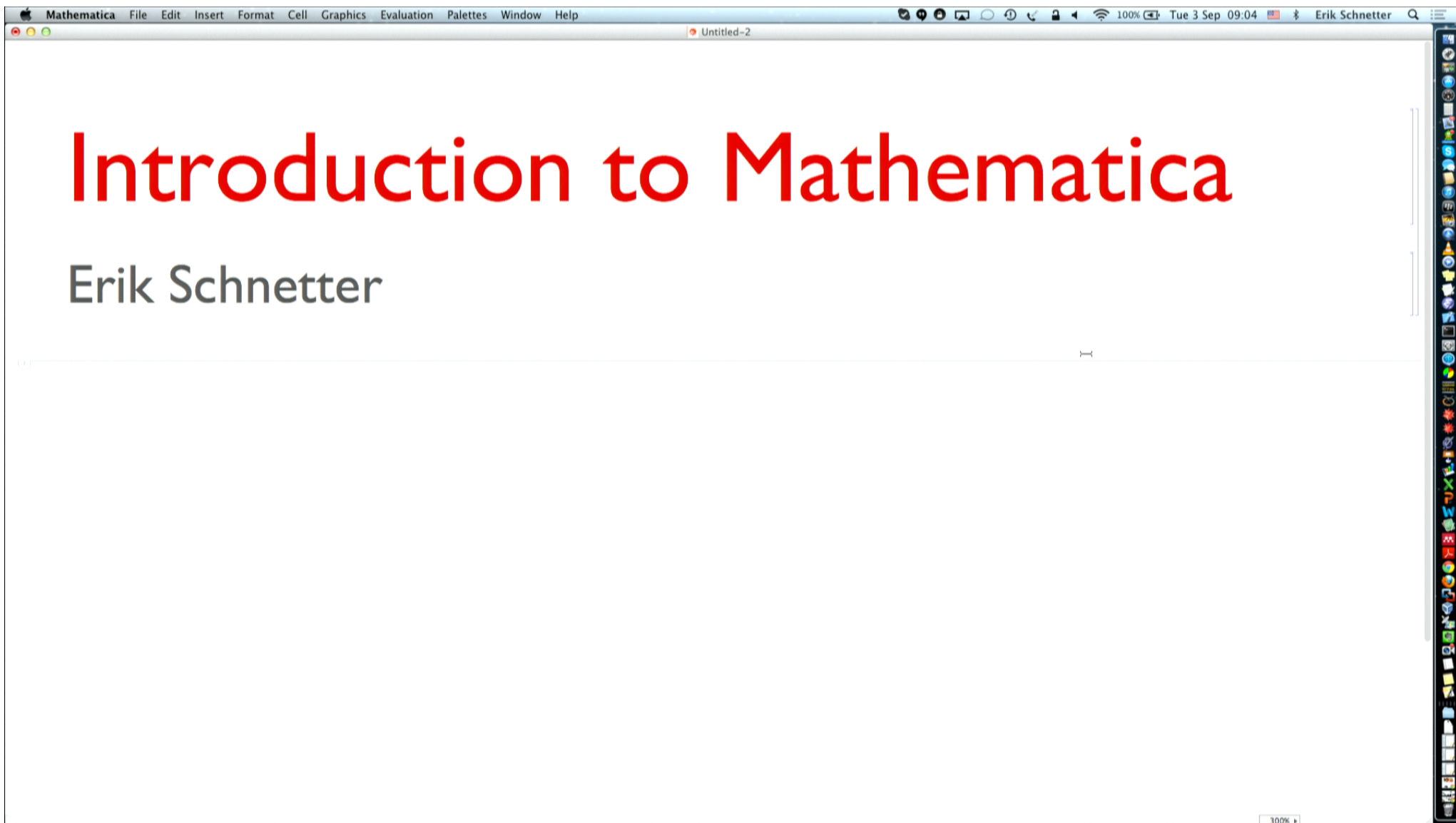


Title: 13/14 PSI - Computational Methods in Physics - Lecture 1

Date: Sep 03, 2013 09:00 AM

URL: <http://pirsa.org/13090052>

Abstract:



Mathematica File Edit Insert Format Cell Graphics Evaluation Palettes Window Help

Untitled-2

$\sqrt{2}$

In[6]:=

$$x^2 + x - 1$$

Out[6]=

$$-1 + x + x^2$$

In[7]:=

$$(x + 1) (x - 1)$$

Out[7]=

$$(-1 + x) (1 + x)$$

In[8]:=

$$\text{Simplify}[(x + 1) (x - 1)]$$

Out[8]=

$$-1 + x^2$$

Sqrt

Sqrt

SqrtBox

300%

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Untitled-2

$x - 3$

Out[13]=

9

In[14]:=

$x = .$

In[15]:=

x

Out[15]=

x

In[16]:=

? Sqrt

Sqrt[z] or $\sqrt{z}$ gives the square root of z. >>

300%

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Untitled-2

x

In[16]:=

? Sqrt

Sqrt[z] or $\sqrt{z}$ gives the square root of z. >>

In[18]:=

Prime[1000]

Out[18]=

7919

In[19]:=

Solve[x^2 + 1 == 0, x]

Out[19]=

$\{\{x \rightarrow -i\}, \{x \rightarrow i\}\}$

In[20]:=

Limit[1/n, n -> Infinity]

Out[20]=

0

300%

Mathematica File Edit Insert Format Cell Graphics Evaluation Palettes Window Help

Untitled-2

Out[18]=

7919

In[19]:=

Solve[$x^2 + 1 == 0$, x]

Out[19]=

$\{\{x \rightarrow -i\}, \{x \rightarrow i\}\}$

In[20]:=

Limit[$1/n$, $n \rightarrow \text{Infinity}$]

Out[20]=

0

Functions

300%

7919

In[19]:=

Solve[$x^2 + 1 == 0$, x]

Out[19]=

$\{\{x \rightarrow -i\}, \{x \rightarrow i\}\}$

In[20]:=

Limit[$1/n$, $n \rightarrow \text{Infinity}$]

Out[20]=

0

Functions

In[21]:=

f[$x_$] = **Sin**[x]

Out[21]=

Sin[x]

Assuming a math expression | Use as a *definition* instead

300%

7919

In[19]:=

Solve[$x^2 + 1 == 0$, x]

Out[19]=

$\{\{x \rightarrow -i\}, \{x \rightarrow i\}\}$

In[20]:=

Limit[$1/n$, $n \rightarrow \text{Infinity}$]

Out[20]=

0

Functions

In[21]:=

f[$x_$] = **Sin**[x]

Out[21]=

Sin[x]

Assuming a math expression | Use as a *definition* instead

300% ▸

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Untitled-2

In[26]:=

$$f[x_] = x + a$$

Out[26]=

$$1 + x$$

In[27]:=

$$f[5]$$

Out[27]=

$$6$$

In[28]:=

$$a = .$$

In[29]:=

$$a$$

Out[29]=

$$a$$

$$f[5]$$

300%

Mathematica File Edit Insert Format Cell Graphics Evaluation Palettes Window Help

Untitled-2

100% Tue 3 Sep 09:17 Erik Schnetter

In[30]:=

$$f[5]$$

Out[30]=

$$6$$

In[31]:=

$$g[x_] := x + a$$

In[32]:=

$$g[x]$$

Out[32]=

$$a + x$$

In[33]:=

$$a = 1$$

Out[33]=

$$1$$

In[34]:=

$$g[x]$$

Out[34]=

$$1 + x$$

plot x derivative x integral zeros more...

300%

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Untitled-2

5 + a

In[38]:=

1 &

Out[38]=

1 &

In[39]:=

1 & [4]

Out[39]=

1

In[40]:=

(2 #) &

Out[40]=

2 #1 &

In[41]:=

(2 # &) [5]

Out[41]=

10

prime factorization divisors binary form number of primes s 10 more...

300%

Mathematica File Edit Insert Format Cell Graphics Evaluation Palettes Window Help

Untitled-2

100% Tue 3 Sep 09:22 Erik Schnetter

In[42]:=

$$(\#1 + \#2) \&$$

Out[42]=

$$\#1 + \#2 \&$$

In[43]:=

$$(\#1 + \#2) \&[2, 3]$$

Out[43]=

$$5$$

In[44]:=

$$\mathbf{f1}[\mathbf{x_}, \mathbf{y_}] := \mathbf{x} + \mathbf{y}$$

In[45]:=

$$\mathbf{f1}[2, 3]$$

Out[45]=

$$5$$

$\mathbf{f2} := (\#1 + \#2) \&$

300%

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Untitled-2

Internal Representation

In[50]:= $a + 2b + 3c$ // TreeForm

Out[50]//TreeForm=

```
graph TD; Plus[Plus] --- a[a]; Plus --- Times1[Times]; Plus --- Times2[Times]; Times1 --- 2[2]; Times1 --- b[b]; Times2 --- 3[3]; Times2 --- c[c];
```

grad a derivative a integral global max more...

200%

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Untitled-2

Tue 3 Sep 09:29 Erik Schnetter

In[54]:= {1, 2, 3, 4, 5, 6, 7, 8, 9, 10}

Out[54]= {1, 2, 3, 4, 5, 6, 7, 8, 9, 10}

In[59]:= Table[i, {i, 1/2, 10, 3}]

Out[59]= $\left\{\frac{1}{2}, \frac{7}{2}, \frac{13}{2}, \frac{19}{2}\right\}$

In[61]:= Sin /@ {0, 1, 2, 3}

Out[61]= {0, Sin[1], Sin[2], Sin[3]}

In[62]:= Sin[{1, 2, 3}]

Out[62]= {Sin[1], Sin[2], Sin[3]}

In[63]:= f = .

In[64]:= f[{1, 2, 3}]

Out[64]= {2, 3, 4}

In[66]:= ClearAll[f]

200%

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Untitled-2

```
{Sin[1], Sin[2], Sin[3]}
```

In[63]:= **f** = .

In[64]:= **f**[{1, 2, 3}]

Out[64]=
{2, 3, 4}

In[66]:= **ClearAll**[**f**]

In[67]:= **f**[{1, 2, 3}]

Out[67]=
f[{1, 2, 3}]

In[68]:= **f** /@ {1, 2, 3}

Out[68]=
{**f**[1], **f**[2], **f**[3]}

In[69]:= (**f**[#, 2] &) /@ {1, 2, 3}

Out[69]=
{**f**[1, 2], **f**[2, 2], **f**[3, 2]}

In[70]:= **? /@**

Map[f, expr] or f /@ expr applies f to each element on the first level in expr.
Map[f, expr, levelspec] applies f to parts of expr specified by levelspec. ➤

In[71]:= **f**@{1, 2, 3}

Out[71]=
f[{1, 2, 3}]

first append delete first change head... more...

200%

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Untitled-2

Differential Equations

In[72]:= **D**[**Sin**[**x**], **x**]

Out[72]=

$$\text{Cos}[x]$$

In[73]:= **D**[**Sin**[**x**], **x**, **x**, **x**, **x**]

Out[73]=

$$\text{Sin}[x]$$

In[74]:= **Integrate**[**Sin**[**x**], **x**]

Out[74]=

$$-\text{Cos}[x]$$

Integrate[**Sin**[**x**], {**x**, 0, 2 **Pi**}]

- Piecewise
- Plot
- PieChart
- PillaiTrace
- PillaiTraceTest

200%

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Untitled-2

100% Tue 3 Sep 09:35 Erik Schnetter

In[72]:= **D**[**Sin**[**x**], **x**]

Out[72]=

$$\text{Cos}[x]$$

In[73]:= **D**[**Sin**[**x**], **x**, **x**, **x**, **x**]

Out[73]=

$$\text{Sin}[x]$$

In[74]:= **Integrate**[**Sin**[**x**], **x**]

Out[74]=

$$-\text{Cos}[x]$$

In[75]:= **Integrate**[**Sin**[**x**], {**x**, 0, 2 **Pi**}]

Out[75]=

$$0$$

In[76]:= **Pi**

Out[76]=

$$\pi$$

In[77]:= **N**[**Pi**]

Out[77]=

$$3.14159$$

In[78]:= **Pi** // **N**

Out[78]=

$$3.14159$$

increase precision integer part digits root approximant more...

200%

Mathematica File Edit Insert Format Cell Graphics Evaluation Palettes Window Help

Untitled-2

In[72]:= **D**[**Sin**[**x**], **x**]

Out[72]=

$$\text{Cos}[x]$$

In[73]:= **D**[**Sin**[**x**], **x**, **x**, **x**, **x**]

Out[73]=

$$\text{Sin}[x]$$

In[74]:= **Integrate**[**Sin**[**x**], **x**]

Out[74]=

$$-\text{Cos}[x]$$

In[75]:= **Integrate**[**Sin**[**x**], {**x**, 0, 2 **Pi**}]

Out[75]=

$$0$$

In[76]:= **Pi**

Out[76]=

$$\pi$$

In[77]:= **N**[**Pi**]

Out[77]=

$$3.14159$$

In[78]:= **Pi** // **N**

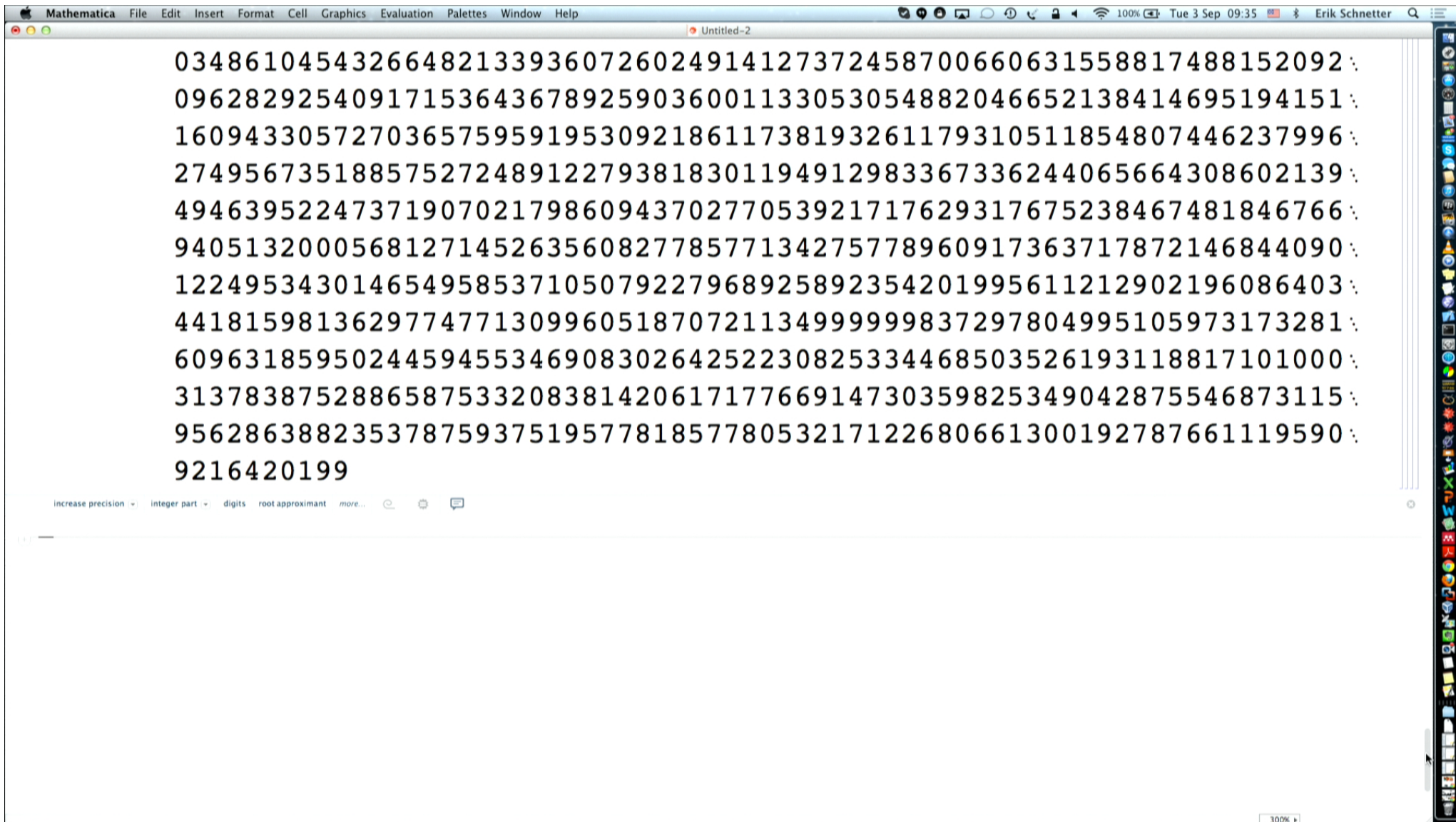
Out[78]=

$$3.14159$$

increase precision integer part digits root approximant more...

50%
75%
100%
125%
150%
✓ 200%
300%

200%



Mathematica File Edit Insert Format Cell Graphics Evaluation Palettes Window Help

Untitled-2

3.14159

In[78]:=

Pi // N

Out[78]=

3.14159

In[80]:=

N[Pi, 1000]

Out[80]=

3.14159265358979323846264338327950288419716939937510582097494459230 \

781640628620899862803482534211706798214808651328230664709384460955 \

058223172535940812848111745028410270193852110555964462294895493038 \

196442881097566593344612847564823378678316527120190914564856692346 \

034861045432664821339360726024914127372458700660631558817488152092 \

096282925409171536436789259036001133053054882046652138414695194151 \

160943305727036575959195309218611738193261179310511854807446237996 \

274956735188575272489122793818301194912983367336244065664308602139 \

494639522473719070217986094370277053921717629317675238467481846766 \

940513200056812714526356082778577134275778960917363717872146844090 \

122495343014654958537105079227968925892354201995611212902196086403 \

441815981362977477130996051870721134999999837297804995105973173281 \

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Untitled-2

781040020020099802005402554211700798214000051520250004709304400955 :
 058223172535940812848111745028410270193852110555964462294895493038 :
 196442881097566593344612847564823378678316527120190914564856692346 :
 034861045432664821339360726024914127372458700660631558817488152092 :
 096282925409171536436789259036001133053054882046652138414695194151 :
 160943305727036575959195309218611738193261179310511854807446237996 :
 274956735188575272489122793818301194912983367336244065664308602139 :
 494639522473719070217986094370277053921717629317675238467481846766 :
 940513200056812714526356082778577134275778960917363717872146844090 :
 122495343014654958537105079227968925892354201995611212902196086403 :
 441815981362977477130996051870721134999999837297804995105973173281 :
 609631859502445945534690830264252230825334468503526193118817101000 :
 313783875288658753320838142061717766914730359825349042875546873115 :
 956286388235378759375195778185778053217122680661300192787661119590 :
 9216420199

In[81]:=

Integrate[x^2 , x]

Out[81]=

$$\frac{x^3}{3}$$

300%

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Untitled-2

058225172555940812848111745028410270195852110555904402294895495058 :
 196442881097566593344612847564823378678316527120190914564856692346 :
 034861045432664821339360726024914127372458700660631558817488152092 :
 096282925409171536436789259036001133053054882046652138414695194151 :
 160943305727036575959195309218611738193261179310511854807446237996 :
 274956735188575272489122793818301194912983367336244065664308602139 :
 494639522473719070217986094370277053921717629317675238467481846766 :
 940513200056812714526356082778577134275778960917363717872146844090 :
 122495343014654958537105079227968925892354201995611212902196086403 :
 441815981362977477130996051870721134999999837297804995105973173281 :
 609631859502445945534690830264252230825334468503526193118817101000 :
 313783875288658753320838142061717766914730359825349042875546873115 :
 956286388235378759375195778185778053217122680661300192787661119590 :
 9216420199

In[82]:=

$$\int x^2 dx$$

Out[82]=

$$\frac{x^3}{3}$$

plot x derivative x integral inverse function more...

300%

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Untitled-2

274956735188575272489122793818301194912983367336244065664308602139 \

494639522473719070217986094370277053921717629317675238467481846766 \

940513200056812714526356082778577134275778960917363717872146844090 \

122495343014654958537105079227968925892354201995611212902196086403 \

441815981362977477130996051870721134999999837297804995105973173281 \

609631859502445945534690830264252230825334468503526193118817101000 \

313783875288658753320838142061717766914730359825349042875546873115 \

956286388235378759375195778185778053217122680661300192787661119590 \

9216420199

In[82]:=

$$\int x^2 dx$$

Out[82]=

$$\frac{x^3}{3}$$

plot x derivative x integral inverse function more...

300%

Mathematica File Edit Insert Format Cell Graphics Evaluation Palettes Window Help

Untitled-2

274956735188575272489122793818301194912983367336244065664308602139 \

494639522473719070217986094370277053921717629317675238467481846766 \

940513200056812714526356082778577134275778960917363717872146844090 \

122495343014654958537105079227968925892354201995611212902196086403 \

441815981362977477130996051870721134999999837297804995105973173281 \

609631859502445945534690830264252230825334468503526193118817101000 \

313783875288658753320838142061717766914730359825349042875546873115 \

956286388235378759375195778185778053217122680661300192787661119590 \

9216420199

In[83]:=

$$\int_0^1 x^2 dx$$

Out[83]=

$$\frac{1}{3}$$

numerical value integer part denominator numerator more...

300%

Mathematica File Edit Insert Format Cell Graphics Evaluation Palettes Window Help

Untitled-2

$\int_0^1 x^2 dx$

Out[83]=

$\frac{1}{3}$

In[85]:=

$\int_{-1}^{+1} \text{Cos}[x] dx$

Out[85]=

$2 \text{Sin}[1]$

In[86]:=

Solve[$x^2 + 1 == 0$, x]

Out[86]=

$\{\{x \rightarrow -i\}, \{x \rightarrow i\}\}$

DSolve[$f'[x] == x$, $f[x]$, x]

300%

Mathematica File Edit Insert Format Cell Graphics Evaluation Palettes Window Help

Untitled-2

$$\int_{-1}^{+1} \text{Cos}[x] \, dx$$

Out[85]=

$$2 \text{Sin}[1]$$

In[86]:=

$$\text{Solve}[x^2 + 1 == 0, x]$$

Out[86]=

$$\{\{x \rightarrow -i\}, \{x \rightarrow i\}\}$$

In[87]:=

$$\text{DSolve}[f'[x] == x, f[x], x]$$

Out[87]=

$$\left\{ \left\{ f[x] \rightarrow \frac{x^2}{2} + C[1] \right\} \right\}$$

In[88]:=

$$\text{DSolve}[f'[x] == x, f, x]$$

Out[88]=

$$\left\{ \left\{ f \rightarrow \text{Function}\left[\{x\}, \frac{x^2}{2} + C[1]\right] \right\} \right\}$$

Assuming a list of rules: Use as a two-dimensional array instead

300%

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Untitled-2

In[86]:=

$$\text{Solve}[x^2 + 1 == 0, x]$$

Out[86]=

$$\{\{x \rightarrow -i\}, \{x \rightarrow i\}\}$$

In[87]:=

$$\text{DSolve}[f'[x] == x, f[x], x]$$

Out[87]=

$$\left\{\left\{f[x] \rightarrow \frac{x^2}{2} + C[1]\right\}\right\}$$

In[88]:=

$$\text{DSolve}[f'[x] == x, f, x]$$

Out[88]=

$$\left\{\left\{f \rightarrow \text{Function}\left[\{x\}, \frac{x^2}{2} + C[1]\right]\right\}\right\}$$

In[89]:=

$$(x + 1)(x - 1) // \text{Simplify}$$

Out[89]=

$$-1 + x^2$$

plot factor x derivative x integral more...

300%

Mathematica File Edit Insert Format Cell Graphics Evaluation Palettes Window Help

Untitled-2

In[98]:=

$$\text{Collect}[(x + y)(x + y) + x^3 + y^2, x]$$

Out[98]=

$$x^2 + x^3 + 2xy + 2y^2$$

In[96]:=

? Collect

Collect[*expr*, *x*] collects together terms involving the same powers of objects matching *x*.
 Collect[*expr*, {*x*₁, *x*₂, ...}] collects together
 terms that involve the same powers of objects matching *x*₁, *x*₂,
 Collect[*expr*, *var*, *h*] applies *h* to the expression that forms the
 coefficient of each term obtained. >>

In[99]:=

? Expand

Expand[*expr*] expands out products and positive integer powers in *expr*.
 Expand[*expr*, *patt*] leaves unexpanded any parts of *expr* that are free of the pattern *patt*. >>

300%

Expand[*expr*] expands out products and positive integer powers in *expr*.
Expand[*expr*, *patt*] leaves unexpanded any parts of *expr* that are free of the pattern *patt*. >>

In[100]:=

? Factor

Factor[*poly*] factors a polynomial over the integers.
Factor[*poly*, Modulus $\rightarrow$ *p*] factors a polynomial modulo a prime *p*.
Factor[*poly*, Extension $\rightarrow$ {*a*₁, *a*₂, ...}] factors a polynomial allowing coefficients that are rational combinations of the algebraic numbers *a*_{*i*}. >>

In[103]:=

Factor[1 + x²]

Out[103]=

1 + x²

? Fac

Factor
FactorInteger
FactorInteger
FactorInteger
FactorInteger
FactorInteger

Mathematica File Edit Insert Format Cell Graphics Evaluation Palettes Window Help

Untitled-2

In[100]:=

? Factor

Factor[*poly*] factors a polynomial over the integers.
 Factor[*poly*, Modulus $\rightarrow p$] factors a polynomial modulo a prime p .
 Factor[*poly*, Extension $\rightarrow \{a_1, a_2, \dots\}$] factors a polynomial allowing coefficients that are rational combinations of the algebraic numbers a_i . $\gg$

In[107]:=

Factor[1 + x^2, Extension $\rightarrow I$]

Out[107]=

$$(-i + x)(i + x)$$

simplify expand x derivative x integral more...

In[104]:=

? Factor

Factor[*poly*] factors a polynomial over the integers.
 Factor[*poly*, Modulus $\rightarrow p$] factors a polynomial modulo a prime p .
 Factor[*poly*, Extension $\rightarrow \{a_1, a_2, \dots\}$] factors a polynomial allowing coefficients that are rational combinations of the algebraic numbers a_i . $\gg$

300%

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Untitled-2

Tue 3 Sep 09:49 Erik Schnetter

In[104]:=

? Factor

Factor[poly] factors a polynomial over the integers.
Factor[poly, Modulus -> p] factors a polynomial modulo a prime p .
Factor[poly, Extension -> { $a_1, a_2, \dots$ }] factors a polynomial allowing coefficients that are rational combinations of the algebraic numbers a_i . ➤

In[108]:=

$x^3 + x^2 + 1$ // TreeForm

Out[108]//TreeForm=

```
graph TD; Plus[Plus] --- 1[1]; Plus --- P1[Power]; Plus --- P2[Power]; P1 --- x1[x]; P1 --- 2[2]; P2 --- x2[x]; P2 --- 3[3];
```

plot x derivative x integral zeros more...

200%

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Untitled-2

Factor[poly] factors a polynomial over the integers.
 Factor[poly, Modulus -> p] factors a polynomial modulo a prime p.
 Factor[poly, Extension -> {a₁, a₂, ...}] factors a polynomial allowing coefficients that are rational combinations of the algebraic numbers a_i. ➤

In[108]:= **x³ + x² + 1 // TreeForm**

Out[108]//TreeForm=

```

graph TD
    Plus[Plus] --- 1[1]
    Plus --- Power1[Power]
    Plus --- Power2[Power]
    Power1 --- x1[x]
    Power1 --- 2[2]
    Power2 --- x2[x]
    Power2 --- 3[3]
  
```

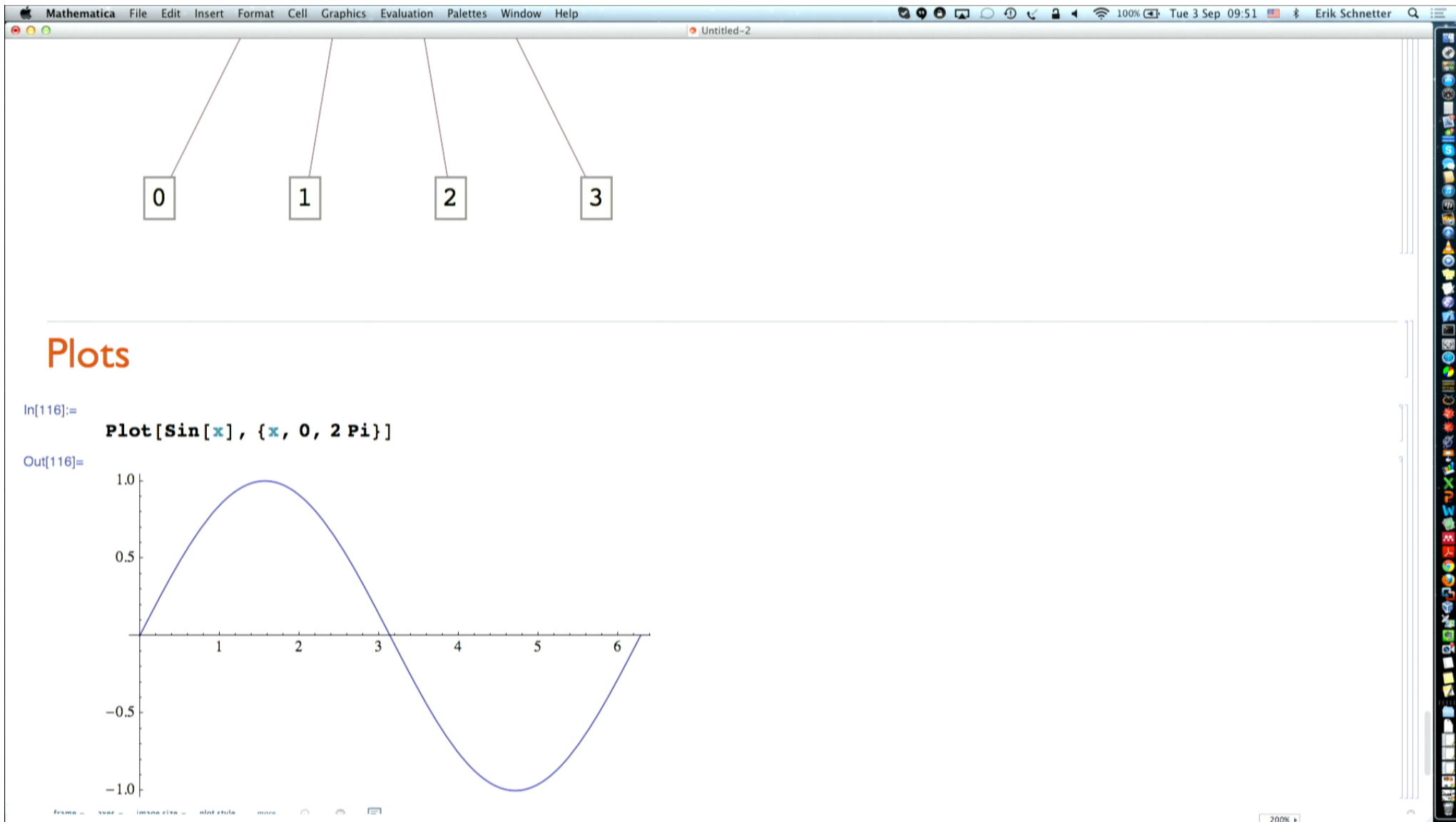
In[109]:= **1 = {1, 2, 3}**

Out[109]= **{1, 2, 3}**

Assuming a vector. Use as a list of digits instead.

total mean max reverse more...

200%



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Untitled-2

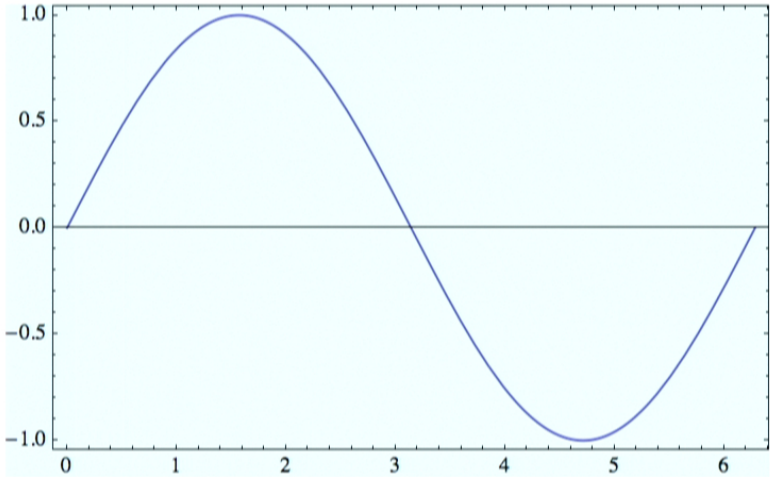
100% Tue 3 Sep 09:53 Erik Schnetter



In[118]:=

```
Show[%117, Background → RGBColor[0.84, 0.92, 1.]]
```

Out[118]=



In[119]:=

↓

? Plot

`Plot[f, {x,  $x_{min}$ ,  $x_{max}$ }]` generates a plot of f as a function of x from x_{min} to x_{max} .

`Plot[{ $f_1$ ,  $f_2$ , ...}, {x,  $x_{min}$ ,  $x_{max}$ }]` plots several functions f_i . ➤

200%

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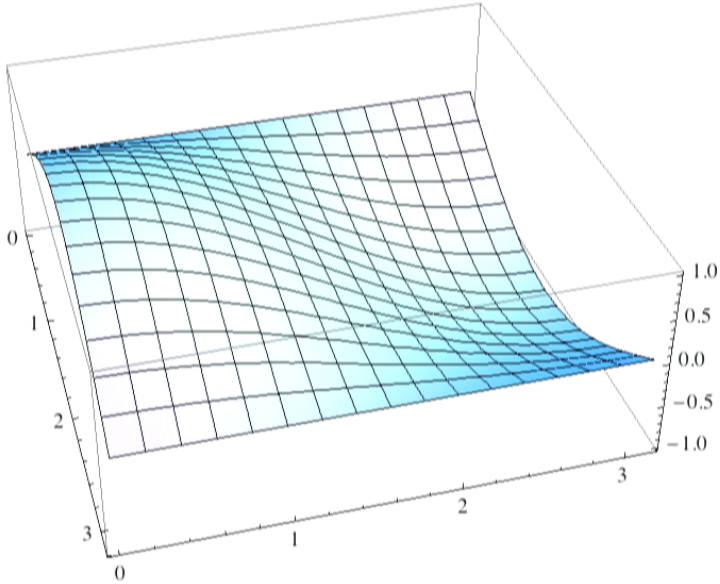
Untitled-2

Tue 3 Sep 09:54 Erik Schnetter

In[122]:=

```
Plot3D[Sin[x] Cos[y], {x, 0, Pi}, {y, 0, Pi}]
```

Out[122]=



In[123]:=

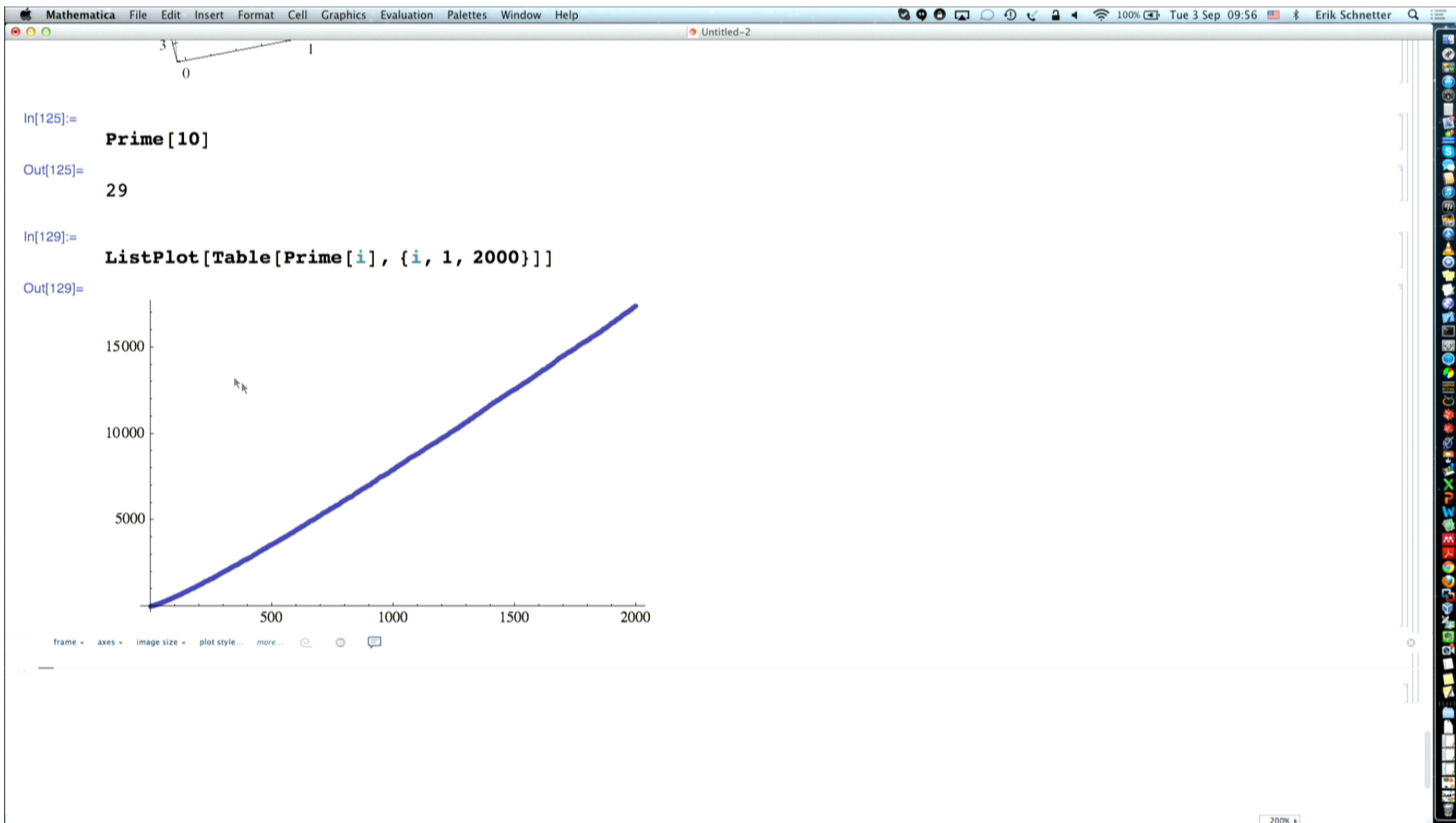
```
Primes[10]
```

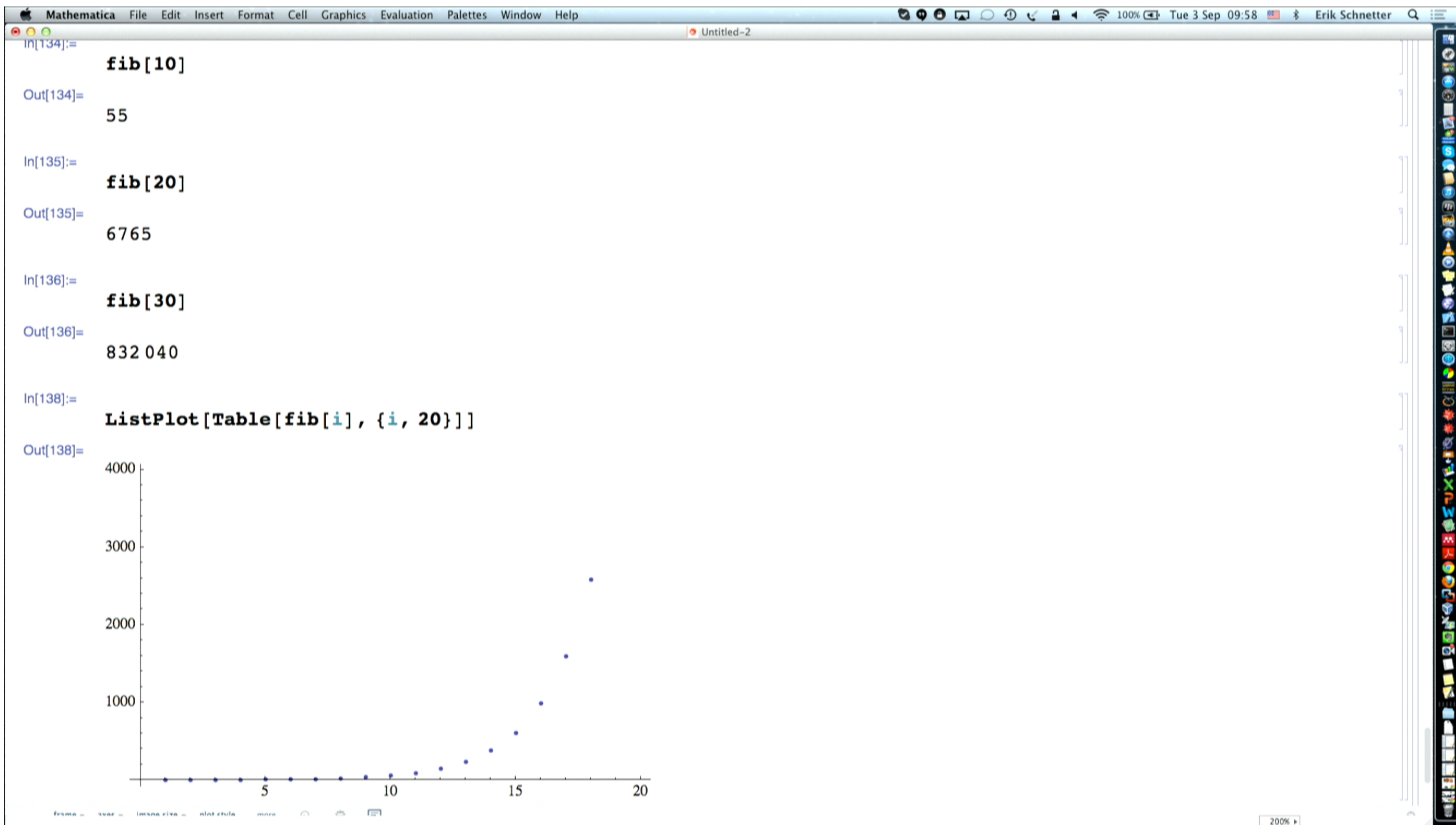
Out[123]=

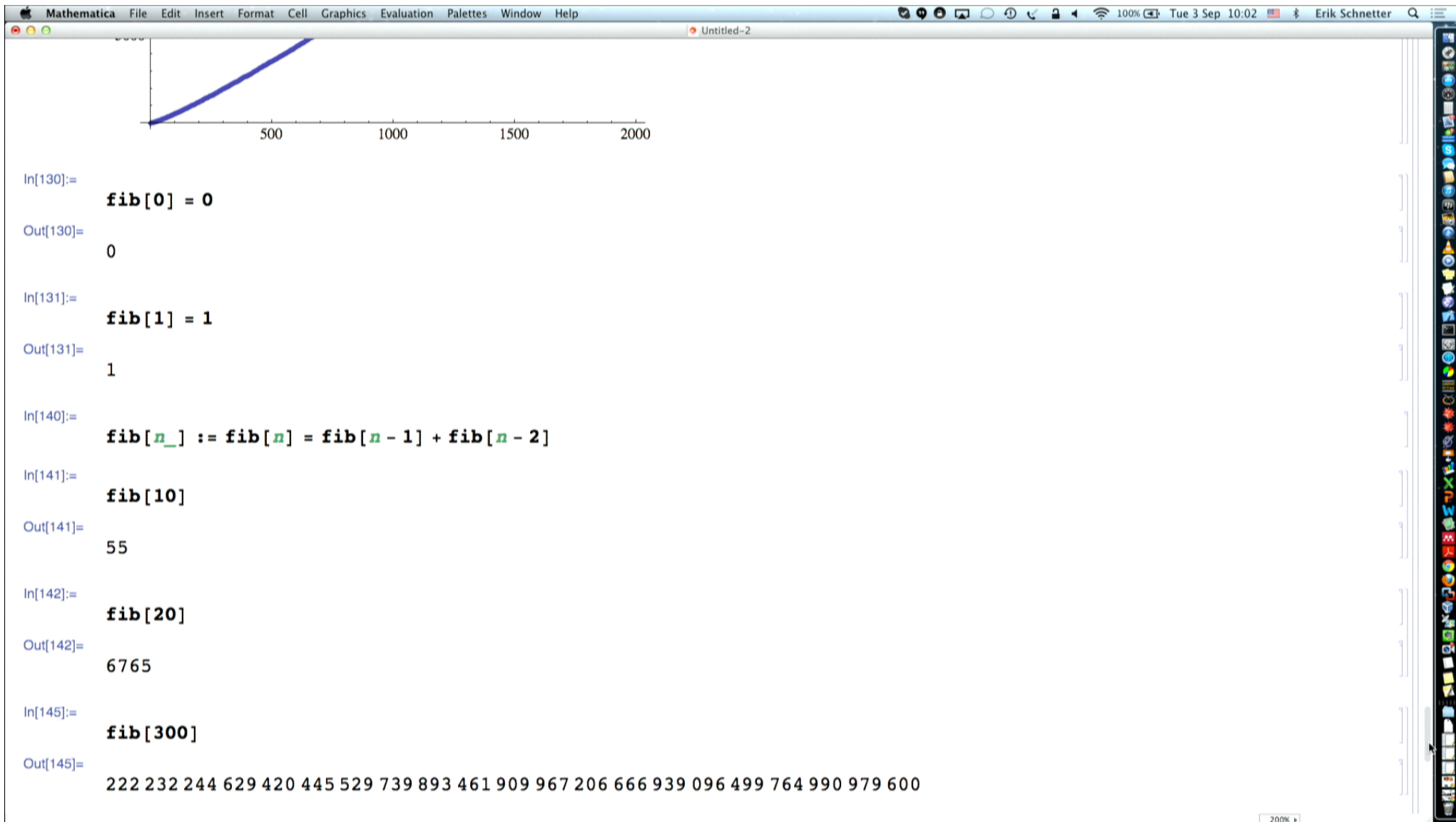
```
Primes[10]
```

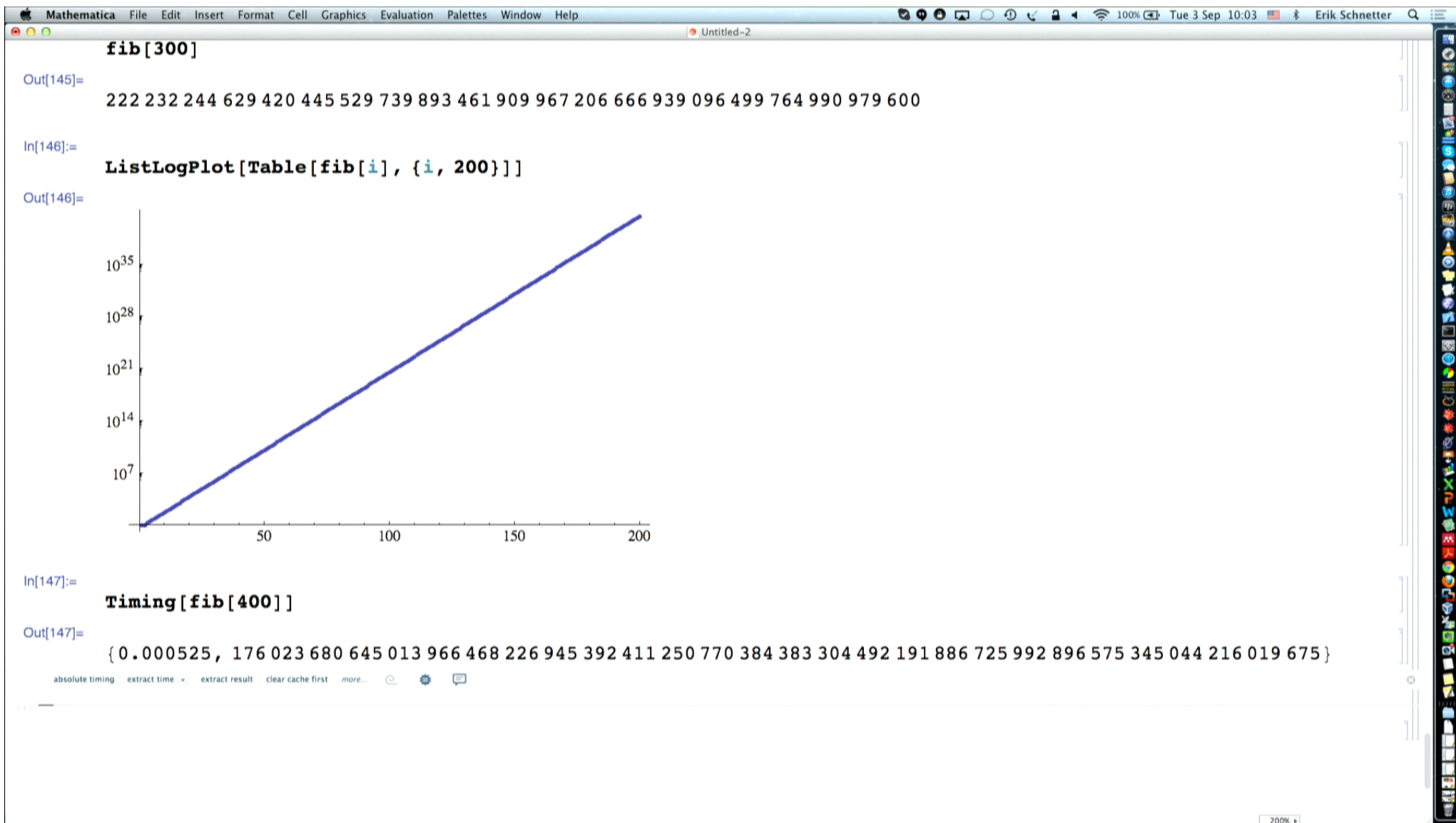
```
Table[Primes[i], {i,
```

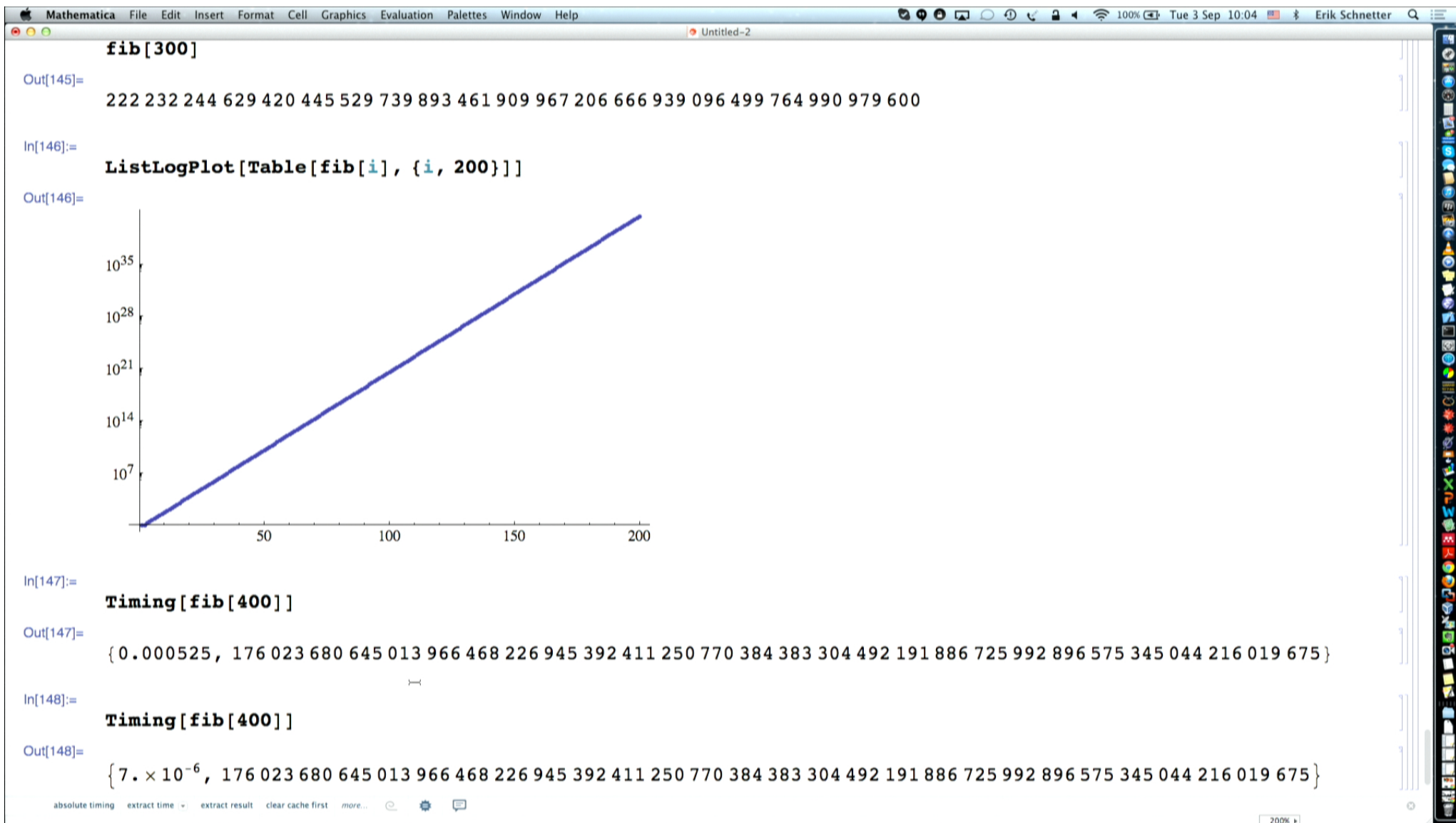
200%











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Untitled-2

50 100 150 200

In[147]:= **Timing[fib[400]]**

Out[147]= {0.000525, 176 023 680 645 013 966 468 226 945 392 411 250 770 384 383 304 492 191 886 725 992 896 575 345 044 216 019 675}

In[148]:= **Timing[fib[400]]**

Out[148]= { $7. \times 10^{-6}$, 176 023 680 645 013 966 468 226 945 392 411 250 770 384 383 304 492 191 886 725 992 896 575 345 044 216 019 675}

Modules

```
ff[x_, y_] := Module[{a, b}
```

200%

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Untitled-2

5
4

In[152]:=

a

Out[152]=

a

Low-level Programming

In[153]:=

Table[**i**, {**i**, 10}]

Out[153]=

{1, 2, 3, 4, 5, 6, 7, 8, 9, 10}

In[154]:=

Do[**Print**[**i**], {**i**, 10}]

1
2
3
4
5
6
7
8
9
10

200%

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Untitled-2

In[155]:=

```
numbers = Table[i, {i, 10}]
```

Out[155]=

```
{1, 2, 3, 4, 5, 6, 7, 8, 9, 10}
```

In[156]:=

```
numbers
```

Out[156]=

```
{1, 2, 3, 4, 5, 6, 7, 8, 9, 10}
```

In[157]:=

```
nonnumbers = Do[Print[i], {i, 10}]
```

```
1
2
3
4
5
6
7
8
9
10
```

In[160]:=

```
nonnumbers
```

200%