

Title: 12/13 PSI - Explorations in Particle Theory Lecture 13

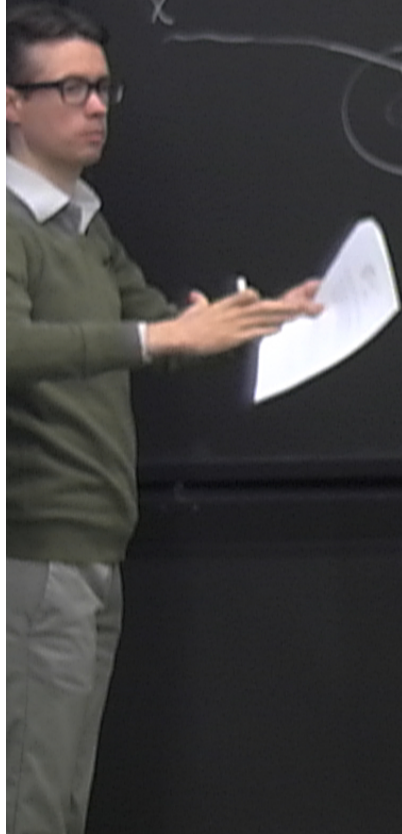
Date: Apr 04, 2013 10:15 AM

URL: <http://pirsa.org/13040041>

Abstract:

DM in Stars

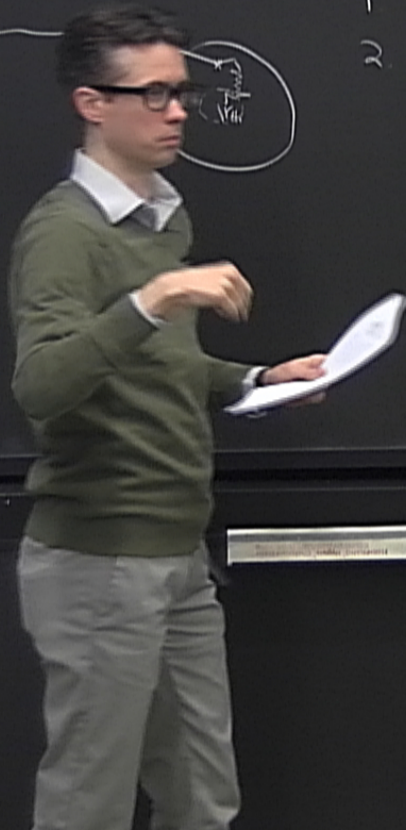
x



DM in Stars

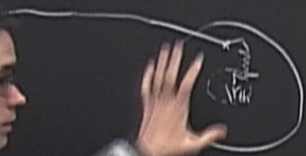
χ

1. scatters to $N < N_{\text{esc}}(R)$
2. more scattering thermalizes χ



DM in Stars

χ



- 1 scatters to $N < N_{\text{esc}}(r)$
- 2 more scattering thermalizes χ
- 3 χ collects within a "thermalsphere"

$$T_c \sim \frac{GM(r)m_\chi}{r}$$

$$r_{\text{th}} \sim \left(\frac{T_c M(r)}{m_\chi \rho_c} \right)^{1/2}$$

DM in Stars

χ

- 1 scatters to $\sigma < \sigma_{\text{esc}}(r)$
- 2 more scattering thermalizes χ
- 3 χ collects within a "thermalsphere"

$$T_c \sim \frac{GM(r)m_\chi}{r}$$

$$r_{\text{th}} \sim \left(\frac{T_c M(r)}{m_\chi \rho_c} \right)^{1/2}$$

DM in Stars

χ



- 1 scatters to $\mathcal{N} < \mathcal{N}_{\text{th}}(r)$
- 2 more scattering thermalizes χ
- 3 χ collects within a "thermalsphere"

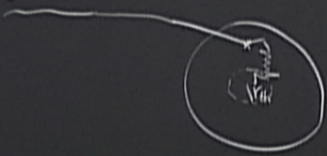
$$T_c \sim \frac{GM(r)m_\nu}{r}$$

$$r_{\text{th}} \sim \left(\frac{T_c M(r)}{m_\nu \rho_c} \right)^{1/2}$$



DM in Stars

χ



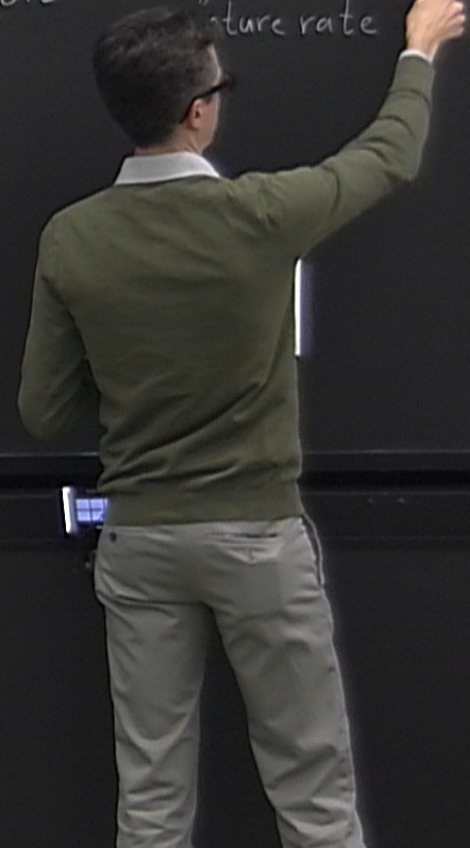
1. scatters to $v < v_{esc}(r)$
2. more scattering thermalizes χ
3. χ collects within a "thermalsphere"
4. χ annihilates in the star.

$$T_c \sim \frac{GM(r)m_\chi}{r}$$

$$r_{th} \sim \left(\frac{T_c M_{\star}}{m_\chi \rho_c} \right)^{1/2}$$

$$\frac{dN}{dt} = C - AN^2$$

"capture rate"



DM in Stars

χ



- 1 scatters to $v < v_{esc}(r)$
- 2 more scattering thermalizes
- 3 χ collects within a "thermalization radius"
- 4 χ annihilates in the star

$$T_c \sim \frac{GM(r)m_\chi}{r}$$

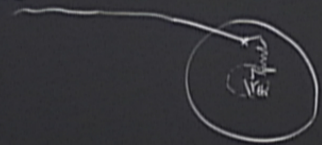
$$r_{th} \sim \left(\frac{T_c M_{\star}}{m_\chi \rho_c} \right)^{1/2}$$

$$\frac{dN}{dt} = C - AN^2$$

capture rate annihilation

DM in Stars

χ



- 1 scatters to $N < N_{\text{esc}}(r)$
- 2 more scattering thermalizes χ
- 3 χ collects within a "thermal sphere"
- 4 χ annihilates in the star.

$$T_c \sim \frac{GM_\star m_\chi}{r}$$

$$r_{\text{th}} \sim \left(\frac{T_c M_\star}{m_\chi \rho_c} \right)^{1/2}$$

$$\frac{dN}{dt} = C - AN^2$$

capture rate annihilation

$$C = \underbrace{\frac{\rho_\chi}{m_\chi}}_{\text{flux}} \cdot \underbrace{\bar{v}}_{\text{kinematic}} \left(\frac{3N_{\text{esc}}}{2N} \right) \sigma_{\text{eff}}$$

$$\sigma_{\text{eff}} = \min \left\{ \sum_i \frac{M_i}{m_i} \right\}$$

DM in Stars

χ



- 1 scatters to $N < N_{\text{esc}}(r)$
- 2 more scattering thermalizes χ
- 3 χ collects within a "thermalsphere"
- 4 χ annihilates in the star.

$$T_c \sim \frac{GM_\star m_\chi}{r}$$

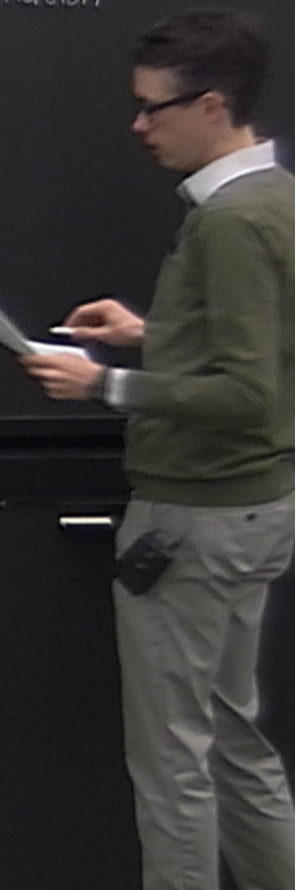
$$r_{\text{th}} \sim \left(\frac{T_c M_\star}{m_\chi \rho_c} \right)^{1/2}$$

$$\frac{dN}{dt} = C - AN^2$$

capture rate annihilation

$$C = \underbrace{\frac{\rho_\chi}{m_\chi}}_{\text{flux}} \cdot \underbrace{\bar{v}}_{\text{kinematic}} \left(\frac{3N_{\text{esc}}}{2N^2} \right) \sigma_{\text{eff}}$$

$$\sigma_{\text{eff}} = \text{min} \left\{ \sum_i \frac{M_h}{m_i} \frac{X_i}{A_i} \bar{\sigma}_{N_i} \right\}$$



$$\frac{dN}{dt} = C - AN^2$$

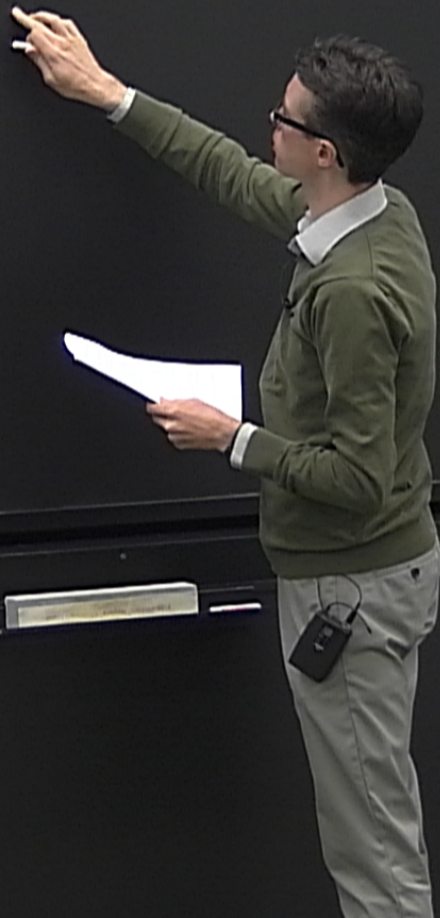
capture rate annihilation

$$C = \underbrace{\frac{\rho_x}{m_x}}_{\text{flux}} \cdot \underbrace{\bar{v}}_{\text{kinematic}} \left(\frac{3N_{esc}}{2N^2} \right) \sigma_{eff}$$

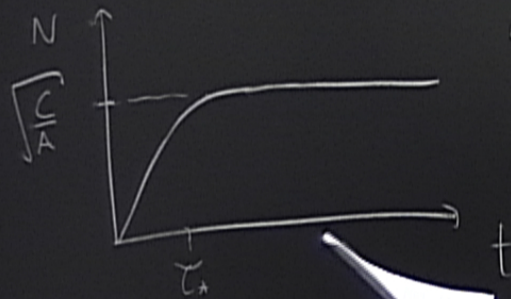
$$A = \langle \sigma N \rangle_{ann} / \left(\frac{4\pi}{3} r_{th}^3 \right)$$

$$\sigma_{eff} = \min \left\{ \sum_i \frac{M_i}{m_i} \frac{X_i}{A_i} \bar{\sigma}_{N_i}, \pi R_*^2 \right\}$$

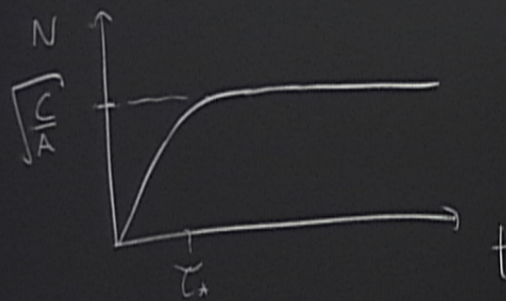
$$N(t) = \sqrt{\frac{C}{A}} \operatorname{TANH}(t/\tau_*)$$



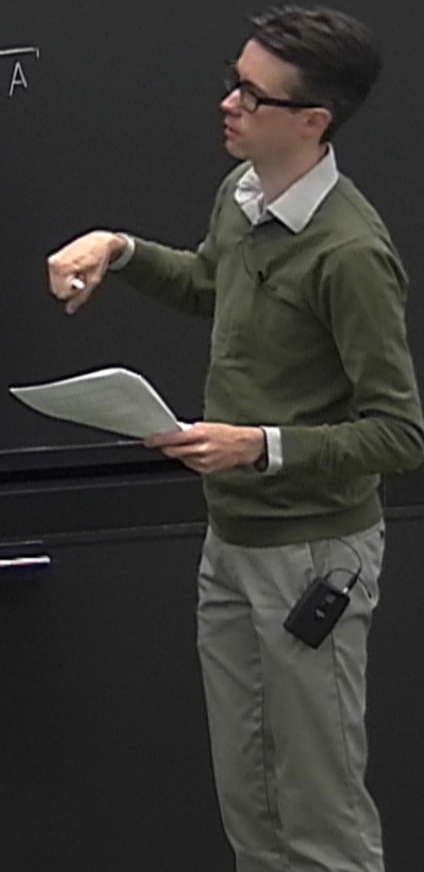
$$N(t) = \sqrt{\frac{C}{A}} \text{TANH}(t/\tau_*)$$



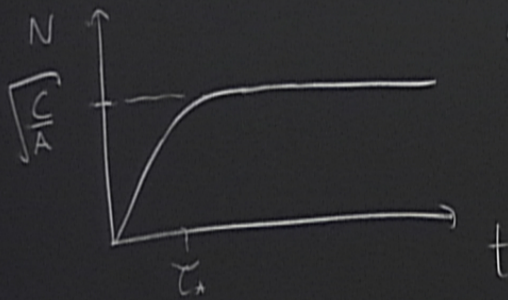
$$N(t) = \sqrt{\frac{C}{A}} \operatorname{TANH}(t/\tau_*)$$



$$\tau_* = 1/\sqrt{CA}$$



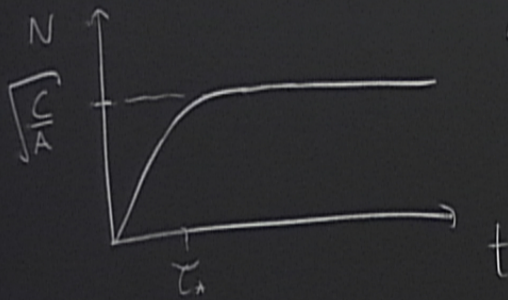
$$N(t) = \sqrt{\frac{C}{A}} \operatorname{TANH}(t/\tau_*)$$



$$\tau_* = 1/\sqrt{CA}$$

Heating Rate. $\frac{dq}{dt} = (m \times 2) AN^2$
 $\rightarrow (2m \times) \cdot C$

$$N(t) = \sqrt{\frac{C}{A}} \operatorname{TANH}(t/\tau_*)$$



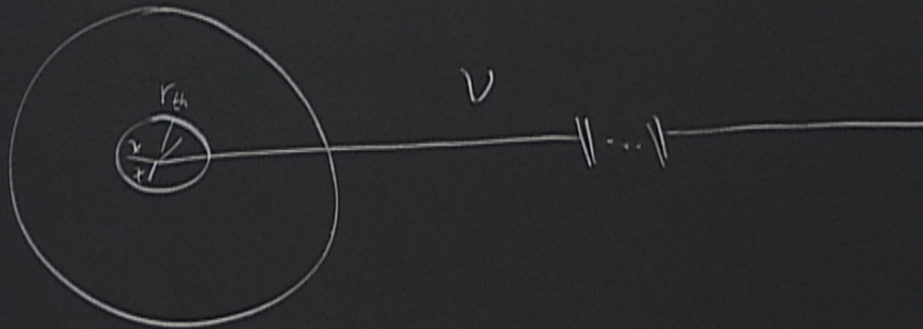
$$\tau_* = 1/\sqrt{CA}$$

Heating Rate $\frac{dq}{dt} = (m \times 2) AN^2$
 $\rightarrow (2mx) \cdot C$

Sun

$$t_{\odot} > \tau_{\odot}, \text{ if } \langle \sigma v \rangle_{\text{ann}} \gtrsim (3 \times 10^{-30} \text{ cm}^3/\text{s}) \cdot \left(\frac{\text{GeV}}{m_{\chi}} \right)^{1/2} \cdot \left(\frac{10^{-10} \text{ cm}^2}{\sigma_p} \right)$$

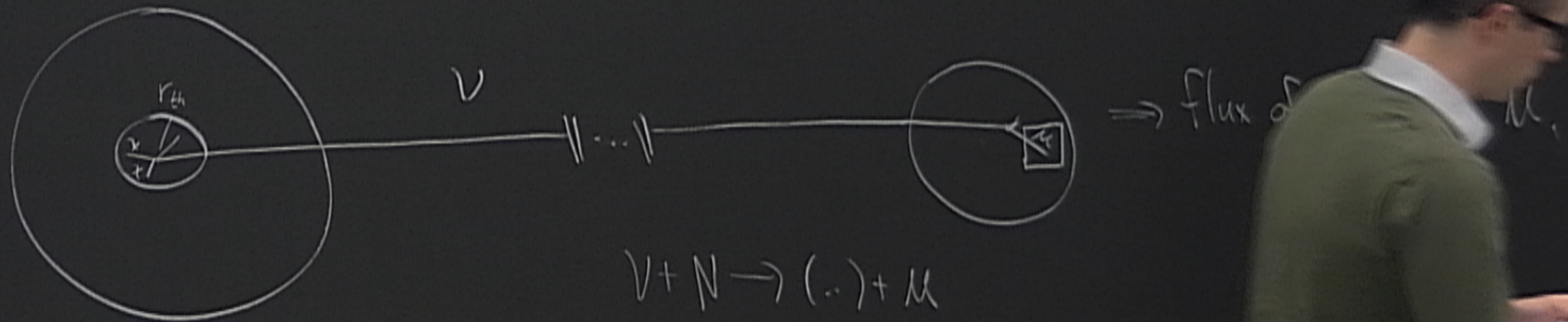
"age of Sun"



Sun

$$t_{\odot} > \tau_{\odot}, \text{ if } \langle \sigma v \rangle_{\text{ann}} \gtrsim (3 \times 10^{-30} \text{ cm}^3/\text{s}) \cdot \left(\frac{\text{GeV}}{m_{\chi}} \right)^{1/2} \cdot \left(\frac{10^{-10} \text{ cm}^2}{\sigma_p} \right)$$

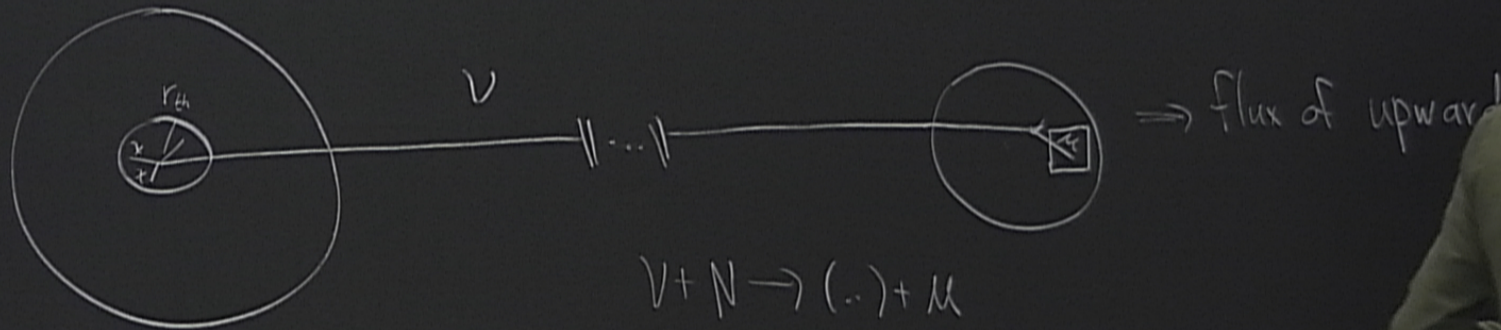
"age of Sun"



Sun

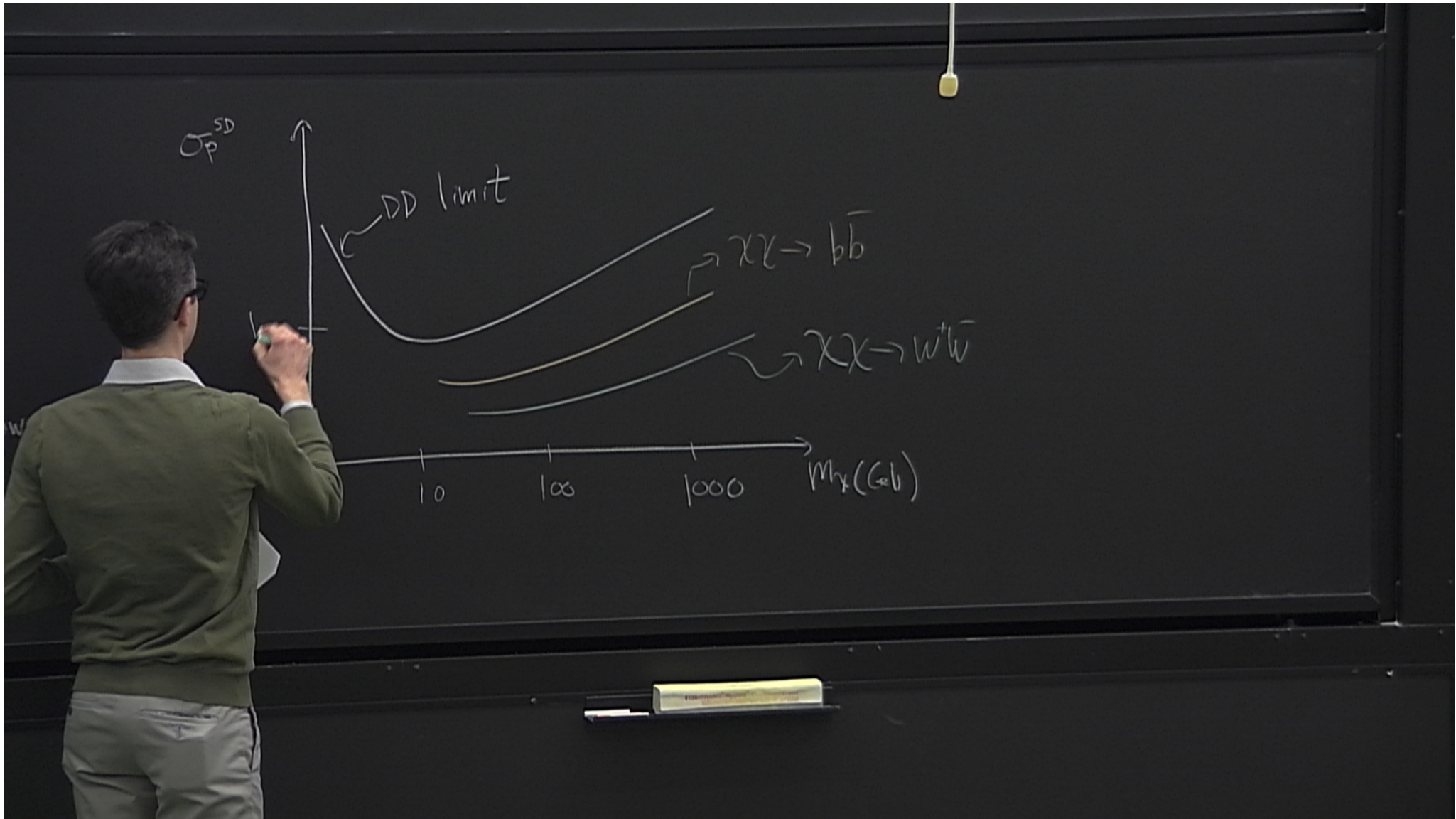
$$t_{\odot} > \tau_{\odot}, \text{ if } \langle \sigma N \rangle_{\text{ann}} \gtrsim (3 \times 10^{-30} \text{ cm}^3/\text{s}) \cdot \left(\frac{\text{GeV}}{m_{\chi}} \right)^{1/2} \cdot \left(\frac{10^{-10} \text{ cm}^2}{\sigma_p} \right)$$

"age of Sun"

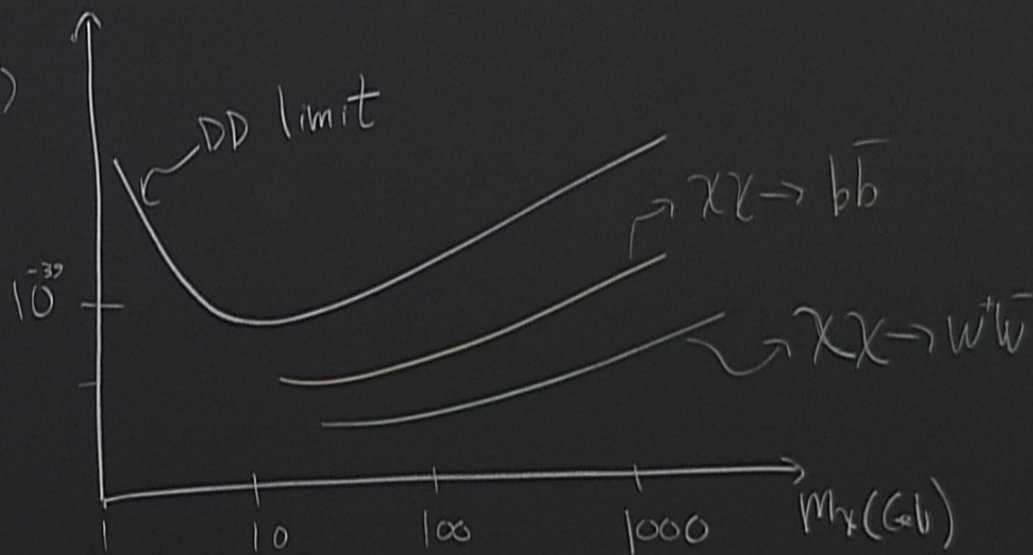


ward u .





σ_p^{SD}
(cm^2)

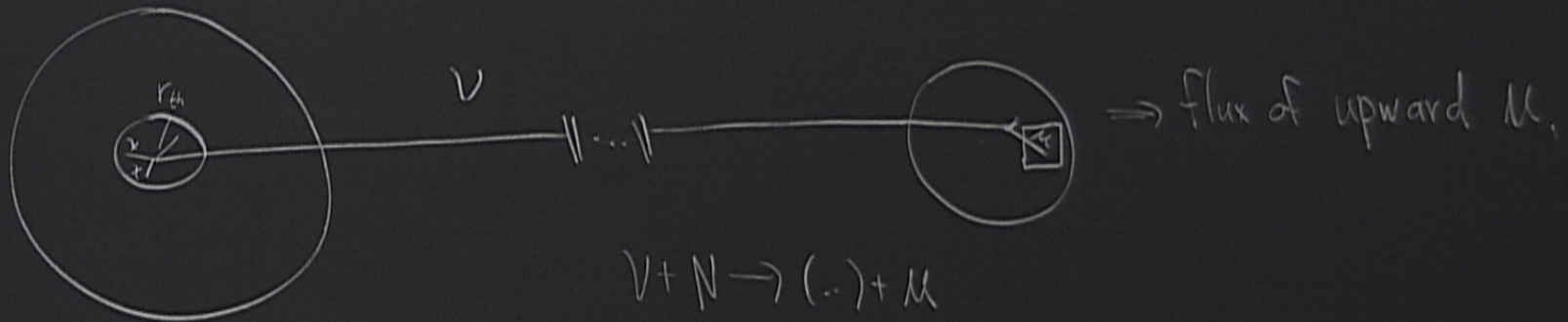


ward M_x

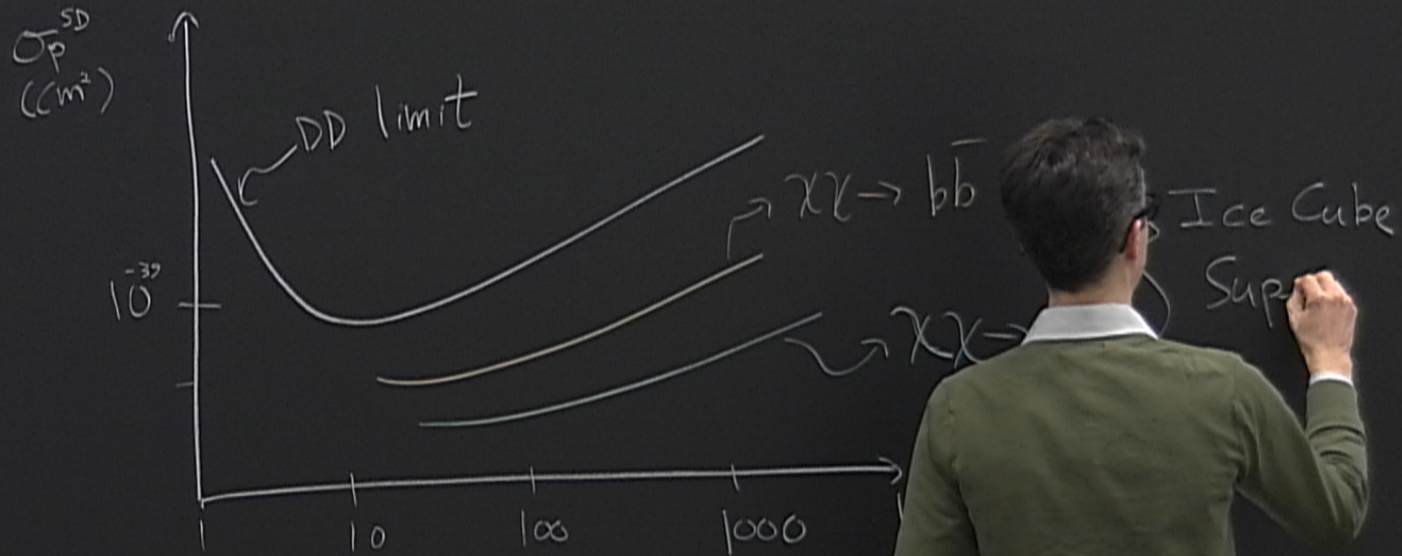
Sun

$$t_{\odot} > \tau_{\odot}, \text{ if } \langle \sigma v \rangle_{\text{ann}} \gtrsim (3 \times 10^{-30} \text{ cm}^3/\text{s}) \cdot \left(\frac{\text{GeV}}{m_{\nu}} \right)^{1/2} \cdot \left(\frac{10^{-10} \text{ cm}^2}{\sigma_p} \right)$$

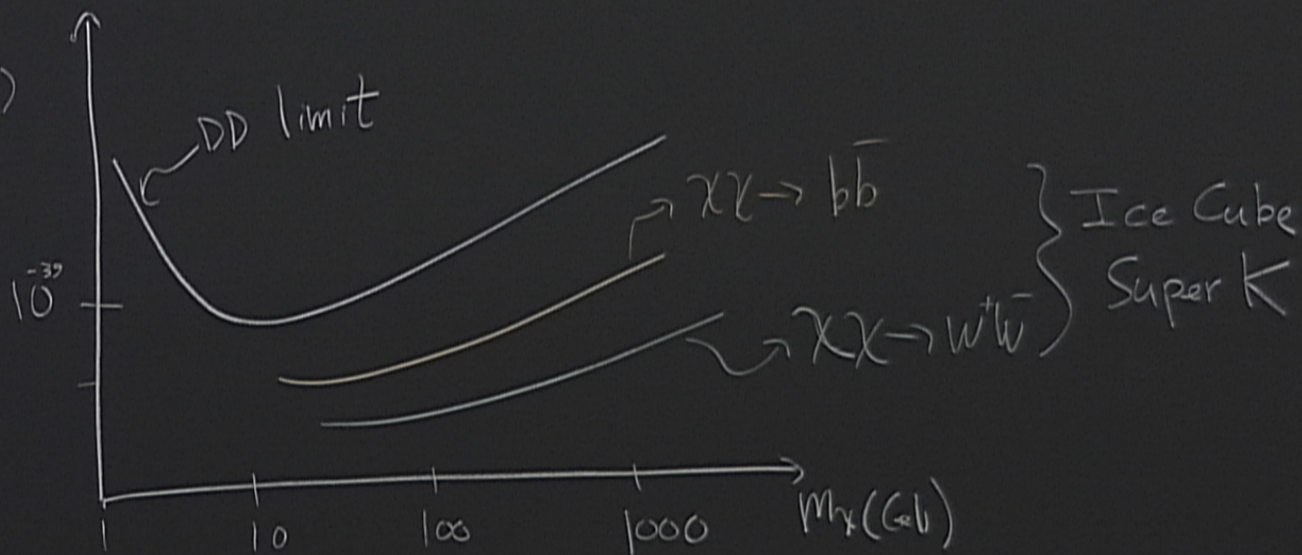
"age of Sun"



ward M.



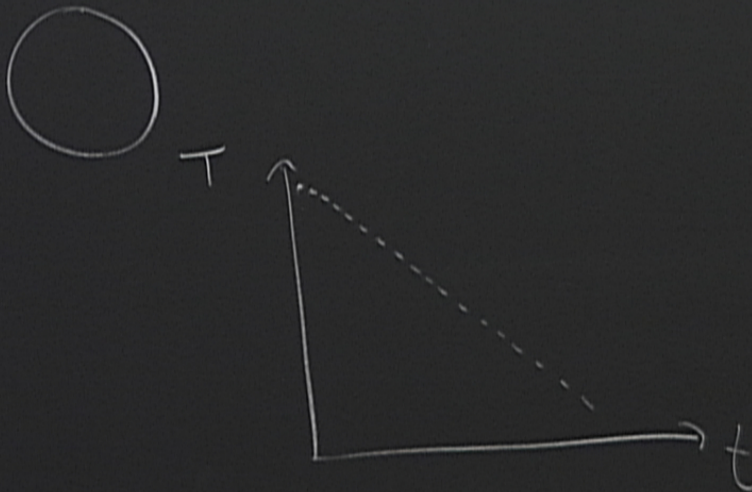
σ_p^{SD}
(cm^2)



ward M_x .

Neutron Star / White Dwarf

↳ supported by degeneracy pressure.



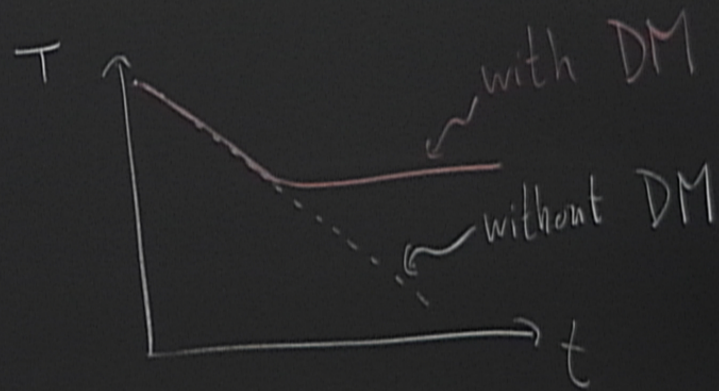
Neutron Star / White Dwarf

↳ supported by degeneracy pressure



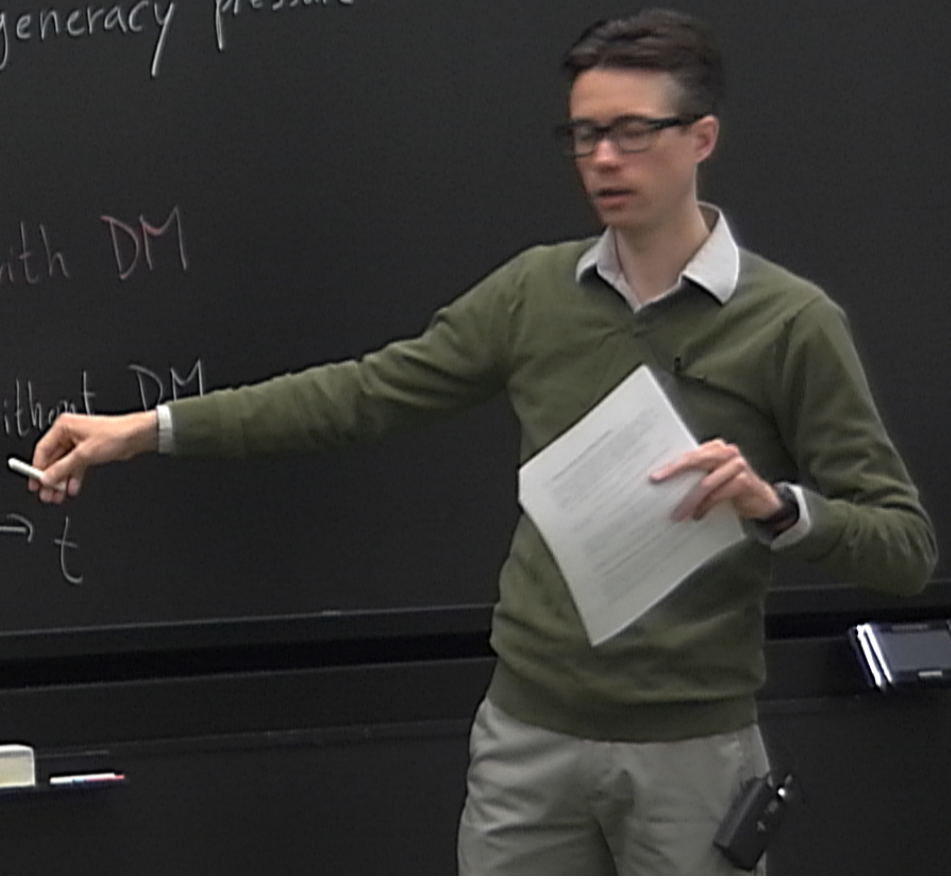
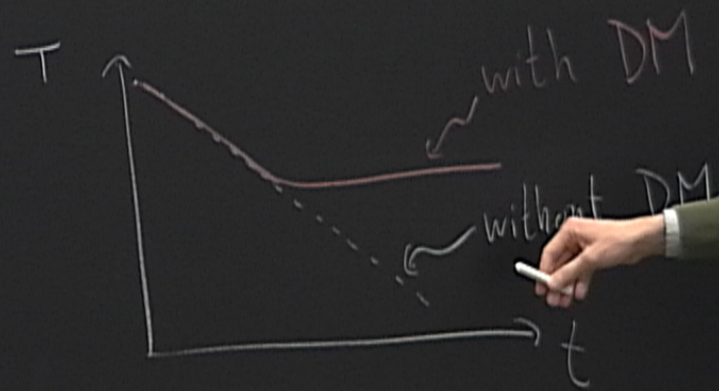
Neutron Star / White Dwarf

↳ supported by degeneracy pressure



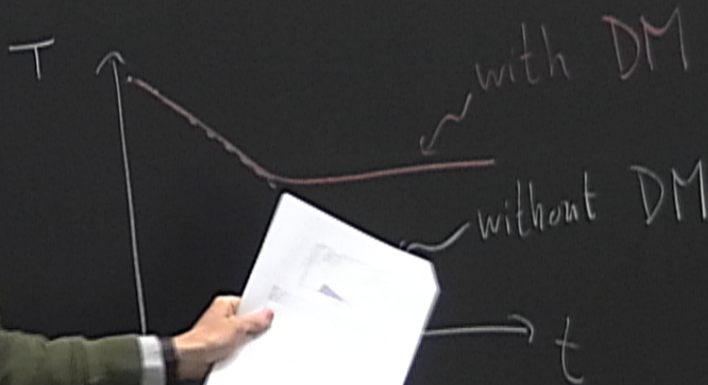
Neutron Star / White Dwarf

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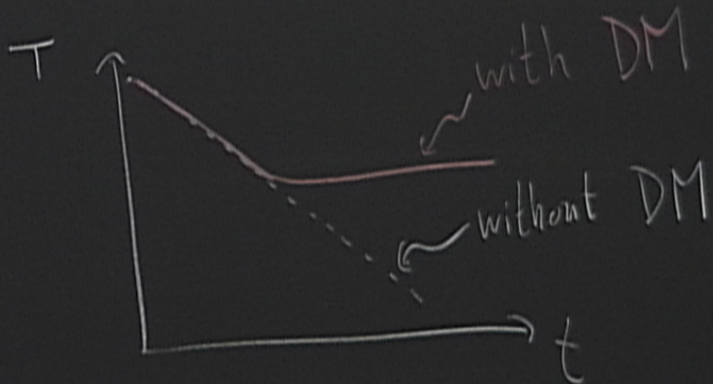
Neutron Star / White Dwarf

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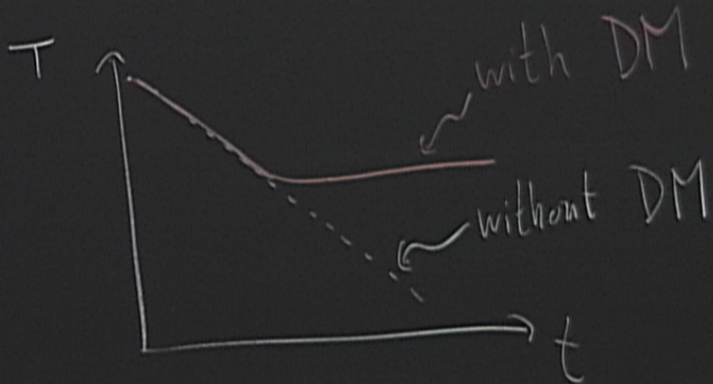
Neutron Star / White Dwarf

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Neutron Star / White Dwarf

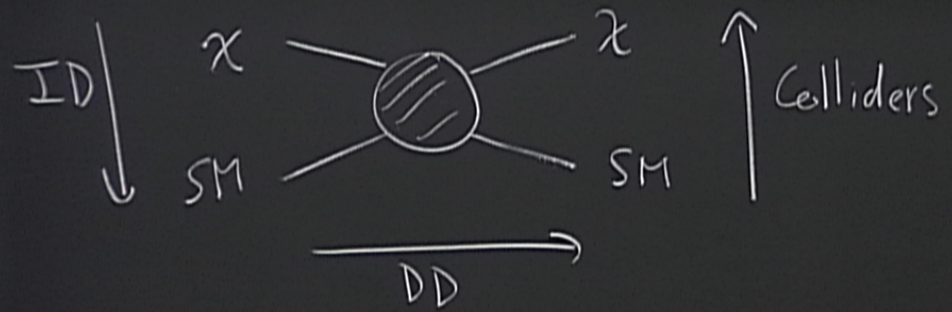
↳ supported by degeneracy pressure



$$v_{th} \sim \left(\frac{10^{-11} \text{ m}^2/\text{s}}{m_{\chi} v_{pc}} \right)$$

$\sigma_{eff} \sim \dots$

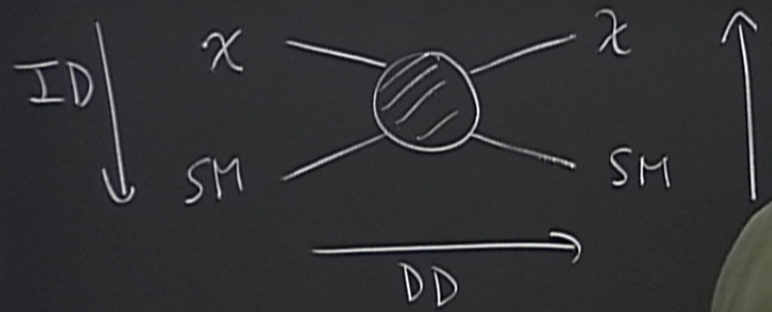
DM at Colliders



$$l_{th} \sim \left(\frac{10^{11} \text{M}}{m_{\chi} \rho_c} \right)$$

$$O_{eff} = \dots$$

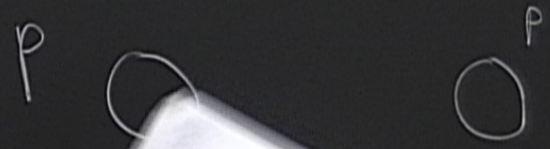
DM at Colliders



hadron = p, \bar{p}

LHC: $pp, \sqrt{s} = 7.8 \text{ TeV}$

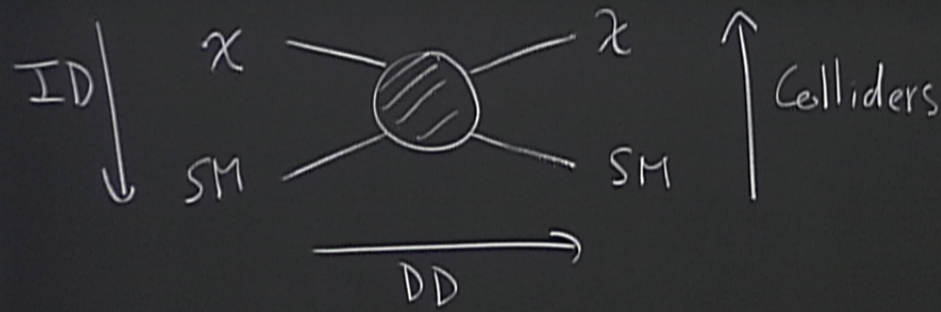
Tevatron: $p\bar{p}, \sqrt{s} = 1.96 \text{ TeV}$



$$v_{th} \sim \left(\frac{10^{11} \text{ m}}{m \times c} \right)$$

$\sigma_{eff} \sim \dots$

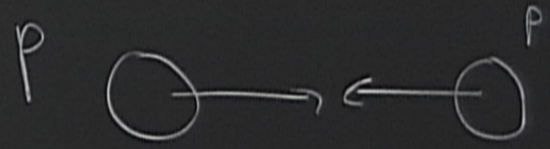
DM at Colliders



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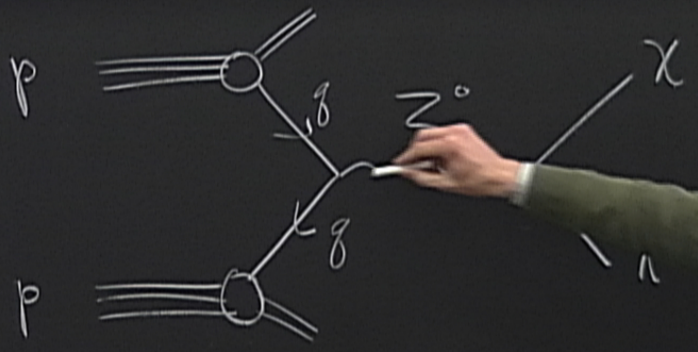
Tevatron: $p\bar{p}, \sqrt{s} = 1.96 \text{ TeV}$



$\text{eff} = \sum_i m_i A_i \langle \sigma v \rangle_i$

partons = q, \bar{q}, g

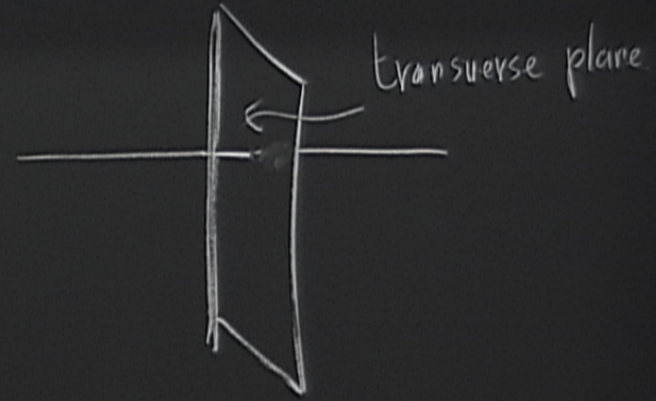
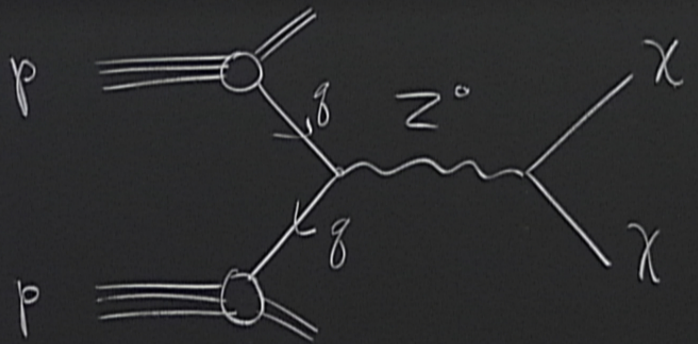
8 TeV
96 TeV



$\sigma_{\text{eff}} = \sum_i m_i A_i \sigma_{N_i} \dots$

partons = q, \bar{q}, g

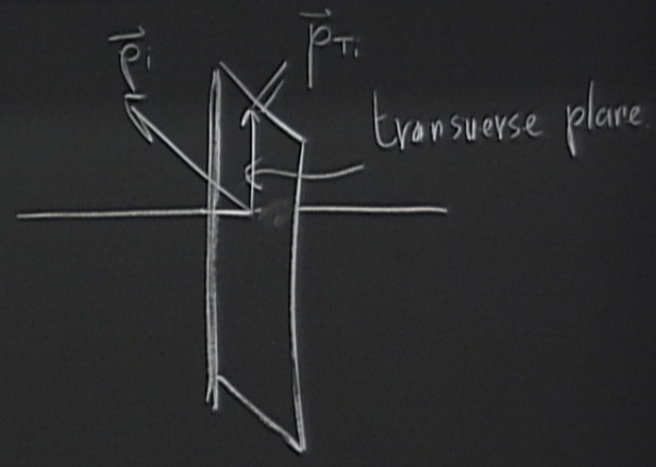
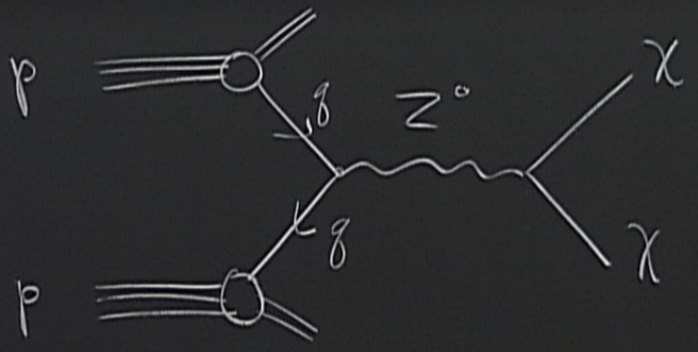
8 TeV
96 TeV



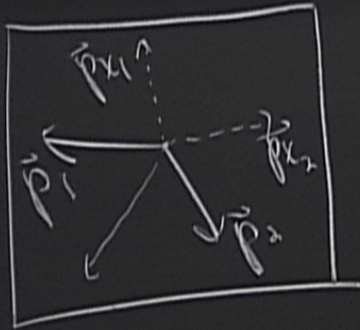
eff $\left(\sum_i m_i A_i \sigma_{N_i}, \dots \right)$

partons = q, \bar{q}, g

8 TeV
96 TeV



X carries some \vec{p}, E



$$\vec{p}_T = - \sum_{i \in \{1,2\}} \vec{p}_{T_i}$$

$$E_T = \|\vec{p}_T\|$$



SUSY DM

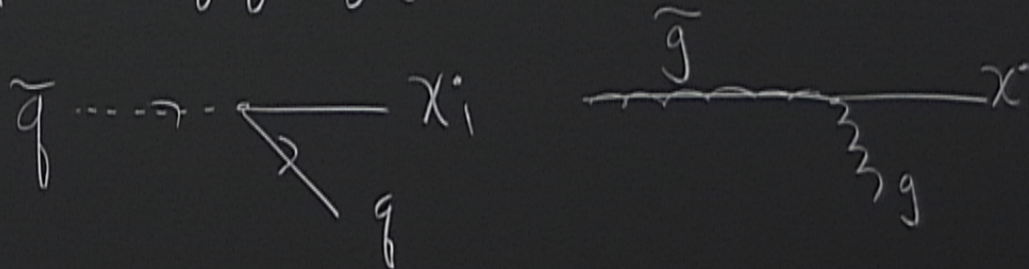
$$1 \quad \gamma = \chi_1^0 = \text{LSP}$$

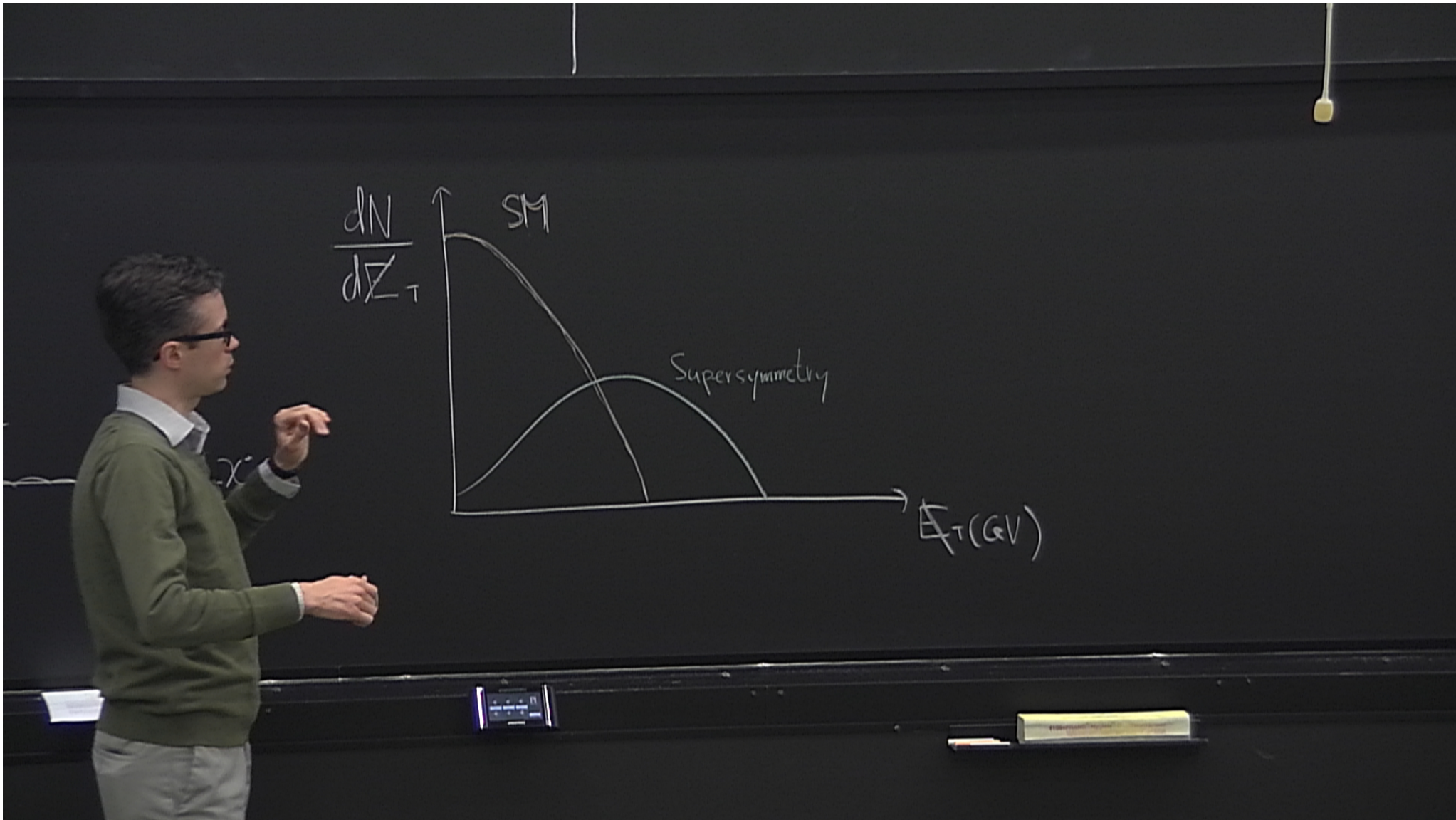
$$\rightarrow \tilde{q}\bar{q}, \tilde{q}\tilde{q}, \tilde{q}\tilde{q}$$

SUSY DM

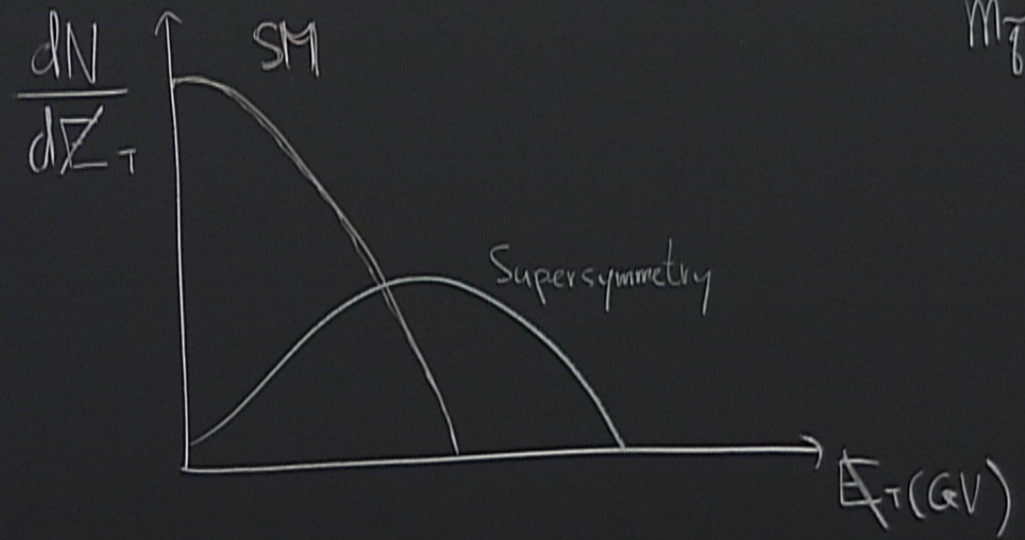
$\hookrightarrow \chi = \chi_1^0 = \text{LSP}$

$pp \rightarrow \bar{q}q, \tilde{q}\tilde{q}, \tilde{q}q$

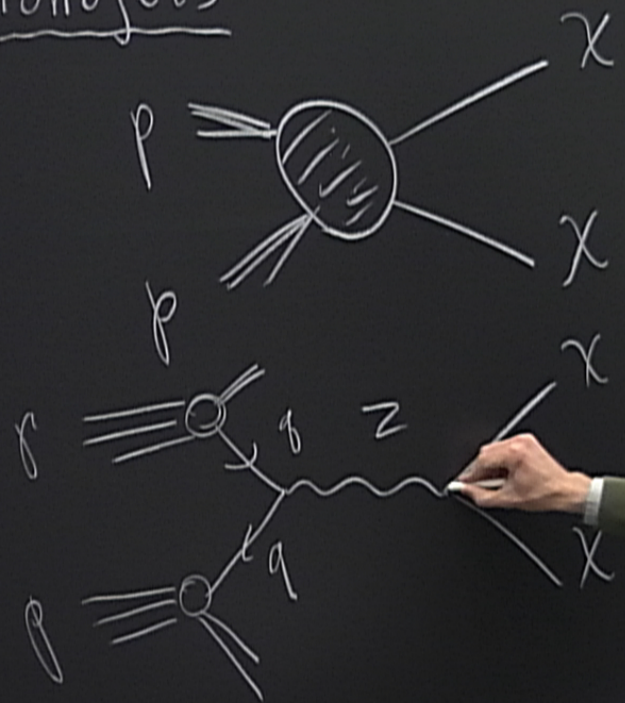




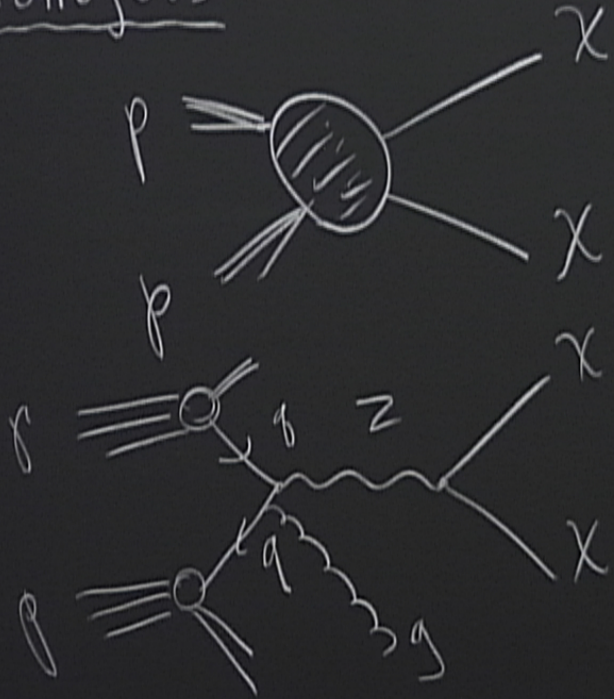
$$M_{\tilde{g}}, M_{\tilde{q}} \geq 1.5 \text{ TeV.}$$



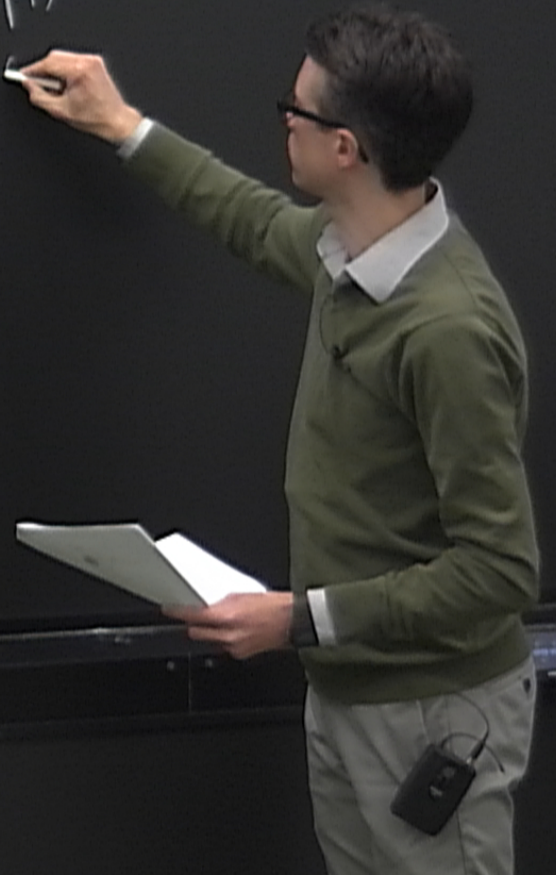
Monojets



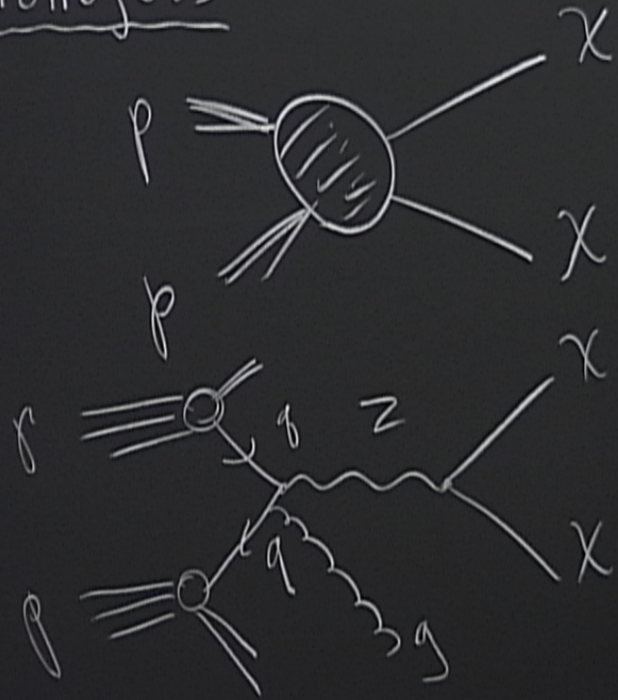
Monojets



$$\sigma_{ij} \sim \sigma_{0j} \cdot \alpha_s(P_T)$$



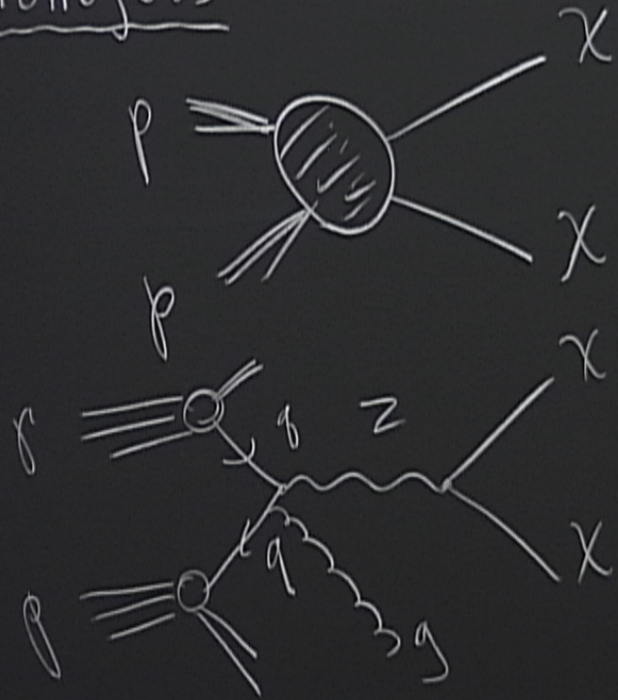
Monojets



$$\sigma_{ij} \sim \sigma_{0j} \cdot \alpha_s(P_T) \cdot \frac{g_s^2}{4\pi}$$



Monojets



$$\sigma_{ij} \sim \sigma_{0j} \cdot \alpha_s^2(P_T)$$

$$\sim \frac{g_s^2}{4\pi} \sim 0.1$$

$$-\mathcal{L}_{\text{eff}} = \frac{1}{\Lambda^2} (\bar{q} \Gamma_1 q) (\bar{\chi} \Gamma_2 \chi)$$



$$-\mathcal{L}_{\text{eff}} = \frac{1}{\Lambda^2} (\bar{q} \Gamma_1 q) (\bar{\chi} \Gamma_2 \chi)$$

VV, AA, SS, PP, AP,

$$\sigma_{DD} = \frac{M_p^2}{\Lambda^4}$$

$$\sigma_{ij} \sim \alpha_s \underbrace{\left(\frac{p_T}{M_p}\right)^2}_{\gg 1} \sigma_{DD}$$

$$\sigma_{ij} \sim \alpha_s \begin{cases} p_T^2 / \Lambda^4 & ; p_T \ll \Lambda \quad (\checkmark) \\ 1/p_T^2 & ; p_T \gg \Lambda \quad (\times) \end{cases}$$

$$-\mathcal{L}_{\text{eff}} = \frac{1}{\Lambda^2} (\bar{q} \Gamma_1 q) (\bar{\chi} \Gamma_2 \chi)$$

VV, AA, SS, PP, AP, ...

$$\sigma_{DD} = \frac{M_p^2}{\Lambda^4}$$

$$\sigma_{ij} \sim \alpha_s \begin{cases} p_T^2 / \Lambda^4 ; & p_T \ll \Lambda \quad (\checkmark) \\ 1/p_T^2 ; & p_T \gg \Lambda \quad (\otimes) \end{cases}$$

$$\sigma_{ij} \sim \alpha_s \underbrace{\left(\frac{p_T}{M_p}\right)^2}_{\gg 1} \sigma_{DD}$$

$$\alpha_s \left(\frac{P_T}{M_p} \right)^2 \gg 1$$

