Title: 3D Digital Holographic Interferometry: Applications in Biomedicine

Date: Aug 16, 2013 04:25 PM

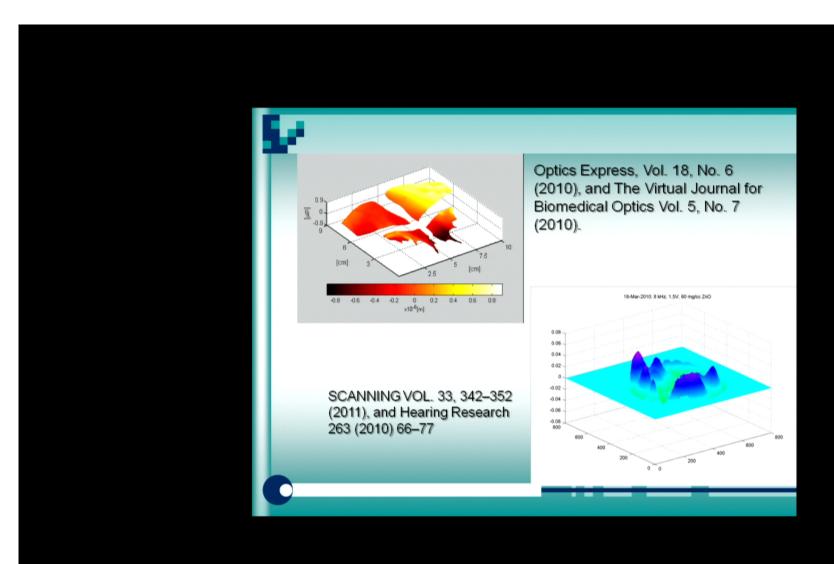
URL: http://pirsa.org/13080047

Abstract: <span>Digital Holographic Interferometry (DHI) plays an important role in the evaluation of object static and dynamic displacements. The state of the art research on this technique is such that it is being used to solve problems in a wide variety of disciplines, from basic Physics to engineering and even social sciences. This invited plenary talk will deal with specific applications in some biomedical objects, even showing preliminary results using Electron Holography.

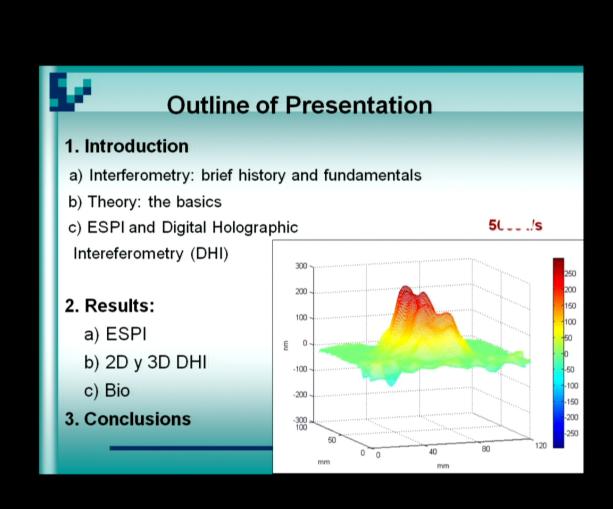
Pirsa: 13080047 Page 1/44



Pirsa: 13080047



Pirsa: 13080047 Page 3/44



Pirsa: 13080047 Page 4/44



### **Definitions**

Interferometry: superposition of n E-M beams in space. The result of interefrence depends on the phase relations between the beams.

Interefrence relates to the interaction betwen propagating beams,

while refraction, scattering and diffraction depend on the interaction between a beam and matter.

Pirsa: 13080047 Page 5/44



### A short history of interferometry

- XVIIc. R. Boyle, R. Hook, observation and analysis of interference effects in a thin air layer limited by two glass plates which demonstrated the wave nature of light
- 2. 1690 C. Huygens, Huyghens theorem (beginning of the wave theory of light)

  Each element of a wavefront may be regarded as the center of a secondary disturbance which gives rise to spherical wevelets and the position of the wevefront at any latter time is the envelope of such wevelets
- 3. 1738 T. Young experiment confirmed Huyghens' hipothesis and gave the basis to modern theory of light coherence
- 4. 1818 A. Fresnel extension of Huyghens theorem, leading to so-called Huyghens-Fresnel principle great importance in the diffraction theory and the basic postulate of the wave theory of light, development of stellar interferometry

1a. 1874 Lord Rayleigh used for the first time moire phenomenon <sup>5</sup>

Pirsa: 13080047 Page 6/44



## A short history of interferometry

- 1881 Michelson experiment (speed of light) and his further works on interferometry, stellar interferometry, high resolution interferometric spectroscopy - he is considered as the father of interferometry (Nobel prize 1907)
- 6. 1916 F. Twyman modifications of Michelson ineterferometer
- 7. 1960 invention of laser: Schawlow, Maiman, Townes, Prochorow....
- 8. 1948 Gabor principles of holography
- 1962 -Leith and Upatnieks off-axis holography and development of holographic interferometry (works of Burch, Brooks, Collier, Stetson...)
- 10. 1970 Archbold, Leendertz speckle interferometry and speckle photography
- 11. 1982- ..Development of phase based interferogram analysis methods
- 11. 1995-....Rapid progress in digital holography
- 12. 2000-...Rapid progress in active interferometry and holography

6

Pirsa: 13080047 Page 7/44



#### Vector of electric field

$$\overline{E}_{i}(\bar{r},t) = \overline{E}_{i0} exp[i(\phi_{i}(\bar{r}) - \omega_{i}t)]$$

Resultant vector in two beam interferometry

$$\overline{E}(\overline{r},t) = \sum_{i} \overline{E}_{i}(\overline{r},t);$$
  $i = 1,2$ 

Result of two beam interference (E field intensity):

$$\mathbf{I(r)\alpha} \ \left|\overline{\mathbf{E}}\right|^2 = \left|\overline{\mathbf{E_1}} + \overline{\mathbf{E_2}}\right|^2 = \left(\overline{\mathbf{E_1}} + \overline{\mathbf{E_2}}\right) \left(\overline{\mathbf{E_1}} + \overline{\mathbf{E_2}}\right)^* = \overline{\mathbf{E_1}} \overline{\mathbf{E_1}}^* + \overline{\mathbf{E_2}} \overline{\mathbf{E_2}}^* + \overline{\mathbf{E_1}} \overline{\mathbf{E_2}}^* + \overline{\mathbf{E_1}} \overline{\mathbf{E_2}}^*$$

$$I(\bar{r}) = I_1 + I_2 + I_{12} = I_1 + I_2 + 2\sqrt{I_1I_2} cos[(\phi_1(\bar{r}) - \phi_2(\bar{r})) - (\omega_1t - \omega_2t)]$$

Conditions for stationary interference field:

$$\omega_1 = \omega_2$$

$$\varphi_1(\overline{r}) - \varphi_2(\overline{r}) = const$$
.

Recommended: parallel polarization of beams



Vector of electric field

$$\overline{E}_{i}(\overline{r},t) = \overline{E}_{i0} exp[i(\phi_{i}(\overline{r}) - \omega_{i}t)]$$

Resultant vector in two beam interferometry

$$\overline{E}(\overline{r},t) = \sum_{i} \overline{E}_{i}(\overline{r},t);$$
  $i = 1,2$ 

Result of two beam interference (E field intensity):

$$\mathbf{I(r)\alpha} \ \left|\overline{\mathbf{E}}\right|^2 = \left|\overline{\mathbf{E_1}} + \overline{\mathbf{E_2}}\right|^2 = \left(\overline{\mathbf{E_1}} + \overline{\mathbf{E_2}}\right) \left(\overline{\mathbf{E_1}} + \overline{\mathbf{E_2}}\right)^* = \overline{\mathbf{E_1}} \overline{\mathbf{E_1}}^* + \overline{\mathbf{E_2}} \overline{\mathbf{E_2}}^* + \overline{\mathbf{E_1}} \overline{\mathbf{E_2}}^* + \overline{\mathbf{E_1}} \overline{\mathbf{E_2}}^*$$

$$I(\bar{r}) = I_1 + I_2 + I_{12} = I_1 + I_2 + 2\sqrt{I_1I_2} cos[(\phi_1(\bar{r}) - \phi_2(\bar{r})) - (\omega_1t - \omega_2t)]$$

Conditions for stationary interference field:

$$\omega_1 = \omega_2$$

$$\varphi_1(\overline{r}) - \varphi_2(\overline{r}) = const$$
.

Recommended: parallel polarization of beams



#### Vector of electric field

$$\overline{E}_{i}(\overline{r},t) = \overline{E}_{i0} exp[i(\phi_{i}(\overline{r}) - \omega_{i}t)]$$

Resultant vector in two beam interferometry

$$\overline{\mathbf{E}}(\bar{r},t) = \sum_{i} \overline{\mathbf{E}}_{i}(\bar{r},t); \qquad i = 1,2$$

Result of two beam interference (E field intensity):

$$\mathbf{I(r)\alpha} \ \left|\overline{\mathbf{E}}\right|^2 = \left|\overline{\mathbf{E_1}} + \overline{\mathbf{E_2}}\right|^2 = \left(\overline{\mathbf{E_1}} + \overline{\mathbf{E_2}}\right) \left(\overline{\mathbf{E_1}} + \overline{\mathbf{E_2}}\right)^* = \overline{\mathbf{E_1}} \overline{\mathbf{E_1}}^* + \overline{\mathbf{E_2}} \overline{\mathbf{E_2}}^* + \overline{\mathbf{E_1}} \overline{\mathbf{E_2}}^* + \overline{\mathbf{E_1}} \overline{\mathbf{E_2}}^*$$

$$I(\bar{r}) = I_1 + I_2 + I_{12} = I_1 + I_2 + 2\sqrt{I_1I_2} cos[(\phi_1(\bar{r}) - \phi_2(\bar{r})) - (\omega_1t - \omega_2t)]$$

Conditions for stationary interference field:

$$\omega_1 = \omega_2$$

$$\varphi_1(\overline{r}) - \varphi_2(\overline{r}) = const$$
.

Recommended: parallel polarization of beams



lm

For  $\omega_1 = \omega_2$  (usually one source applied)

$$I(\bar{r}) = I_1 + I_2 + 2\sqrt{I_1I_2}cos\left(\phi_1(\bar{r}) - \phi_2(\bar{r})\right) = a(\bar{r}) + b(\bar{r})\cos\phi(\bar{r}) \cong 1 + \gamma(\bar{r})\cos\phi(\bar{r})$$

Where a(r) and b(r) are background and fringe modulation functions

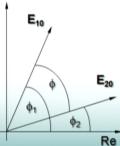
$$\gamma = \frac{2\sqrt{I_1I_2}}{I_1 + I_2}$$

is the interferogram contrast  $% \left( \mathbf{r}_{\mathbf{r}}\right) =\mathbf{r}_{\mathbf{r}}$ 

$$\varphi(\bar{r}) = \varphi_1(\bar{r}) - \varphi_2(\bar{r})$$

is the phase difference between the interfering beams

Graphic representation of interf. E vectors



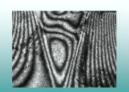


$$I = |a|^2 = (a_1 + a_2) (a_1^* + a_2^*) =$$

$$A_1^2 + A_2^2 + A_1 A_2 e^{i(\varphi_2 - \varphi_1)} + A_1 A_2 e^{-i(\varphi_2 - \varphi_1)} =$$

$$I_1 + I_2 + 2 \sqrt{I_1 I_2} \cos \Delta \varphi \quad (3)$$
where  $\Delta \varphi = \varphi_1 - \varphi_2$ .

Output: interferogram





# Modifications to interferograms help retrieve the imbeded phase

$$I(x, y, t) = a(x, y) + b(x, y)cos[2\pi [(f_{ox}x + f_{oy}y) + \nu_{o}(t)] + \alpha(t) + \phi(x, y)]$$

Required controlled modifications of phase in FP:

 $v_0(t)$  – introduces temporal heterodyning (running fringes)

 $\alpha(t)$  – introduces controlled phase shifts

 $f_{0x}$ ,  $f_{0y}$  – introduce spatial carrier fringes (spatial heterodyning)

However the requirement to get a high quality interferogram: Source with spatial and temporal coherence:

11

Pirsa: 13080047 Page 13/44



# Modifications to interferograms help retrieve the imbeded phase

$$I(x, y, t) = a(x, y) + b(x, y)cos[2\pi [(f_{ox}x + f_{oy}y) + \nu_{o}(t)] + \alpha(t) + \phi(x, y)]$$

Required controlled modifications of phase in FP:

 $v_0(t)$  – introduces temporal heterodyning (running fringes)

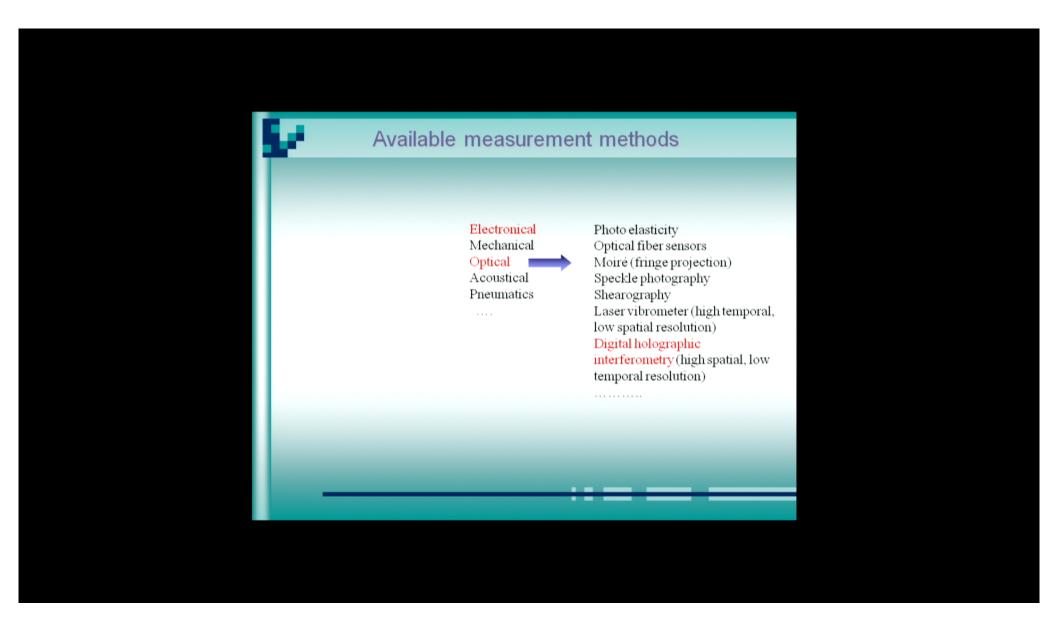
 $\alpha(t)$  – introduces controlled phase shifts

 $f_{0x}$ ,  $f_{0y}$  – introduce spatial carrier fringes (spatial heterodyning)

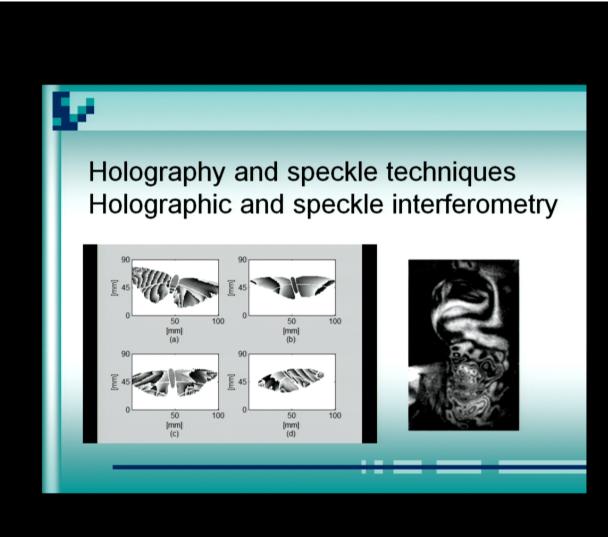
However the requirement to get a high quality interferogram: Source with spatial and temporal coherence:

11

Pirsa: 13080047 Page 14/44

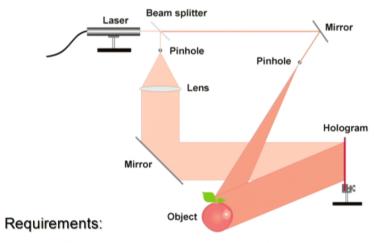


Pirsa: 13080047 Page 15/44



Pirsa: 13080047

### Registration of optical hologram basic setup



1. Need to have equal optical paths of reference and object beams (within coherence length of laser)

2. During recording the phase between object and reference beams cannot change more than  $\Delta\phi_{\rm max} < 0.2\pi$ 



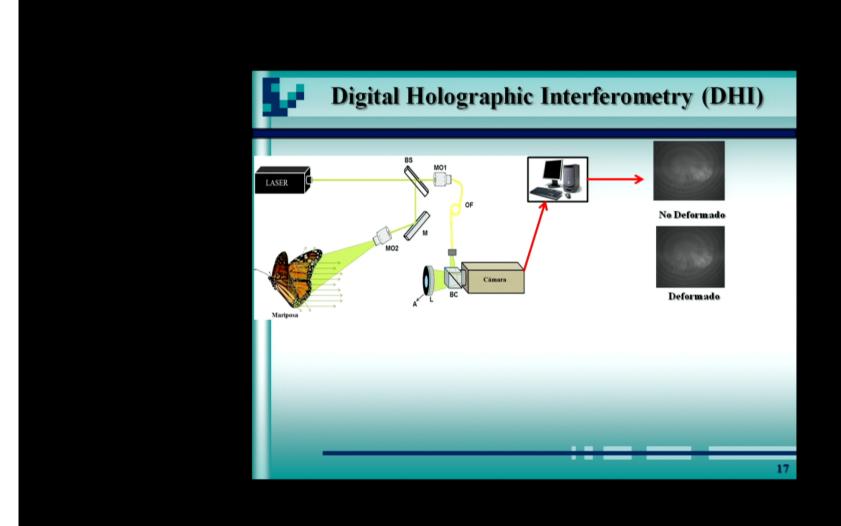
### **Basic Theoretical Considerations**

Two wave addition: Object and Reference

$$U_{\rm T} = U_{\rm o} + U_{\rm r} \tag{1}$$

Intensity/Irradiance on the CCD sensor is proportional to

$$I_{T} = U_{o}^{\dagger}U_{o} + U_{r}^{\dagger}U_{r} + U_{o}U_{r}^{\dagger} + U_{r}U_{o}^{\dagger}$$
 (2)



Pirsa: 13080047 Page 19/44

### Limitations of digital holography

The recording medium has to fulfil the Nyquist condition! Each fringe has to be sampled by at least two pixels of CCD matrix

CCD cameras;

- resolution 1024x1534;
- Pixel size  $\Delta = 9\mu m$ ; for 4.5  $\mu$ m
- Spatial resolution ap. 111 lines/mm, 220l/mm holographic materials (plates) >3000 lines/mm). Limitations

$$\delta = \lambda / \left(2\sin(\gamma / 2)\right) \qquad \qquad \text{Assumption.: } \gamma \approx \sin\gamma \approx \tan\gamma$$

$$\text{For small } \gamma \qquad \qquad \gamma \leq \lambda / \left(2\Delta\right)$$

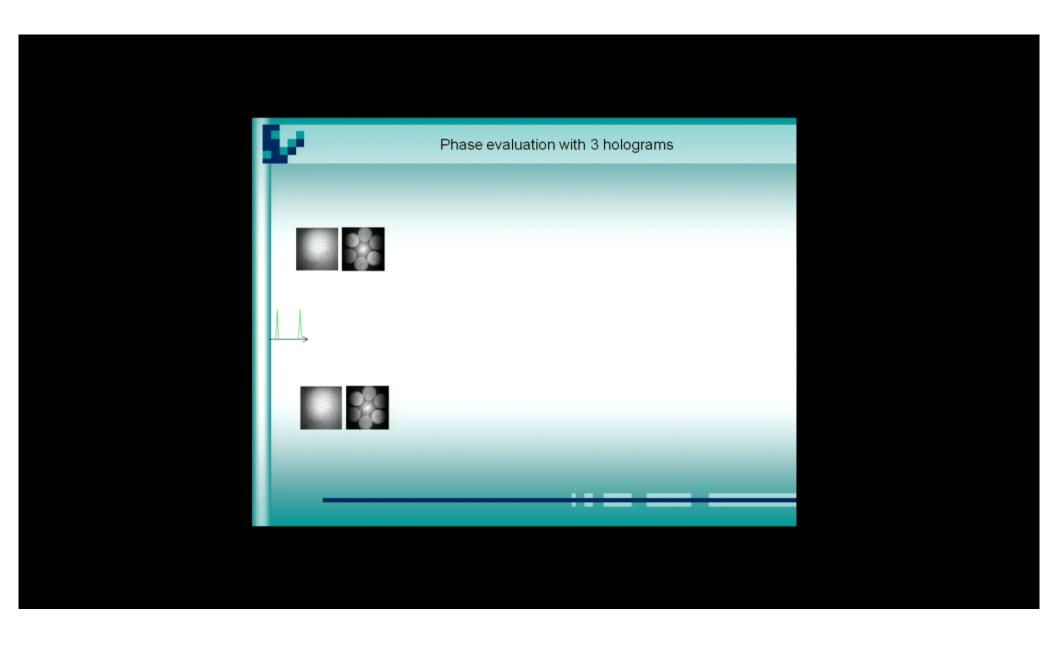
$$2\Delta \leq \delta \qquad \qquad = \rangle \qquad \qquad \text{for } \lambda = 632.8 \,\text{nm and } \Delta = 9 \,\mu\text{m}, \ \gamma \approx 3.5^{\circ}$$

Conclusion: SMALL angular size of object (a few degrees) i.e.

**SMALL OBJECT or Object SITUATED FAR from CAMERA** 

18

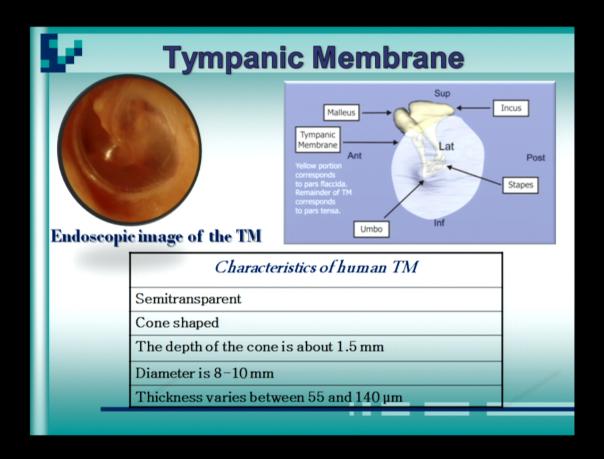
Pirsa: 13080047 Page 20/44



Pirsa: 13080047 Page 21/44



Pirsa: 13080047 Page 22/44

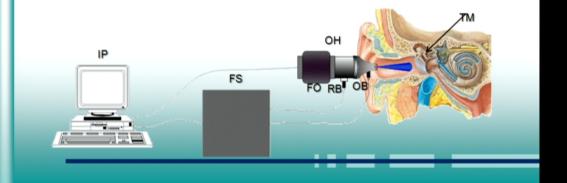


Pirsa: 13080047 Page 23/44

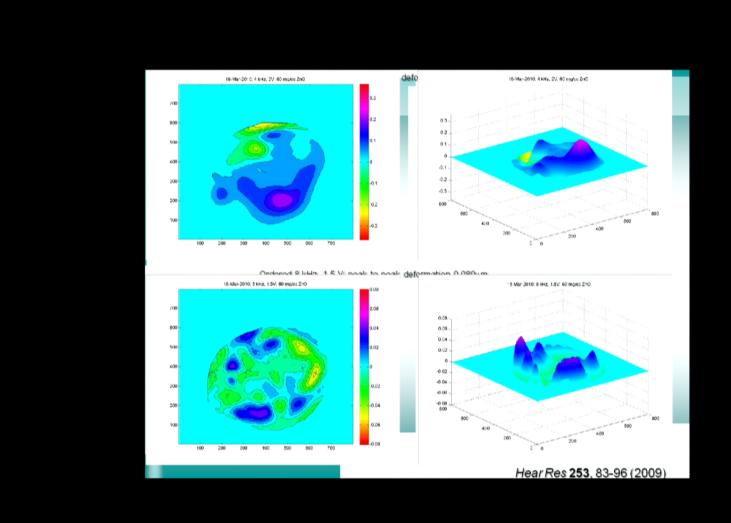


#### The inspection system consists of:

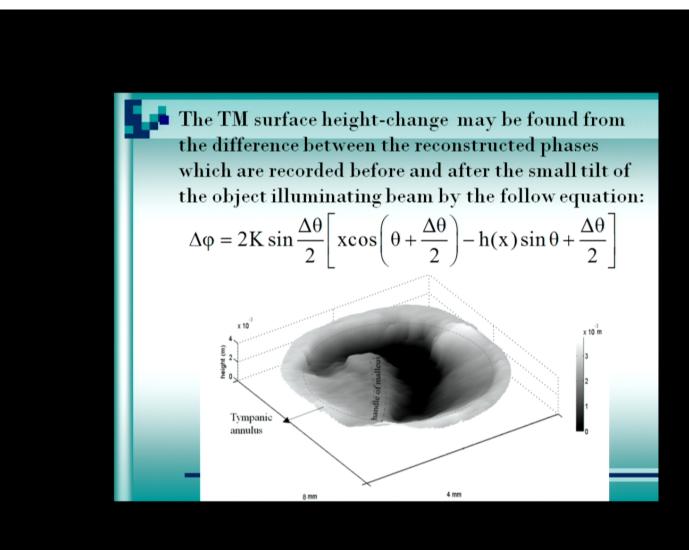
- High speed PC with dedicated software and hardware,
- Fiber optics, FS, and
- A compact optics head resembling an otoscope, OH

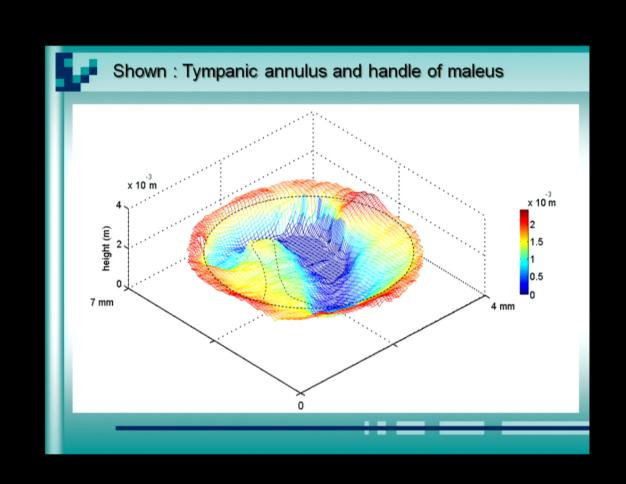


Pirsa: 13080047 Page 24/44

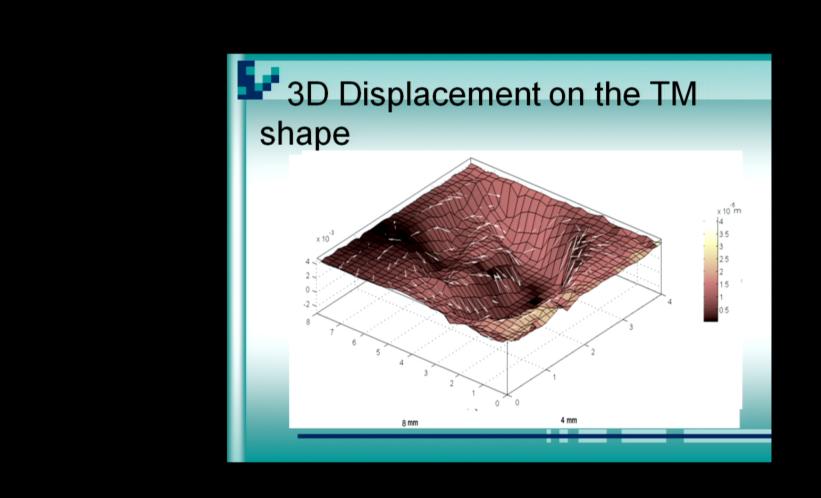


Pirsa: 13080047 Page 25/44





Pirsa: 13080047



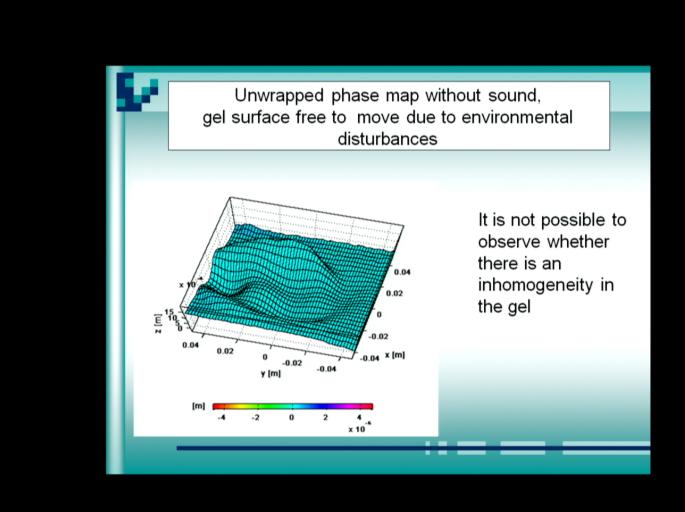
Pirsa: 13080047 Page 28/44



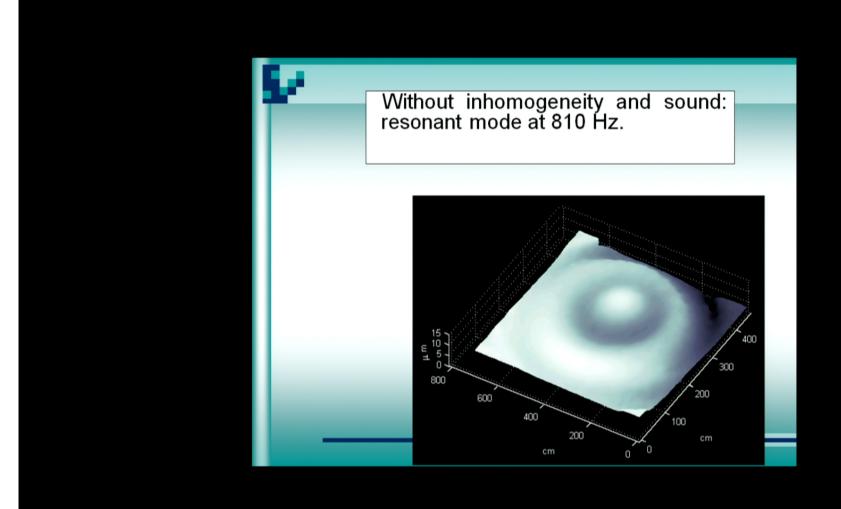
# INHOMOGENEITIES DETECTION (TUMORS)

- Input sound power of approximately 661 mW, equivalent to a pressure of 2.3 x 105 pa.
- Laser pulse separation 14 ms, at 532 nm, 15 ns pulse width, 20 mJ/pulse, average power of 0.639 μW/cm² at the surface, and 6 m of coherence length.
- CCD with 1024 by 1280 pixels at 12 bits.
- Phantom is a semi sphere with an 8.4 cm in diameter and 4 cm height.

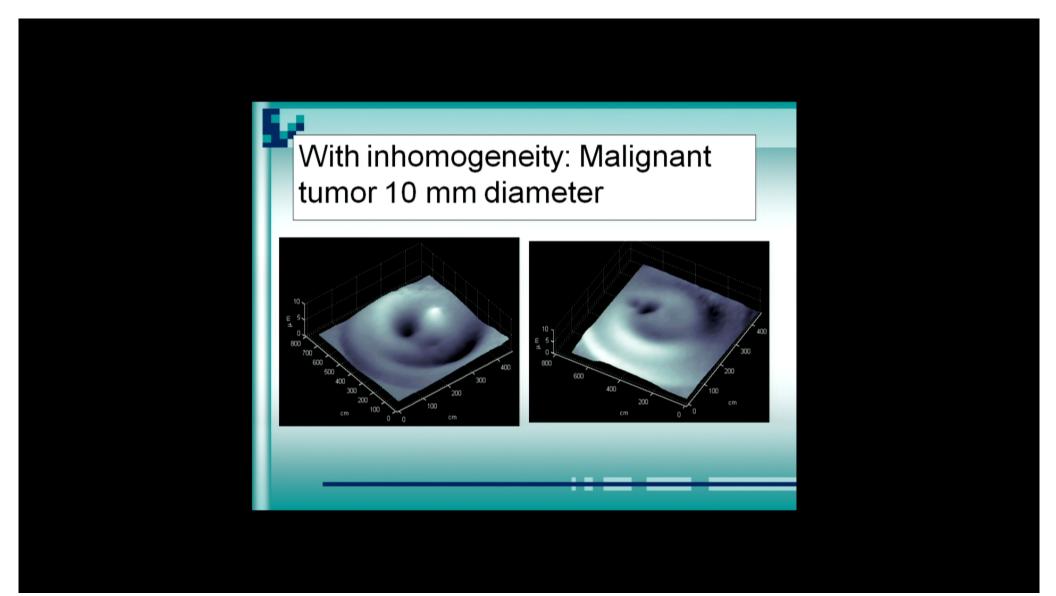
Pirsa: 13080047 Page 29/44



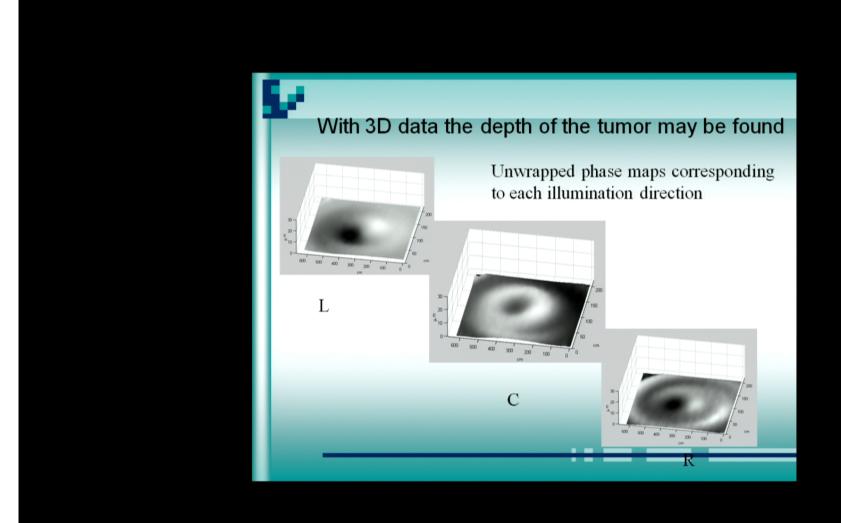
Pirsa: 13080047 Page 30/44



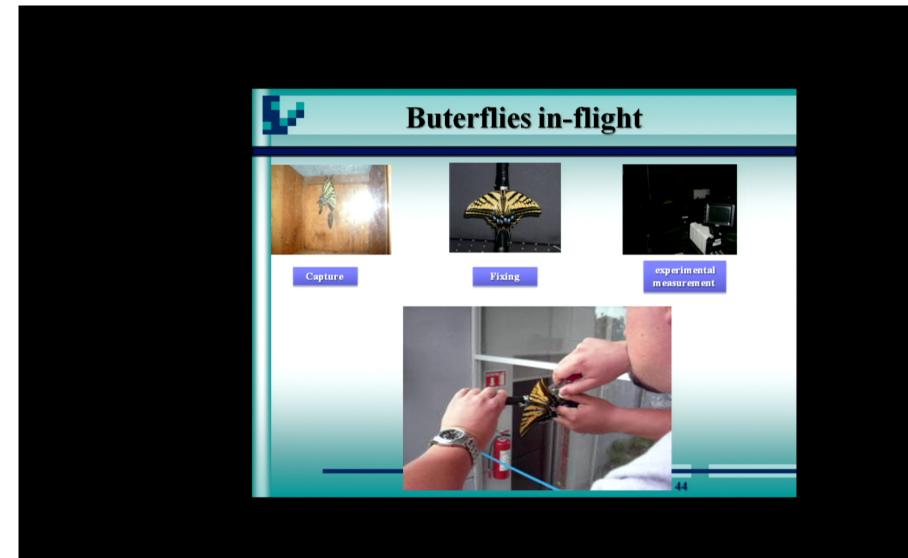
Pirsa: 13080047 Page 31/44



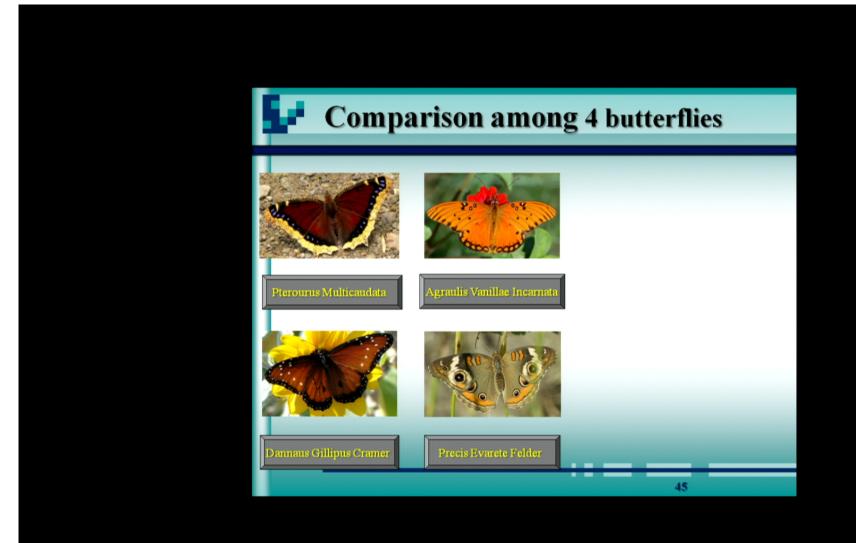
Pirsa: 13080047 Page 32/44



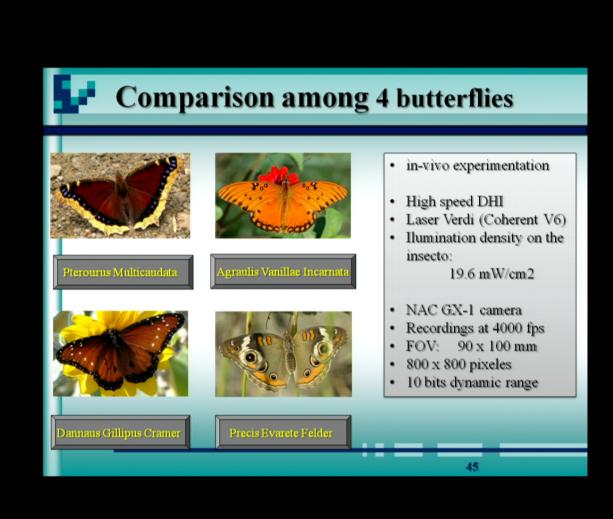
Pirsa: 13080047 Page 33/44



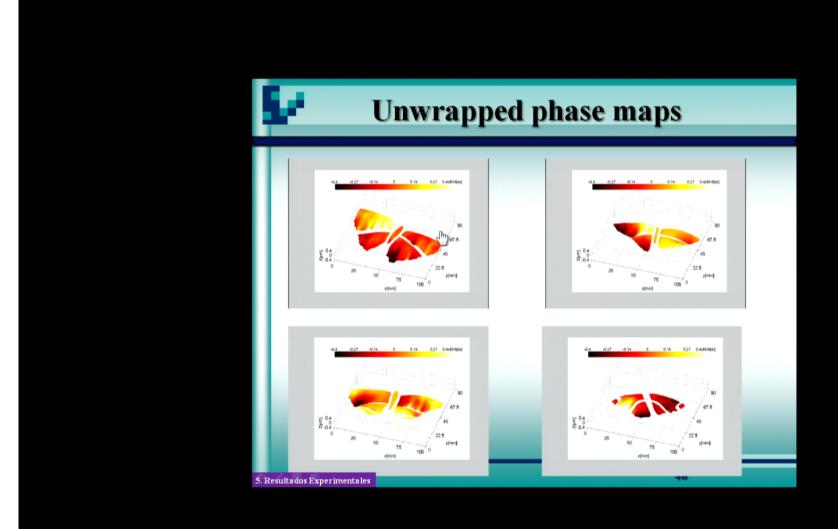
Pirsa: 13080047 Page 34/44



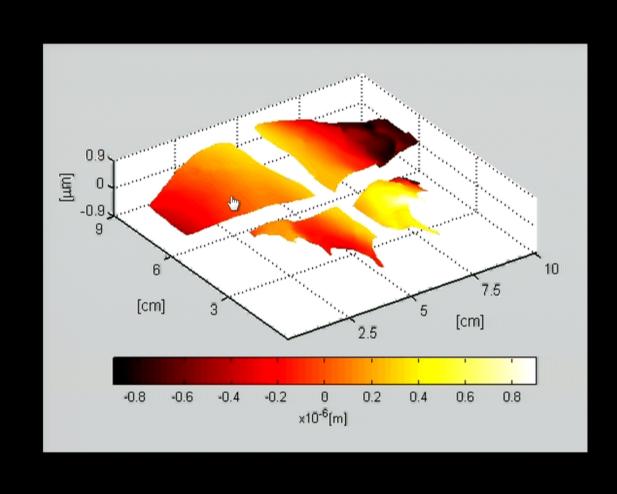
Pirsa: 13080047 Page 35/44



Pirsa: 13080047 Page 36/44



Pirsa: 13080047 Page 37/44



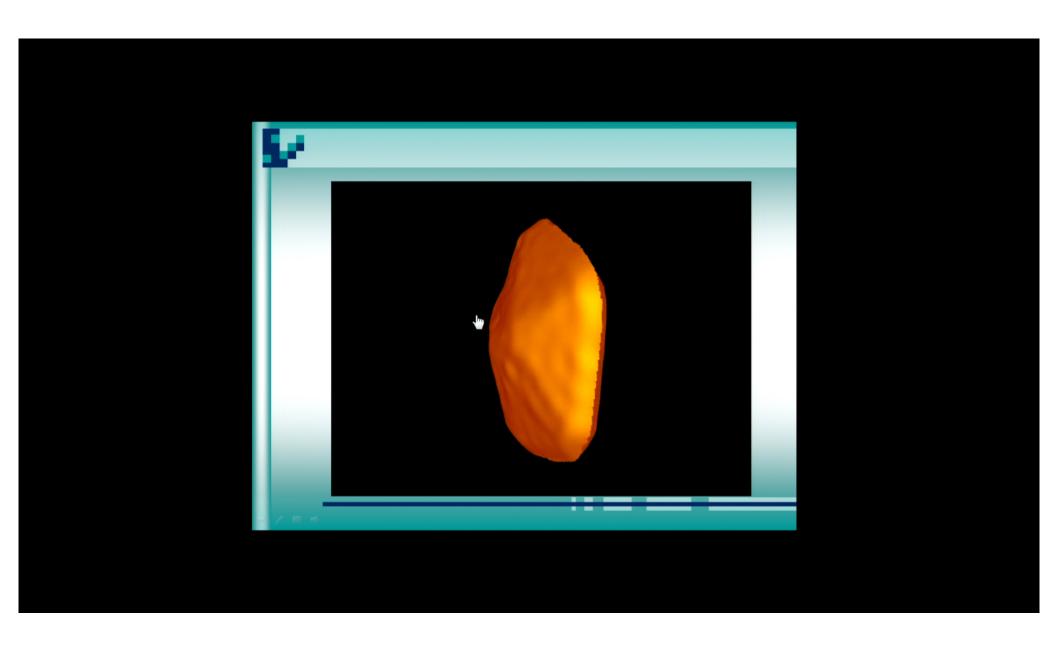
Pirsa: 13080047 Page 38/44



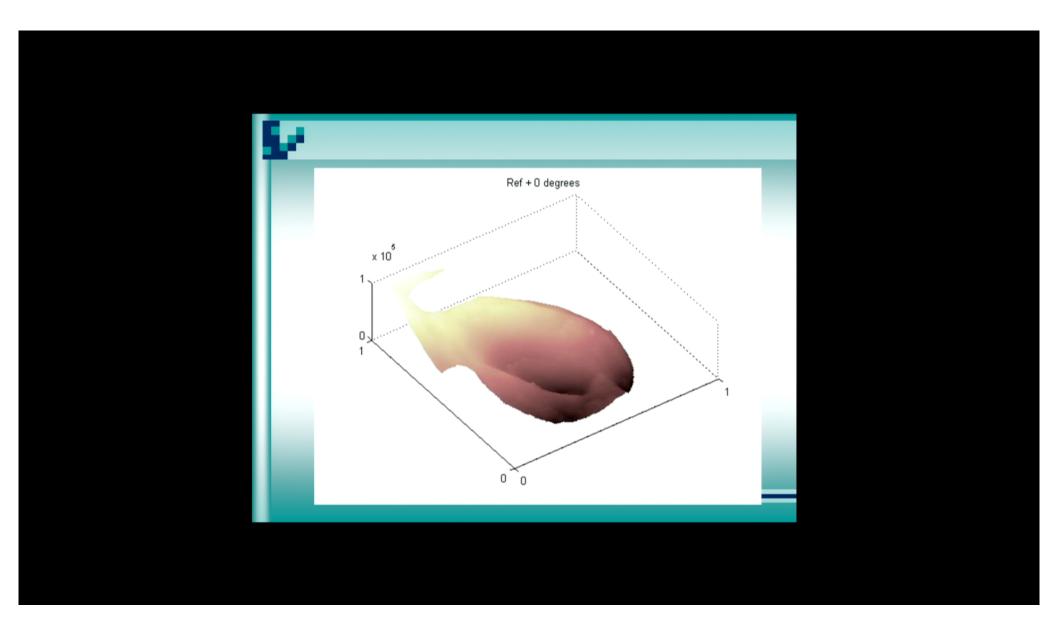
## BACTERIAAND NANOPARTICLES

Determination of the surface morphology of gold-decahedra nanoparticles using an off-axis electron holography dual-lens imaging system, accepted in Micron

Pirsa: 13080047 Page 39/44



Pirsa: 13080047 Page 40/44



Pirsa: 13080047 Page 41/44



## Research Team

- Dra. María del Socorro Hernández Montes
- Dr. Carlos Pérez López
- Dr. Manuel De la Torre Ibarra
- Dr. Jorge Mauricio Flores
- Jesus Cantu, Dr. Arturo Ponce and Prof.
   Miguel Jose Yacaman, UTSA

Pirsa: 13080047 Page 42/44



Pirsa: 13080047 Page 43/44



Pirsa: 13080047 Page 44/44