

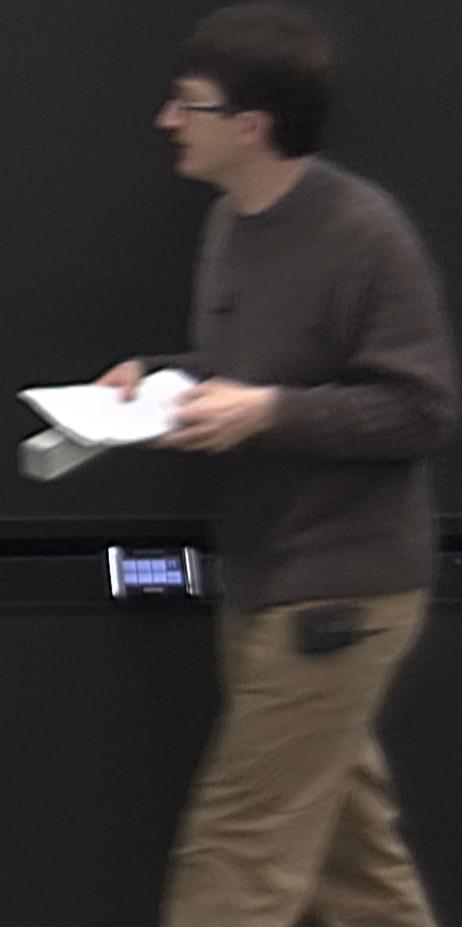
Title: 12/13 PSI - Cosmology Review Lecture 9

Date: Mar 01, 2013 11:30 AM

URL: <http://pirsa.org/13030038>

Abstract:

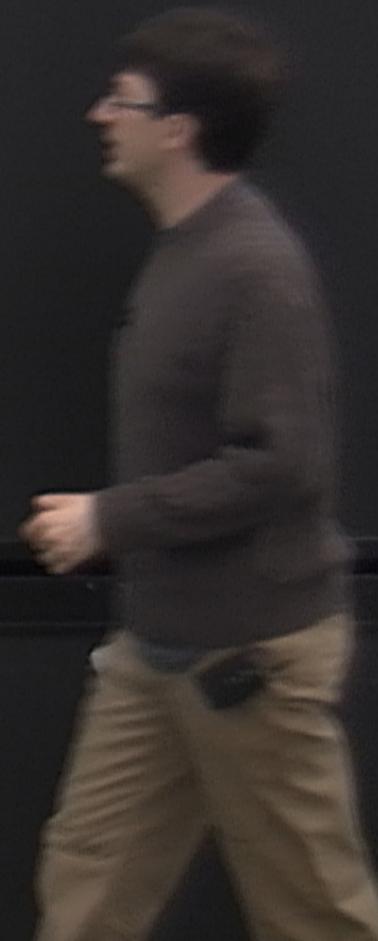
CMB + BBN



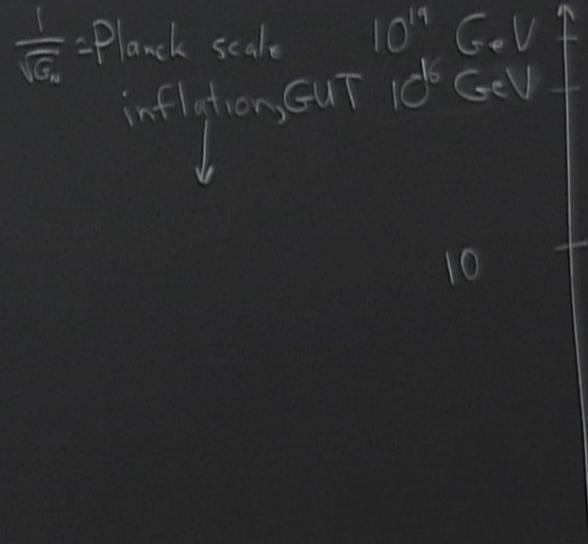
CMB + BBN

$\frac{1}{\sqrt{G_N}}$ = Planck scale

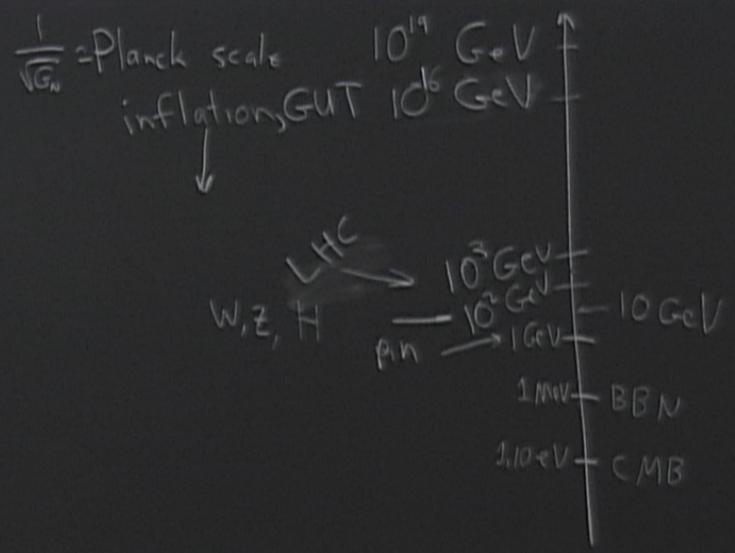
10^{19} GeV
 10^6 GUT



CMB + BBN

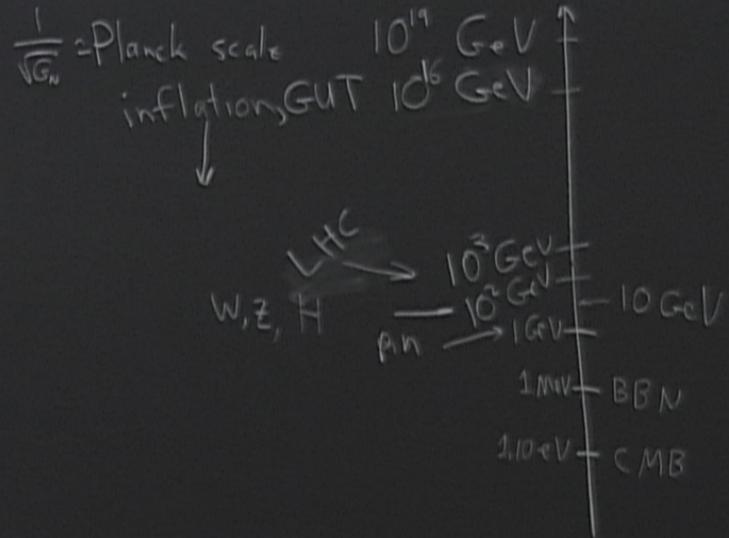


CMB + BBN



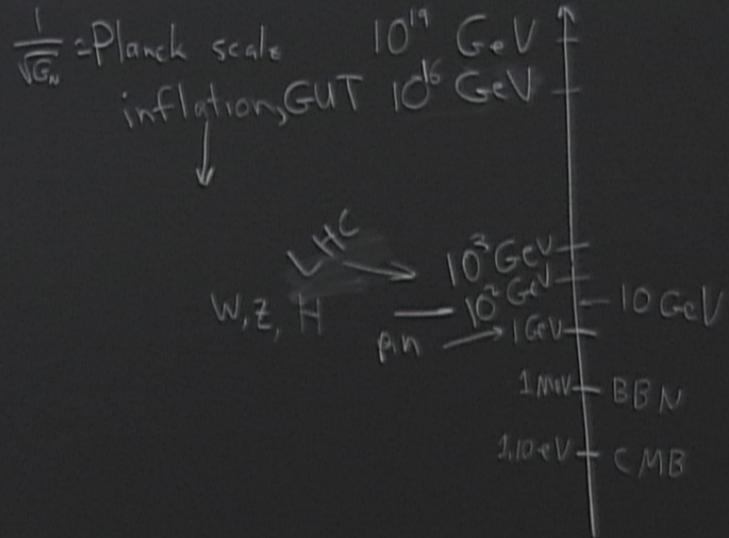
P.P.N.N

CMB + BBN



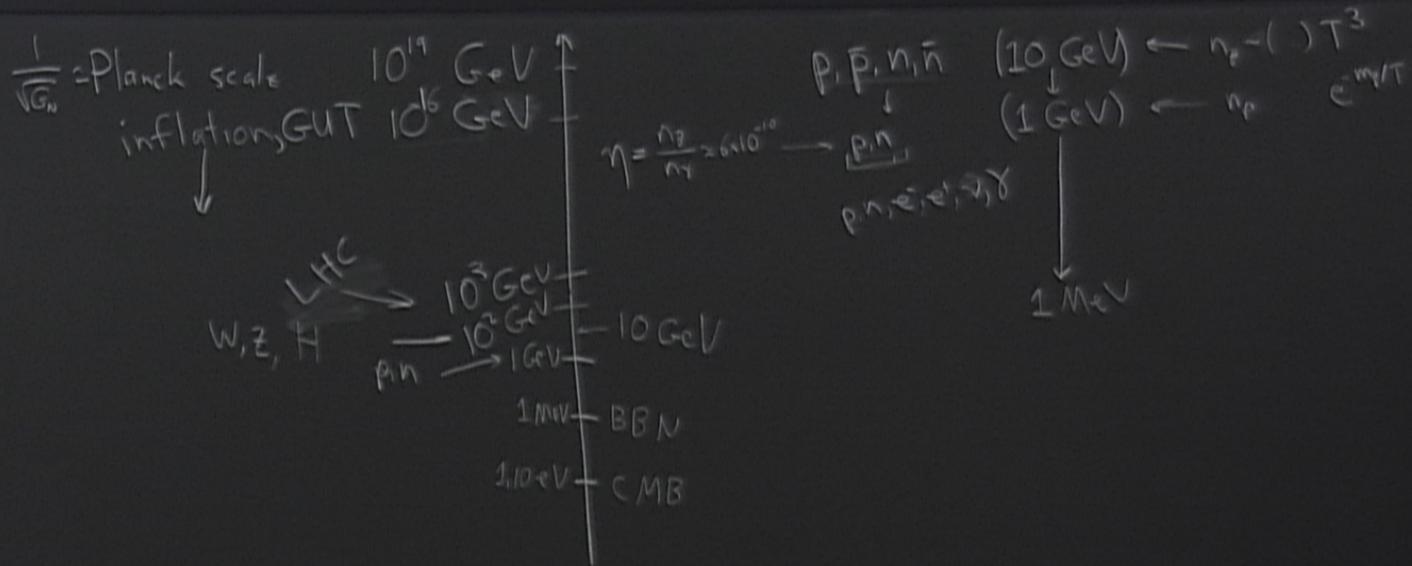
p, \bar{p}, n, \bar{n} (10 GeV) $\leftarrow n_p \propto T^3$
 $(1 \text{ GeV}) \leftarrow n_p \propto e^{-m_p/T}$

CMB + BBN

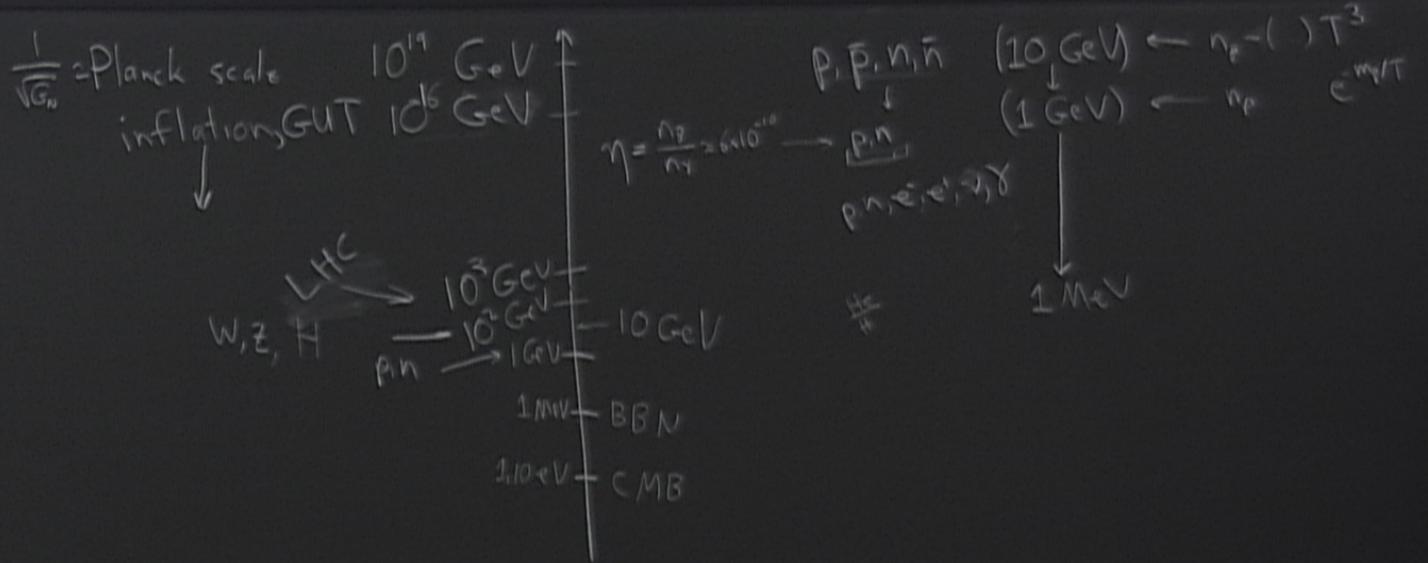


p, \bar{p}, n, \bar{n} $(10 \text{ GeV}) \leftarrow n_p \propto T^3$
 p, n $(1 \text{ GeV}) \leftarrow n_n \propto e^{-m_p/T}$

CMB + BBN



CMB + BBN

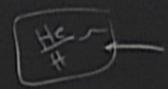
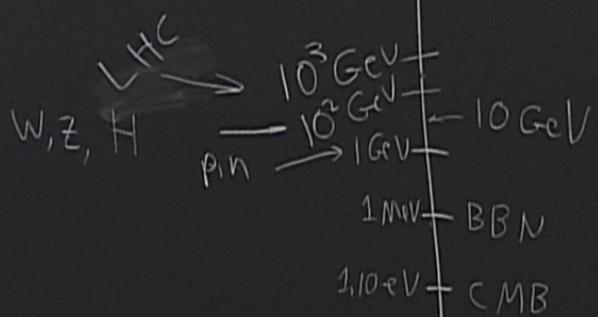


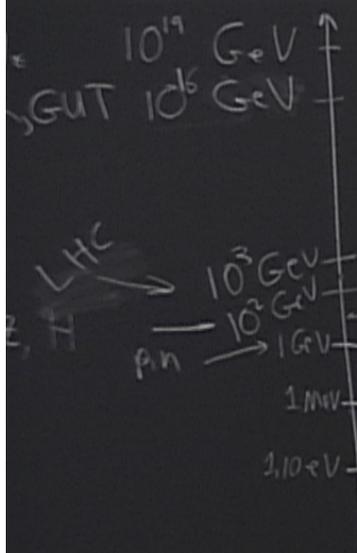
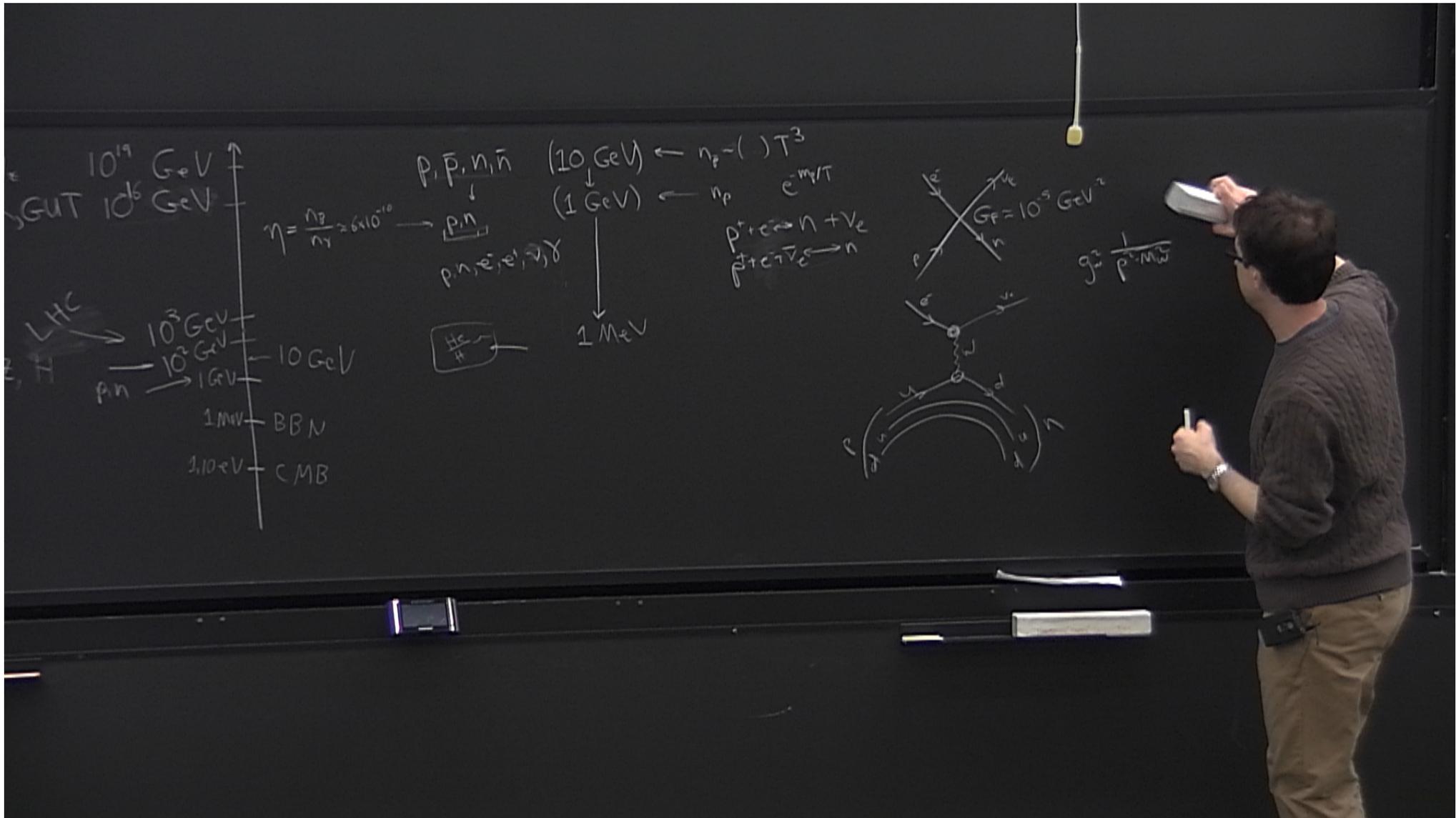
$\frac{1}{\sqrt{G_N}}$ = Planck scale

10^{19} GeV
inflation, GUT 10^{16} GeV

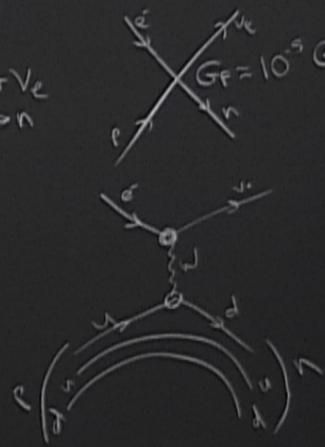
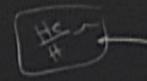
$\eta = \frac{n_B}{n_\gamma} \approx 6 \times 10^{-10}$

p, \bar{p}, n, \bar{n}
 $(10 \text{ GeV}) \leftarrow n_f \propto T^3$
 $(1 \text{ GeV}) \leftarrow n_p \propto e^{-m_p/T}$
 $p + e = n + \bar{v}_e$

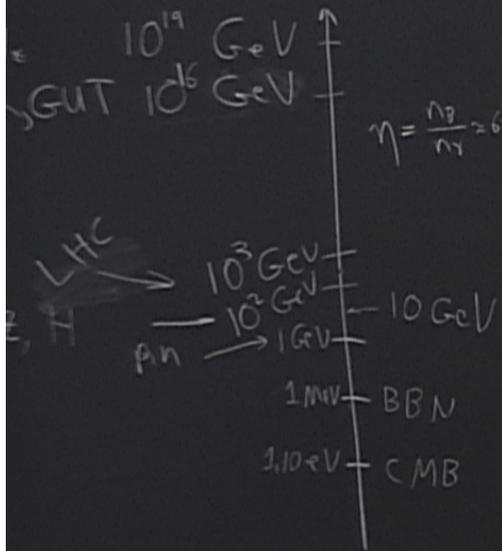




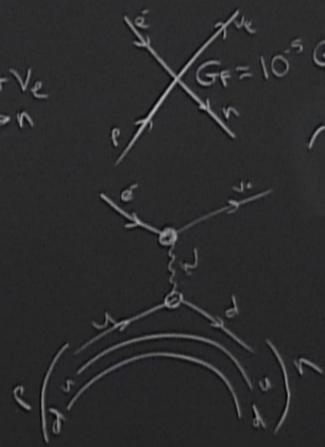
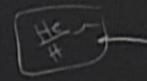
$\eta = \frac{n_B}{n_\gamma} = 6 \times 10^{-10}$
 p, \bar{p}, n, \bar{n} (10 GeV) $\leftarrow n_F \sim T^3$
 $(1 \text{ GeV}) \leftarrow n_p e^{-m/T}$
 $p, n, e, \bar{e}, \nu, \gamma$
 $p + e^- \rightarrow n + \nu_e$
 $\bar{p} + e^- \bar{\nu}_e \rightarrow n$



$g_s^2 \sim \frac{1}{p^2 - M_W^2}$



$\eta = \frac{n_B}{n_\gamma} = 6 \times 10^{-10}$
 p, \bar{p}, n, \bar{n} (10 GeV) $\leftarrow n_F \sim T^3$
 $(1 \text{ GeV}) \leftarrow n_p e^{-m/T}$
 $p, n, e, \bar{e}, \nu, \bar{\nu}, \gamma$
 $p + e \rightarrow n + \nu_e$
 $\bar{p} + e + \bar{\nu}_e \rightarrow n$



$$M \sim g_W^2 \frac{1}{k^2 - M_W^2}$$

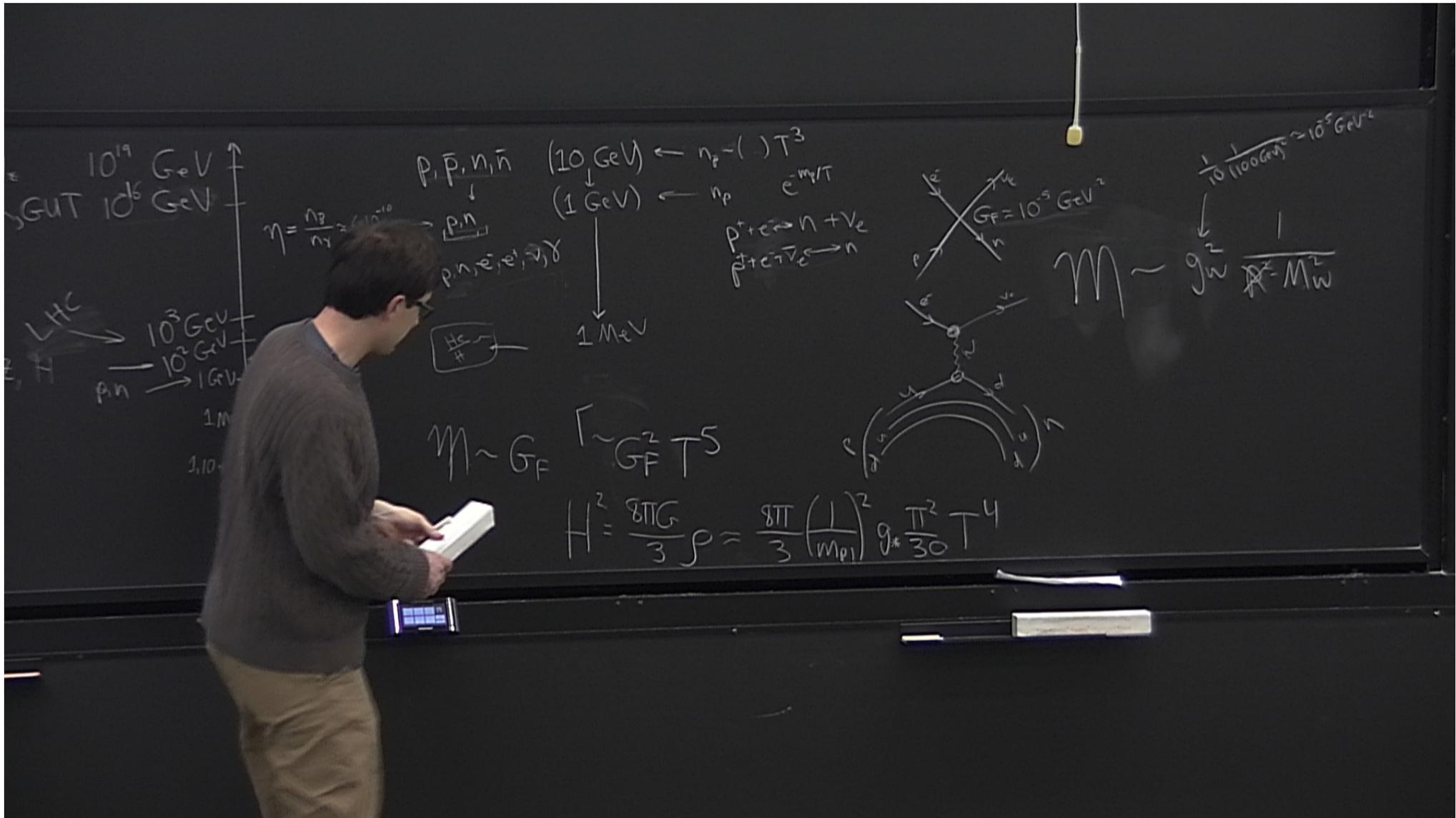
10^{19} GeV
 GUT 10^{16} GeV
 LHC 10^4 GeV
 H 10^2 GeV
 p, n 1 GeV
 1 MeV BBN
 1.10 eV CMB

$\eta = \frac{n_B}{n_\gamma} = 6 \times 10^{-10}$
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 $\eta = \frac{n_B}{n_\gamma} = 6 \times 10^{-10}$

p, \bar{p}, n, \bar{n} (10 GeV) $\leftarrow n_F \sim T^3$
 $(1 \text{ GeV}) \leftarrow n_p e^{-m/T}$
 $p, n, e, \bar{e}, \nu, \bar{\nu}$
 1 MeV
 $M \sim GF$

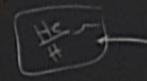
$p + e \rightarrow n + \nu_e$
 $\bar{p} + e + \bar{\nu}_e \rightarrow n$

$G_F = 10^{-5} \text{ GeV}^{-2}$
 $M \sim \frac{1}{\Lambda^2} = \frac{1}{M_W^2}$
 $\frac{1}{10^{16} \text{ GeV}^2} \sim 10^{-32} \text{ GeV}^{-2}$



10^{19} GeV
 GUT 10^{16} GeV
 LHC 10^3 GeV
 H 10^2 GeV
 p, n 1 GeV
 1 M
 1, 10

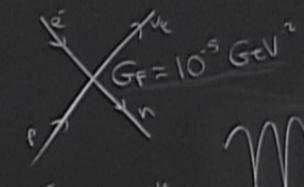
$\eta = \frac{n_B}{n_\gamma} \approx 6 \cdot 10^{-10}$
 p, \bar{p}, n, \bar{n}
 $(10 \text{ GeV}) \leftarrow n_p \sim T^3$
 $(1 \text{ GeV}) \leftarrow n_p e^{-m/T}$
 $p, n, e, e^-, \nu, \gamma$
 $p + e^- \leftrightarrow n + \nu_e$
 $\bar{p} + e^- \leftrightarrow \bar{n}$



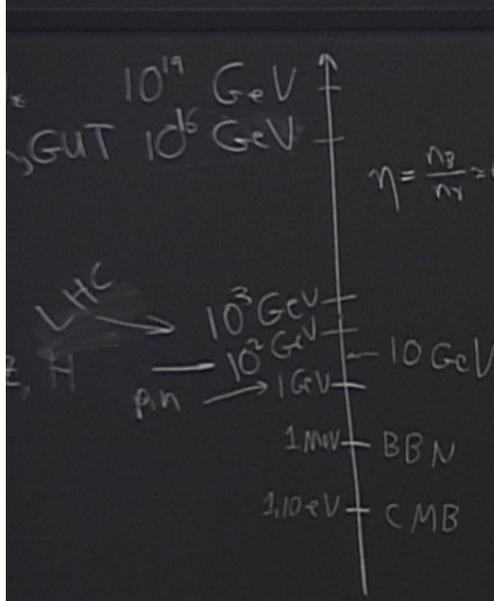
1 MeV

$\mathcal{M} \sim G_F$
 $\Gamma \sim G_F^2 T^5$

$$H^2 = \frac{8\pi G}{3} \rho = \frac{8\pi}{3} \left(\frac{1}{m_{pl}}\right)^2 g_* \frac{\pi^2}{30} T^4$$

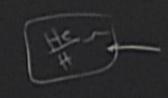


$\mathcal{M} \sim g_w^2 \frac{1}{M_w^2}$
 $\frac{1}{10 (100 \text{ GeV})^2} \approx 10^{-5} \text{ GeV}^{-2}$



$$\eta = \frac{n_B}{n_\gamma} = 6 \times 10^{-10}$$

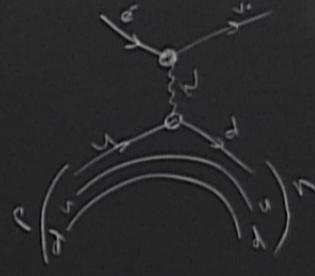
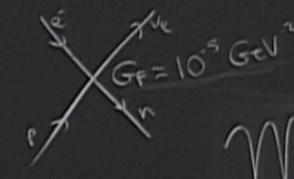
p, \bar{p}, n, \bar{n} (10 GeV) $\leftarrow n_F \sim T^3$
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 $p, n, e, \bar{e}, \nu, \bar{\nu}$
 $p + e \rightarrow n + \nu_e$
 $\bar{p} + \bar{e} \rightarrow \bar{n} + \bar{\nu}_e$



1 MeV

$$\mathcal{M} \sim G_F \quad \Gamma \sim G_F^2 T^5$$

$$H^2 = \frac{8\pi G}{3} \rho = \frac{8\pi}{3} \left(\frac{1}{m_{pl}}\right)^2 g_* \frac{\pi^2}{30} T^4$$



$$M \sim g_w^2 \frac{1}{\Lambda^2} = M_w^2$$

$$T \sim 1 \text{ MeV}$$

$$\frac{1}{10^{16} \text{ GeV}^2} \approx 10^{-5} \text{ GeV}^{-2}$$

$$n \approx \left(\frac{mT}{2\pi} \right)^{3/2} \exp\left[-\frac{m}{T} \right]$$

$$\frac{n_n}{n_p} \approx \left(\frac{m_n}{m_p} \right)^{3/2} \exp\left[-\frac{(m_n - m_p)}{T} \right] \sim \exp\left[-\frac{(1.3 \text{ MeV})}{.8 \text{ MeV}} \right]$$

$$n \approx \left(\frac{mT}{2\pi} \right)^{3/2} \exp\left[-\frac{m}{T} \right]$$

$\tau_{n-15 \text{ min}}$

$$\frac{n_n}{n_p} \approx \left(\frac{m_n}{m_p} \right)^{3/2} \exp\left[-\frac{(m_n - m_p)}{T} \right] \sim \exp\left[-\frac{(1.3 \text{ MeV})}{.8 \text{ MeV}} \right] \sim \frac{1}{6} \rightarrow \frac{1}{7}$$

$$H = \frac{c^2}{3} \rho = \frac{c^2}{3} \left(\frac{1}{m_{pl}} \right) \rho$$

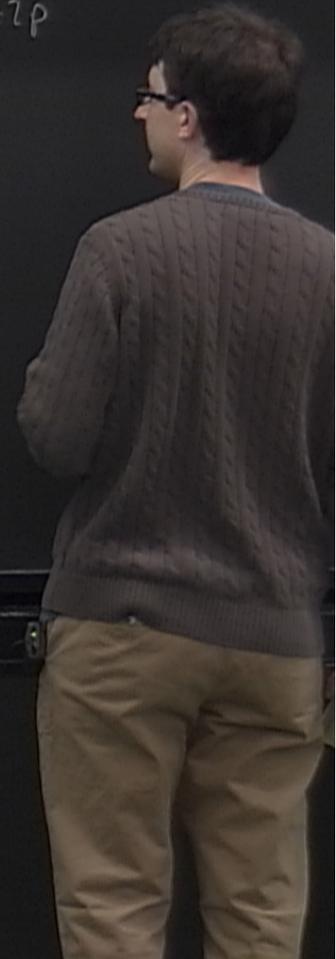
$$n = \left(\frac{mT}{2\pi} \right)^{3/2} \exp\left[-\frac{m}{T} \right]$$

$\tau_{n-15 \text{ min}}$

$${}^4\text{H} = 2n + 2p$$

n_n

$$\frac{n_n}{n_p} = \left(\frac{m_n}{m_p} \right)^{3/2} \exp\left[-\frac{(m_n - m_p)}{T} \right] \sim \exp\left[-\frac{(1.3 \text{ MeV})}{.8 \text{ MeV}} \right] \sim \frac{1}{6} \rightarrow \frac{1}{7}$$



$$H = \frac{c}{3} \rho = \frac{c}{3} \left(\frac{1}{m_{pl}} \right) \rho$$

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$${}^4\text{H} = 2n + 2p$$

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$$\frac{\frac{n_n}{2}}{n_n + n_p}$$

$$H = \frac{81G}{3\rho} = \frac{81}{3} \left(\frac{1}{m_{pl}} \right) g$$

$$n = \left(\frac{mT}{2\pi} \right)^{3/2} \exp\left[-\frac{m}{T} \right]$$

$T_{n-15 \text{ min}}$

$${}^4\text{H} = 2n + 2p$$

$$\frac{n_n}{n_p} = \left(\frac{m_n}{m_p} \right)^{3/2} \exp\left[-\frac{(m_n - m_p)}{T} \right] \sim \exp\left[-\frac{(1.3 \text{ MeV})}{.8 \text{ MeV}} \right] \sim \frac{1}{6} \rightarrow \frac{1}{7}$$

$$\frac{4n_p \frac{n_n}{2}}{n_p (n + n_p)}$$

$$H = \frac{8\pi G}{3} \rho = \frac{8\pi}{3} \left(\frac{1}{m_{pl}} \right) g$$

$$n = \left(\frac{mT}{2\pi} \right)^{3/2} \exp\left[-\frac{m}{T} \right]$$

$T_{n-15 \text{ min}}$

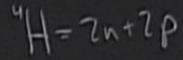
$${}^4\text{H} = 2n + 2p$$

$$\frac{n_n}{n_p} = \left(\frac{m_n}{m_p} \right)^{3/2} \exp\left[-\frac{(m_n - m_p)}{T} \right] \sim \exp\left[-\frac{(1.3 \text{ MeV})}{.8 \text{ MeV}} \right] \sim \frac{1}{6} \rightarrow \frac{1}{7}$$

$$\frac{4 \times \frac{n_n}{2n_p}}{\frac{n_n + n_p}{n_p}} = \frac{4 \cdot \frac{1}{2}}{\frac{1}{2} + 1}$$

$$H = \frac{8\pi^5}{3} \rho = \frac{8\pi^5}{3} \left(\frac{1}{m_p}\right) g_* \frac{11}{30} T^4$$

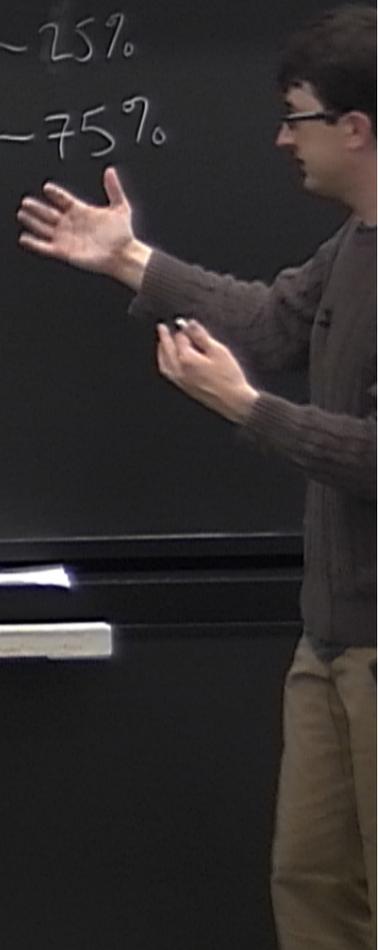
$T_n \sim 15 \text{ min}$



$$\sim \exp\left[-\frac{(1.3 \text{ MeV})}{.8 \text{ MeV}}\right] \sim \frac{1}{6} \rightarrow \frac{1}{7}$$

$$\frac{4 \exp\left(\frac{n_n}{2n_p}\right)}{\frac{n_n + n_p}{n_p}} = \frac{4 \frac{1/7}{2}}{\frac{1}{7} + 1} = \frac{1}{4}$$

He ~ 25%
H ~ 75%



$$H = \frac{616}{3} \rho = \frac{611}{3} \left(\frac{1}{m_p} \right) g_* \frac{11}{30} T^4$$

$\tau_{n-15 \text{ min}}$

${}^4\text{H} = 2n + 2p$

$$\left[\frac{-(1.3 \text{ MeV})}{.8 \text{ MeV}} \right] \sim \frac{1}{6} \rightarrow \frac{1}{7}$$

$$\frac{4 n_p \frac{n_n}{2 n_p}}{\frac{n_n + n_p}{n_p}} = \frac{4 \frac{1/7}{2}}{\frac{1}{7} + 1} = \frac{1}{4}$$

He ~ 25%

H ~ 75%

$\text{Li}^7 \rightarrow \frac{\text{observed}}{\text{predicted}} = \frac{1}{3}$

$$H = \frac{616}{3} \rho = \frac{611}{3} \left(\frac{1}{m_p} \right) g_* \frac{11}{30} T^4$$

$\tau_{n-15 \text{ min}}$

${}^4\text{H} = 2n + 2p$

$$\left[\frac{-(1.3 \text{ MeV})}{.8 \text{ MeV}} \right] \sim \frac{1}{6} \rightarrow \frac{1}{7}$$

$$\frac{4n_p \frac{n_n}{2n_p}}{\frac{n_n + n_p}{n_p}} = \frac{4 \frac{1/7}{2}}{\frac{1}{7} + 1} = \frac{1}{4}$$

He ~ 25%
H ~ 75%
→ $\text{Li}^7 \rightarrow \frac{\text{observed}}{\text{predicted}} = \frac{1}{3}$

$$H = \frac{c^2}{3} \rho = \frac{8\pi}{3} \left(\frac{1}{m_p} \right) g_* \frac{11}{30} T^4$$

$\tau_{n-15 \text{ min}}$

${}^4\text{H} = 2n + 2p$

$$\left[\frac{-(1.3 \text{ MeV})}{.8 \text{ MeV}} \right] \sim \frac{1}{6} \rightarrow \frac{1}{7}$$

$$\frac{4n_p \frac{n_n}{2n_p}}{\frac{n_n + n_p}{n_p}} = \frac{4 \frac{1/7}{2}}{\frac{1}{7} + 1} = \frac{1}{4}$$

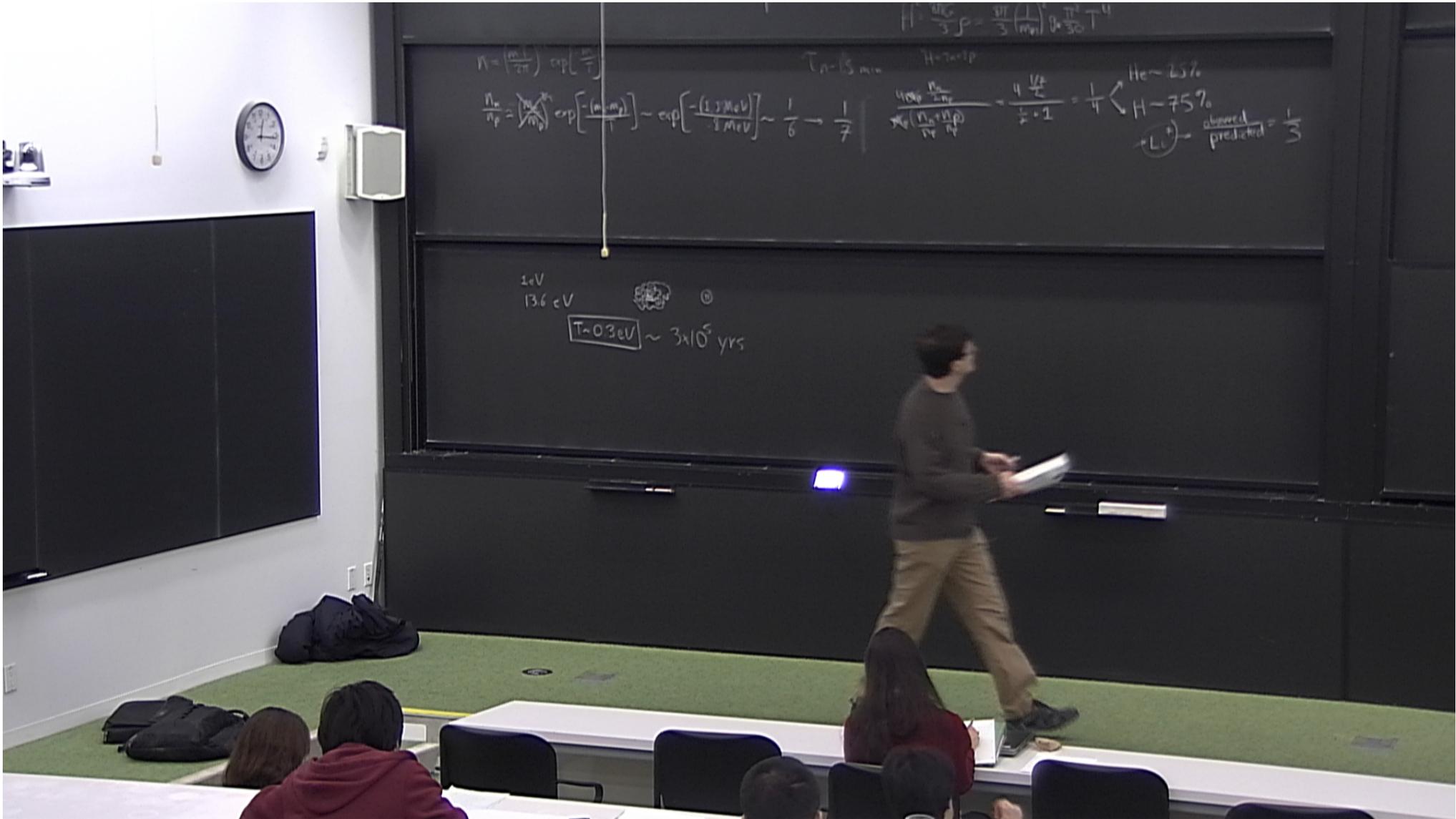
He ~ 25%

H ~ 75%

$\rightarrow \text{Li}^7$

$\frac{\text{observed}}{\text{predicted}} = \frac{1}{3}$

$$m(2n+2p) > m_{H^2}$$



$$n = \left(\frac{m\lambda}{2\pi}\right) \exp\left(-\frac{m\lambda^2}{2}\right)$$

$$\frac{n_n}{n_p} = \left(\frac{m_n}{m_p}\right)^{3/2} \exp\left[-\frac{(m_n - m_p)c^2}{kT}\right] \sim \frac{1}{6} \rightarrow \frac{1}{7}$$

$$H^2 = \frac{8\pi G}{3} \rho = \frac{8\pi}{3} \left(\frac{1}{m_p}\right) \rho_0 \frac{T^4}{30}$$

$$T_n = 1.3 \text{ min} \quad H = 70 \text{ km/s/Mpc}$$

$$\frac{4n_n \frac{m_n}{m_p}}{4n_p \frac{m_p}{m_p}} = \frac{4 \frac{1}{7}}{4} = \frac{1}{7} \rightarrow \frac{1}{4}$$

$$\left. \begin{array}{l} \text{He} \sim 25\% \\ \text{H} \sim 75\% \end{array} \right\} \text{Li}^+ \rightarrow \frac{\text{observed}}{\text{predicted}} = \frac{1}{3}$$

$$1 \text{ eV} \\ 13.6 \text{ eV} \quad \text{⊙}$$

$$\tau \sim 0.3 \text{ eV} \sim 3 \times 10^5 \text{ yrs}$$

1 eV

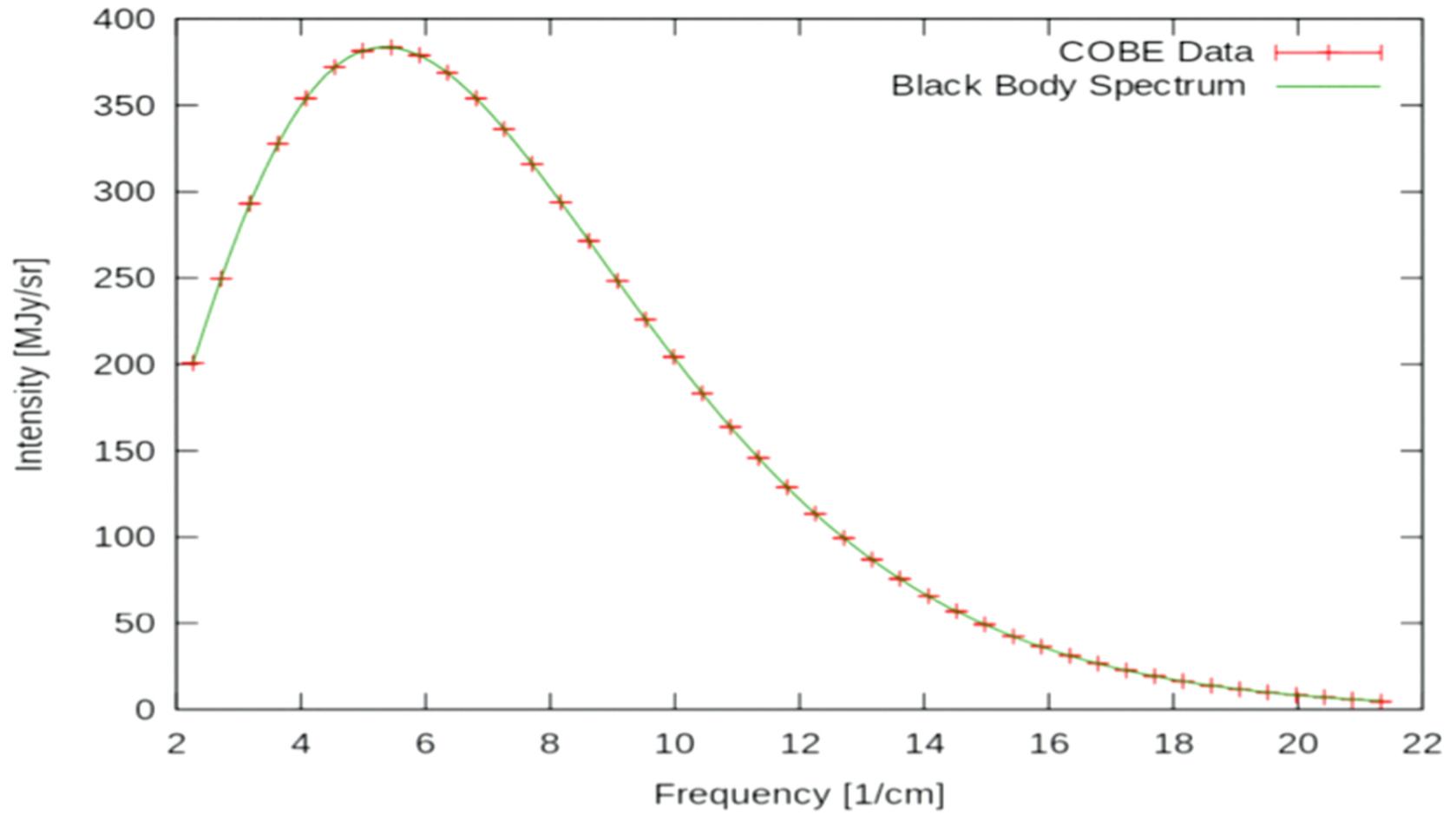
13.6 eV

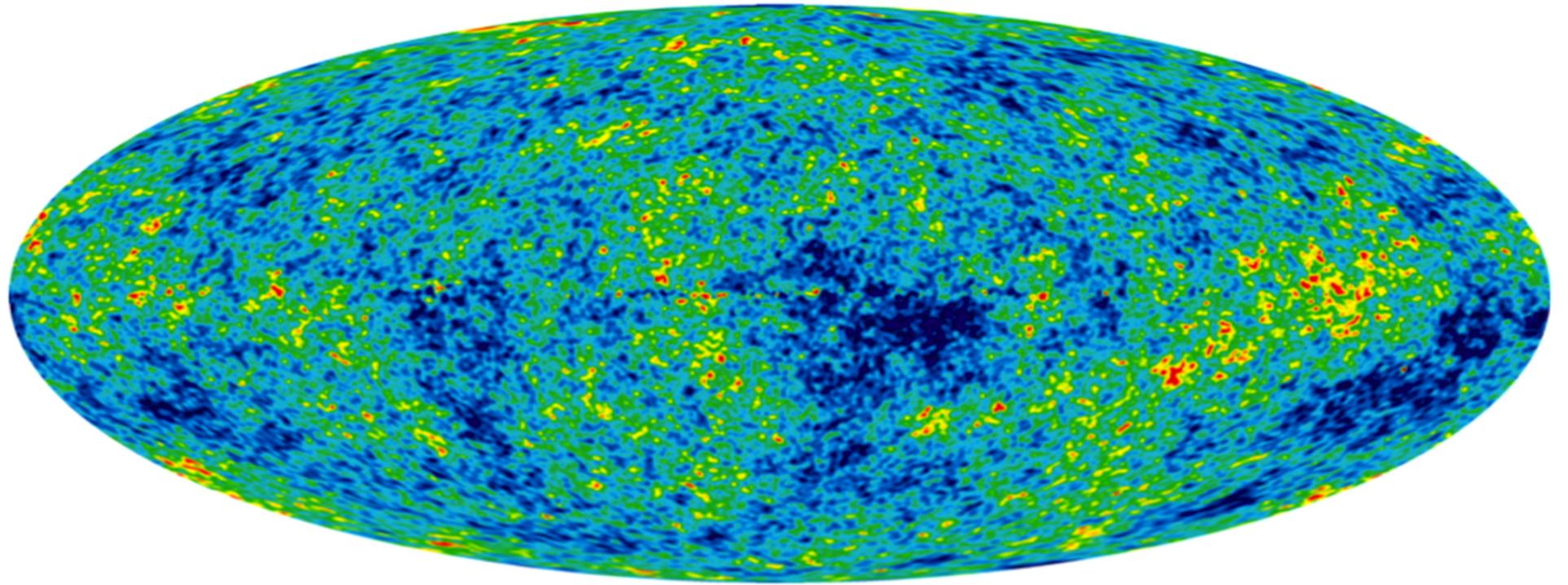


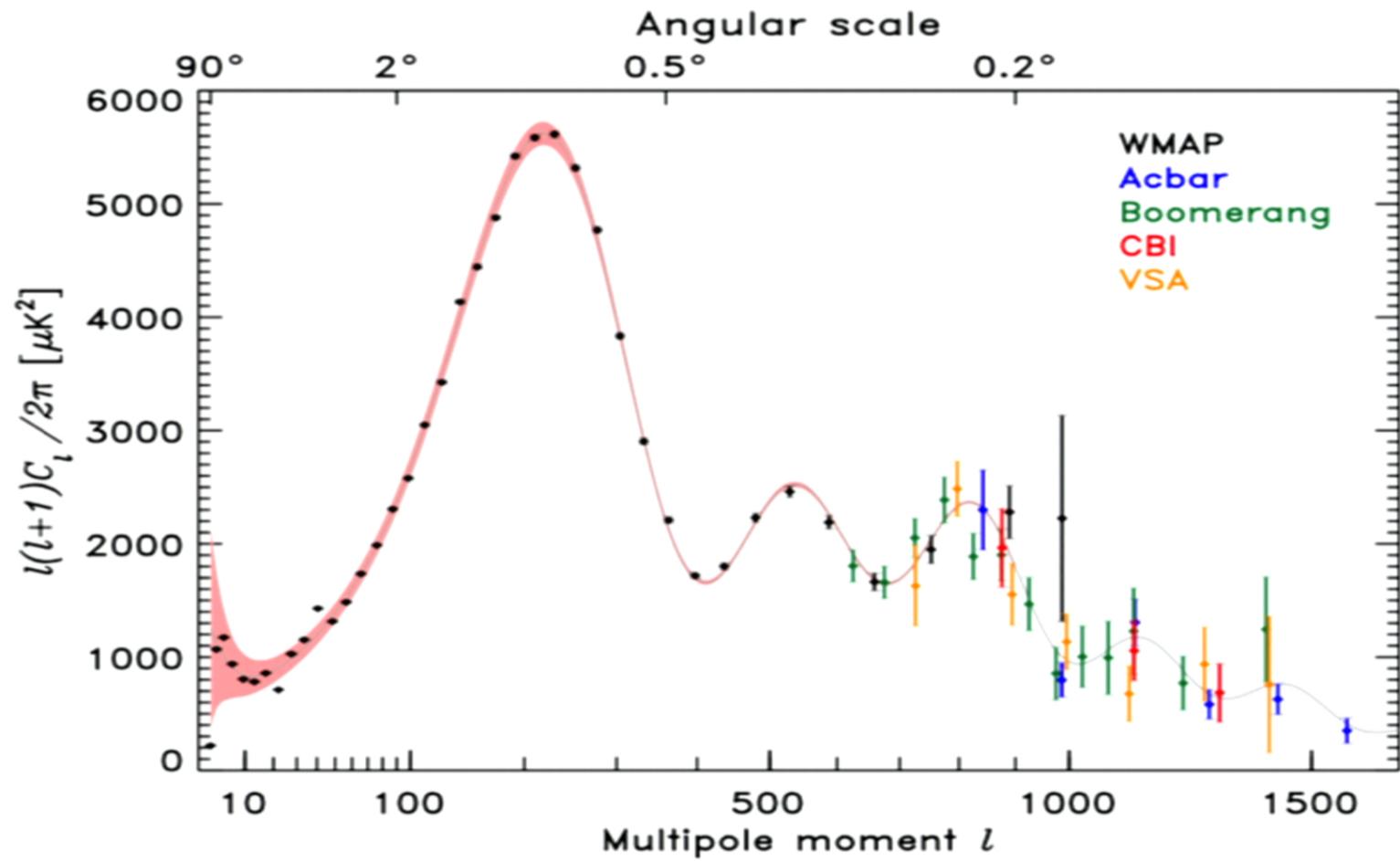
(H)

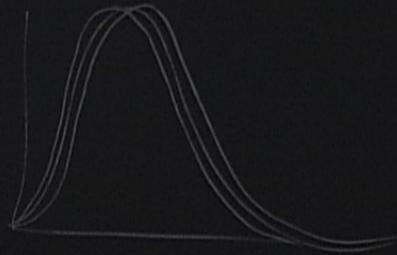
$$T \sim 0.3 \text{ eV} \sim 3 \times 10^5 \text{ yrs}$$

Cosmic Microwave Background Spectrum from COBE









$$C_l = \sum_{m=-l}^l \frac{|a_{lm}|^2}{2l+1}$$

$$T(\theta, \varphi) = T_0 + \delta T(\theta, \varphi)$$

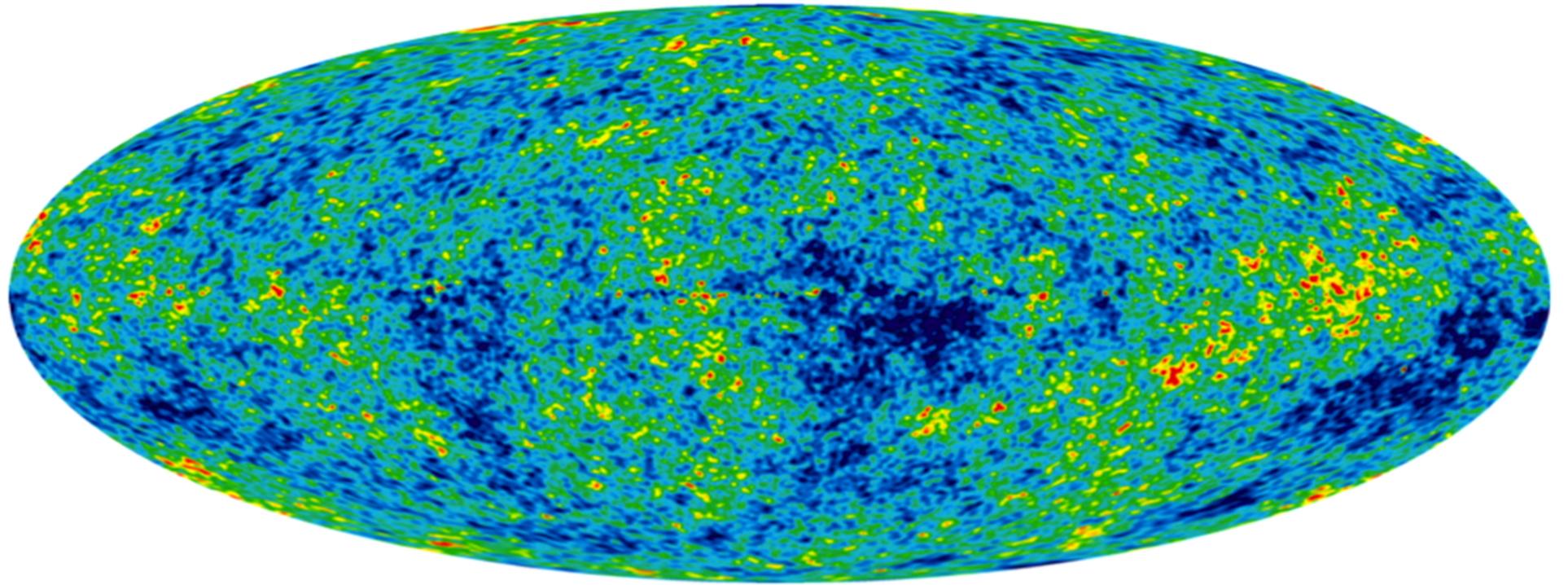
↑
27K

$$\delta T(\theta, \varphi)$$

$$\sum_{l=0}^{\infty} \sum_{m=-l}^l a_{lm} Y_l^m(\theta, \varphi)$$

$$Y_l^m(\theta, \varphi)$$

$l=0, 1, \dots, \infty$
 $-l < m < l \quad (2l+1)$



DM

Baryonic

δ



x

DM

Baryonic

δ

↑



→ x

