

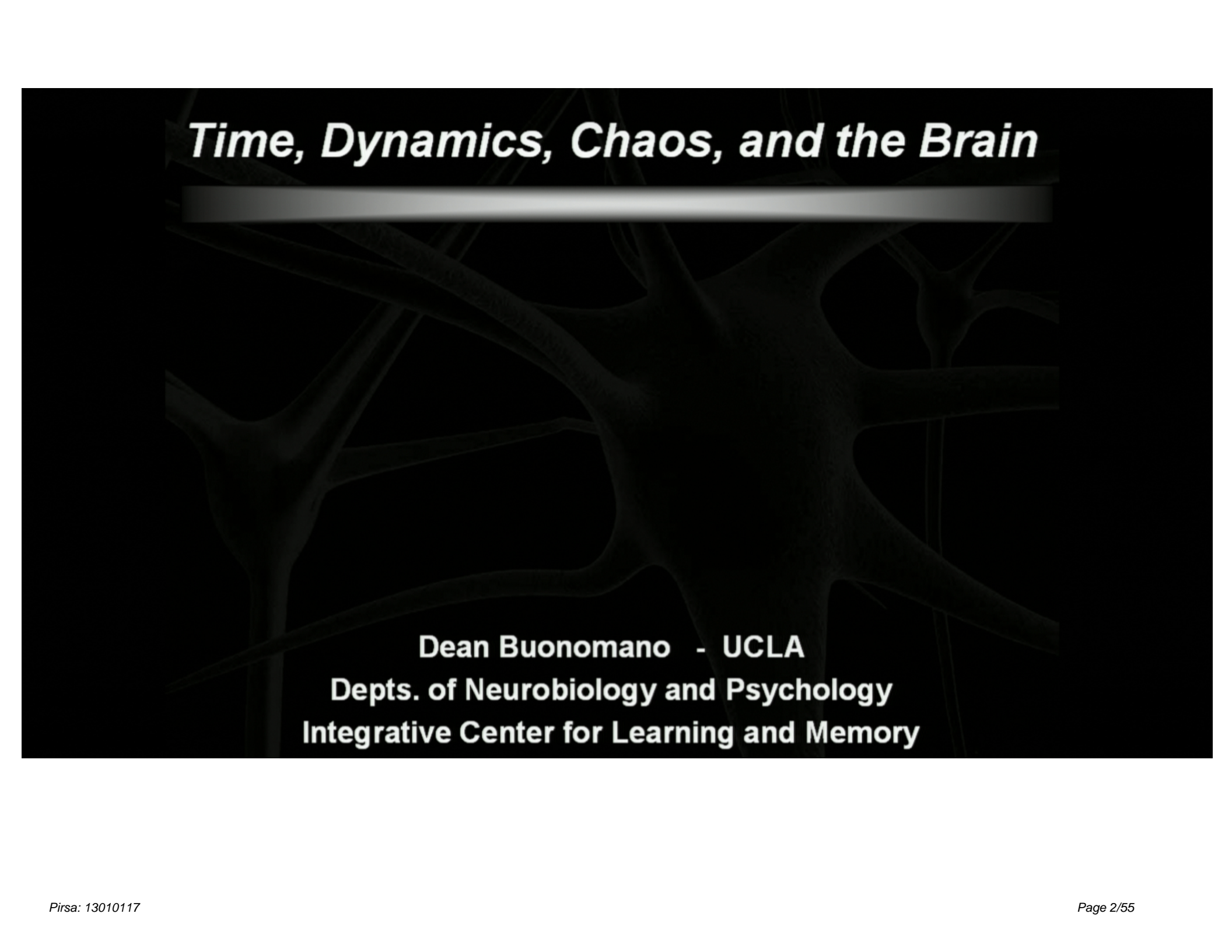
Title: Time, Dynamics, Chaos, and the Brain

Date: Jan 29, 2014 02:00 PM

URL: <http://pirsa.org/13010117>

Abstract: <span>Time poses a fundamental problem in neuroscience, in part, because at its core the brain is a prediction machine: the brain evolved to allow animals to anticipate, adapt, and prepare for future events. To accomplish this function the brain tells time on scales spanning 12 orders of magnitude. In contrast to most man made clocks that share a very simply underlying principle-counting the "tics" of an oscillator-evolution has devised many different solutions to the problem of telling time. On the scale of milliseconds and seconds experimental and computational evidence suggests that the brain relies on neural dynamics to tell time. For this strategy to work two conditions have to be met: the states of the neural network must evolve in a nonrepeating pattern over the relevant interval, and the sequence of states must be reproducible every time the system is reengaged. Recurrently connected networks of neurons can generate rich dynamics, but a long standing challenge is that the regimes that create computationally powerful dynamics are chaotic-and thus cannot generate reproducible patterns. We have recently demonstrated that by tuning the weights (the coupling coefficients) between the units of artificial neural networks it is possible to generate locally stable trajectories embedded within chaotic attractors. These stable patterns function as "dynamic attractors" and can be used to encode and tell time. They also exhibit a novel feature characteristic of biological systems: the ability to autonomously "return" to the pattern being generated in the face of perturbations.</span>

# ***Time, Dynamics, Chaos, and the Brain***

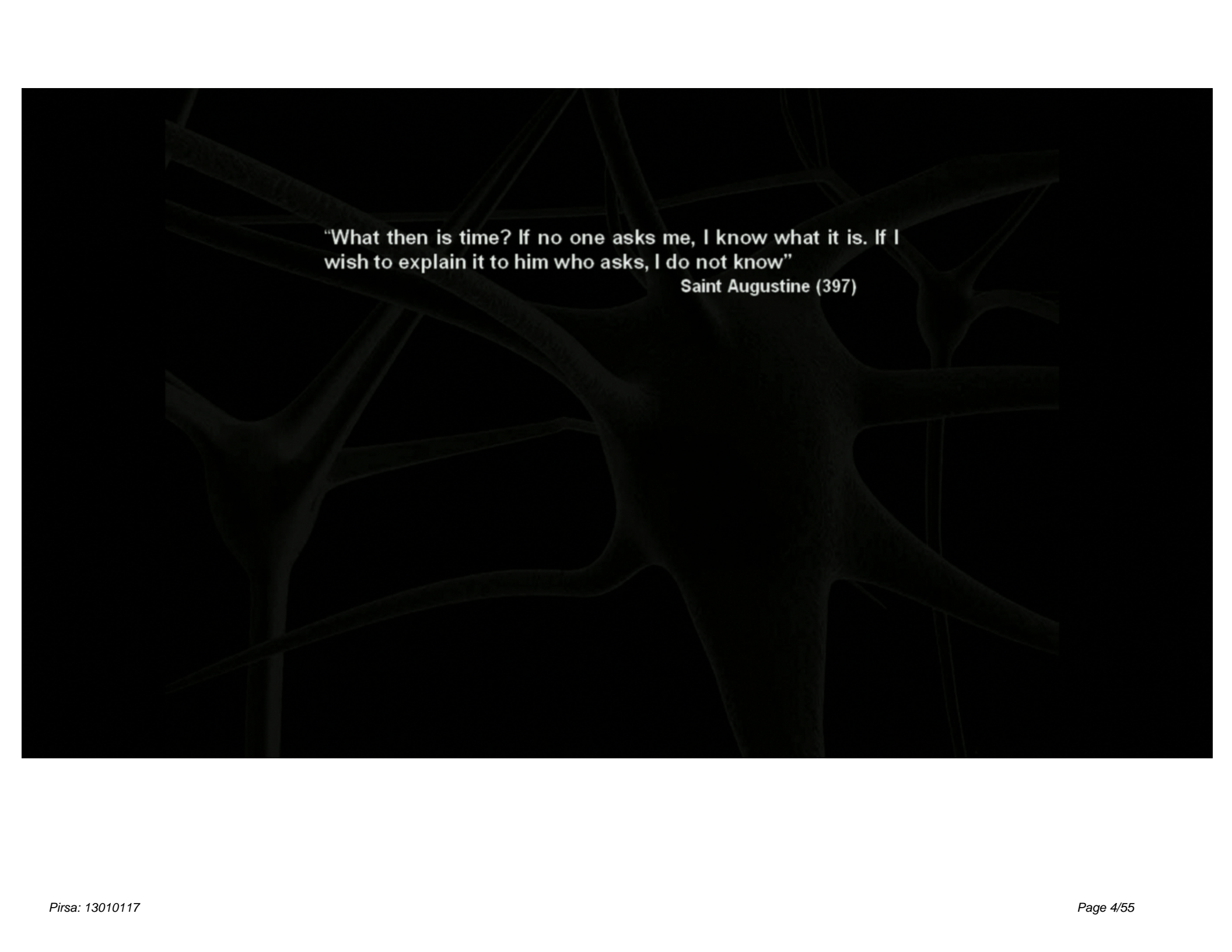


**Dean Buonomano - UCLA**  
**Depts. of Neurobiology and Psychology**  
**Integrative Center for Learning and Memory**

# Time, Dynamics, Chaos, and the Brain

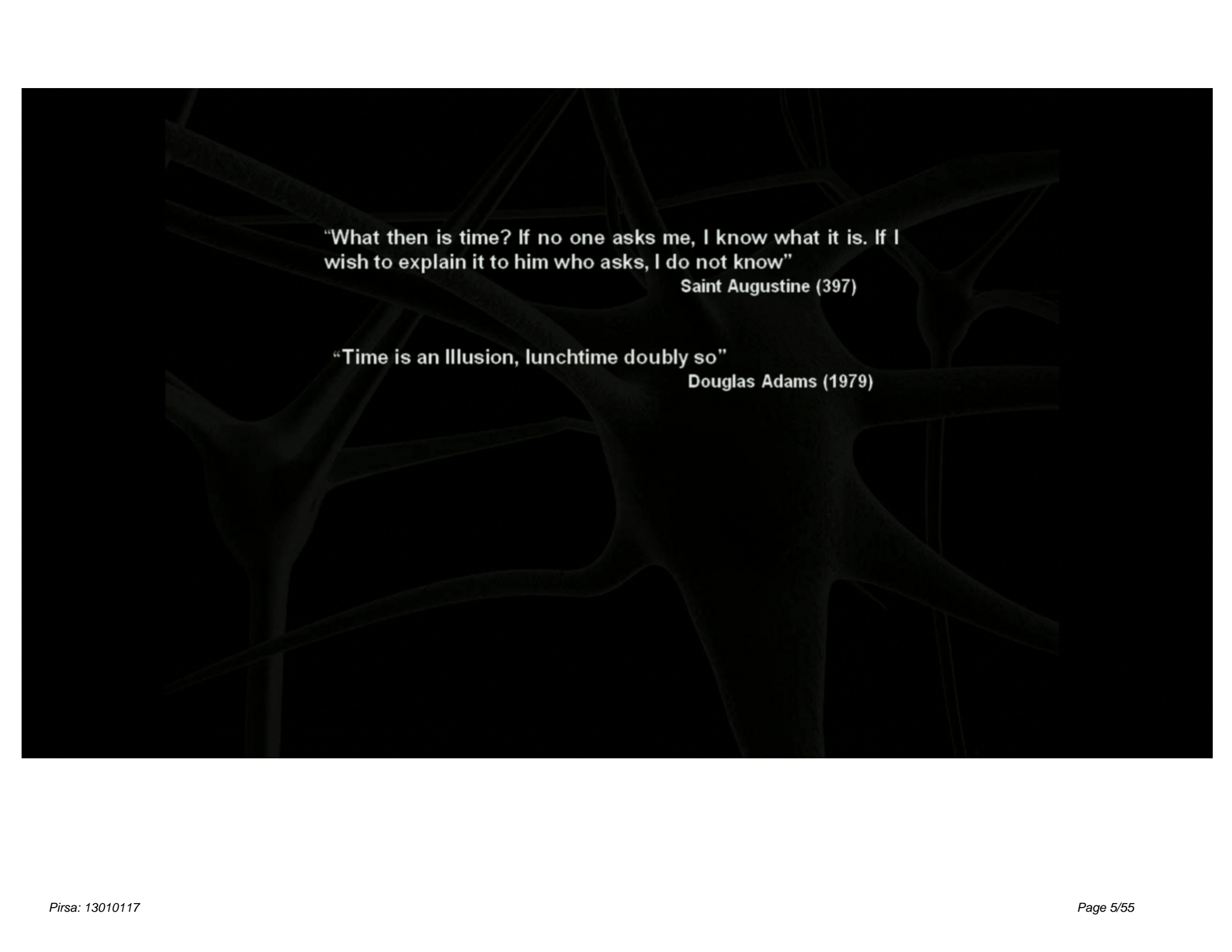
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"What then is time? If no one asks me, I know what it is. If I wish to explain it to him who asks, I do not know"

Saint Augustine (397)



**“What then is time? If no one asks me, I know what it is. If I wish to explain it to him who asks, I do not know”**

**Saint Augustine (397)**

**“Time is an Illusion, lunchtime doubly so”**

**Douglas Adams (1979)**

**“What then is time? If no one asks me, I know what it is. If I wish to explain it to him who asks, I do not know”**

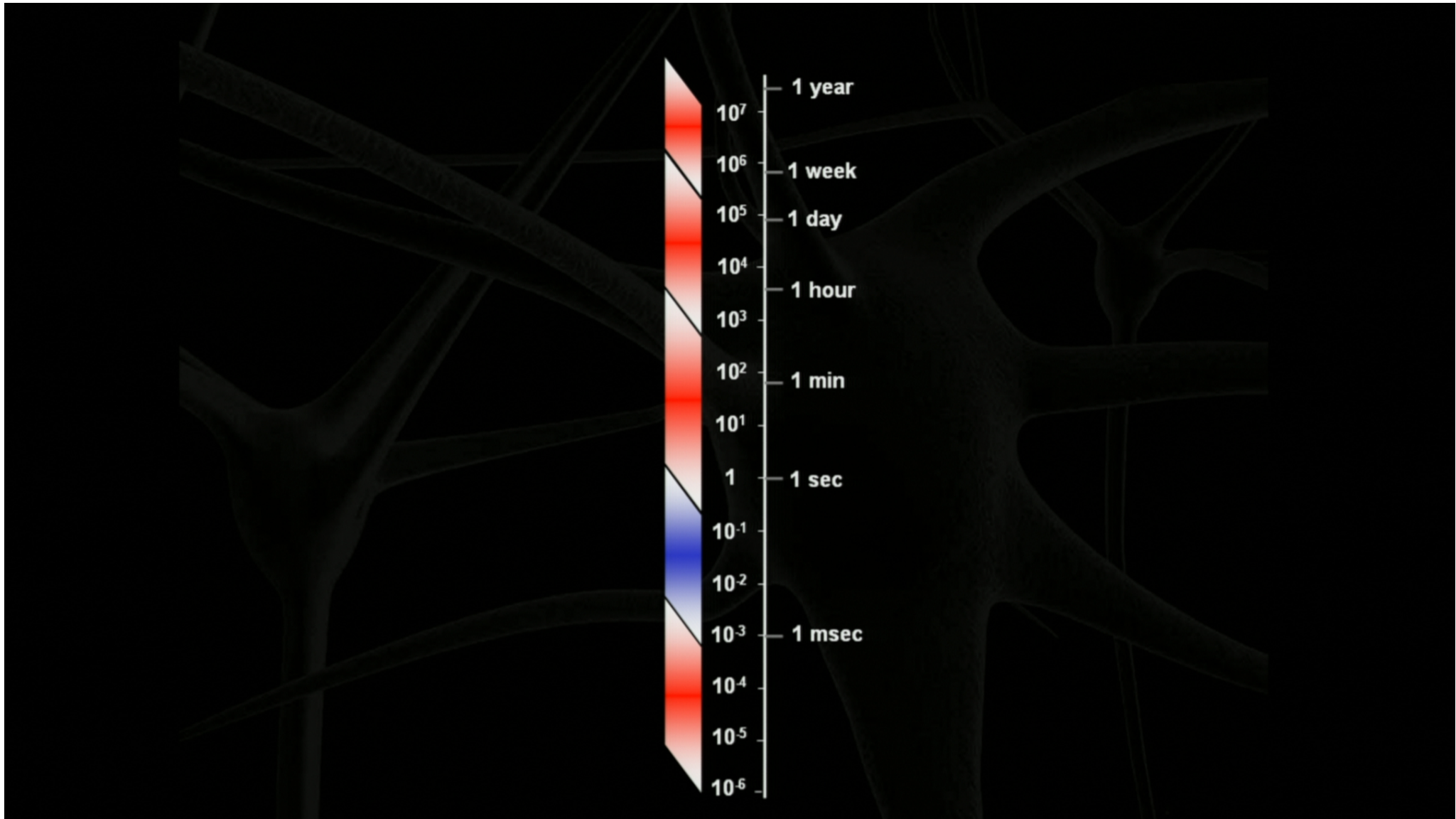
**Saint Augustine (397)**

**“Time is an Illusion, lunchtime doubly so”**

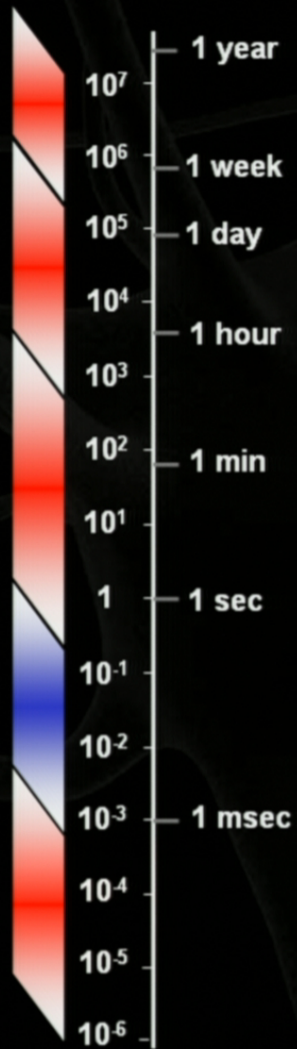
**Douglas Adams (1979)**

**“Maybe it is just as well if we face the fact that time is one of the things we probably cannot define ... What really matters anyways is not how we define time, but how we measure it.”**

**Richard Feynman (1963)**



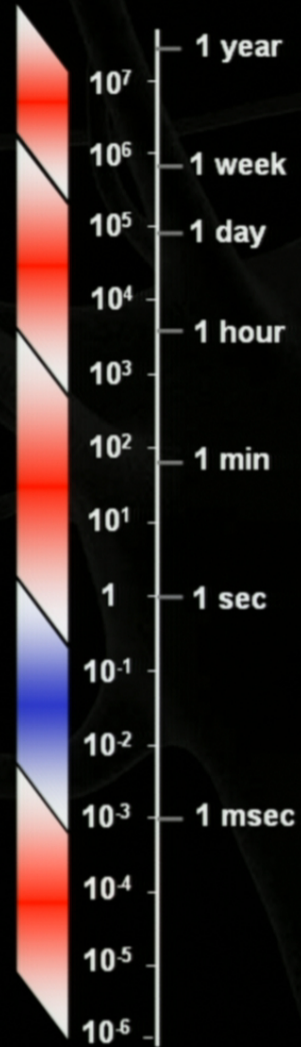
**Microsecond Processing  
Sound Localization**





Time Perception  
Speech Recognition  
Music Perception  
Motor Coordination

Microsecond Processing  
Sound Localization

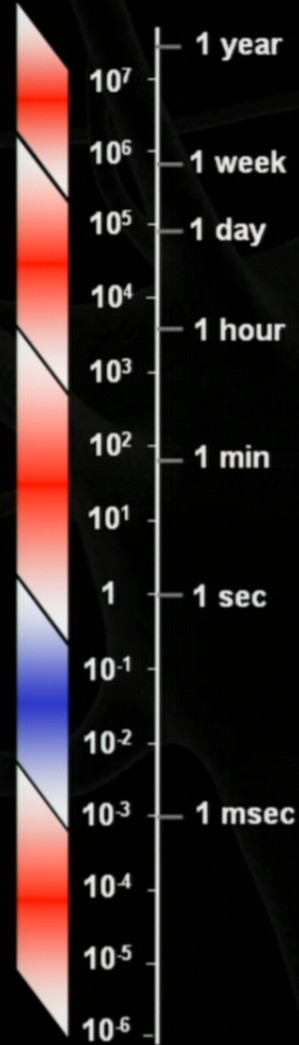


Circadian Rhythms  
Sleep-Wake Cycles  
Feeding Rhythms

Time Estimation  
Subjective Time  
Anticipatory Responses  
Interval Timing

Time Perception  
Speech Recognition  
Music Perception  
Motor Coordination

Microsecond Processing  
Sound Localization

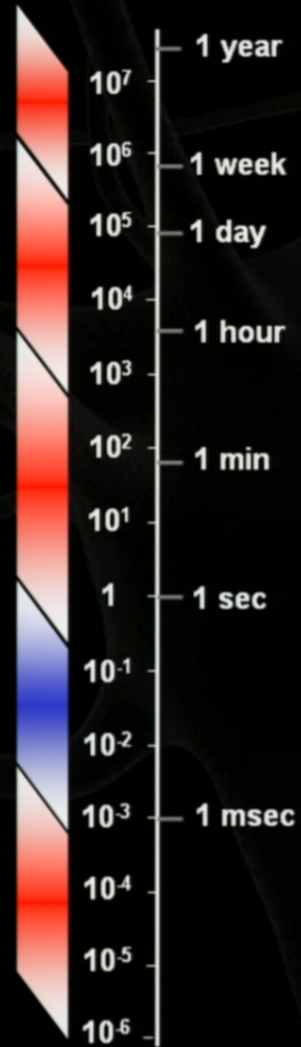


**Circadian Rhythms**  
**Sleep-Wake Cycles**  
**Feeding Rhythms**

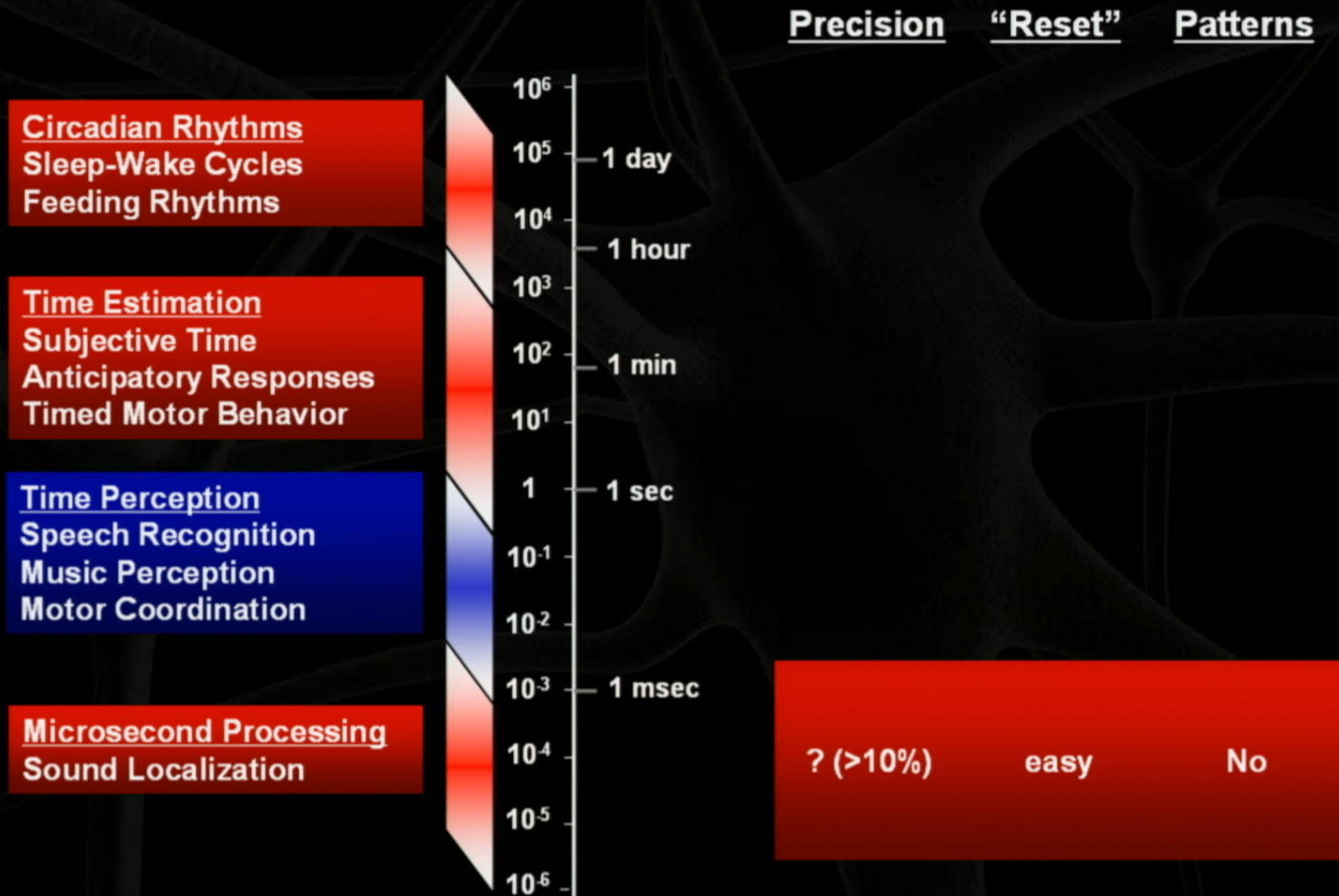
**Time Estimation**  
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**Anticipatory Responses**  
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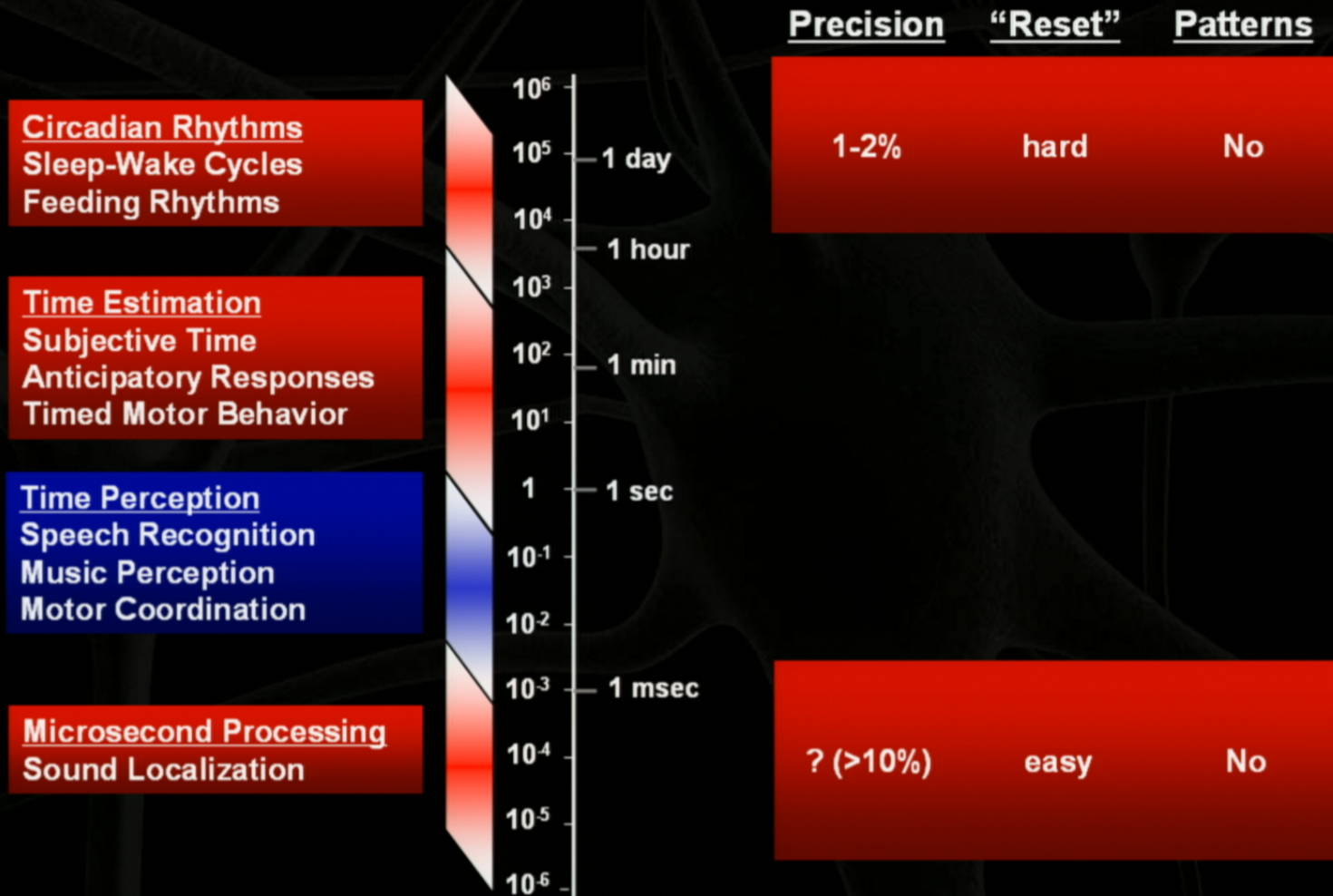
**Microsecond Processing**  
**Sound Localization**



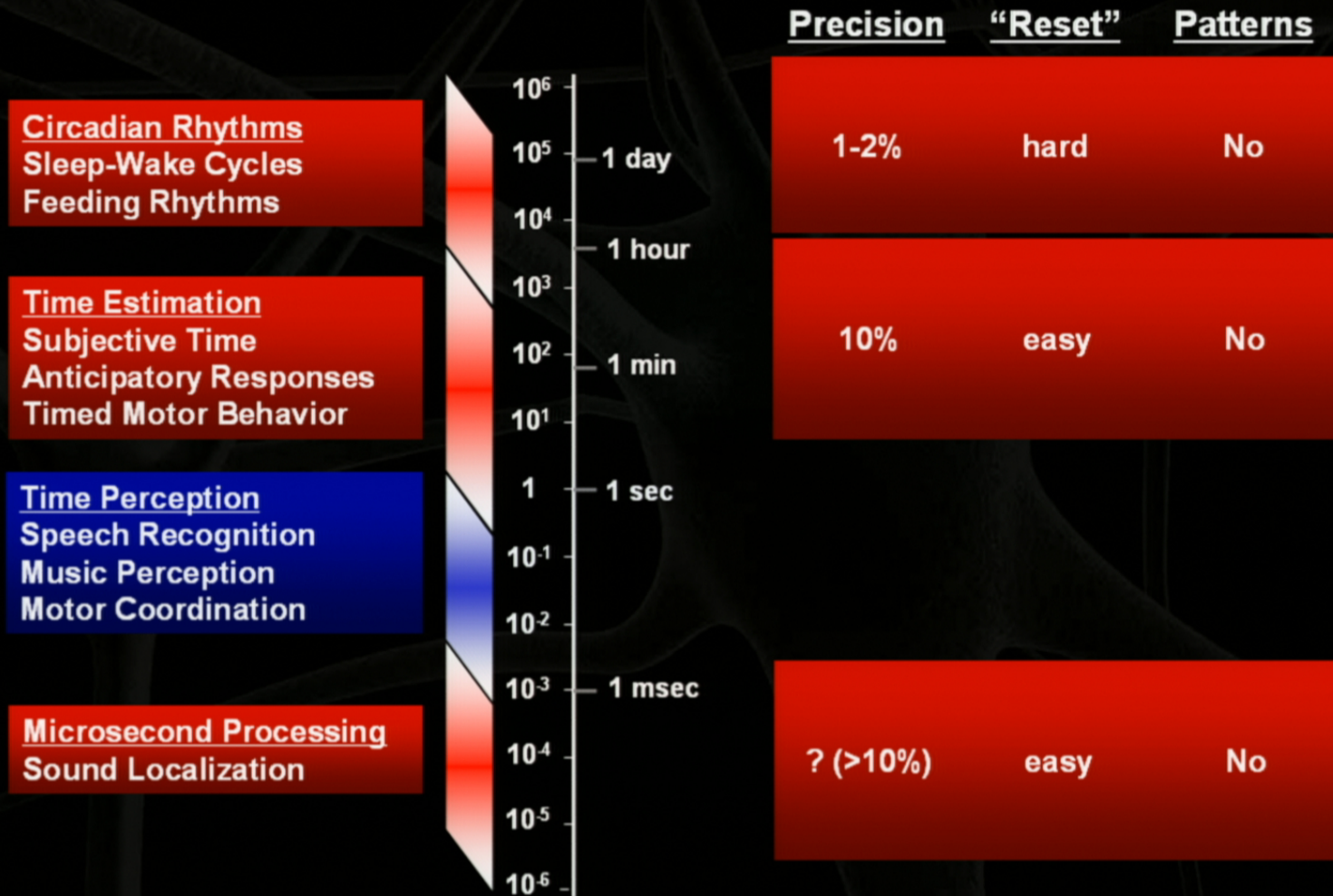
# Different Timing Problems have Different Requirements



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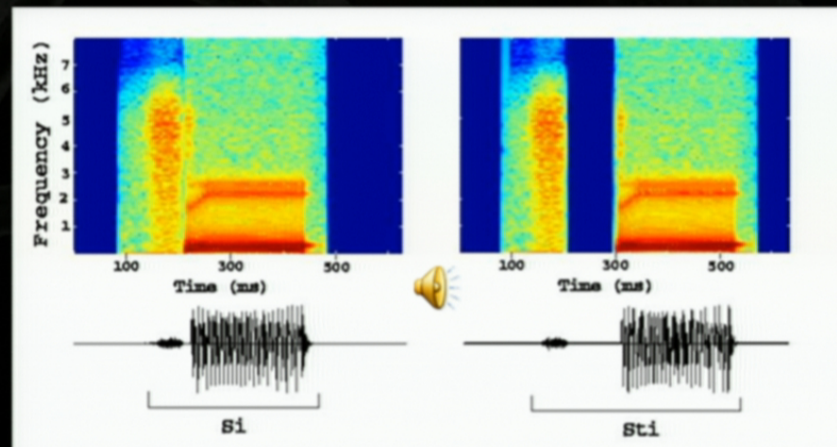


# Timing in Speech and Language

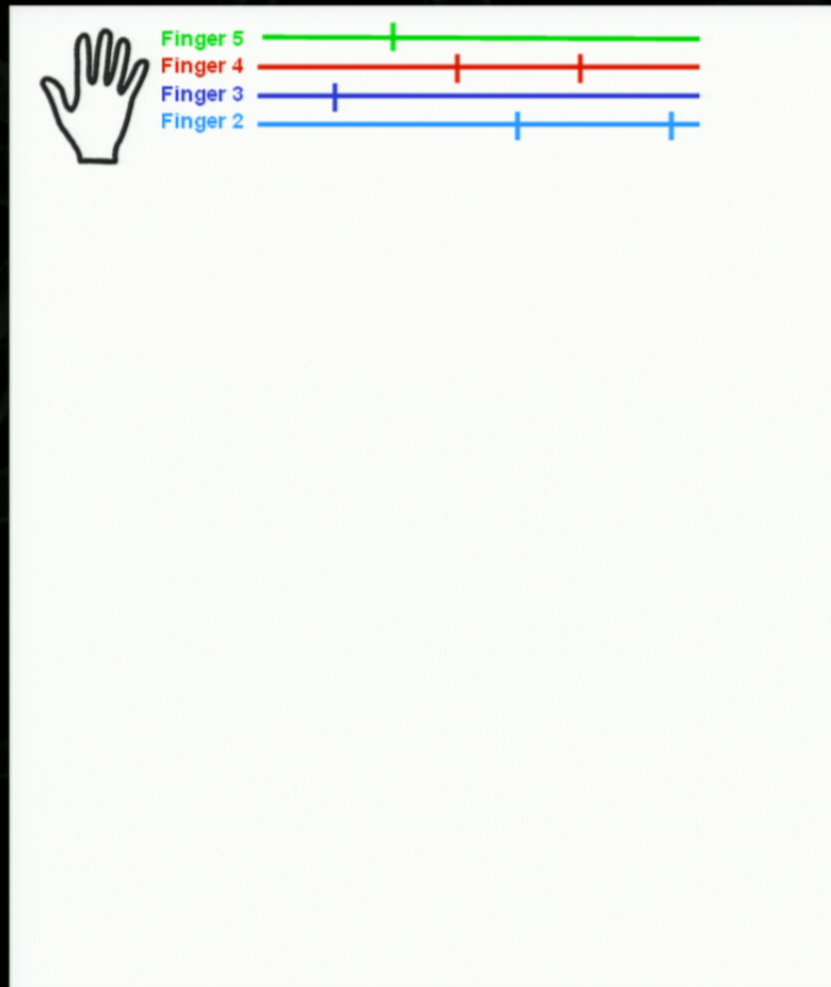
“He gave her cat food”

X

“He gave her cat food”



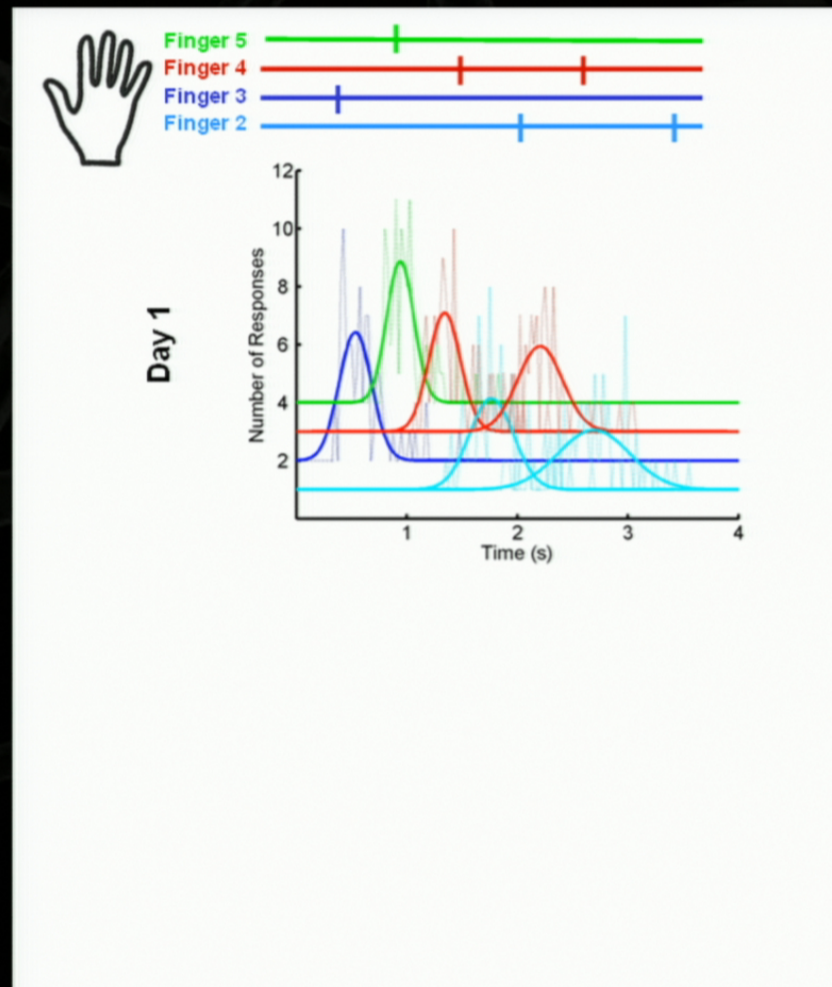
# Motor Timing: Production of Complex Temporal Patterns



Laje, Cheng, Buonomano, 2011  
(Front Integr Neurosci)

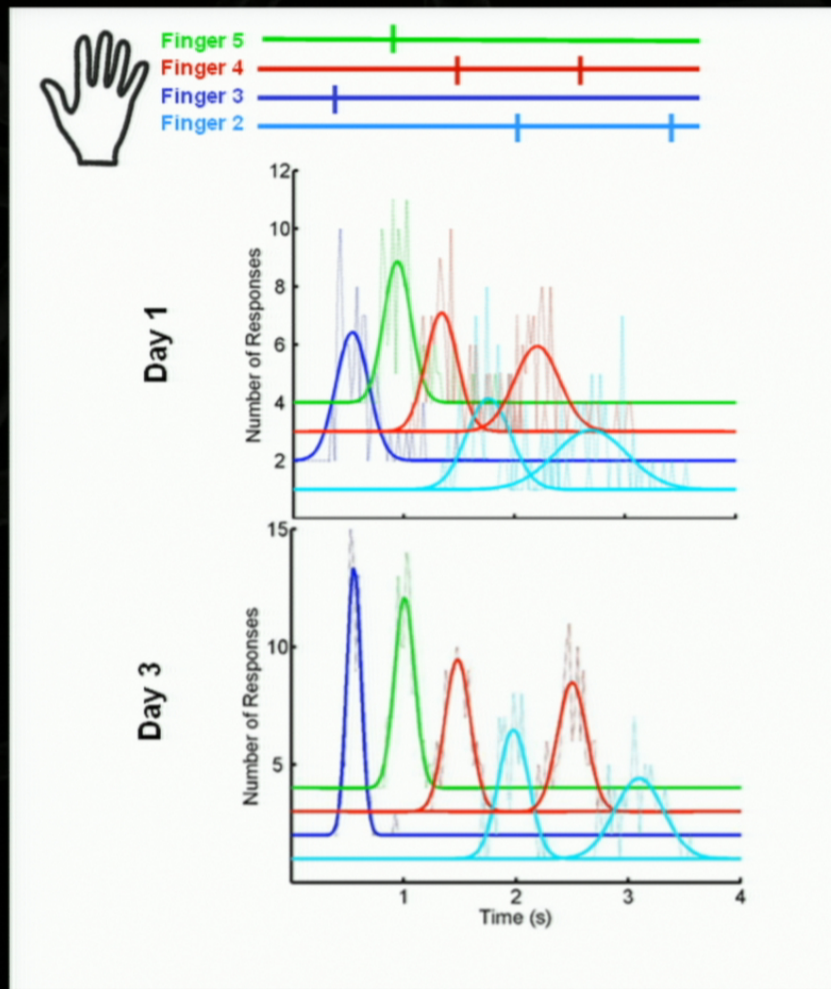


# Motor Timing: Production of Complex Temporal Patterns



Laje, Cheng, Buonomano, 2011  
(Front Intergr Neurosci)

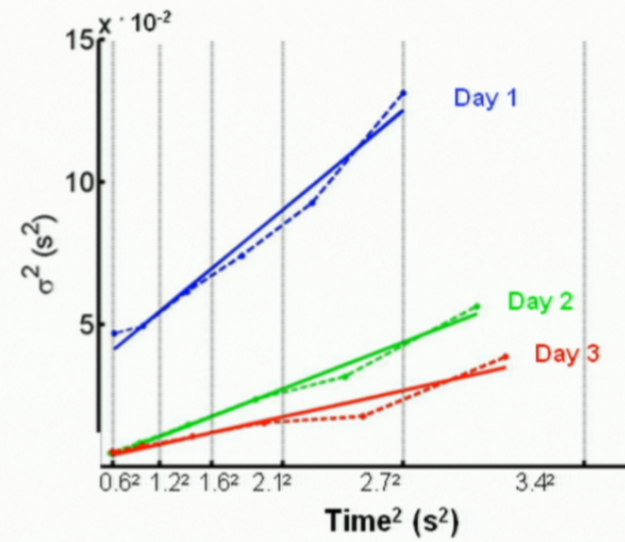
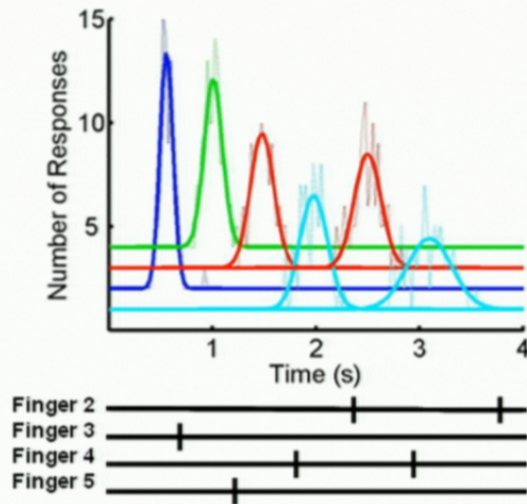
# Motor Timing: Production of Complex Temporal Patterns



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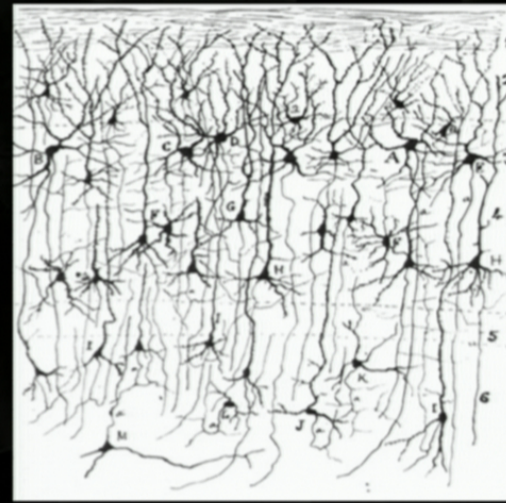
# Signature of the Brain's Clocks: Weber's Law ( $\sigma^2 \uparrow$ linearly with $t^2$ )

$$\sigma^2 = k T^2 + \sigma_{\text{indep}}^2 \quad (\text{Generalized Weber's law})$$

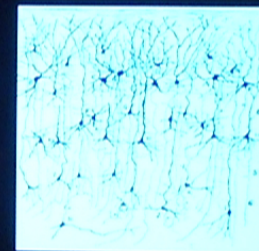


Laje et al, 2011 (Front Integr Neurosci)

# *How do we build a time keeping device with neurons?*



*How do we build a time keeping device with neurons?*



# Random Recurrent Neural Networks

VOLUME 61, NUMBER 3

PHYSICAL REVIEW LETTERS

18 JULY 1988

## Chaos in Random Neural Networks

H. Sompolinsky<sup>(a)</sup> and A. Crisanti

*AT&T Bell Laboratories, Murray Hill, New Jersey 07974, and  
Racah Institute of Physics, The Hebrew University, 91904 Jerusalem, Israel<sup>(b)</sup>*

and

H. J. Sommers<sup>(a)</sup>

*Fachbereich Physik, Universität-Gesamthochschule Essen, D-4300 Essen, Federal Republic of Germany*

(Received 30 March 1988)

REPORTS

2 APRIL 2004 VOL 304 SCIENCE [www.sciencemag.org](http://www.sciencemag.org)

## Harnessing Nonlinearity: Predicting Chaotic Systems and Saving Energy in Wireless Communication

Herbert Jaeger<sup>\*</sup> and Harald Haas

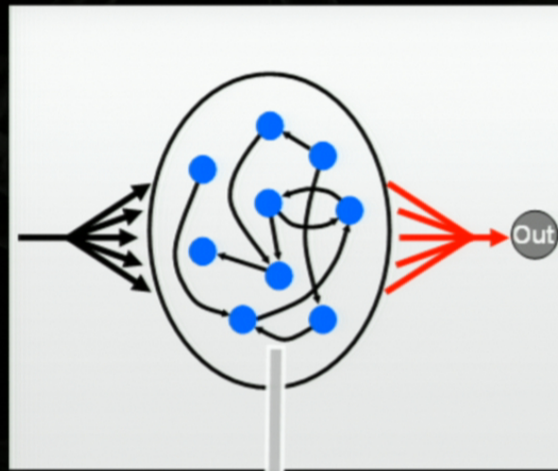
## Generating Coherent Patterns of Activity from Chaotic Neural Networks

David Sussillo<sup>1,\*</sup> and L.F. Abbott<sup>1,\*</sup>

<sup>1</sup>Department of Neuroscience, Department of Physiology and Cellular Biophysics, Columbia University College of Physicians and Surgeons,  
New York, NY 10032-2695, USA

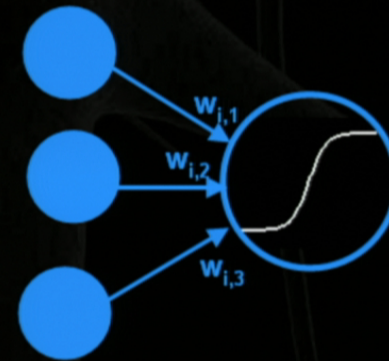
Neuron 63, 544–557, August 27, 2009 ©2009 Elsevier Inc.

# Firing-Rate Models of Recurrent Neural Networks



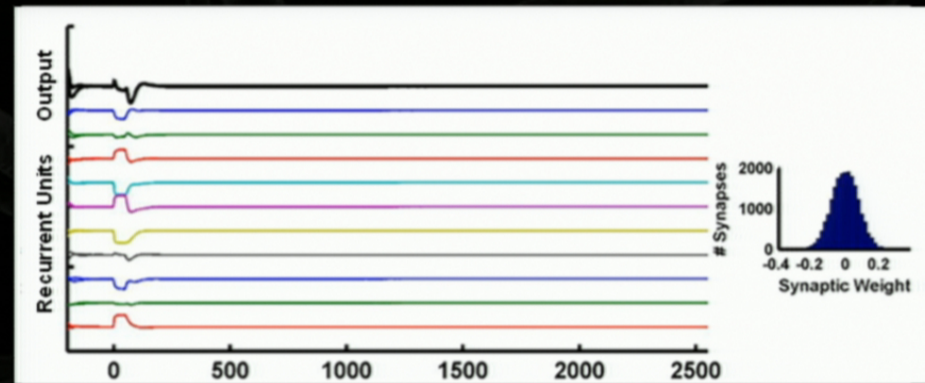
$$\text{Out} = \sum_j^N W_{ij}^{\text{Out}} v_j$$

$$\tau \frac{dv_i}{dt} = -v_i + \sum_j^N W_{i,j}^{\text{Rec}} \tanh(v_j) + \sum_j^N W_{i,j}^{\text{In}} v_j + I_{\text{noise}}$$

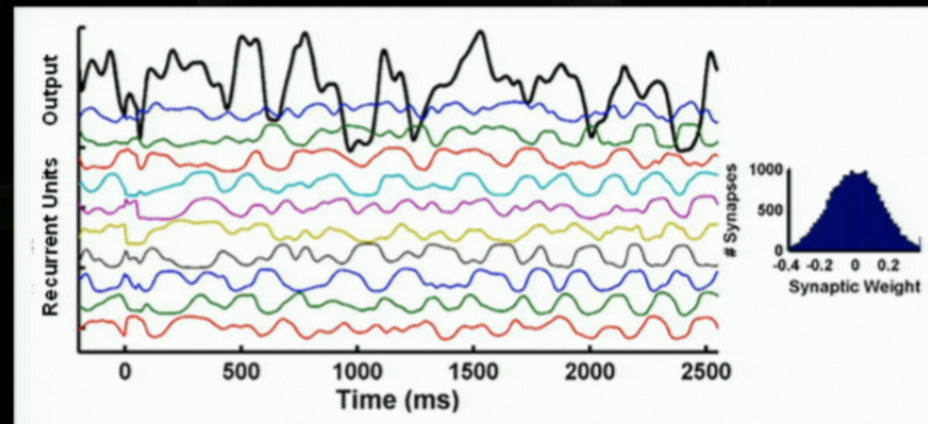


# Dynamic Regimes within Random Recurrent Networks

“Low Gain”



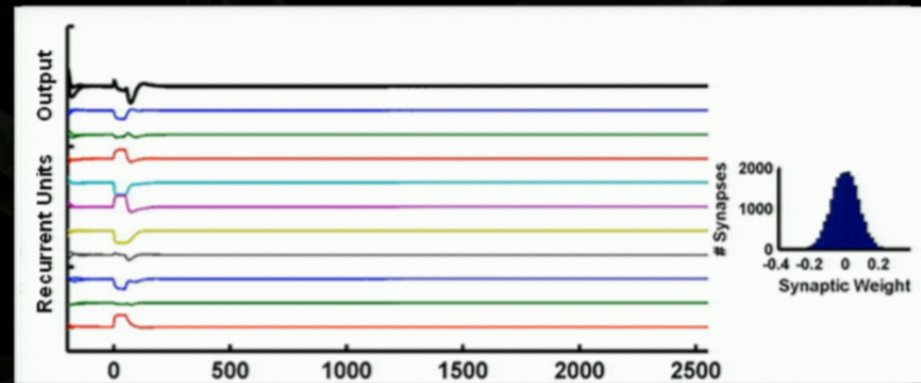
“High Gain”



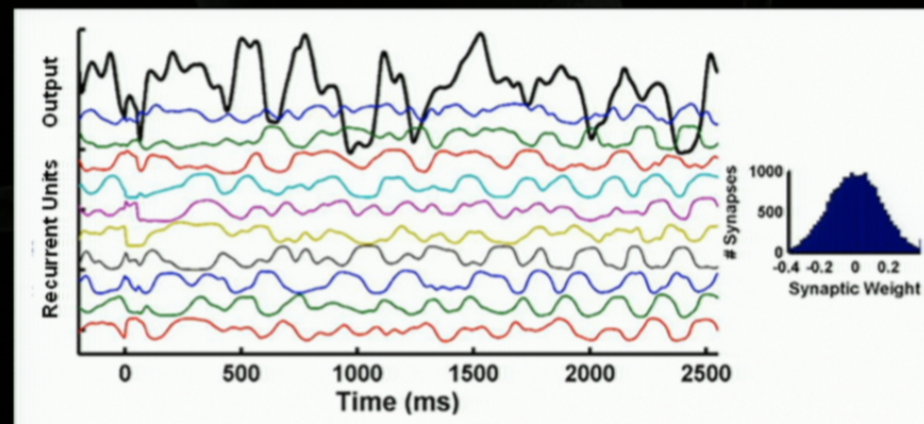


# Dynamic Regimes within Random Recurrent Networks

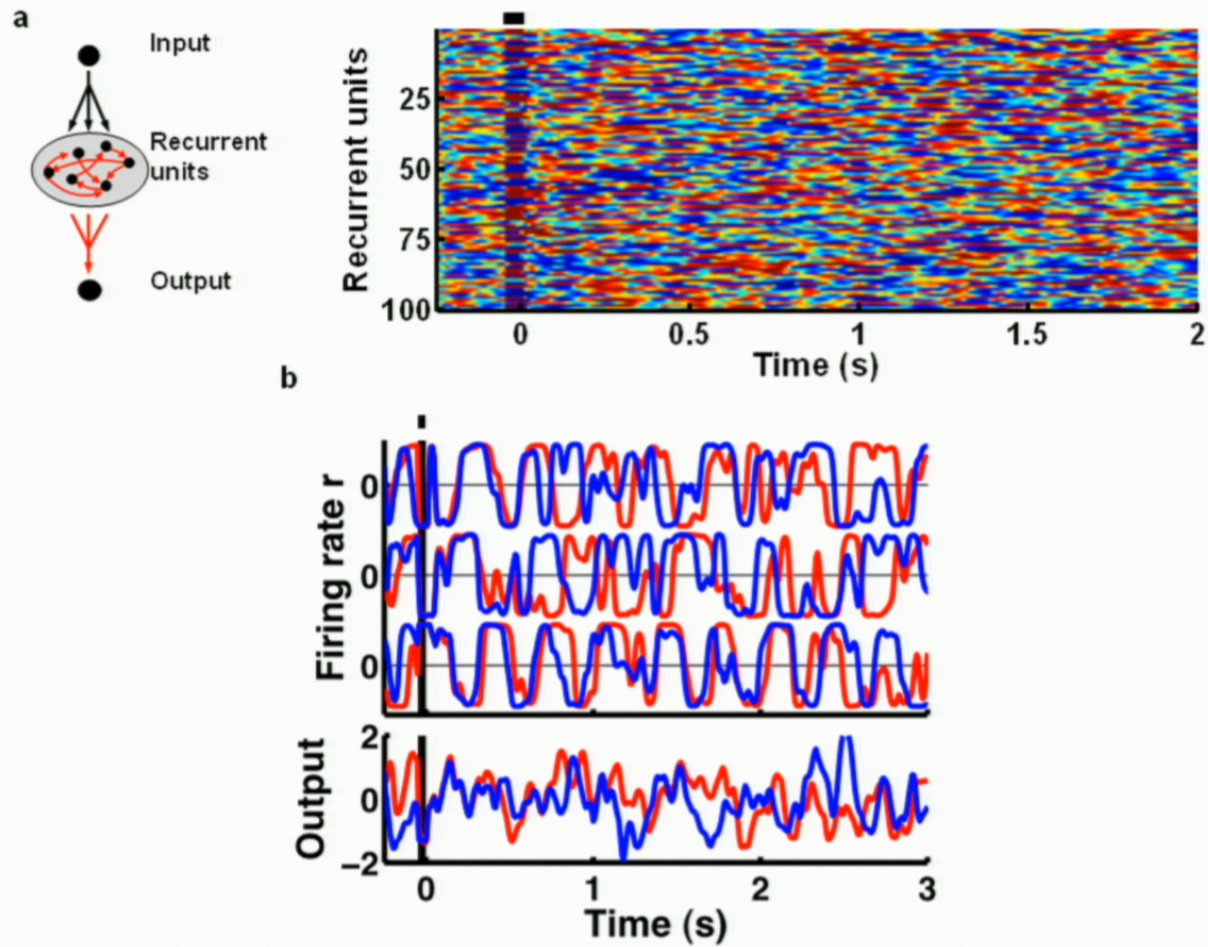
“Low Gain”



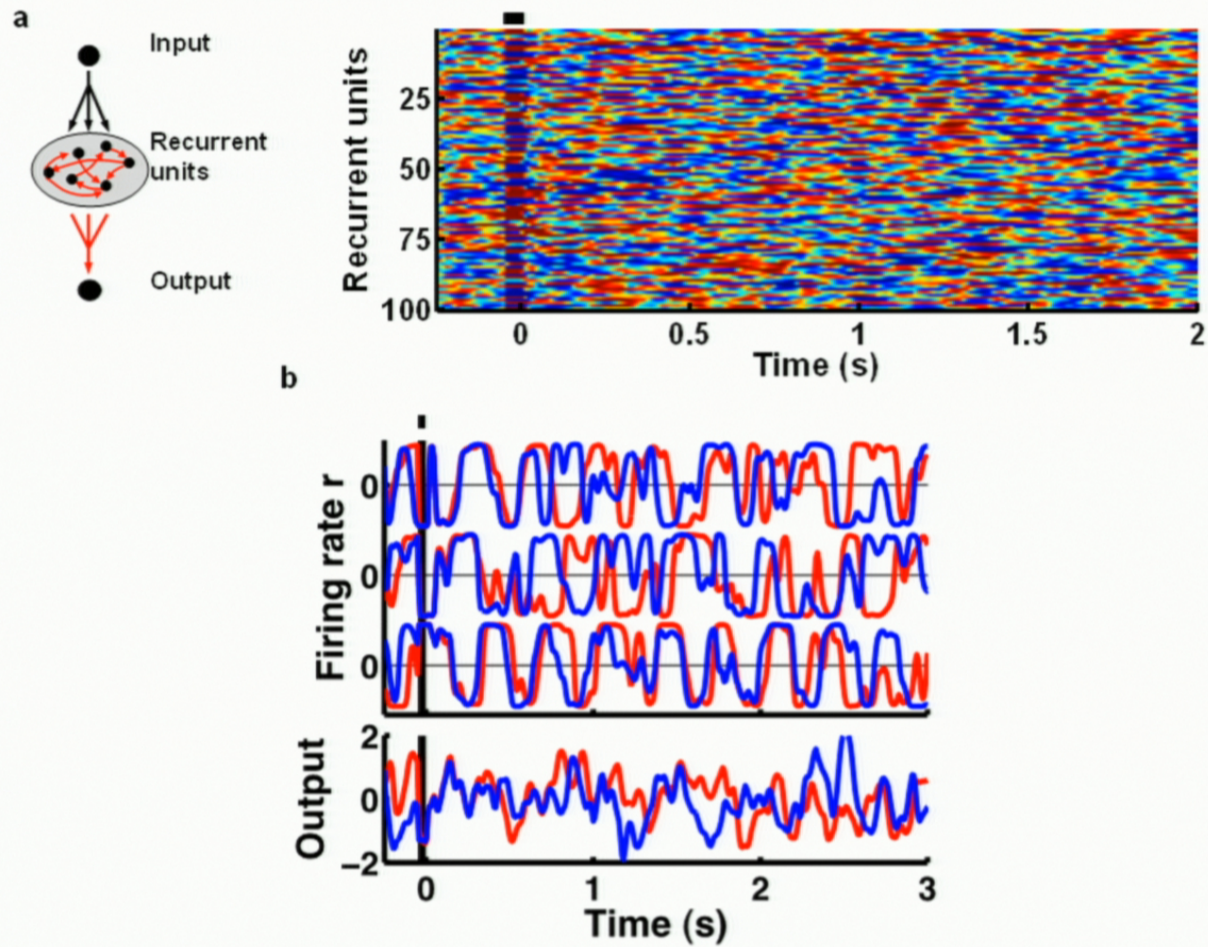
“High Gain”



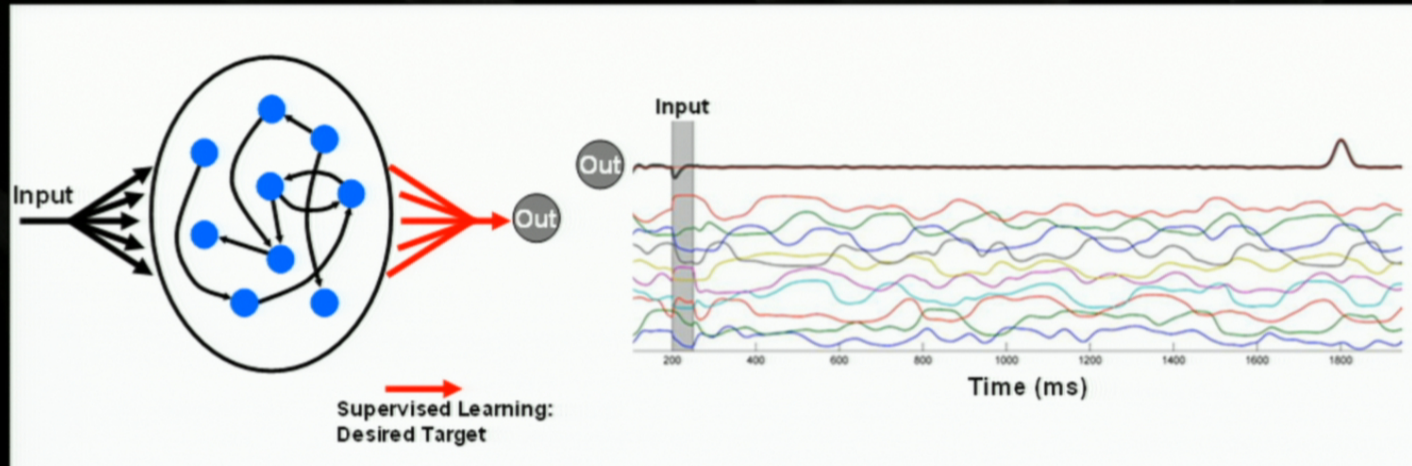
# High Gain Regimes are Chaotic



# High Gain Regimes are Chaotic



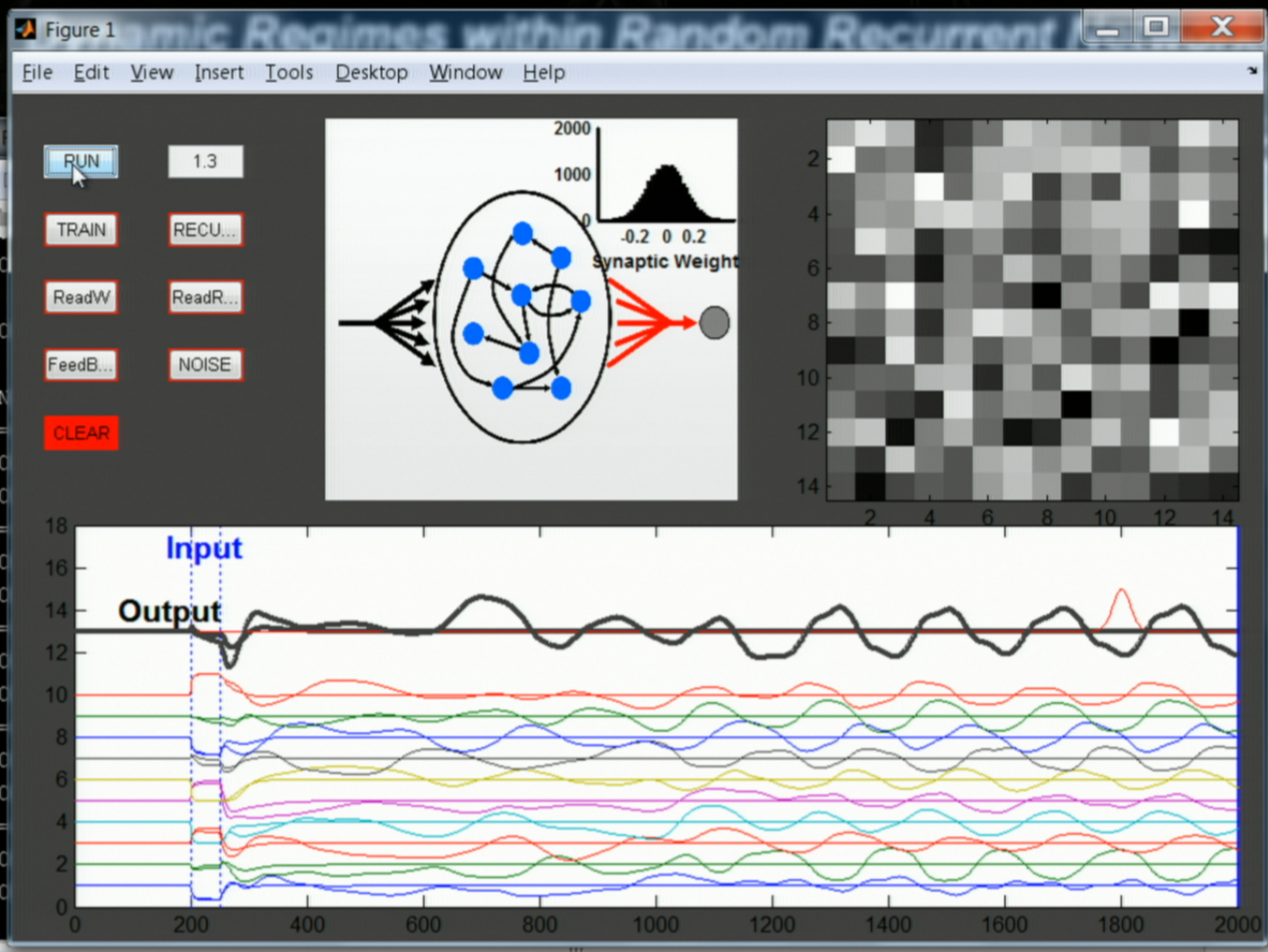
# The High Gain Regime has High Computational "Potential" (e.g., telling time)



## Dynamic Regimes within Random Recurrent Networks

```
MATLAB R2011b
File Edit Debug Format Desktop Window Help
Current Folder: c:\matlab\bin\demo
t= 7200
t= 7300
t= 7400
t= 7500
t= 7600
t= 7700
t= 7800
t= 7900
t= 8000
t= 8100
RUN=0
t= 8200
>> cc
>> RRN_Talk
LOOP = 1
t= 1000
t= 2000
LOOP = 1
t= 1000
t= 2000
>>
```





```

MATLAB
File Edit
t= 810
RUN=0
t= 820
>> cc
>> RRN
LOOP =
t= 100
t= 200
LOOP =
t= 100
t= 200
LOOP =
t= 100
t= 200
LOOP =
t= 100
t= 200
LOOP =
t= 100
t= 200
fx >>

```

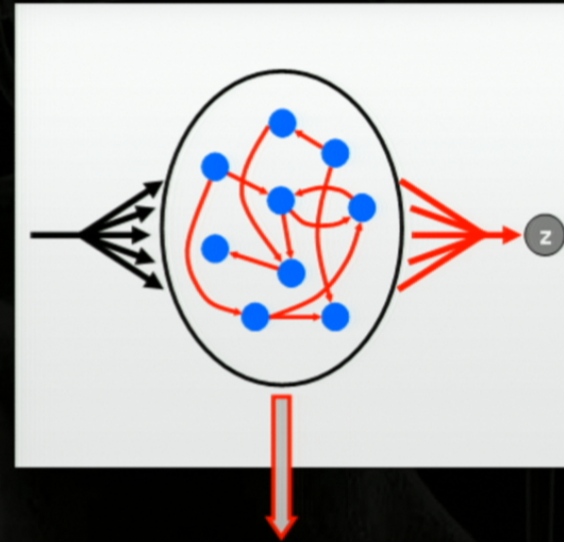
Windows taskbar showing icons for Start, Internet Explorer, Firefox, Word, and other applications. The system clock displays 11:22 AM, Wednesday, 1/29/2014.

## **Tuning Recurrent Connections Through “Innate Training”**

- 1. Traditional supervised learning rules require a target pattern in order to calculate the error (used to adjust the weights)  
But what is the target pattern of the recurrent network?**
- 2. In the current framework (SDN / reservoir computing) it does not matter what the network does! As long as the pattern is high-dimensional and reproducible.**
- 3. Innate training trains the network to do what it can already do by picking an “innate” pattern as the target.**

# Tuning Recurrent Connections Through “Innate Training”

Train the network to do what it can already to by picking an “innate” pattern as the target.



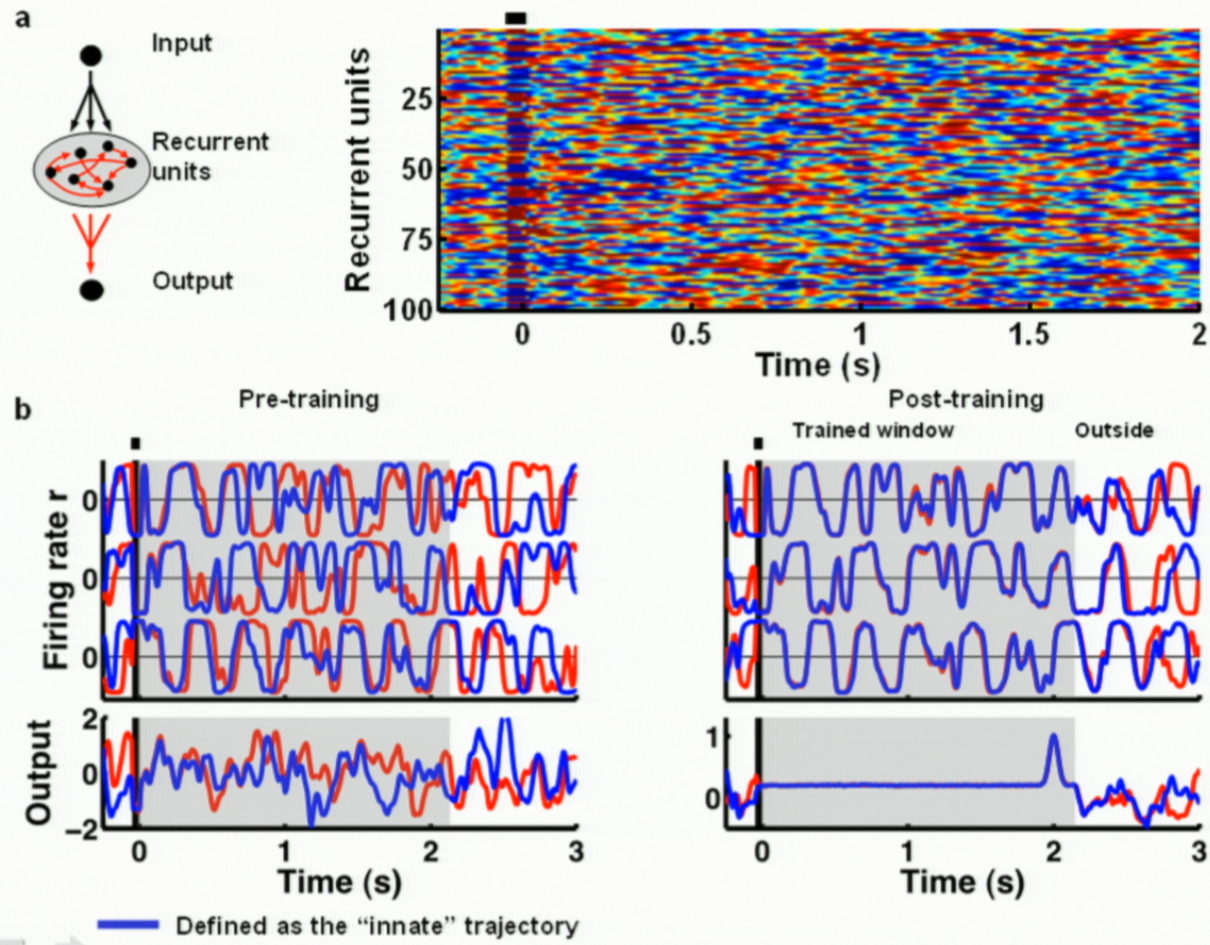
Supervised Learning:  
“Continuous” RLS (FORCE)

$$w_{ij} = w_{ij}(t - \Delta t) + \text{error}_i(t) \sum_k^{\text{Pre}} P_{j,k}(t) r_k(t)$$

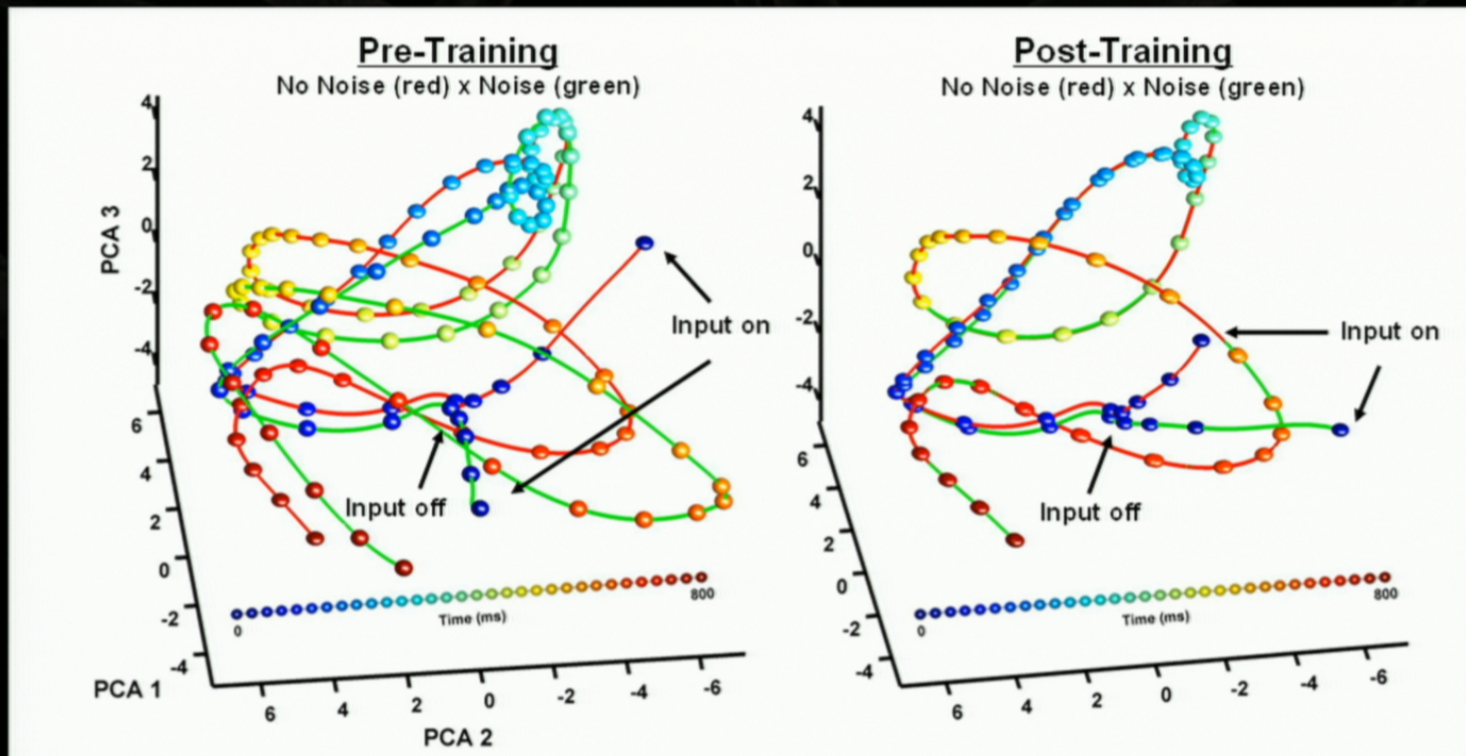
P = running inverse correlation of  
vector r (presynaptic elements)



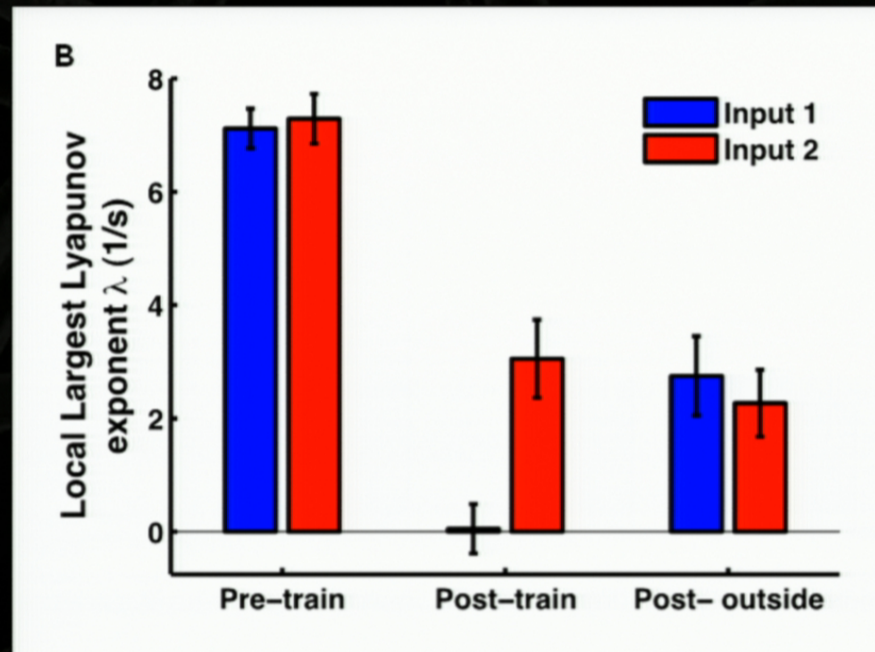
# Trained Trajectories are Locally Stable



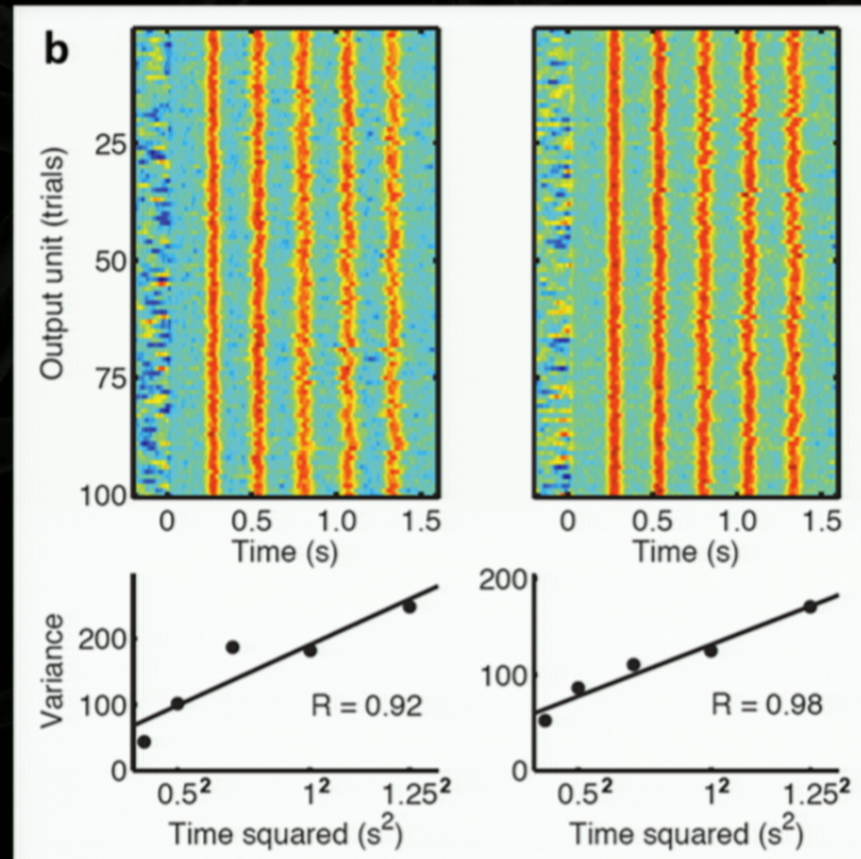
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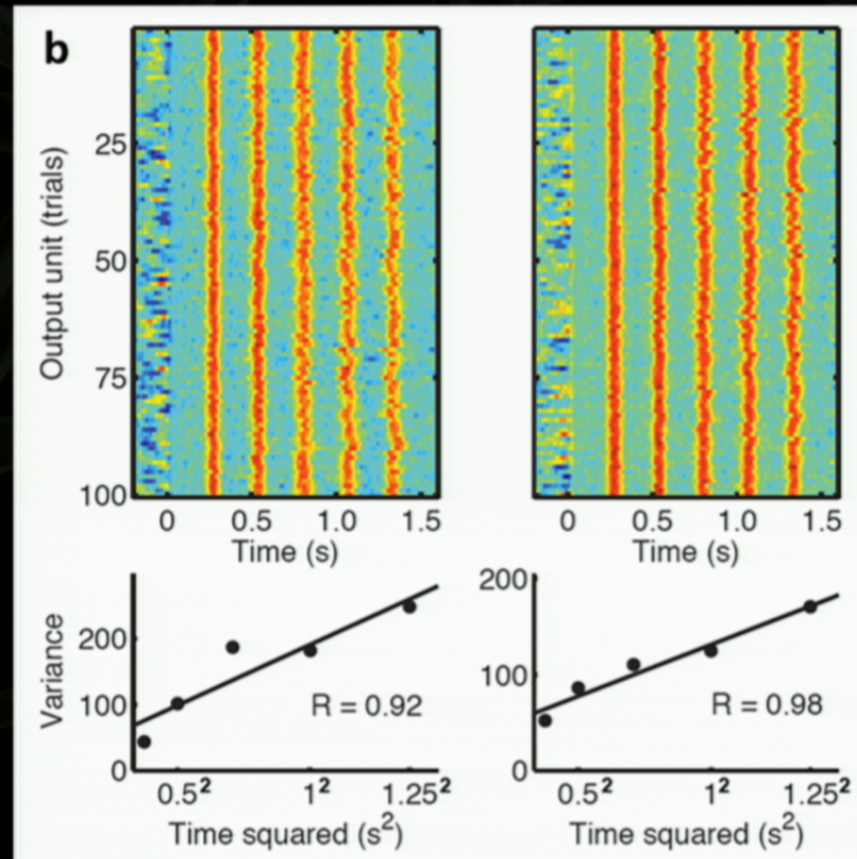


# Stable Trajectories can Account for the Experimentally Observed Variance Signature (Weber's Law)



Laje, Buonomano, 2013 (Nat. Neurosci.)

# Stable Trajectories can Account for the Experimentally Observed Variance Signature (Weber's Law)

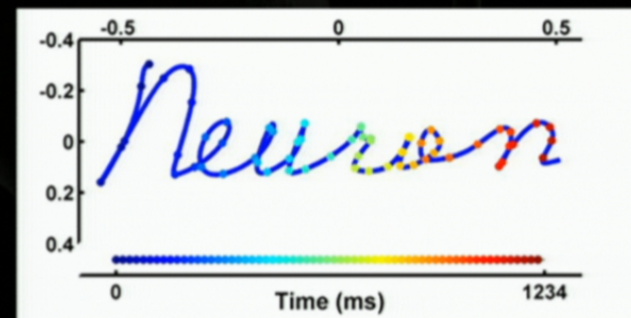
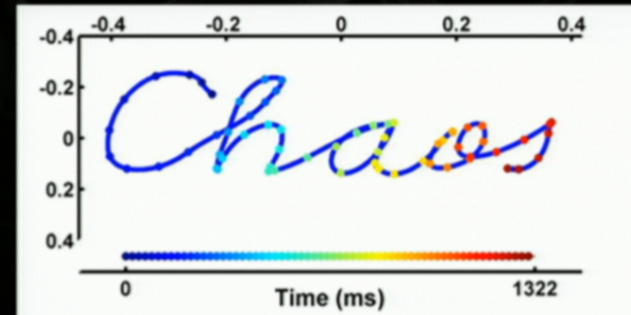
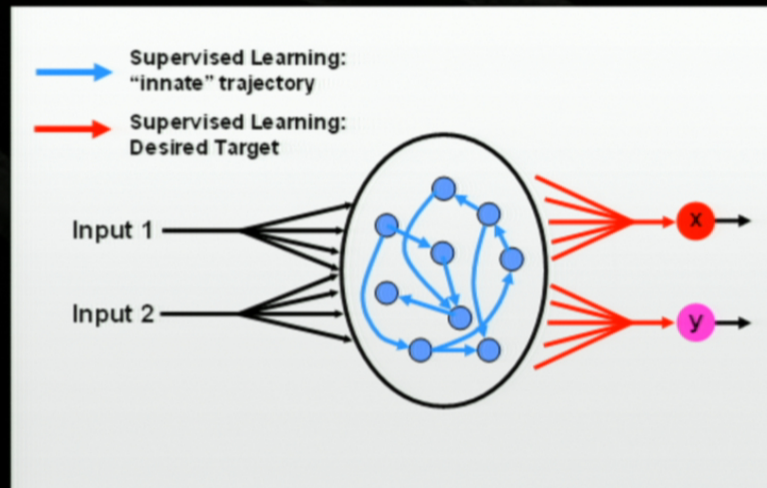


Laje, Buonomano, 2013 (Nat. Neurosci.)

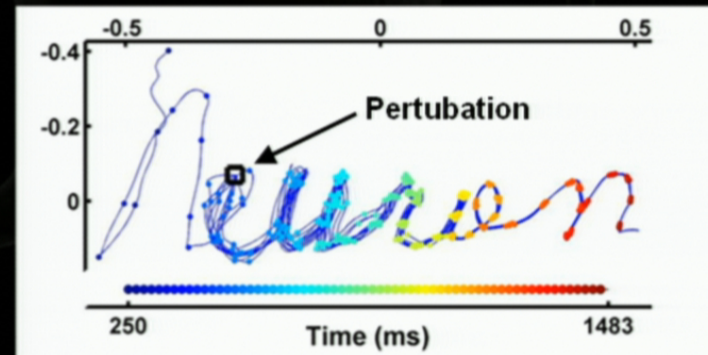
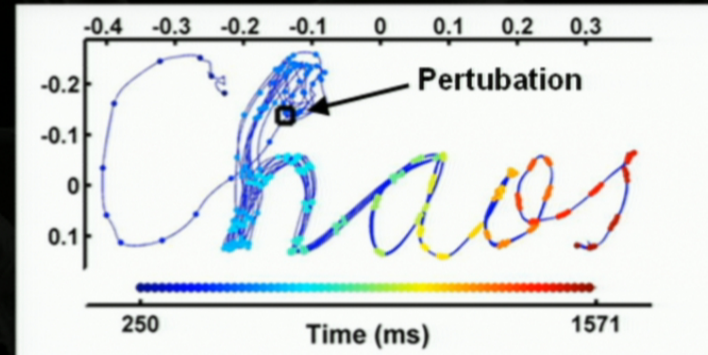
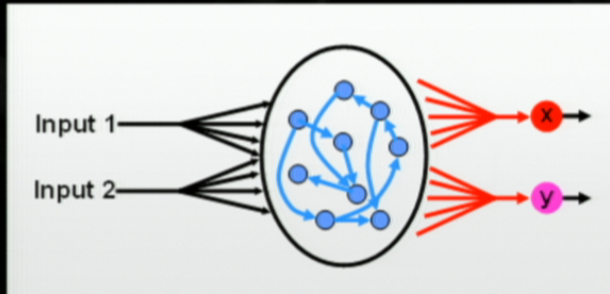
# Using Stable Transient Dynamics to Generate Motor Patterns



# Complex Spatiotemporal Patterns: Handwriting



# Dynamic Attractor: Return to the Trajectory after Perturbation





Using S

DAC\_Handwriting\_Demo

RUN

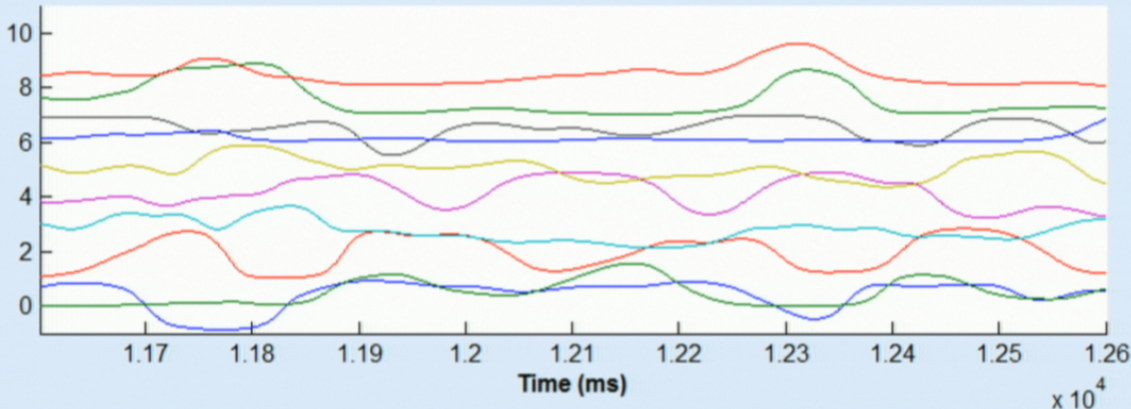
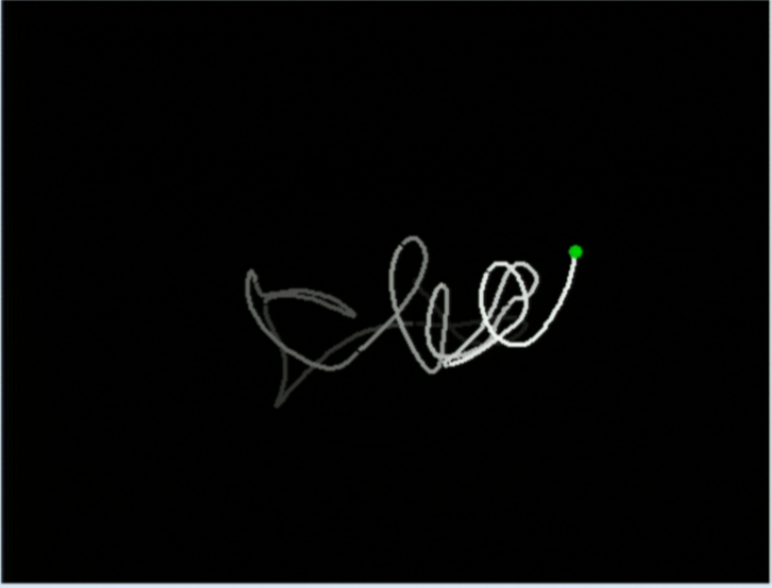
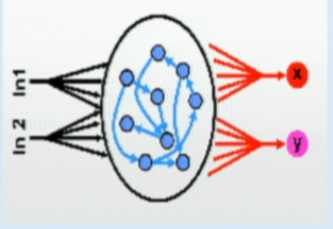
Input1

Input2

Perturb

Noise=0

Pause=0



erns

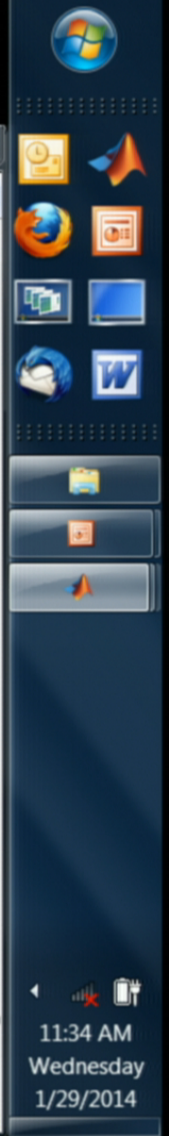
MATLAB R2011b

File Edit Debug Parallel

```
t=10700
t=10800
t=10900
t=11000
t=11100
t=11200
t=11300
t=11400
t=11500
t=11600
t=11700
t=11800
t=11900
t=12000
t=12100
t=12200
t=12300
t=12400
t=12500
t=12600
```

fx >>

Start



11:34 AM  
Wednesday  
1/29/2014

OVR

Using S

DAC\_Handwriting\_Demo

erns

MATLAB R2011b

File Edit Debug Parallel

File Edit Debug Parallel

```
t=37800
t=37900
t=38000
t=38100
t=38200
t=38300
t=38400
t=38500
t=38600
t=38700
t=38800
t=38900
t=39000
t=39100
t=39200
t=39300
t=39400
t=39500
t=39600
t=39700
```

fx >>

Start

RUN

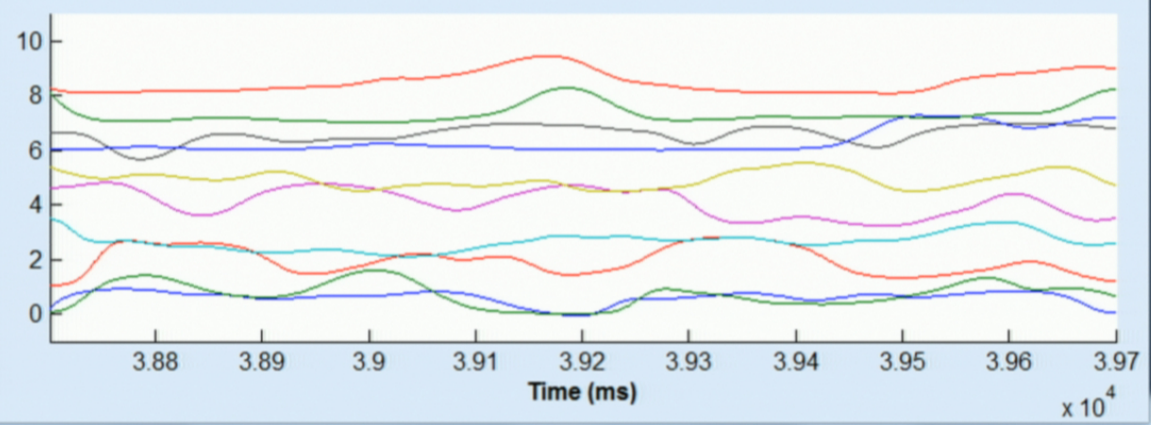
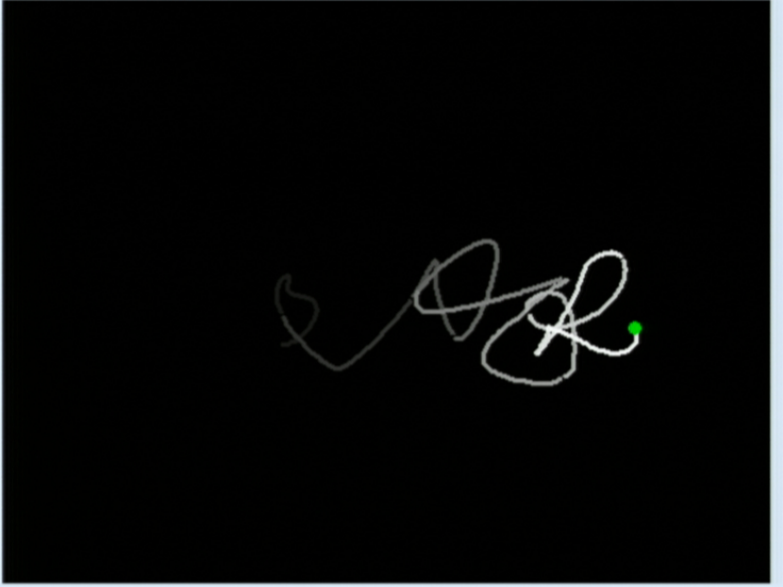
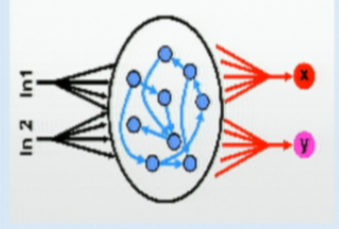
Input1

Input2

Perturb

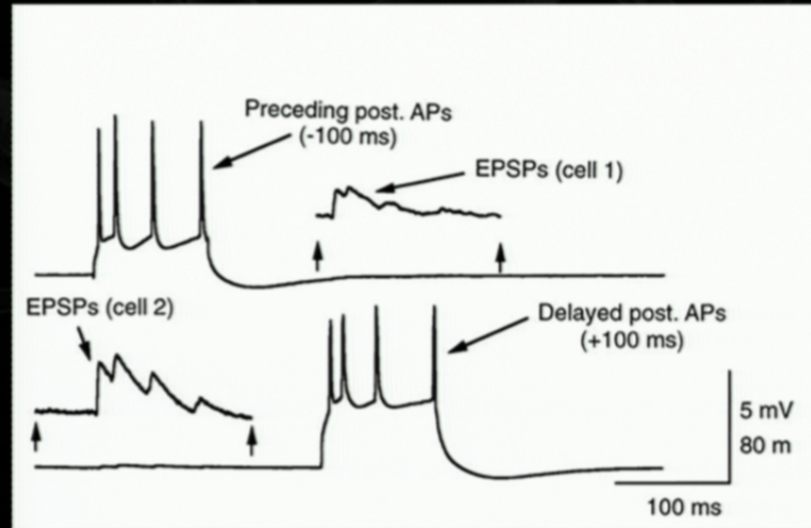
Noise = 0.0100

Pause=0

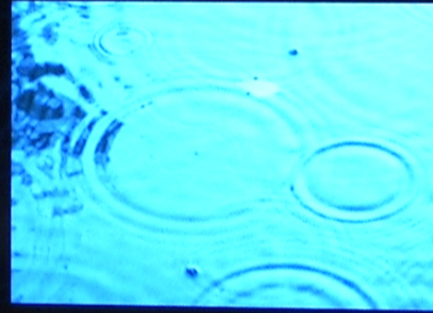


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Wednesday  
1/29/2014

# Real Neural Networks are Much More Complicated



State-Dependent Networks / Liquid-State Machines



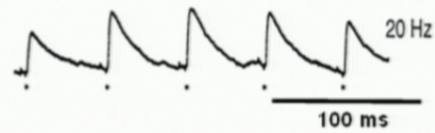
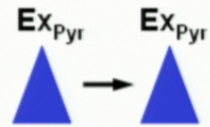
**PI**  
PERIMETER  
INSTITUTE  
FOR THEORETICAL PHYSICS

## ***State-Dependent Networks / Liquid-State Machines***

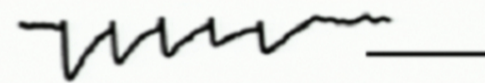
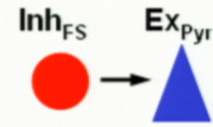
- 1. In the sensory domain temporal computations arise from the interaction between the internal state of neural networks and incoming stimuli. The state of a network is defined both by its “active” and “hidden” state.**
- 2. The inherent complexity and size of recurrent neural networks ensures that virtually any stimulus set is represented in high-dimensional space—which facilitates the decoding (e.g., support vector machines)**

Buonomano & Maass, 2009 (Nat. Neuroscience)

# Short-term Synaptic Plasticity



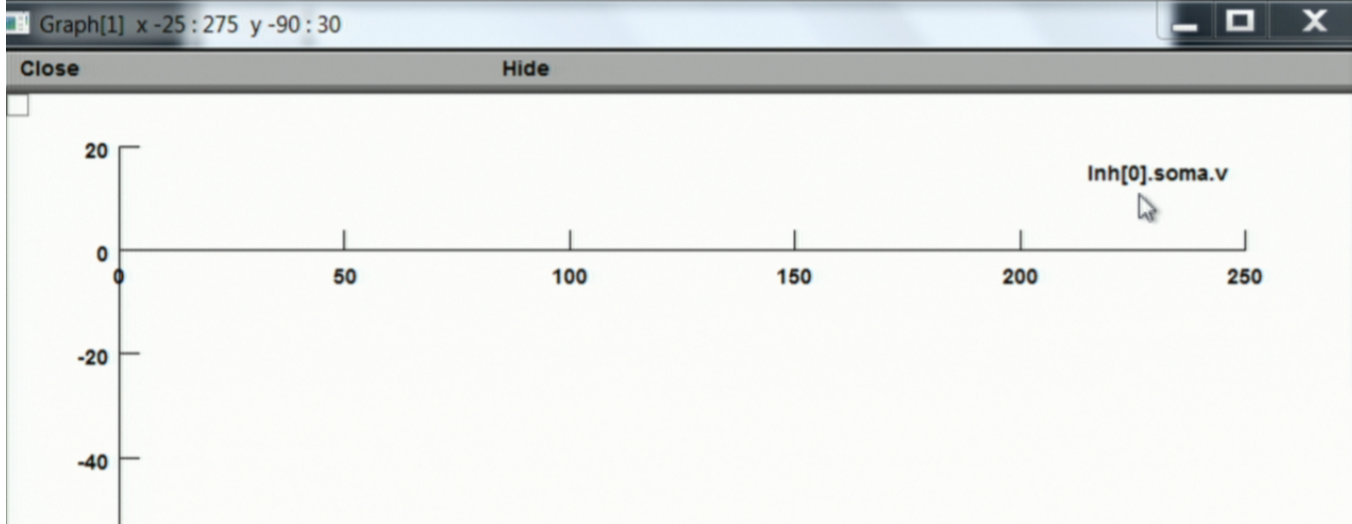
Reyes & Sakmann, 1999



Reyes, 2011



Ma, Hu, Agmon, 2012



Common\_Parameters

Close Hide

RUN

Synaptic Weights

sExEx[ExINPUT][0].gmaxAMPA 0.015

sExInh[0][0].gmaxAMPA 0.0025

slnhEx[ExINPUT][0].gmaxGABA 0.1

Short-term Plasticity

U\_EPlasSom(Ex->Ex) 0.2

trec\_EPlasSom(Ex->Ex) (ms) 10

tfac\_EPlasSom(Ex->Ex) (ms) 400

U\_EtolPlasSom(Ex->Inh) 0.2

trec\_EtolPlasSom(Ex->Inh) (ms) 10

tfac\_EtolPlasSom(Ex->Inh) (ms) 100

U\_(Inh->Ex) 0.25

trec(Inh->Ex) (ms) 700

tfac\_(Inh->Ex) (ms) 20

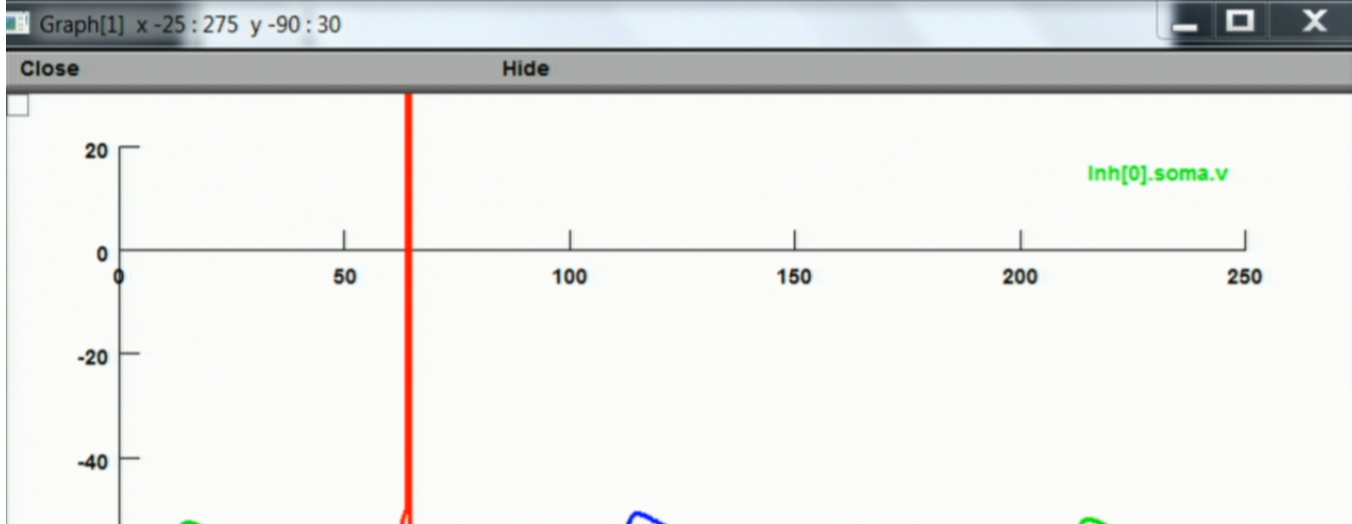
50 ms

100 ms

200 ms

quit

11:43 AM  
Wednesday  
1/29/2014



Common\_Parameters

Close Hide

RUN

Synaptic Weights

sExEx[ExINPUT][0].gmaxAMPA 0.014

sExInh[0][0].gmaxAMPA 0.0023

slnhEx[ExINPUT][0].gmaxGABA 0.1

Short-term Plasticity

U\_EPlasSom(Ex->Ex) 0.2

trec\_EPlasSom(Ex->Ex) (ms) 10

tfac\_EPlasSom(Ex->Ex) (ms) 400

U\_EtolPlasSom(Ex->Inh) 0.2

trec\_EtolPlasSom(Ex->Inh) (ms) 10

tfac\_EtolPlasSom(Ex->Inh) (ms) 100

U\_(Inh->Ex) 0.25

trec(Inh->Ex) (ms) 700

tfac\_(Inh->Ex) (ms) 20

50 ms

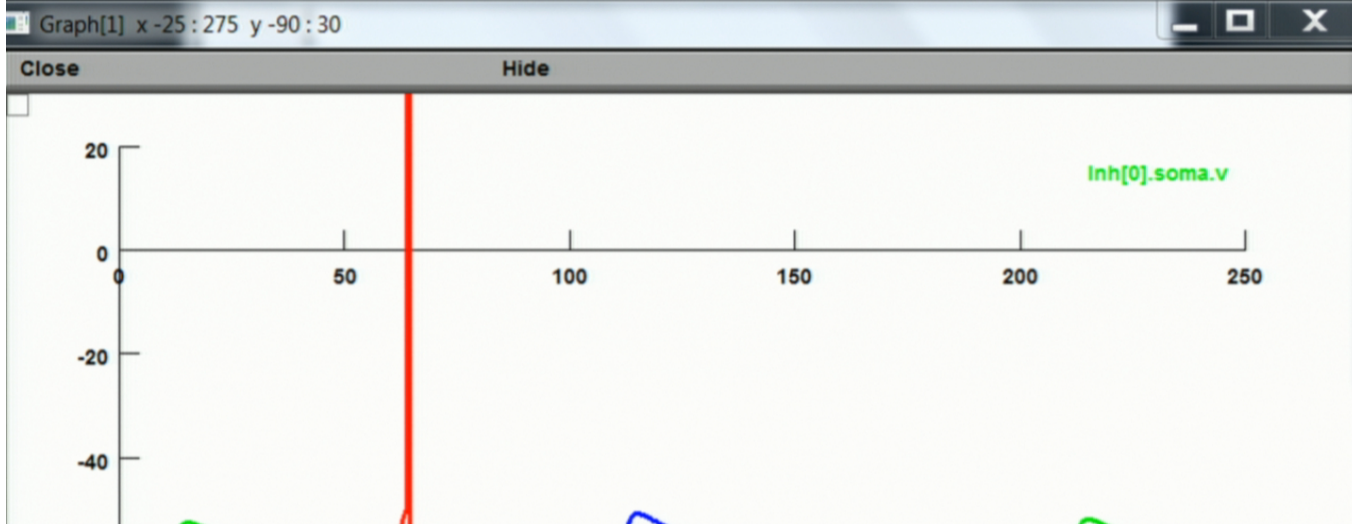
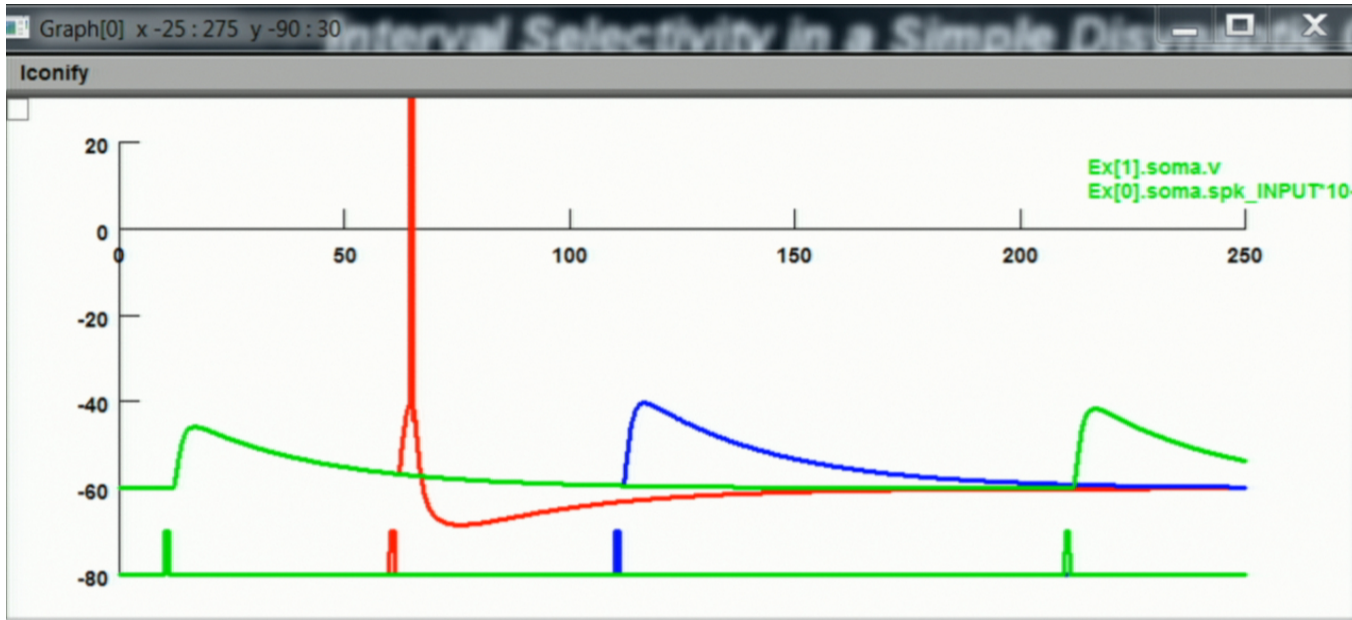
100 ms

200 ms

quit

11:44 AM  
Wednesday  
1/29/2014





Common\_Parameters

Close Hide

RUN

Synaptic Weights

sExEx[ExINPUT][0].gmaxAMPA 0.014

sExInh[0][0].gmaxAMPA 0.0023

slnhEx[ExINPUT][0].gmaxGABA 0.1

Short-term Plasticity

U\_EPlasSom(Ex->Ex) 0.2

trec\_EPlasSom(Ex->Ex) (ms) 10

tfac\_EPlasSom(Ex->Ex) (ms) 400

U\_EtolPlasSom(Ex->Inh) 0.2

trec\_EtolPlasSom(Ex->Inh) (ms) 10

tfac\_EtolPlasSom(Ex->Inh) (ms) 100

U\_(Inh->Ex) 0.25

trec(Inh->Ex) (ms) 700

tfac\_(Inh->Ex) (ms) 20

50 ms

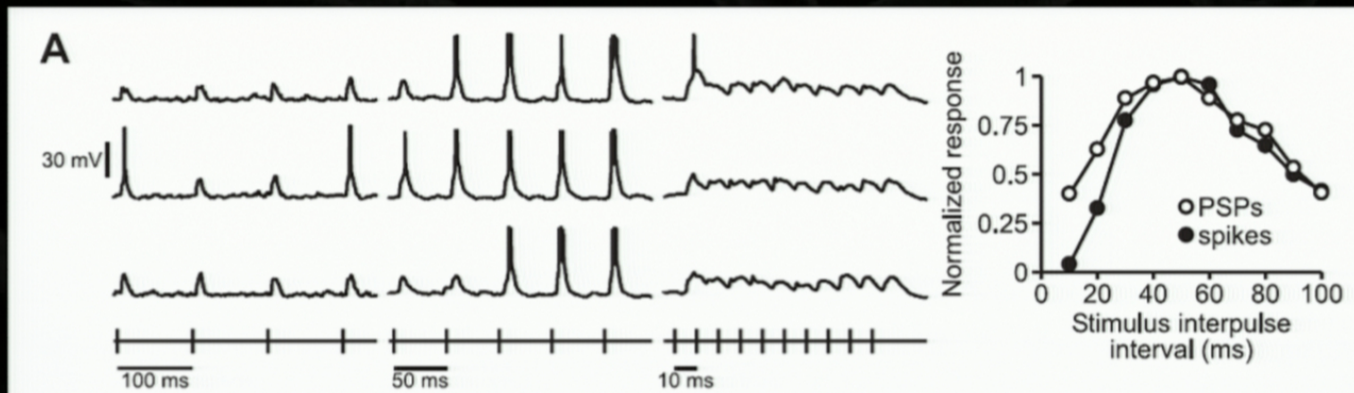
100 ms

200 ms

quit

11:45 AM  
Wednesday  
1/29/2014

# Short-Term Synaptic Plasticity Seems to Underlie Neuronal Interval Selectivity in Some Cases



Behavioral/Systems/Cognitive

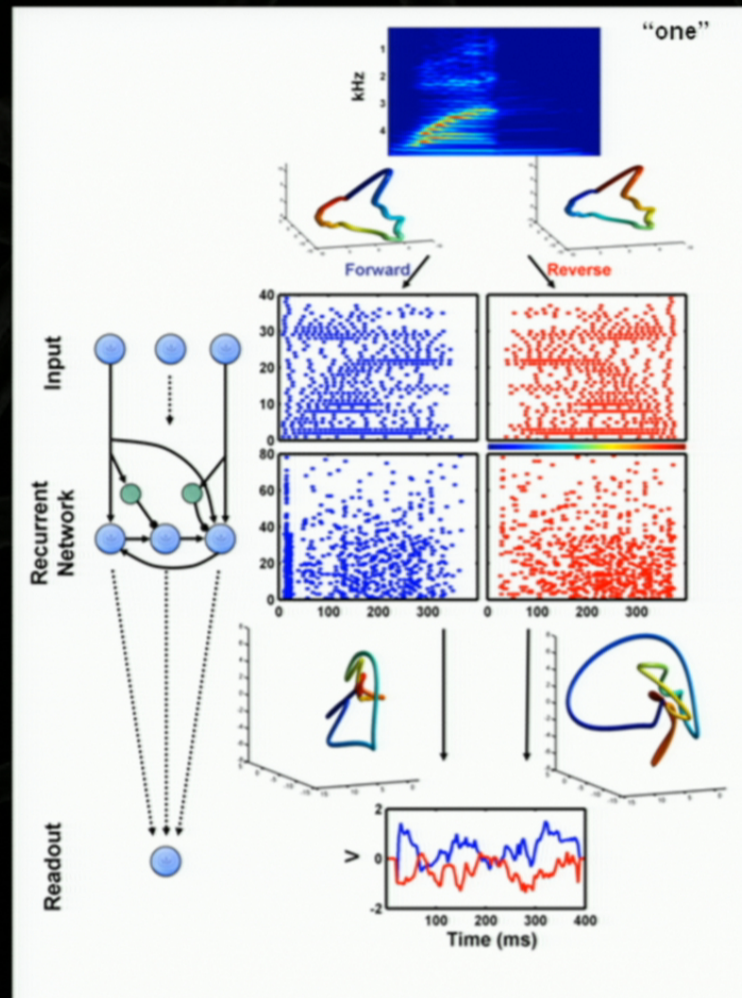
Carlson, 2009 (J. Neurosci)

## Temporal-Pattern Recognition by Single Neurons in a Sensory Pathway Devoted to Social Communication Behavior

Bruce A. Carlson

Department of Biology, Washington University in St. Louis, St. Louis, Missouri 63130, and Department of Neurobiology and Behavior, Cornell University, Ithaca, New York 14853

# Neural Trajectories are Time Asymmetric



Haeusler & Maass, 2007

## **Conclusions**

- **The brain has many different “clocks”. Each specialized for different temporal scales and functional needs (precision, reset, patterns, ...)**

## **Conclusions**

- **The brain has many different “clocks”. Each specialized for different temporal scales and functional needs (precision, reset, patterns, ...)**
- **Experimental and theoretical evidence that the brain uses neural dynamics of recurrent neural networks to tell time on the scale of milliseconds and seconds.**
- **But these networks have traditionally been subject to chaos. We now know that we can “tame” chaos through plasticity of the recurrent connections.**
- **Recent shift in thinking about how the brain works: Computations arise from the voyage through state space, as opposed to a destination in state space**

Current Lab Members



Thank you

Previous Lab Members



