Title: Including astroparticle observables in global fits to new physics scenarios

Date: Oct 15, 2013 01:00 PM

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Abstract: Searches for physics beyond the standard model come in many forms, from terrestrial probes to astroparticle experiments and cosmological observations. Efforts to combine multiple search channels in 'global fits' to new physics scenarios typically consider only a subset of the available channels. Astroparticle searches in particular are usually only included in a very approximate way, if at all. In this talk I will review recent progress in including detailed gamma-ray, neutrino and CMB searches for dark matter in global fits. I will also preview some of the future developments and challenges in this field, where the applicability of global fits will move well beyond the small range of constrained supersymmetric models they have so far mostly been applied to.

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Including astroparticle observables in global fits to new physics scenarios

Pat Scott

Department of Physics, McGill University

Slides available from

http://www.physics.mcgill.ca/~patscott



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Including astroparticle observables in BSM global fits

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Including astroparticle observables in BSM global fits

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Outline

- The Problem
- Progress
 - Gamma-rays
 - Neutrinos
 - CMB constraints
- Future Challenges
 - Respectable LHC likelihoods
 - Statistical/numerical issues
 - Parameter space → Theory space



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Searching for new physics

Many reasons to look for physics Beyond the Standard Model (BSM):

- Higgs mass (hierarchy problem + vacuum stability)
- Dark matter exists
- Baryon asymmetry
- Neutrino masses and mixings

So what do we do about it?

- Make new particles at high-E colliders
- Study rare processes at high-L colliders
- Hunt for dark matter
- Look for kooky neutrino physics



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Combining searches I

Question

How do we know which models are in and which are out?



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Combining searches I

Question

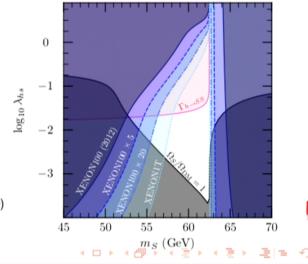
How do we know which models are in and which are out?

Answer

Combine the results from different searches

- Simplest method: take different exclusions, overplot them, conclude things are "allowed" or "excluded"
- Simplest BSM example: the scalar singlet model

(Cline, Kainulainen, PS & Weniger, PRD, 1306.4710)



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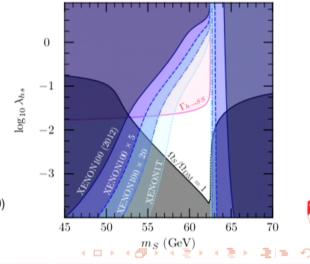
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Combining searches II

That's all well and good if there are only 2 parameters and few searches...

Question

What if there are many different constraints?



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Combining searches II

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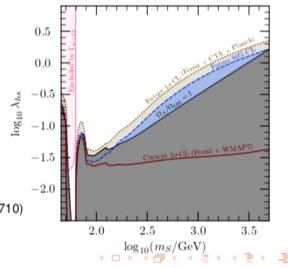
What if there are many different constraints?

Answer

Combine constraints in a statistically valid way

 $\rightarrow \text{composite likelihood}$

(Cline, Kainulainen, PS & Weniger, PRD, 1306.4710)



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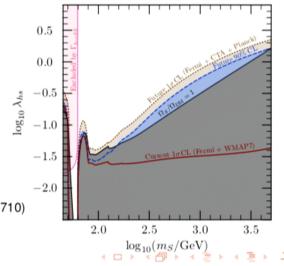
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Combining searches III

That's all well and good if there are only 2 parameters and few searches...

Question

What if there are many parameters?



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Combining searches III

That's all well and good if there are only 2 parameters and few searches...

Question

What if there are many parameters?

Answer

Need to

- scan the parameter space (smart numerics)
- interpret the combined results (Bayesian / frequentist)
- project down to parameter planes of interest (marginalise / profile)
- \rightarrow global fits





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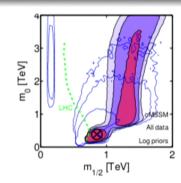
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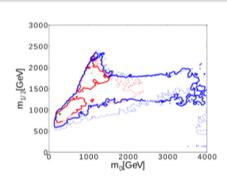
Know your (SUSY) scans

Global fits:

Quantitative? per-point: always overall: always



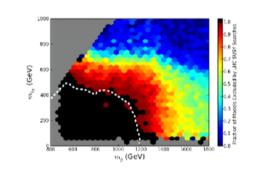
Strege et al *JCAP*, 1212.2636



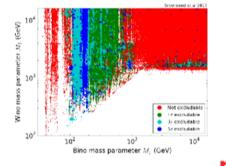
MasterCode, EPJC, 1207.7315

Not global fits:

Quantitative? per-point: sometimes overall: never



Cahill-Rowley et al, 1307.8444



Silverwood, PS, et al, JCAP, 1210.0844

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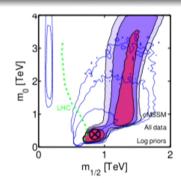
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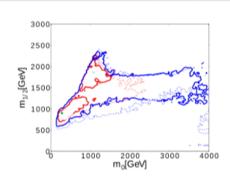
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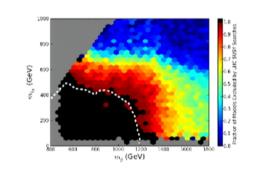
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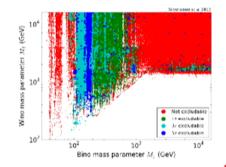
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BSM Model Scanning – Statistics 101

Goals:

- Given a particular theory, determine which parameter combinations fit all experiments, and how well
- @ Given multiple theories, determine which fit the data better, and quantify how much better





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BSM Model Scanning – Statistics 101

Goals:

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⇒ parameter estimation

Given multiple theories, determine which fit the data better, and quantify how much better model comparison



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BSM Model Scanning – Statistics 101

Goals:

 Given a particular theory, determine which parameter combinations fit all experiments, and how well

⇒ parameter estimation

Given multiple theories, determine which fit the data better, and quantify how much better model comparison

Why simple IN/OUT analyses are not enough...

- Only partial goodness of fit, no measure of convergence, no idea how to generalise to regions or whole space.
- Frequency/density of models in IN/OUT scans is not proportional to probability

 means essentially nothing.





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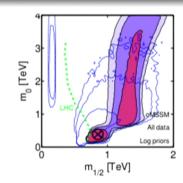
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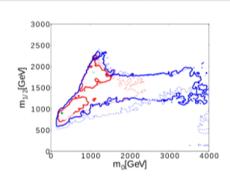
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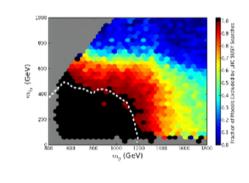
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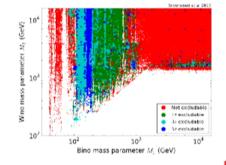
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Including astroparticle observables in BSM global fits

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Putting it all together: global fits

Issue 1: Combining fits to different experiments Relatively easy – composite likelihood ($\mathcal{L}_1 \times \mathcal{L}_2 \equiv \chi_1^2 + \chi_2^2$ for simplest \mathcal{L})

- dark matter relic density from WMAP
- precision electroweak tests at LEP
- LEP limits on sparticle masses
- *B*-factory data (rare decays, $b \rightarrow s\gamma$)
- muon anomalous magnetic moment

ches, direct detection (only roughly implemented for now)





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Including astroparticle observables in BSM global fits

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Putting it all together: global fits

Issue 2: Including the effects of uncertainties in input data Easy – treat them as *nuisance parameters*

Issue 3: Finding the points with the best likelihoods
Tough – MCMCs, nested sampling, genetic algorithms, etc

Issue 4: Comparing theories

Depends – Bayesian model comparison, *p* values

(*TS* distribution? → coverage???)



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Including astroparticle observables in BSM global fits

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Two different approaches to including astro data in BSM scans

- Just use the published limits on $\langle \sigma v \rangle$ (or $\sigma_{SI,SD}$)
 - Fast can cover large parameter spaces
 - Not so accurate experimental limits are invariably based on theoretical assumptions, e.g. bb̄ spectrum
 - Full likelihood function almost never available
- Use the data points directly in BSM scans
 - Slow requires full treatment of instrument profile for each point
 - Accurate can test each point self-consistently
 - Allows marginalisation over theoretical assumptions
 - Allows construction of full multi-dimensional likelihood function





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Including astroparticle observables in BSM global fits

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- (indirect only: use just flux upper limits)



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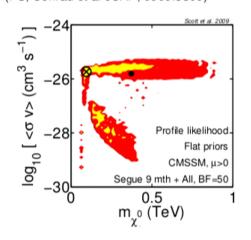
Gamma-rays

Gamma-ray annihilation searches in CMSSM global fits:

Fermi-LAT

Satellite pair conversion telescope Dwarf galaxy Segue 1

(PS, Conrad et al *JCAP*, 0909.3300)



- Full binned Poissonian likelihood (no χ^2 approximation)
- Full treatment of PSF and energy dispersion (with fast convolution library FLATlib)
- Marginalisation over systematic error on effective area
- Diffuse BG from Fermi-LAT Galprop fits
- Isotropic BG best-fit isotropic power law
- J-factor from Martinez et al (JCAP, 0902.4715; best at the time)



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Gamma-rays

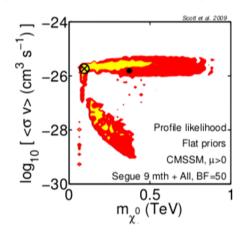
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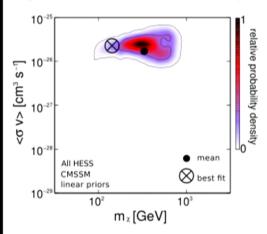
Gamma-ray annihilation searches in CMSSM global fits:

HESS

Air Čerenkov telescope

Milky Way+Carina+Sculptor+Sag dwarf

(Ripken, Conrad & PS JCAP, 1012.3939)



- \bullet χ^2 -based analysis using public flux limits
- 'Milky Way' = halo just beyond GC (45–150 pc)
- Virtual internal bremsstrahlung from co-annihilation strip models caught at high-E by HESS
- but: J-factors for Sag dwarf rather uncertain





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Gamma-rays
Neutrinos
CMB constraints

How to find DM with neutrino telescopes

The short version:



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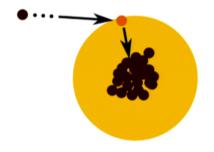
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Gamma-rays
Neutrinos
CMB constraints

How to find DM with neutrino telescopes

The short version:

Halo WIMPs crash into the Sun





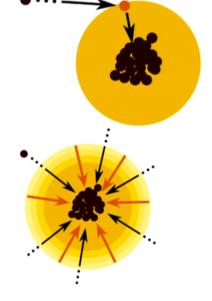


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The short version:

- Halo WIMPs crash into the Sun
- Some lose enough energy in the scatter to be gravitationally bound
- Scatter some more, sink to the core





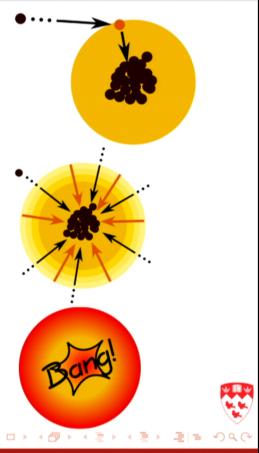
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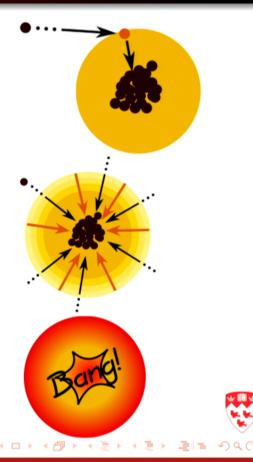
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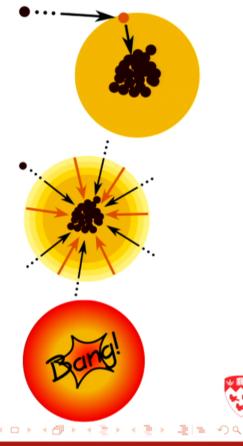


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- Propagate+oscillate their way to the Earth, convert into muons in ice/water
- Look for Čerenkov radiation from the muons in IceCube, ANTARES, etc



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Including astroparticle observables in BSM global fits

Simplest way to do anything is to first make it a counting problem...

Compare observed number of events n and predicted number θ for each model, taking into account error σ_{ϵ} on acceptance:

$$\mathcal{L}_{\text{num}}(n|\theta_{\text{BG}} + \theta_{\text{sig}}) = \frac{1}{\sqrt{2\pi}\sigma_{\epsilon}} \int_{0}^{\infty} \frac{(\theta_{\text{BG}} + \epsilon\theta_{\text{sig}})^{n} e^{-(\theta_{\text{BG}} + \epsilon\theta_{\text{sig}})}}{n!} \frac{1}{\epsilon} \exp\left[-\frac{1}{2} \left(\frac{\ln \epsilon}{\sigma_{\epsilon}}\right)^{2}\right] d\epsilon.$$
(1)

Nuisance parameter ϵ takes into account systematic errors on effective area, etc. $\sigma_{\epsilon} \sim$ 20% for IceCube.





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(1)

Then: upgrade to full unbinned likelihood with number (\mathcal{L}_{num}), spectral (\mathcal{L}_{spec}) and angular (\mathcal{L}_{ang}) bits:

$$\mathcal{L} = \mathcal{L}_{\text{num}}(n|\theta_{\text{signal+BG}}) \prod_{i=1}^{n} \mathcal{L}_{\text{spec},i} \mathcal{L}_{\text{ang},i}$$
 (2)

All available in DarkSUSY v5.0.6 and later: www.darksusy.org



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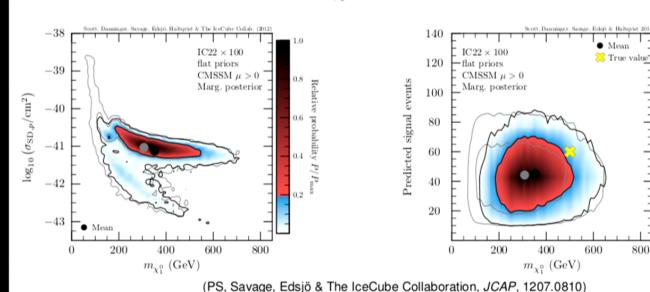
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CMSSM model reconstruction with IceCube event data

Benchmark recovery with 22-string IceCube WIMP-search neutrino events + full likelihood:

Mock signal: 60 events, $m_{\chi} = 500 \, \text{GeV}$, 100% $\chi \chi \to W^+ W^-$





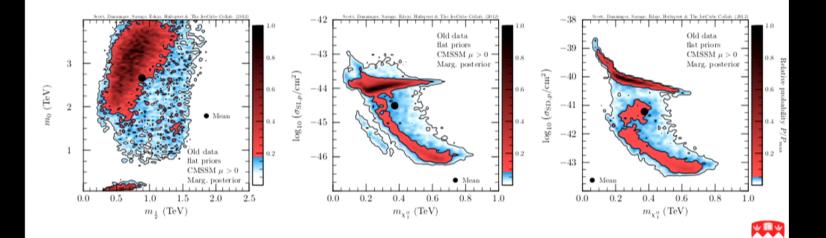
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Base Observables



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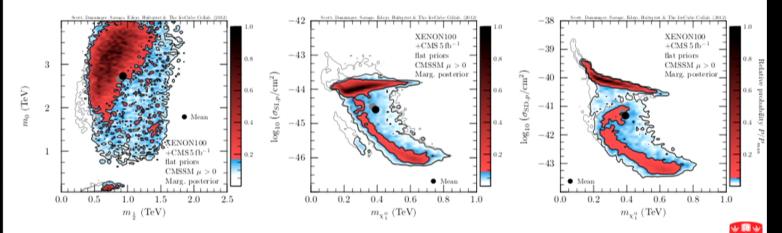
Including astroparticle observables in BSM global fits

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Base Observables + XENON-100 + CMS 5 fb⁻¹

Grey contours correspond to Base Observables only



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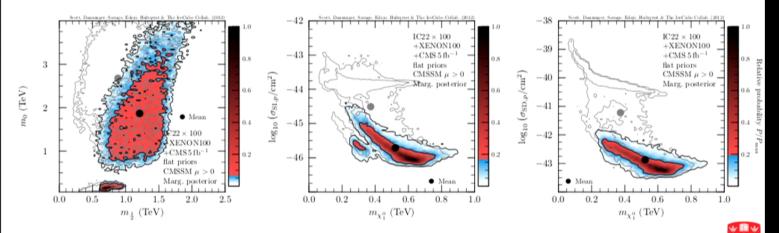
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Base Observables + XENON-100 + CMS 5 fb⁻¹ + projected IC86-DeepCore

Grey contours correspond to Base Observables only



CMSSM, IceCube-22 with 100× boosted effective area (kinda like IceCube-DeepCore)

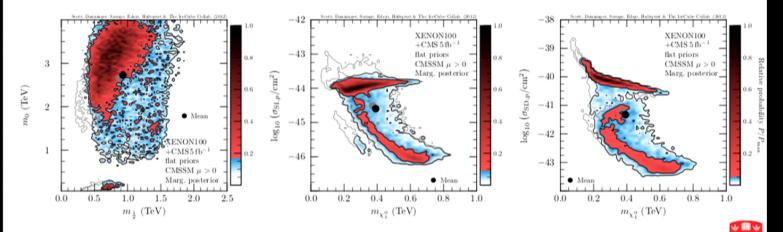
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Base Observables + XENON-100 + CMS 5 fb⁻¹

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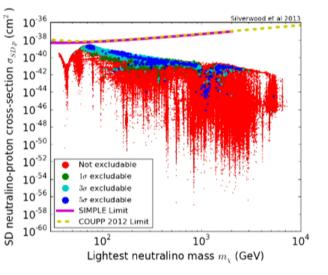
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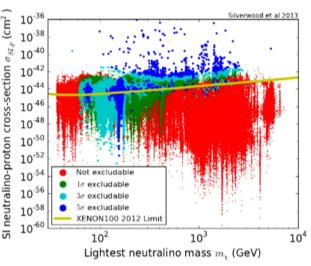
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Prospects for detection in the MSSM-25

86-string IceCube vs Direct Detection (points pass $\Omega_{\chi} h^2$, $b \to s\gamma$, LEP)





(Silverwood, PS, et al, JCAP, 1210.0844)

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Many models that IceCube-86 can see are not accessible to direct detection...



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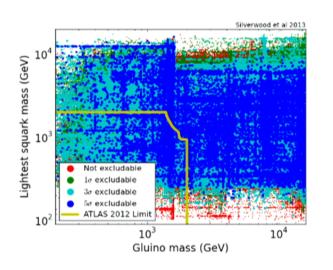
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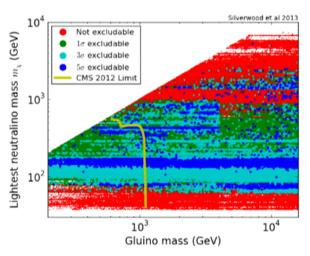
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Prospects for detection in the MSSM-25

86-string IceCube vs LHC (very naively)

SMS limits: 7 TeV, 4.7 fb⁻¹, jets + $E_{T,miss}$; 0 leptons (ATLAS), razor + M_{T2} (CMS)





(Silverwood, PS, et al, *JCAP*, 1210.0844)

Many models that IceCube-86 can see are also not accessible at colliders.



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Outline

- The Problem
- Progress
 - Gamma-rays
 - Neutrinos
 - CMB constraints
- Future Challenges
 - Respectable LHC likelihoods
 - Statistical/numerical issues
 - Parameter space → Theory space





Simple CMB likelihood function, for

- Any combination of annihilation or decay channels
- Any dark matter mass
- Any decay lifetime/annihilation cross-section
- \rightarrow just requires interpolating one number in a table.

Cline & PS, *JCAP*, 1301.5908, using

- CMB energy deposition from
 - Slatyer (PRD, 1211.0283)
 - Finkbeiner et al (PRD, 1109.6322)
- PYTHIA annihilation/decay spectra from
 - Cirelli et al (PPPC4DMID; JCAP, 1012.4515)





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Simple CMB likelihood function, for

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 $f_{\rm eff}$ for annihilation:

$$\ln \mathcal{L}(\langle \sigma v \rangle | m_{\chi}, r_i) = -\frac{1}{2} f_{\text{eff}}^2(m_{\chi}, r_i) \lambda_1 c_1^2 \left(\frac{\langle \sigma v \rangle}{2 \times 10^{-27} \text{cm}^3 \text{s}^{-1}} \right)^2 \left(\frac{\text{GeV}}{m_{\chi}} \right)^2 \quad (3)$$





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 η for decay:

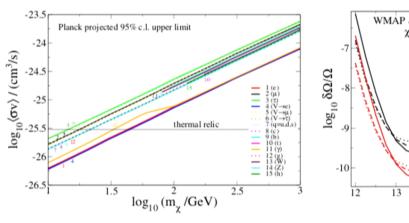
$$\ln \mathcal{L}(au|m_\chi,r_i) = -rac{1}{2} \left(rac{\delta\Omega}{\Omega_{
m DM} au}
ight)^2 \eta^2(au,m_\chi,r_i)$$

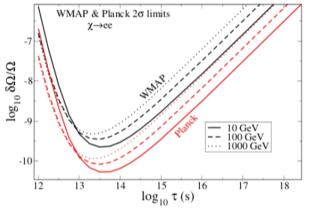


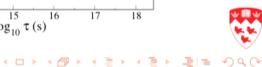


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The Problem Progress
Future Challenges

Respectable LHC likelihoods
Statistical/numerical issues
Parameter space → Theory spac

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The Problem Progress Future Challenges Respectable LHC likelihoods
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Parameter space → Theory space

The LHC likelihood monster

Time per point:

 $\mathcal{O}(\textit{minute})$ in best cases



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The LHC likelihood monster

Time per point:

 $\mathcal{O}(\textit{minute})$ in best cases

Time per point for global fits to converge:

 $\mathcal{O}(seconds)$ in worst cases



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The LHC likelihood monster

Time per point:

O(minute) in best cases

Time per point for global fits to converge:

O(seconds) in worst cases

Challenge:

About 2 orders of magnitude too slow to actually include LHC data in global fits properly





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The Problem Progress Future Challenges Respectable LHC likelihoods
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Taming the LHC monster

Zeroth Order Response:

"Stuff it, just use the published limits and ignore the dependence on other parameters"



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Taming the LHC monster

Zeroth Order Response:

"Stuff it, just use the published limits and ignore the dependence on other parameters"

Obviously naughty – plotted limits assume CMSSM, and fix two of the parameters

- Don't really know dependence on other parameters
- Don't have a likelihood function, just a line
- Can't use this at all for non-CMSSM global fits e.g. MSSM-25

SuperBayeS



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The Problem Progress Future Challenges Respectable LHC likelihoods
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Taming the LHC monster

First Order Response:

"Test if things depend on the other parameters (hope not), re-simulate published exclusion curve"



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Taming the LHC monster

First Order Response:

"Test if things depend on the other parameters (hope not), re-simulate published exclusion curve"

Not that great, but OK in some cases

- At least have some sort of likelihood this time
- Still a bit screwed if things do depend a lot on other parameters, but
- allows (potentially shaky) extrapolation, also to non-CMSSM models

Fittino, Mastercode



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Taming the LHC monster

Second Order Response:

"That's ridiculous. I've never met a calculation I can't speed up. There must be some way to have my cake and eat it too"

Maybe – this is the challenge.

- Interpolated likelihoods (how to choose nodes?)
- Neural network functional approximation (how to train accurately?)
- Some sort of smart reduction based on event topology?
- Something else?

Balázs, Buckley, Farmer, White et al (1106.4613, 1205.1568)



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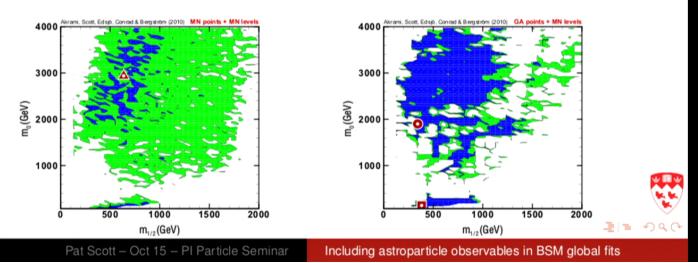
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Scanning algorithms

Convergence remains an issue, especially for profile likelihood Messy likelihood \implies best-fit point can be (and often is) easily missed (Akrami, PS et al JHEP, 0910.3950, Feroz et al JHEP, 1101.3296)

- frequentist CLs are off, as isolikelihood levels are chosen incorrectly
- can impact coverage (overcoverage, or masking of undercoverage due to non- χ^2 TS distribution)
- need to use multiple priors and scanning algorithms (one optimised for profile likelihoods?)



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Coverage

[Statistical aside]

Test statistic: a measure on data used to construct statistical tests (e.g. χ^2 , ln \mathcal{L} , etc.) **Coverage**: the percentage of the time that a supposed 'x%' confidence region actually contains the true value

- Distribution of the test statistic and design of the test it's used in determine coverage.
- p-value calculation requires the test statistic distribution to be well known.

We don't *really* know the distribution of our test statistic in BSM global fits, as it is too expensive to Monte Carlo

 coverage is rarely spot-on unless mapping from parameters to data-space is linear

(Akrami, Savage, PS et al *JCAP*, 1011.4297, Bridges et al *JHEP*, 1011.4306, Strege et al *PRD*, 1201.3631)

 p-value assessments of goodness of fit should be viewed with serious scepticism (→MasterCode)





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CMSSM, SMS \neq BSM

(SMS = Simplified Model Spectrum)

Want to do model comparison to actually work out which theory is right. . .

Challenge:

How do I easily adapt a global fit to different BSM theories?



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CMSSM, SMS \neq BSM

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Want to do model comparison to actually work out which theory is right. . .

Challenge:

How do I easily adapt a global fit to different BSM theories?

Somehow, we must recast things quickly to a new theory

- data
- likelihood functions
- scanning code 'housekeeping'
- even predictions





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Hitting the wall

Issues with current global fit codes:

- Strongly wedded to a few theories (e.g. constrained MSSM / mSUGRA)
- Strongly wedded to a few theory calculators
- All datasets and observables basically hardcoded
- Rough or non-existent treatment of most experiments (astroparticle + collider especially)
- Sub-optimal statistical methods / search algorithms
- already hitting the wall on theories, data & computational methods





GAMBIT: a second-generation global fit code

GAMBIT: Global And Modular BSM Inference Tool

Overriding principles of GAMBIT: flexibility and modularity

- General enough to allow fast definition of new datasets and theoretical models
- Plug and play scanning, physics and likelihood packages
- Extensive model database not just small modifications to constrained MSSM (NUHM, etc), and not just SUSY!
- Extensive observable/data libraries (likelihood modules)
- Many statistical options Bayesian/frequentist, likelihood definitions, scanning algorithms
- A smart and fast LHC likelihood calculator
- Massively parallel
- Full open-source code release



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The GAMBIT Collaboration

22 Members, 13 Institutes

8 Experiments, 3 major theory codes

Fermi-LAT J. Conrad, J. Edsjö, G. Martinez, P. Scott[†]

IceCube J. Edsjö, C. Savage, P. Scott

ATLAS A. Buckley, P. Jackson, C. Rogan, A. Saavedra, M. White

LHCb N. Serra

HESS J. Conrad

AMS-02 A. Putze

CTA C. Balázs, T. Bringmann, J. Conrad, M. White

DARWIN J. Conrad

Theory C. Balázs, T. Bringmann, J. Cornell, L.-A. Dal, J. Edsjö,

B. Farmer, A. Krislock, A. Kvellestad, F.N. Mahmoudi,

A. Raklev, C. Savage, P. Scott, C. Weniger, M. White

† PI



Closing remarks

- Robust analysis of dark matter and BSM physics requires multi-messenger global fits
- Lots of interesting astroparticle observables to include in global fits
- Quite a bit of technical (statistical/computational) detail to worry about
- GAMBIT is coming





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Closing remarks

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