

Title: Fuzzballs to Firewalls: A Post-Firewall Review of the Fuzzball Proposal: Lecture 1

Date: May 30, 2013 11:00 AM

URL: <http://pirsa.org/13050087>

Abstract: The fuzzball proposal makes a conjecture about the nature of black hole microstates. Now, more than a decade old and including several different philosophies and perspectives, it is especially relevant after the recent firewall argument and ensuing debate. Over three lectures, I plan to start with a very general discussion of the general ideas and motivations, then review the theoretical evidence from string theory, and finally close by discussing open questions, including the fate of a freely falling observer as he/she passes through the black hole horizon.

References

Mathur hep-th/0502050

" " /0510180

Bena¹, Warner /0701216

Skenderis³, Taylor 0804.0552

Balasubramanian et al. 0811.0263

www.physics.ohio-state.edu/~mathur/

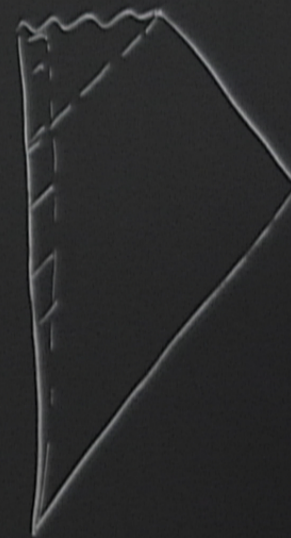
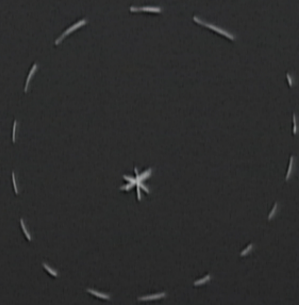
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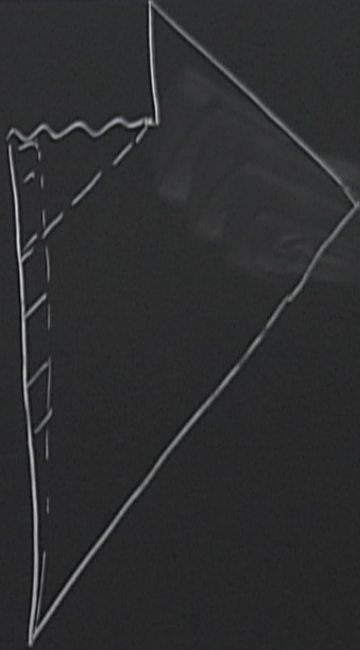
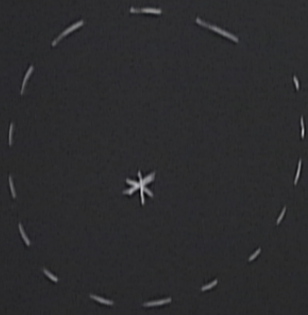
- I. Introduction, Definition, and Abstract Motivations
- II. Fuzzballs in String Theory
- III. Open Questions and Problems

Schwarzschild (S+1)

$$r = 2GM$$

$$\sqrt{(R_{\text{Schw}})^2} = \sqrt{48} \frac{GM}{c^3}$$

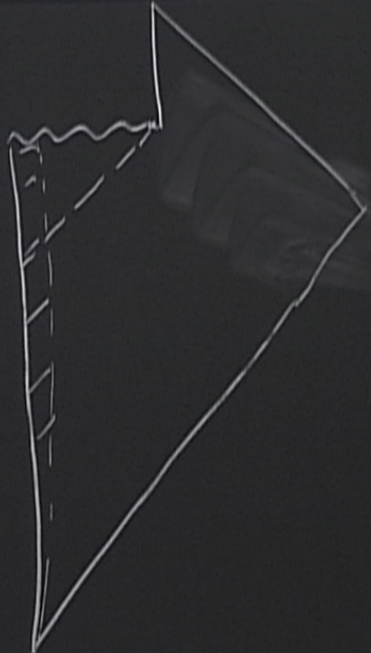




$$S = \frac{A}{4G}$$

$$T = \frac{1}{8\pi M}$$

$$l_{pl} = \sqrt{\frac{G\hbar}{c^3}}$$



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expect (curvature) $\sim \frac{1}{l_{pl}^2}$



$$S = \frac{A}{4G} \quad T = \frac{1}{8\pi M}$$

$$l_{pl} = \sqrt{\frac{G\hbar}{c^3}}$$

expect (curvature) $\sim \frac{1}{l_{pl}^2}$ $r \sim M^2 \ll r_{horizon}$

Information Paradox



Information Paradox

initial matter $|\psi_m\rangle$

final state $P_{\text{rad}} \approx P_{\text{term}}$

Entropy Puzzle

Information Paradox

initial matter $|4_m\rangle$

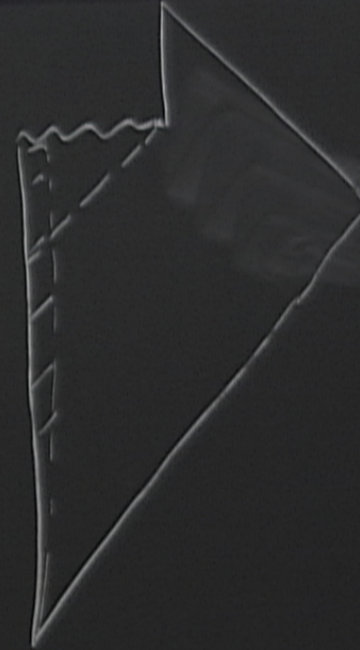
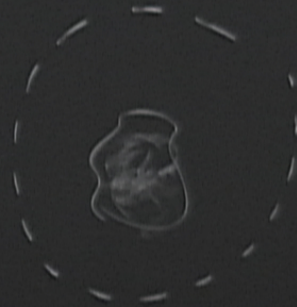
final state $P_{\text{rad}} \approx P_{\text{term}}$

Entropy Puzzle

Schwarzschild (3+1)

$$r = 2GM$$

$$\sqrt{(R_{\text{Schw}})^2} = \sqrt{48} \frac{GM}{c^3}$$



$$S = \frac{A}{4G}$$

Information Paradox

initial matter $|\psi_m\rangle$

final state $P_{\text{rad}} \approx P_{\text{term}}$

Entropy Puzzle

Where are the microstates?

Infall

The Fuzzball Proposal

1) the BH has $e^{S_{\text{BH}}}$ microstates

2) microstates have following properties:

(i) Smooth & horizon-free

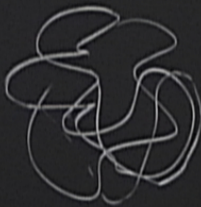
The Fuzzball Proposal

1) the BH has $e^{S_{BH}}$ microstates

2) microstates have following properties:

(i) Smooth & horizon-free

(ii) nontrivial structure up to the (would-be) horizon



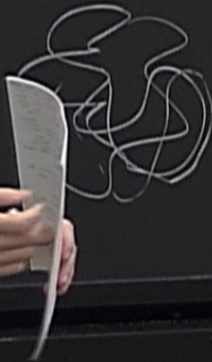
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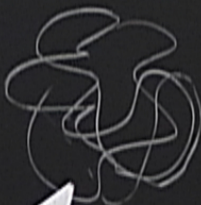
The Fuzzball Proposal

1) the BH has $e^{S_{BH}}$ microstates

2) microstates have following properties:

~~(i) smooth & horizon-free~~

(ii) nontrivial structure up to the (would-be) horizon



$$l_{\text{eff}} \sim \left(\frac{M}{M_{\text{pl}} \uparrow} \right)^d l_{\text{pl}} \quad \left\{ \begin{array}{l} \# \text{ of particles} \end{array} \right.$$

$$N^d \lambda_T$$

$$\text{unnel} \sim e^{-S_{\text{BH}}}$$

$$\text{states}) \sim e^{S_{\text{BH}}}$$

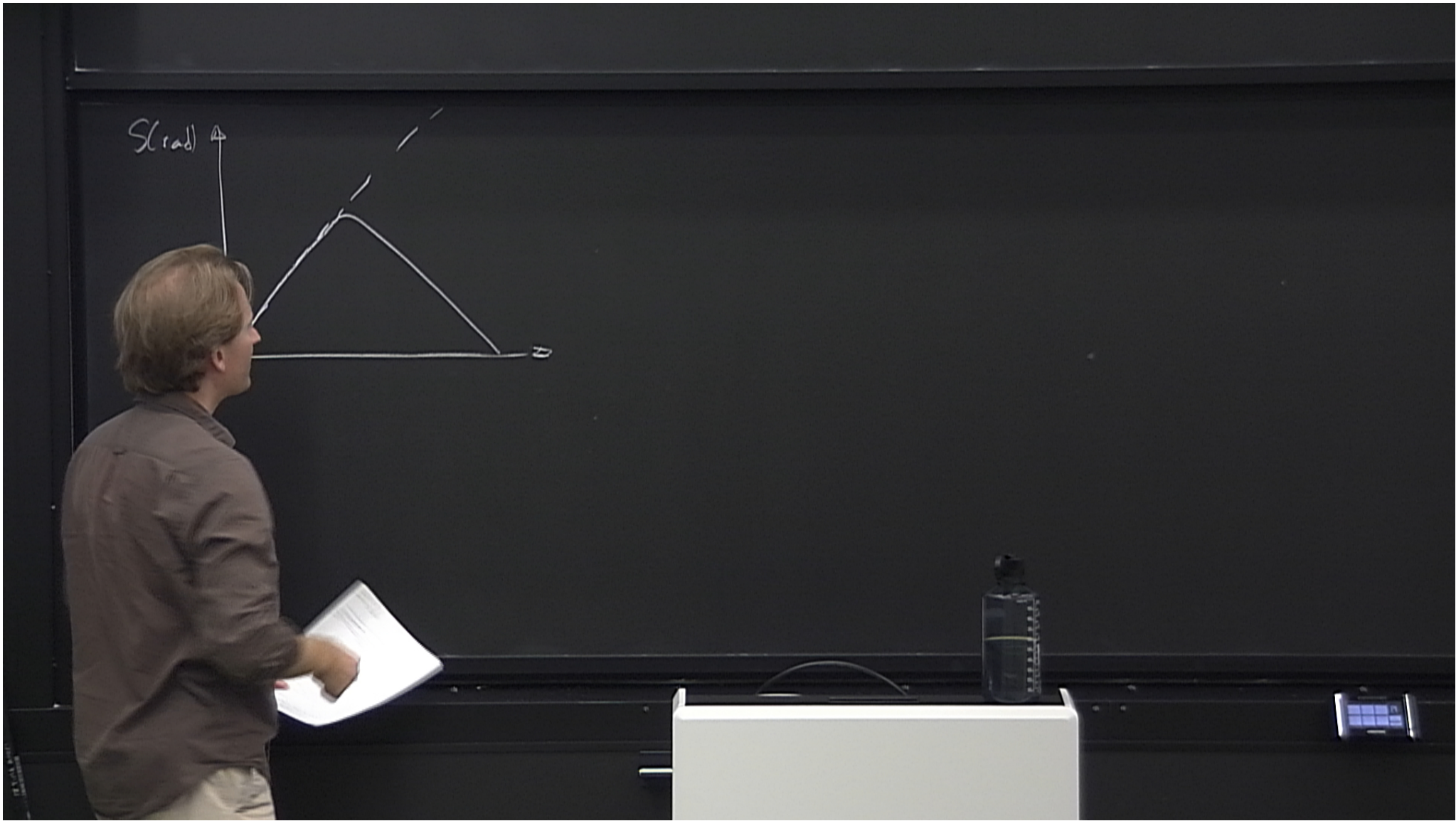
What keeps microstates from collapsing?

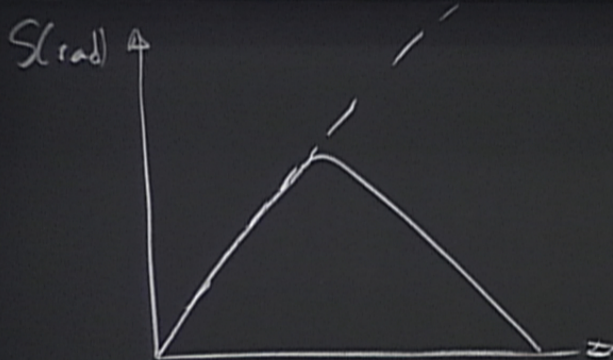
Physical mechanism: "fractionation"

F1 string
 n_w winding
 n_p momentum

$$E_{\text{graviton}} \sim \frac{2}{R}$$
$$\text{multisoid F1} \sim \frac{2}{n_w R}$$

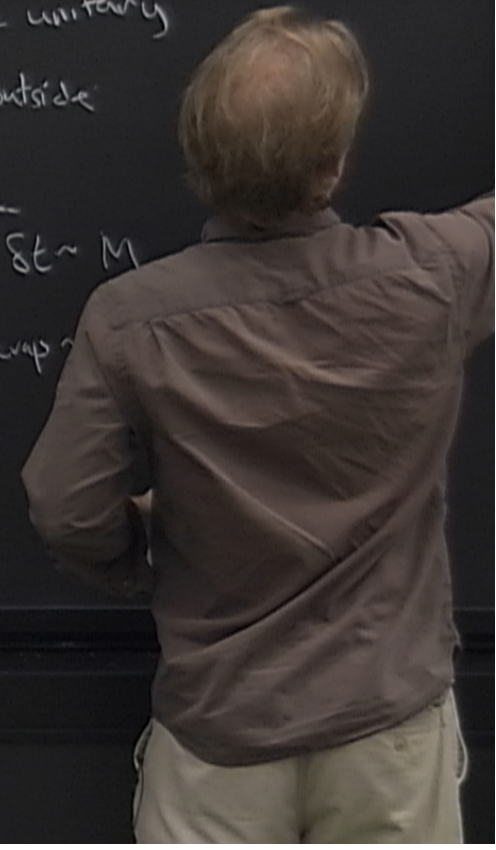
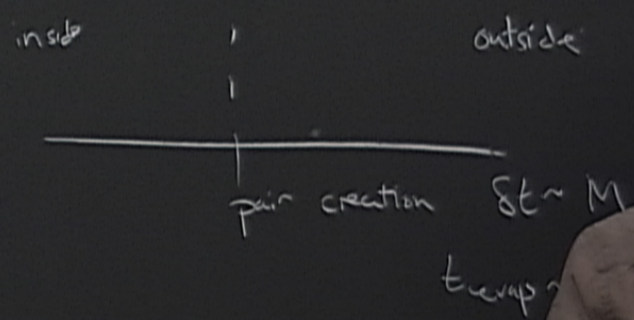
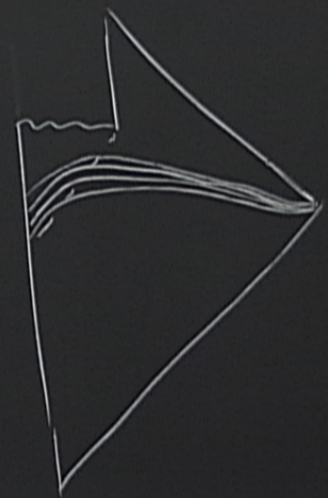
"fractional brane" $T_{\text{eff}} \sim \frac{T_1}{n_w}$





Claim: small corrections to Hawking evap. process
 don't accumulate to restore unitarity

$10^7 \sim 10^6$

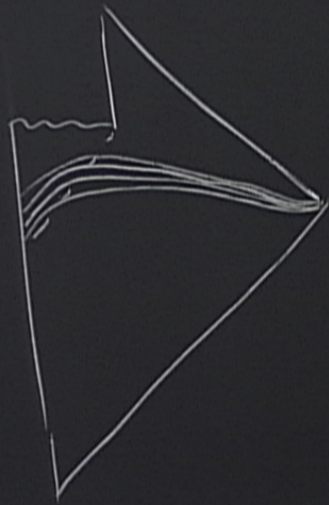


Claim: small corrections to Hawking evap. process
 don't accumulate to restore unitarity

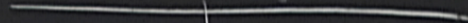
$|0\rangle \sim 10^6$ particles

$|1\rangle \sim 1$ particle

$$\mathcal{H}_{\text{tot}} = \hat{\mathcal{H}}_{\text{int}} \otimes \mathcal{H}_{\text{out}}$$



inside | outside



pair creation $\delta t \sim M$

$$t_{\text{evap}} \sim M^3 \sim S_{\text{BH}} \delta t$$



regions to Hawking evap. process

accumulate to restore unitarity

inside

outside

pair creation $\delta t \sim M$

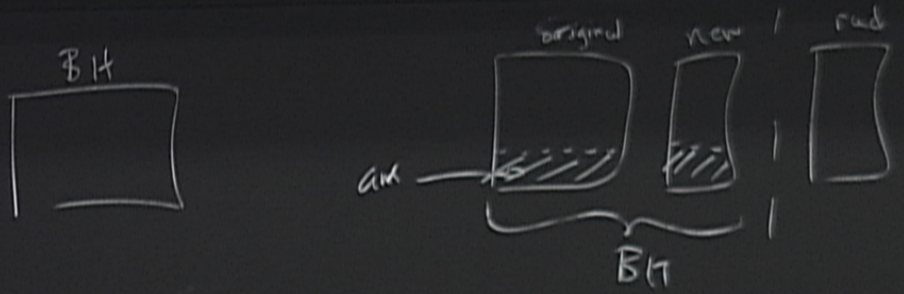
$$t_{\text{evap}} \sim M^3 \sim S_{\text{BH}} \delta t$$

$|0\rangle \sim$ no particle

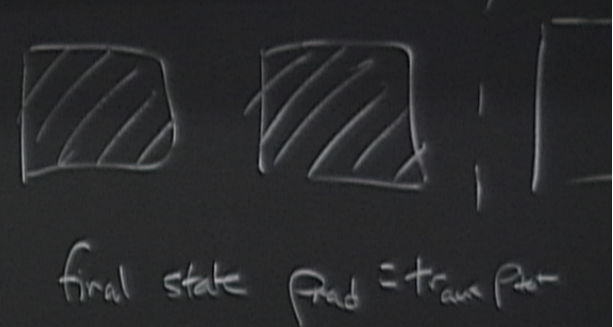
$|1\rangle \sim$ particle

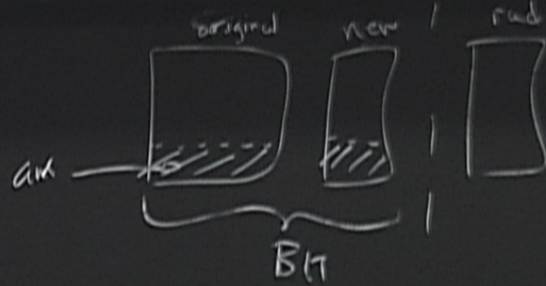
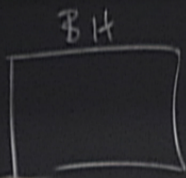
$$\mathcal{H}_{\text{tot}} = \hat{\mathcal{H}}_{\text{int}} \otimes \mathcal{H}_{\text{out}}$$

Hawking pair $|\psi\rangle = \frac{1}{\sqrt{2}} (|00\rangle + |11\rangle)$



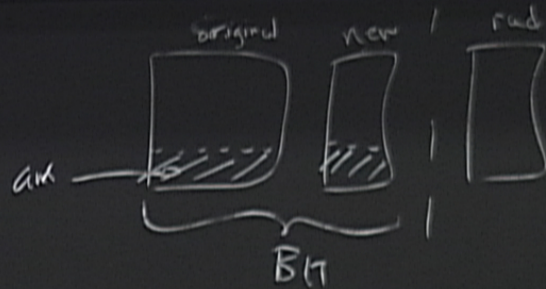
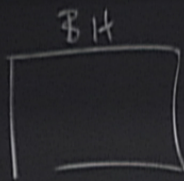
$$\rho_{\text{physical}} = \text{tr}_{\text{rad}} \rho_{\text{tot}}$$





$$P_{\text{physical}} = \tau_{\text{aux}} P_{\text{tot}}$$

final state $P_{\text{rad}} = \tau_{\text{aux}} P_{\text{tot}}$

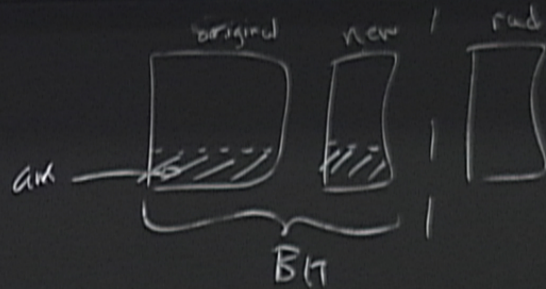
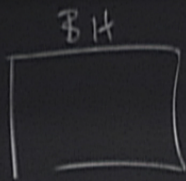


final state $P_{rad} = P_{air} P_{B14}$

$$P_{physical} = P_{air} P_{tot}$$

$$|\psi_i\rangle \xrightarrow{\tilde{L}_i} \tilde{L}_i |\psi_i\rangle \xrightarrow{\hat{U}_i \otimes U_i} (\tilde{L}_i |\psi_i\rangle) = |\psi_{fin}\rangle$$

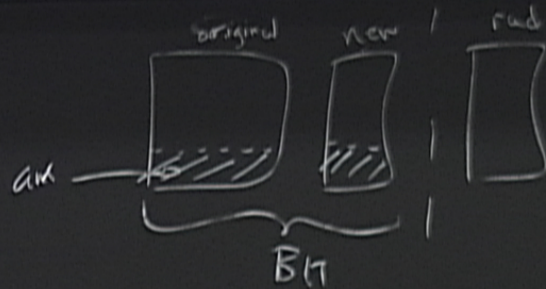
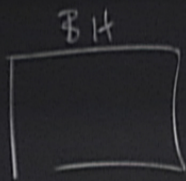
$$\tilde{L}_i \tilde{L}_i = \hat{I}$$



$$P_{\text{physical}} = P_{\text{trans}} P_{\text{tot}}$$

$$|\psi_i\rangle \xrightarrow{\tilde{L}_i} \tilde{L}_i |\psi_i\rangle \xrightarrow{\hat{U}_i \otimes U_i} (\tilde{L}_i |\psi_i\rangle) = |\psi_{\text{fin}}\rangle$$

$$\tilde{L}_i^\dagger \tilde{L}_i = \hat{I}$$

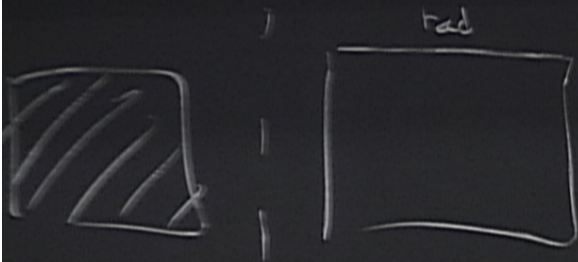


final state $P_{rad} = P_{air} P_{tot}$

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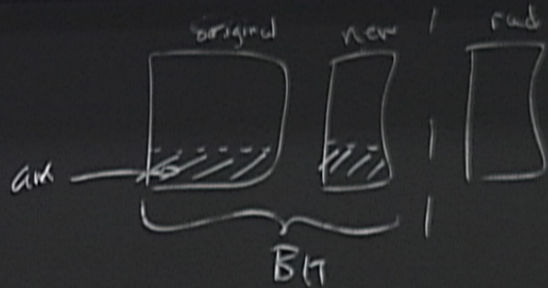
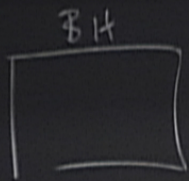
$$P_{\text{rad}} = \text{trace } P_{\text{tot}}$$

$$\Delta S_i = S_{i+1}(\text{rad}) - S_i(\text{rad})$$

$$S_i^{\text{Hawking}}(\text{rad}) = i \log 2$$

$$\| \tilde{I}_i - \tilde{I}_i^{\text{Hawking}} \| < \epsilon < 1$$

$$\Delta S_i \geq \log 2 - \epsilon$$



final state $P_{rad} = \text{trace } P_{tot}$

$$P_{\text{physical}} = \text{trace } P_{\text{tot}}$$

$$|\psi_i\rangle \xrightarrow{\tilde{L}_i} \tilde{L}_i |\psi_i\rangle \xrightarrow{\hat{U}_i \otimes U_i} (\tilde{L}_i |\psi_i\rangle) = |\psi_{fin}\rangle$$

$$\tilde{L}_i + \tilde{L}_i^\dagger = \hat{I} \quad \tilde{L}_i = |e_1\rangle\langle f_1| + |e_2\rangle\langle f_2| + \dots + |e_n\rangle\langle f_n|$$