Title: 12/13 PSI - Student Presentations 2A

Date: Aug 17, 2012 01:30 PM

URL: http://www.pirsa.org/12080039

Abstract:

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Arthur Lee.'Physics in Nature'. 17th Aug.

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N₂ tyre filling - Brillant idea or scam?



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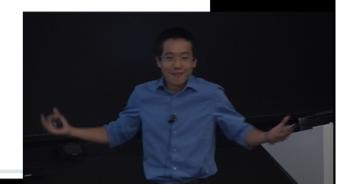
What happens.



psedealerequipment.com

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Why fill your tires with N_2 ?



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Why fill your tires with N₂?

Benefits claimed:

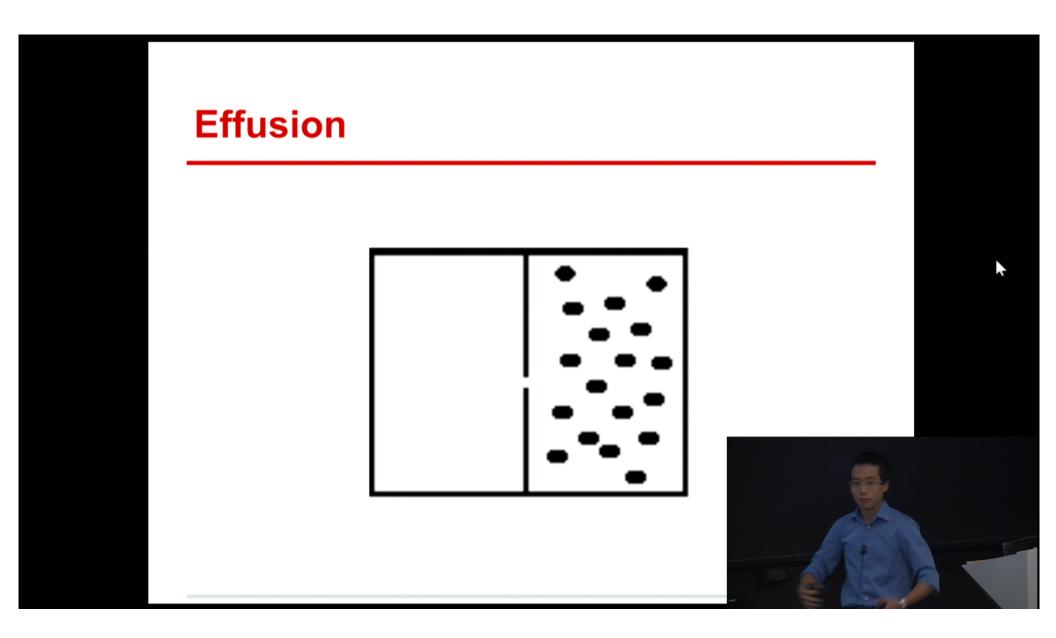
- Slower loss of pressure due to diffusion through the tyre,
- decreased rate of corrosion of tyre frame, and
- retarding the chemical degradation of rubber.

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Decrease rate of frame corrosion

- frame corrosion produces aluminum oxide powder
- which can get stuck in air valves

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Effusion

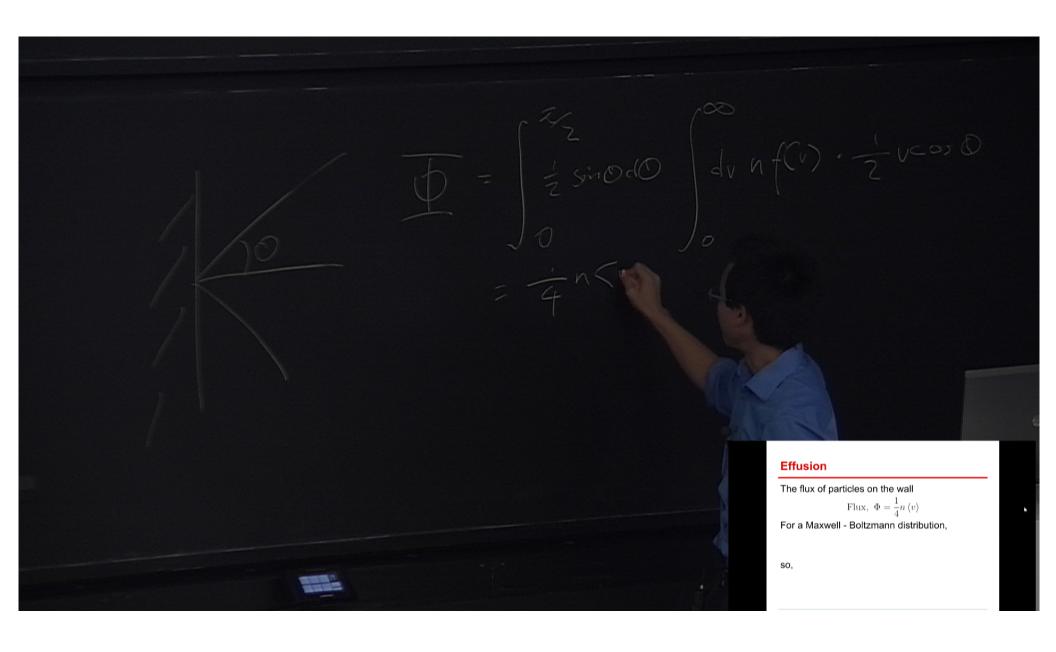
The flux of particles on the wall

Flux,
$$\Phi = \frac{1}{4} n \langle v \rangle$$

For a Maxwell - Boltzmann distribution,

SO,





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Effusion

The flux of particles on the wall

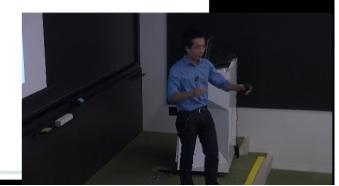
Flux,
$$\Phi = \frac{1}{4} n \langle v \rangle$$

For a Maxwell - Boltzmann distribution,

$$\langle v \rangle = \sqrt{\frac{8k_BT}{\pi m}} \propto \frac{1}{\sqrt{m}}$$

SO,

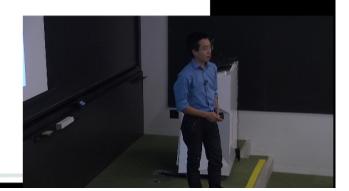
$$\Phi \propto \langle v \rangle \propto \frac{1}{\sqrt{m}}$$



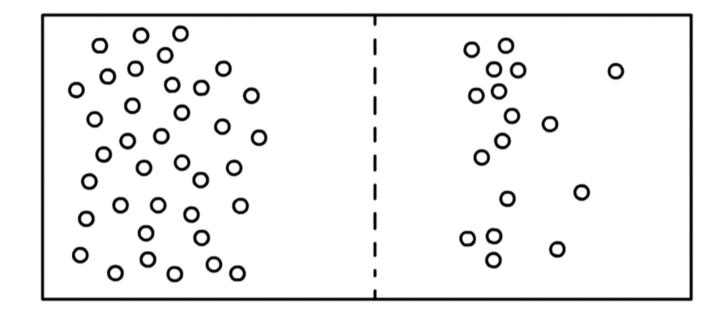
Effusion

Hence,

$$\frac{\Phi_{O_2}}{\Phi_{N_2}} = \sqrt{\frac{m_{N_2}}{m_{O_2}}} = 0.935$$



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Flux of particles

Flux,
$$\vec{\Phi} = -\frac{1}{3}\lambda \langle v \rangle \nabla n$$

For a Maxwell - Boltzmann distribution,

Also,

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So,

$$\Phi \propto \frac{1}{d^2 \sqrt{m}}$$

Using the data

$$d_{O_2} = 0.358 \, nm, \quad d_{N_2} = 0.370 \, nm$$

Thus,

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So,

$$\Phi \propto \frac{1}{d^2 \sqrt{m}}$$

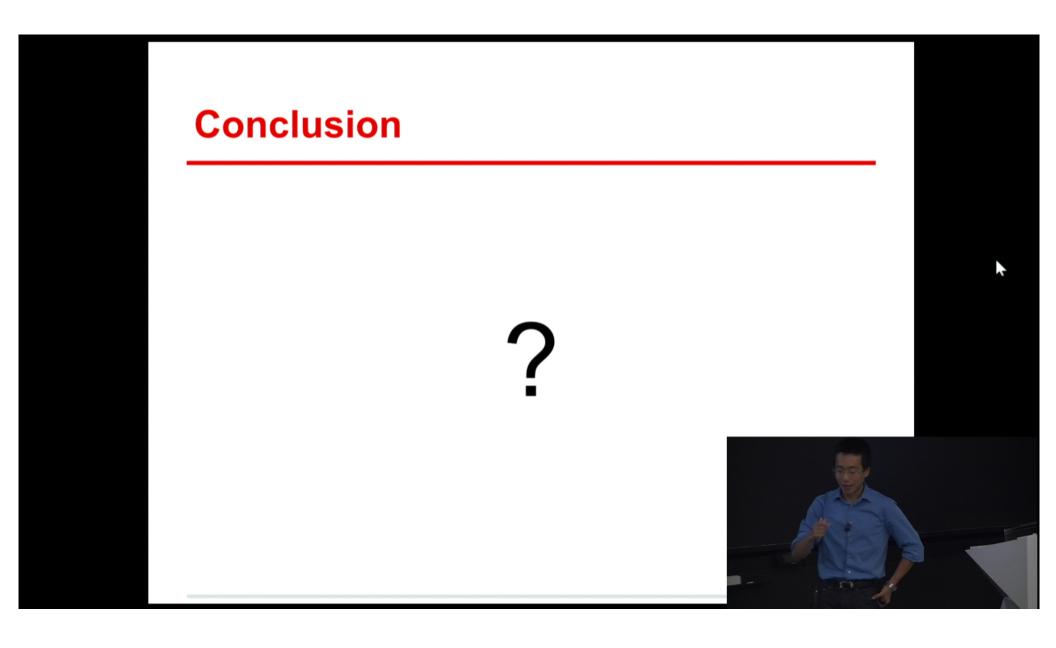
Using the data

$$d_{O_2} = 0.358 \, nm, \quad d_{N_2} = 0.370 \, nm$$

Thus,

$$\frac{\Phi_{O_2}}{\Phi_{N_2}} = \left(\frac{d_{N_2}}{d_{O_2}}\right)^2 \sqrt{\frac{m_{N_2}}{m_{O_2}}} = 0.9992$$

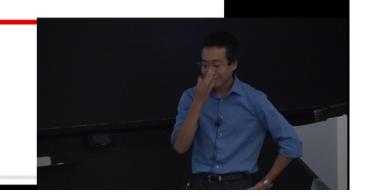
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Epilogue

the happy ending

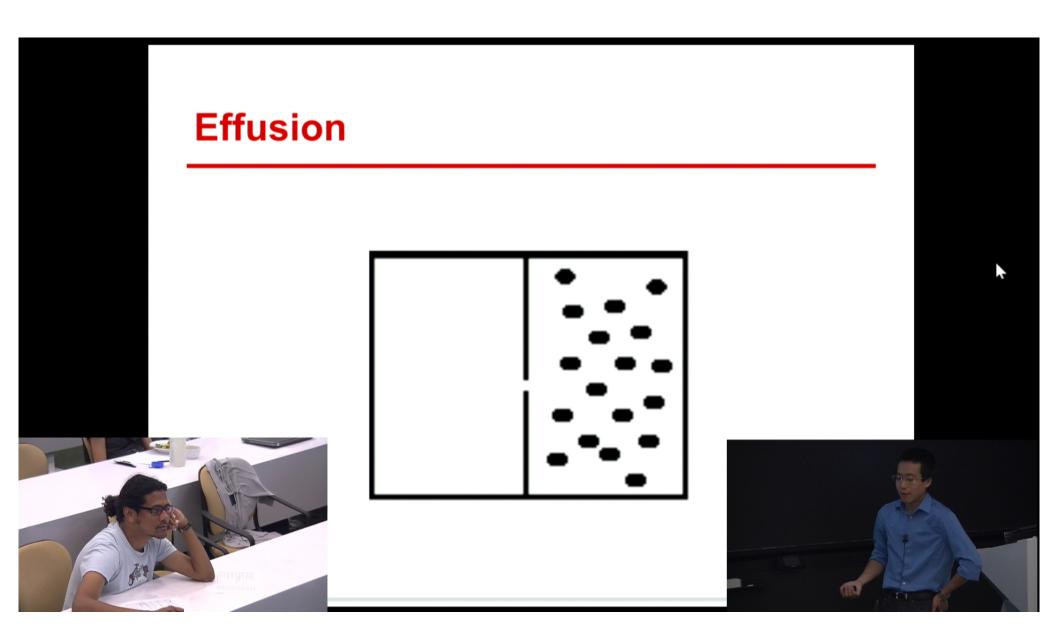


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The end



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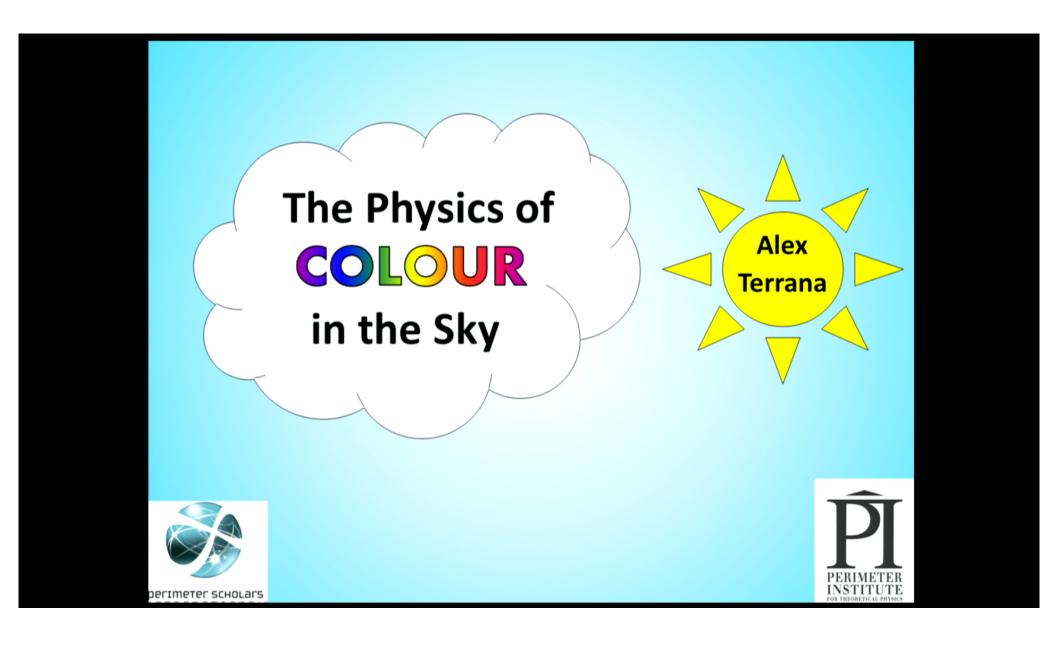
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Why fill your tires with N₂?

Benefits claimed:

- Slower loss of pressure due to diffusion through the tyre,
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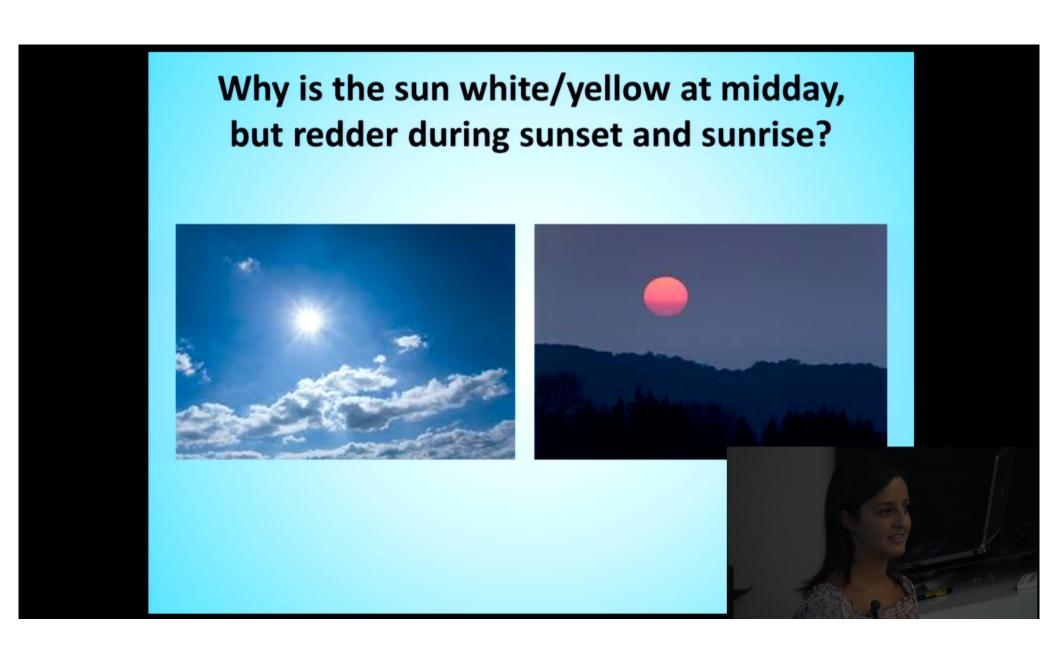
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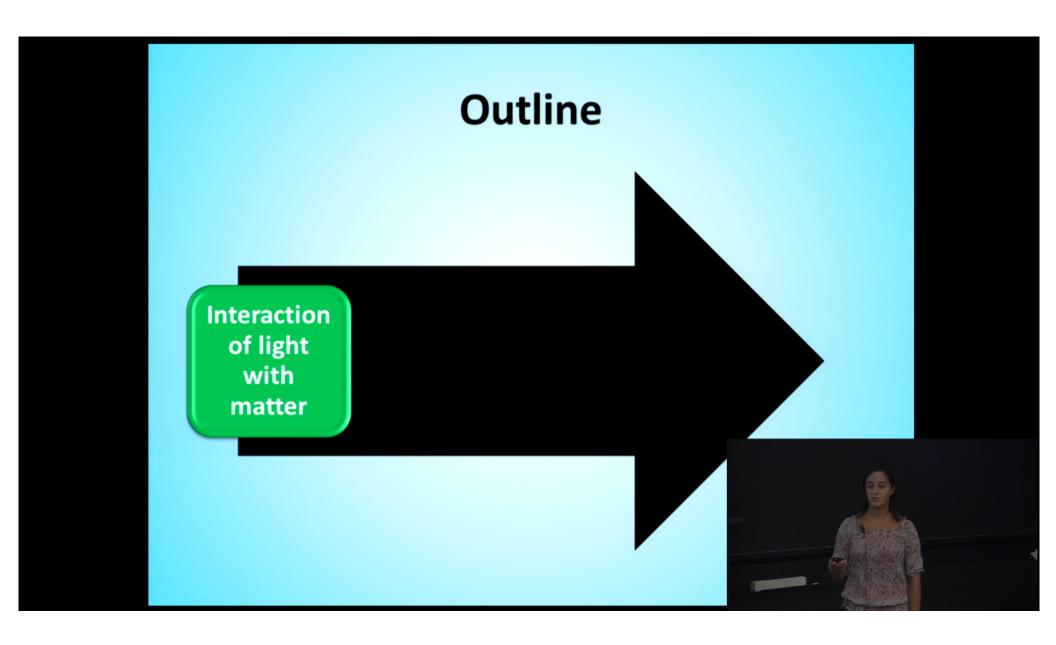
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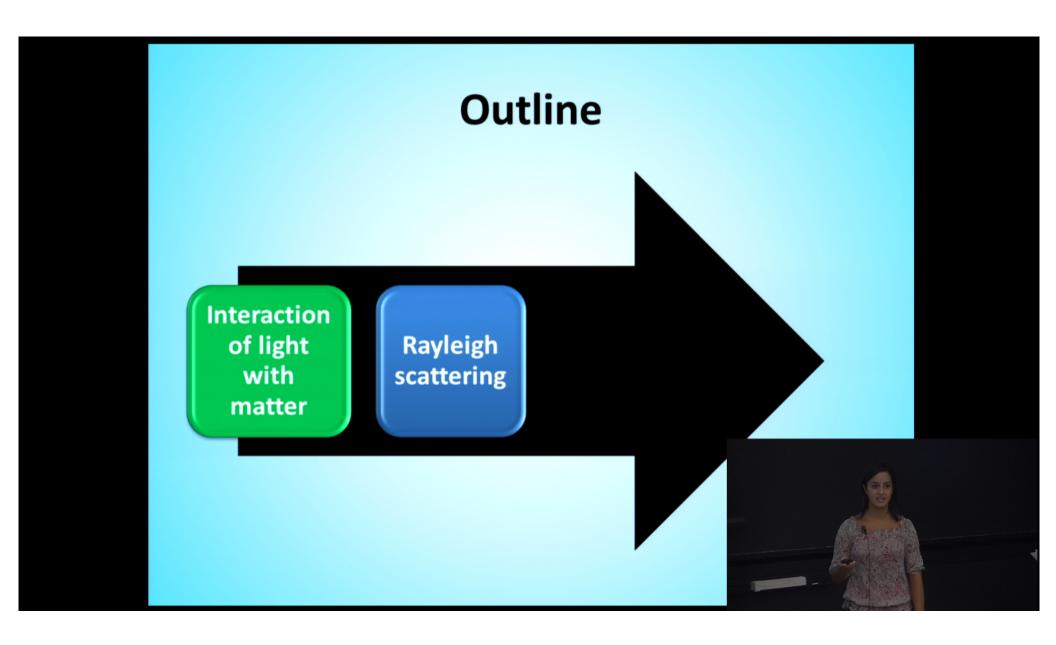
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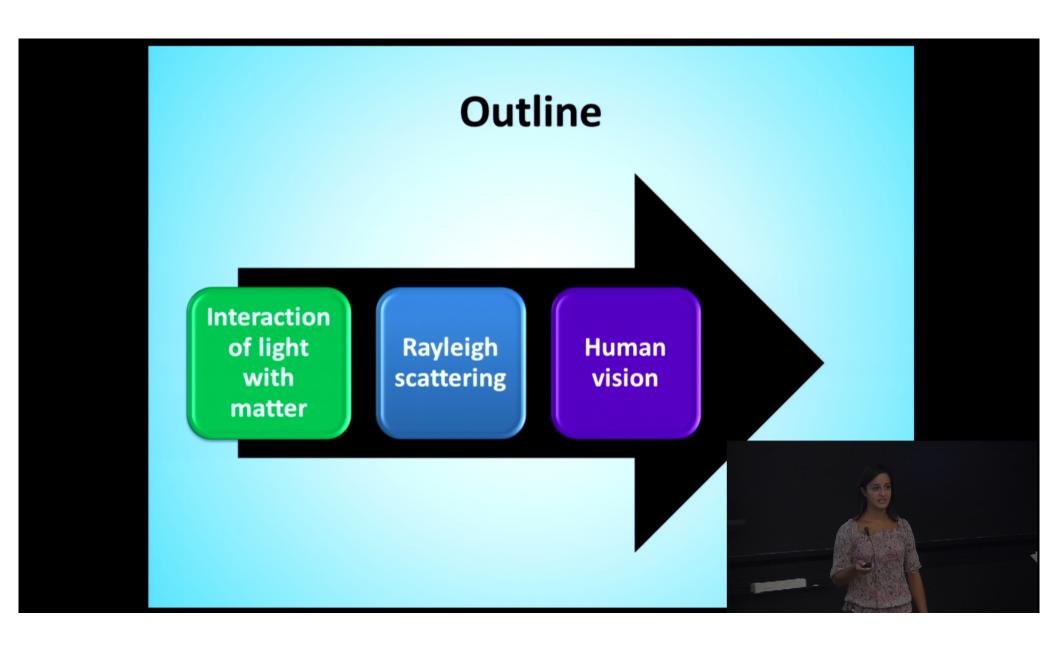
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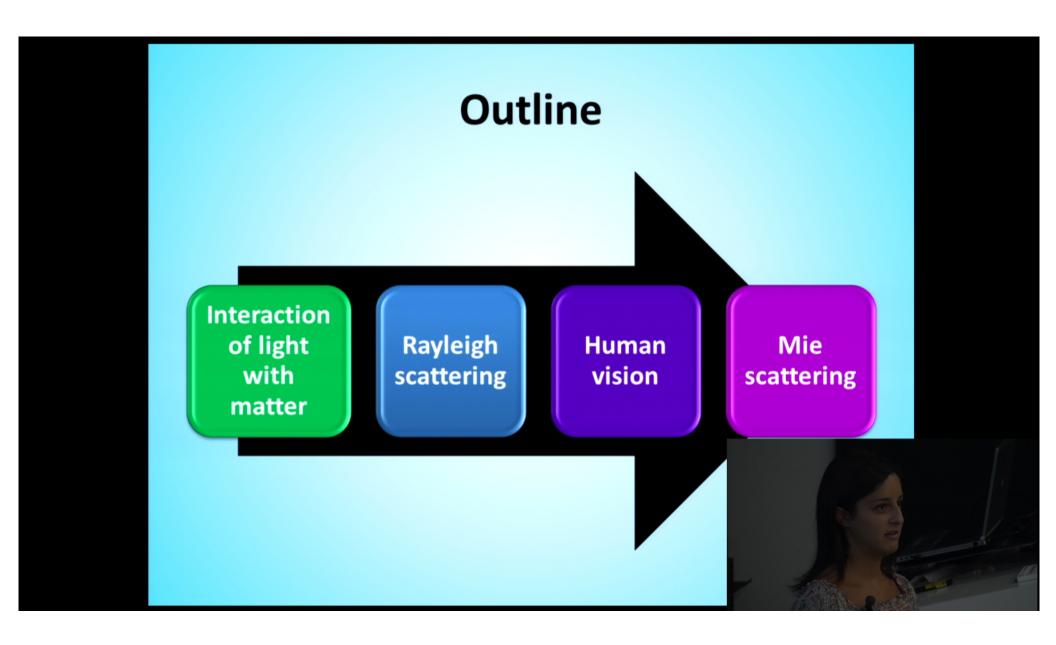
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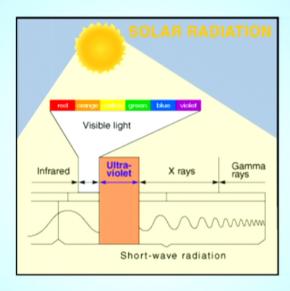


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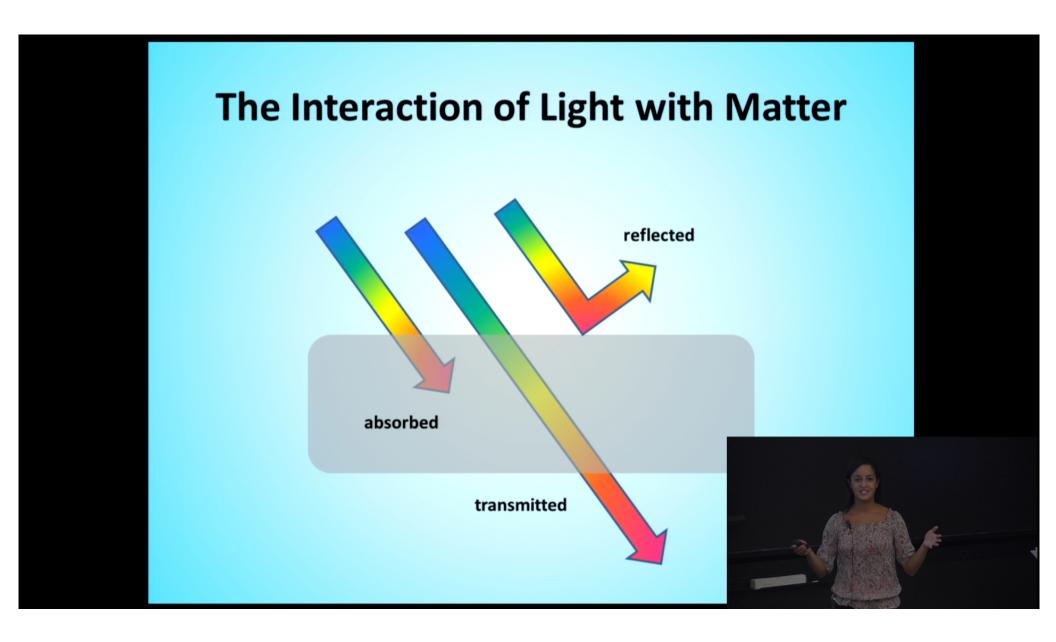
Light From the Sun



Picture source: http://serc.carleton.edu/usingdata/nasaimages/index4.html



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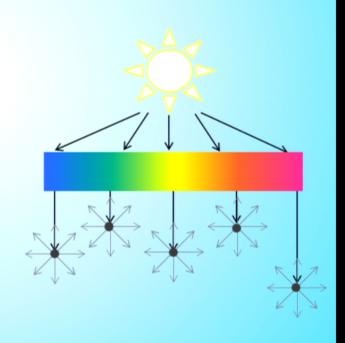


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The Interaction of Light with Matter

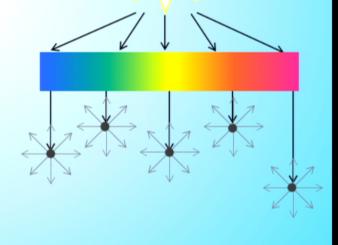


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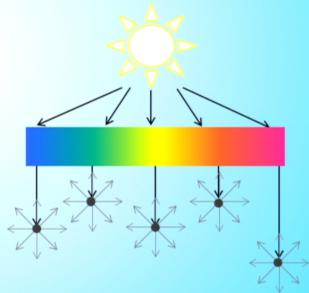
Solar radiation is scattered by particles in the atmosphere



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Solar radiation is scattered by particles in the atmosphere

- Two types:
 - Rayleigh scattering
 - Mie scattering

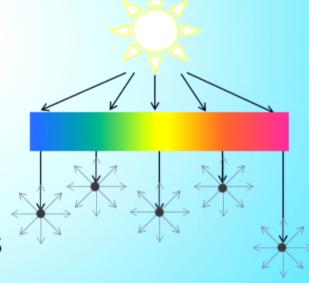


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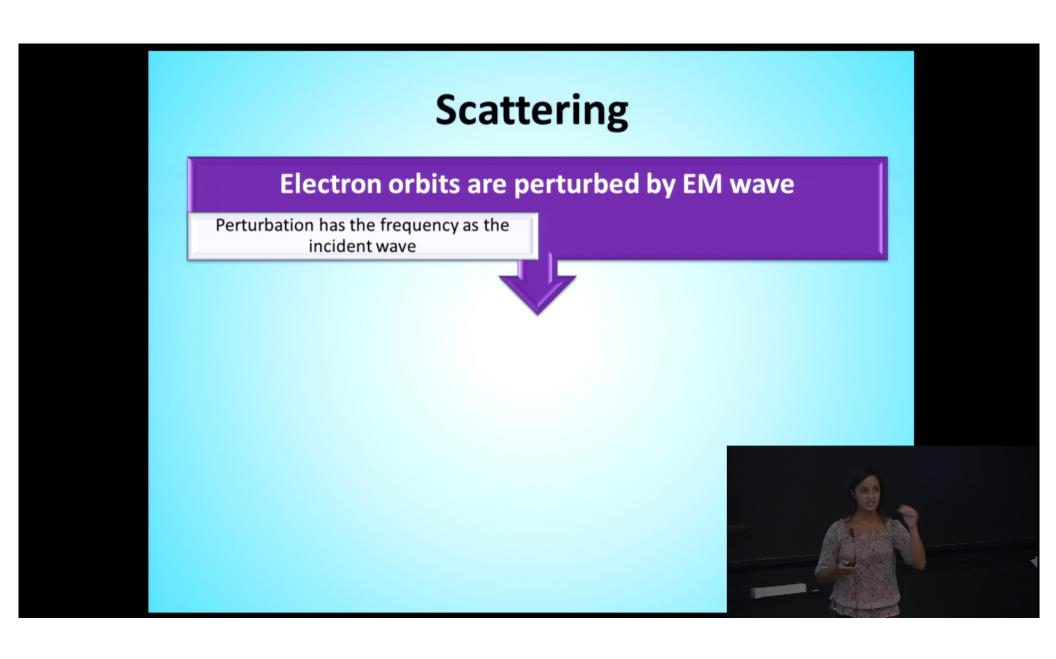
Solar radiation is scattered by particles in the atmosphere

- Two types:
 - Rayleigh scattering
 - Mie scattering

These are elastic processes



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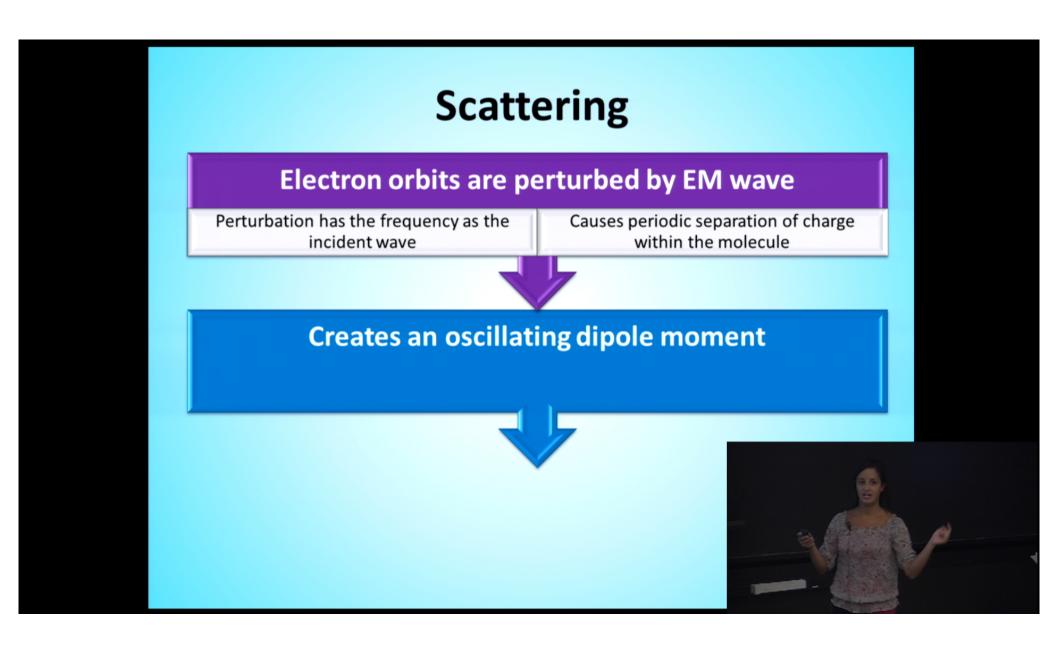
Electron orbits are perturbed by EM wave

Perturbation has the frequency as the incident wave

Causes periodic separation of charge within the molecule



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Scattering

Electron orbits are perturbed by EM wave

Perturbation has the frequency as the incident wave

Causes periodic separation of charge within the molecule



Creates an oscillating dipole moment

Its magnitude is proportional to the field and to the particle's polarizability



The dipole moment radiates light

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Rayleigh Scattering

 Particles much smaller than the wavelength of the light:

 $r \ll \lambda$

The particles can be individual atoms or molecules

• N_2 molecule has $r \approx 0.11$ nm visible light has $\lambda \approx 500$ nm



Rayleigh Scattering

 The Intensity of light scattered by a single molecule is given by

$$I = I_0 \frac{8\pi^4 \alpha^2}{\lambda^4 R^2} (1 + \cos^2 \theta)$$

 I_0 is the light's intensity λ is the wavelength θ is the scattering angle

 α is the molecular polarizability R is the distance to the particle

Seinfeld and Pandis, Atmospheric Chemistry and Physics, 2nd Edition, John Wiley and Sons, New Jersey 2006, Chapter 15.1.1

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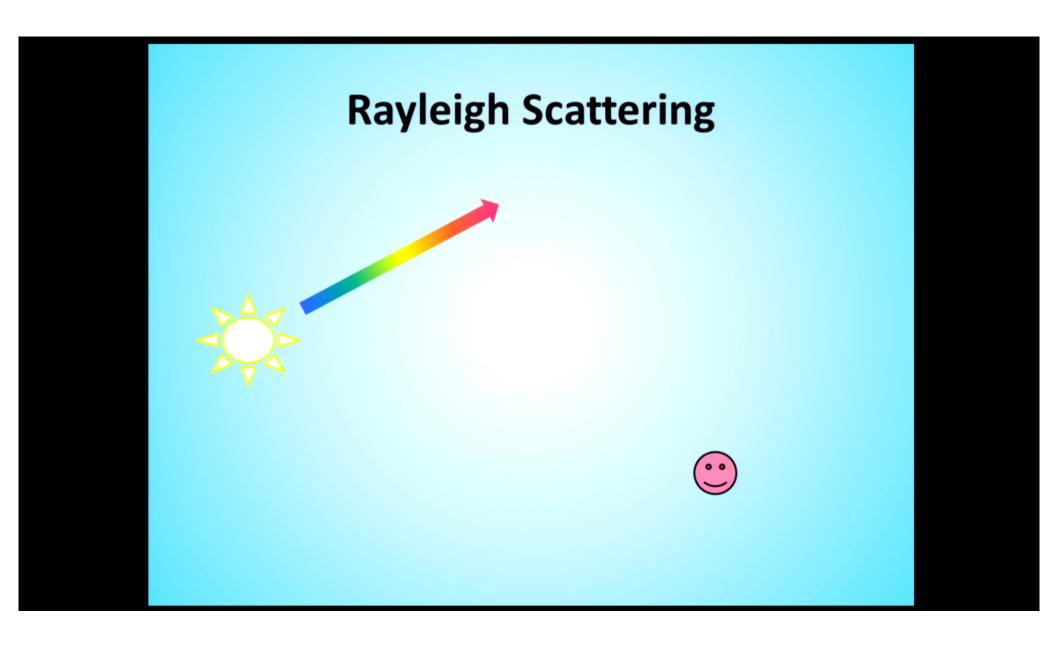
400nm 700nm

Scattered the most

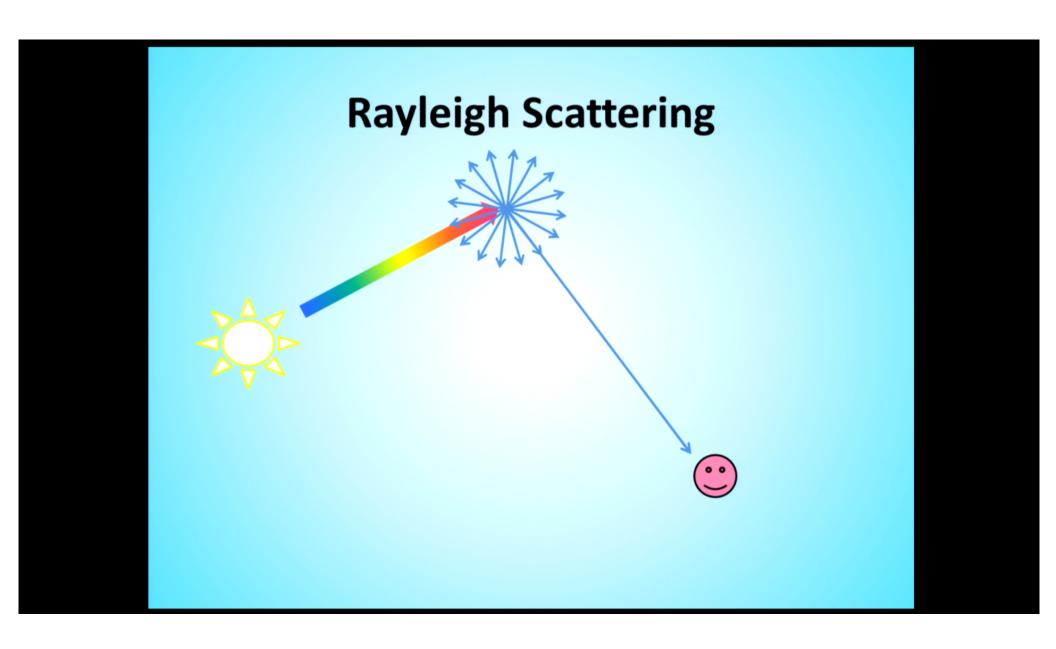
Scattered the least

~9.4 x more scattering

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Colour Perception

- There are 5 million cones in our retinas which are responsible for colour vision
 - Three types: long, medium and short-wavelength
- The ranges of the cone types overlap

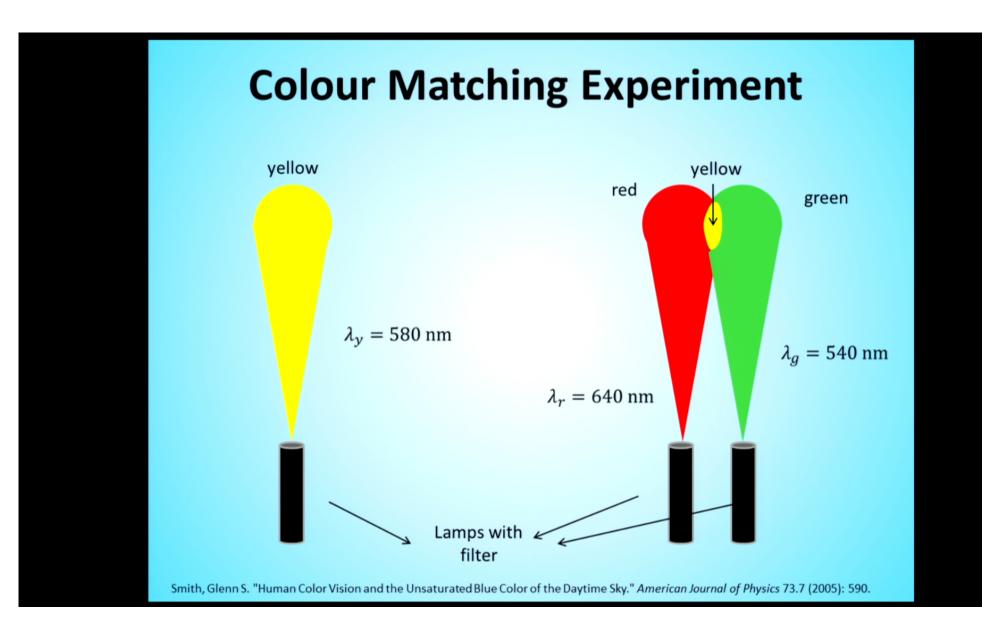


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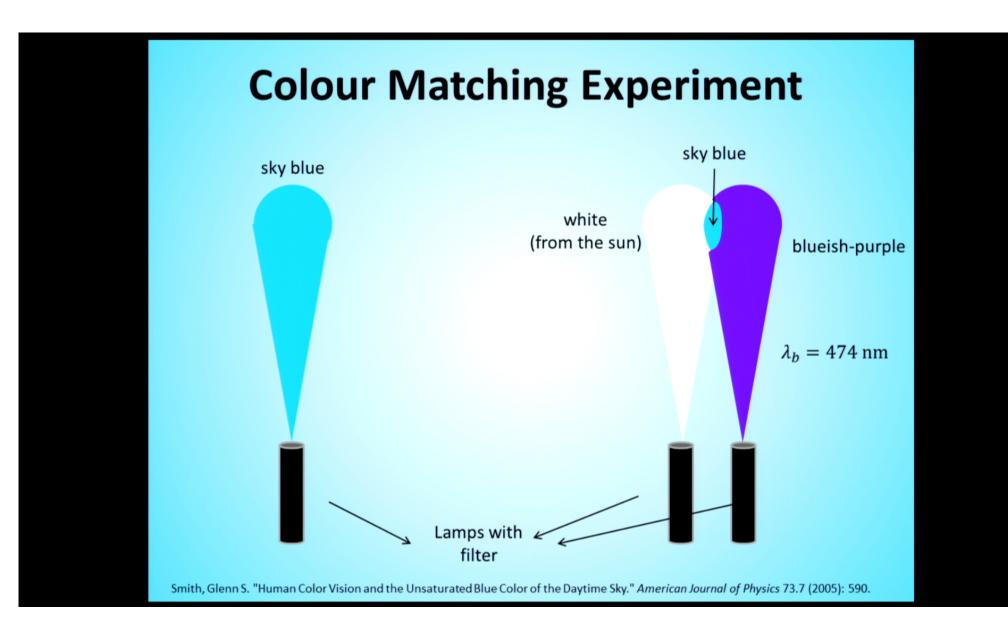
Colour Perception

- There are 5 million cones in our retinas which are responsible for colour vision
 - Three types: long, medium and short-wavelength
- The ranges of the cone types overlap
- Different spectral combinations can be detected as the same colour

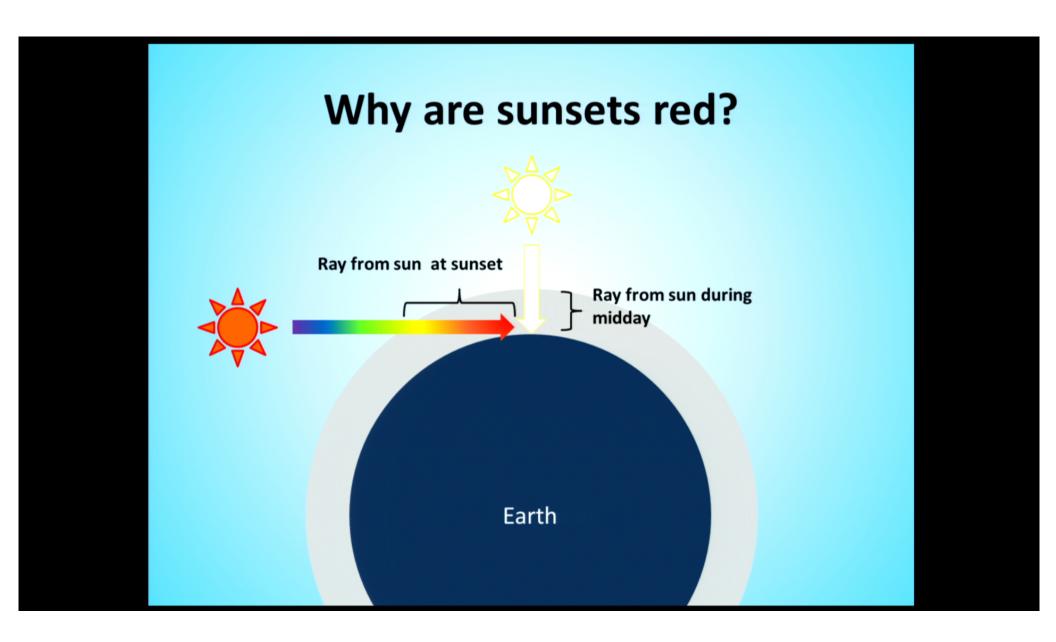
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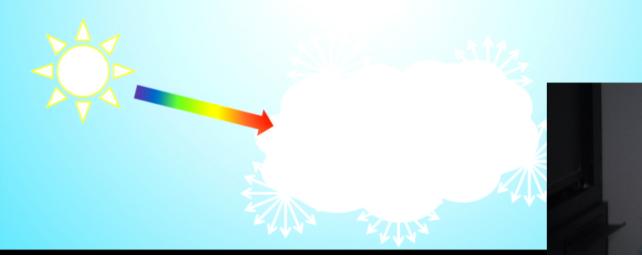
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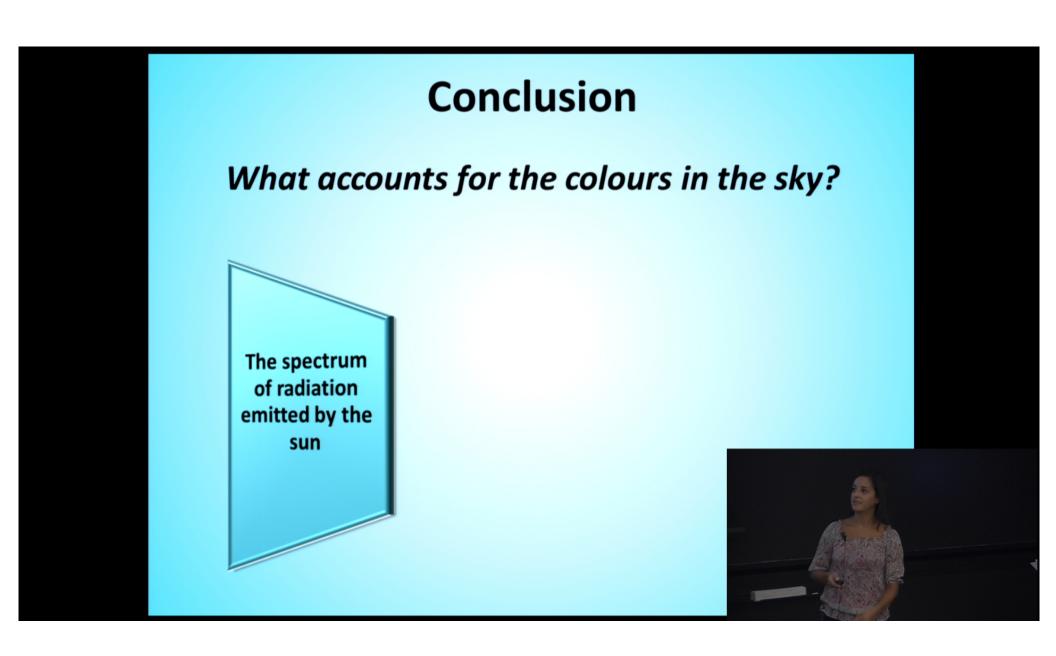
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Mie Scattering

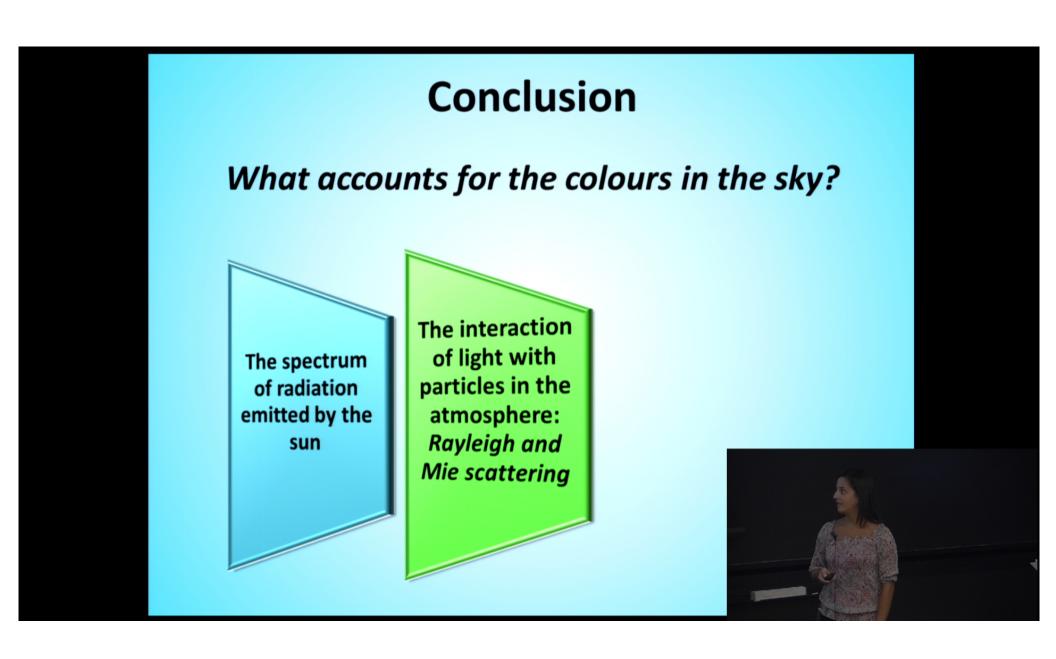
- size of the particle ≥ wavelength
- Not heavily wavelength dependent in the visible range
- Produces the white light from clouds, mist and fog
- Rayleigh scattering is just an approximation to Mie scattering in the limit of small particle size.



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What accounts for the colours in the sky?

The spectrum of radiation emitted by the sun

The interaction of light with particles in the atmosphere:
Rayleigh and Mie scattering

Human colour vision

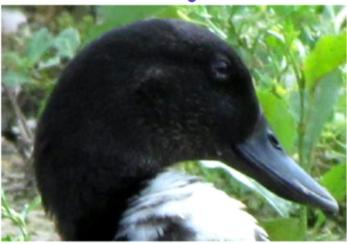
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Physics in Nature: A Birdseye View

Perimeter Scholars International 2012/2013 Daniel Xavier Ogburn





"To see a world in a grain of sand, And a heaven in a wild flower. Hold infinity in the palm of your hand, And eternity in an hour."

- William Blake: Auguries of Innocence













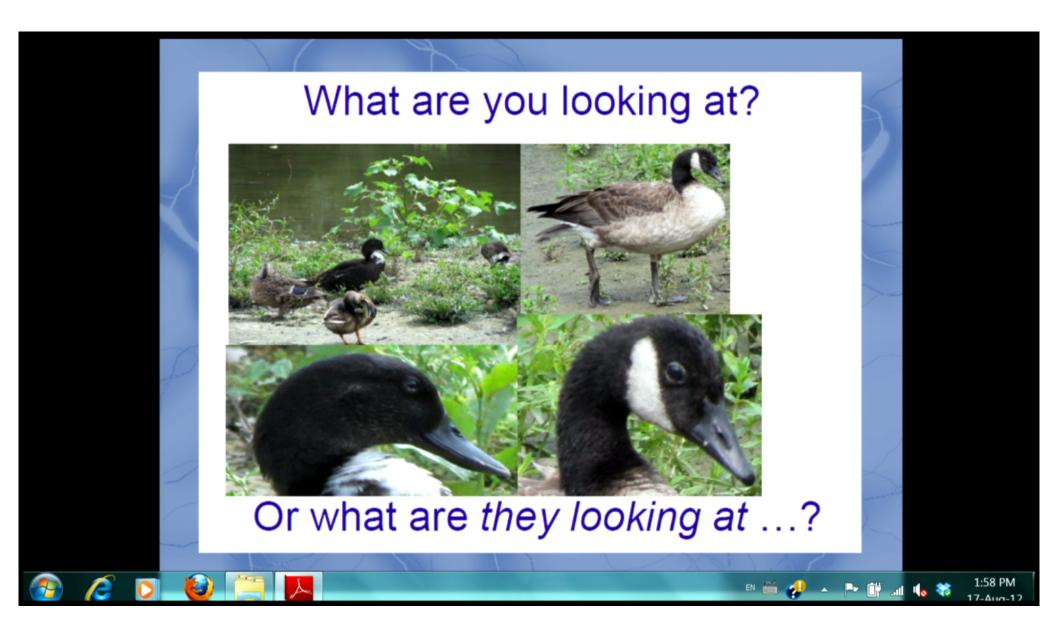








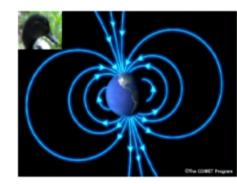
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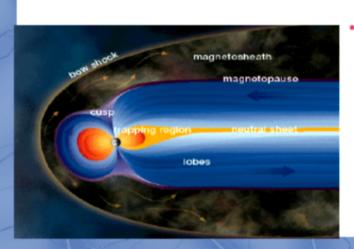


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Magnetic Navigation: Just Wing It

- Many bird species migrate
 - e.g. Ducks and Geese in Waterloo
 - Changing photoperiod
 - Weather, food, habitat
- ~ 50 known animal species use Earth's magnetic field to navigate.





- Earth's magnetic field:
 - Background dipole ~ 50μT (stable, long time scales).
 - Solar wind perturbation (dayside/nightside tail).
 - Plasma waves & resonances in magnetosphere and ionosphere: ~ short (s) nT pertbuation.























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The Avian Compass: Nature's Magnetometer

- Humans:
 - -Compass
 - -Aeromagnetic survey: Fluxgate magnetometer (~0.2nT)



Cesium vapor magnetometers (QM, Zeeman ~ 0.01nT)

- How do Migratory Birds navigate?
 - Klaus Schulten 1970s: geomagnetically sensitive biochemical reaction in eye
 - Cryptocrome protein molecule.
 - Photons → Cryptocrome energy boost → ...





















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Fancy some entanglement?



"iMagnetometer"

Photons \rightarrow Eye \rightarrow Cryptocrome energy boost →

Free Radical Pair →

Entangled Electrons (separated, but spins linked) →

Hypersensitivity to Magnetic Fields →

Chemical Reactions →

Magneto-reception and the Avian Compass.

- Nature: QM entanglement in warm, noisy environment! ٧S
- Humans: QM entanglement in isolated, cryogenic setting without noise.





















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Fancy more entanglement?



- Sense variations < 0.3% of Earth's magnetic field strength ~ 150 nT! (Conservative model used by Gauger et al).
- Experiments of Ritz et al. sensitivity as low as ~ 15nT (European robin).
- Bird "sees" the magnetic field.
- Requires electrons to be entangled for $\sim 100 \ \mu s$.
- No cryogenics, outperforms NaC0⁶⁰ by at least 20µs!
- Robust sensor (training, protected by noise).

















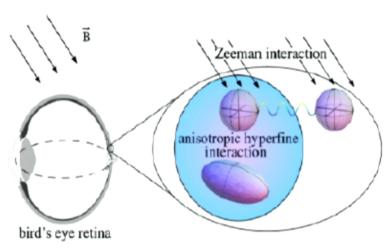




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A Radical Notion: The RP Mechanism

- Quantum Evolution of spatially separated pair of e spins after energized by photon.
- Two e spins and one nuclear spin.
- Spheroid directionality



- Spatial separation: Nucleus interacts with one spin
 - Asymmetry for singlet-triplet oscillations.
 - RP formation at t=0, Hamiltonian for system after separation.
 - one e⁻ coupled to nucleus, one e⁻ ~'free (Gauger et al.)

$$H = \hat{I} \cdot \mathbf{A} \cdot \hat{S}_1 + \gamma \mathbf{B} \cdot (\hat{S}_1 + \hat{S}_2)$$



















Radical Pair Mechanism (2)

- Gauger et al. also Investigated more detailed models: -e.g. add 2nd nuclear spin, replace nuclear asymmetry with anisotropic g-factor for e.
- All models give rise to same qualitative behavior and decoherence timescales as the simple RP model.
- **Underlying principle**: e⁻ spins of RP must be protected from decoherence to be susceptible to the experimentally applied RF magnetic field.
- External magnetic field: $\mathbf{B} = \mathbf{B}_0 + \cos(\omega t)\mathbf{B}_{rf}$
- At Frankfurt: $B_0 \sim 47 \mu T$. Experiment and Simulation: $B_{rf} = 150 nT$.





















Radical Pair Mechanism (2)

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- External magnetic field: B = B₀ + cos(ωt)B_{rf}
- At Frankfurt: B₀ ~ 47μT.
 Experiment and Simulation: B_{rf} =150nT.























Time Evolution: Master Equation

- Resonant excitation with uncoupled e⁻ spin: B_{rf} frequency 1.316MHz.
- 8-dimensional Hilbert space of 3 spins (entangled electrons + nucleus)
 - 2 singlet projectors and 3 triplet projectors P_i
- Model dynamics with Linblad Master Equation (density matrix):

$$\dot{\rho} = -\frac{i}{\hbar}[H,\rho] + k\sum_{i=1}^{8} P_i \rho P_i^{\dagger} - \frac{1}{2}(P_i^{\dagger} P_i \rho + \rho P_i^{\dagger} P_i).$$

- Decay rate k for projectors.
- Solve for density matrix ρ.



















Entanglement + Background Noise = Good Times

- Choosing constants:
 - Resonance frequency of the 'free' electron = 1.316MHz.
 - Experiments show a 1.316MHz perturbing magnetic field can disorient the bird.
 - No disruption if B_{rf} is parallel to B₀.
- Resulting bound on decay rate: k ≤ 10⁴ s⁻¹.
- Consistent with long RP lifetimes for cryptochrome molecules in migratory birds.
- Q: How robust is this mechanism against environmental noise?
 A: Random noise actually protects against decohorence!
- Anti-intuitive: Human experiments achieve entanglement by using cryogenic temperatures and minimizing noise.



















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Modeling Noise

Add Linblad dissipator to Linblad Master Equation:

$$\dot{\rho} = -\frac{i}{\hbar}[H,\rho] + k\sum_{i=1}^{8}P_{i}\rho P_{i}^{\dagger} - \frac{1}{2}(P_{i}^{\dagger}P_{i}\rho + \rho P_{i}^{\dagger}P_{i}) + \text{Noise}$$

Noise =
$$\sum_{i} \Gamma_{i} \left(L_{i} \rho L_{i}^{\dagger} - \frac{1}{2} (L_{i}^{\dagger} L_{i} \rho + \rho L_{i}^{\dagger} L_{i}) \right)$$

- Noise Operators L_i and their decoherence rate Γ_i.
- Conservative estimate: when $\Gamma \ge k$ angular sensitivity degrades.
- Implies that the decoherence time for the two-electron avian compass is of the order of 100μS or more.

















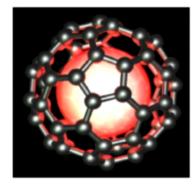


Bird vs Scientists

- Avian compass decoherence time (at room temp.) $\geq \sim 100 \mu S$.
- Best decoherence time achieved in a laboratory at room temp for preservation of a molecular electron spin state: 80μS for NaC⁶⁰.







- Compass mechanism is almost immune to phase noise.
- If strong phase is present t the level of Gamma ~ >= 10k it would actually render the bird immune to weak RF magnetic perburations!

















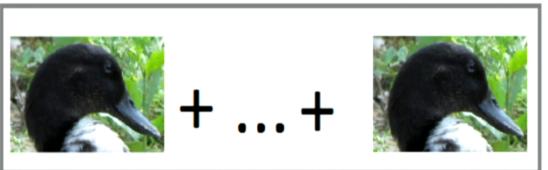


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- Imitate nature:
 - Entangled states with long lifetimes at room temp.

Intel Pentium X





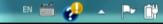














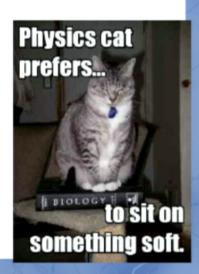


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Quantum Biology: More Examples

- Photosynthesis:
 - Classically invalid pathways
 - Photoelectric effect
 - Photoelectron entanglement, Hamiltonian least path calculation in Chlorophyll to reach target molecule.
- Sunlight: Fusion, QM tunneling through Coulomb barrier.
- Sense of Smell: entanglement (debated).
- Cats in boxes.



















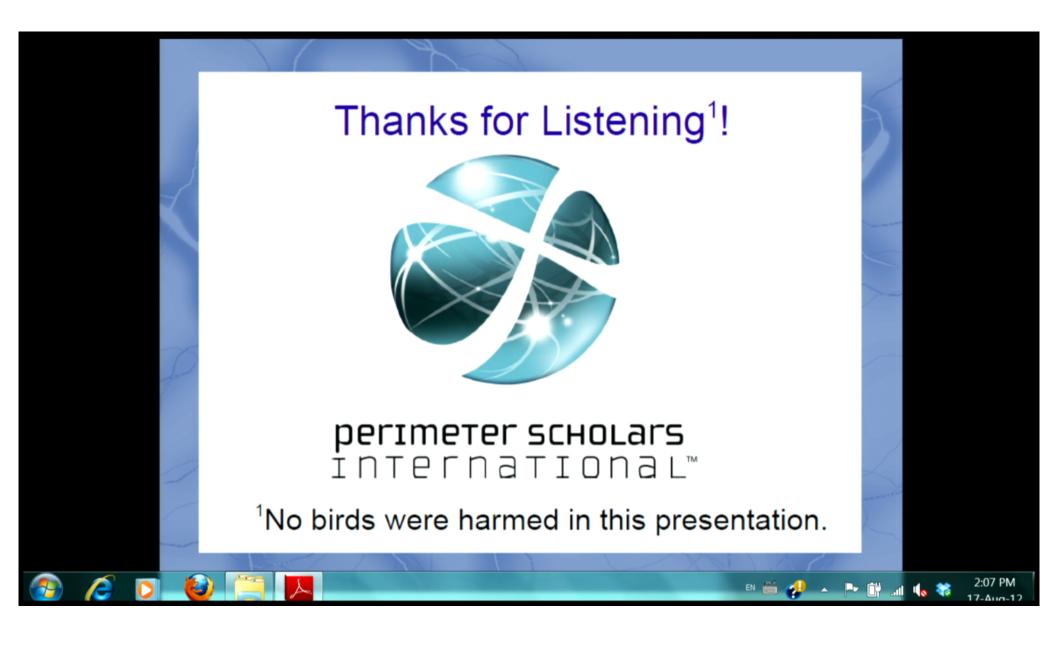








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Physics in nature: Phase transitions

Presentation by Dominique Soutière

















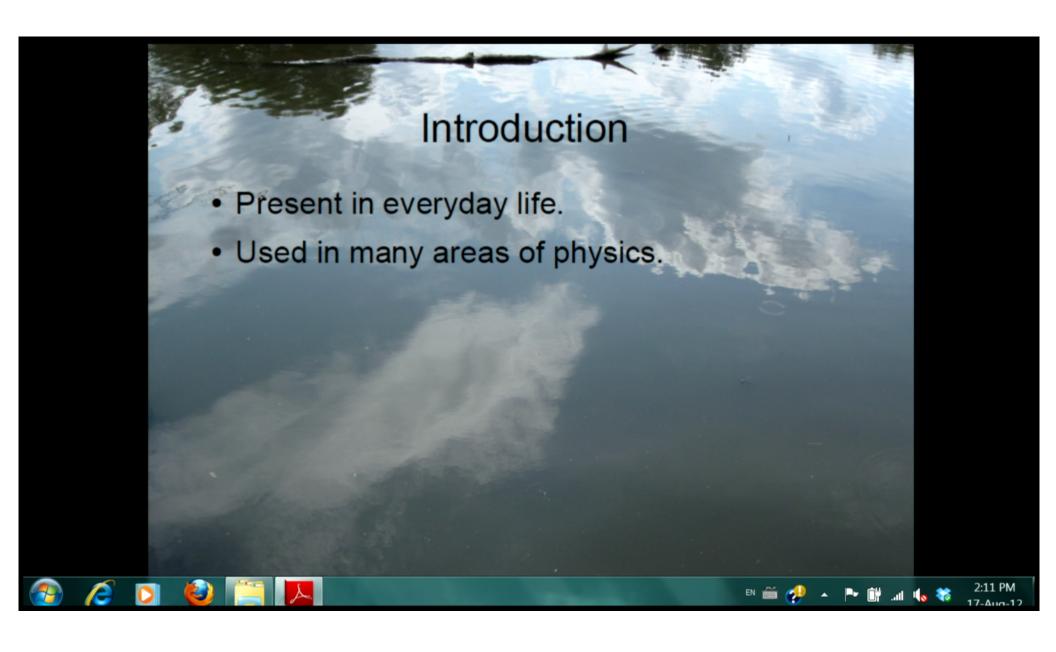








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Outline

- Introduction
- Definitions
- Some examples
- Revision of thermodynamic quantities
- 2 types of transitions
- · Transitions for water
- Ising model
- Conclusion













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Definitions

- Phase: An homogeneous system.
- A phase transition usually occurs by varying external conditions.
- Characteristic by a discontinuity in one of the derivatives of a thermodynamic property.
- Order parameter: A quantity that varies from 0 to a non-zero value during the transition.



















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Some examples

- Solid, liquid, gas and plasma
- Ferromagnetic and paramagnetic solids
- Superconductivity and superfluidity
- Breaking of symmetries (cosmology)















17-Aug-17

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Quick revision

• Gibbs free energy G = E - TS + PV

$$dG = -SdT + VdP$$

- Specific volume $V/N = [1/N] \partial G/\partial P$
- Specific Heat $C_p = T \partial S / \partial T = -T \partial^2 G / \partial T^2$



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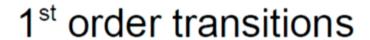
Quick revision

• Gibbs free energy G = E - TS + PV

$$dG = -SdT + VdP$$

- Specific volume $V/N = [1/N] \partial G/\partial P$
- Specific Heat $C_p = T \partial S / \partial T = -T \partial^2 G / \partial T^2$



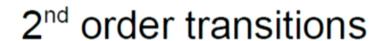


- A first derivative of the Energy is discontinuous.
- Latent heat: Fixed amount of energy absorbed or released.
- In liquid-gas transition below the critical point, the specific volume is discontinuous.



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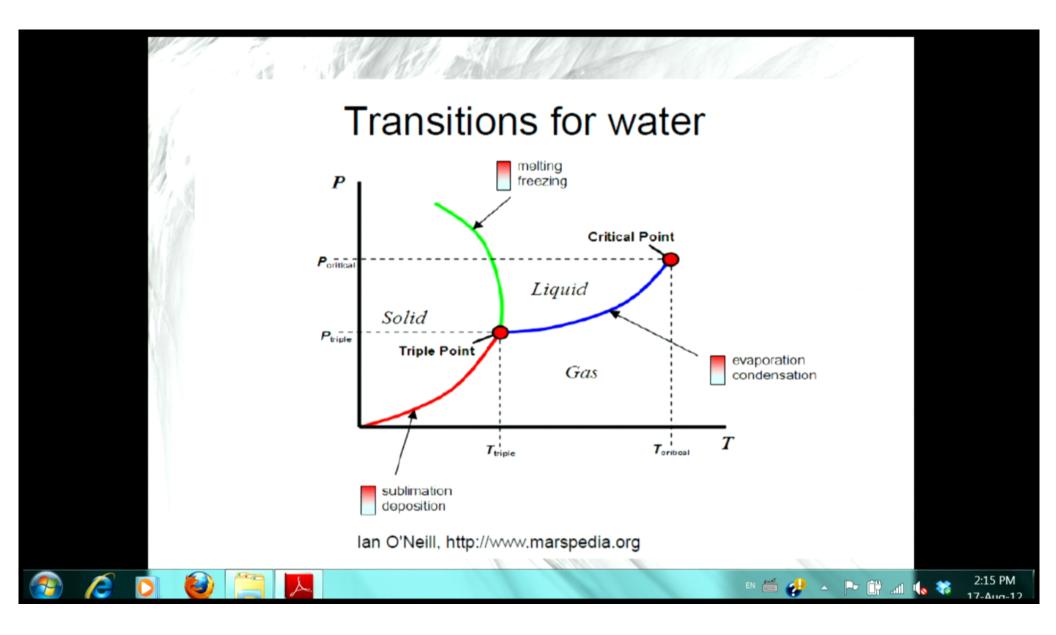
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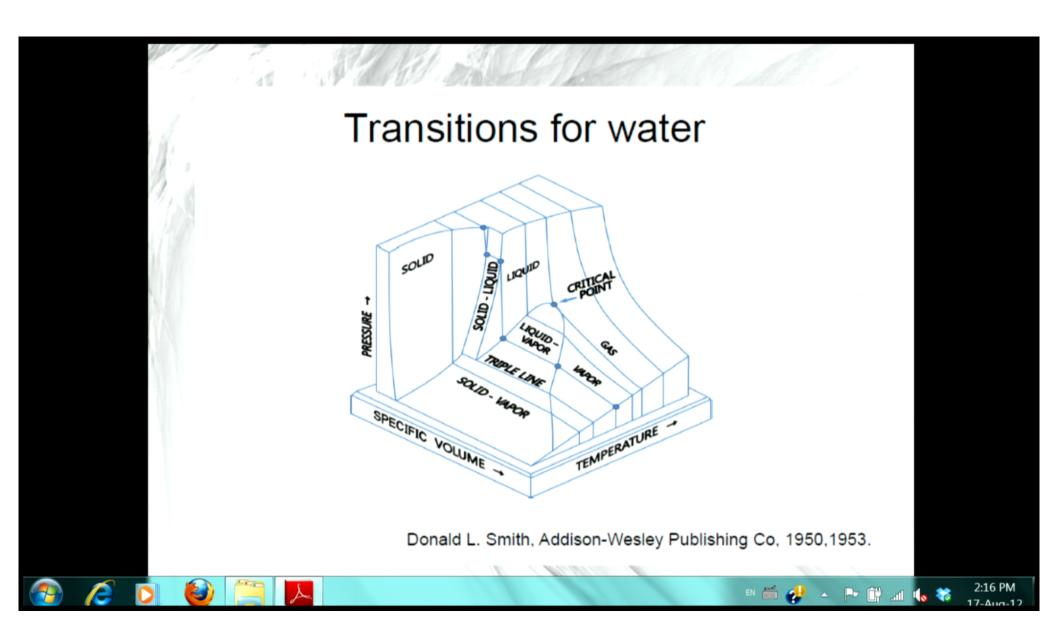
- A second derivative of the Energy is discontinuous.
- In liquid-gas transition beyond the critical point, the specific volume is continuous but the heat capacity is discontinuous



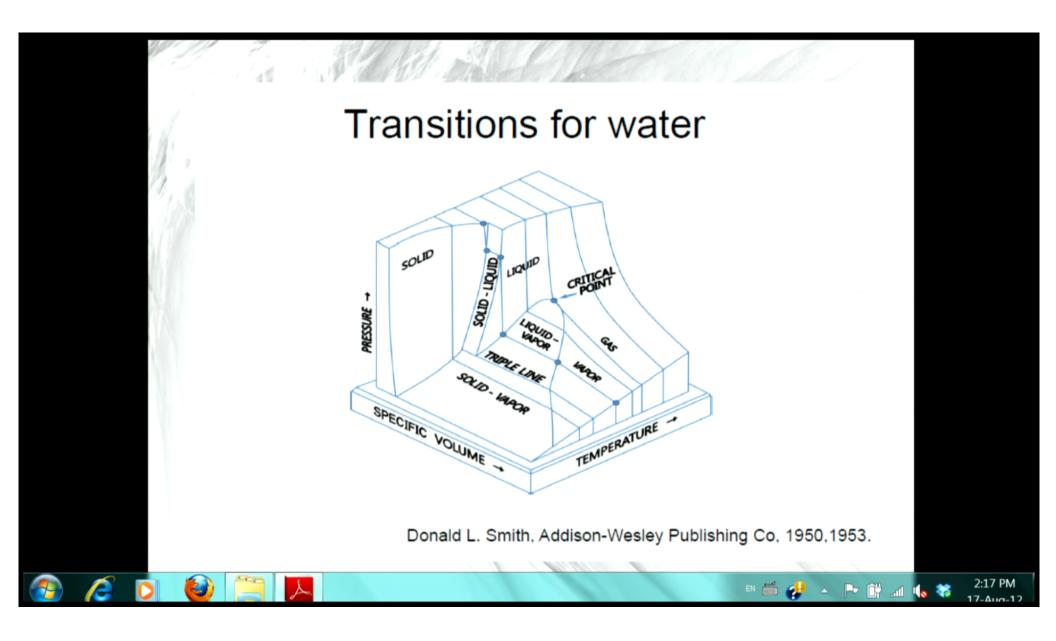
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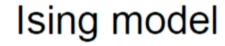
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Ising model

- Model of interacting particles in 2D placed on a square lattice.
- Short range spin interaction, 2 possible alignment.
- Energetic advantage to have nearby spins aligned

$$H = -J \sum s_i s_j$$
, $s_i = \pm 1$





- Above critical temperature: Short length correlation.
- Below the critical temperature: Spins align on large scale.
- At the critical temperature: Infinite correlation length.

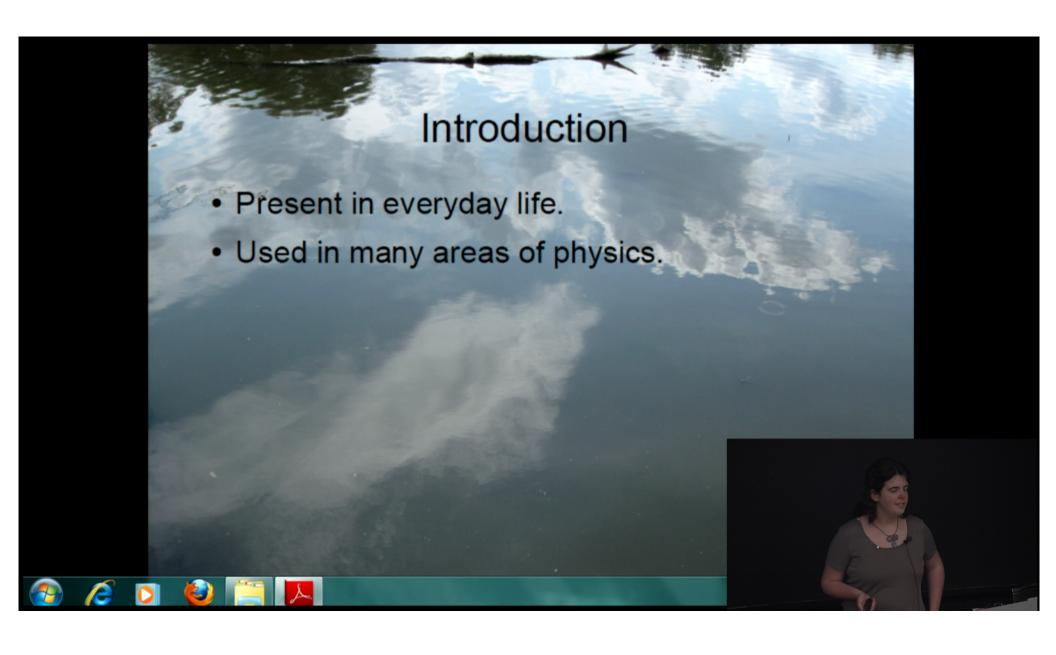


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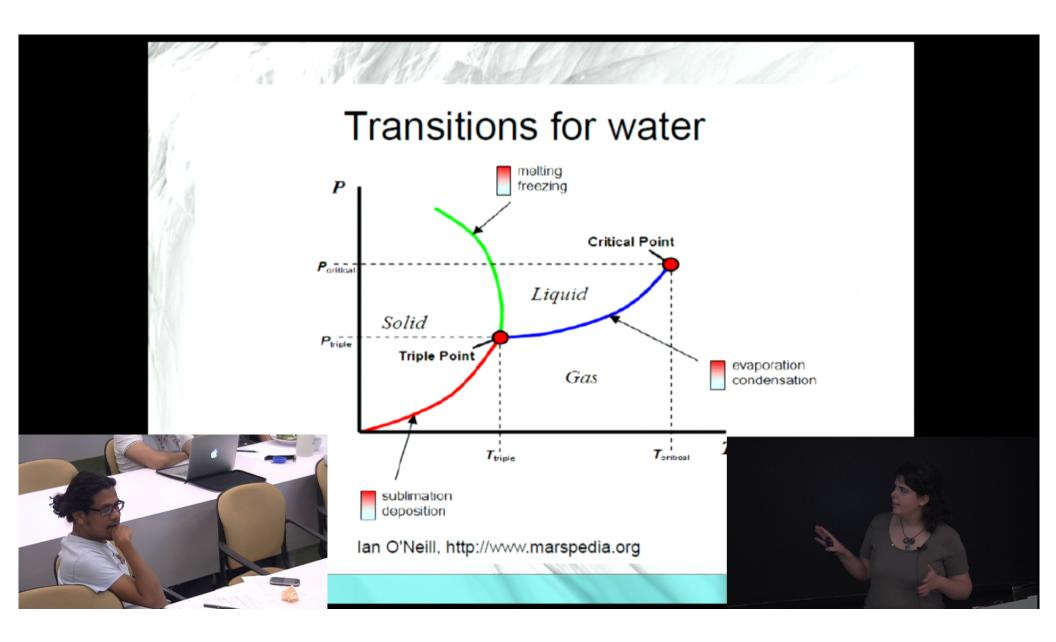
Conclusion

- 2 types of transitions depending on discontinuities.
- We use the order parameters to differentiate between phases.
- Is used in a variety of situations and scales, from condensed matter to renormalization groups.





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The Hydraulic Mechanism in Spiders' Legs

By Jin-Mann (Jenny) Wong

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Contents

- Introduction
- Anatomy of a Spider
- Hydraulics
- A Simple Model
- Experimental Results
- Industrial Applications
- Summary

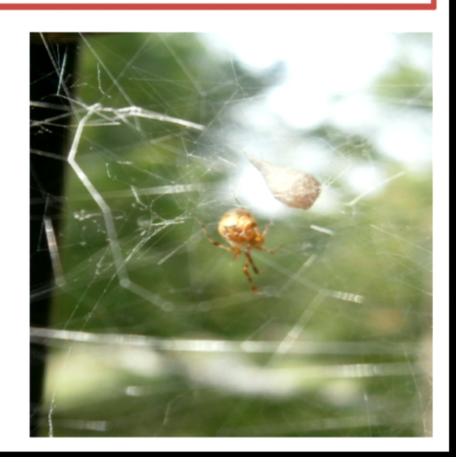


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Introduction

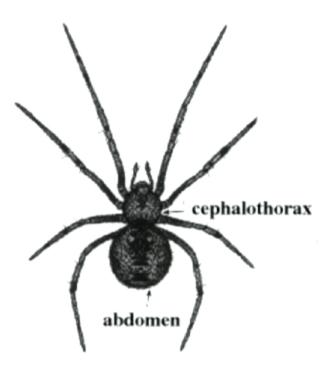
Hydraulic and muscular mechanisms

 No leg extension muscles



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Anatomy of a Spider



Open circulatory system

Seven joints

Cephalothorax muscles

Image from http://www.explorit.org/science/spider.html

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Hydraulics

- Pascal's principle
- Pressure = Force/Area
- $V_{in} = V_{out}$

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- Pascal's principle
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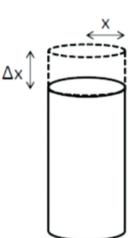
A Simple Model ∆x \$____

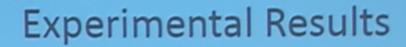
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A Simple Model

$$\Delta V = \frac{4\pi}{3} \left(r^3 - \left(\frac{r}{2}\right)^3 \right)$$

$$\Delta V = 8\pi x^2 \Delta x$$





- Resting pressure: 6.6 kilopascals
- Transient pressure: 60 kilopascals
- Contraction due to Cephalothorax

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Robotic Spider



 $\frac{\text{Image from } \underline{\text{http://www.engineeringontheedge.com/2011/11/3d-printing-spawns-robotic-spiders/}}{\underline{\text{spiders/}}}$

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Smart Stick

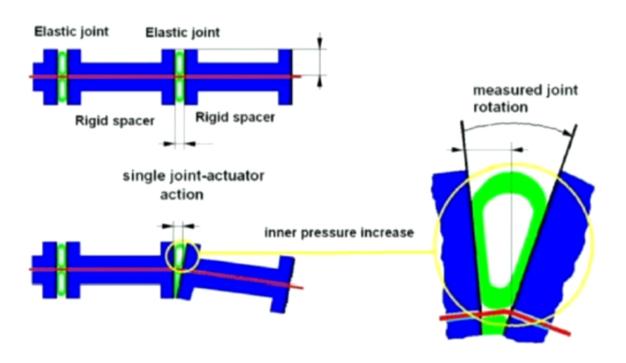


Image from C. Menon and C. Lira. "Spider-inspired embedded actuator for space applications."

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Summary

• Hydraulic mechanism

Cephalothorax muscles

• Simple model

Applications

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L. Zentner, S. Petkun and R. Blickham. (2000) "From the Spider Leg to a Hydraulic Device."

http://www.findaspider.org.au/info/Mobility.htm

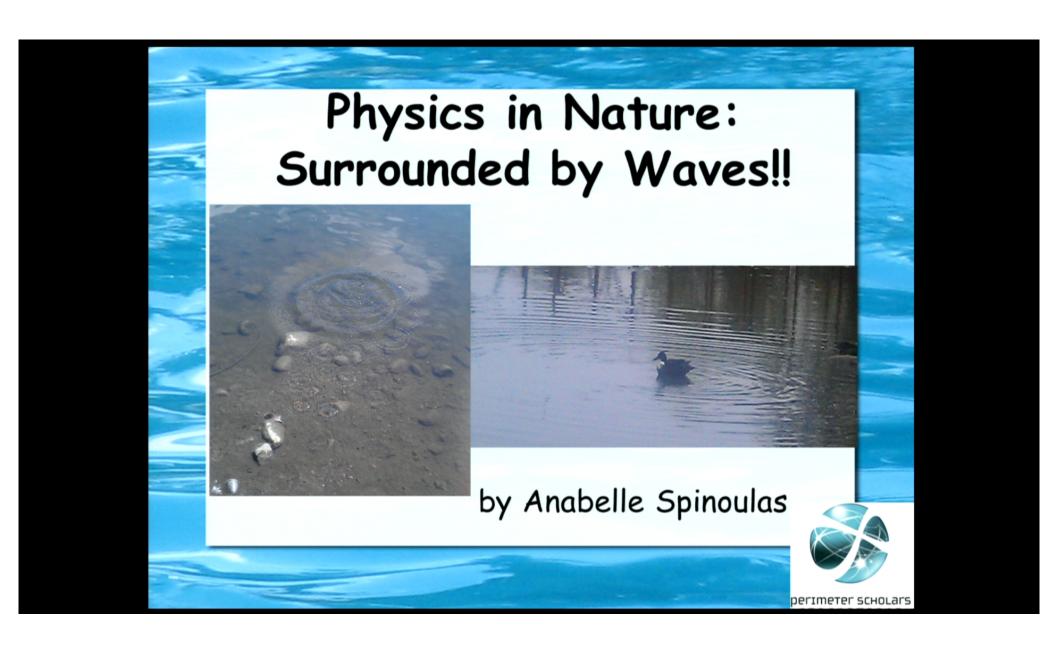
- D. Parry and R. Brown. (1959) "The Hydraulic Mechanism of the Spider Leg."
- J. Anderson and K. Prestwich. (1975) "The Pressure Fluid Pumps of Spiders."

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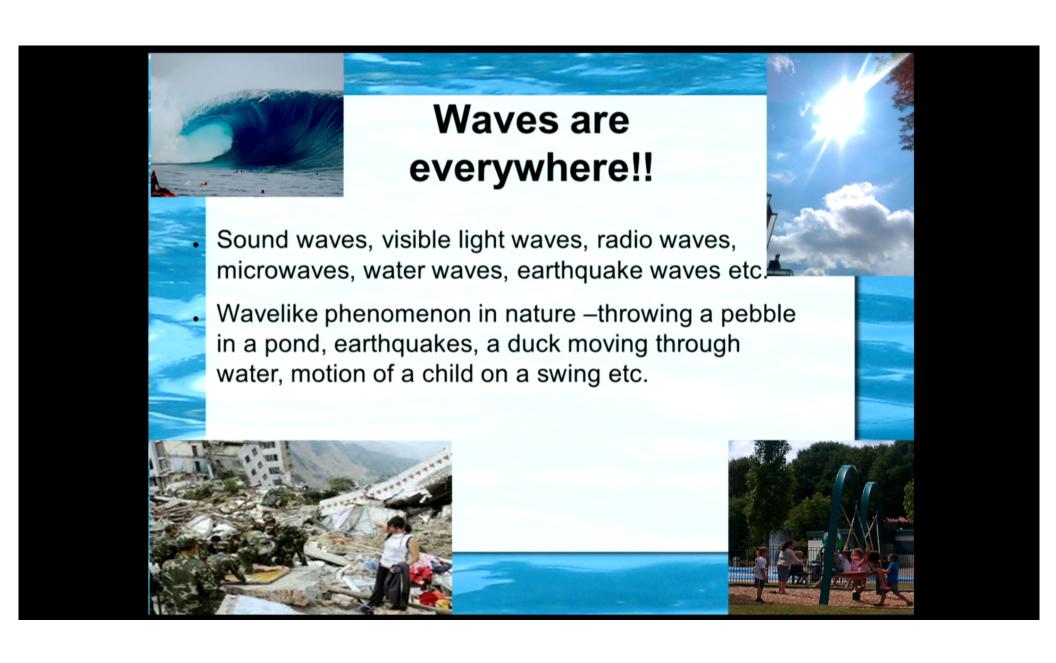


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Outline

- What is a wave and where do we see them in Nature
- Properties of Waves
- Types of Waves
- Study of ripples in pond water waves in action!
- Conclusions

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What is a wave?

- A disturbance that travels through a medium from one location to another.
- Medium (matter)

 collection of interacting particles.
- Adjacent particles of the medium interact disturbance is able to travel through the medium.
- Example: Water wave: medium the water; interacting particles the individual molecules of water.

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What is a wave?

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Waves transport energy, <u>not</u> matter

- Individual particles of medium
- **temporarily** displaced from their rest position
- restorative force brings them back to their original position.

 Therefore, while waves move, the medium (water) does not.

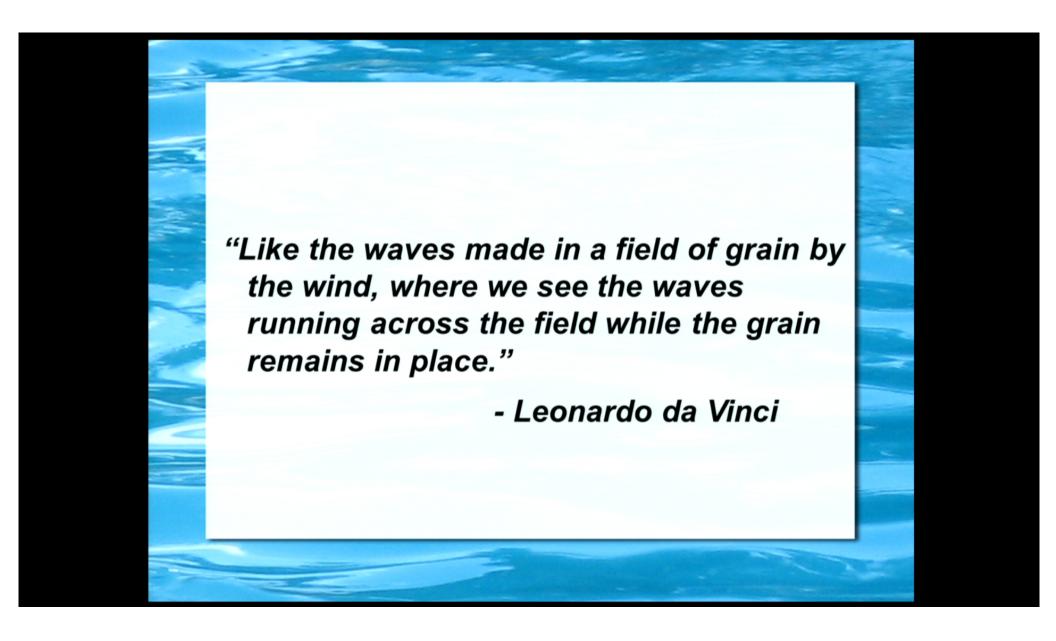
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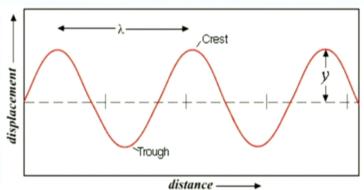
Different types of Mechanical Waves

•Transverse wave - the displacement of the particles of the medium is perpendicular to the direction that the wave moves.

Wave equation:

$$u(x, t) = y \sin(kx - \omega t + \phi)$$

Where, x is position, t is time, k is wavenumber, ω is the angular frequency, ϕ is the phase



 $\lambda = wavelength$

y = amplitude

Figure 1: Diagram of transverse wave

Frequency, f:

$$f = \frac{v}{\lambda}$$

Where, v is the phase velocity of the wave

Period, T:

$$T = \frac{1}{f}$$

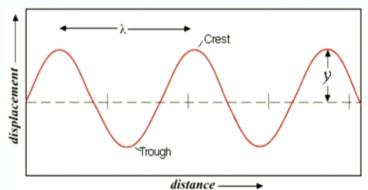
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Period, T:

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Different types of Mechanical Waves

 A longitudinal wave – the displacement of the particles of the medium is parallel to the direction that the wave moves. Example: sounds waves

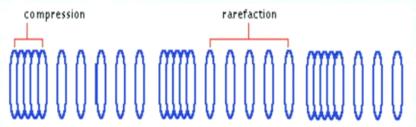
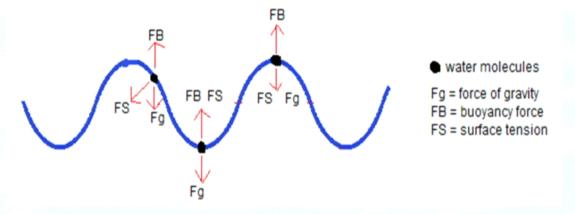


Figure 2: Longitudinal Wave (Edlin, 2012)

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- Three main forces acting on each water molecule force of gravity, buoyant force and most importantly surface tension.
- Longitudinal component of the surface tension.
- Surface wave Combination of both transverse and longitudinal waves.



•These surface waves execute simple harmonic motion in 2-dimensions.

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Ripples on the surface of a pond

Surface wave (combination of transverse and longitudinal waves)

Particles along the surface of the water move in a circular motion

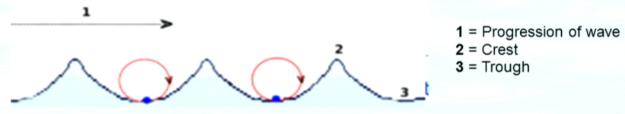


Figure 4: Diagram of surface wave showing circular motion of particles on surface of the medium (Zimbres, 2006)

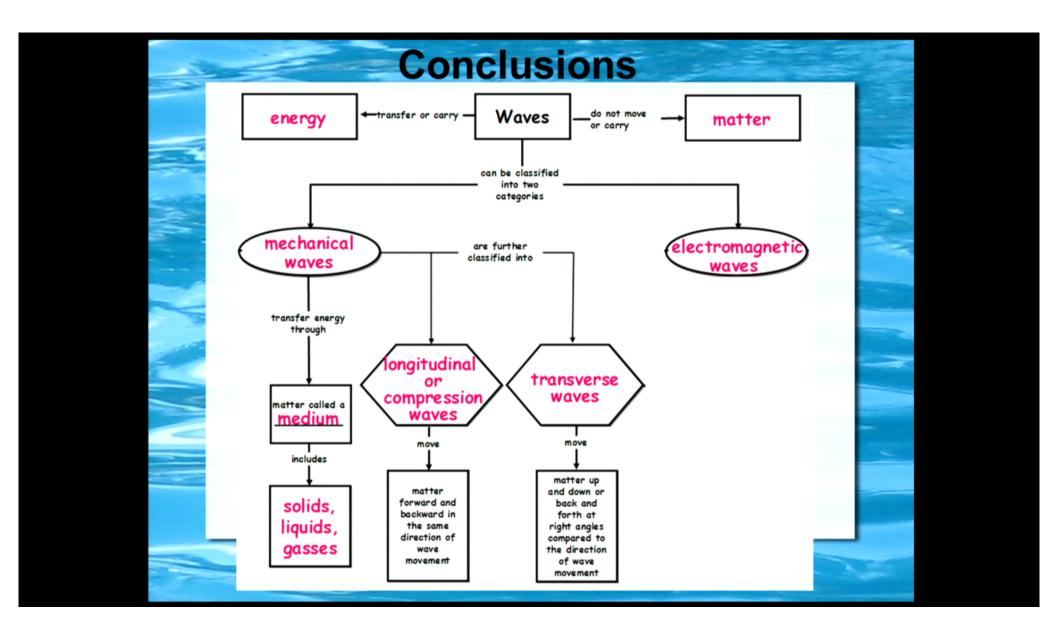
Once the effects of the disturbance dissipate, the water will return to a still pond.

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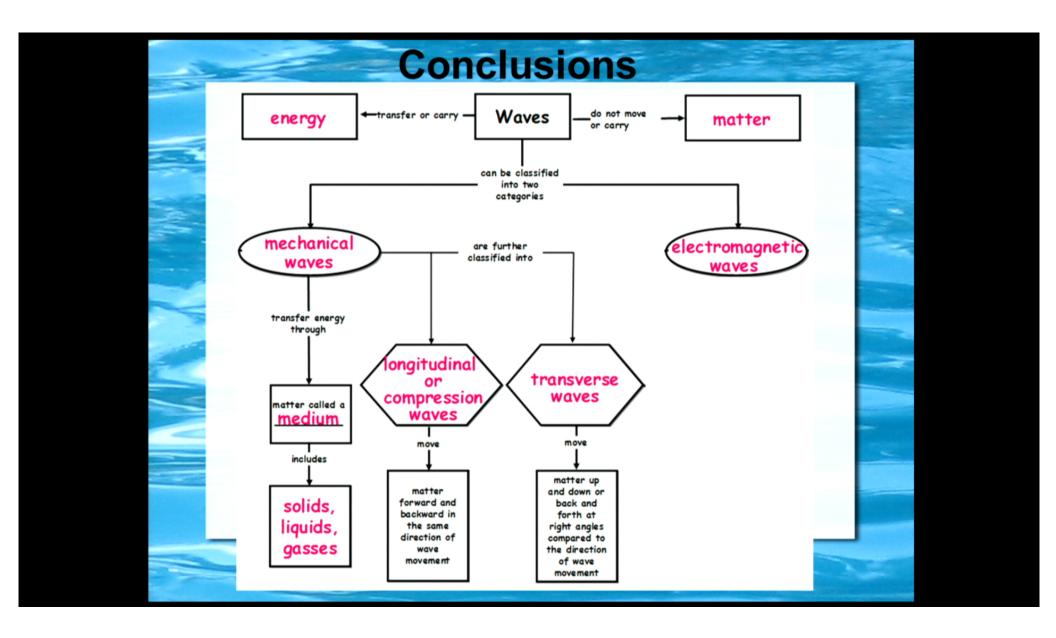
Assumptions

- ·Originally a flat and still pond.
- •Considered the pebble to be a point source when it comes in contact with the water.
- •Only the three forces mentioned are involved.
- •Wind, under-currents, biological factors are all excluded.
- •Boundaries of pond not included therefore no interference.
- •NOTE: The parameter of depth has not been investigated.

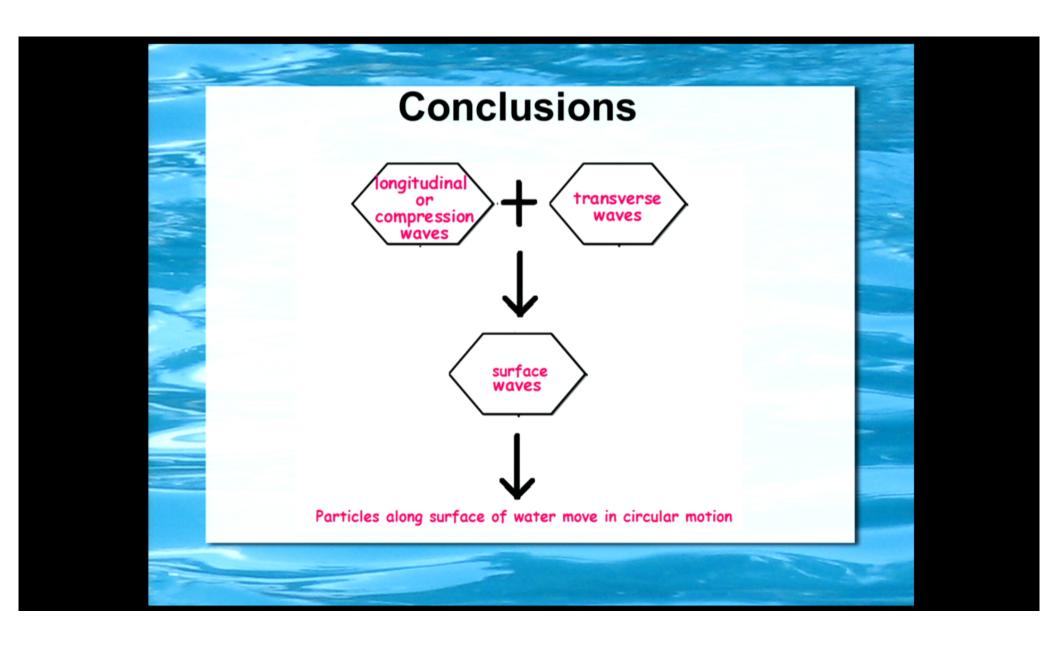
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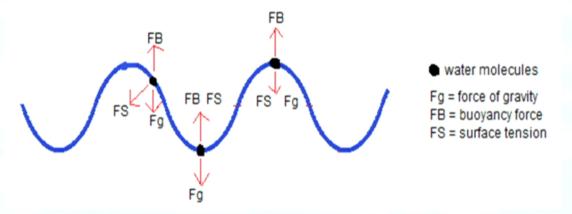


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- Three main forces acting on each water molecule force of gravity, buoyant force and most importantly surface tension.
- Longitudinal component of the surface tension.
- Surface wave Combination of both transverse and longitudinal waves.



•These surface waves execute simple harmonic motion in 2-dimensions.

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