

Title: CMB as a Probe of New Physics: The Story of Cosmic Birefringence

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Abstract: Cosmological birefringence is a postulated rotation of the linear polarization of photons that arises due to a Chern-Simons coupling of a new scalar field to electromagnetism. In particular, it appears as a generic feature of simple quintessence models for Dark Energy, and therefore, should it be detected, could provide insight into the microphysics of cosmic acceleration. Prior work has sought this rotation, assuming the rotation angle to be uniform across the sky, by looking for the parity-violating TB and EB correlations in the CMB temperature/polarization. However, if the scalar field that gives rise to cosmological birefringence has spatial fluctuations, then the rotation angle may vary across the sky. In this talk, I will present the results of the first CMB-based search for direction-dependent cosmological birefringence, using WMAP-7 data, and report the constraint on the rotation-angle power spectrum for all multipoles up to the resolution of the instrument. I will discuss the implications for a specific models for rotation, and show forecasts for Planck and future experiments. I will then conclude with a brief discussion of other exotic physical models, such as chiral gravity, and astrophysical scenarios, such as inhomogeneous reionization, that can be probed using the same analysis.

# CMB as a Probe of New Physics:

*~The Story of Cosmic Birefringence~*

Vera Gluscevic  
(Caltech)

with Marc Kamionkowski, Duncan Hanson, Chris Hirata, Robert  
Caldwell, and Asantha Cooray

December 2012

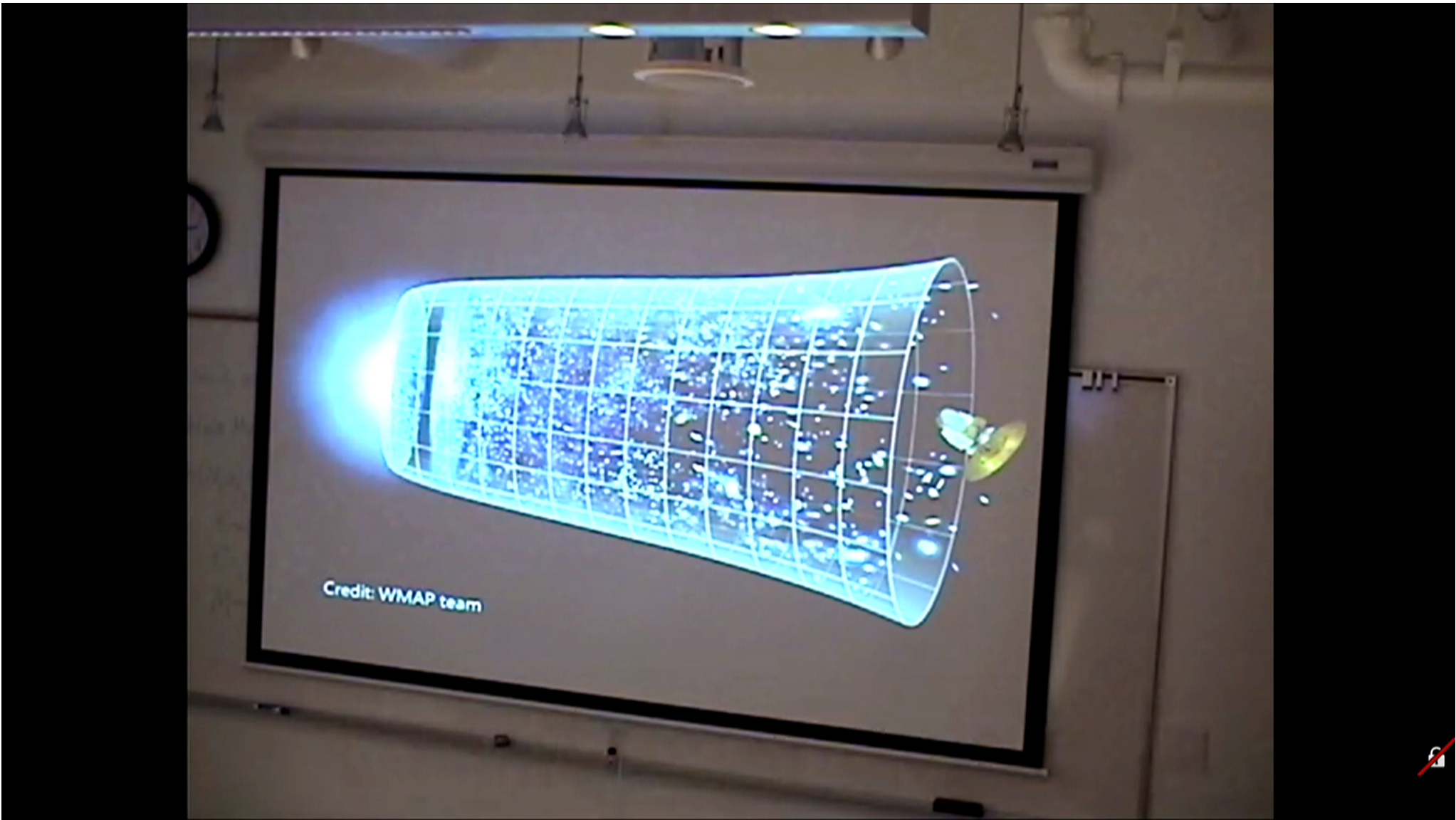
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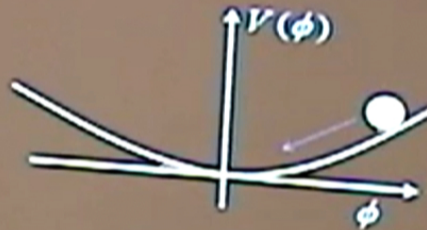


photons traveling cosmological distances.



Scalar field with slow roll:

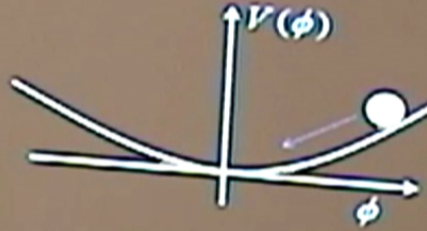
$$w = \frac{p}{\rho} = \frac{\frac{1}{2}\dot{\phi}^2 - V(\phi)}{\frac{1}{2}\dot{\phi}^2 + V(\phi)}$$



## Dark Energy model: quintessence $\phi$

Scalar field with slow roll:

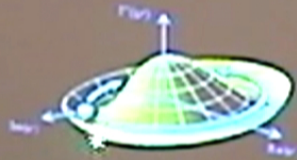
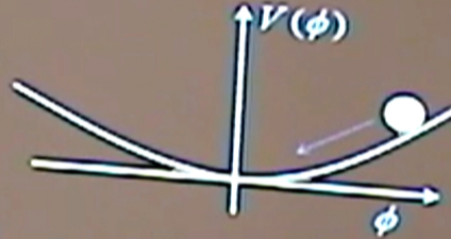
$$w = \frac{p}{\rho} = \frac{-V(\phi)}{+V(\phi)} \approx -1$$



## Dark Energy model: quintessence $\phi$

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Pseudo Nambu-Goldstone Boson



$$\mathcal{L} = -\frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi) - \frac{1}{2M} \phi F_{\mu\nu} \tilde{F}^{\mu\nu}$$

### Coupling to SM?

- dim 5
- gauge invariant
- shift-symmetry

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⇒ Modified Maxwell's eqs.  
⇒ phase difference for  
L and R polarizations  
⇒ rotation.

$$\alpha \sim \frac{\Delta\phi}{M}$$

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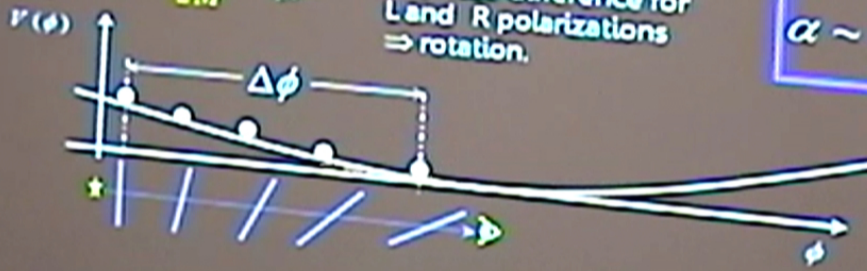
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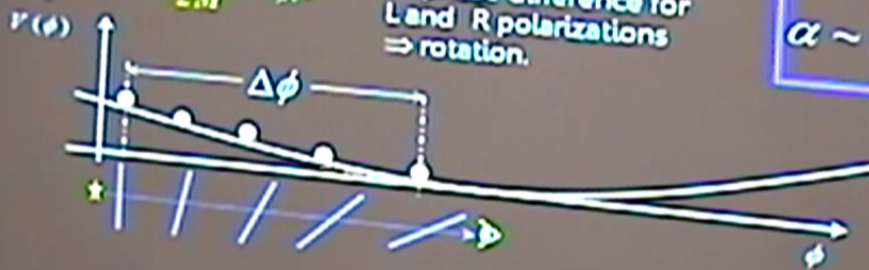
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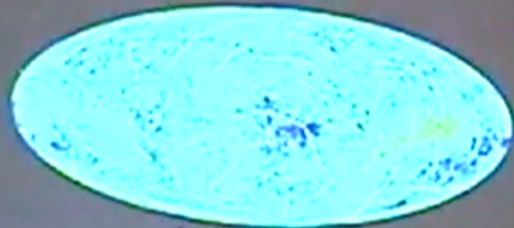
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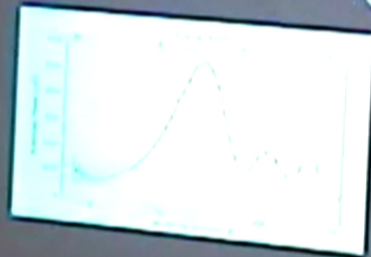
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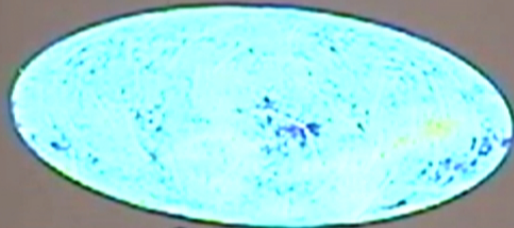


Credit: WMAP team



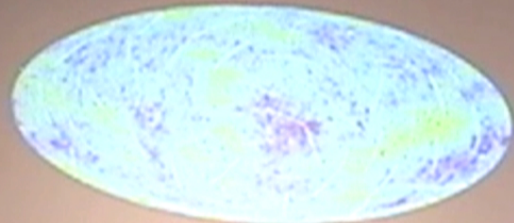
$$T(\hat{n}) = \sum_{lm} T_{lm} Y_{lm}(\hat{n})$$

$$C_l^{-1} \delta_{ll'} \delta_{mm'} \equiv \langle T_{lm} T_{l'm'}^* \rangle$$



Credit: WMAP team

$$p(\hat{n}) = Q(\hat{n}) + iU(\hat{n}) = -\sum_{lm} (E_{lm} + iB_{lm}) {}_2Y_{lm}(\hat{n})$$



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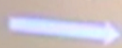
$$\downarrow e^{2i\alpha(\hat{n})}$$

$$Q'' = -2\alpha U + Q$$

$$U'' = 2\alpha Q + U$$

  
E mode

$\alpha(\hat{n})$



= E + B mode

$$B \sim \alpha E$$



Start with pure E-mode... — rotation generates B-modes.

Can reconstruct  $\alpha$  from EB, TB, EE, TE.

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Standard picture:

$$\langle E_{lm} B_{l'm'} \rangle = \delta_{ll'} C_l^{EB} = 0$$

$$\langle T_{lm} B_{l'm'} \rangle = \delta_{ll'} C_l^{TB} = 0$$

Start with pure E-mode... — rotation generates B-modes.

Can reconstruct  $\alpha$  from EB, TB, EE, TE.

With CB rotation:

$$\langle E_{lm} B_{l'm'} \rangle = \sum_N C_l^{EB} \neq 0$$

$$\langle T_{lm} B_{l'm'} \rangle = \sum_N C_l^{TB} \neq 0$$

Previous work:

- Uniform rotation constraints from WMAP, Bicep, QUaD:  
 $-1.4^\circ < \alpha < 0.9^\circ$  (95%CL)
- rms fluctuation from AGN  $< 4^\circ$  (Kamionkowski, 2009)

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This work: *Direction-dependent* rotation:

$$\alpha(\hat{n}) = \sum_{LM} \alpha_{LM} Y_{LM}(\hat{n}) \rightarrow C_L^{-1} \delta_{LL} \delta_{MM'} = \langle \alpha_{LM} \alpha_{L'M'}^* \rangle$$

- ✓ Why not?
- ✓ Increase sensitivity
- ✓ Consider models with no uniform rotation.
- ✓ Discern different models.
- + Full sky to maximize sensitivity.

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$$\langle B_{lm}^{map} T_{l'm'}^{map,*} \rangle = \int d\hat{n} Y_{LM} \alpha_{LM} \tilde{C}_{l'}^{TE} \left[ {}_2Y_{lm}^* {}_2Y_{l'm'} + {}_{-2}Y_{lm}^* {}_{-2}Y_{l'm'} \right]$$

$l+l'+L = \text{even}$

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$l+l'+L = \text{even}$

theory



$$\tilde{\alpha}_{LM} = N_L \int d\hat{n} Y_{LM} \left( \sum_{lm} \bar{B}_{lm}^{*,map} {}_2Y_{lm} \right) \left( \sum_{l'm'} \bar{T}_{l'm'}^{*,map} {}_2Y_{l'm'} \right)^* + cc$$

$l+l'+L = \text{even}$

$$\hat{\alpha}_{LM} = N_L \int d\hat{n} Y_{LM} \left( \sum_{lm} \bar{B}_{lm}^{*map} Y_{lm} \right) \left( \sum_{l'm'} \bar{T}_{l'm'}^{*map} Y_{l'm'} \right)^* + cc$$

$l+l'+L = \text{even}$

Inverse-variance filtering:  $\bar{B}_{lm} = \frac{B_{lm}^{map}}{C_{l}^{BB^{*map}}}$      $\bar{T}_{l'm'} = \tilde{C}_{l'}^{TE} \frac{T_{l'm'}^{map}}{C_{l'}^{TT^{*map}}}$

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simple analytic IVF:  $C_l^{*map} = \tilde{C}_l + C_l^{noise} / B_l^2$

Optimal quadratic estimator and its variance:

$$\hat{\alpha}_{LM} = \left( \frac{1}{\langle \hat{\alpha}_{LM}^{l'l'} \hat{\alpha}_{LM}^{l'l'} \rangle} \right)^{-1} \sum_{l'l'} \frac{\hat{\alpha}_{LM}^{l'l'}}{\langle \hat{\alpha}_{LM}^{l'l'} \hat{\alpha}_{LM}^{l'l'} \rangle} = \frac{1}{N_L} \sum_{l'l'} \frac{\hat{\alpha}_{LM}^{l'l'}}{\langle \hat{\alpha}_{LM}^{l'l'} \hat{\alpha}_{LM}^{l'l'} \rangle}$$

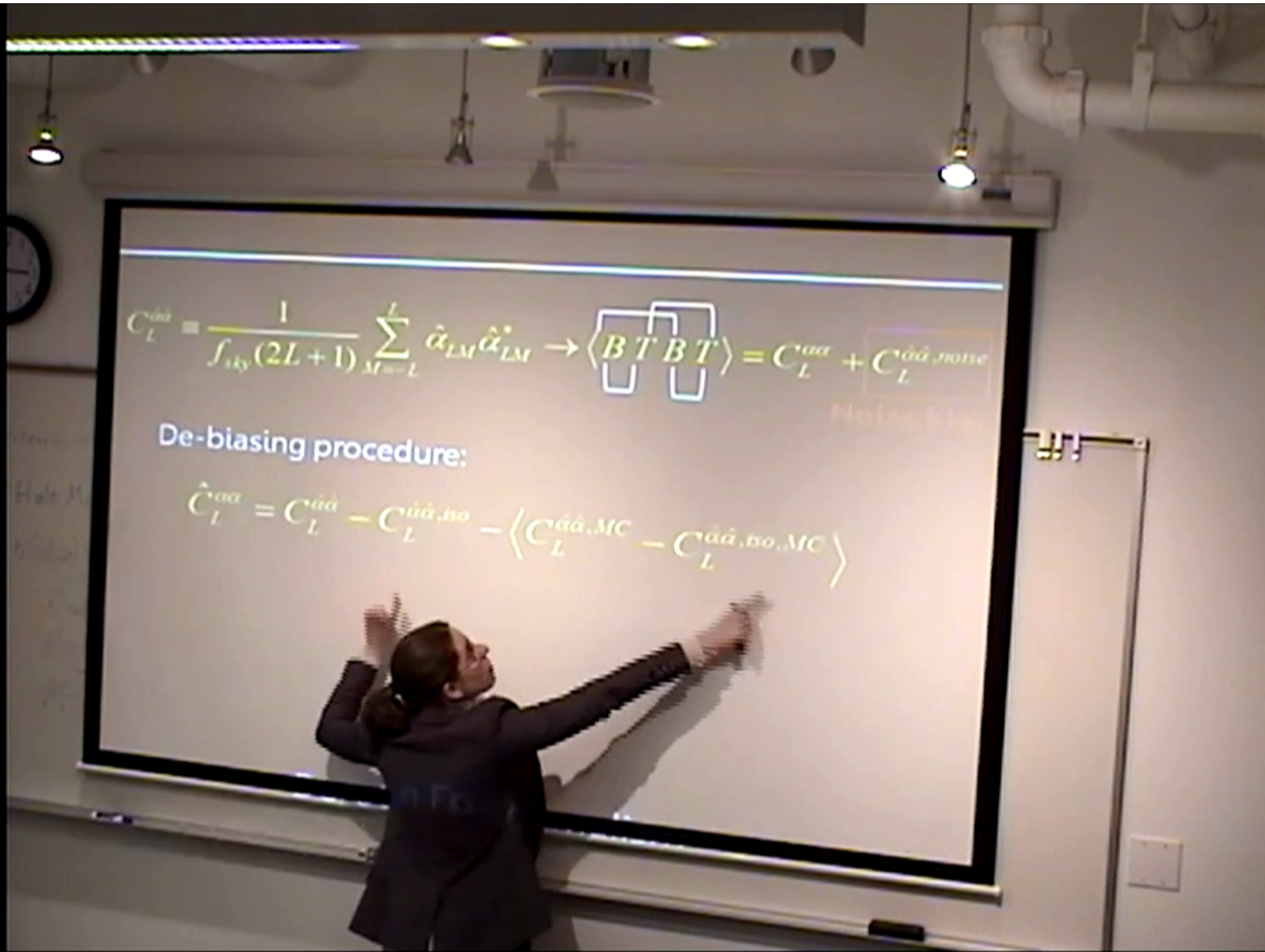
$$N_L = \langle \hat{\alpha}_{LM} \hat{\alpha}_{LM} \rangle = \sum_{l'l'} \frac{(\tilde{C}_l^{TE})^2}{C_l^{BB, map} C_l^{TT, map}} W_{l'l' L}$$

$$l + l' + L = \text{even}$$

VG et al. 2009

$$C_L^{\hat{a}\hat{a}} = \frac{1}{f_{sky}(2L+1)} \sum_{M=-L}^L \hat{\alpha}_{LM} \hat{\alpha}_{LM}^* \rightarrow \langle BTBT \rangle = C_L^{aa} + C_L^{\hat{a}\hat{a}, noise}$$

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Noise bias

De-biasing procedure:

$$\hat{C}_L^{\alpha\alpha} = C_L^{\hat{a}\hat{a}} - C_L^{\hat{a}\hat{a}, iso} = \langle C_L^{\hat{a}\hat{a}, MC} - C_L^{\hat{a}\hat{a}, iso, MC} \rangle$$

from data  
[isotropic bias]

$$C_L^{aa} = \frac{1}{f_{sky}(2L+1)} \sum_{M=-L}^L \hat{\alpha}_{LM} \hat{\alpha}_{LM}^* \rightarrow \langle \boxed{B^T B^T} \rangle = C_L^{aa} + C_L^{aa, noise}$$

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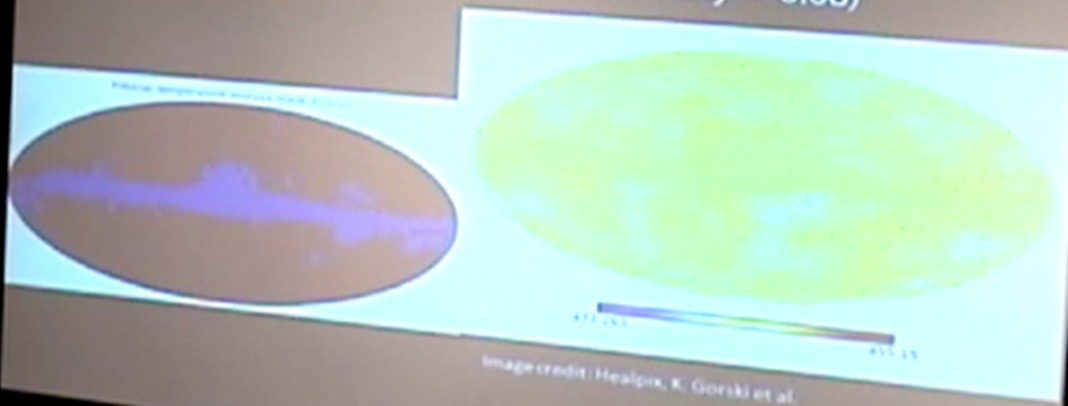
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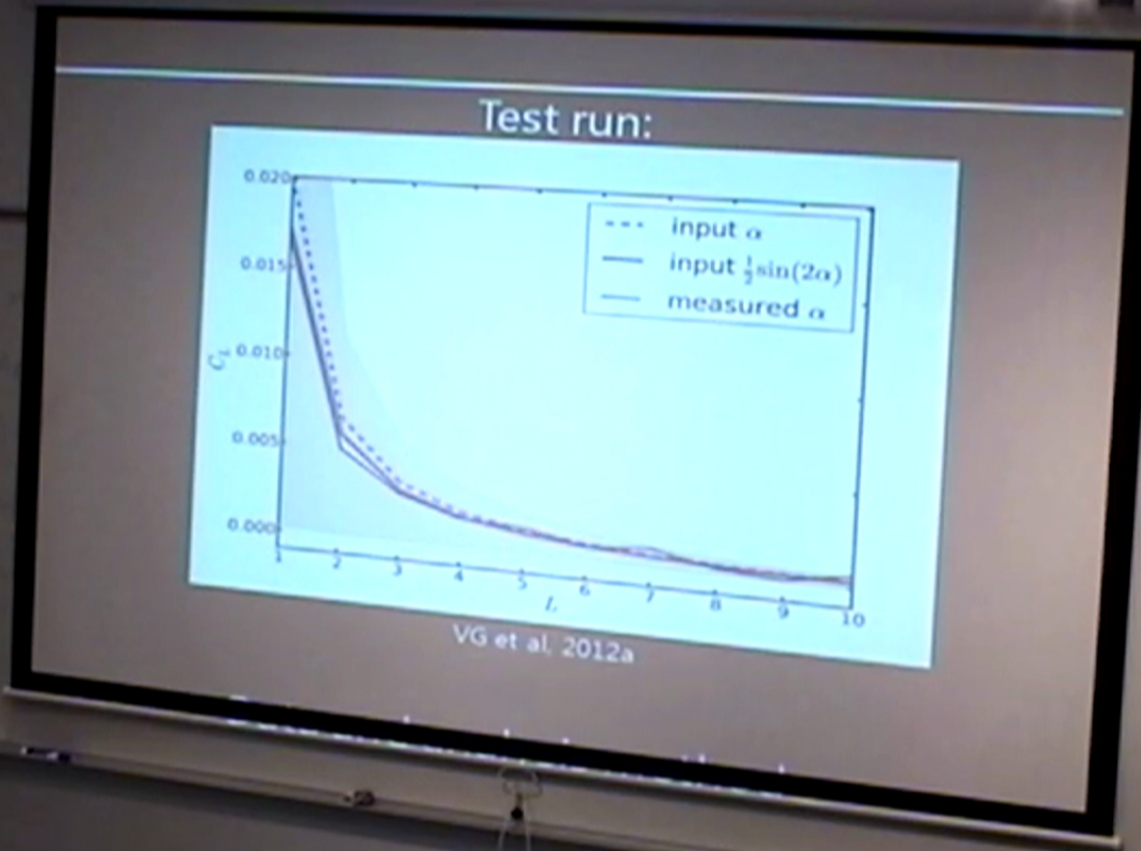
WMAP-7 Data:

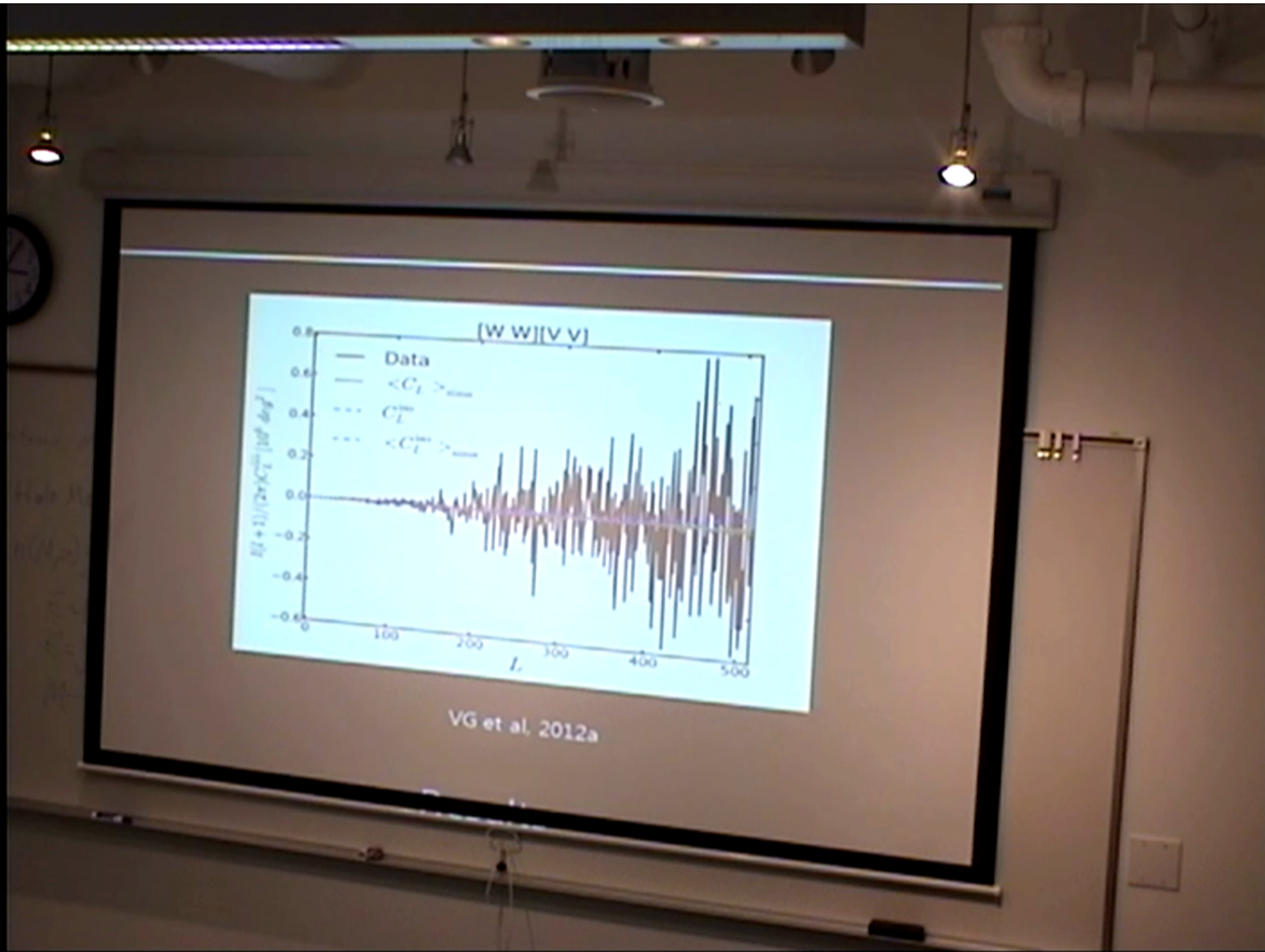
- ✓ Foreground-reduced V, W, and Q frequency-band maps of T and P (highest resolution)
- ✓ Analysis Masks (sky cuts with combined fsky = 0.68)

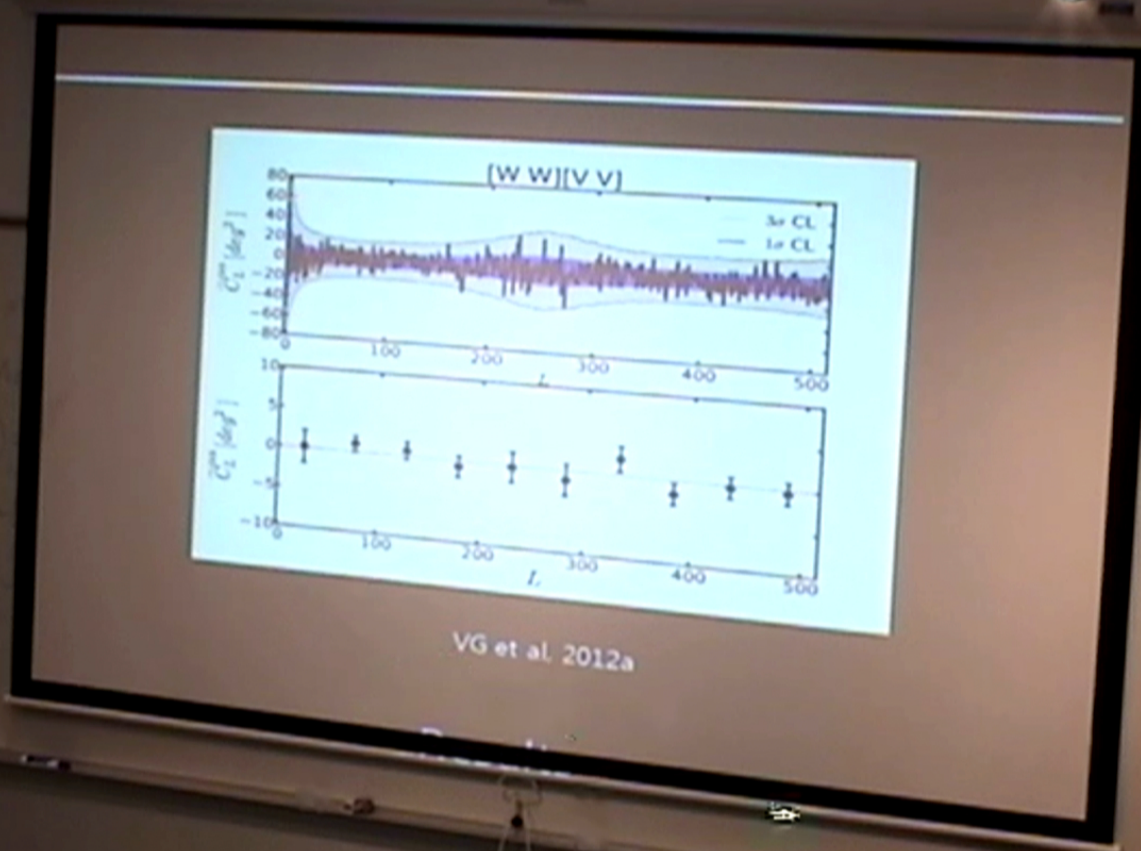


### Simulations:

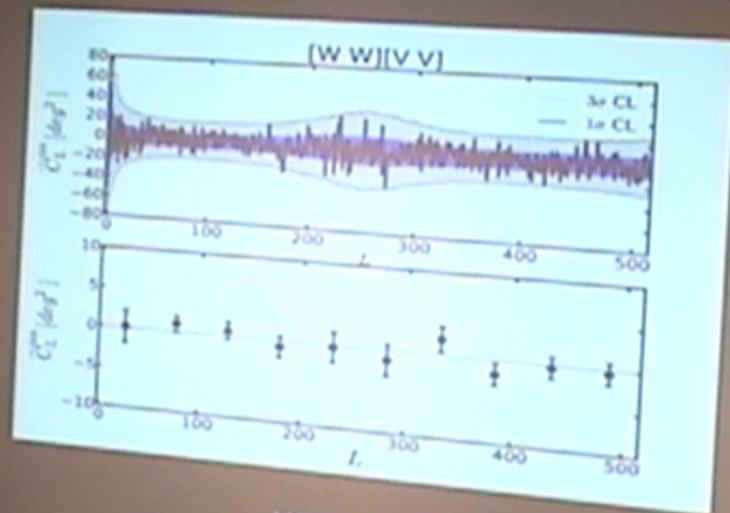
- ✓ CMB realizations with WMAP-7 best-fit power spectra
- ✓ Inhomogeneous noise with Q-U correlations + symmetric beams
- ✓ Analysis masks











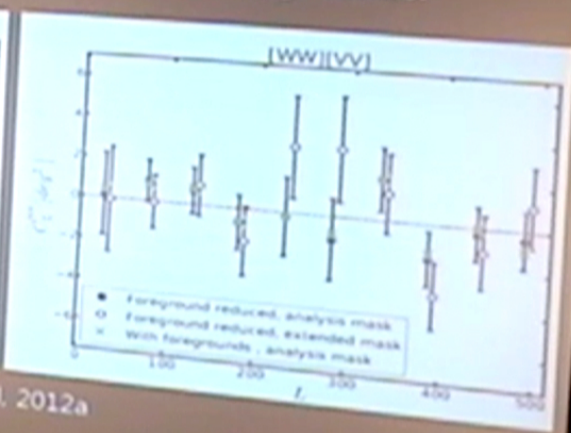
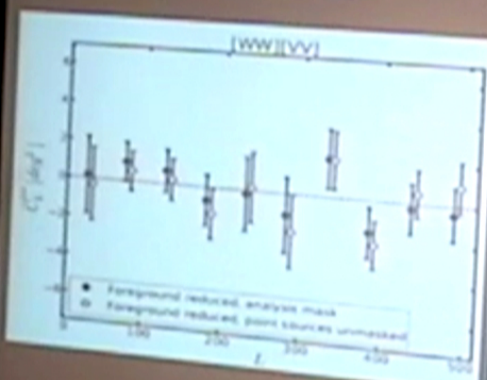
VG et al. 2012a

### Contamination tests:

point sources

+

foregrounds:



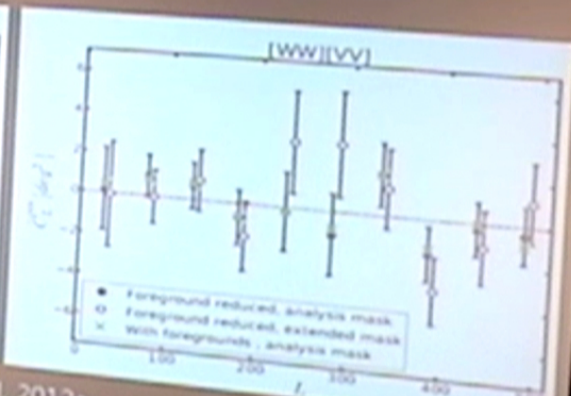
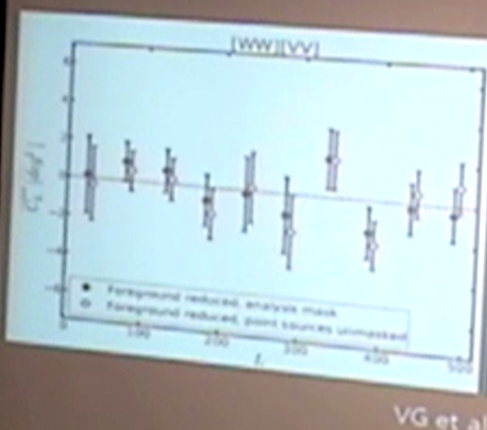
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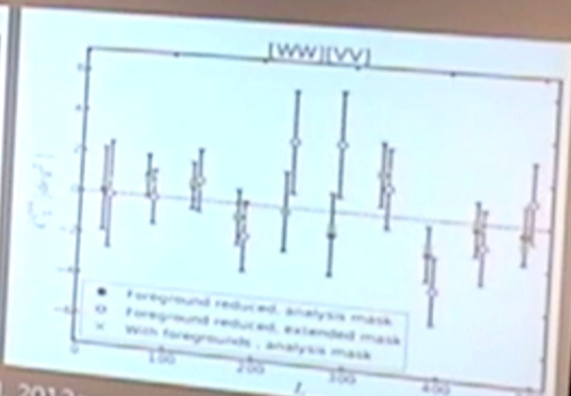
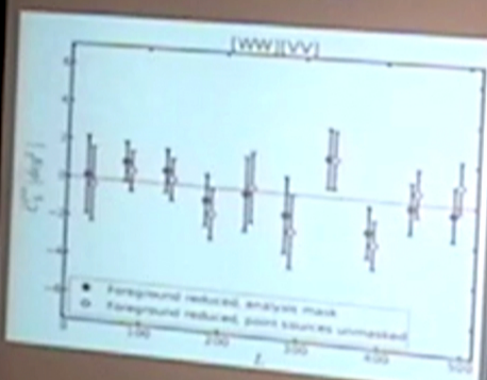
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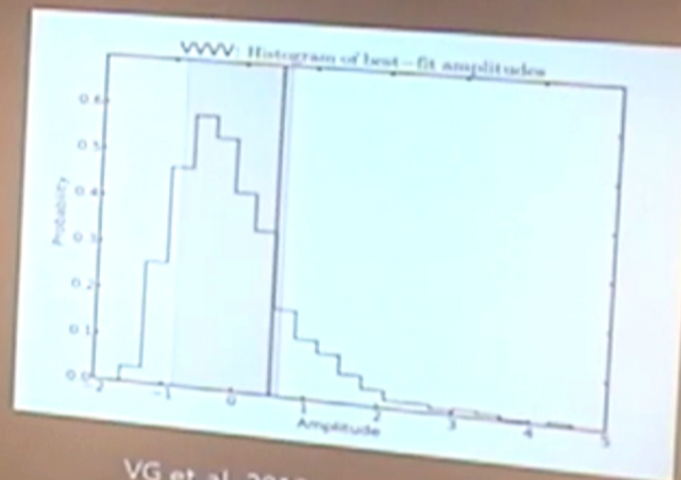
VG et al. 2012a

Constraints on a scale-invariant power spectrum:

$$C_L^{var, fiducial} = \frac{A}{L(L+1)}$$

Minimum-variance estimator for the amplitude A:

$$\sqrt{C_2^{var} / (4\pi)} < 1^\circ$$



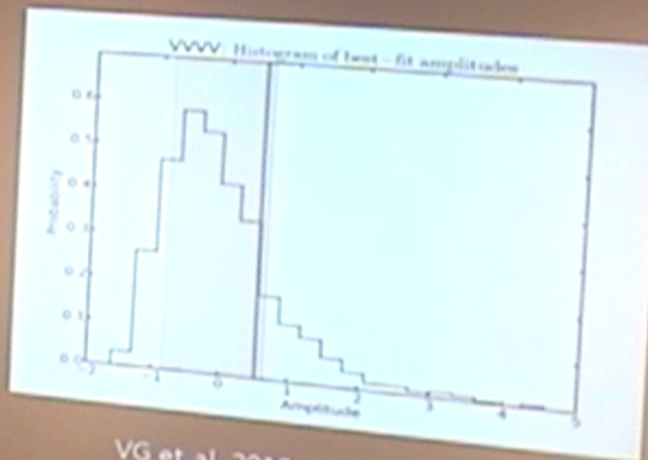
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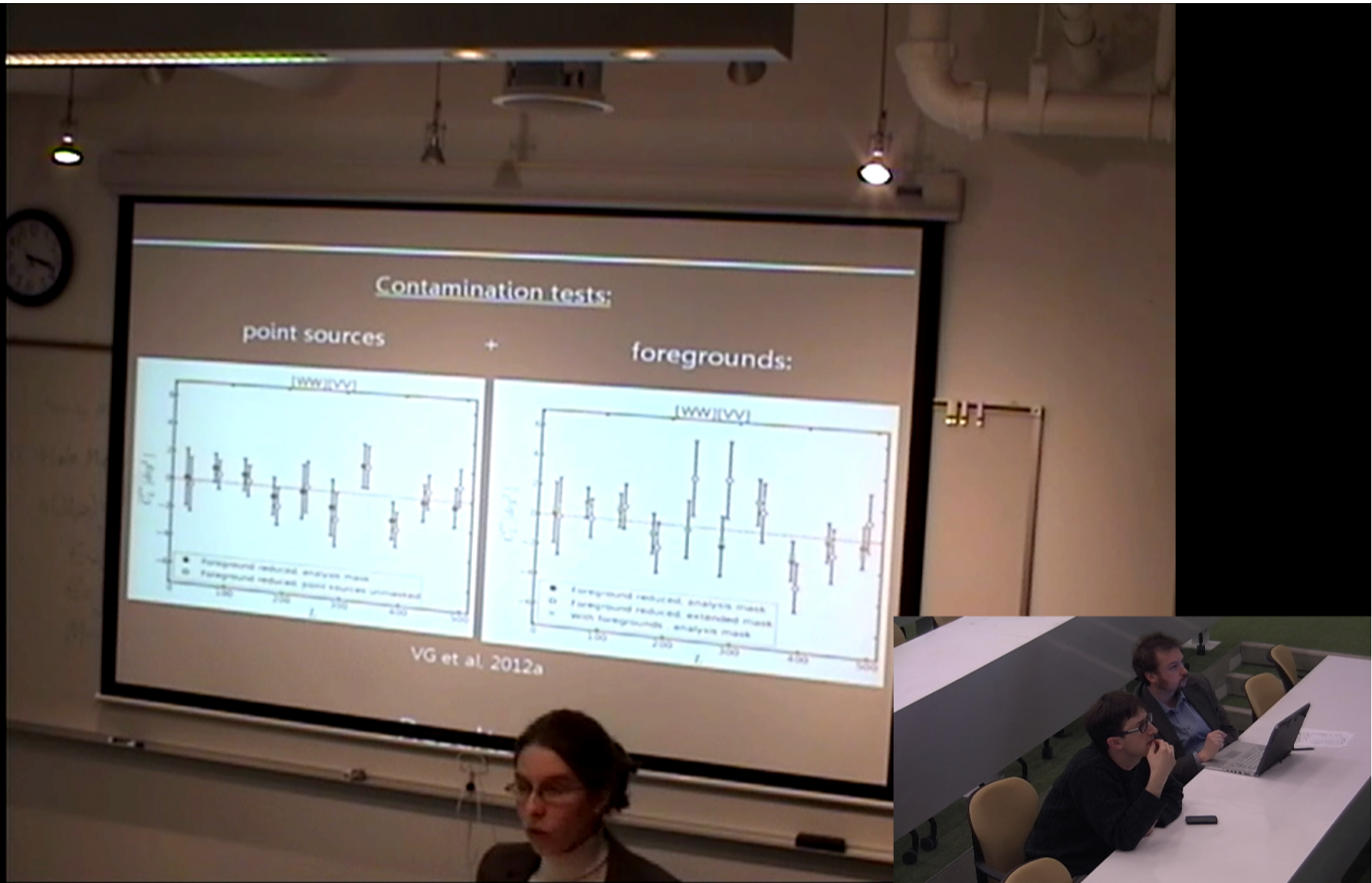
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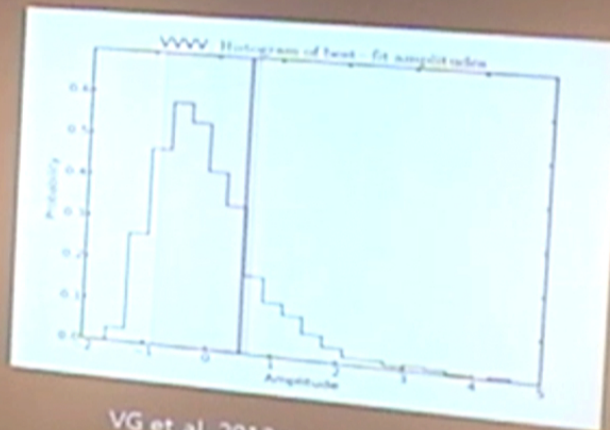


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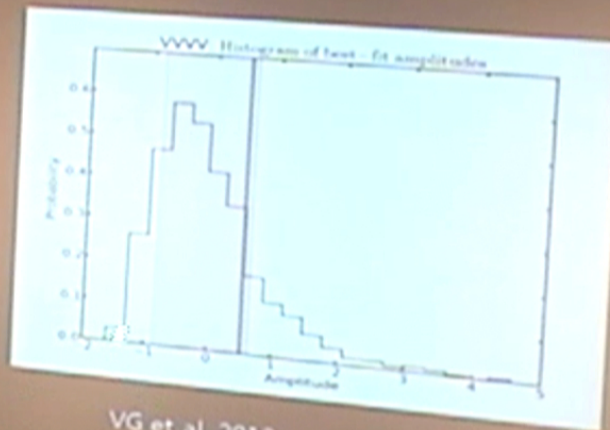


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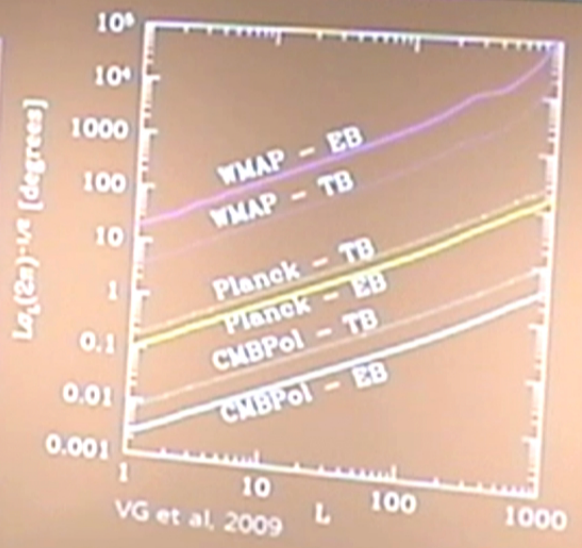
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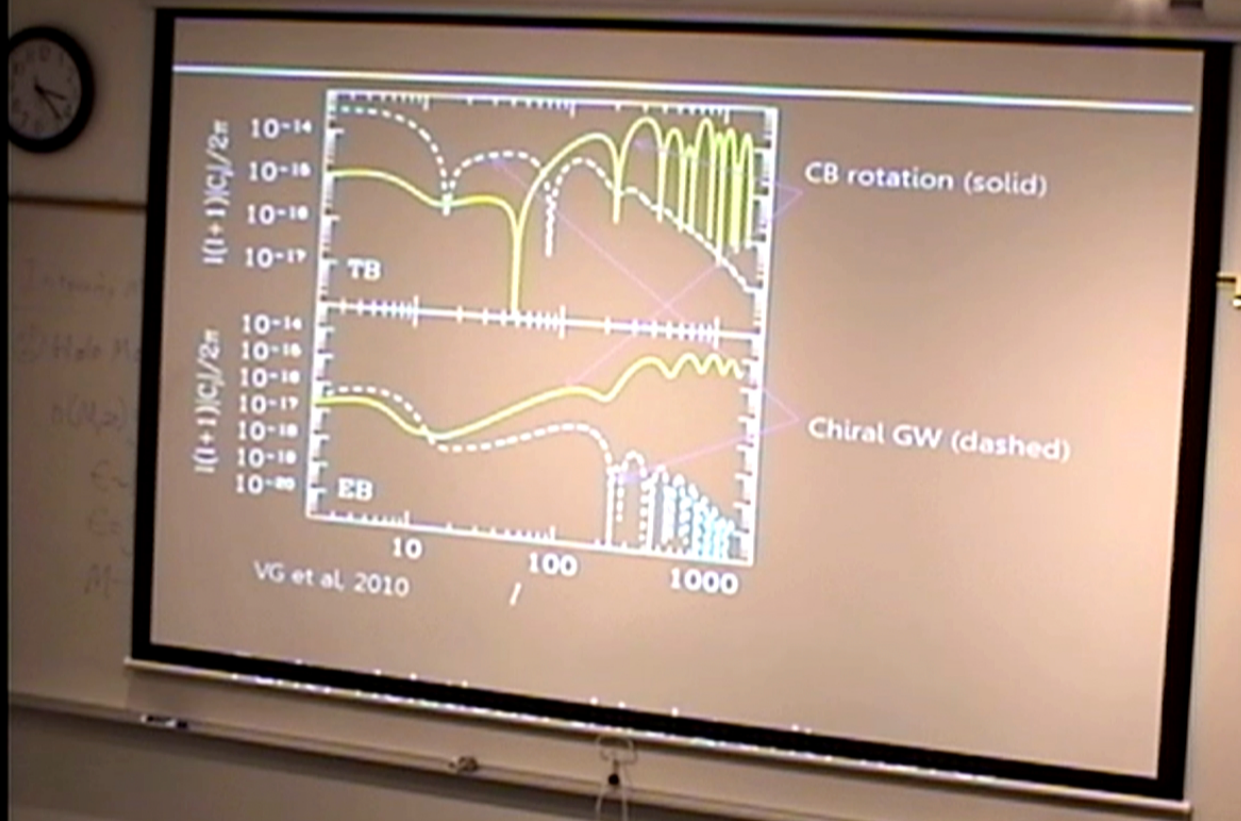
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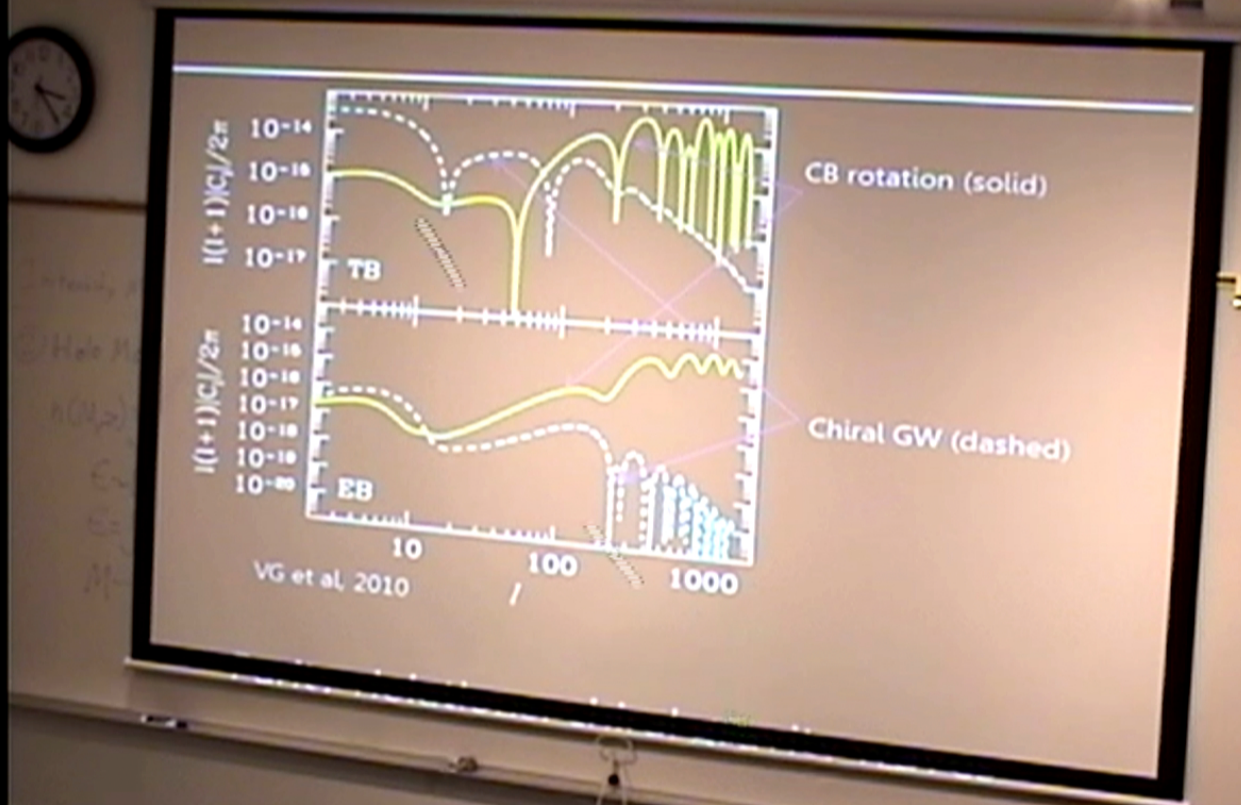


VG et al. 2012a


Instrument	Uniform rotation
WMAP	2° (TB)
Planck	4' (EB)
CMBPol-like	6" (EB)







- Cosmic scalar field with shift symmetry  $\rightarrow$  *cosmological birefringence*.
- Rotation induces TB and EB off-diagonal correlations.
- Full-sky QE formalism to look for direction-dependent rotation angle.
- Used WMAP-7 fg-reduced T and P maps.
- Constrained  $C_l^{aa}$  for  $L < 512$ , implying  $\Rightarrow \sqrt{C_2^{aa} / (4\pi)} < 1$
- Planck: an OoM improvement.
- CMB probes P-violating physics beyond the SM

A woman with glasses and a dark blazer over a white turtleneck is standing in front of a large projector screen in a lecture hall. The screen displays the text 'Appendix: Cosmic Reionization' in a white serif font. The room has a clock on the wall to the left, a whiteboard to the right, and several spotlights on the ceiling. The woman is looking towards the right side of the frame.

*Appendix:*  
Cosmic Reionization

## Theory

Inhomogeneous process: growing ionized bubbles.

## Observations:

- Completed by  $z \sim 6-7$
- Optical depth to the LSS,  $\tau \sim 0.074$  (WMAP-7)  $\rightarrow z \sim 10$
- $\Delta z > 0.06$  (EDGES, new result)
- $\Delta z < 7.9$  (SPT, for specific models)



Zahn et al. 2012

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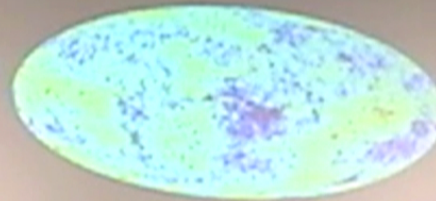
Zahn et al. 2012

$$\Delta T(\hat{n}) = e^{-\tau(\hat{n})} \Delta \tilde{T}(\hat{n})$$

$$p(\hat{n}) = Q(\hat{n}) + iU(\hat{n}) = e^{-\tau(\hat{n})} \tilde{p}(\hat{n})$$



Induces off-diagonal correlations.



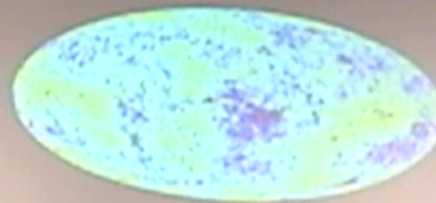
$$\dot{\tau}_{LM} = -iN_L \int d\hat{n} Y_{LM}(\hat{n}) \left[ \sum_{lm} \tilde{B}_{lm}^* Y_{lm}(\hat{n}) \sum_{l'm'} \tilde{T}_{l'm'} Y_{l'm'}^*(\hat{n}) + cc \right]$$

$l+l'+L = \text{odd}$

Dvorkin et al, 2009; Hanson and Lewis, 2009

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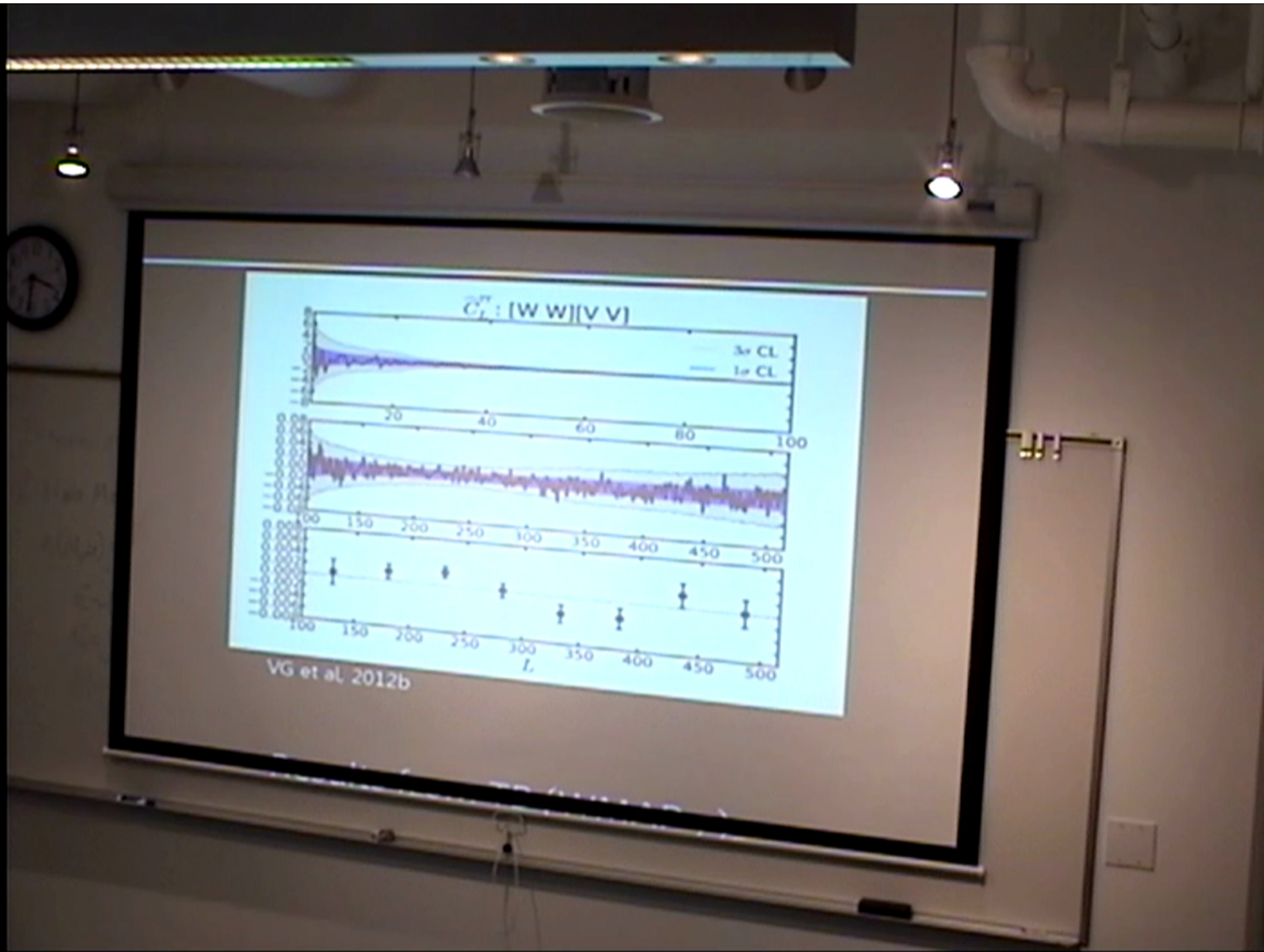


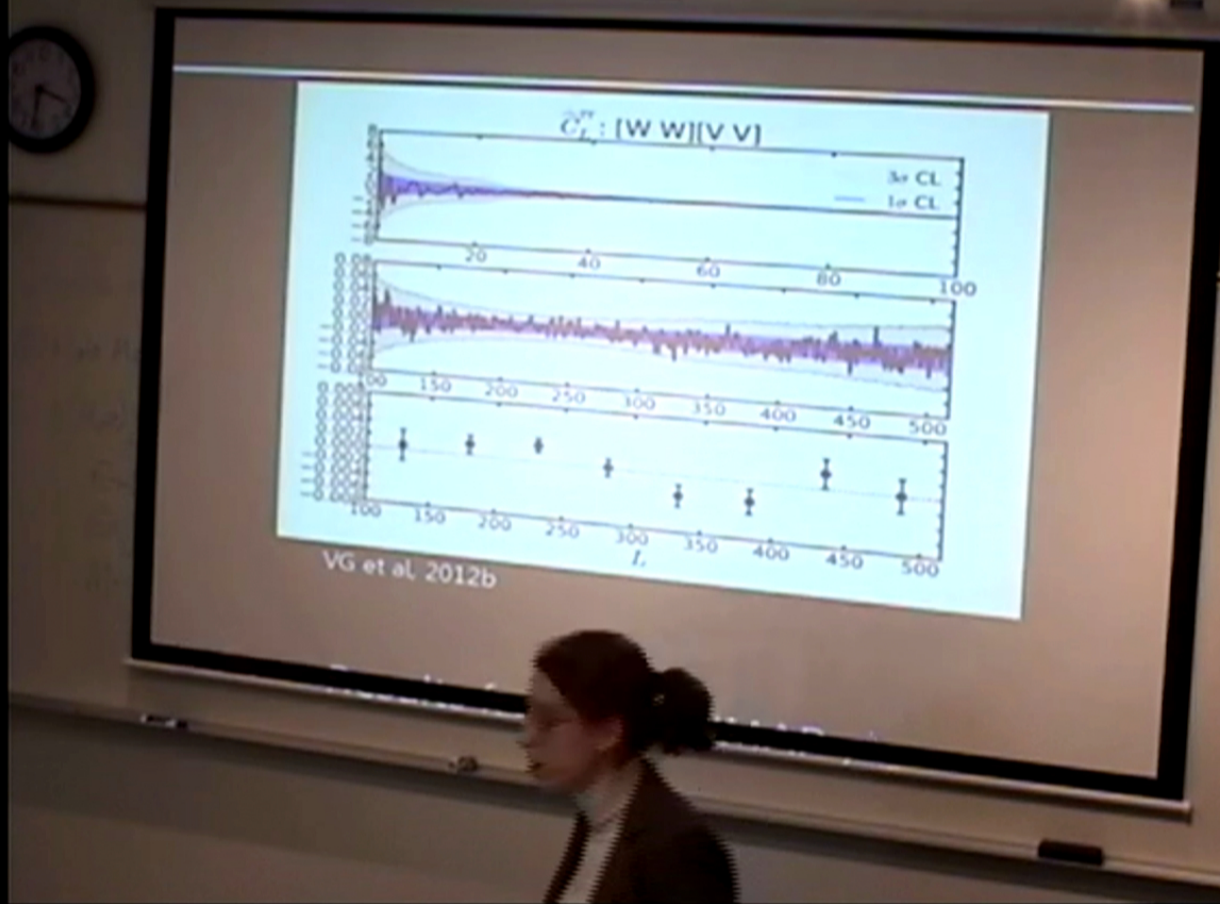
Induces off-diagonal correlations.

$$\dot{\tau}_{LM} = -iN_L \int d\hat{n} Y_{LM}(\hat{n}) \left[ \sum_{lm} \tilde{B}_{lm}^* Y_{lm}(\hat{n}) \sum_{l'm'} \tilde{T}_{l'm'} Y_{l'm'}^*(\hat{n}) + cc \right]$$

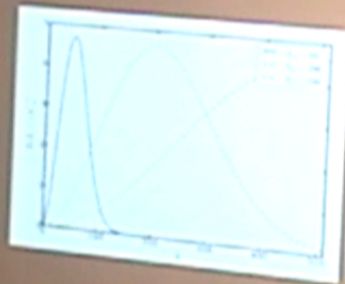
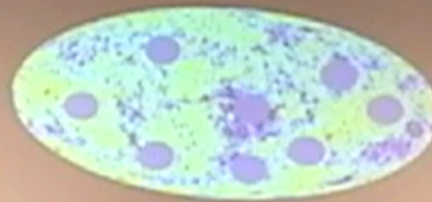
$l+l' = \text{odd}$

Dvorkin et al, 2009; Hanson and Lewis, 2009



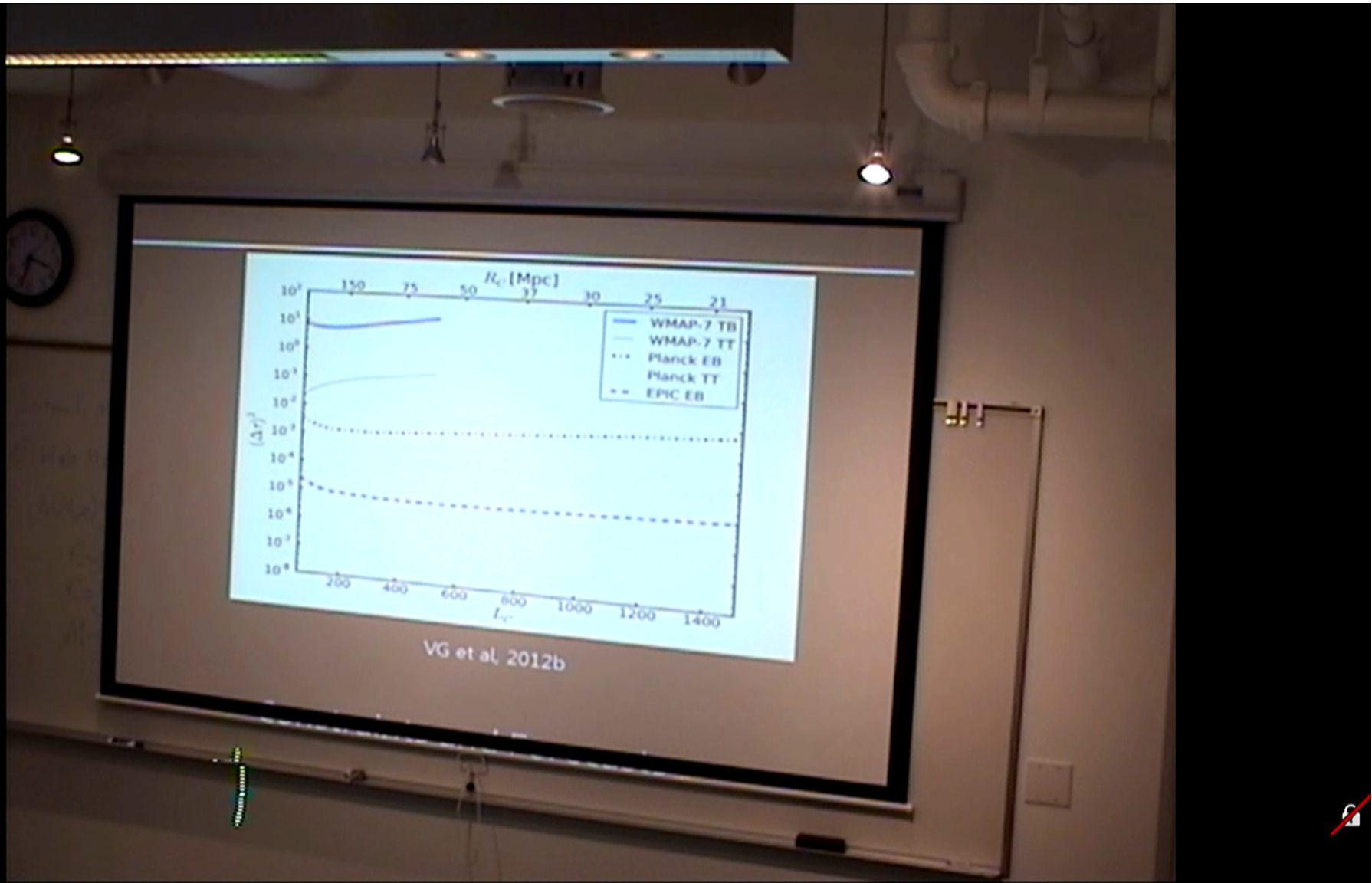


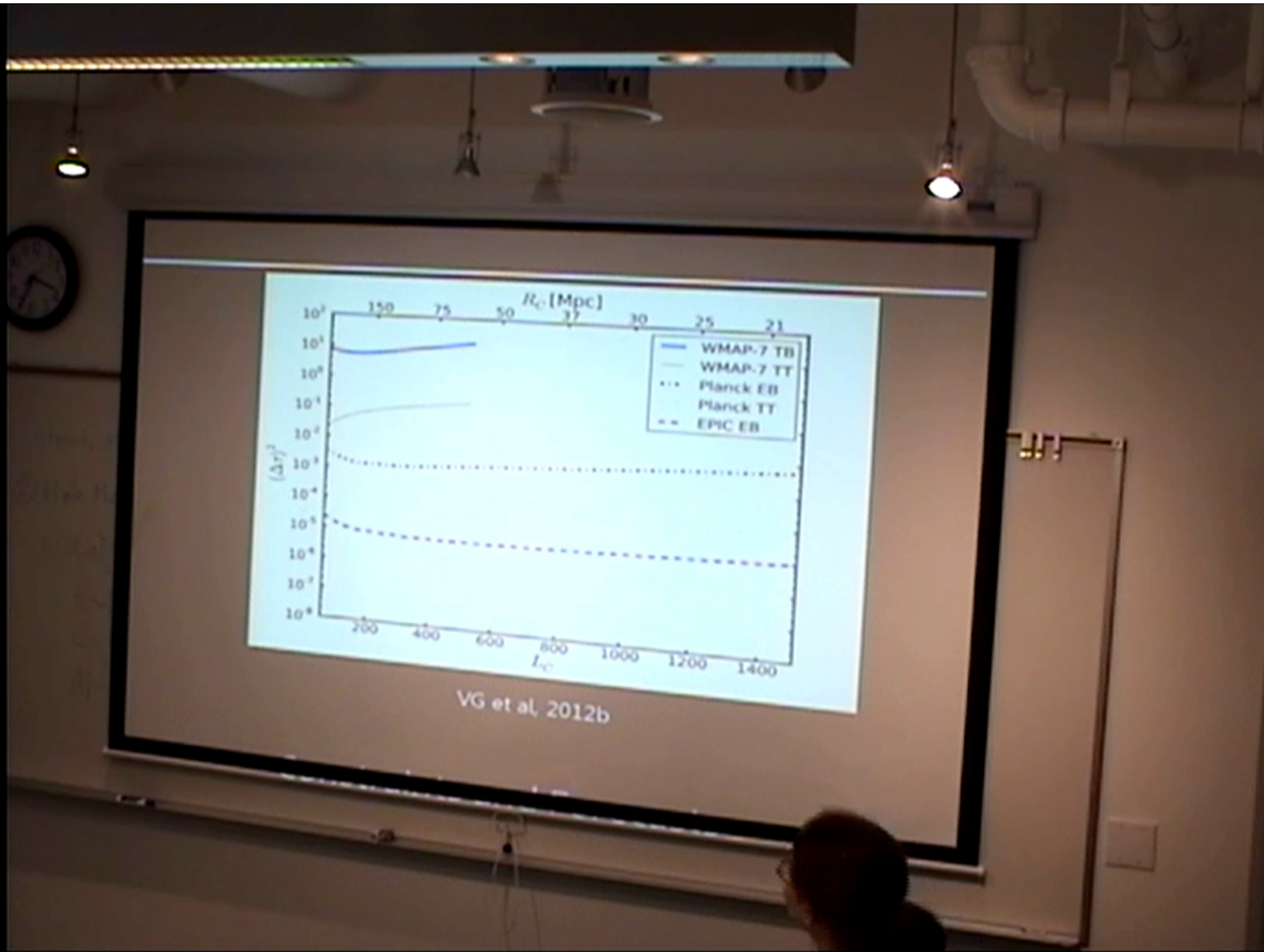
Assume:  
white noise power with rms  
 $\Delta\tau$  below coherence scale  
 $\theta_c \sim \pi/L_c$ , smoothed on  
larger scales.



$$C_L^{\pi} = \frac{4\pi}{L_c^2} (\Delta\tau)^2 e^{-L/L_c}$$

VG et al. 2012b








$$\frac{\Delta\tau}{\tau} \approx \frac{3}{2} \frac{\Delta z}{z}$$

$$\Delta z \approx R_c z^{-1/2} \Omega_m^{1/2} H_0 / c$$

↓

$$\Delta\tau \approx 0.001 \frac{R_c}{20 \text{ Mpc}}$$

↔ Optical-depth fluctuation  $\Delta\tau$  is related to bubble size  $R_c$



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Optical-depth fluctuation  $\Delta\tau$  is related to bubble size  $R_c$

The diagram shows a yellow, irregularly shaped bubble with a dashed outline. A double-headed arrow labeled  $R_c$  indicates the radius of the bubble.

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Optical-depth fluctuation  $\Delta\tau$  is related to bubble size  $R_c$

The diagram shows a bubble with a radius  $R_c$  and a central region. The bubble is depicted as a glowing yellow sphere with a dashed outline, and a double-headed arrow indicates the radius  $R_c$ .

- Used MVE formalism + WMAP-7 data to look for signatures of patchy screening.
- Forecasts → best constraints from EB.
- Simple model + EDGES result → parameter space is limited!
- Future-generation CMB experiments can be used to probe tomography of reionization.

- Use MVE formalism and higher-order TB/EB correlations to look for cosmic birefringence and map tomography of reionization.

- WMAP-7 constraints:

$$\sqrt{C_2^{Q\alpha} / (4\pi)} < 1'$$
$$\Delta\tau < 0.1$$

- Forecasts:

Planck :

$$\alpha \sim 1'$$

CMBPol-like:

$$R_c \sim 20 \text{ Mpc}$$