

Title: Phase-field model for cellular monolayers : a cancer cell migration studyauthors : Benoit Palmieri and Martin Grant

Date: Dec 05, 2013 05:25 PM

URL: <http://pirsa.org/13120037>

Abstract: Recent experimental work [1] suggests that the increased motility of cancer cells observed in a confluent monolayer of normal cells is due to the mechanical mismatch between the two cell types. The soft cancer cell undergoes large deformations and can squeeze between small channels defined by the space between the normal cells. We developed a phase-field model description of cellular monolayers to study such a process. The system is setup as a free-boundary problem where each cell is a highly deformable soft body [2]. The motion of each cell is described by a persistent random walk where the velocities and persistent times can be obtained from experimental observations. Our model is used to test the hypothesis that the mechanical mismatch alone increases the motility of softer cells when all other parameters are the same.[1] Lee et al. Biophys. J. vol. 102 p. 2731 (2012).[2] Najem et al. Europhys. Lett. vol. 102 p. 16001 (2013).

Phase-field model for cellular monolayers : a cancer cell migration study

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McGill

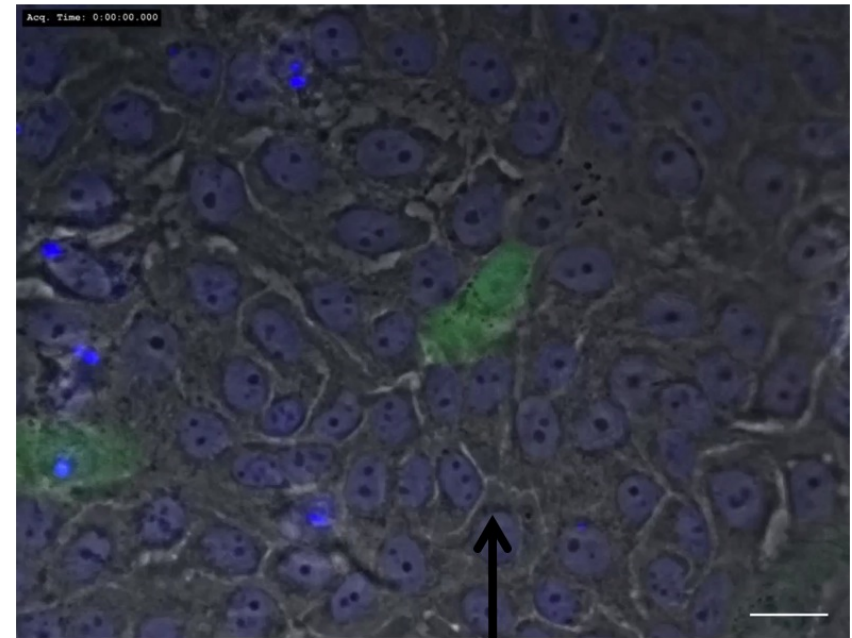
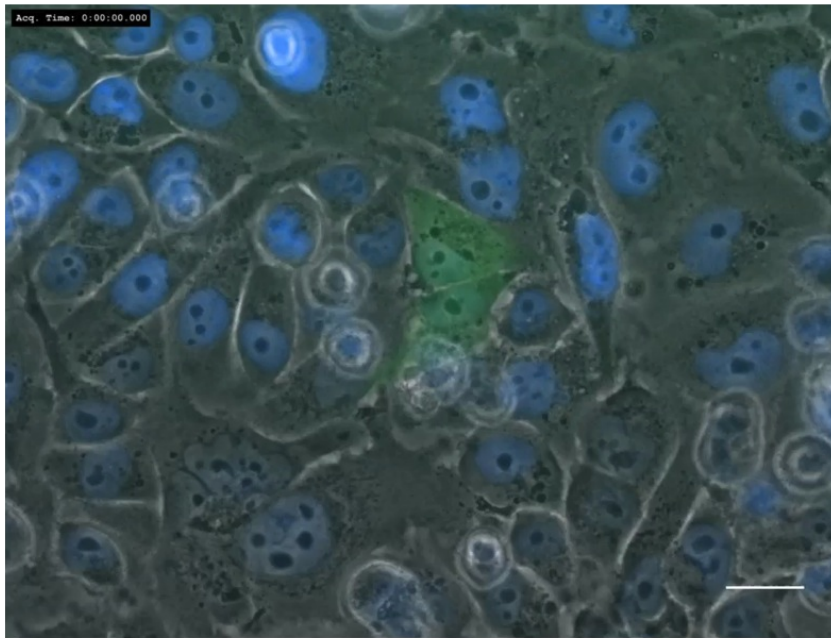
Experiments : Motile Cancer Cells in a monolayer of Normal or other Cancer cells

Lee et al., Biophys. J., **102**, 2732 (2012)

Cancer cell monolayer

Cancer cell in a monolayer of normal cells

Acquisition time - hours



Increased Motility

Phase-field model for Cells: Highly deformable elastic bodies

$$\mathcal{F}_n = \int dx \int dy \left[\sum_n \{ \gamma_n (\nabla \phi_n)^2 + a_n \phi_n^2 (\phi_n - 1)^2 \} + \sum_{n,m \neq n} \kappa \phi_n^2 \phi_m^2 \right]$$

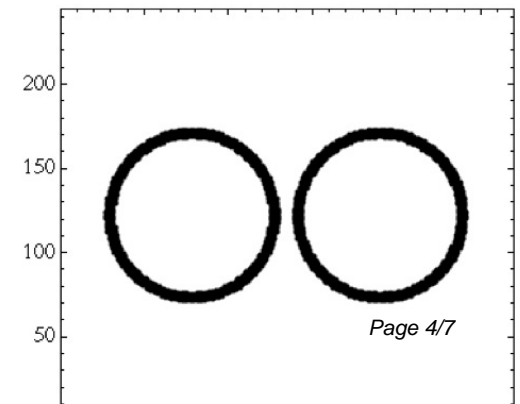
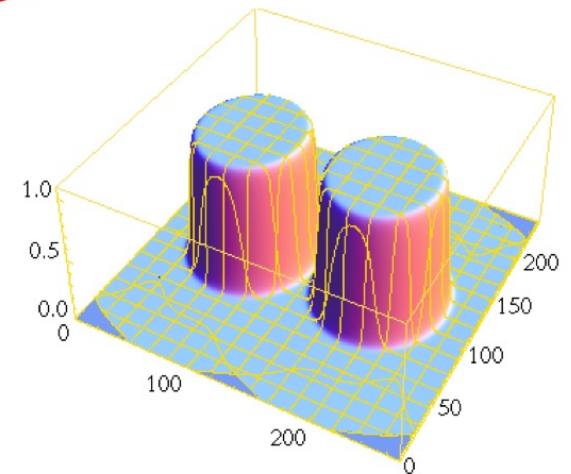
Energy cost for overlapping cells

For each cell $\phi_n = 1$ inside the cell
 $\phi_n = 0$ outside the cell

Cell Interface width: $\lambda_n = \left(\frac{30\gamma_n}{a_n} \right)^{1/2}$

Deformation of cell boundary: $R'_n = R_n + \epsilon \cos k\theta$

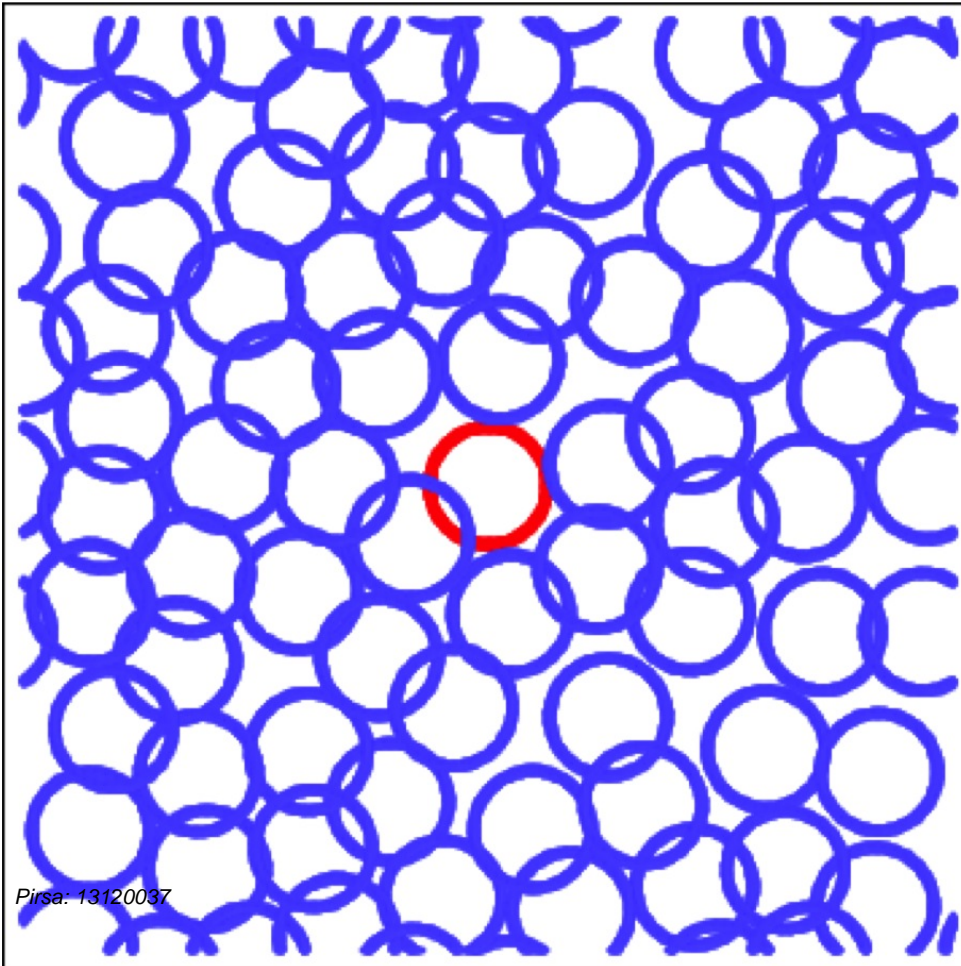
$$\Delta \mathcal{F}_{def} = \frac{\epsilon^2 (k^2 - 1/2) \pi}{R_n} \left(\frac{\gamma_n a_n}{30} \right)^{1/2}$$



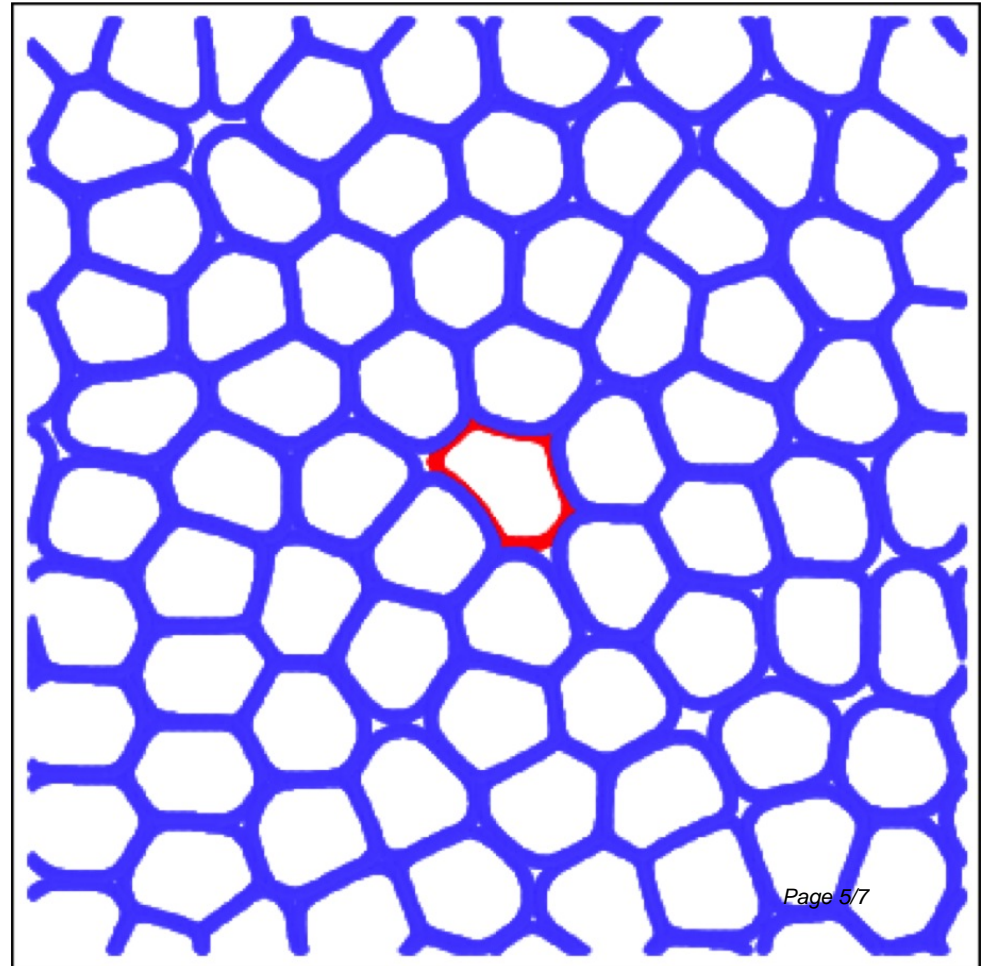
Numerical Simulations : all model parameters can be measured/estimated by experiments

Red cell (cancer cell) is 3 times softer than the others

Aging – no velocity



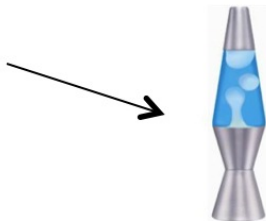
Persistent Random walk for each cell



Conclusions

Future avenues:

- 1 soft cell vs all normal cells.
- Follow cell deformation as it migrates.
- Cell internal degrees of freedom.
- Cell-Cell adhesion
- Other applications
 1. Soft glasses¹.
 2. Confluent monolayers response to external stresses and forces².
 3. ...



Talk to me

Acknowledgement:

- Denis Wirtz (Johns Hopkins)
- Sam Safran (Weizmann)
- Nir Gov (Weizmann)



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Phase-field model for Cells: Elastic bodies with a free-boundary

Dynamics: (Conserved Field)^{1,2}

$$\frac{\partial \phi_n}{\partial t} + \mathbf{v}_n \cdot \nabla \phi_n = D_n \nabla^2 \frac{\delta \mathcal{F}}{\delta \phi_n}$$

Cell Shape
rearrangement

Cell translation : Persistent Random Walk³

$$\gamma \mathbf{v}_n = \gamma \mathbf{v}_0^\dagger + \underbrace{\int dx \int dy \, 4\phi_n (\nabla \phi_n) \sum_{m \neq n} \kappa \phi_m^2}_{\text{Force due to the other cells}}$$

\mathbf{v}_0^\dagger has a constant amplitude v_0 .

Random time between reorientation events:
(exponential distribution)

$$P(t_r)dt_r = \frac{1}{\tau}e^{-t_r/\tau}dt_r$$