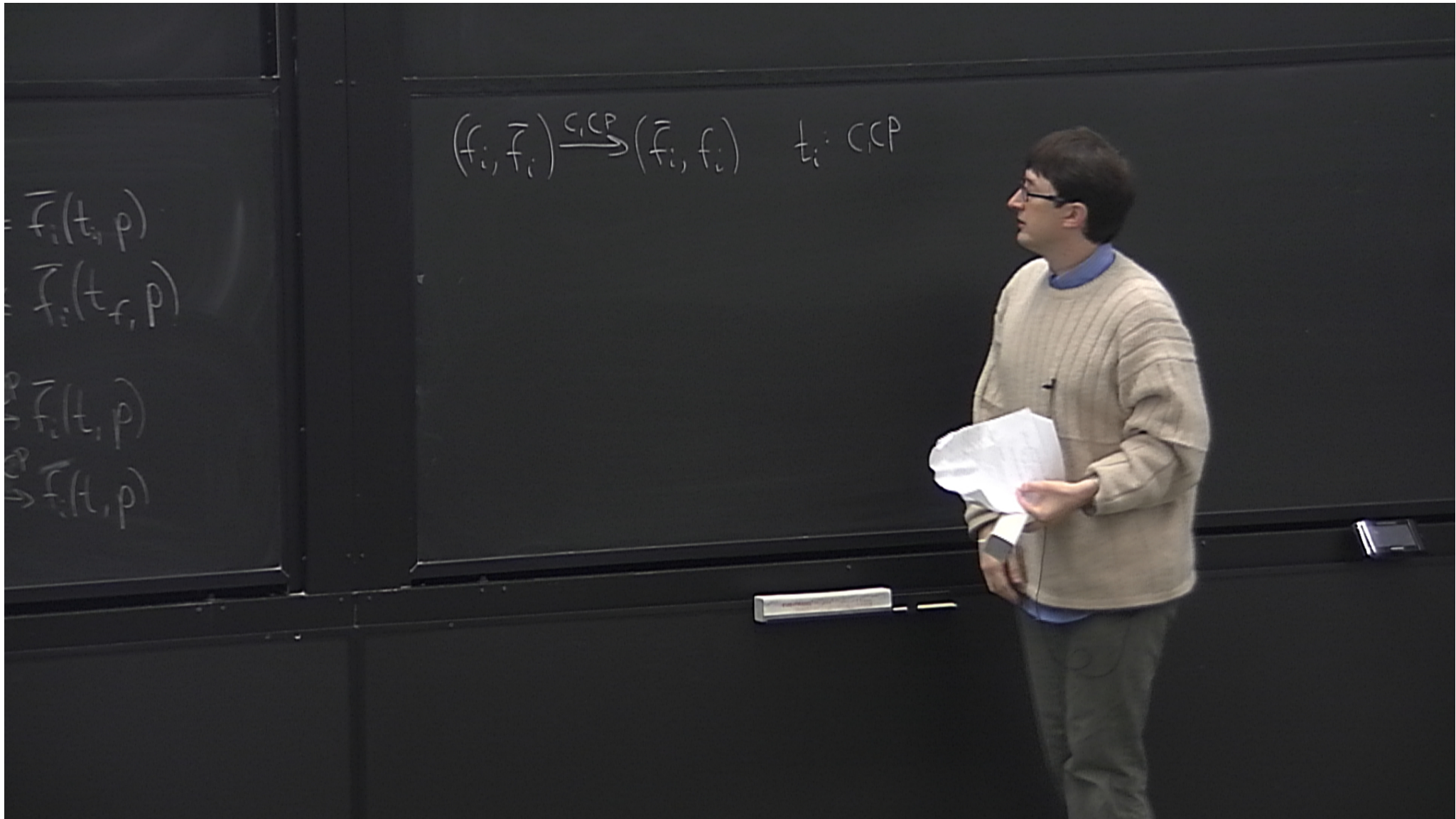
$$\rightarrow f_i(t, p) = \bar{f}_i(t, p)$$

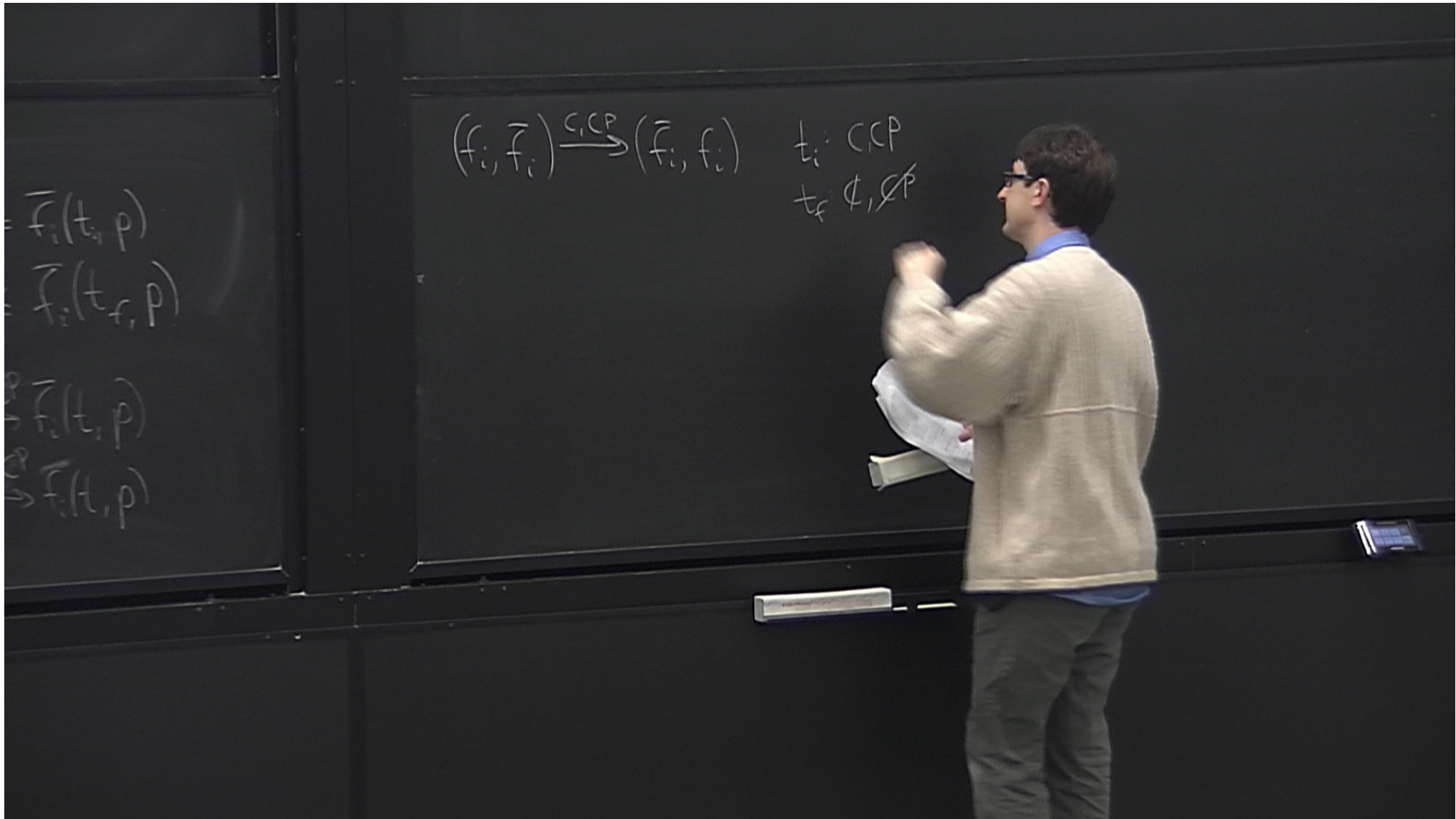
$$f_i(t_f, p) \neq \bar{f}_i(t_f, p)$$

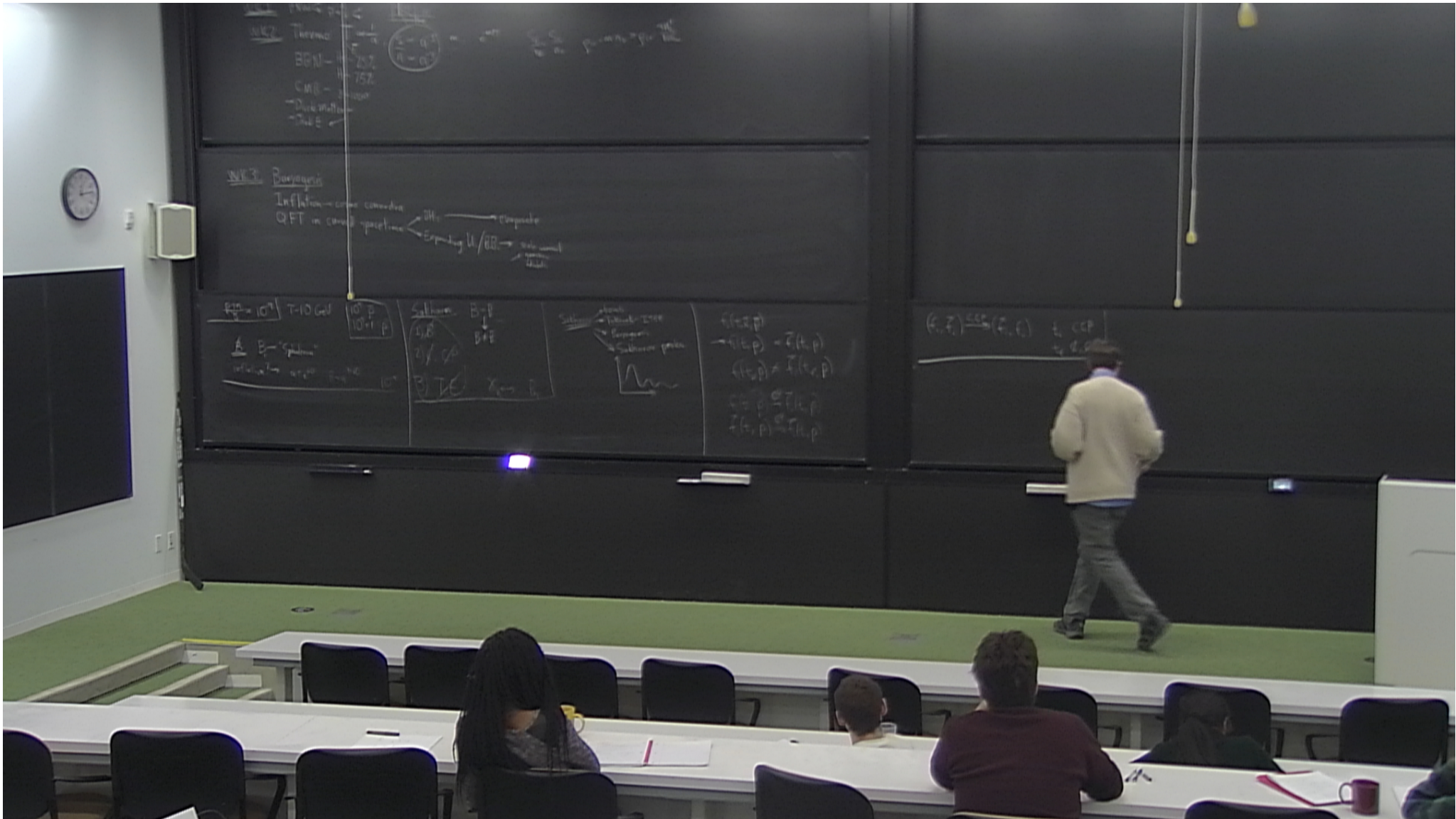






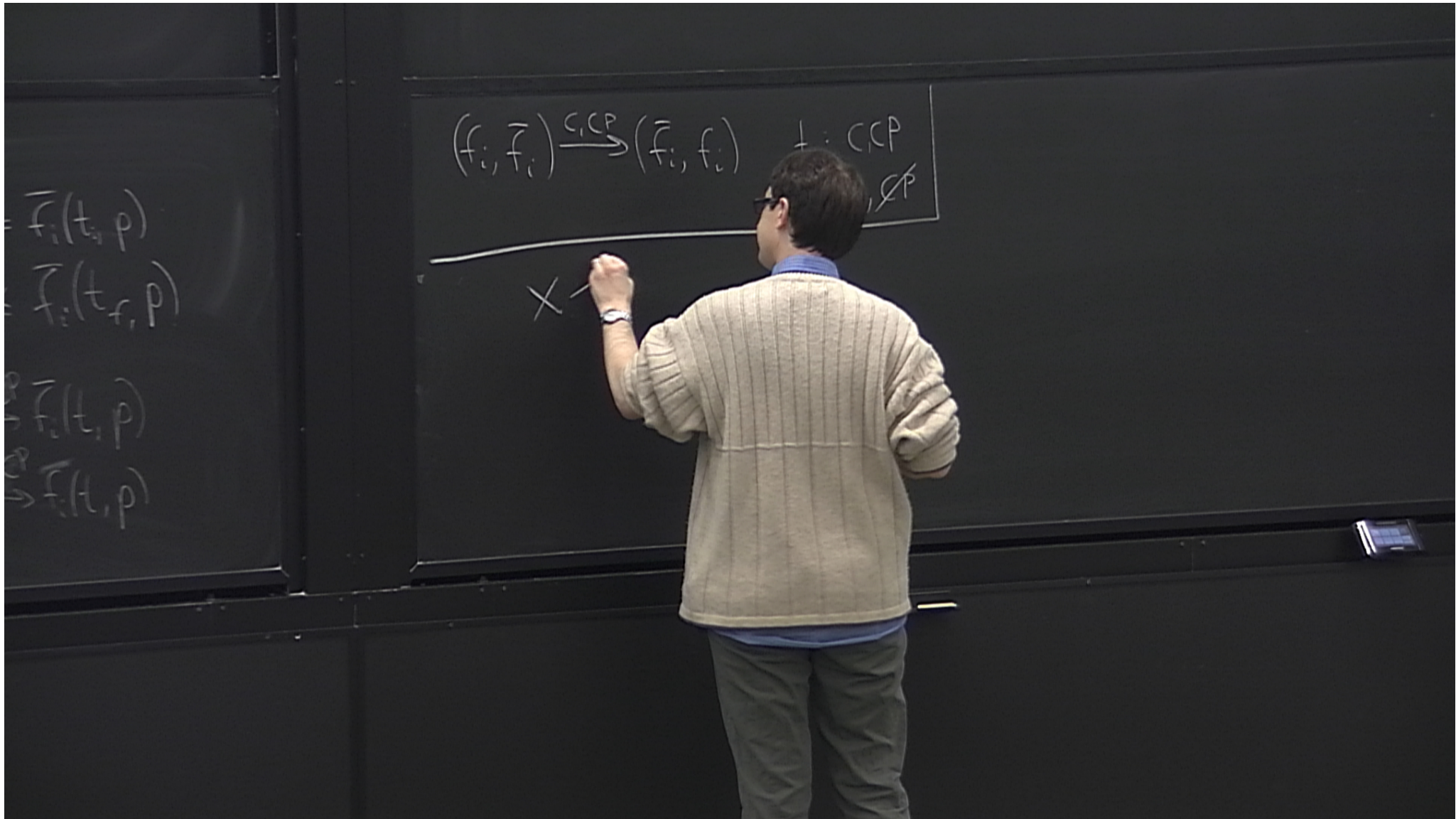






$\bar{f}_i(t_i, p)$
 $\bar{f}_i(t_f, p)$
 $\bar{f}_i(t_i, p)$
 $\bar{f}_i(t_i, p)$

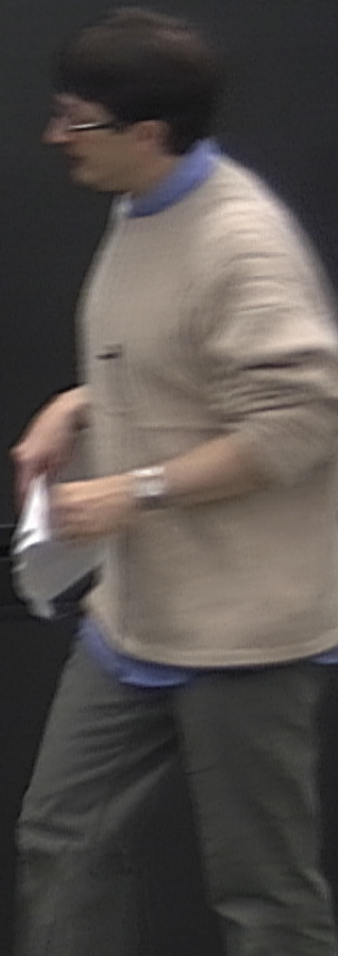
$$(f_i, \bar{f}_i) \xrightarrow{C, CP} (\bar{f}_i, f_i) \quad \begin{array}{l} t_i: CCP \\ t_f: \emptyset, \cancel{CP} \end{array}$$

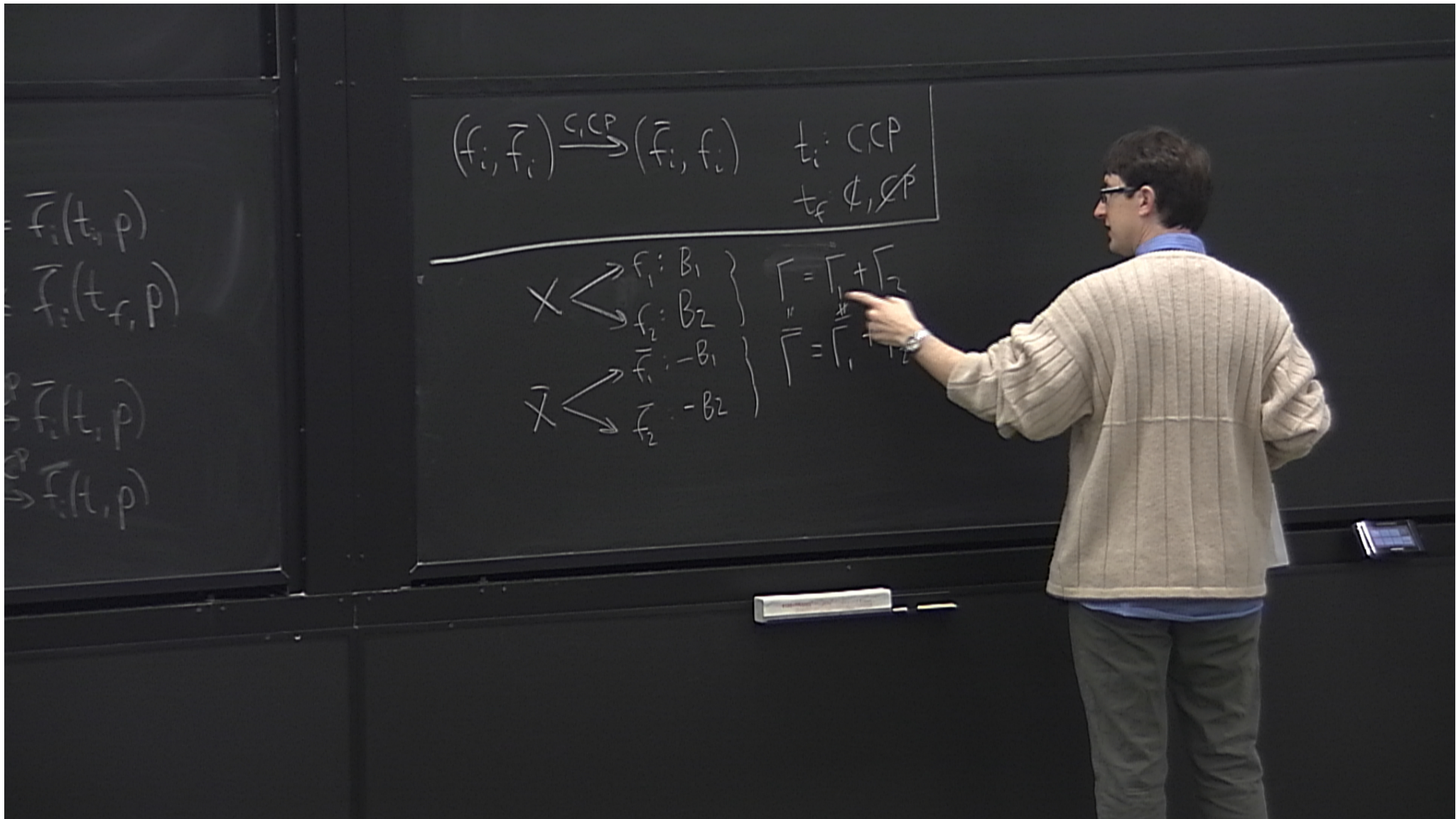


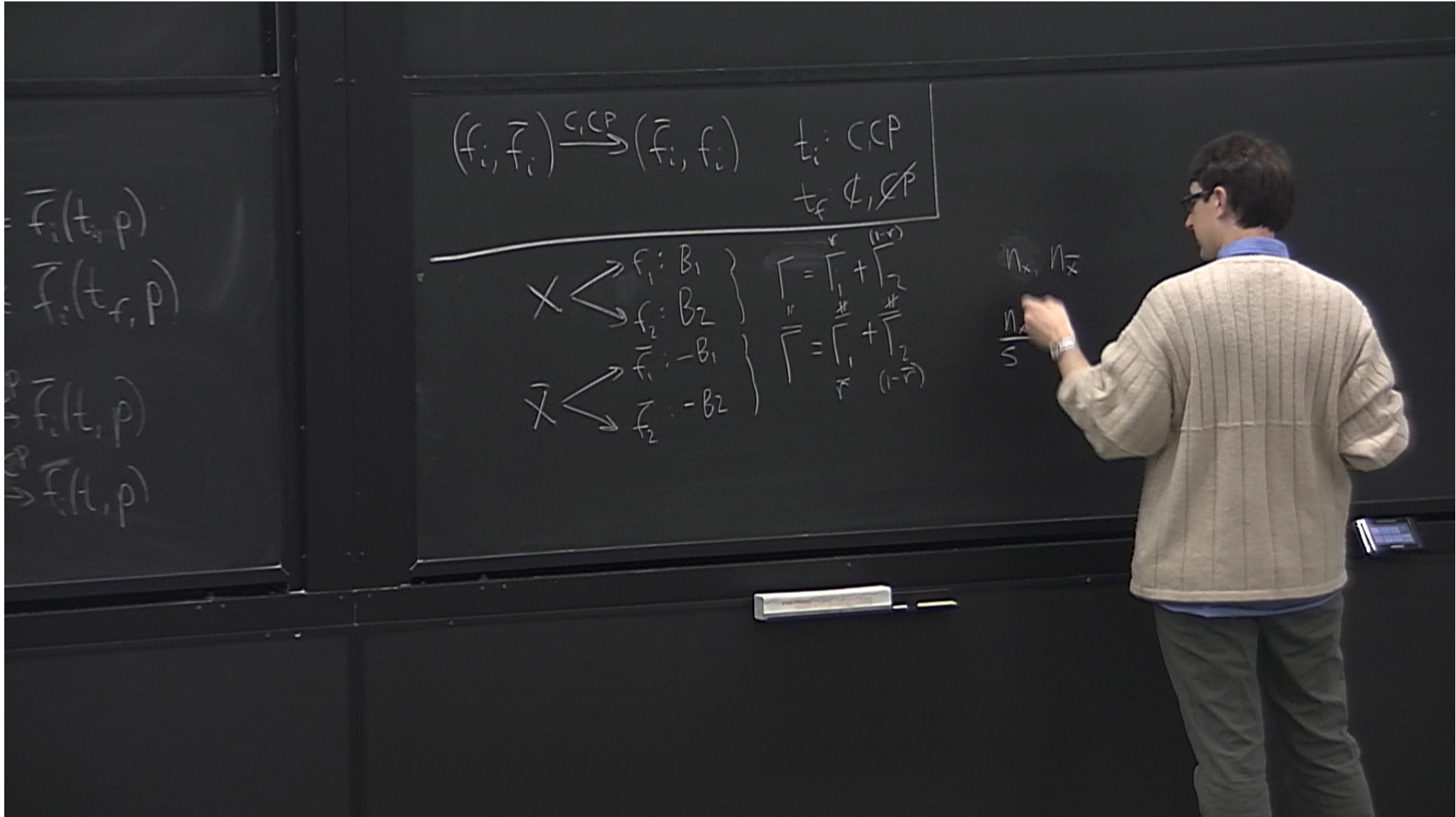
$\bar{f}_1(t, p)$
 $\bar{f}_2(t, p)$
 $\bar{f}_1(t, p)$
 $\bar{f}_2(t, p)$

$$(f_i, \bar{f}_i) \xrightarrow{C, CP} (\bar{f}_i, f_i) \quad \begin{array}{l} t_i: CCP \\ t_f: \emptyset, \emptyset^P \end{array}$$

$$\begin{array}{l} X \begin{cases} \rightarrow f_1: B_1 \\ \rightarrow f_2: B_2 \end{cases} \\ X \begin{cases} \rightarrow \bar{f}_1: -B_1 \\ \rightarrow \bar{f}_2: -B_2 \end{cases} \end{array} \quad \left. \begin{array}{l} \Gamma = \Gamma_1 + \Gamma_2 \\ \bar{\Gamma} = \bar{\Gamma}_1 + \bar{\Gamma}_2 \end{array} \right\}$$

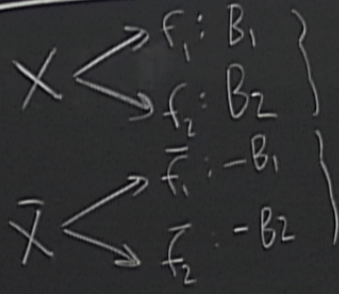






$$(f_i, \bar{f}_i) \xrightarrow{CCP} (\bar{f}_i, f_i) \quad \begin{array}{l} t_i: CCP \\ t_f: \emptyset, \emptyset^P \end{array}$$

$\bar{f}_i(t_i, p)$
 $\bar{f}_i(t_f, p)$
 $\bar{f}_i(t_i, p)$
 $\bar{f}_i(t_i, p)$



$$\begin{array}{l}
 \bar{\Gamma} = \bar{\Gamma}_1^r + \bar{\Gamma}_2^{(1-r)} \\
 \bar{\Gamma} = \bar{\Gamma}_1^{\#} + \bar{\Gamma}_2^{\#} \\
 \bar{\Gamma} \quad \bar{\Gamma} \quad (1-\bar{r})
 \end{array}$$

$$\begin{array}{l}
 n_x, n_{\bar{x}} \\
 \frac{n_x}{s}
 \end{array}$$

$$(f_i, \bar{f}_i) \xrightarrow{C, CP} (\bar{f}_i, f_i) \quad \begin{array}{l} t_i: CCP \\ t_f: \emptyset, \emptyset^P \end{array}$$

$$\begin{array}{l} X \begin{cases} \rightarrow f_1: B_1 \\ \rightarrow f_2: B_2 \end{cases} \\ \bar{X} \begin{cases} \rightarrow \bar{f}_1: -B_1 \\ \rightarrow \bar{f}_2: -B_2 \end{cases} \end{array} \quad \begin{array}{l} \bar{r} = \bar{r}_1 + \bar{r}_2 \\ \bar{r} = \bar{r}_1 + \bar{r}_2 \end{array}$$

$$\begin{array}{l} n_x, n_{\bar{x}} \\ \frac{n_x}{s} \Big|_i = \frac{n_B}{s_f} = \end{array}$$

$$(f_i, \bar{f}_i) \xrightarrow{C, CP} (\bar{f}_i, f_i)$$

t_i : CCP

t_f : \emptyset, \emptyset^P

$$\begin{array}{l} X \begin{cases} \rightarrow f_1: B_1 \\ \rightarrow f_2: B_2 \end{cases} \\ \bar{X} \begin{cases} \rightarrow \bar{f}_1: -B_1 \\ \rightarrow \bar{f}_2: -B_2 \end{cases} \end{array}$$

$$\begin{aligned} \Gamma &= \Gamma_1^r + \Gamma_2^{(1-r)} \\ \bar{\Gamma} &= \bar{\Gamma}_1^{\bar{r}} + \bar{\Gamma}_2^{(1-\bar{r})} \end{aligned}$$

$n_x, n_{\bar{x}}$

$$\frac{n_x}{S_i} = \frac{n_{\bar{x}}}{S_f} =$$

$$rB_1 + (1-r)B_2 + \bar{r}(-B_1) + (1-\bar{r})(-B_2)$$

$$(f_i, \bar{f}_i) \xrightarrow{C, CP} (\bar{f}_i, f_i)$$

$t_i: CCP$

$t_f: \emptyset, \emptyset^P$

$$\begin{array}{l} X \begin{cases} \rightarrow f_1: B_1 \\ \rightarrow f_2: B_2 \end{cases} \\ \bar{X} \begin{cases} \rightarrow \bar{f}_1: -B_1 \\ \rightarrow \bar{f}_2: -B_2 \end{cases} \end{array}$$

$$\begin{aligned} \Gamma &= \Gamma_1^r + \Gamma_2^{(1-r)} \\ \bar{\Gamma} &= \bar{\Gamma}_1^{\bar{r}} + \bar{\Gamma}_2^{(1-\bar{r})} \end{aligned}$$

$n_x, n_{\bar{x}}$

$$\frac{n_x}{S_i} = \frac{n_{\bar{x}}}{S_f} =$$

$$\frac{rB_1 + (1-r)B_2 + \bar{r}(-B_1) + (1-\bar{r})(-B_2)}{S}$$

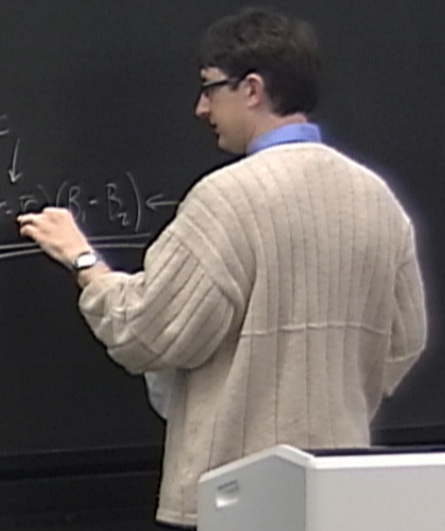
$$(f_i, \bar{f}_i) \xrightarrow{C, CP} (\bar{f}_i, f_i) \quad t_i: CCP$$

$t_f: C, CP$

$$\begin{array}{l}
 X \rightarrow \left. \begin{array}{l} f_1: B_1 \\ f_2: B_2 \end{array} \right\} \\
 \bar{X} \rightarrow \left. \begin{array}{l} \bar{f}_1: -B_1 \\ \bar{f}_2: -B_2 \end{array} \right\}
 \end{array}
 \quad
 \begin{array}{l}
 \Gamma = \Gamma_1 + \Gamma_2 \\
 \bar{\Gamma} = \bar{\Gamma}_1 + \bar{\Gamma}_2
 \end{array}$$

$$\frac{n_x}{s_x} = \frac{n_B}{s_f}$$

$$\frac{rB_1 + (1-r)B_2 + \bar{r}(-B_1) + (1-\bar{r})(-B_2)}{s} \propto \frac{c}{(r-\bar{r})(B_1-B_2)}$$



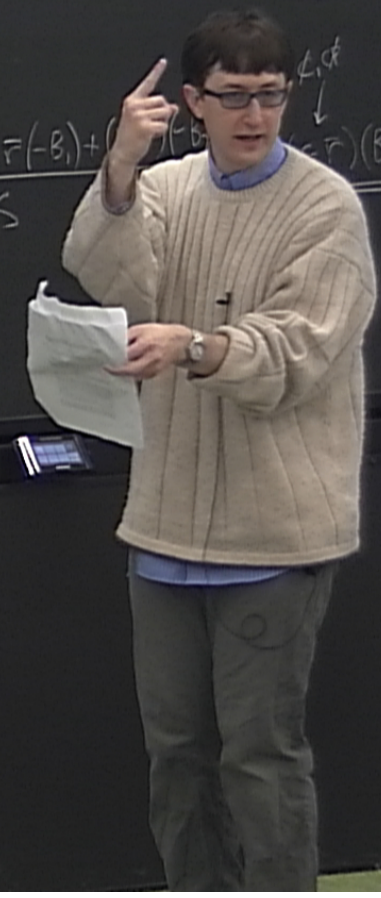
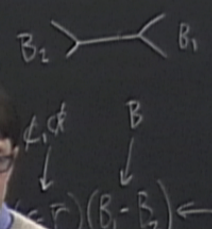
$$(f_i, \bar{f}_i) \xrightarrow{C, CP} (\bar{f}_i, f_i) \quad t_i: CCP$$

$t_f \notin \mathcal{P}$

$$\begin{array}{l}
 X \begin{cases} \rightarrow f_1: B_1 \\ \rightarrow f_2: B_2 \end{cases} \\
 \bar{X} \begin{cases} \rightarrow \bar{f}_1: -B_1 \\ \rightarrow \bar{f}_2: -B_2 \end{cases}
 \end{array}
 \quad
 \begin{array}{l}
 \Gamma = \Gamma_1 + \Gamma_2 \\
 \bar{\Gamma} = \bar{\Gamma}_1 + \bar{\Gamma}_2
 \end{array}$$

$$\frac{n_x}{s} \Big|_i = \frac{n_B}{s} \Big|_f$$

$$r B_1 + (1-r) B_2 + \bar{r} (-B_1) + \dots$$



$$(f_i, \bar{f}_i) \xrightarrow{CCP} (\bar{f}_i, f_i) \quad t_i: CCP$$

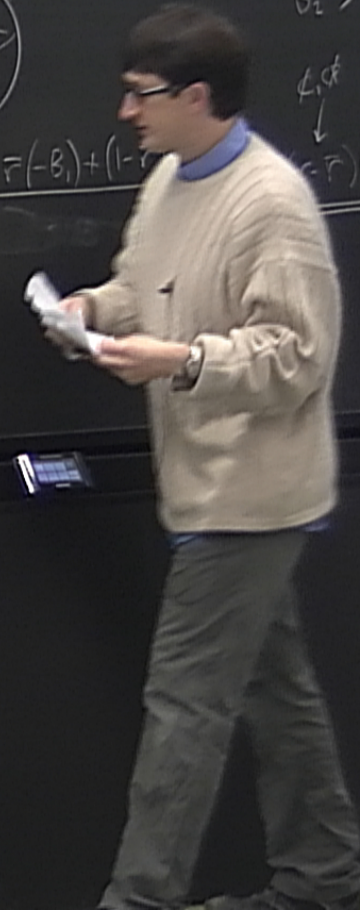
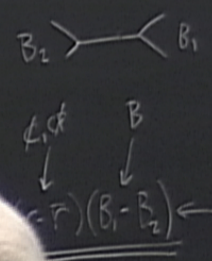
$t_f \notin \mathcal{P}$

$$\begin{array}{l}
 X \begin{cases} \rightarrow f_1: B_1 \\ \rightarrow f_2: B_2 \end{cases} \\
 \bar{X} \begin{cases} \rightarrow \bar{f}_1: -B_1 \\ \rightarrow \bar{f}_2: -B_2 \end{cases}
 \end{array}
 \quad
 \begin{array}{l}
 \Gamma = \Gamma_1 + \Gamma_2 \\
 \bar{\Gamma} = \bar{\Gamma}_1 + \bar{\Gamma}_2
 \end{array}$$

$$\frac{n_x}{s} \Big|_i = \frac{n_B}{s} \Big|_f$$



$$rB_1 + (1-r)B_2 + \bar{r}(-B_1) + (1-\bar{r})(-B_2)$$



$$(f_i, \bar{f}_i) \xrightarrow{C, CP} (\bar{f}_i, f_i) \quad t_i: CCP$$

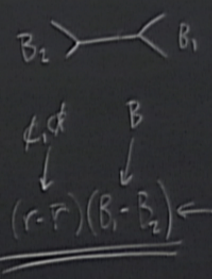
$t_f \neq \emptyset, \neq \emptyset$

$$\begin{matrix} X & \begin{matrix} \rightarrow & f_1: B_1 \\ \rightarrow & f_2: B_2 \end{matrix} \\ \bar{X} & \begin{matrix} \rightarrow & \bar{f}_1: -B_1 \\ \rightarrow & \bar{f}_2: -B_2 \end{matrix} \end{matrix} \quad \left. \begin{matrix} \Gamma = \Gamma_1 + \Gamma_2 \\ \bar{\Gamma} = \bar{\Gamma}_1 + \bar{\Gamma}_2 \end{matrix} \right\} \begin{matrix} r & (1-r) \\ \# & \# \\ \# & \# \\ (-r) & \end{matrix}$$

$$\frac{n_x}{s} \Big|_i = \frac{n_B}{s} \Big|_f$$



$$rB_1 + (1-r)B_2 + \bar{f}_1 = (-B_2) \propto (r-f)(B_1 - B_2) \leftarrow$$



$$(f_i, \bar{f}_i) \xrightarrow{C, CP} (\bar{f}_i, f_i) \quad t_i: CCP$$

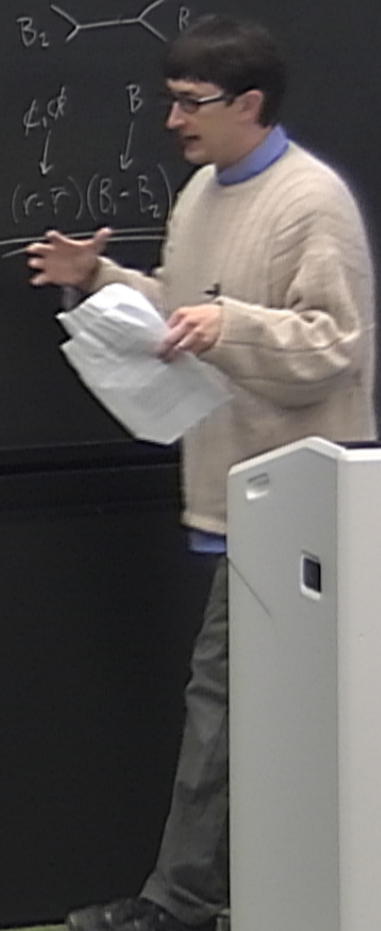
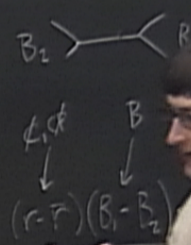
$t_f: \emptyset, \emptyset^P$

$$\begin{array}{l}
 X \begin{cases} \rightarrow f_1: B_1 \\ \rightarrow f_2: B_2 \end{cases} \\
 \bar{X} \begin{cases} \rightarrow \bar{f}_1: -B_1 \\ \rightarrow \bar{f}_2: -B_2 \end{cases}
 \end{array}
 \quad
 \begin{array}{l}
 \Gamma = \Gamma_1 + \Gamma_2 \\
 \bar{\Gamma} = \bar{\Gamma}_1 + \bar{\Gamma}_2
 \end{array}$$

$$\frac{N_x}{S} \Big|_i = \frac{N_B}{S} \Big|_f = \frac{N_x}{S}$$

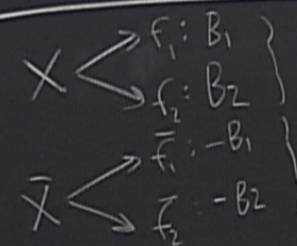


$$rB_1 + (1-r)B_2 + \bar{r}(-B_1) + (1-\bar{r})(-B_2) \propto (r-\bar{r})(B_1 - B_2)$$



$$(f_i, \bar{f}_i) \xrightarrow{C, CP} (\bar{f}_i, f_i) \quad t_i: CCP$$

$t_f \notin \mathcal{P}$



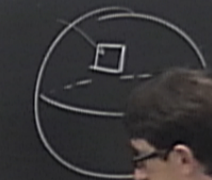
$$\Gamma = \Gamma_1 + \Gamma_2$$

$$\Gamma'' = \Gamma_1 + \Gamma_2$$

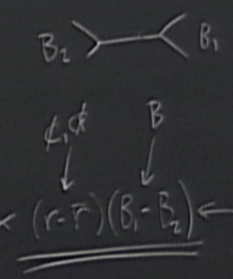
$$N_x, N_{\bar{x}}$$

$$\frac{N_x}{S} = \frac{NB}{S_f}$$

$$\frac{N_{\bar{x}}}{S}$$

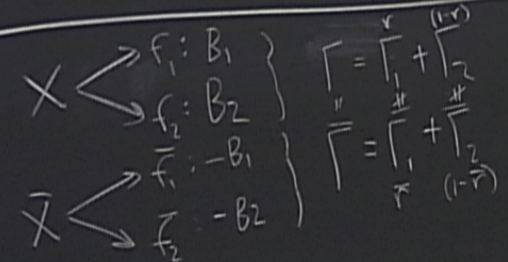


$$B_1 + (1-r)B_2 + \dots$$

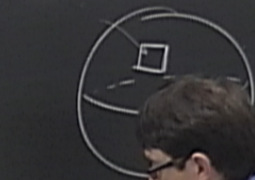


$$\propto (r-F)(B_1 - B_2)$$

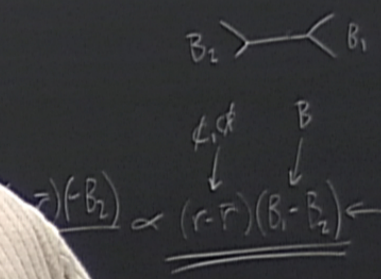
$$(f_i, \bar{f}_i) \xrightarrow{CCP} (\bar{f}_i, f_i) \quad t_i: CCP$$

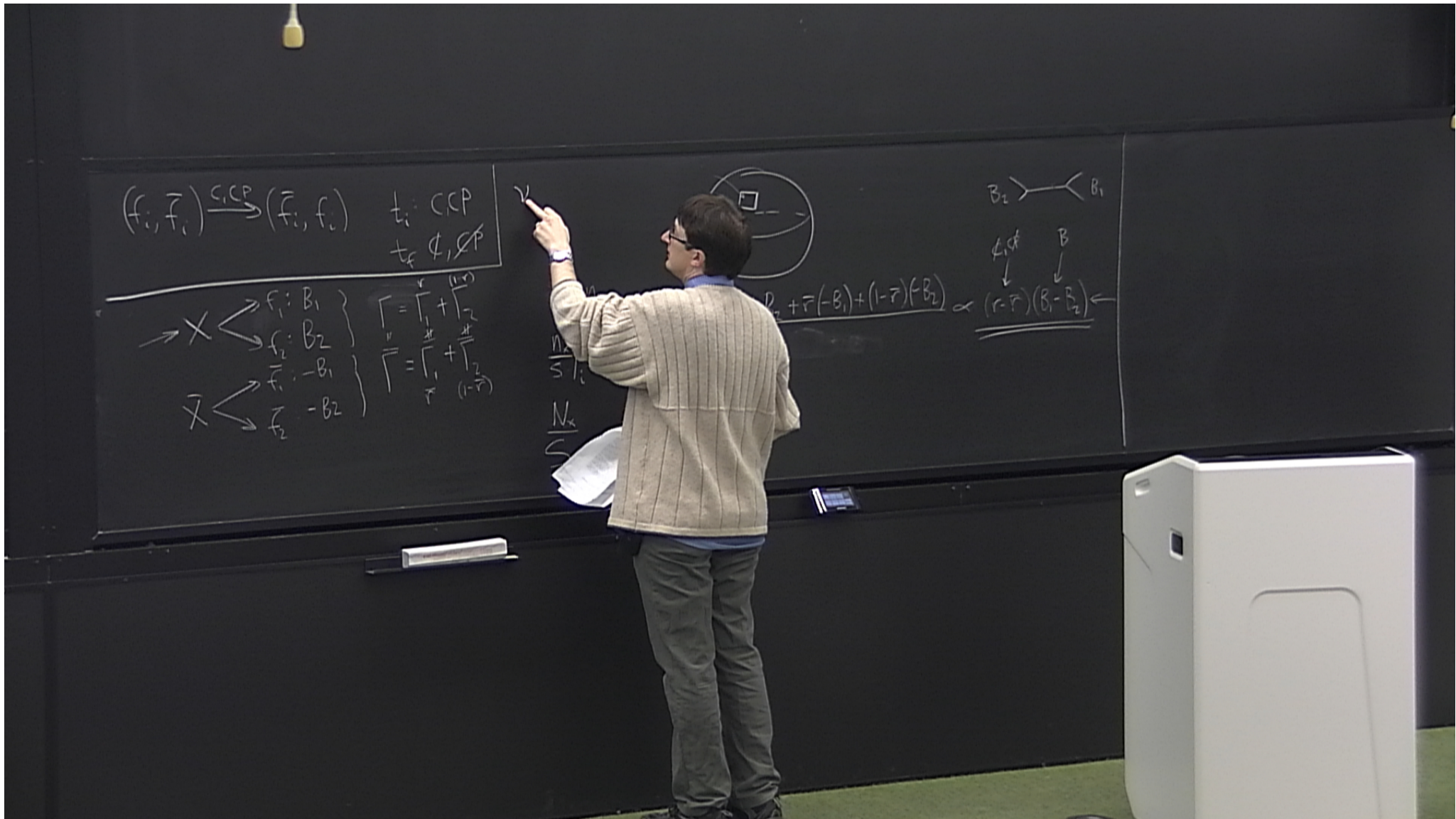


$$\frac{N_x}{S} = \frac{N_{\bar{x}}}{S}$$



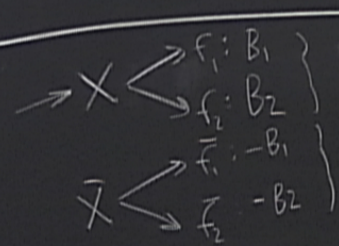
$$rB_1 + (1-r)B_2$$





$$(f_i, \bar{f}_i) \xrightarrow{CCP} (\bar{f}_i, f_i)$$

t_i : CCP
 t_f : CP, CP

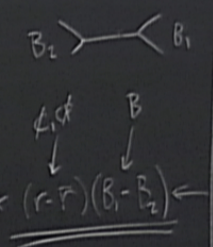


$$\bar{r} = \frac{r}{1+r} + \frac{(1+r)}{1+r}$$

$$\bar{r} = \frac{r}{1+r} + \frac{1}{1+r}$$



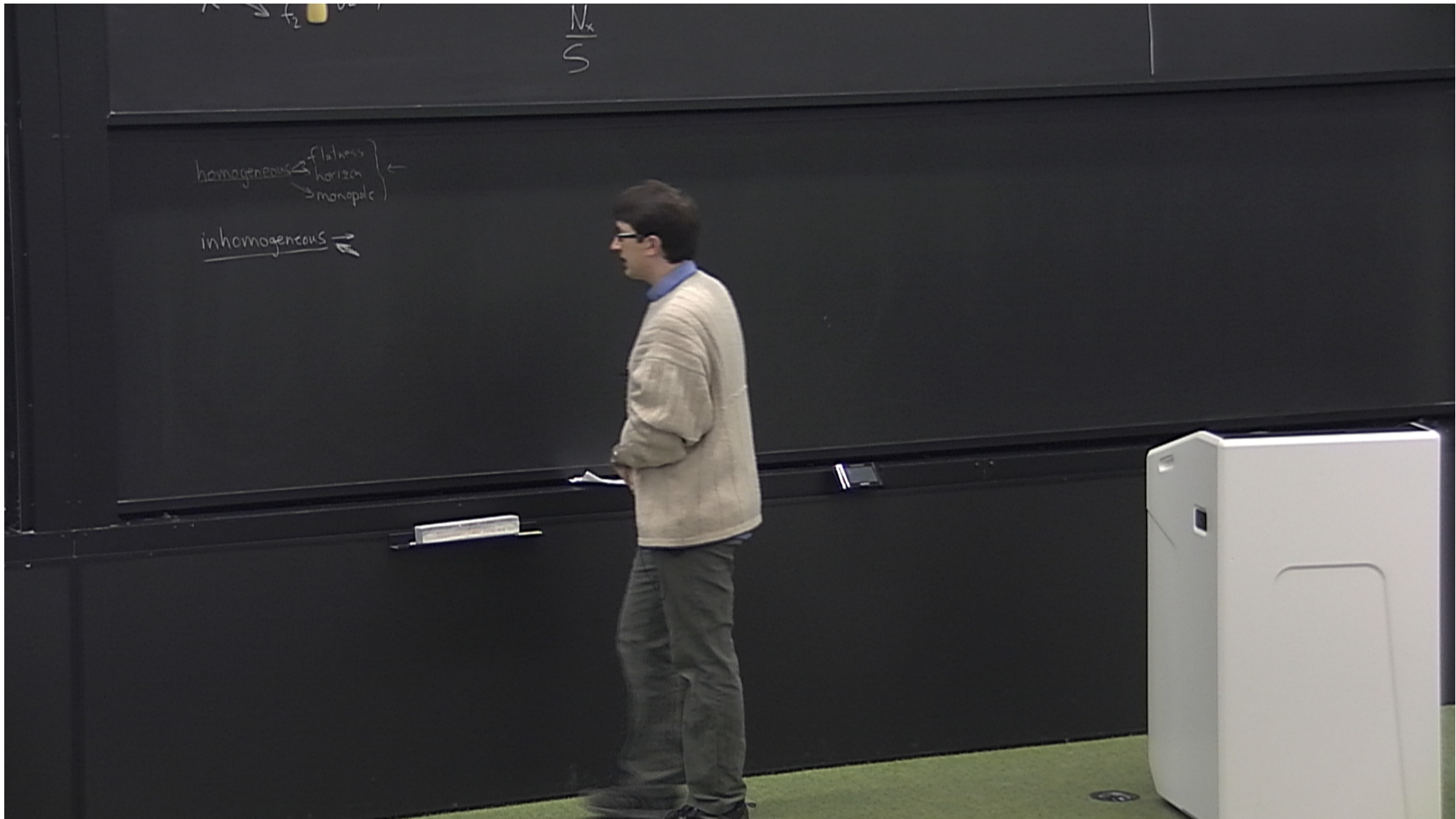
$$D_2 + \bar{r}(-B_1) + (1-\bar{r})(-B_2) \propto \frac{r-r}{(1+r)}(B_1 - B_2)$$

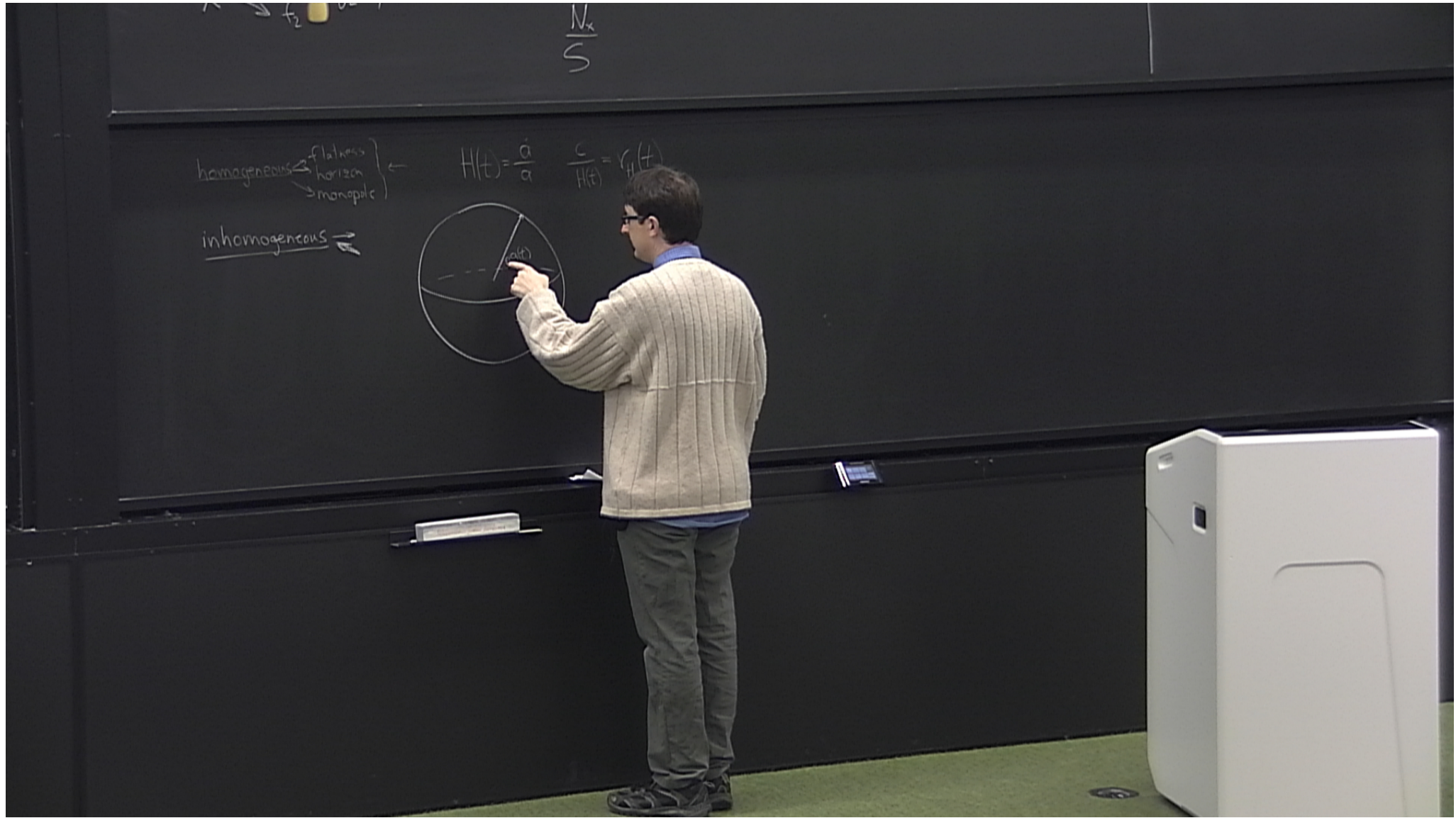


f_2 $\frac{N_x}{S}$

homogeneous → flatness
 → horizon
 → monopole ←

inhomogeneous →

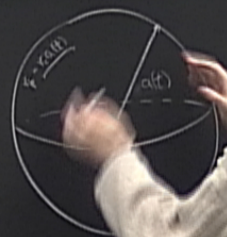




t_2 $\frac{N_x}{S}$

homogeneous $\left\{ \begin{array}{l} \rightarrow \text{flatness} \\ \rightarrow \text{horizon} \\ \rightarrow \text{monopile} \end{array} \right\}$ $H(t) = \frac{a}{a}$ $\frac{c}{H(t)} = r_{ii}(t)$ $\boxed{\frac{1}{at}}$

inhomogeneous \rightarrow



homogeneous $\left\{ \begin{array}{l} \rightarrow \text{flatness} \\ \rightarrow \text{horizon} \\ \rightarrow \text{monopole} \end{array} \right\}$

inhomogeneous \rightarrow

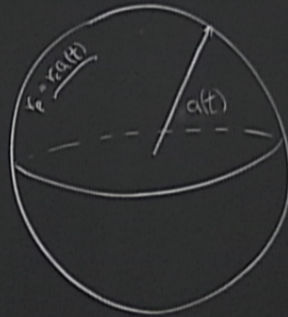
$$H(t) = \frac{\dot{a}}{a}$$

$$\frac{c}{H(t)} = r_H(t)$$

$$\frac{1}{aH}$$

$$a(t)$$

$$\ddot{a} < 0 \quad \frac{1}{aH} \uparrow$$



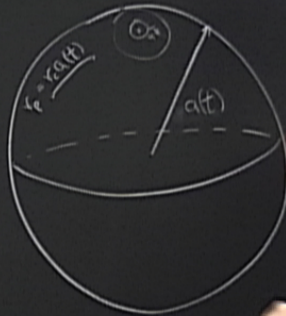
homogeneous → flatness
horizon
→ monopole

inhomogeneous →

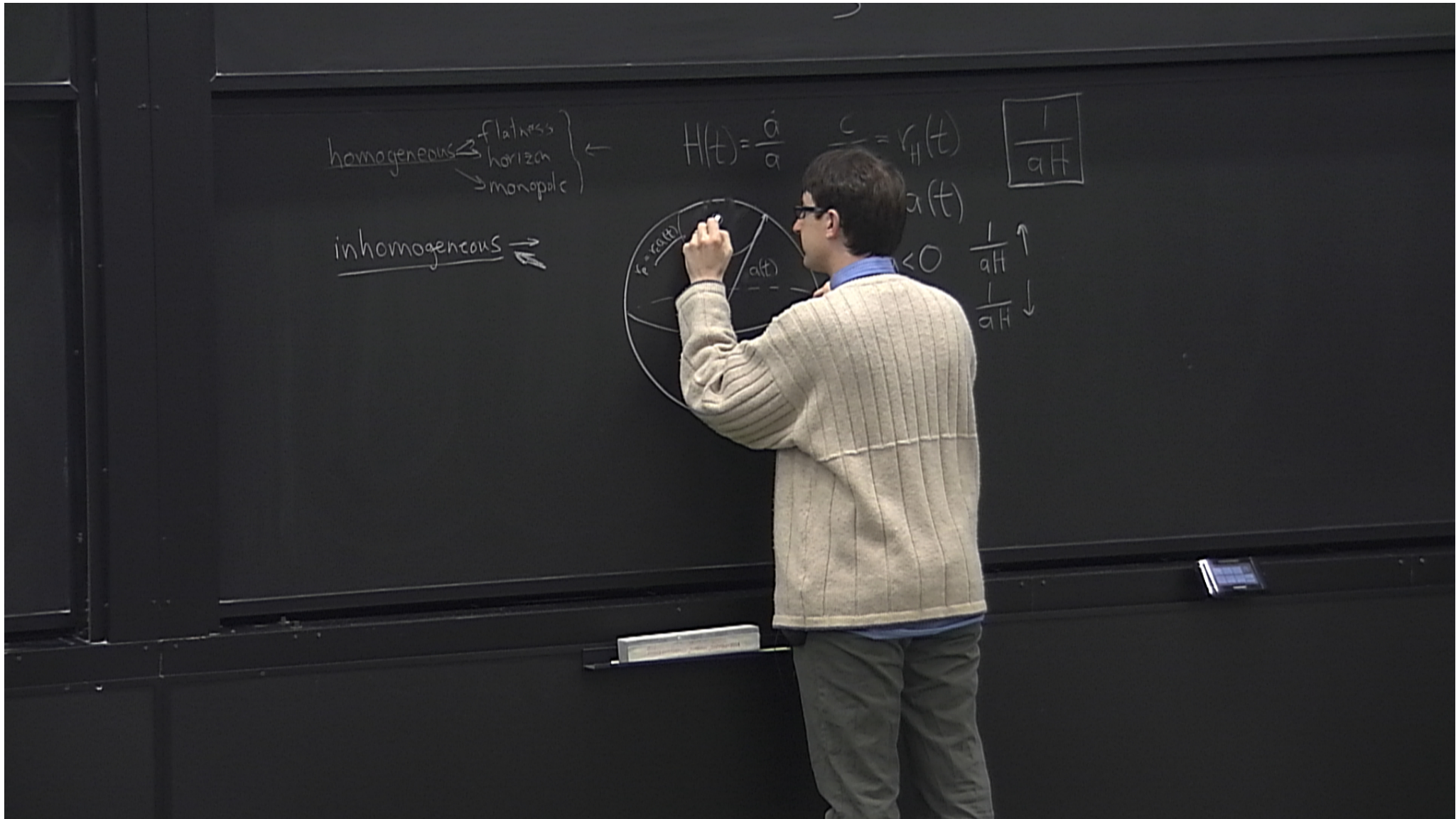
$$H(t) = \frac{\dot{a}}{a}$$

$$\frac{c}{H(t)} = r_H(t)$$

$$\frac{1}{aH}$$



$$\frac{1}{aH}$$



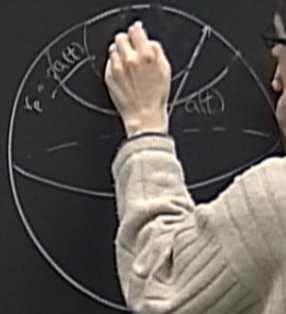
homogeneous $\left\{ \begin{array}{l} \rightarrow \text{flatness} \\ \rightarrow \text{horizon} \\ \rightarrow \text{monopole} \end{array} \right\}$

inhomogeneous \rightarrow

$$H(t) = \frac{\dot{a}}{a}$$

$$\frac{c}{H} = r_H(t)$$

$$\frac{1}{aH}$$



$$r_H(t)$$

$$0$$

$$\frac{1}{aH} \uparrow$$

$$\frac{1}{aH} \downarrow$$