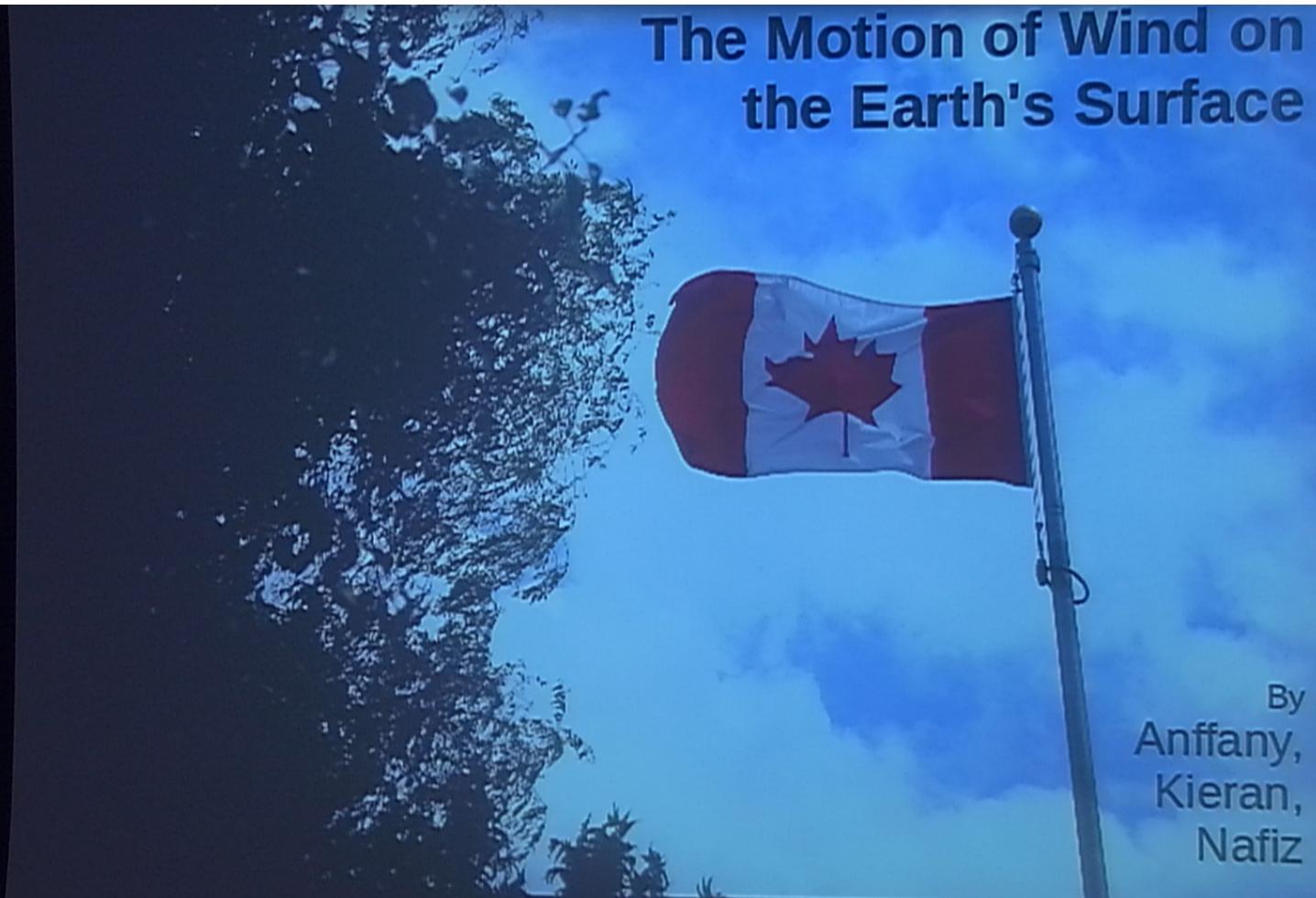


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Date: Aug 16, 2013 03:30 PM

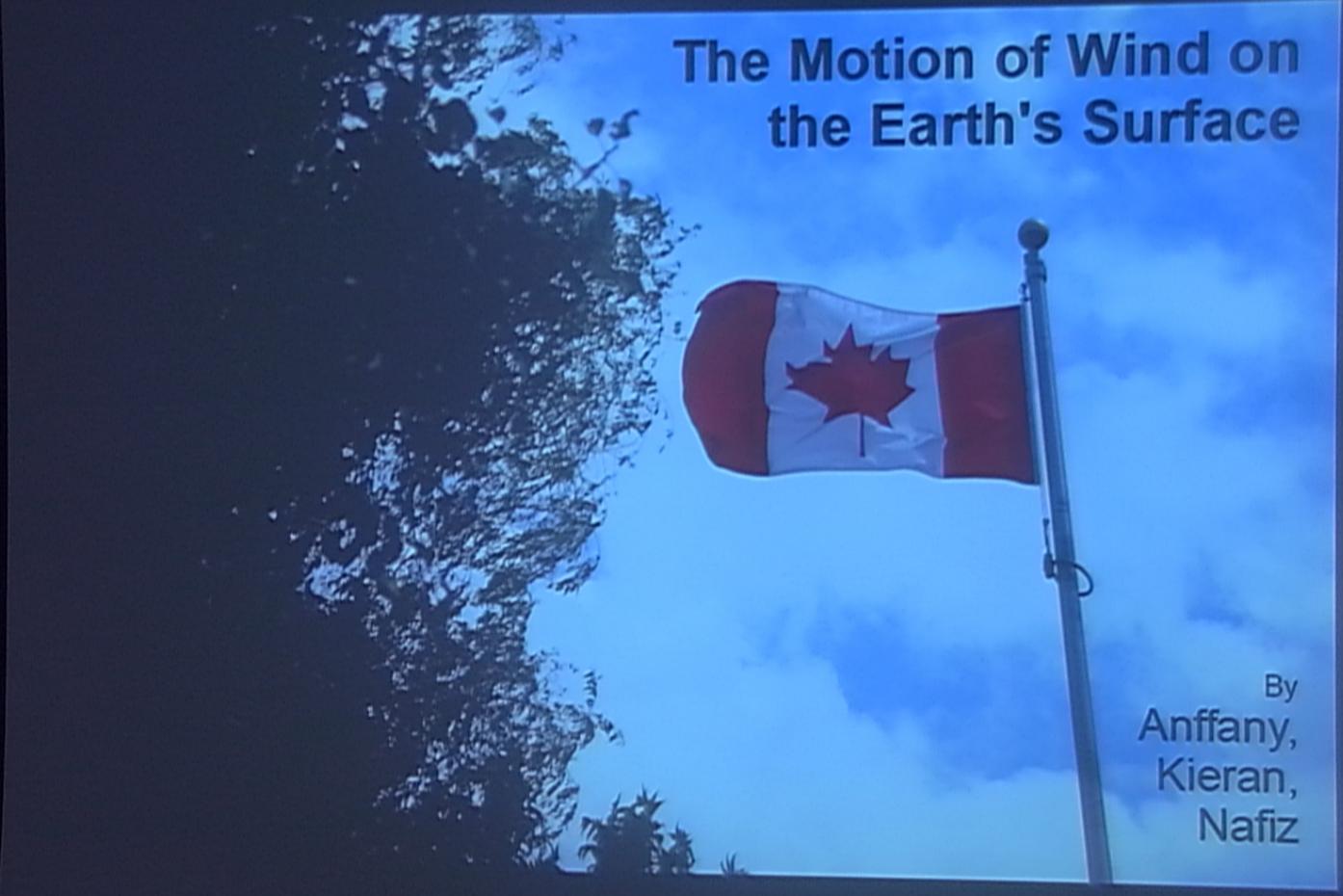
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Abstract:



The Motion of Wind on the Earth's Surface

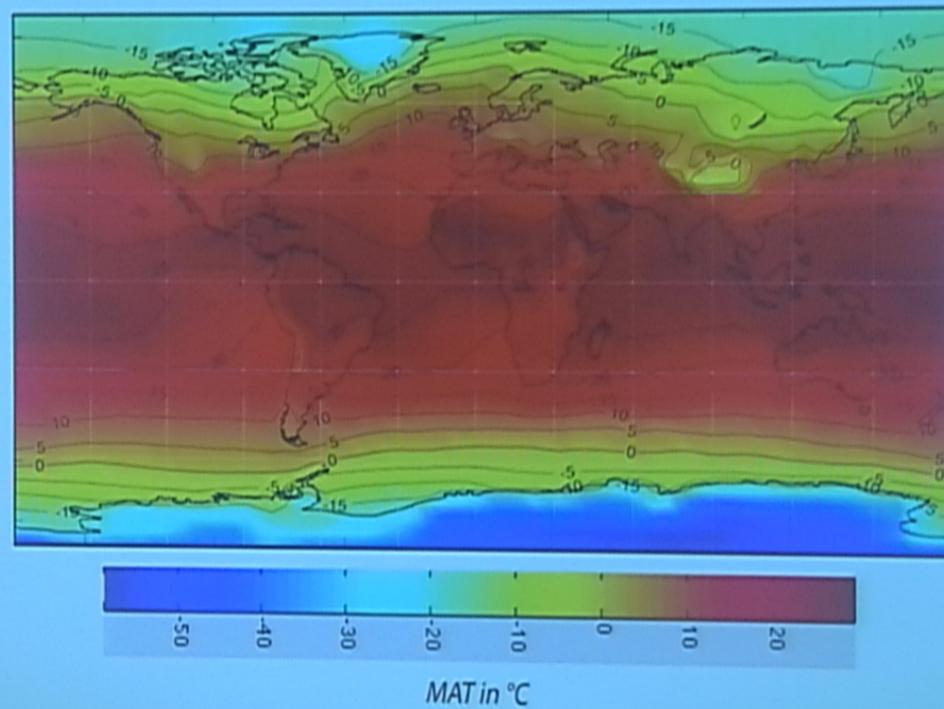
By
Anffany,
Kieran,
Nafiz



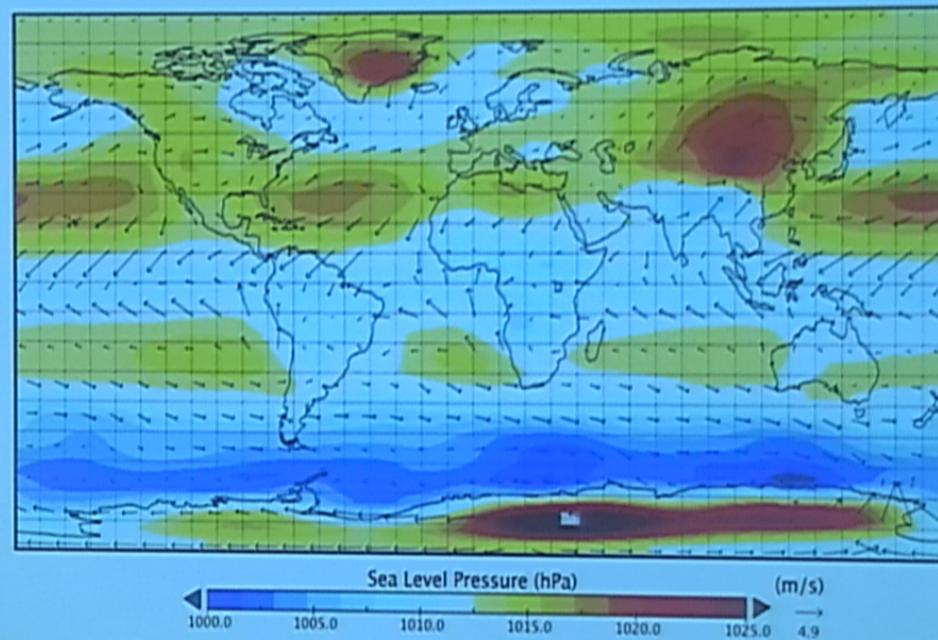
The Motion of Wind on the Earth's Surface

By
Anffany,
Kieran,
Nafiz

Temperature variation on the surface of the Earth



Pressure variation on the surface of the earth



The governing dynamics of atmospheric air flow

1. Equation of continuity

Equation of continuity

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho v) = 0$$

Here,

ρ = Air density

v = Velocity of air

Equation of continuity

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho v) = 0$$

Here,

ρ = Air density

v = Velocity of air

Thermodynamic equation

$$c_v \frac{DT}{Dt} = -\nabla \cdot v - \nabla \cdot J$$

Here,

$$\frac{D}{Dt} = \frac{\partial}{\partial t} + v \cdot \nabla = \text{Material derivative}$$

c_v = Specific heat of air

J = Heat flux

T = Temperature

Momentum equation

$$\text{The Navier-Stokes equation: } \rho \frac{D\mathbf{v}}{Dt} = -\nabla p + \mathbf{f}$$

Where,

ρ = Pressure

\mathbf{f} = All other forces

$$\text{Force, } \mathbf{f} = \rho g - 2\Omega \times \mathbf{v} + \mathbf{D}$$

Gravitational force

Coriolis force

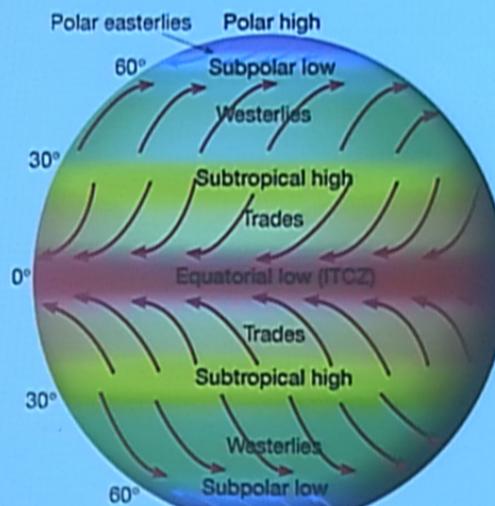
Frictional force

Where,

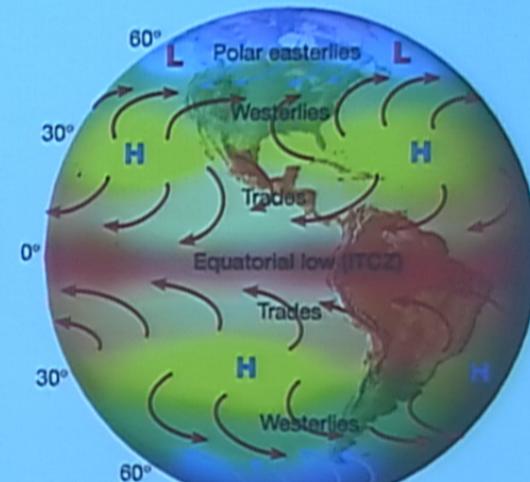
g = Gravitational acceleration

Ω = Angular velocity of earth

Resultant wind flow



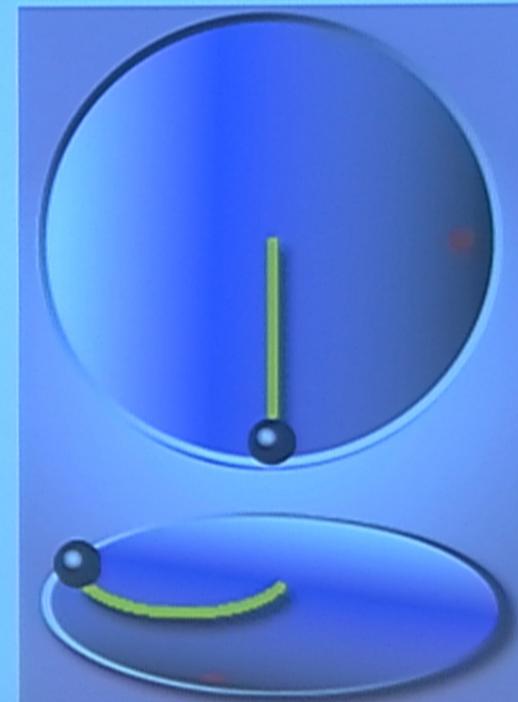
(a)



(b)

Coriolis Effect – where from?

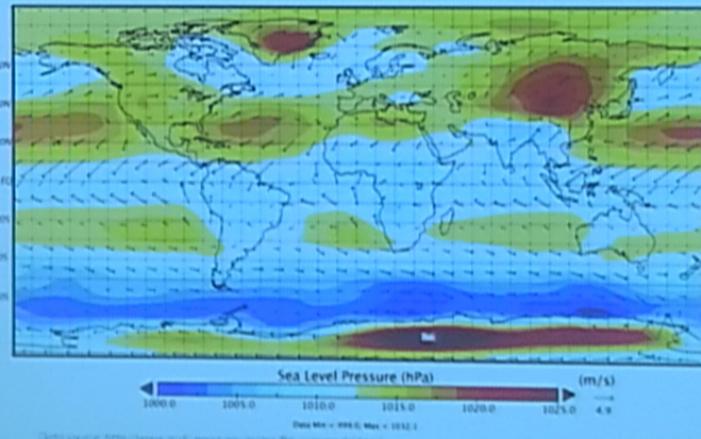
$$\mathbf{F}_C = -2m\Omega \times \mathbf{v}$$



Coriolis Effect – on Earth frame

Clockwise winds in Northern Hemisphere
Counterclockwise winds in Southern Hemisphere

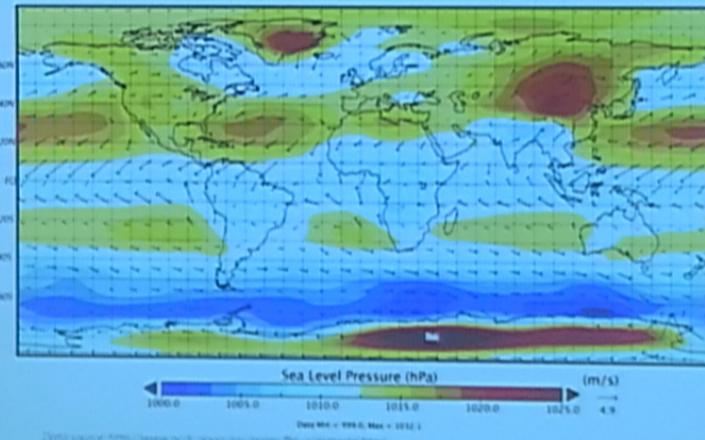
Mean Annual Atmospheric Pressure at Sea Level and Surface Winds
Model CCM3 PMIP Pre-Industrial 10-yr Simulation with Computed SSTs from ccm3 R15E12 model



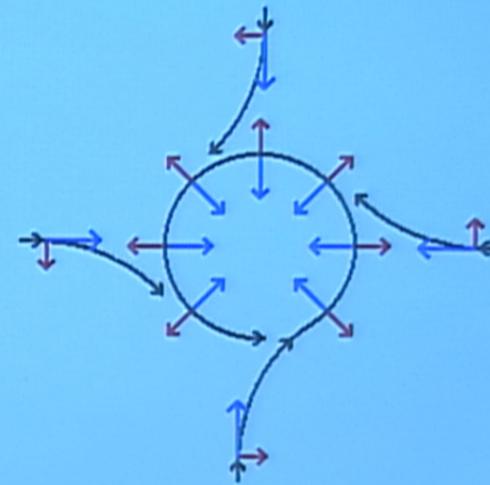
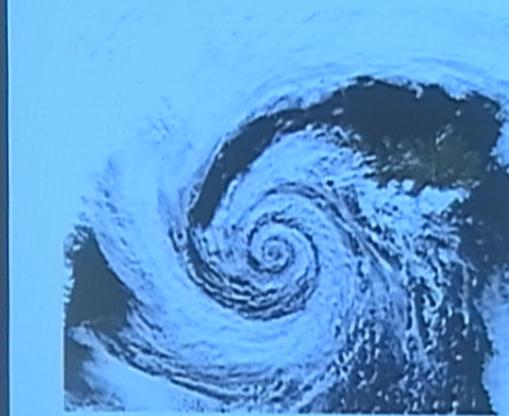
Coriolis Effect – on Earth frame

Clockwise winds in Northern Hemisphere
Counterclockwise winds in Southern Hemisphere

Mean Annual Atmospheric Pressure at Sea Level and Surface Winds
Model CCM1 PMIP Pre-Industrial 10-yr Simulation with Computed SSTs from ccm1 R15E12 model

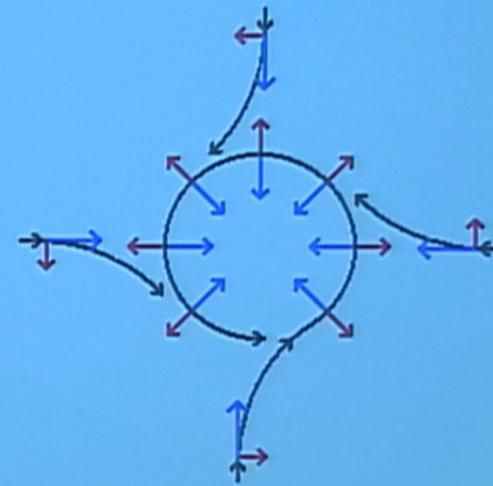


Coriolis Effect – cyclone



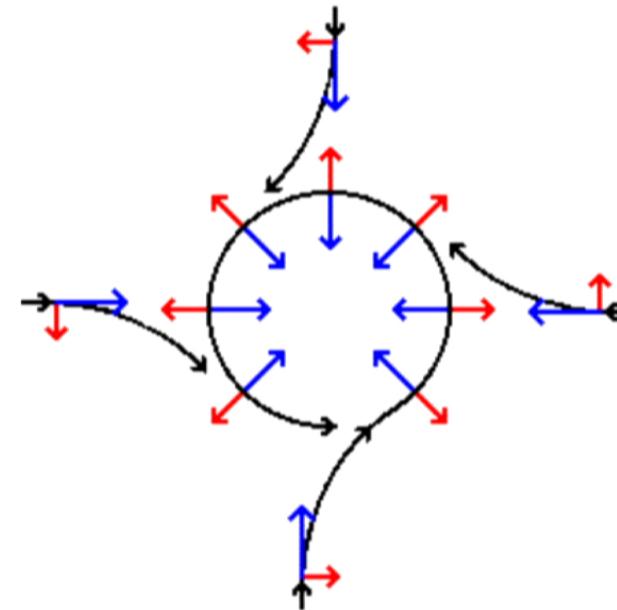
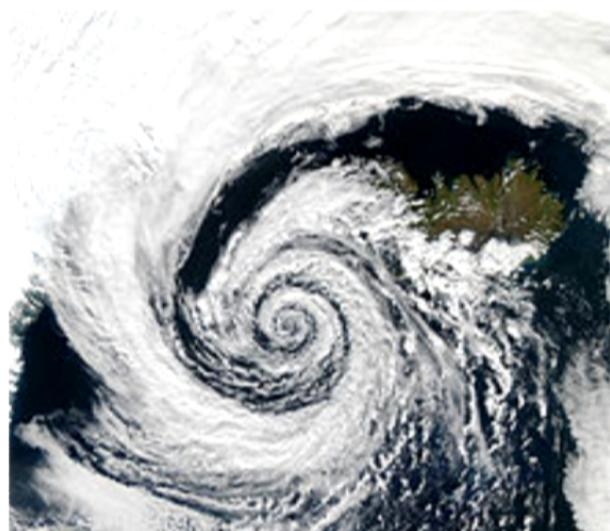
Blue: Pressure-gradient force
Red: Coriolis force

Coriolis Effect – cyclone



Blue: Pressure-gradient force
Red: Coriolis force

Coriolis Effect – cyclone



Blue: Pressure-gradient force
Red: Coriolis force

Mathematical argument

$$\frac{DU}{Dt} = -2\Omega \times U - \frac{1}{\rho} \nabla P + g + F$$

↑
Coriolis

Mathematical argument

$$\frac{D\mathbf{U}}{Dt} = -2\Omega \times \mathbf{U} - \frac{1}{\rho} \nabla P + \mathbf{g} + \mathbf{F}$$

↑
Coriolis ↑
 Gravity

↑
Friction

$$\mathbf{U} = \begin{pmatrix} u \\ v \\ 0 \end{pmatrix} \quad \Omega = \omega \begin{pmatrix} \cos \phi \sin \theta \\ \cos \phi \cos \theta \\ \sin \phi \end{pmatrix}$$

Mathematical argument

$$\frac{DU}{Dt} = -2\Omega \times U - \frac{1}{\rho} \nabla P + g + F$$

↑
Coriolis ↑
 Gravity ↑
 Friction

$$U = \begin{pmatrix} u \\ v \\ 0 \end{pmatrix} \quad \Omega = \omega \begin{pmatrix} \cos \phi \sin \theta \\ \cos \phi \cos \theta \\ \sin \phi \end{pmatrix}$$