

Title: Mass and Tension (momentum) Sum Rules in AdS (dS)

Date: Nov 27, 2012 11:00 AM

URL: <http://www.pirsa.org/12110042>

Abstract: >The stress-energy tensor in a conformal field theory has zero trace.

Hence AdS boundary stress-tensors are traceless by construction, to match this property of the dual CFT. An elegant (aka nifty) construction based on the conformal isometry of AdS will be presented which shows that in an asymptotically AdS spacetime, the sum of the ADM mass and the ADM tensions is zero. This result follows strictly from the gravitational point of view- that is, the Einstein equations and the definitions of the ADM charges. Further, it turns out that perturbative stress-energy sources in an asymptotically AdS spacetime must satisfy a local version of this constraint, namely that the sum of the energy density minus the pressures equals zero. The situation with positive cosmological constant is both similar and distinct in interesting ways, which will be briefly discussed. The analogous (analytically continued) conformal isometry in dS is the root of the

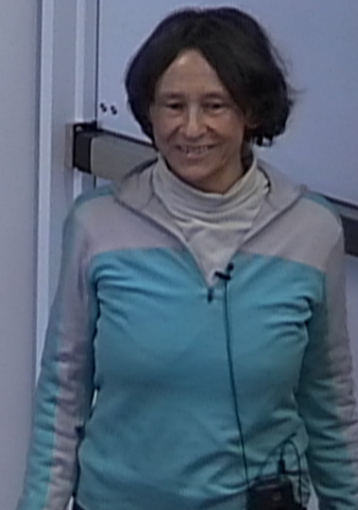
k^4 ϵ power spectrum for causal cosmological perturbations. Work in progress (speculations) will be presented about a corresponding sum-rule for gravitational charges defined at future infinity in a spacetime that approaches dS at late times.

Sum Rules for Mass and
Tension in AdS / dS (?)!!

Cosmology

$\vec{V} =$

MFVF



Sum Rules for Mass and
Tension in AdS / d S C(?)

Sum Rules for Mass and
Tension in AdS / dS (?)

Sum Rules for Mass and
Tension in AdS / dS (?)!!

MFVF

Cosmology (flat)

$$\dot{V} = \frac{\partial}{\partial t} - H x^{\mu} \frac{\partial}{\partial x^{\mu}}$$

Sum Rules for Mass and
Tension in AdS / dS (?)

Cosmology (flat)

MFVF

$$\dot{V} = \frac{\partial}{\partial t} - H x^{\mu} \frac{\partial}{\partial x^{\mu}}$$

Sum Rules for Mass and
Tension in AdS / dS (?)

MFVF

Cosmology (flat)

$$\vec{V} = \frac{\partial}{\partial t} - H x^a \frac{\partial}{\partial x^a}$$

$\vec{V}_{(F)}$

Sum Rules for Mass and
Tension in AdS / dS (?)

Cosmology (flat)

$$\vec{V} = \frac{\partial}{\partial t} - H x^a \frac{\partial}{\partial x^a}$$

MFVF

$$+ \vec{V}_{(F)}$$

$$\delta T^a_b n_a$$

Sum Rules for Mass and
Tension in AdS / dS (?)

Cosmology (flat)

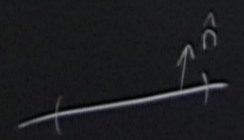
MFVF $\vec{V} = \frac{\partial}{\partial t} - H x^i \frac{\partial}{\partial x^i}$

$\int_{\text{Vol}} \delta T^a_b n_a V^b = \int$

Sum Rules for Mass and
Tension in AdS / dS (?)

Cosmology (flat)

MFVF $\vec{V} = \frac{\partial}{\partial t} - H x^i \frac{\partial}{\partial x^i}$

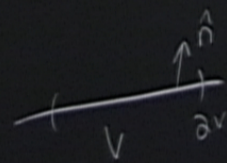


$\int_{Vol} \delta T^a_b n_a V^b = \int B^c da_c$

Sum Rules for Mass and
Tension in AdS / dS (?)

Cosmology (flat)

MFVF $\vec{V} = \frac{\partial}{\partial t} - H x^i \frac{\partial}{\partial x^i}$



+ $\vec{V}_{(E)}$
 $\int_{Vol} \delta T^a_b n_a V^b = \int B^c da_c$

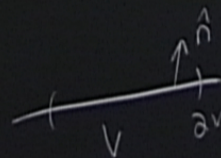
$\mathcal{Z}(k)$

Sum Rules for Mass and
Tension in AdS / dS (?)

MFVF

Cosmology (flat)

$$\vec{V} = \frac{\partial}{\partial t} - H x^i \frac{\partial}{\partial x^i}$$



$$\int_{\text{Vol}} \delta T^a_b n_a V^b = \int \mathcal{B}^c da_c$$

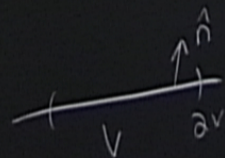
$$\zeta(k) \propto k^4 \quad k \rightarrow 0$$

Sum Rules for Mass and Tension in AdS / dS (?)

Cosmology (flat)

MFVF

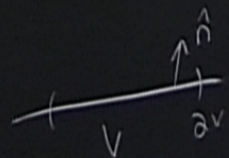
$$\vec{V} = \frac{\partial}{\partial t} - H x^i \frac{\partial}{\partial x^i}$$



$$\int_{\text{Vol}} \delta T^a_b n_a V^b = \int B^c da_c$$

$\zeta(k) \propto k^4 \quad k \rightarrow 0$
 Local Causal Perturbs
 $\Rightarrow B, T_i = 0$

MFVF

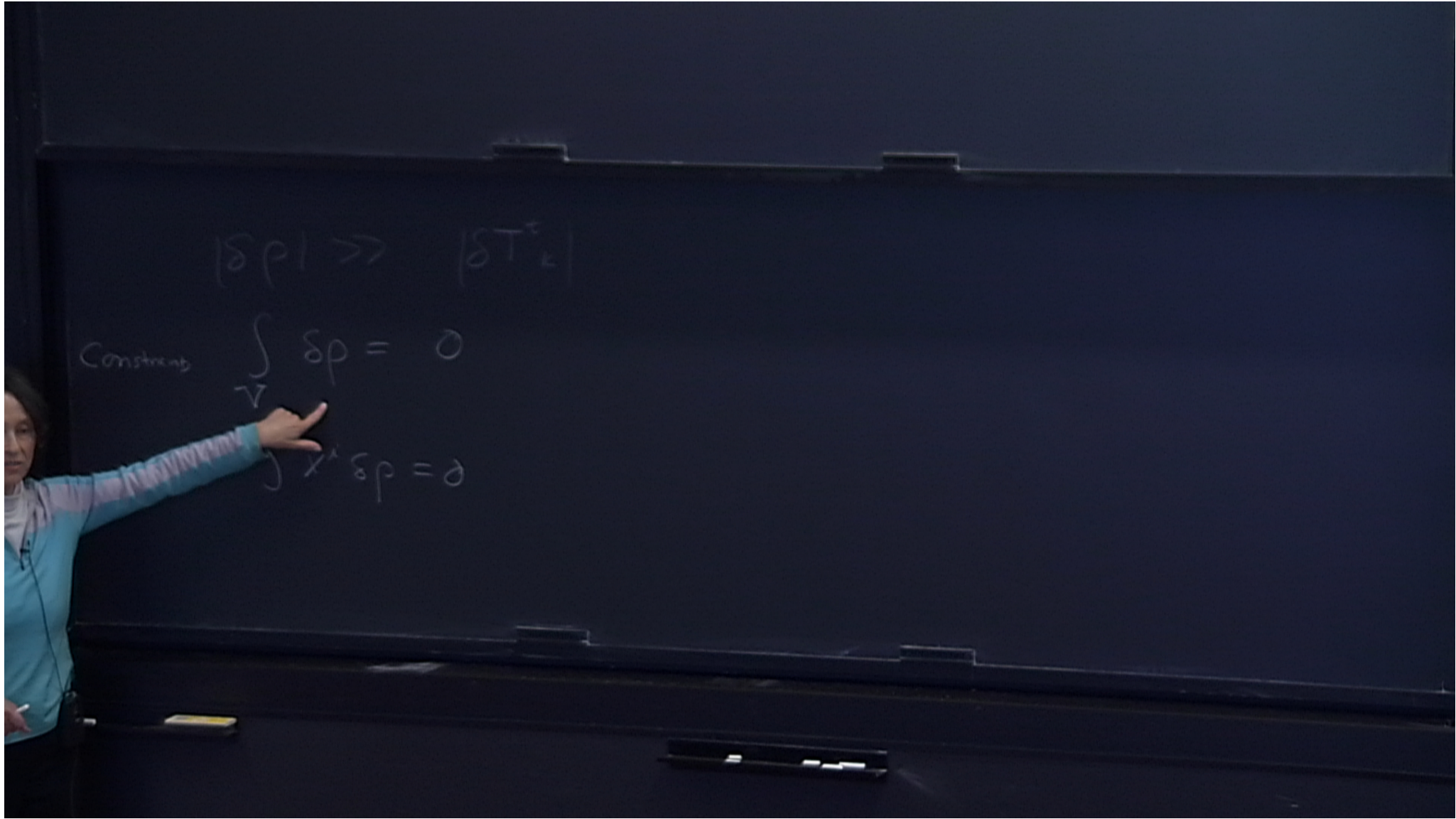


Sum Rules for Mass and Tension in AdS / dS (?)

Cosmology (flat)

$$\vec{V} = \frac{\partial}{\partial t} - H x^i \frac{\partial}{\partial x^i}$$

$$\int_{\text{Vol}} \delta T^a_b n_a V^b = \int B^c da_c$$

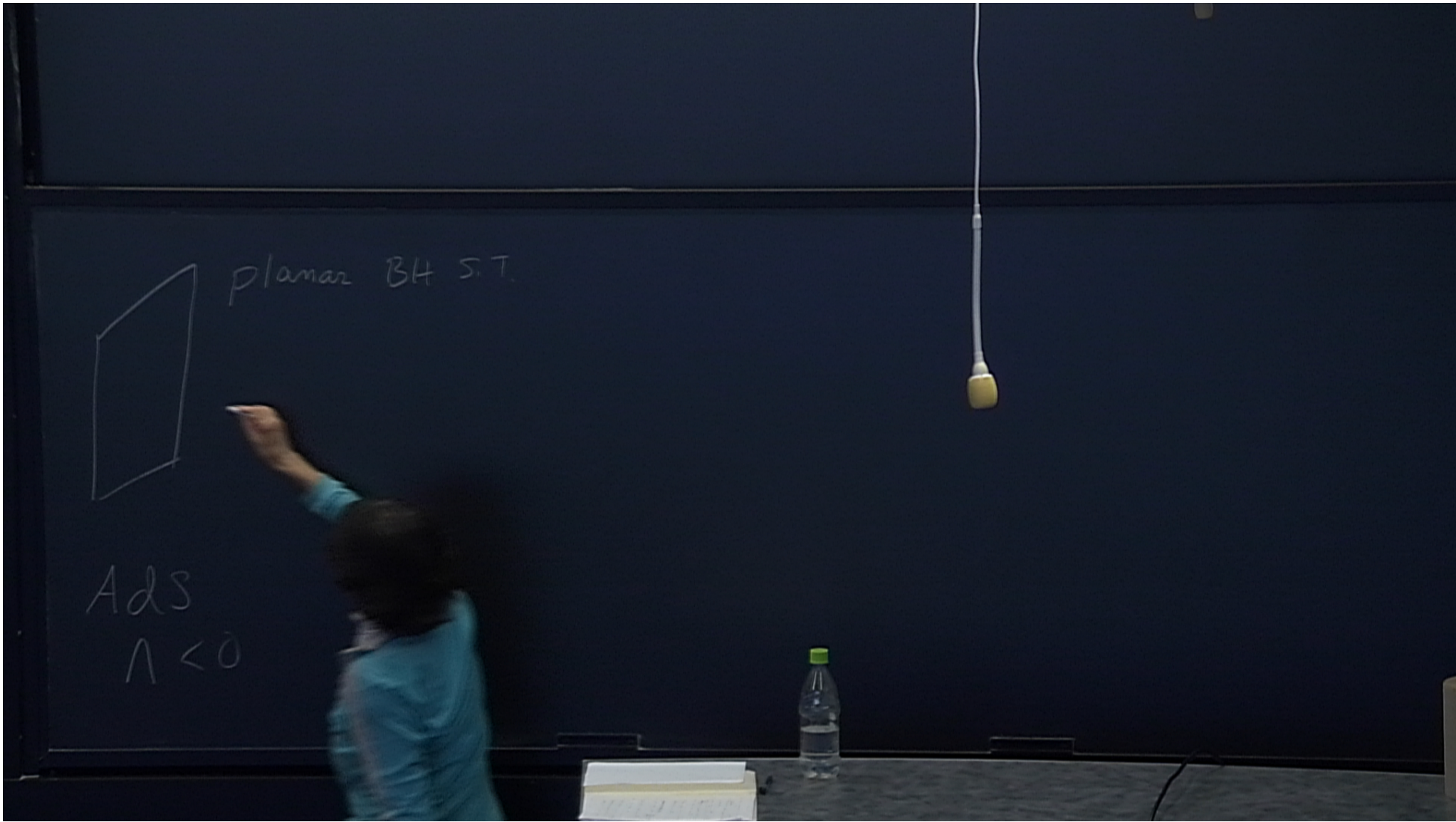


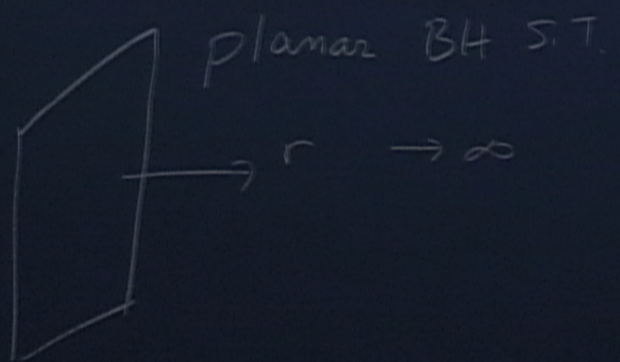
$$|\delta p| \gg |\delta T_c|$$

Constraints

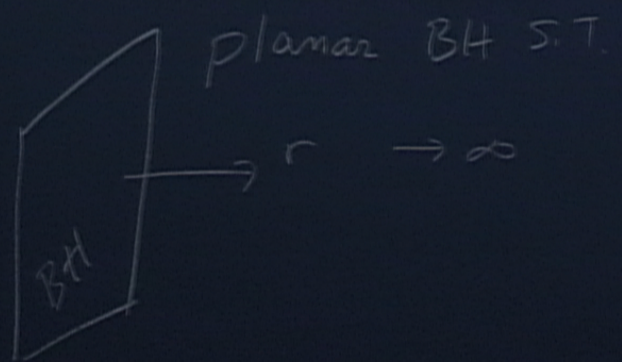
$$\int_V \delta p = 0$$

$$\int x^i \delta p = 0$$





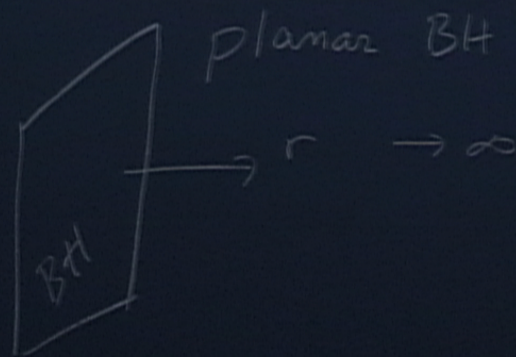
AdS
 $\Lambda < 0$



AdS
 $\Lambda < 0$



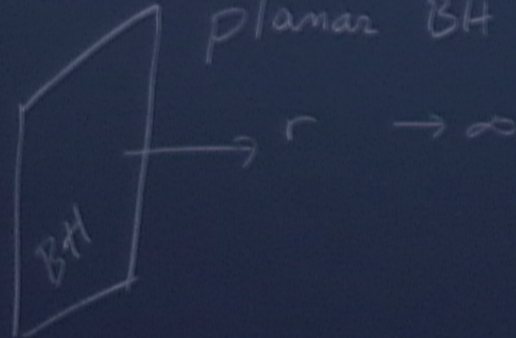
planar BH S.T. (Eke & Mahmoud)



$r \rightarrow \infty$

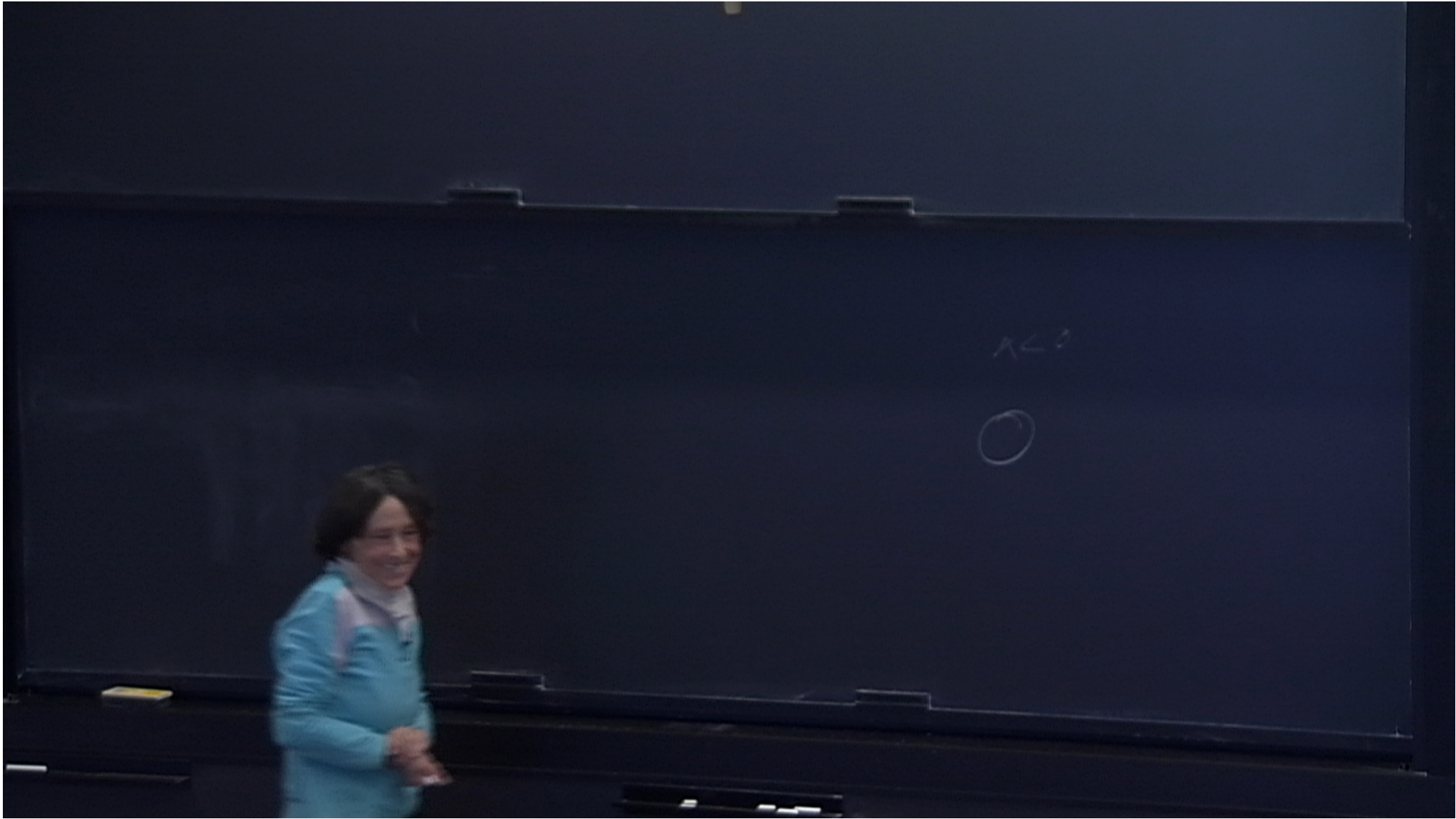
AdS
 $\Lambda < 0$

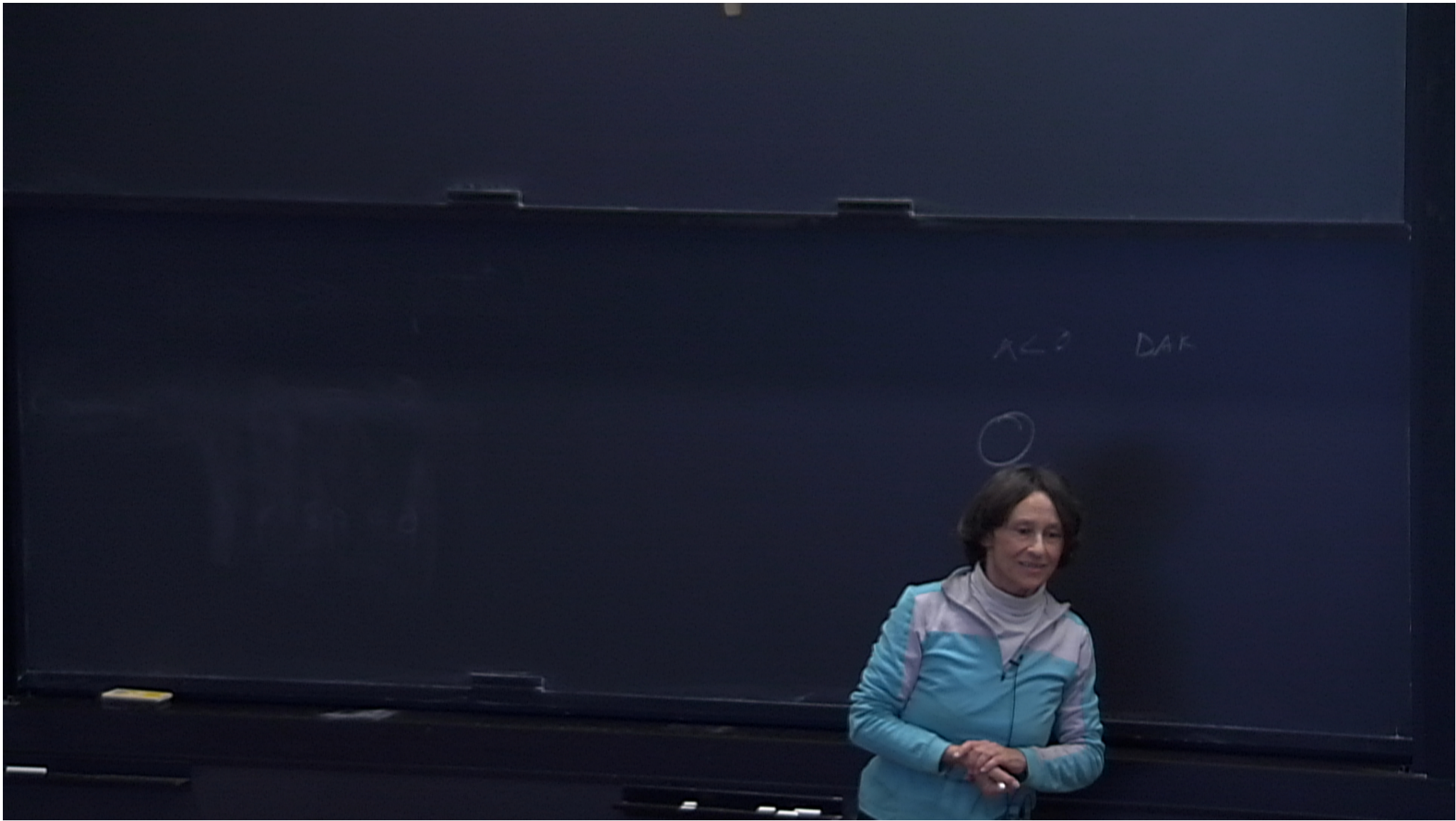
planar BH S.T. (Eke & Mahmoud)

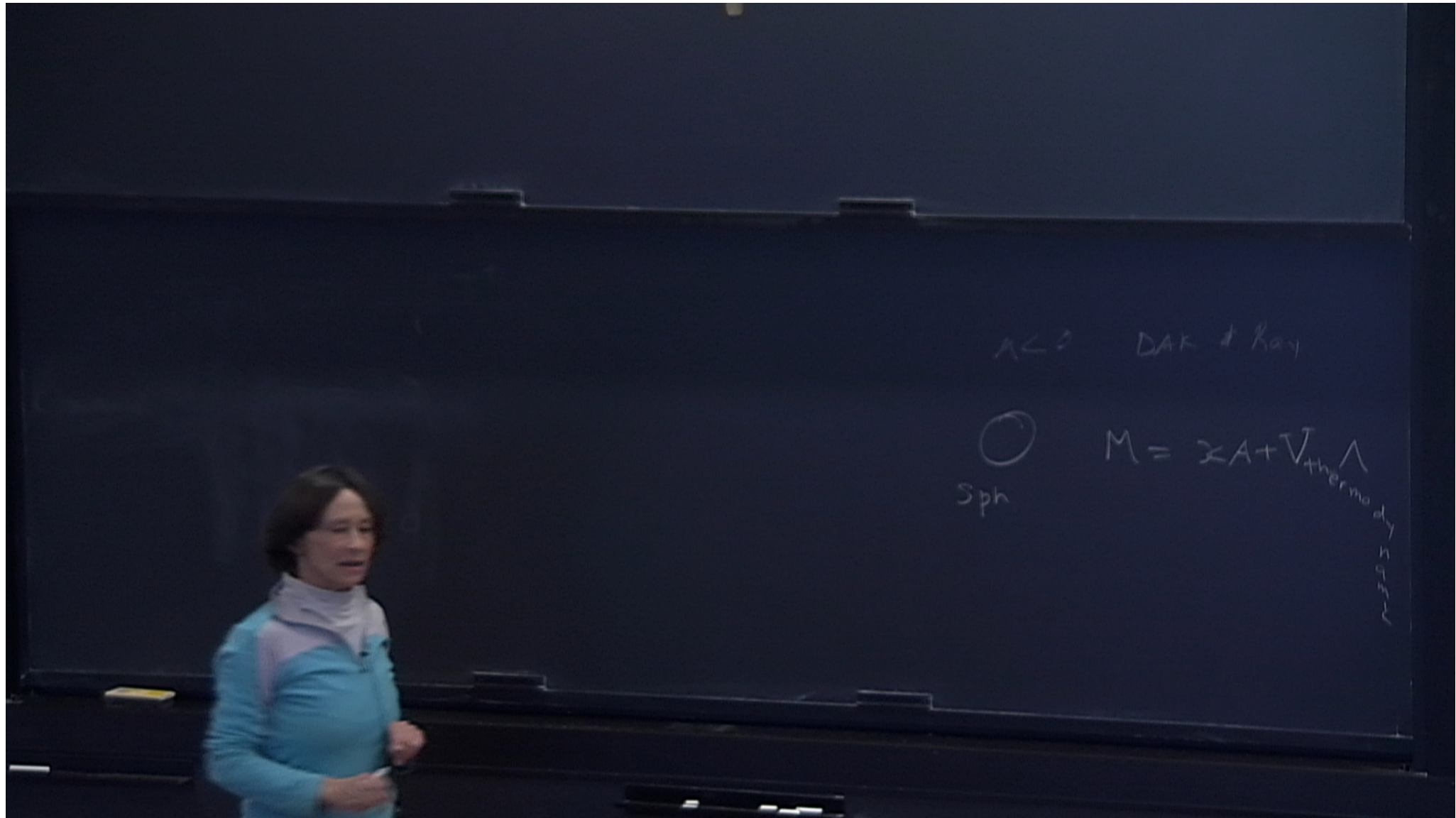


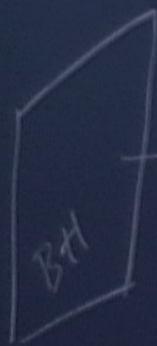
$r \rightarrow \infty$ $M = \frac{1}{2} A$

Ads
 $\Lambda < 0$





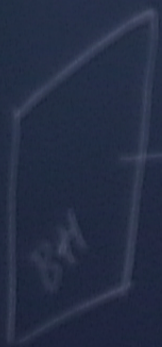




planar BH S.T. (Etk & Mahmoud)

$$M = \frac{\kappa A}{8\pi} + \frac{\Lambda V_{+h}}{8\pi}$$
$$Q$$

AdS
 $\Lambda < 0$

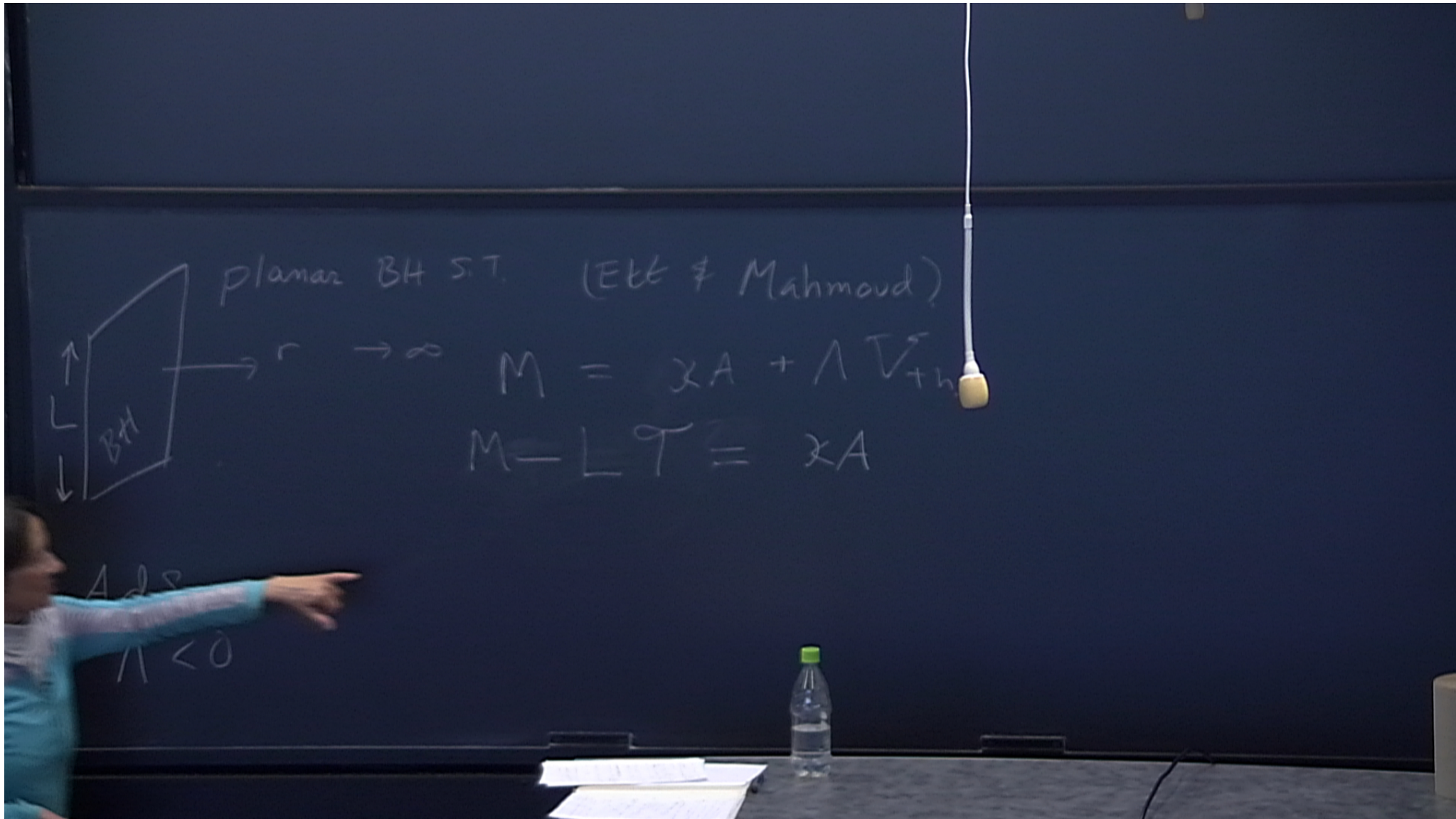


planar BH ST. (Ebb & Mahmoud)

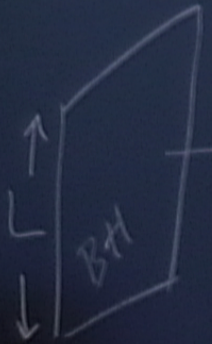
$$M = \chi A + \Lambda V_{+h}$$

$$M = L T = \chi A$$

AdS
 $\Lambda < 0$

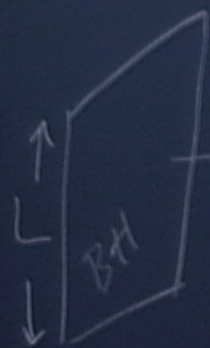


planar BH S.T. (Ekt & Mahmoud)



$$M = \chi A + \Lambda V_{+h}$$
$$M - L T = \chi A$$

$A > 0$
 $\Lambda < 0$



planar BH S.T. (Ekk & Mahmoud)

$$M = \chi A + \Lambda V_{+n}$$
$$M - LT = \chi A$$

AdS
 $\Lambda < 0$

1. Asympt Ads (planar)

$$M_{ADM} + L \Sigma$$

$A < 0$ DAK & Ray



Sph

$$M = \chi A + V_{\text{thermo}} \Lambda$$

1. Asympt Ads (planar)

$$M_{ADM} + L \sum_i T_i^{ADM} = 0$$

$$T_z = -p_z$$

$A < 0$ DAK & Ray



Sph

$$M = \chi A + V_{thermo} \Lambda$$

1. Asympt AdS (planar)

$$\textcircled{1} M_{\text{ADM}} + L \sum_i T_i^{\text{ADM}} = 0$$

Why — from GR

$\Lambda < 0$ DAK & Ray



Sph

$$M = \frac{\kappa}{8\pi} A + V_{\text{thermo}} \Lambda$$

1. Asympt Ads (planar)

$$\textcircled{P} M_{ADM} + L \sum_i T_i^{ADM} = 0$$

Why — from GR

2. Local version for
 $\delta p, \delta p_k$?

$\Lambda < 0$ DAK & Ray



Sph

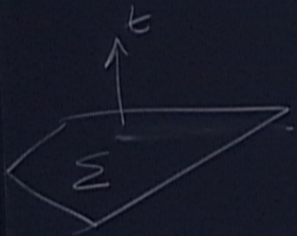
$$M = \frac{\kappa}{8\pi} A + V_{\text{thermo}} \Lambda$$

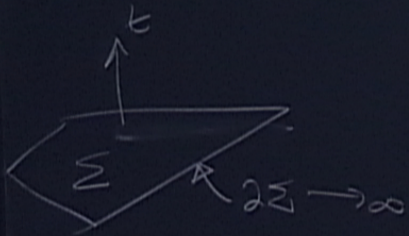
1. Asympt Ads (planar)

$$\textcircled{P} M_{ADM} + L \sum_i T_i^{ADM} = 0$$

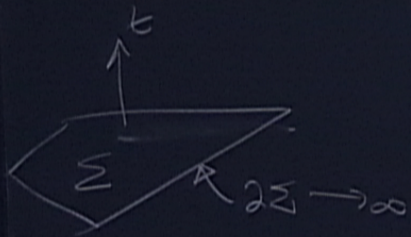
Why — from GR

2. Local version for
 $\delta p, \delta p_k?$

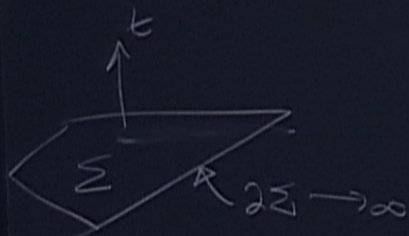




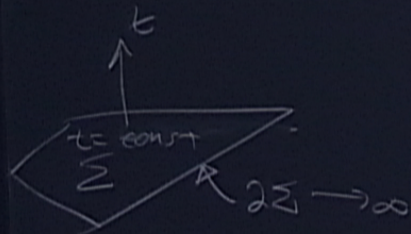
$$M_{ADM} = \int_{\partial(t=\text{const}), \infty} \partial(\delta q_{ab})$$



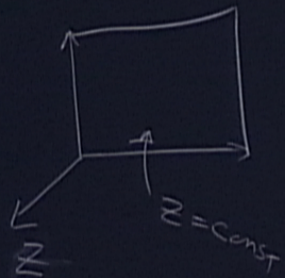
$$M_{ADM} = \int_{\partial(t=\text{const}), \infty} \partial(\delta q_{ab}; \frac{\partial}{\partial t})$$

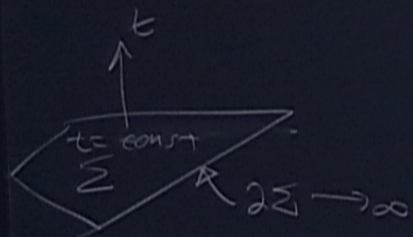


$$M_{ADM} = \int_{\partial(t=\text{const}), \infty} \partial(\delta q_{ab}; \frac{\partial}{\partial t}) = Q(\frac{\partial}{\partial t})$$

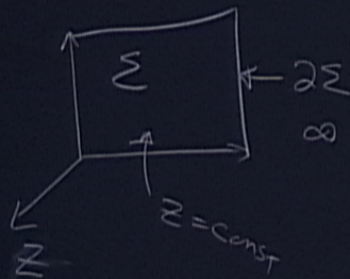


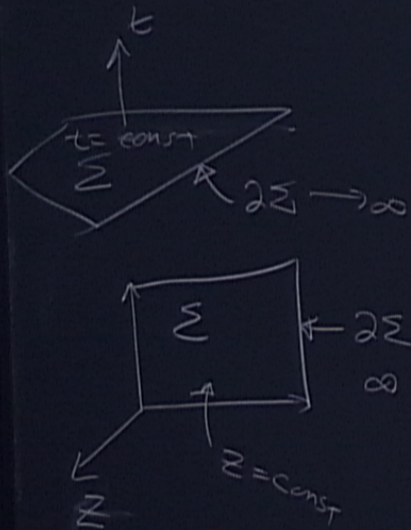
$$M_{\text{ADM}} = \int_{\partial(t=\text{const})_\infty} \partial(\delta q_{ab}; \frac{\partial}{\partial t}) = Q(\frac{\partial}{\partial t})$$





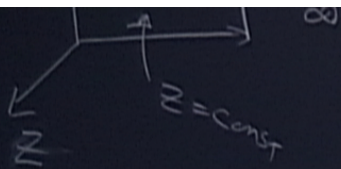
$$M_{ADM} = \int_{\Sigma(t=\text{const}), \infty} \partial(\delta g_{ab}; \frac{\partial}{\partial t}) = Q(\frac{\partial}{\partial t})$$





$$M_{ADM} = \int_{\partial(t=\text{const}), \infty} \mathcal{L}(\delta g_{ab}; \frac{\partial}{\partial t}) = Q(\frac{\partial}{\partial t})$$

$$T_z = \int_{\partial(z=\text{const}), \infty} \mathcal{L}(\delta g_{ab}; \frac{\partial}{\partial z}) = Q(\frac{\partial}{\partial z})$$



∞

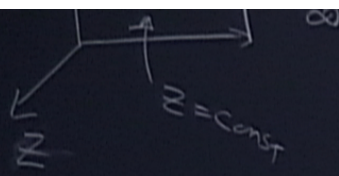
1. Asympt Ads (planar)

$$\textcircled{1} M_{ADM} + L \sum_i T_i^{ADM} = 0$$

Why — from GR

2. Localisation for
Sp, ...

ADM charges — defined at ∞



∞

1. Asympt Ads (planar)

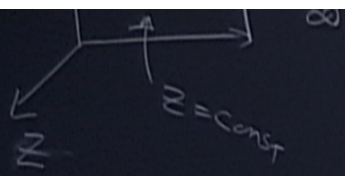
$$\textcircled{1} M_{ADM} + L \sum_i T_i^{ADM} = 0$$

Why from eq

2. Local for $\delta p, \delta p$

ADM charges — defined at ∞
Sources: $\Lambda = 0$

δp $\textcircled{2}$



∞

1. Asympt Ads (planar)

$$\textcircled{1} M_{ADM} + L \sum_i T_i^{ADM} = 0$$

Why for GR

2. Local version for

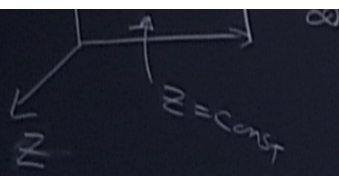
δp

ADM charges — defined at ∞

Sources: $\Lambda = 0$

→ Flat

δp $\textcircled{2}$



1. Asympt Ads (planar)

$$\textcircled{1} M_{ADM} + L \sum_i T_i^{ADM} = 0$$

Why from \mathcal{E}

2. Local \mathcal{E} for $\delta p, \delta$

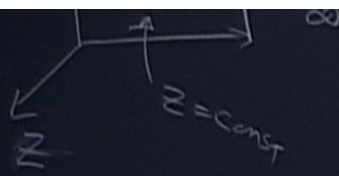
ADM charges — defined at ∞

Sources: $\Lambda = 0$

→ Flat

$$g_{ab} = \eta_{ab} + \delta g_{ab}$$

δp $\textcircled{2}$



1. Asympt Ads (planar)

$$\textcircled{1} M_{ADM} + L \sum_i T_i^{ADM} = 0$$

Why from GR

2. Linearization for

δp

ADM charges — defined at ∞

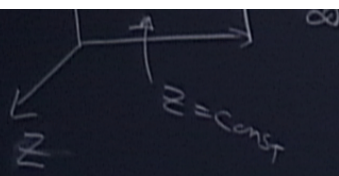
Sources: $\Lambda = 0$

→ Flat

$$g_{ab} = \eta_{ab} + \delta g_{ab}$$

$$a_i =$$

δp $\textcircled{2}$



∞

1. Asympt Ads (planar)

$$\textcircled{1} M_{ADM} + L \sum_i T_i^{ADM} = 0$$

Why from GR

2. local version for δp_k ?

ADM charges — defined at ∞

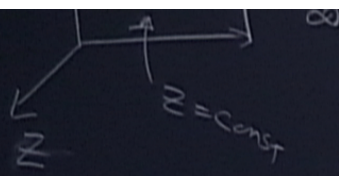
Sources: $\Lambda = 0$

→ Flat

$$g_{ab} = \gamma_{ab} + \delta g_{ab}$$

δp @

$$a_i = \int_{vol} \delta p$$



1. Asympt Ads (planar)

$$\textcircled{1} M_{ADM} + L \sum_i T_i^{ADM} = 0$$

Why from GR

2. Local version for $\delta\rho, \delta p_k$?

ADM charges — defined at ∞

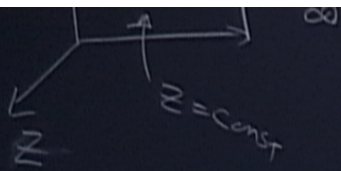
Sources: $\Lambda = 0$

→ Flat

$\delta\rho$ $\textcircled{2}$

$$g_{ab} = \eta_{ab} + \delta g_{ab}$$

$$a_i = \int_{vol} \delta\rho \quad \Rightarrow \quad M_{ADM}$$



∞

1. Asympt Ads (planar)

$$\textcircled{1} M_{ADM} + L \sum_i T_i^{ADM} = 0$$

Why — from GR

2. Local version for $\delta p, \delta p_k$?

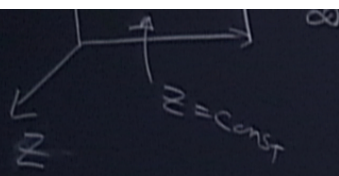
→ Flat



ADM charges — defined at ∞

Sources: $\Lambda = 0$; KK —

$$g_{ab} = \gamma_{ab} + \delta g_{ab}$$



1. Asympt Ads (planar)

$$\textcircled{1} M_{ADM} + L \sum_i T_i^{ADM} = 0$$

Why — from GR

2. Local version for $\delta p, \delta p_k$?

ADM charges — defined at ∞

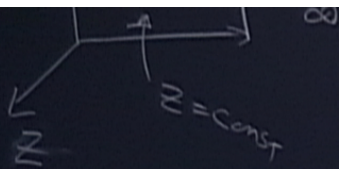
Sources: $\Lambda = 0$; KK —

→ Flat



$$g_{ab} = \gamma_{ab} + \delta g_{ab}$$

$\delta p, \delta p_i$



∞

1. Asympt Ads (planar)

$$\textcircled{1} M_{ADM} + L \sum_i T_i^{ADM} = 0$$

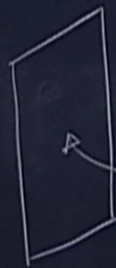
Why — from GR

2. Local version for $\delta p, \delta p_k$?

ADM charges — defined at ∞

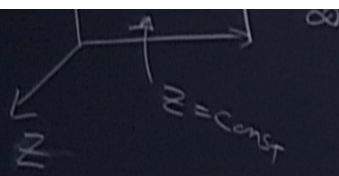
Sources: $\Lambda = 0$; KK

→ Flat



$\delta p, \delta p_x, \delta p_y$

$$g_{ab} = \gamma_{ab} + \delta g_{ab}$$



1. Asympt Ads (planar)

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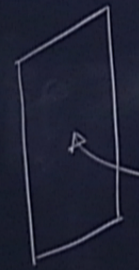
Why from GR

2. Local version for δp_k ?

ADM charges — defined at ∞

Sources: $\Lambda = 0$; KK

→ Flat

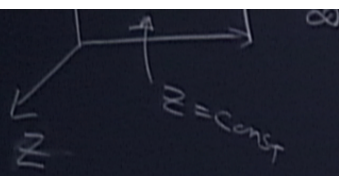


$$g_{ab} = \eta_{ab} + \delta g_{ab}$$

$$a_1 = \int \delta p = M$$

$$a_2 = \int \delta p_x = -Q_x$$

$$a_3 = \int \delta p_y = -Q_y$$



1. Asympt Ads (planar)

$$\textcircled{P} M_{ADM} + L \sum_i T_i^{ADM} = 0$$

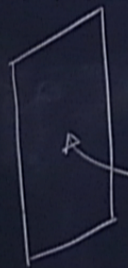
Why - from GR

2. Local v for
 $\delta p, \delta p_x, \delta p_y$

ADM charges - defined at ∞

Sources: $\Lambda = 0$; KK - Hartman & Obers

→ Flat

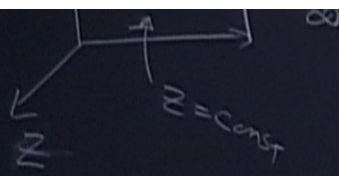


$$g_{ab} = \eta_{ab} + \delta g_{ab}$$

$$a_1 = \int \delta p = M$$

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$$a_3 = \int \delta p_y = -Q_y$$



∞

1. Asympt Ads (planar)

$$\textcircled{1} M_{ADM} + L \sum_i T_i^{ADM} = 0$$

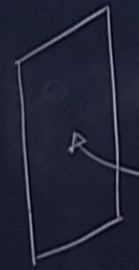
Why from GR

2. Local version for $\delta p, \delta p_k$?

ADM charges — defined at ∞

Sources: $\Lambda = 0$; KK — Harmant & Obers

→ Flat



$$g_{ab} = \eta_{ab} + \delta g_{ab}$$

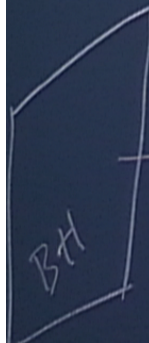
J, T, DK, P_{at}

$$a_1 = \int \delta p = M$$

$$a_2 = \int \delta p_x = -Q_x$$

$$a_3 = \int \delta p_y = -Q_y$$

planar BH S.T. (Ekk & Mahmoud)



$$M = \chi A + \Lambda V_{+h}$$

$$M - LT = \chi A$$

M_{soliton}

Ads
 $\Lambda < 0$

BH

$r \rightarrow \infty$

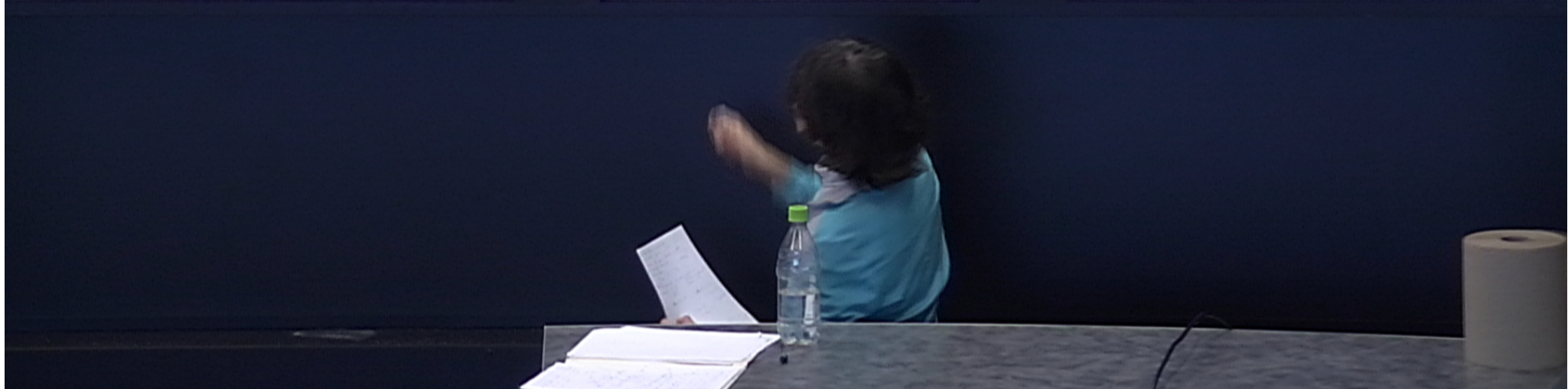
$$M = \chi A + \Lambda V_{+h}$$

$$M - L T = \chi A$$

$$M_{\text{soliton}} < 0 < M_{\text{BH}}$$

$$M = (D-2)\hat{A}$$

AdS
 $\Lambda < 0$



BH

$r \rightarrow \infty$

$$M = \chi A + \Lambda V_{+h}$$

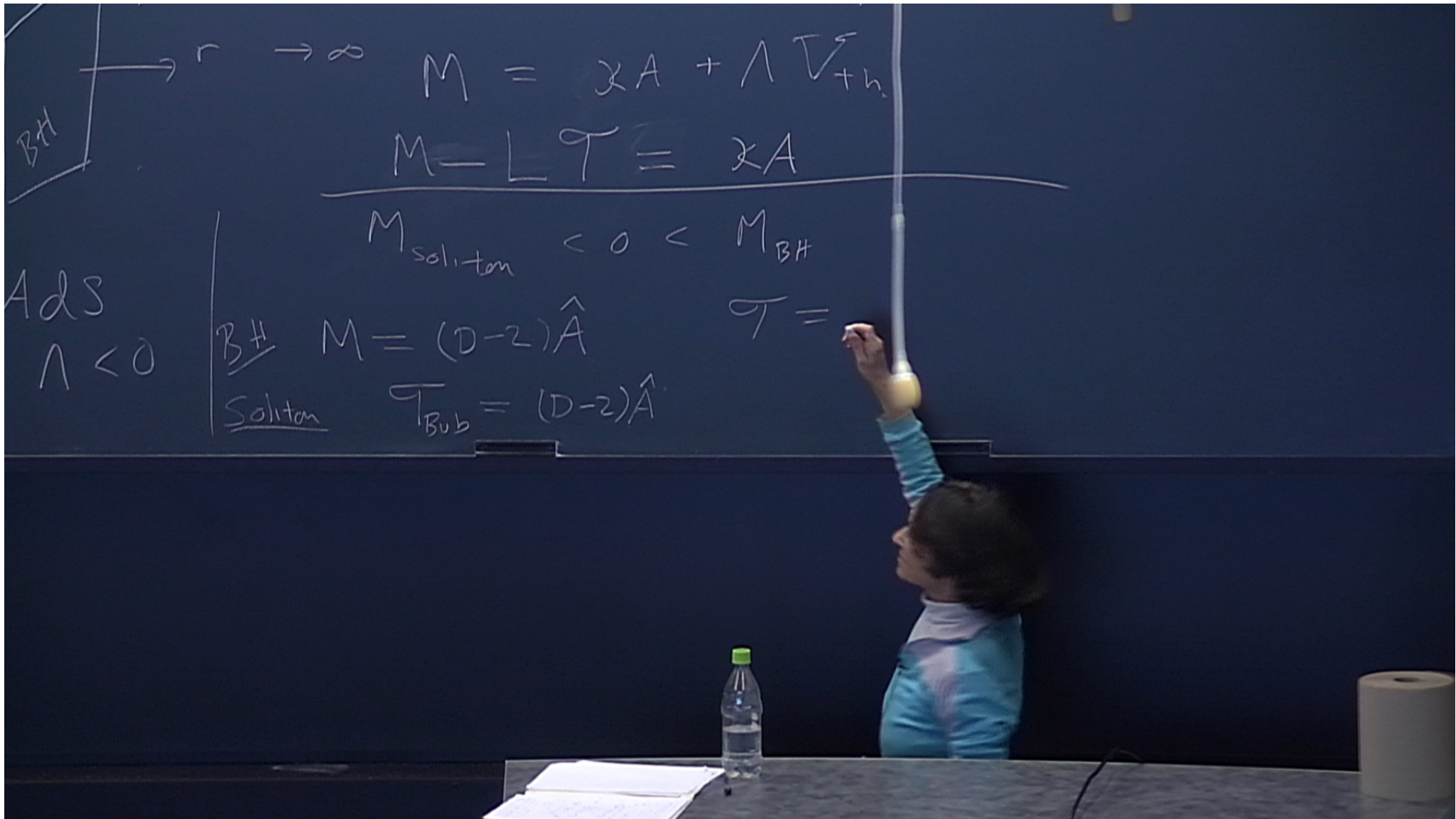
$$M - LT = \chi A$$

$$M_{\text{soliton}} < 0 < M_{\text{BH}}$$

AdS $\Lambda < 0$

BH	$M = (D-2)\hat{A}$
Soliton	\mathcal{Q}





BH

$$\rightarrow r \rightarrow \infty \quad M = \chi A + \Lambda V_{+h}$$

$$M - LT = \chi A$$

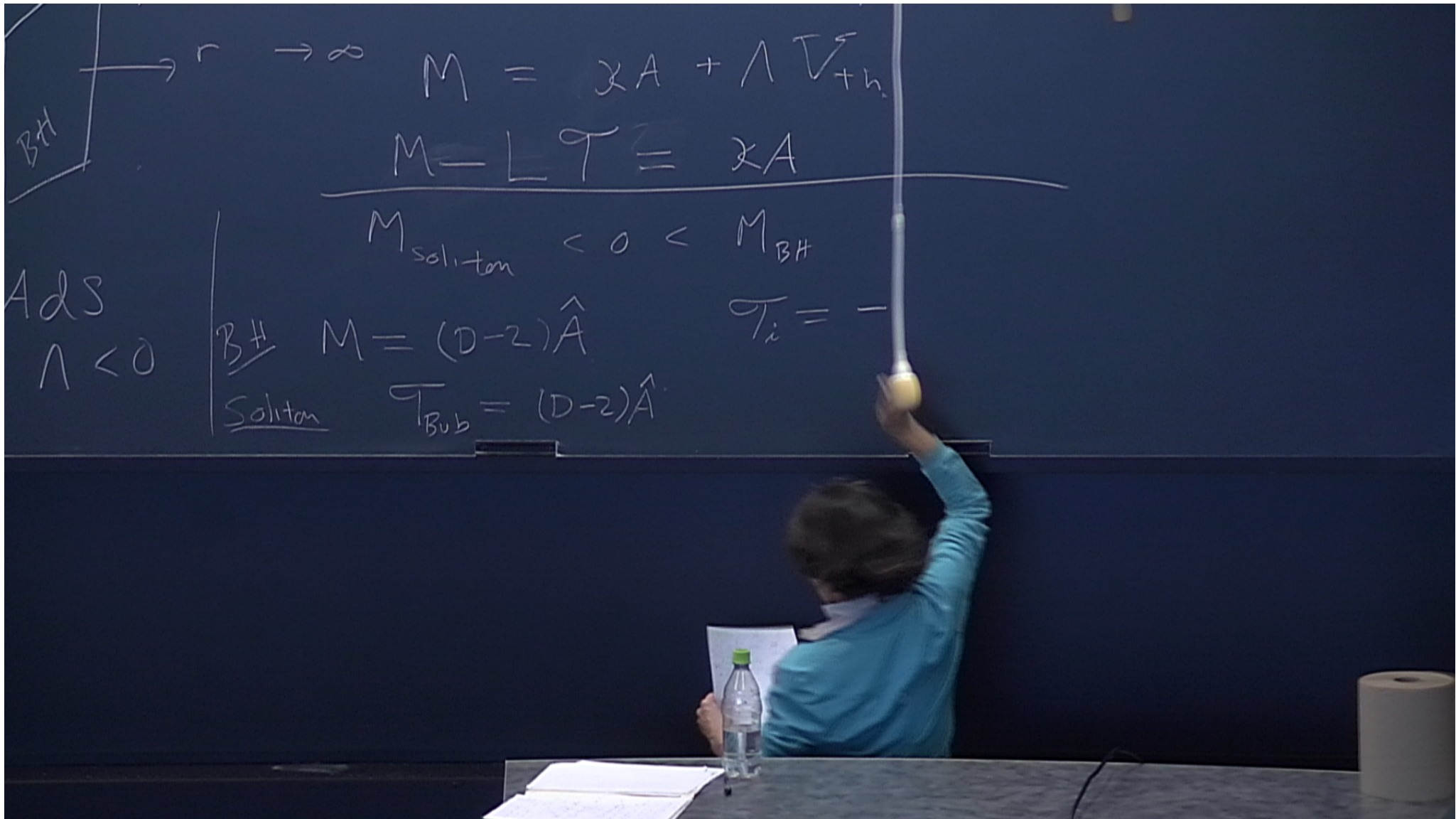
$$M_{\text{soliton}} < 0 < M_{\text{BH}}$$

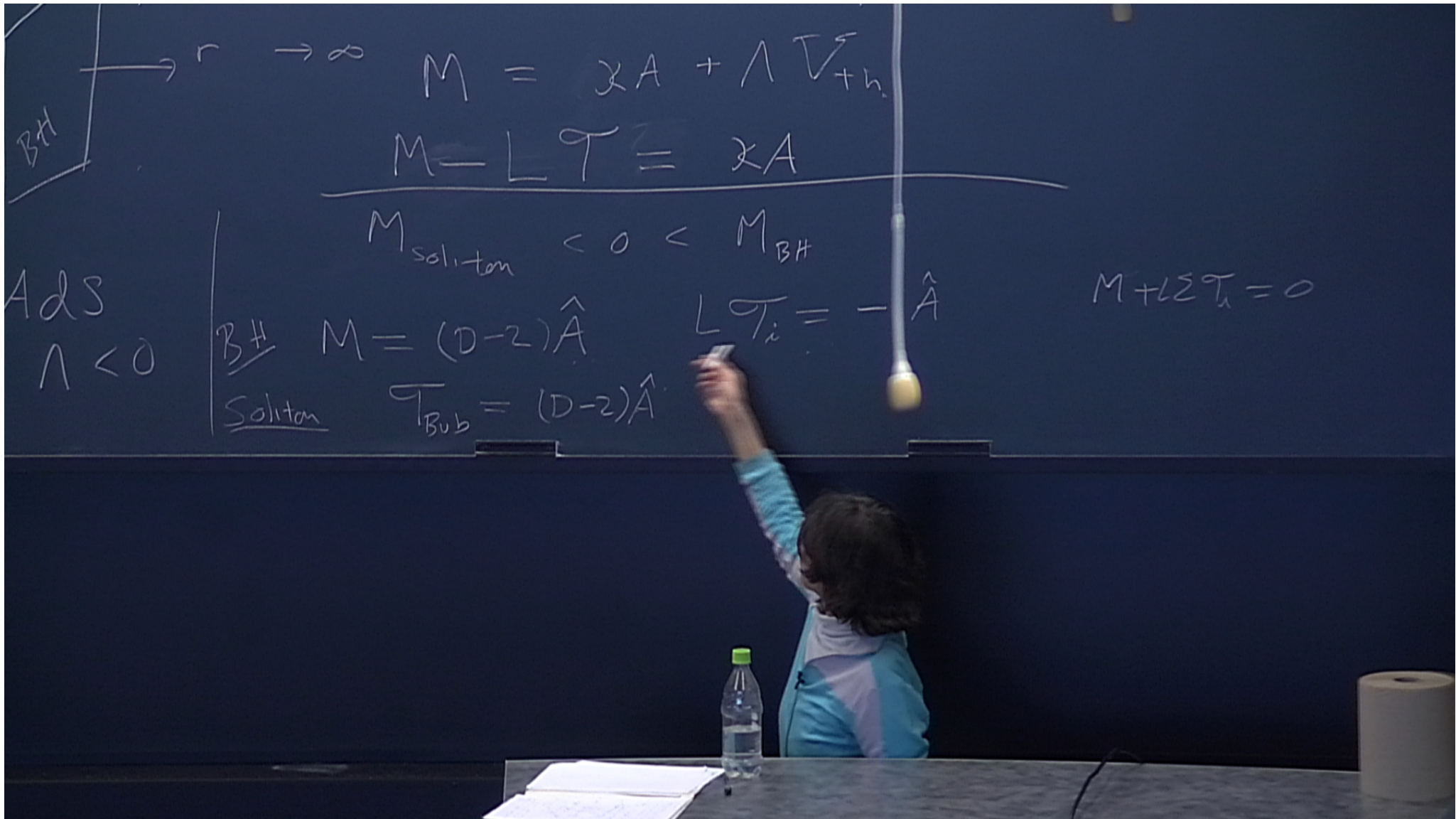
AdS
 $\Lambda < 0$

BH $M = (D-2)\hat{A}$

Soliton $T_{\text{Bub}} = (D-2)\hat{A}$

$$T =$$







Ads
 $\Lambda < 0$

$$M_{\text{soliton}} < 0 < M_{\text{BH}}$$

$$L \mathcal{T}_i = -\hat{A}$$

$$M + L \mathcal{T}_i = 0$$

<u>BH</u>	$M = (D-2)\hat{A}$
<u>Soliton</u>	$\mathcal{T}_{\text{Bub}} = (D-2)\hat{A}$

$$M = L \mathcal{T}_i = -\hat{A}$$





Ads
 $\Lambda < 0$

$$M_{\text{soliton}} < 0 < M_{\text{BH}}$$

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Ads
 $\Lambda < 0$

BH $M = (D-2)\hat{A}$

Soliton $T_{Bub} = (D-2)\hat{A}$

$L T_i = -\hat{A}$

$M + L^2 T_i = 0$

$M = L^2 T_i = -\hat{A}$

Asympt Ads

$$ds^2 = \frac{r^2}{l^2} \left[\frac{M}{\alpha\beta} + \frac{C_{\alpha\beta}}{r^{D-1}} \right] dx^\alpha dx^\beta + \frac{l^2}{r^2} \left(1 + \frac{C_r}{r^{D-1}} \right) dr^2$$

Ads
 $\Lambda < 0$

BH $M = (D-2)\hat{A}$

Soliton $T_{Bub} = (D-2)\hat{A}$

$L T_i = -\hat{A}$

$M = L T_i = -\hat{A}$

$M + L T_i = 0$

Asympt Ads

$$ds^2 \rightarrow \frac{r^2}{l^2} \left[\eta_{\alpha\beta} + \frac{C_{\alpha\beta}}{r^{D-1}} \right] dx^\alpha dx^\beta + \frac{l^2}{r^2} \left(1 + \frac{C_r}{r^{D-1}} \right)$$

AdS
 $\Lambda < 0$

BH $M = (D-2)\hat{A}$

Soliton $T_{Bub} = (D-2)\hat{A}$

$L T_i = -\hat{A}$

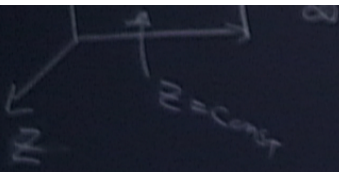
$M + L^2 T_i = 0$

$M = L T_i = -\hat{A}$

Asympt AdS
Sols.

$$ds^2 \rightarrow \frac{r^2}{l^2} \left[\gamma_{\alpha\beta} + \frac{C_{\alpha\beta}}{r^{D-1}} \right] dx^\alpha dx^\beta + \frac{l^2}{r^2} \left(1 + \frac{C_r}{r^{D-1}} \right)$$

Sat \textcircled{T}



∞

1. Asympt Ads (planar)

$$\textcircled{1} M_{ADM} + L \sum_i T_i^{ADM} = 0$$

Why from GR

2. Local version for $\delta p, \delta p_k$?

ADM charges — defined at ∞

Sources: $\Lambda = 0$; KK — Hartman & Obers
 J, T, DK, P_{α}

→ Flat



$$g_{ab} = \eta_{ab} + \delta g_{ab}$$

$\delta p, \delta p_x, \delta p_y$

$$a_1 = \int \delta p = M$$

$$a_2 = \int \delta p_x = -Q_x$$

$$a_3 = \int \delta p_y = -Q_y$$

Ads
 $\Lambda < 0$

BH $M = (D-2)\hat{A}$

Soliton $T_{Bub} = (D-2)\hat{A}$

$L T_i = -\hat{A}$

$M + L \Sigma T_i = 0$

$M = L T_i = -\hat{A}$

Asympt AdS
Sols

$$ds^2 \rightarrow \frac{r^2}{l^2} \left[\eta_{\alpha\beta} + \frac{C_{\alpha\beta}}{r^{D-1}} \right] dx^\alpha dx^\beta + \frac{l^2}{r^2} \left(1 + \frac{C_r}{r^{D-1}} \right) dr^2$$

Sat \textcircled{T}

$$\vec{V} = x^\alpha \frac{\partial}{\partial x^\alpha} - r \frac{\partial}{\partial r}$$

Ads
 $\Lambda < 0$

soliton BH

$$M = (D-2)\hat{A} \quad L\mathcal{T}_i = -\hat{A} \quad M + L\mathcal{T}_i = 0$$

Soliton

$$\mathcal{T}_{Bub} = (D-2)\hat{A} \quad M = \mathcal{T}_i = -\hat{A}$$

Asympt
 Sols

$$ds^2 \rightarrow \frac{r^2}{l^2} \left[\eta_{\alpha\beta} + \frac{C_{\alpha\beta}}{r^{D-1}} \right] dx^\alpha dx^\beta + \frac{l^2}{r^2} \left(1 + \frac{C_r}{r^{D-1}} \right)$$

Sat \textcircled{T}

$$\vec{V} = x^\alpha \frac{\partial}{\partial x^\alpha} - r \frac{\partial}{\partial r} \quad KV \quad Ads$$

Ads
 $\Lambda < 0$

BH $M = (D-2)\hat{A}$

Soliton $T_{Bub} = (D-2)\hat{A}$

$L T_i = -\hat{A}$

$M = T_i = -\hat{A}$

$M + L \Sigma T_i = 0$

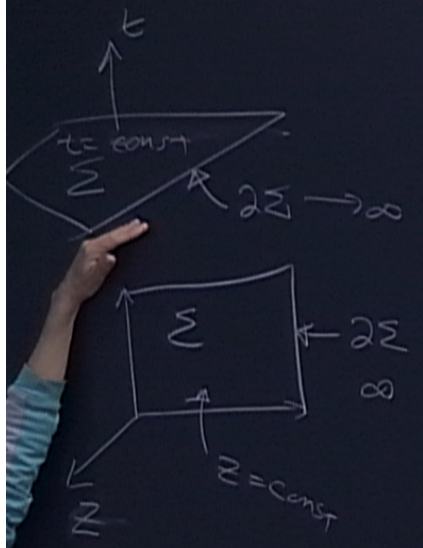
Asympt Ads Sols $ds^2 \rightarrow \frac{r^2}{l^2} \left[\frac{M}{r^2} + \frac{C_{\alpha\beta}}{r^{D-1}} \right] dx^\alpha dx^\beta + \frac{l^2}{r^2} \left(1 + \frac{C_r}{r^{D-1}} \right)$

Sat $\vec{V} = x^\alpha \frac{\partial}{\partial x^\alpha} - r \frac{\partial}{\partial r}$ KV Ads

Conformal isom.

$$M_{ADM} = \int_{\Sigma(t=\text{const}), \infty} \mathcal{L}(\delta g_{ab}; \frac{\partial}{\partial t}) = Q(\frac{\partial}{\partial t})$$

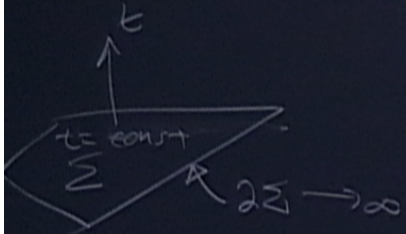
$$Q_z = \int_{\Sigma(z=\text{const})} \mathcal{L}(\delta g_{ab}; \frac{\partial}{\partial z}) = Q(\frac{\partial}{\partial z})$$



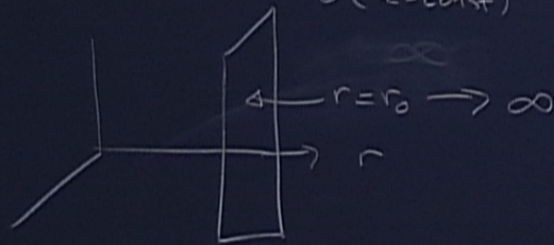
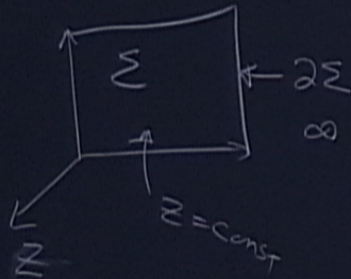
$\delta p, \delta p_k$

$$Q_3 = \int \delta p_x = -Q_x$$

$$M_{ADM} = \int_{\Sigma(t=\text{const})} \mathcal{L}(\delta g_{ab}; \frac{\partial}{\partial t}) = Q(\frac{\partial}{\partial t})$$



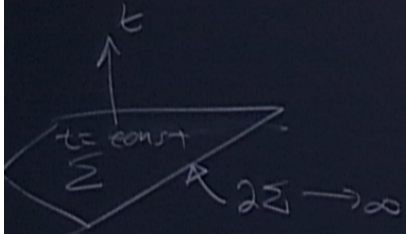
$$Q_z = \int_{\Sigma(z=\text{const})} \mathcal{L}(\delta g_{ab}; \frac{\partial}{\partial z}) = Q(\frac{\partial}{\partial z})$$



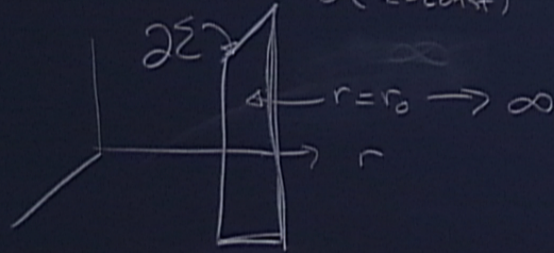
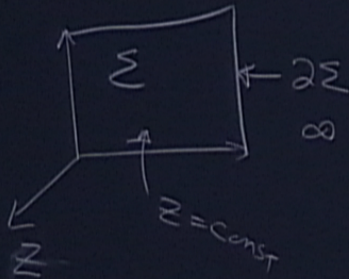
$\delta p_i, \delta p_k$

$$a_3 = \int \delta p_x = -Q_x$$

$$M_{ADM} = \int_{\Sigma(t=\text{const}, \infty)} \mathcal{L}(\delta g_{ab}; \frac{\partial}{\partial t}) = Q(\frac{\partial}{\partial t})$$

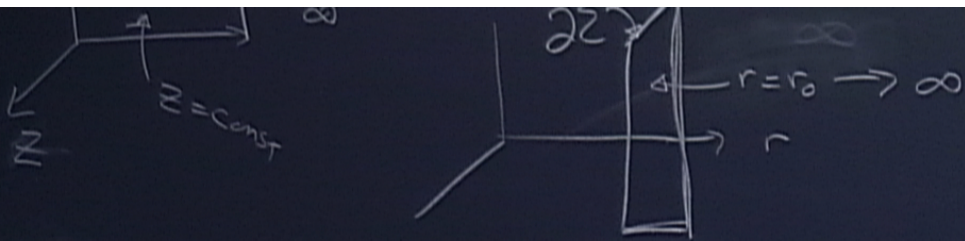


$$T_z = \int_{\Sigma(z=\text{const}, \infty)} \mathcal{L}(\delta g_{ab}; \frac{\partial}{\partial z}) = Q(\frac{\partial}{\partial z})$$



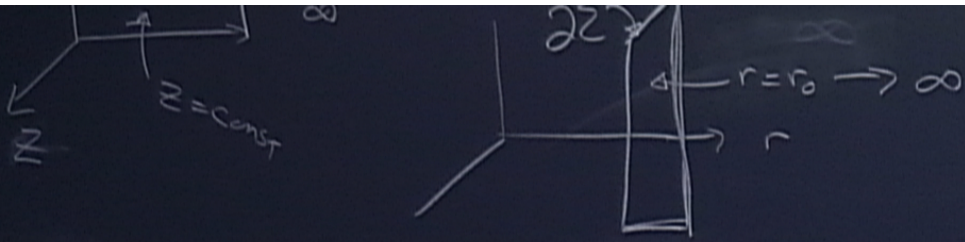
$\delta p_j, \delta p_k$

$$a_3 = \int \delta p_j = -\frac{q}{T}$$



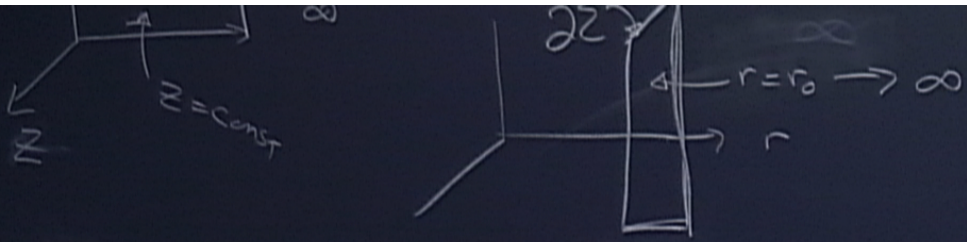
$$\int_{\text{Vol}} \delta T^a_b W^b_{wa} = \int_{\text{Vol}} D_a B^a + \int_{\text{Vol}} (\text{PDEs})$$

\uparrow
 on Sols



$$0 = \int_{\text{Vol}} \delta T^a_b W^b_{wa} = \int_{\text{Vol}} D_a B^a + \int_{\text{Vol}} (\text{PDEs})$$

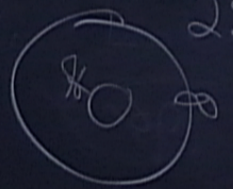
↑ on Sols
 ↑ 0



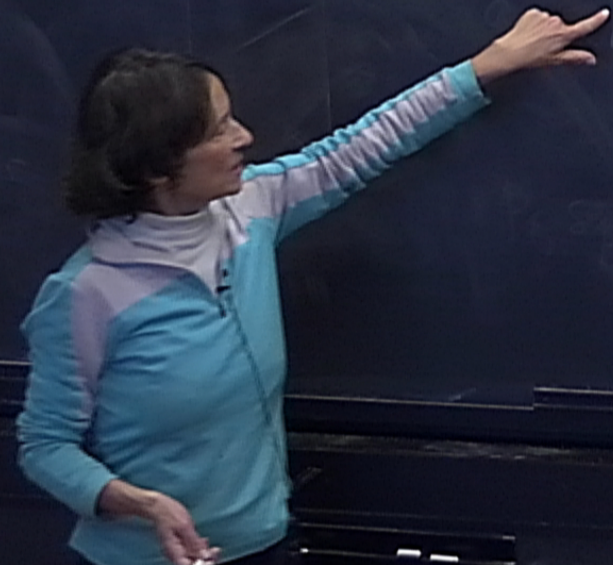
$$0 = \int_{Vol} \delta T^a_b W^b_{wa} = \int_{Vol} D_a B^a + \int_{Vol} (PDEs)$$

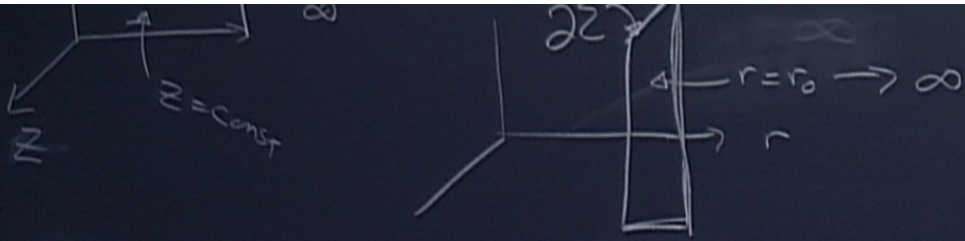
\uparrow
 on Sols

$$\Rightarrow \int_{\Sigma_{Tot}} B^c da_c = 0$$



||
0

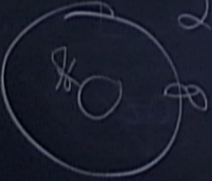




$$0 = \int_{Vol} \delta T^a_b W^b_{wa} = \int_{Vol} D_a B^a + \int_{Vol} (PDEs)$$

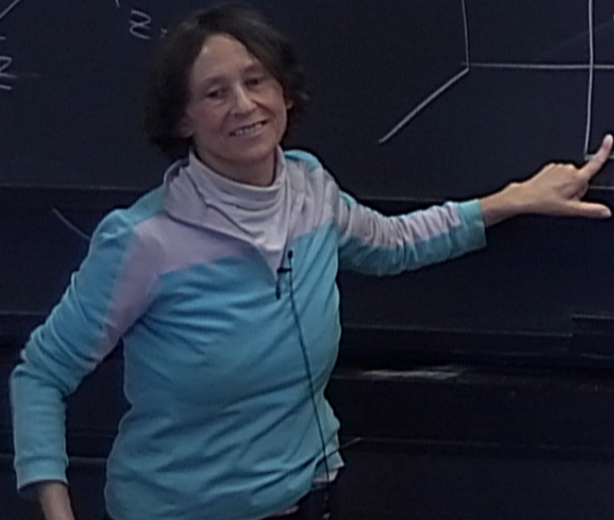
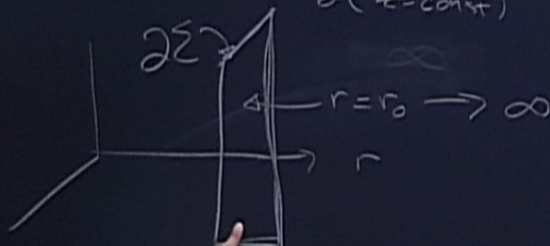
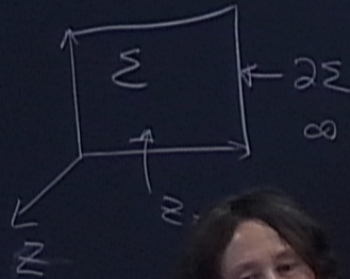
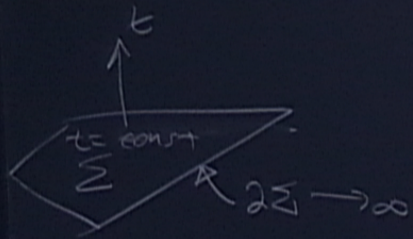
\uparrow on Sols $\underbrace{\hspace{10em}}$ \downarrow 0

\vec{W} KV for Vac, or Λ

$$\Rightarrow \int_{\Sigma_{Tot}} B^c da_c = 0$$


$$M_{ADM} = \int_{\Sigma(t=\text{const})} \mathcal{L}(\delta g_{ab}; \frac{\partial}{\partial t}) = Q(\frac{\partial}{\partial t})$$

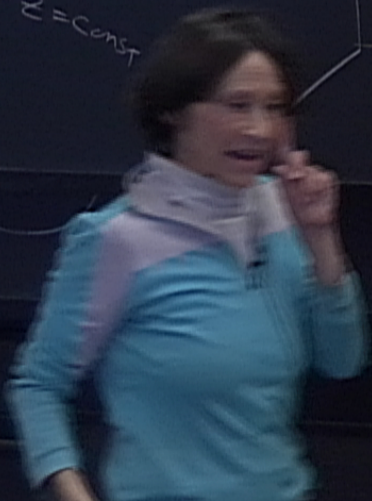
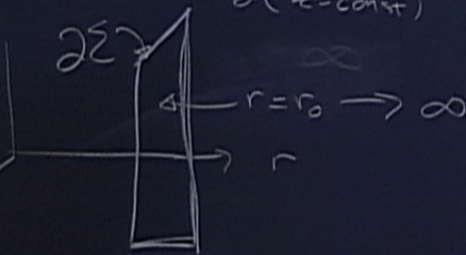
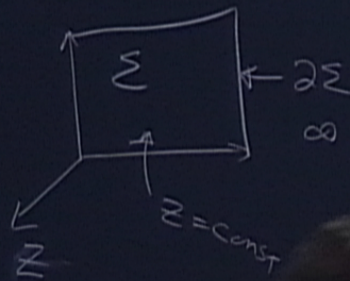
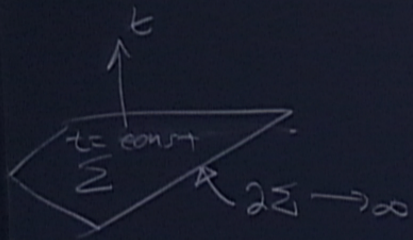
$$T_z = \int_{\Sigma(z=\text{const})} \mathcal{L}(\delta g_{ab}; \frac{\partial}{\partial z}) = Q(\frac{\partial}{\partial z})$$



$$M_{ADM} = \int_{\Sigma(t=\text{const})} \mathcal{L}(g_{ab}; \frac{\partial}{\partial t}) = Q(\frac{\partial}{\partial t})$$

$$T_z = \int_{\Sigma(z=\text{const})} \mathcal{L}(g_{ab}; \frac{\partial}{\partial z}) = Q(\frac{\partial}{\partial z})$$

$$\int_{\Sigma} B^c da_c = 0$$

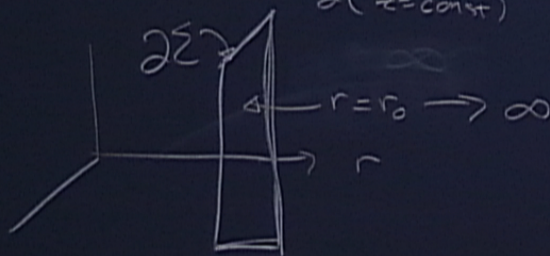
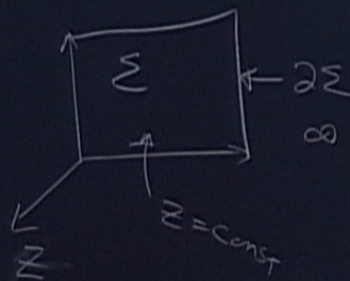
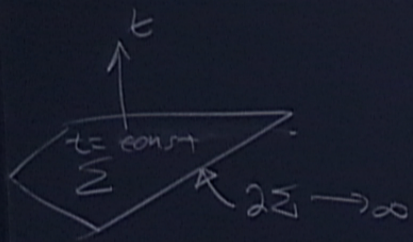


$$M_{ADM} = \int_{\Sigma(t=\text{const})} \mathcal{L}(g_{ab}; \frac{\partial}{\partial t}) = Q(\frac{\partial}{\partial t})$$

$$T_z = \int_{\Sigma(z=\text{const})} \mathcal{L}(g_{ab}; \frac{\partial}{\partial z}) = Q(\frac{\partial}{\partial z})$$

$$Q(\vec{\nabla}) = \int_{\Sigma} B^c da_c = 0$$

Scaling ∇



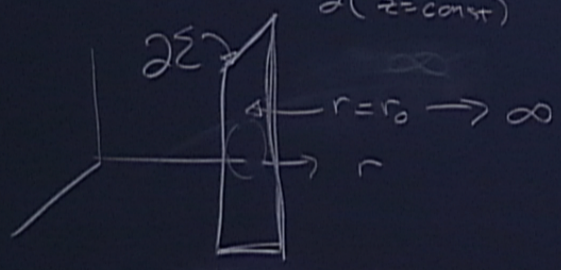
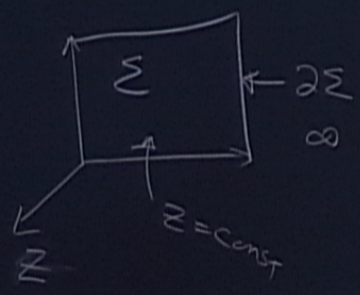
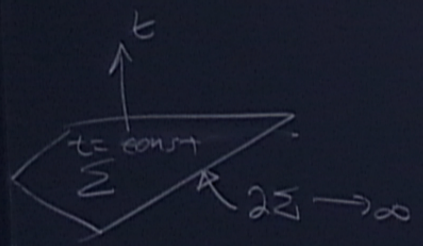
$$M_{ADM} = \int_{\Sigma(t=\text{const})} \mathcal{L}(\delta g_{ab}; \frac{\partial}{\partial t}) = Q(\frac{\partial}{\partial t})$$

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$$Q(\vec{\nabla}) = \int_{\Sigma} B^c da_c = 0$$

Scaling \uparrow ∇

$$M + L \sum T_i$$



Ads
 $\Lambda < 0$

BH $M = (D-2)\hat{A}$

$L T_i = -\hat{A}$

$M + L^2 T_i = 0$

Soliton $T_{\text{Bub}} = (D-2)\hat{A}$

$M = L T_i = -\hat{A}$

Asympt Ads
 Sols

$$ds^2 \rightarrow \frac{r^2}{l^2} \left[\gamma_{\alpha\beta} + \frac{C_{\alpha\beta}(x)}{r^{D-1}} \right] dx^\alpha dx^\beta + \frac{l^2}{r^2} \left(1 + \frac{C_r}{r^{D-1}} \right) dr^2$$

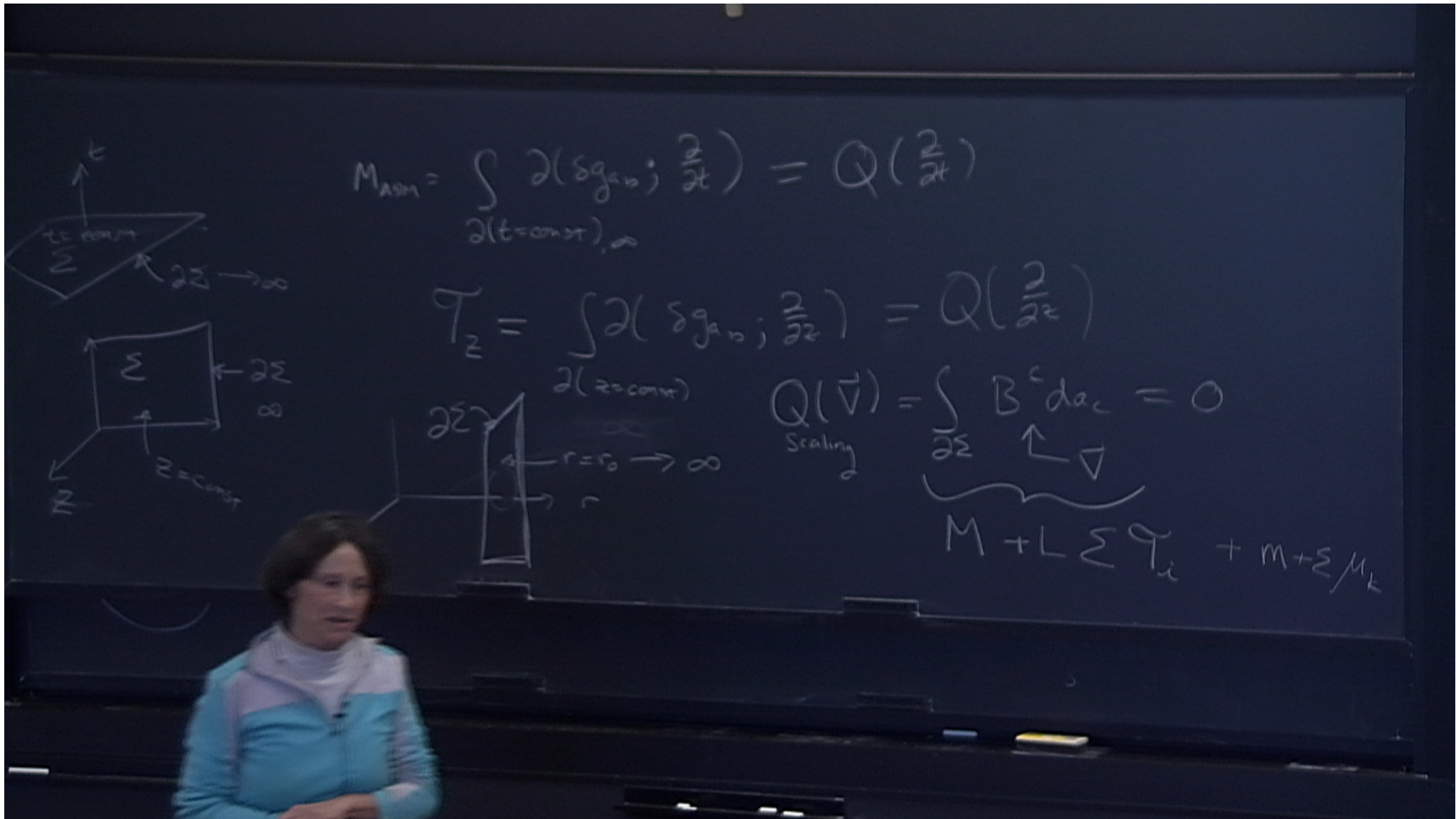
Sat

⊕

$$\vec{V} = x^\alpha \frac{\partial}{\partial x^\alpha} - r \frac{\partial}{\partial r}$$

KV Ads

Conformal isom.



$$M_{ADM} = \int_{\partial(t=\text{const}), \infty} \mathcal{L}(\delta g_{ab}; \frac{\partial}{\partial t}) = Q(\frac{\partial}{\partial t})$$

$$T_z = \int_{\partial(z=\text{const})} \mathcal{L}(\delta g_{ab}; \frac{\partial}{\partial z}) = Q(\frac{\partial}{\partial z})$$

$$Q(\vec{\nabla}) = \int_{\partial\Sigma} B^c da_c = 0$$

Scaling ∇

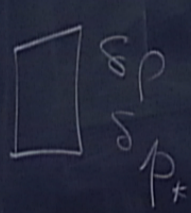
$$M + L \sum T_i + m + \epsilon / \mu_L$$

$Q(V) = \int_{\partial\Sigma} B^c da_c = 0$
 Scaling ∇
 $M + L \sum \rho_i + m + \epsilon \mu_k$

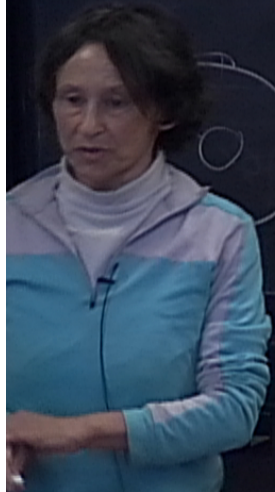
$$0 = \int_{Vol} \delta T^a_b W^b_{wa} = \int_{Vol} D_a B^a + \int_{Vol} (PDEs)$$

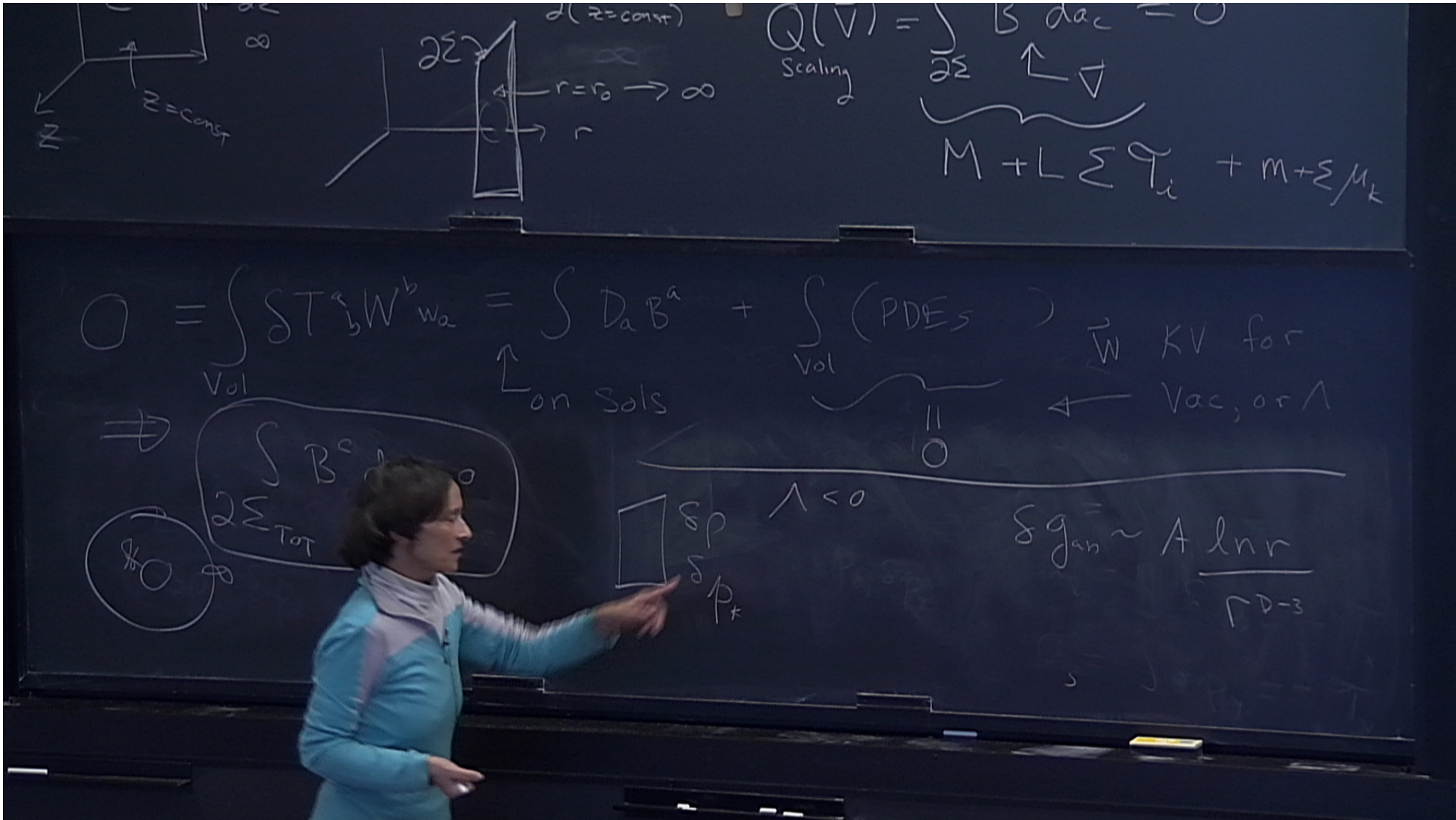
on Sols \parallel KV for Vac, or Λ

$$\int_{\partial\Sigma_{Tot}} B^c da_c = 0$$



$\Lambda < 0$





$Q(V) = \int_{\partial\Sigma} B da_c = 0$
 Scaling ∇
 $M + L \sum \rho_i + m + \epsilon/\mu_k$

$0 = \int_{Vol} \delta T^a_b W^b_{wa} = \int D_a B^a + \int_{Vol} (PDEs)$
 on sols $\parallel 0$ \vec{W} KV for Vac, or Λ

$\Rightarrow \int_{\partial\Sigma} \delta \rho^c da_c = 0$

$\delta g_{\mu\nu} \sim A \ln r$
 $A = \int [\delta p - \epsilon \delta p_k]$
 $\Lambda < 0$

