

Title: Insightful supersymmetry

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Abstract: It has recently been realized that some studies of supersymmetric gauge theories, when properly interpreted, lead to insights whose importance transcends supersymmetry. I will illustrate the insightful nature of supersymmetry by two examples having to do with the microscopic description of the thermal deconfinement transition, in non-supersymmetric pure Yang-Mills theory and in QCD with adjoint fermions. A host of strange ``topological" molecules will be seen to be the major players in the confinement-deconfinement dynamics. Interesting connections between topology, ``condensed-matter" gases of electric and magnetic charges, and attempts to interpret the divergent perturbation series will emerge. Much of the presentation will be aimed at non-experts.

Insightful supersymmetry

Erich Poppitz



in collaboration with

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I. deconfinement

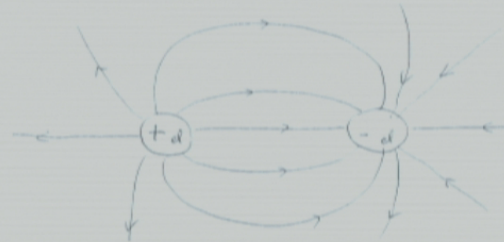
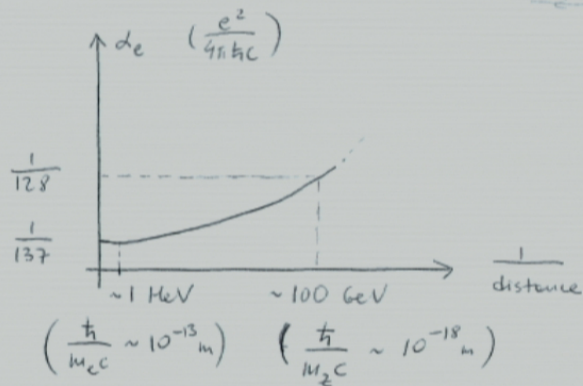
what is it and how do we study it?

QCD - theory of the strong interactions:

quarks and gluons, discovered in 1970s

asymptotic freedom - antiscreening, reverse of QED

QED:



Coulomb-like field
at **long** distances

I. deconfinement

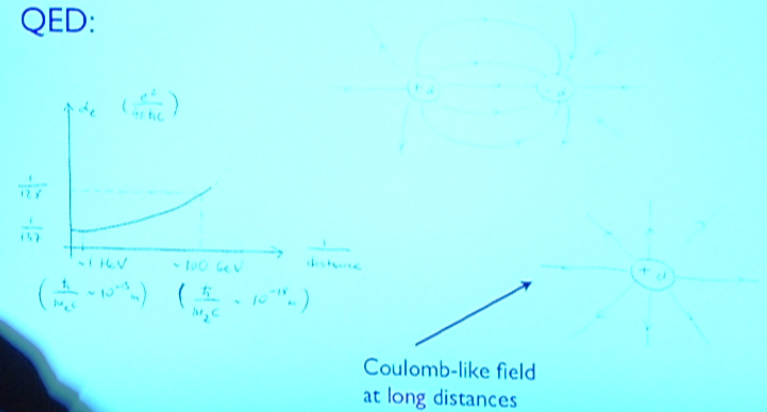
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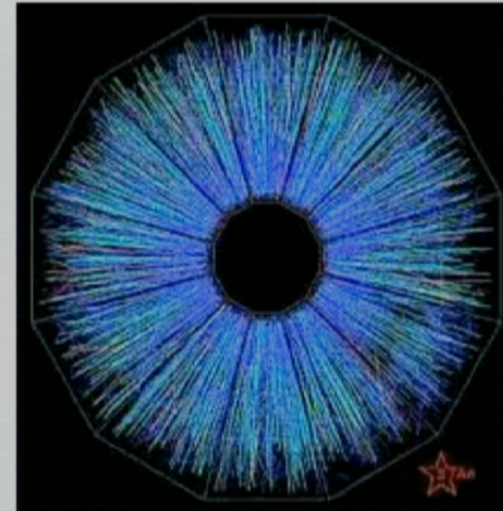
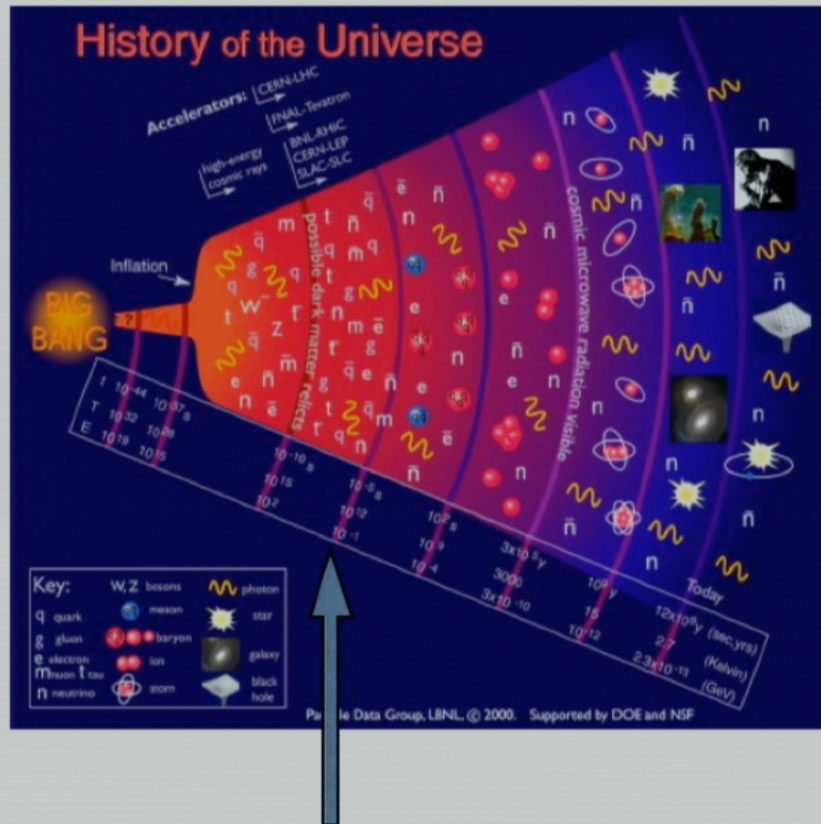
quarks and gluons, discovered in 1970s

asymptotic freedom - antiscreening, reverse of QED

QED:



What happens when quarks and gluons are “heated up”?



$$k_B T \sim 100 \text{ MeV} \quad T \sim 10^{12} \text{ K}$$

(10^{-10} s after big bang)

- quarks and gluons are
“liberated” or “deconfined”

Why does deconfinement occur? - a picture and an estimate...

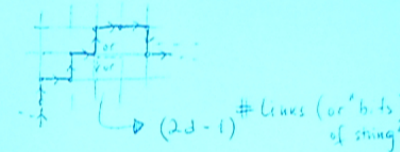
assume YM theory confines, hence it is a theory of chromoelectric fluxes

energy of a flux tube of length L

$$E \sim L\sigma$$

entropy of a flux tube of length L

$$S \sim k_B \log(2d - 1)^{L\sqrt{\sigma}}$$



$$F = E - TS \sim L\sigma - k_B T L \sqrt{\sigma} \log(2d - 1)$$

Z diverges at T_c $k_B T_c \sim \sqrt{\sigma} \sim 100 \text{ MeV}$

above T_c entropy dominates strings "melt" (or "condense"), confinement lost...

... despite "success" - this is a "picture", quite far from a "theory" (QCD)

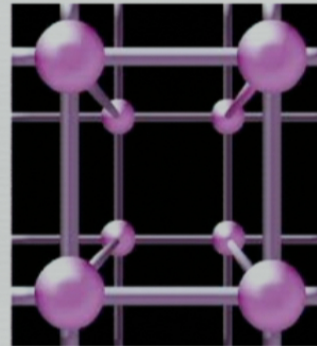
"picture" becomes a "theory" - but of compact lattice $U(1)$
at strong coupling in the Villain representation [Polyakov; Susskind (1970)]

How do people **actually** study deconfinement?

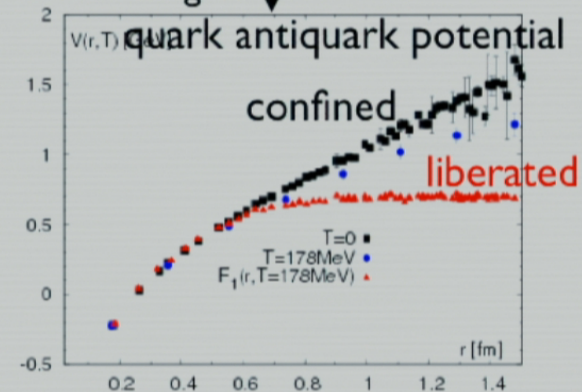
experiment: real or lattice, *i.e. numerical*



- description of hydrodynamic flow
- equation of state...

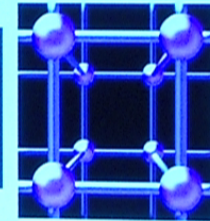
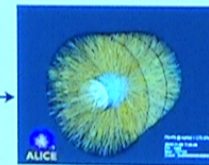


e.g.:

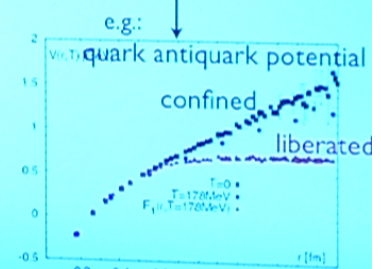


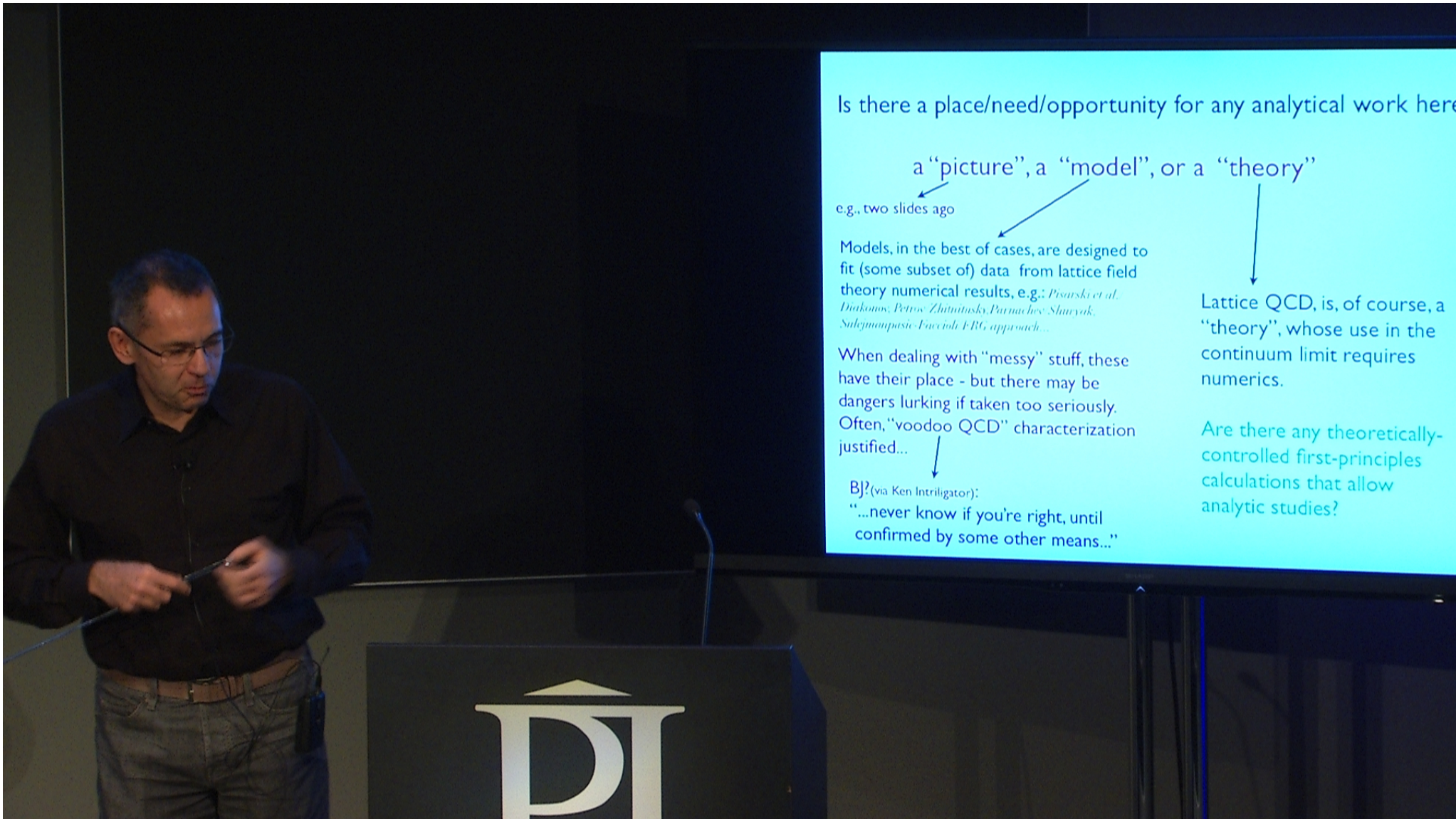
How do people actually study deconfinement?

experiment: real or lattice, *i.e. numerical*



- description of hydrodynamic flow
- equation of state...





Is there a place/need/opportunity for any analytical work here?

a “picture”, a “model”, or a “theory”

e.g., two slides ago

Models, in the best of cases, are designed to fit (some subset of) data from lattice field theory numerical results, e.g.: *Pisarski et al./* *Diakonov, Petrov/Zhitnitsky; Parnachev/Shuryak,* *Sulejmanpasic-Faccioli/FRG approach...*

When dealing with “messy” stuff, these have their place - but there may be dangers lurking if taken too seriously. Often, “voodoo QCD” characterization justified...

BJ? (via Ken Intriligator):

“...never know if you’re right, until confirmed by some other means...”

Lattice QCD, is, of course, a “theory”, whose use in the continuum limit requires numerics.

Are there any theoretically-controlled first-principles calculations that allow analytic studies?

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Are there any theoretically-controlled first-principles calculations that allow analytic studies?

There are a only a few of these.

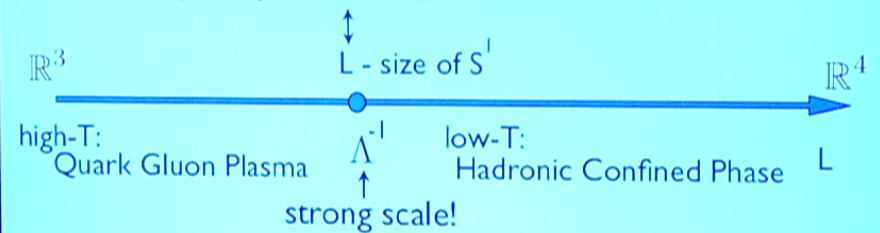
None of them captures all features of real QCD.

So why do we care?

Before answering, recall some facts about thermal theories.

Thermal partition function is (without fermions):

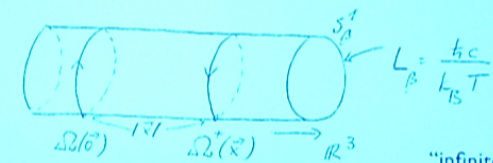
$$Z(\beta) = \text{tr}[e^{-\beta H}], \quad \beta = 1/T = \text{radius of } S^1 \quad \mathbb{R}^3 \times S^1$$



a static quark probe

$$\Omega = \text{tr} \mathcal{P} \exp[i \int_{S^1} A_4 dx^4]$$

Wilson/Polyakov loop

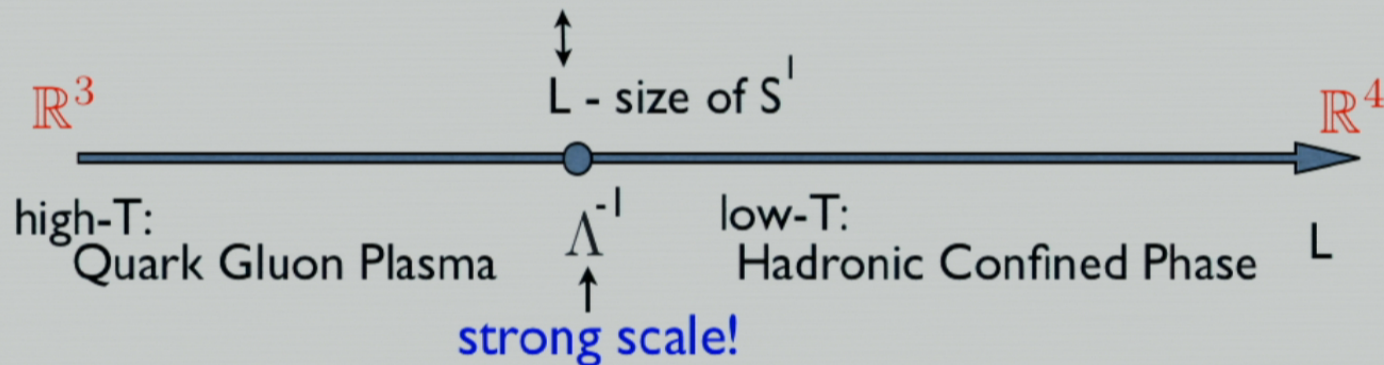


$$\langle \Omega^\dagger(\vec{x}) \Omega(0) \rangle \sim e^{-\frac{V(|\vec{x}|)}{T}} \begin{cases} \text{confined} & e^{-\frac{\sigma|\vec{x}|}{T}} \rightarrow 0 \\ \text{deconfined} & e^{-\frac{m_e|\vec{x}|}{T}} \rightarrow 1 \end{cases} \quad \text{hence} \quad \begin{cases} \langle \Omega \rangle = 0 & \text{confined} \\ \langle \Omega \rangle \neq 0 & \text{deconfined} \end{cases}$$

"infinite F_{quark} "

Thermal partition function is (without fermions):

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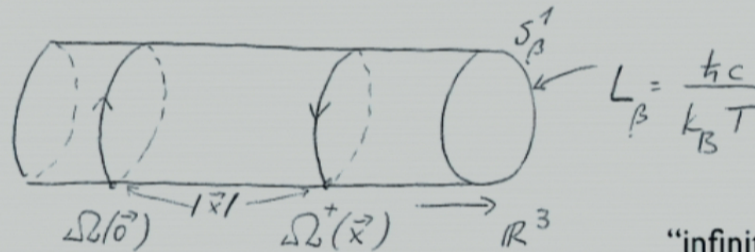
$$\Omega = \text{tr} \mathcal{P} \exp[i \int_{S^1} A_4 dx^4]$$

Wilson/Polyakov loop

$$\bar{q} \text{ at } \vec{x} \quad q \text{ at } \vec{0}$$

$$\langle \Omega^\dagger(\vec{x}) \Omega(0) \rangle \sim e^{-\frac{V(|\vec{x}|)}{T}}$$

confined $\rightarrow e^{-\frac{\sigma|\vec{x}|}{T}} \rightarrow 0$ as $x \rightarrow \infty$
 deconfined $\rightarrow e^{-\frac{e^{-m_e}|\vec{x}|}{|\vec{x}|T}} \rightarrow 1$ as $x \rightarrow \infty$



"infinite F_quark"

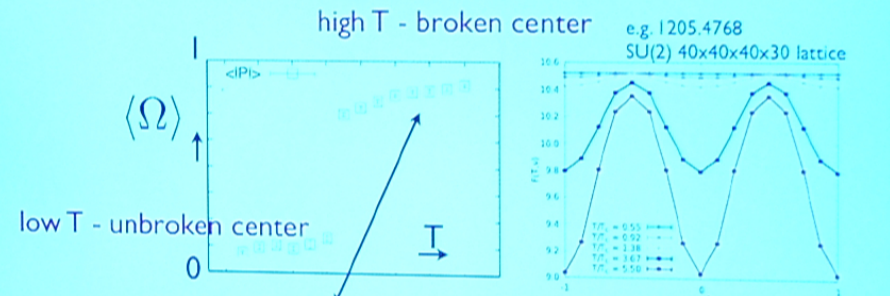
$$\langle \Omega \rangle = 0 \quad \text{confined}$$

$$\langle \Omega \rangle \neq 0 \quad \text{deconfined}$$

in SU(N) theory without fundamentals, deconfinement =
 breaking of global Z_N center symmetry ["gauge transform" periodic up to center]

$$\Omega_{\text{fund}} \xrightarrow{z \in Z_N} z \Omega_{\text{fund}}$$

$$\Omega = \text{tr} \mathcal{P} \exp \left[i \int_{S^1} A_4 dx^4 \right]$$



$T \gg T_c$ behavior has been understood for 30 years

[Gross, Pisarski, Yaffe, 1981]

High-T perturbation theory good, gives one-loop $V(\text{pert})$, favors center-broken vacuum, e.g.

$$V_{\text{pert}}(\Omega) = -\frac{2}{\pi^2 \beta^4} \sum_{n=1}^{\infty} \frac{1}{n^4} |\text{tr} \Omega^n|^2 (1 + O(g^2))$$

$$\Omega = \frac{1}{2} \text{Tr} \begin{pmatrix} e^{i\pi\nu} & 0 \\ 0 & e^{-i\pi\nu} \end{pmatrix}$$

high-T:
 coinciding
 eigenvalues

I. Gauge-gravity duality [many, after Witten 1998, ...]

pro: semiclassical string theory provides a weak-coupling description of strongly-coupled gauge theory

deconfinement=Hawking-Page

useful macroscopically (especially out-of-equilibrium)

con: comes with extra baggage - non decoupling KK modes;
no asymptotic freedom;
microscopic connection ?

2. $S^1 \times S^3$ compactifications [Aharony, Marsano, Minwalla, Papadodimas, van Raamsdonk, 2003-5]

↙ ↘
thermal non-thermal

pro: at small S^3 , a weakly coupled matrix model

low-T: Vandermonde repulsion of EVs

high-T: pert. attraction of Polyakov loop EVs

con: thermodynamic limit means large-N transition only

These authors rejected the possibility of finding a weak-coupling transition at infinite volume...

such a description has been found:

3. $R^2 \times S^1 \times S^1$ compactifications

non-thermal \leftrightarrow thermal

[Simic, Unsal 2010
Unsal 2012]

Anber, EP, Unsal 2011
Anber, Collier, EP 2012
Anber, Collier, Strimas-Mackey,
Teeple, EP 2013]

"deformed" pure-YM

"QCD(adj)" = YM with many
massless adjoint Weyl fermion

(~ large-N limit of QCD with fundamental
quarks via some large-N "orientifold" equivalences...)

pro: at small S^1 , map 4d thermal gauge theory to a 2d spin system - "affine"
XY spin models related to cond. mat. systems: e.g., 2d triangular lattice
crystal melting for $SU(3)(\text{adj})$ - or more general new stat-mech models

con: abelianized, $L < \infty$

nonetheless (I think) fascinating systems:

2d "gases" of el. and m. charged particles, with Aharonov-Bohm
interactions, inheriting the symmetries of their respective 4d gauge
theories and showing a deconfinement transition [far from all is understood!]

In the process of unraveling the above map, SUSY played a crucial role...

- to be explained later; note the $nf=1$ adjoint theory is $N=1$ SYM -

4. $\mathbb{R}^3 \times S^1$ compactifications of SYM*

(non-) thermal

[Schaefer, Unsal, EP 1205.0290, 1212.1238
Anber 1302.2641; Sulejmanpasic, EP 1307.1317;
early remarks in Unsal, Yaffe 1006.2101]

DEFINITIONS:

1

super YM = “SYM” = YM + massless quark, a triplet of SU(2), aka “gaugino”

fields: gauge bosons + gauginos; Z_4 chiral symmetry

2

SYM* = SYM + mass for the triplet quark, i.e. with a “gaugino mass” m

supersymmetry and Z_4 chiral symmetry **explicitly broken** by m

we study SYM* on $\mathbb{R}^3 \times S^1_L$ with periodic (supersymmetric, non-thermal)
boundary condition for gaugino

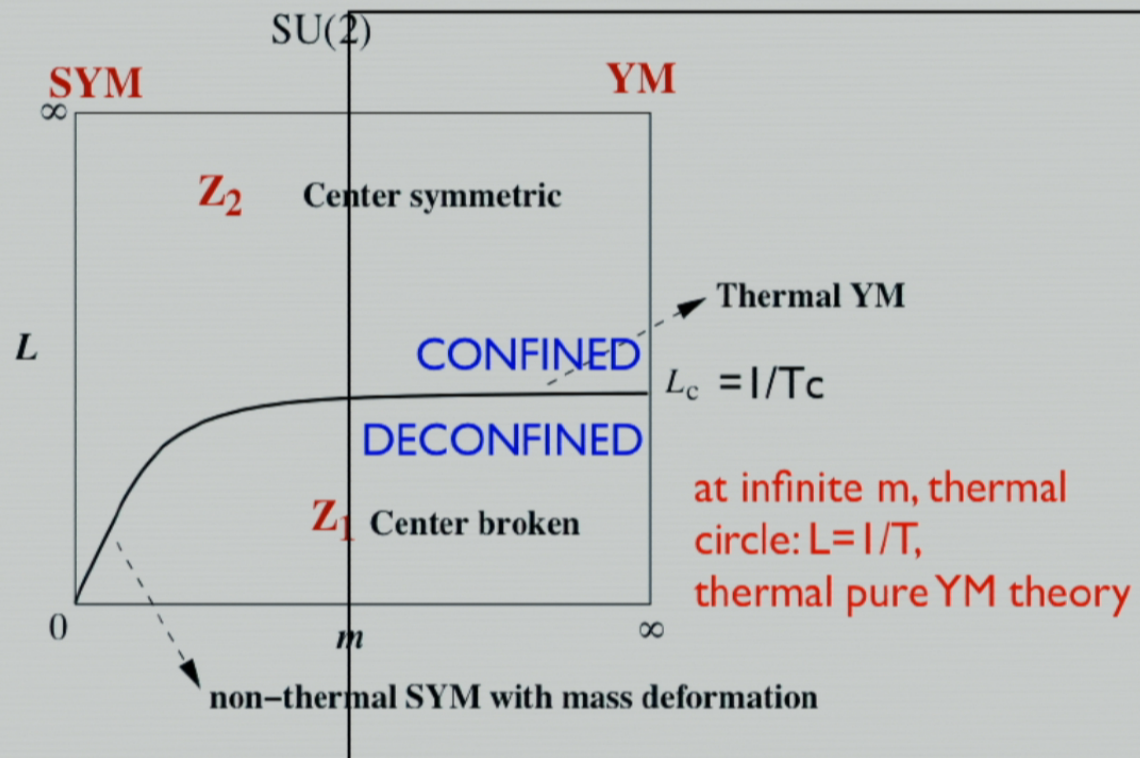
there are only two parameters to vary: L and m Z_2 center symmetry- S^1_L

the theory is asymptotically free with a **strong scale!**

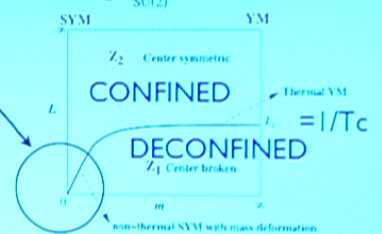
$$\Lambda \quad \left(\frac{m}{\Lambda} \quad \Lambda L \right)$$

4. $R^3 \times S^1$ compactifications of SYM*

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I will tell you how this part of the phase diagram comes about.



What is the role of SUSY?

theory is weakly coupled at small L - abelian!, not just asymptotic freedom
thus

allows us to have calculable non-perturbative effects

$$\text{roughly} \sim e^{-\frac{\mathcal{O}(1)}{g^2}}$$

and

calculable perturbative effects - which are suppressed by m -
so the two can compete and result in a calculable transition

$$\text{roughly} \sim g^2 m$$

major players: monopole-instanton "BPS" and twisted "KK" [Piljin Yi, Kimeyong Lee, 1997]

and various "topological molecules made thereof"

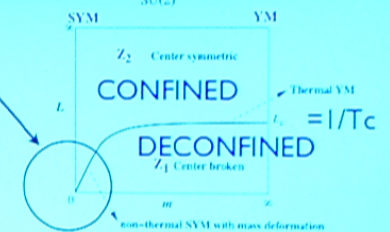


[Unsal 2007, Unsal EP 2011]

2. topological

... how this part of the phase diagram comes about ...

- small-L theory is abelian
SU(2) breaks to U(1)
- no light charged states
(remember this is T=0 quantum transition!)



relevant bosonic fields: A_4 - gauge field in compact direction -
and A_i - 3d gauge field - in the unbroken U(1) of SU(2), equivalent to:

- σ - 3d dual to A_i = "dual photon" (potential for magnetic charge)
- ϕ - deviation of A_4 from center symmetric value $\text{Tr } \Omega = 0$

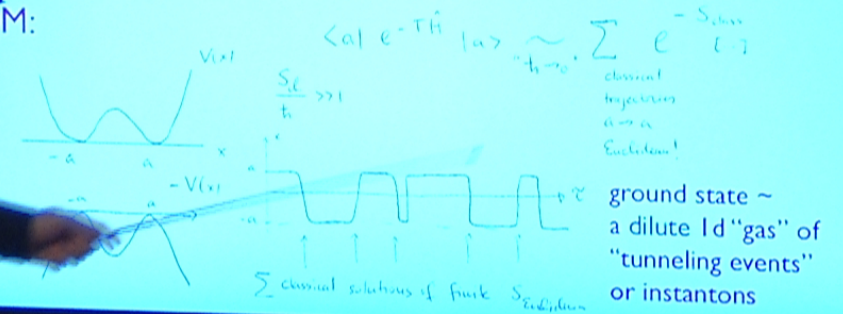
without taking into account nonperturbative physics, these are FREE...

2. topological

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(remember this is T=0 quantum transition!)

all (almost) dynamics is due to nonperturbative objects: vacuum of the theory is a dilute 3d "gas" of "molecules" interacting via long-range forces due to (dual) photon, scalar modulus, and fermion zero-mode hopping

QM:

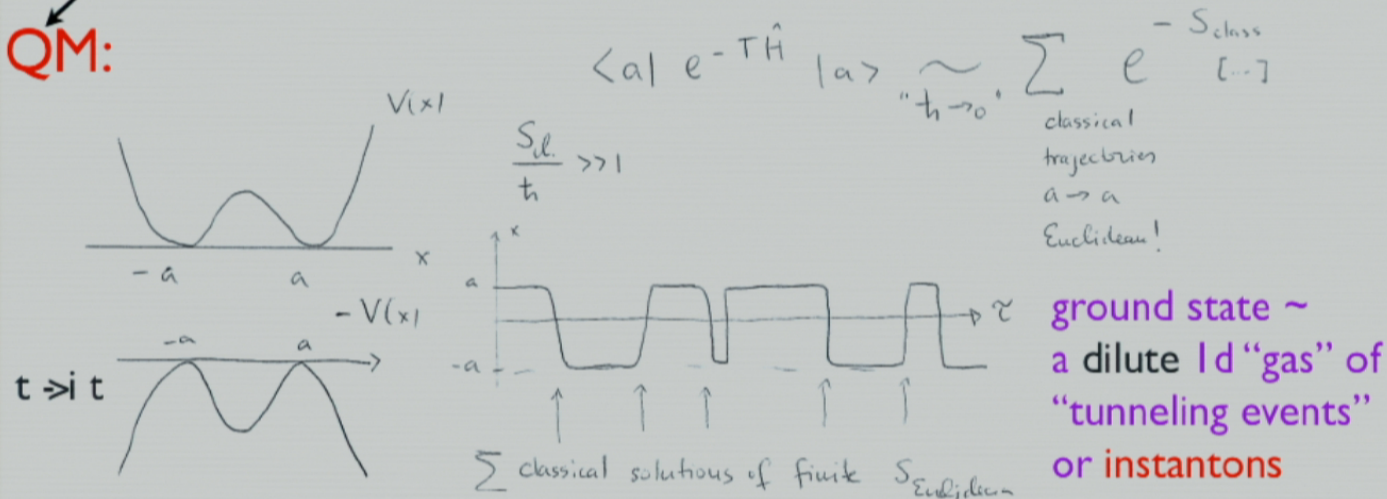


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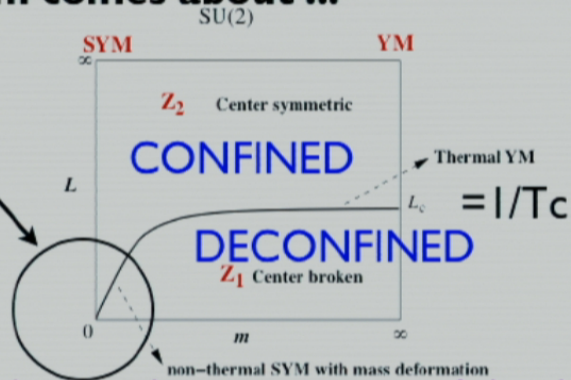
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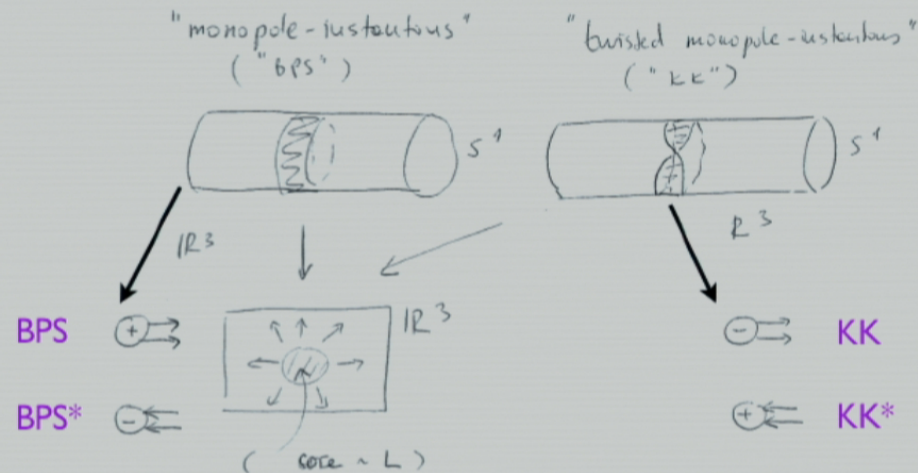


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QFT: $\frac{S_{cl.}}{\hbar} \gg 1$

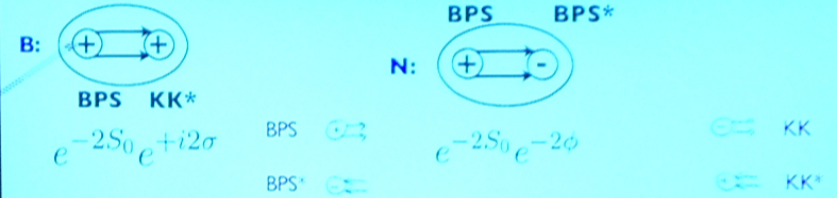
$$\langle 0 | e^{-T\hat{H}} | 0 \rangle \sim$$

$$\sim \sum \left(\text{finite action saddle points of path integral} \right)$$

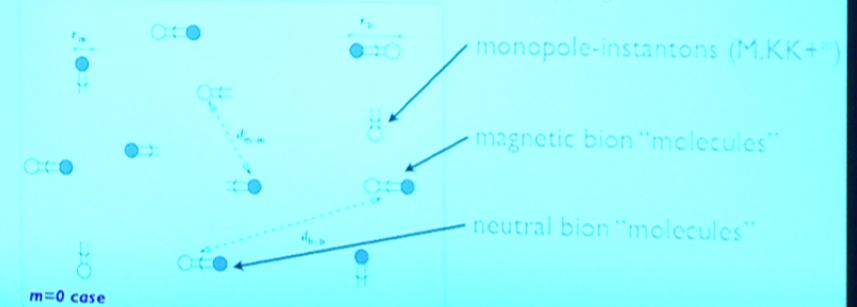


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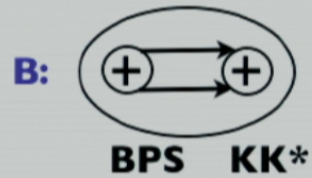
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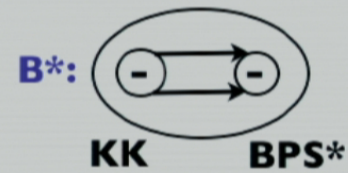
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(BPS-KK* “molecules”) “magnetic bions” - confinement!



$$e^{-2S_0} e^{+i2\sigma}$$

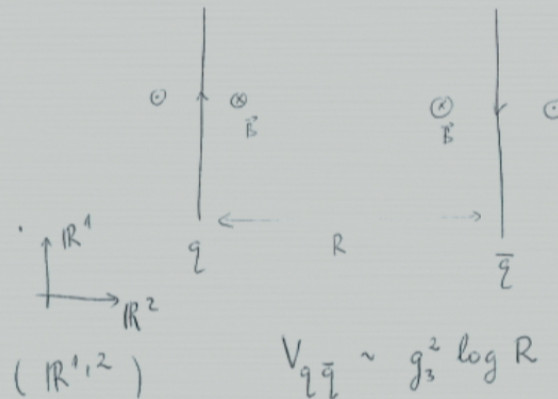


$$e^{-2S_0} e^{-i2\sigma}$$

$m=0$ case - physics is that of 3d Debye screening - mass gap and confinement:

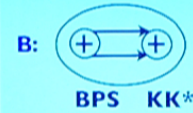
if nonperturbative saddle points are not summed over...

magnetic bion gas: classical
 3d Coulomb plasma

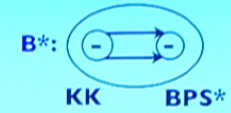


$$V_{q\bar{q}} \sim g^2 \log R \quad \text{- 2d Coulomb potential}$$

(BPS-KK* "molecules") "magnetic bions" - confinement!



$$e^{-2S_0} e^{+i2\sigma}$$



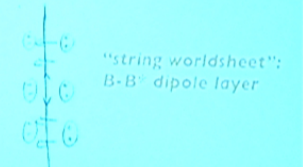
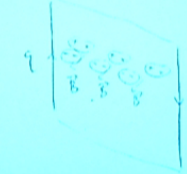
$$e^{-2S_0} e^{-i2\sigma}$$

$m=0$ case - physics is that of 3d Debye screening - mass gap and confinement:

magnetic bion gas; classical
3d Coulomb plasma



... in reality, B - B^* plasma screens magnetic field of external probes



[Polyakov 1977]

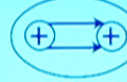
"monopole condensation" is due to composite

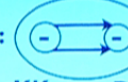
"molecular" objects - this theory does not confine in 3d limit

[Unsal 2007]

$$V_{ii} \sim g_s^2 \log R \Rightarrow \sigma R$$

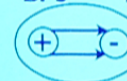
(BPS-KK* "molecules") "magnetic bions" - confinement!

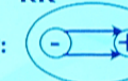
B:  $e^{-2S_0} e^{+i2\sigma}$
BPS KK*

B*:  $e^{-2S_0} e^{-i2\sigma}$
KK BPS*

(BPS-BPS*, KK-KK* "molecules") "neutral bions"

in pure-SYM: center-stabilizing

N:  $e^{-2S_0} e^{-2\phi}$
BPS BPS*

N*:  $e^{-2S_0} e^{+2\phi}$
KK KK*

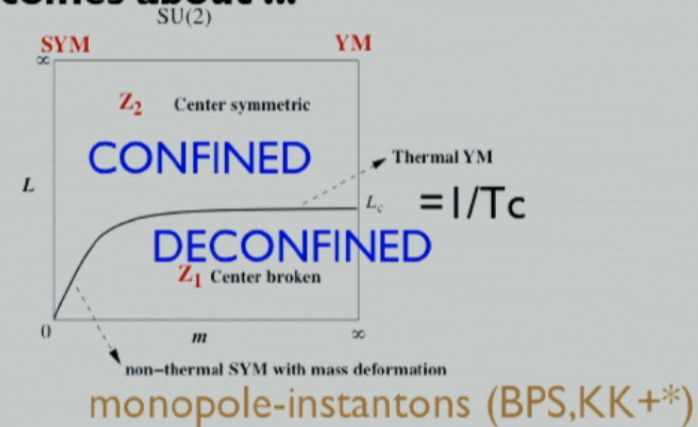
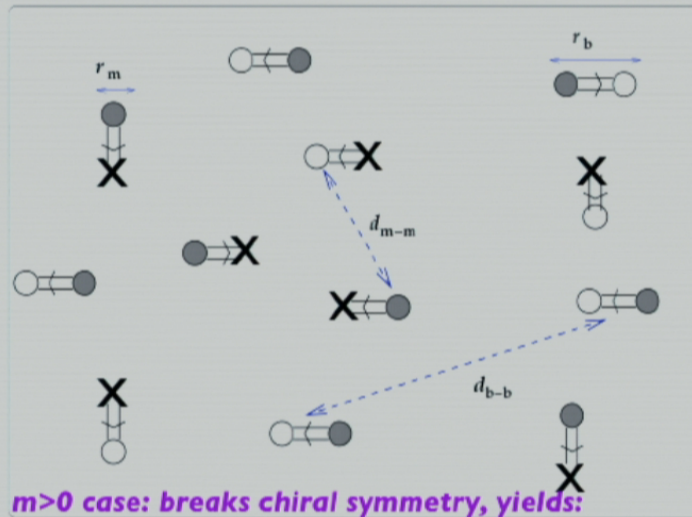
magnetic bion gas: classical
3d Coulomb plasma

magnetic bions: break chiral Z_2 , mass gap for dual photon
neutral bions: stabilize center Z_2 , mass gap for modulus
($\phi=0$ - center stable)

Our interest is in the center Z_2 (as chiral Z_2 broken at $m>0$)

Recall it is the center Z_2 which becomes the thermal
center symmetry of pure YM when m goes to infinity.

... how this part of the phase diagram comes about ...



magnetic bion “molecules”

[breaking of discrete chiral symmetry]

neutral bion “molecules”

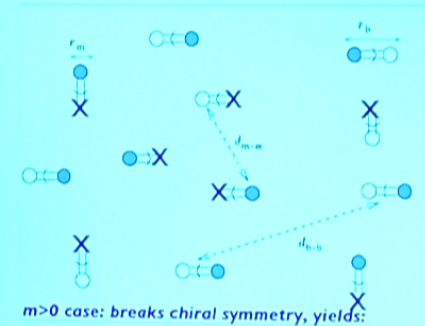
[stability of Z_2 center symmetry [non-thermal]]

1. extra nonperturbative contributions from monopole-instantons (no fermion zero modes)

2. extra perturbative Gross-Pisarski-Yaffe-like contribution (small since m is small)

small SUSY breaking “ m ” allows us to have perturbative and nonperturbative contributions compete while under theoretical control, resulting in a center-breaking transition as $\frac{m}{L^2 \Lambda^3}$ becomes $\mathcal{O}(1)$ (2nd order for $SU(2)$; 1st for $SU(N)$...)

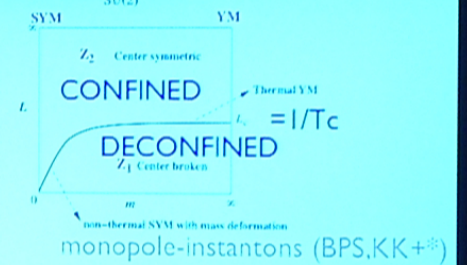
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2. extra perturbative Gross-Pisarski-Yaffe-like contribution (small since m is small)

small SUSY breaking " m " allows us to have perturbative and nonperturbative contributions compete while under theoretical control, resulting in a center-breaking transition as $\frac{m}{L^2 \Lambda^3}$ becomes $O(1)$ (2nd order for $SU(2)$; 1st for $SU(N)$...)



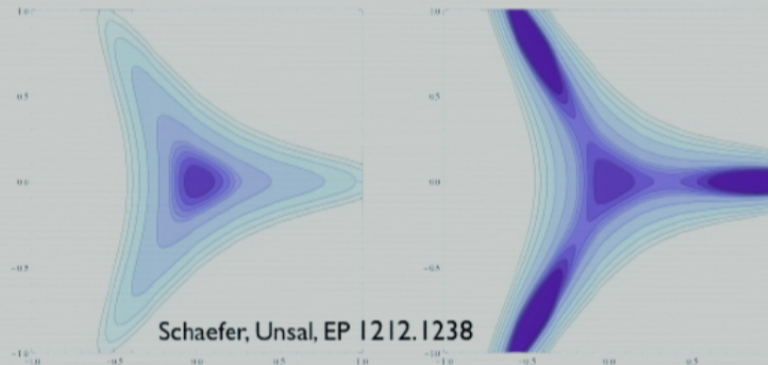
magnetic bion "molecules"

[breaking of discrete chiral symmetry]

neutral bion "molecules"

[stability of Z_2 center symmetry (non-thermal)]

instead of formulae, plot of potential due to “neutral bions” for $SU(3)$:
 Z_3 -symmetric vs Z_3 -breaking as $\frac{m}{L^2 \Lambda^3}$ increases (deviation of Ω EVs from Z_3)



Same objects that were identified in SYM also exist in pure thermal YM. What is lost is the theoretical control...

Instanton-liquid type models of the deconfinement transition can be considered, incorporating “molecular” contributions...

[Shuryak, Sulejmanpasic... '13]

- one can build models and/or compare small- L calculations with lattice ... eventually entire m/L

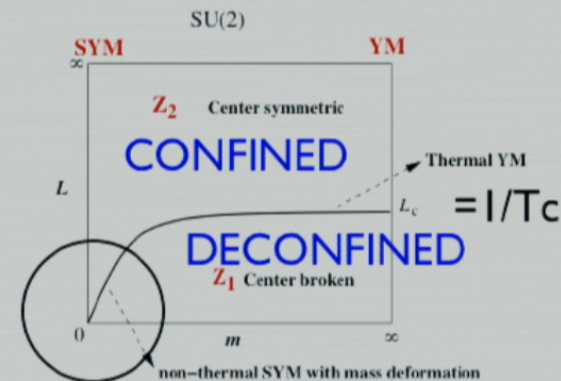
So far I told you about

1. a quantum center-breaking transition continuously connected (? ... gave evidence) to thermal deconfinement

2. driven by topological molecules, incl. some rather strange ones -

appear related to renormalons and needed to make sense of the divergent perturbation series... and even define the theory?

[Argyres, Dunne, Unsal ... 2012-]



All of this was non-thermal -but quantum connected to thermal (electric charges were not directly present).

Can one have a controllable thermal deconfinement transition? - YES

3. $R^2 \times S^1 \times S^1$ compactifications

[Simic, Unsal 2010
Unsal 2012]

Anber, EP, Unsal 2011
Anber, Collier, EP 2012
Anber, Collier, Strimas-Mackey,
Teeple, EP 2013]

non-thermal \leftrightarrow thermal

"deformed" pure-YM

"QCD(adj)" = YM with many
massless adjoint Weyl fermion

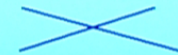
In the process of unraveling the above map, SUSY played a crucial role...

- notice the $nf=1$ adjoint theory is $N=1$ SYM
(already mentioned relation of QCD(adj) to a large- N limit of QCD(fund.) via various equivalences)

"QCD(adj)" on $R^3 \times S^1$ with fermions periodic around the circle, retains many features of SYM.

Consider first theory on $R^3 \times S^1$ with fermions periodic around the circle and then study nonzero- T of this theory (i.e. add a second "thermal circle").

Go back to my SYM slide... and proceed by applying

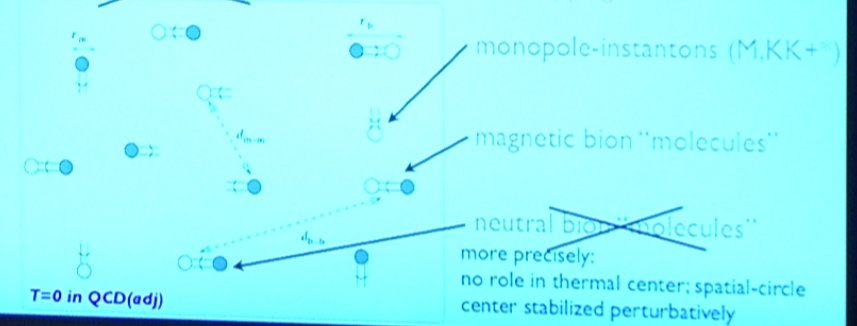


QCD(adj) on $\mathbb{R}^3 \times S^1$ (spatial)

- small-L theory is abelian
SU(2) breaks to U(1)
- no light charged states
(remember this is $T=0$ quantum transition!)

(same features as SYM before)

all (almost) dynamics is due to nonperturbative objects: vacuum of the theory is a dilute 3d "gas" of "molecules" interacting via long-range forces due to (dual) photon, ~~scalar modulus~~, and fermion zero-mode hopping



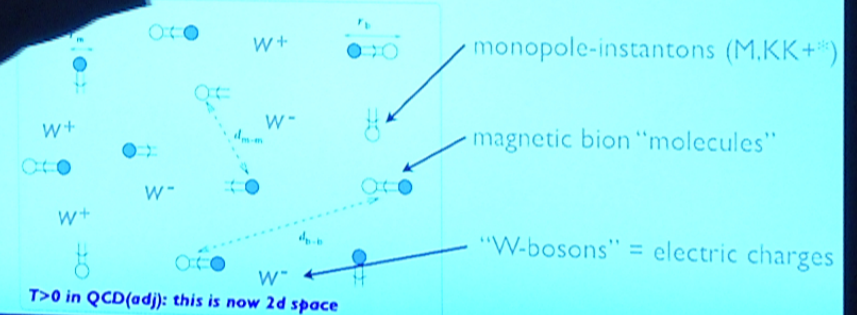
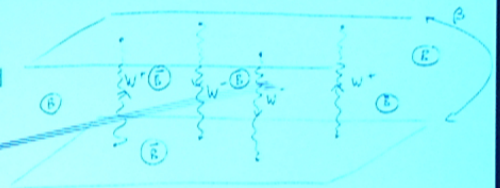
3. thermal gases of electric and magnetic charges

QCD(adj) on $\mathbb{R}^2 \times S^1$ (spatial) $\times S^1$ (thermal)

At T near T_c for deconfinement, the theory is approximately two-dimensional
- a thermal, not a quantum transition.

The partition function of the theory is that of a classical 2d gas of electric and magnetically charged particles.

Not just words: due to weak coupling at small- L , reduction of Z to the gas is justified and correct. Z is computed.



3. thermal gases of electric and magnetic charges

QCD(adj) on $R^2 \times S^1$ (spatial) $\times S^1$ (thermal)

$$\kappa_w(u) = \kappa_m(u) \leftrightarrow \frac{q^2}{2\pi LT} \leftarrow \text{strength of W-W Coulomb interaction}$$

For $SU(N_c)$

$$Z = \sum_{(N_{1+}^1 \geq 0, \dots, q_{1+} = +1)} \sum_{(N_{1-}^1 \geq 0, \dots, q_{1-} = +1)} \frac{\left(\frac{2q_1}{q^2}\right)^{\sum_i (N_{1+}^i + N_{1-}^i)} \left(\frac{2q_2}{q^2}\right)^{\sum_i (N_{2+}^i + N_{2-}^i)}}{\prod_i N_{1+}^i! N_{1-}^i! N_{2+}^i! N_{2-}^i!}$$

← magnetic bion fugacity ← electric (W) fugacity

$$\times \int \prod_{a,j} d^2 R_a^j \int \prod_{A,j} d^2 R_A^j \leftarrow \text{sum/integral over all coordinates/charges}$$

$$\times \exp \left[\kappa_w \sum_{i>j} \sum_{A>B} q_A q_B \vec{\alpha}_i \cdot \vec{\alpha}_j \ln \frac{|\vec{R}_A^i - \vec{R}_B^j|}{a} + \frac{4}{\kappa_m} \sum_{i>j} \sum_{a>b} q_a q_b \vec{Q}_i \cdot \vec{Q}_j \ln \frac{|\vec{R}_a^i - \vec{R}_b^j|}{a} \right]$$

W-charges, electric Coulomb interaction magnetic bion charges, magnetic Coulomb interaction

$$\vec{Q}_i = \vec{\alpha}_i - \vec{\alpha}_{i-1} \text{ magnetic bion charges} + 2i \sum_{i,j} \sum_{a,B} q_a q_B \vec{\alpha}_j \cdot \vec{Q}_i \Theta(|\vec{R}_a^i - \vec{R}_B^j|)$$

$\vec{\alpha}_i$ affine roots = W charges Aharonov-Bohm interaction of magnetic bions and W-bosons

3. thermal gases of electric and magnetic charges

QCD(adj) on $\mathbb{R}^2 \times S^1$ (spatial) $\times S^1$ (thermal)

How do we study the phase transition?

- SU(2): el.-m. Coulomb gas RGEs have a fixed line extending to weak coupling (fugacities); transition is second order; can calculate (some) critical exponents
- SU(N>2): small fugacity RGEs break down
 - map to XY "affine" spin model
 - study via Monte Carlo
 - Monte Carlo of Coulomb gas

For SU(N_c)

$$Z = \sum_{\substack{(N_{ij}^e \geq 0, i,j \geq 0, q_A = +1) \\ (N_{ij}^m \geq 0, i,j \geq 0, q_A = +1)}} \sum_{\substack{(N_{ij}^e \geq 0, i,j \geq 0, q_A = +1) \\ (N_{ij}^m \geq 0, i,j \geq 0, q_A = +1)}} \frac{(2q_A)^{\sum_i (N_{i0}^e + N_{i0}^m)} (2q_A)^{\sum_i (N_{i0}^e + N_{i0}^m)}}{\prod_i N_{i0}^e! N_{i0}^m! N_{i0}^e! N_{i0}^m!}$$

$$\times \int \prod_{a,j} d^2 R_a^j \int \prod_{A,j} d^2 R_A^j$$

$$\times \exp \left[\kappa_e \sum_{i>j} \sum_{A>B} q_A q_B \vec{\alpha}_i \cdot \vec{\alpha}_j \ln \frac{|\vec{R}_A^i - \vec{R}_B^j|}{a} + \frac{4}{\kappa_m} \sum_{i>j} \sum_{a>b} q_a q_b \vec{Q}_i \cdot \vec{Q}_j \ln \frac{|\vec{R}_a^i - \vec{R}_b^j|}{a} \right.$$

$$\left. + 2i \sum_{i,j} \sum_{a,B} q_a q_B \vec{\alpha}_j \cdot \vec{Q}_i \Theta(|\vec{R}_a^i - \vec{R}_B^j|) \right]$$

For SU(2) and SU(3): Kramers-Wanier duality (low-T/high-T); self dual point: T_c

3. thermal gases of electric and magnetic charges

QCD(adj) on $\mathbb{R}^2 \times S^1$ (spatial) $\times S^1$ (thermal)

physics of transition...

but in a different “duality frame” ... $SU(2)$

arrows = XY spins = photon ($U(1)$ in $SU(2)$)

(W-bosons are, now, represented by external field potential)

randomly fluctuating

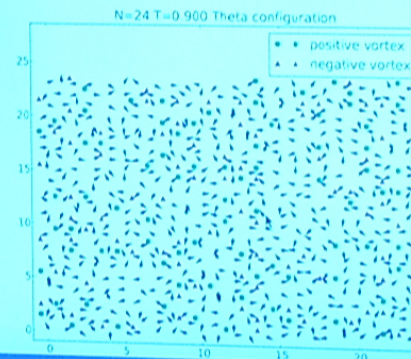
arrows =

small correlation length,
mass gap

ordered arrows =

center symmetry breaking

in spin model (unphysical “half-electron” operator so Z_2)



vortices = magnetic bions

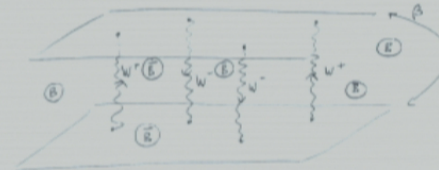
movie courtesy Seth Styrnas-Mackey, Nov. 2013

BRIEF SUMMARY AND A FEW MORE QUESTIONS:

I told you about how SUSY can - directly or otherwise - help in finding calculable realizations of deconfinement - generally, a complicated strongly-coupled (non-BPS, non-protected, non-holomorphic) problem.

SYM with gaugino mass on $R^3 \times S^1$
where a quantum phase transition
appears continuously related to
thermal deconfinement

QCD(adj) on $R^2 \times S^1 \times S^1$
where deconfinement maps to
the transition in a “simple” electric
magnetic “Coulomb gas”
(potential use in nonequilibrium?)



In both cases, various properties of the transition agree with known 4d lattice results.

We pointed out many erroneous assumptions/statements in existing models of deconfinement via topology.

Some new effort in “model building” (“instanton-monopole liquid”?)

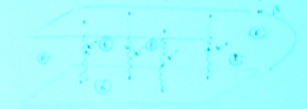
Lattice work - in pure YM; in studying the phases of QCD(adj) on S^1 ; also incl. SYM.

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