

Title: Hidden Structures in High Dimensional Entanglement

Date: May 14, 2012 04:00 PM

URL: <http://pirsa.org/12050064>

Abstract: The minimal dimension of the Hilbert space that hosts states of an entangled pair of photons can be extremely high. The process of spontaneous parametric down-conversion (SPDC) is a possible way of producing highly entangled photon pairs, in both the spatial and temporal parts of the wave function. However, the most common approximations that are used in the analytical treatment of SPDC hinder the possibility of noticing further structures of the single joint modes. We used a more general formalism, showing that the entangled modes are still eigenfunctions of the orbital angular momentum, but the radial modes are far from the usual ones and they show novel interesting features that might be explained by introducing an additional quantum number. The problem of dealing with SPDC states has two faces: we need to know with enough confidence what state are created, and we need to know with enough confidence what states we are projecting on, upon measurement. We tried to approach both these problems together, and we showed that high dimensional entanglement shields the amount of information that can be stored in a photon from imperfect measurements. In my talk I will present both these aspects of high-dimensionally entangled states of photon pairs.

# Hidden structures in high dimensional entanglement



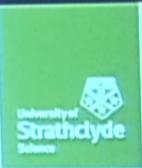
Filippo Miatto, Strathclyde University



Perimeter  
Institute, 14 May 2012



# Outline

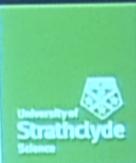


- spatial field modes and orbital angular momentum
- down-conversion and entanglement
- shared information and Schmidt modes
- generation and detection of high dimensional entanglement
- some cool stuff we can do with it

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# Spatial field modes



Scalar wave equation

$$\nabla^2 \phi - \frac{1}{c^2} \ddot{\phi} = 0$$

+

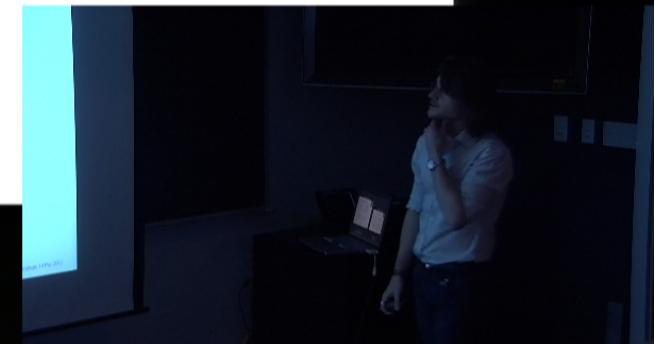
Separability  
of solutions

$$\phi(\mathbf{r}, t) = u(\mathbf{r})T(t)$$

Helmholtz equation

$$= (\nabla^2 + k^2)u = 0$$

Hankel functions  
Bessel functions  
Mathieu functions



# Spatial field modes



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# Spatial field modes



Helmholtz equation

$$(\nabla^2 + k^2)u = 0$$

+

$$u(x, y, z) = E(x, y, z)e^{ik_z z}$$

Paraxial  
approximation

$$+ \left| \frac{\partial^2 E}{\partial^2 z} \right| \ll \left| \frac{k \partial E}{\partial z} \right|$$

=

Paraxial  
Helmholtz equation

$$\left( \nabla_{\perp}^2 - 2ik \frac{\partial}{\partial z} \right) E = 0$$

# Spatial field modes



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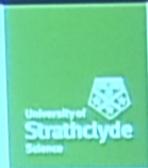
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# Spatial field modes



Paraxial  
Helmholtz equation

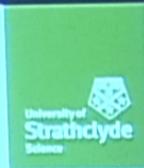
$$\left( \nabla_{\perp}^2 - 2ik \frac{\partial}{\partial z} \right) E = 0$$

Physical solutions!

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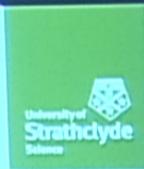
# Spatial field modes



- Standard Hermite-Gauss (HG)
- Elegant Laguerre-Gauss (ELG)
- Laguerre-Gauss (LG)
- Elegant Hermite-Gauss (EHG)
- Ince-Gauss (IG)
- Elegant Ince-Gauss (EIG)
- Helical Ince-Gauss (HIG)
- Helmholtz-Gauss (HzG)
- Bessel-Gauss (BG)
- Cosine-Gauss (CG)
- Mathieu-Gauss (MG)
- Helical Mathieu-Gauss (HMG)
- Parabolic-Gauss (PG)
- Traveling Parabolic-Gauss (TPG)
- Hypergeometric-Gauss (HyGG)
- Modified Bessel-Gauss (MBG)
- Modified Laguerre-Gauss (MLG)
- Modified Exponential-Gauss (MEG)
- Vector Helmholtz-Gauss (vHzG)
- Vector Bessel-Gauss (vBG)
- Vector even Mathieu-Gauss (vMG<sup>e</sup>)
- Vector even Parabolic-Gauss (vPG<sup>e</sup>)
- Vector Laplace-Gauss (vLpG)

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# Spatial field modes



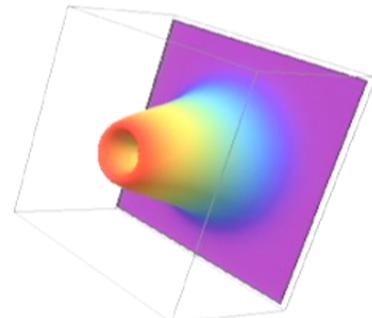
- Laguerre-Gauss (LG)

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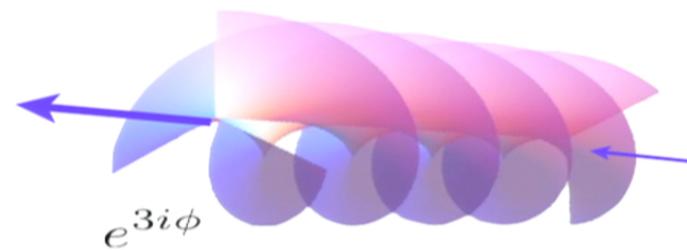
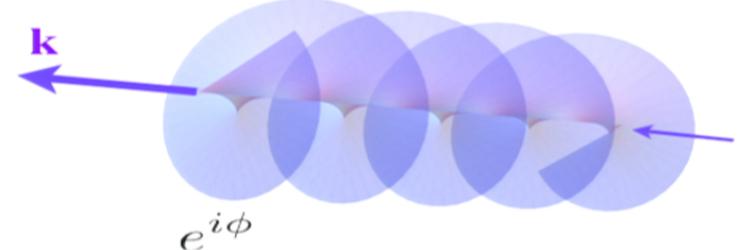
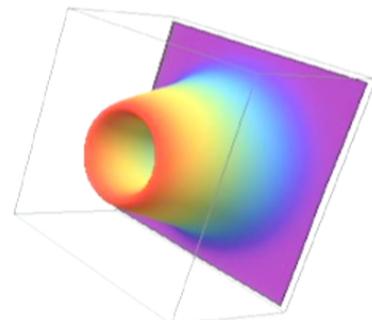
## LG modes - $\ell$



$LG_0^1$



$LG_0^3$

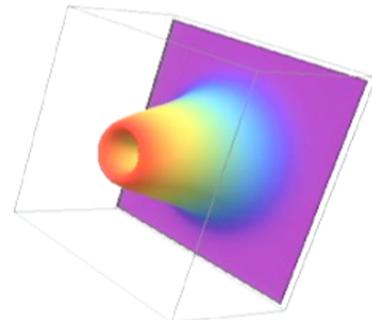


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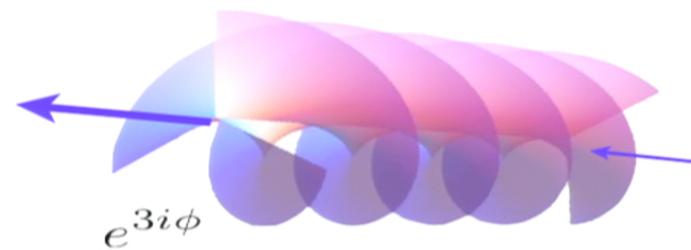
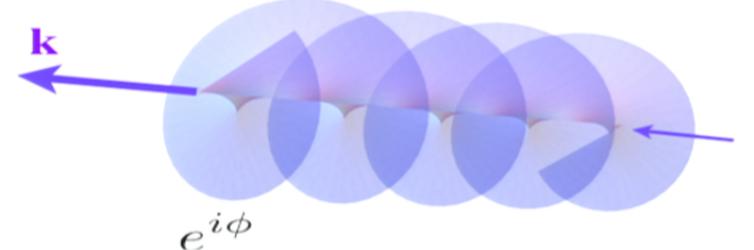
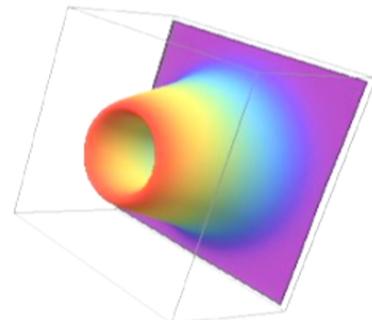
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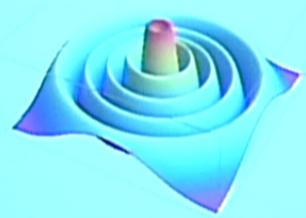
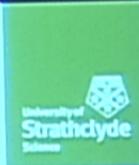


$LG_0^3$

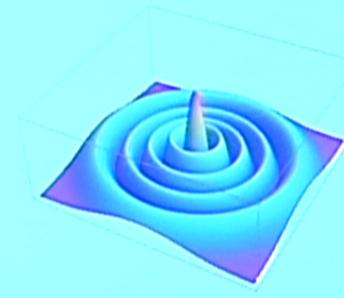


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## LG modes - p

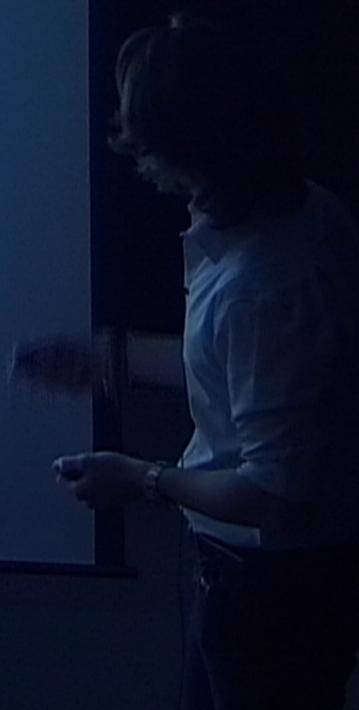


$LG_4^1$

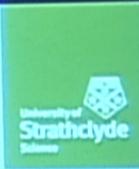


$LG_4^0$

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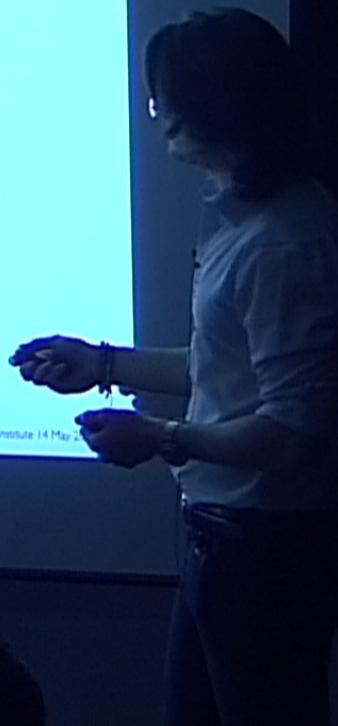
## orbital angular momentum



$$|\ell, p\rangle \longrightarrow$$



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# orbital angular momentum



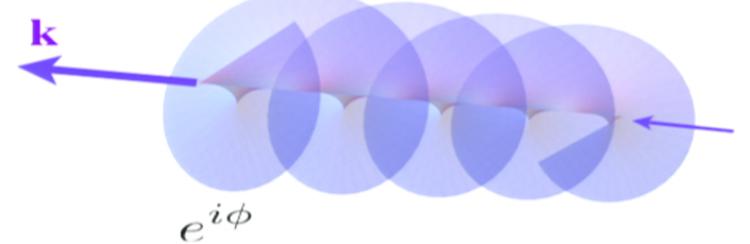
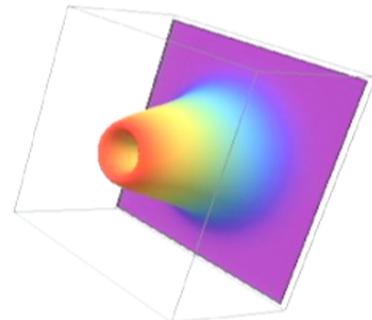
$$|\ell, p\rangle \longrightarrow$$



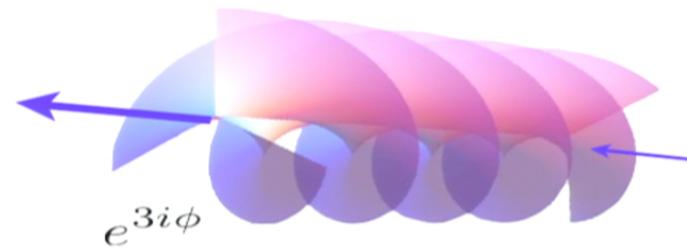
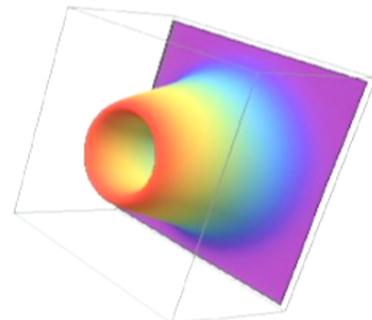
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# orbital angular momentum



$$|\ell, p\rangle \longrightarrow \text{○}$$

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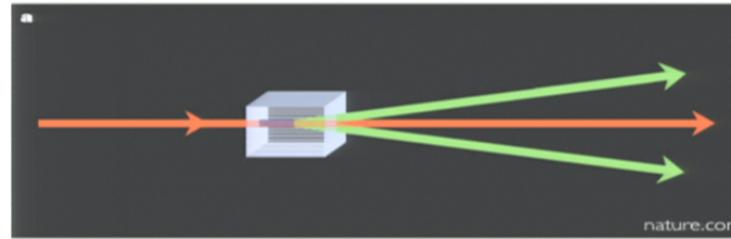
# orbital angular momentum



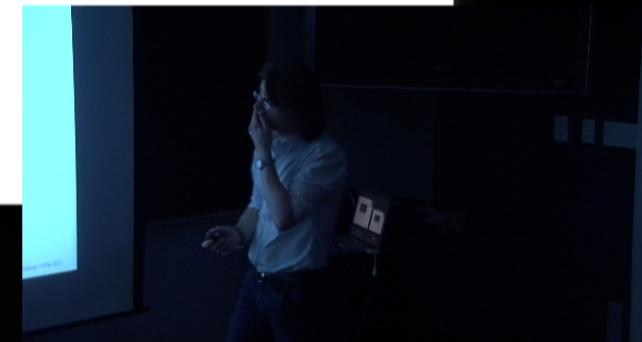
$$|\ell, p\rangle \longrightarrow \text{○}$$



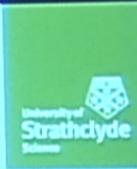
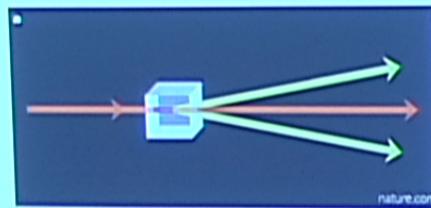
# down-conversion



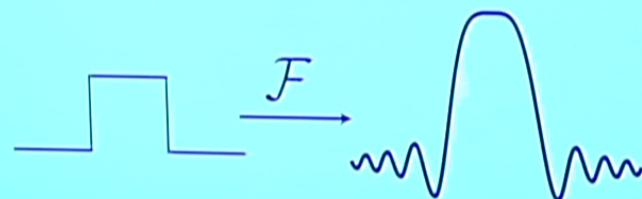
Nonlinear susceptibility → nonlinear terms in hamiltonian → down-conversion



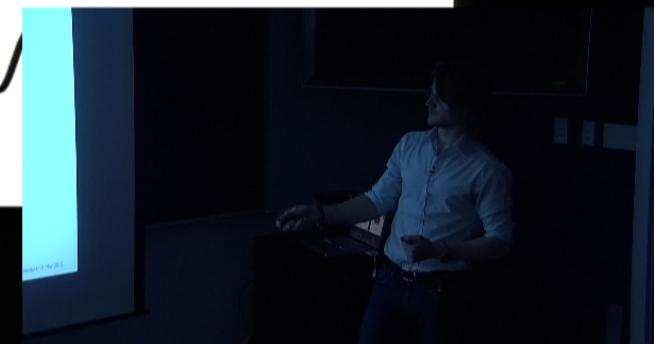
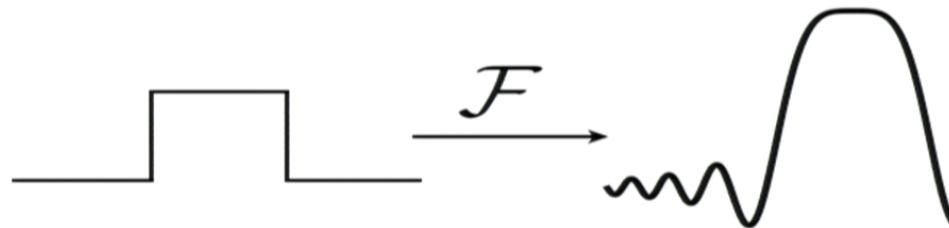
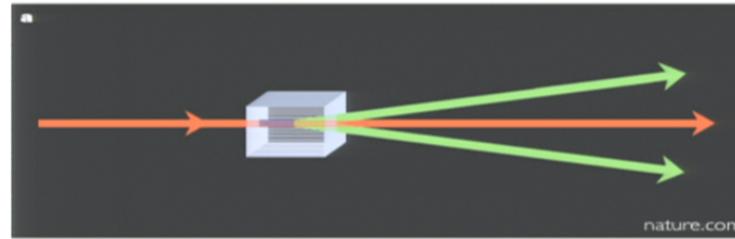
down-conversion



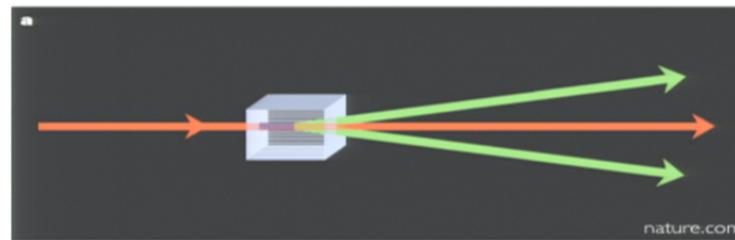
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## down-conversion



# down-conversion

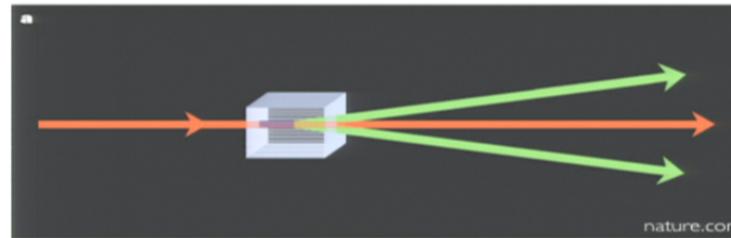


nature.com



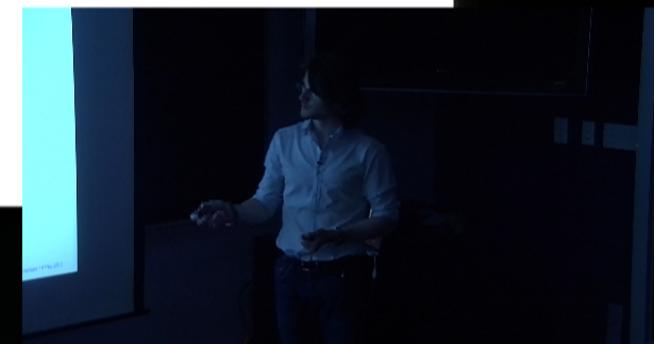
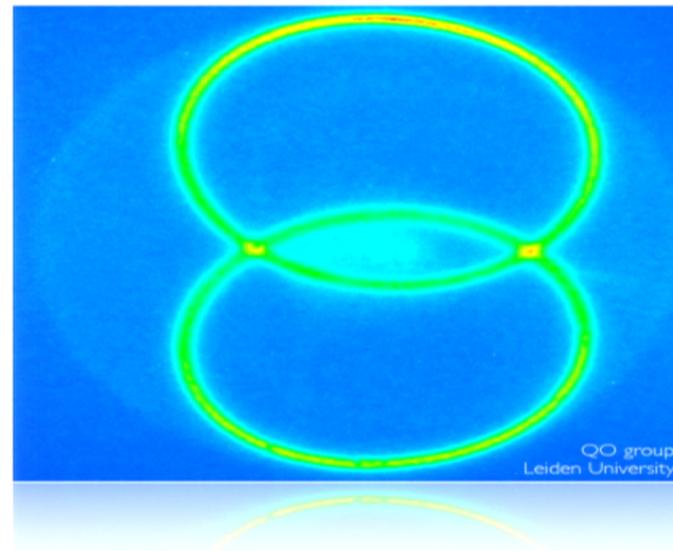
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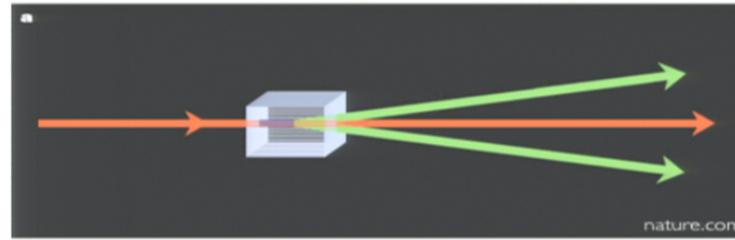


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# down-conversion



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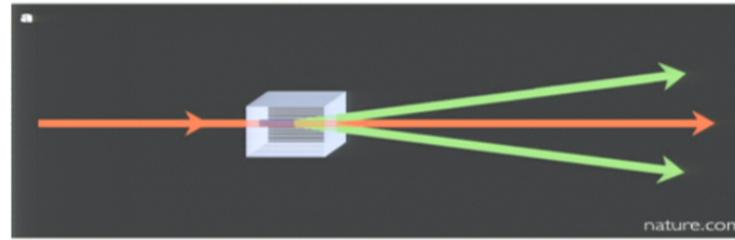
nature.com

$$\text{Hyperentanglement} = \boxed{\text{position/ momentum}} \otimes \boxed{\text{frequency/ time}} \otimes \boxed{\text{polarisation}}$$

$$\mathcal{H}_{\text{SPDC}} = \mathcal{H}_{\text{space}} \otimes \mathcal{H}_{\text{time}} \otimes \mathcal{H}_{\text{spin}}$$



# down-conversion

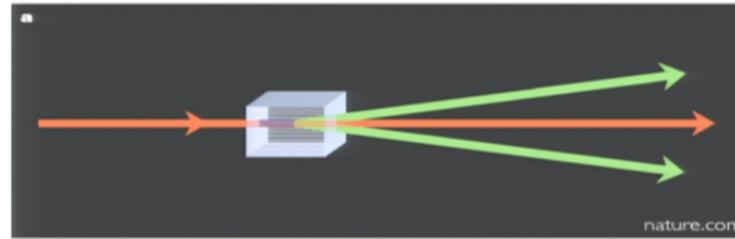


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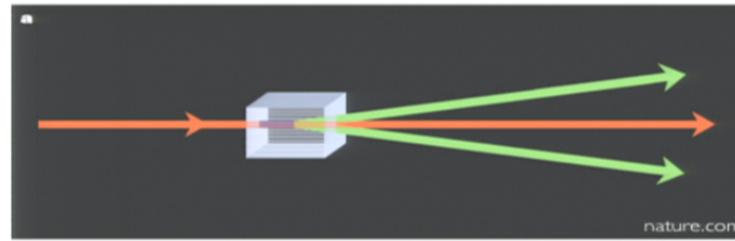


$$|\psi\rangle = \sum_{\ell,p} \sqrt{\lambda_{\ell,p}} |\ell, p\rangle \otimes |-\ell, p\rangle$$

$$K = \frac{1}{\sum_{\ell,p} \lambda_{\ell,p}^2} = 2^{H_2(\{\lambda\})}$$



## down-conversion

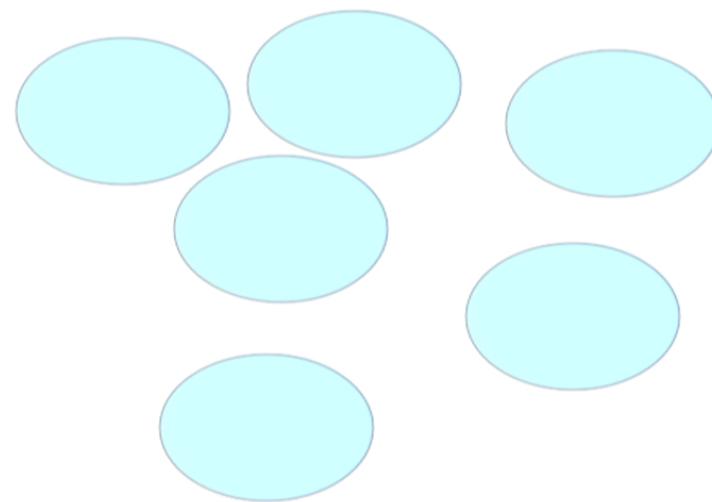


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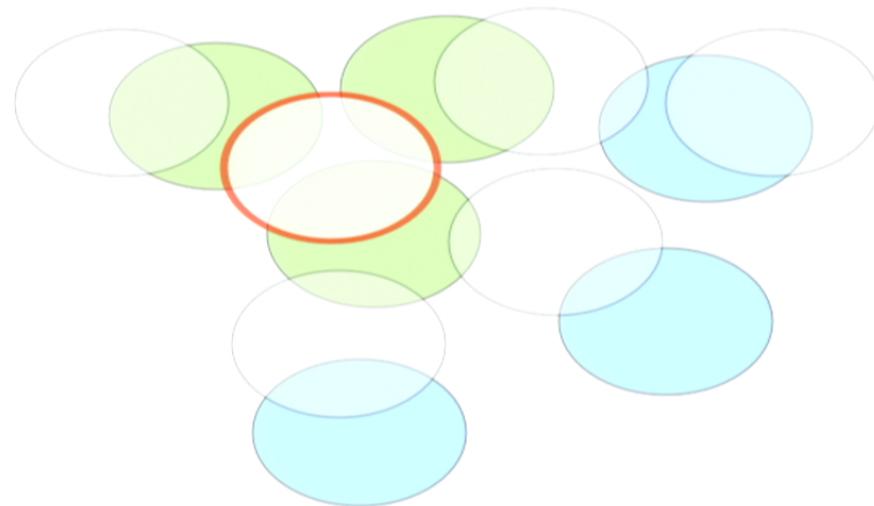


# shared information



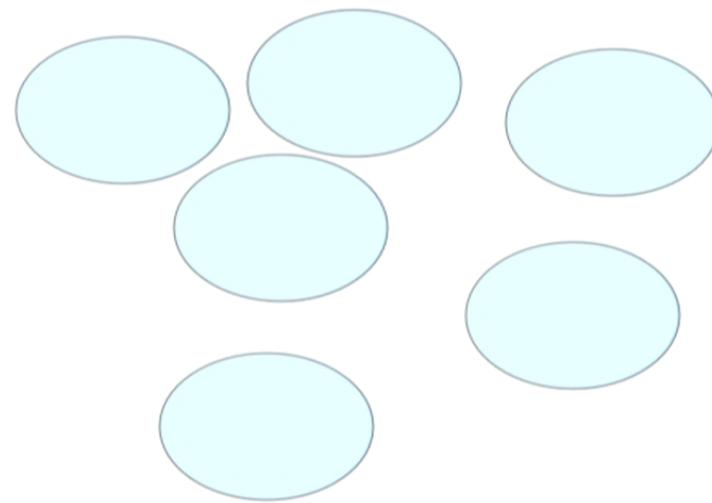
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# shared information



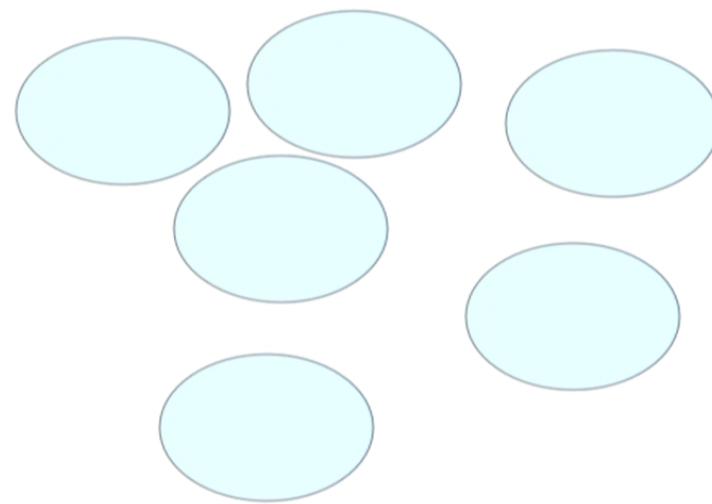
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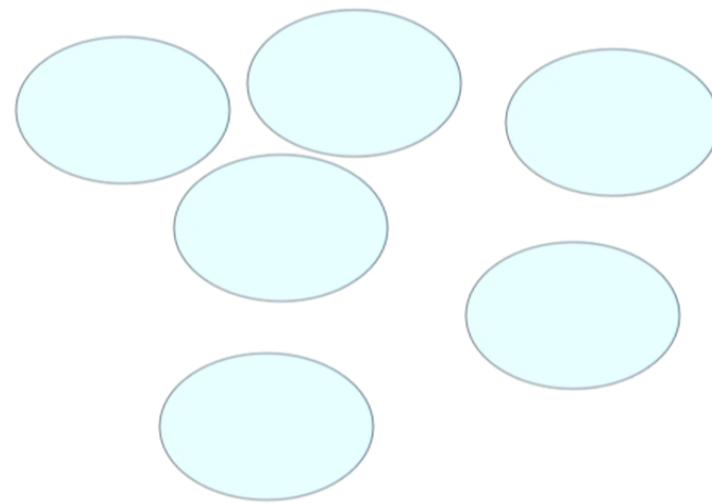
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# shared information



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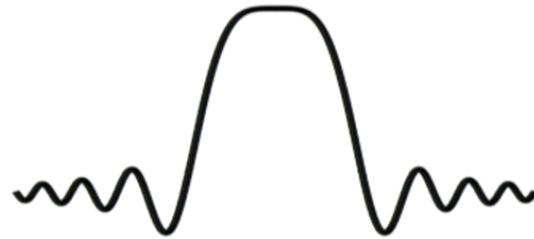


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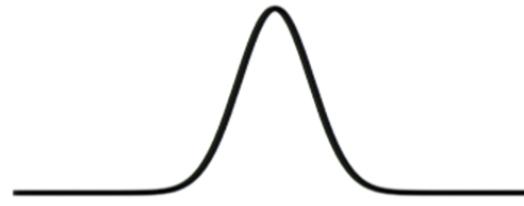
# phase matching



This is what the phase matching function looks like



This is what people approximate it with

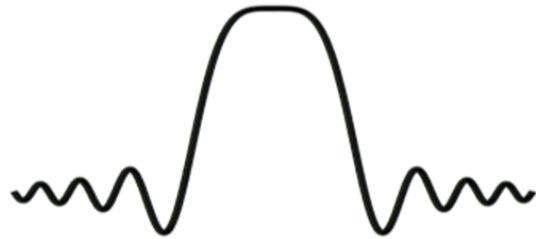


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# phase matching



This is what the phase matching function looks like



$$K = ?$$

This is what people approximate it with



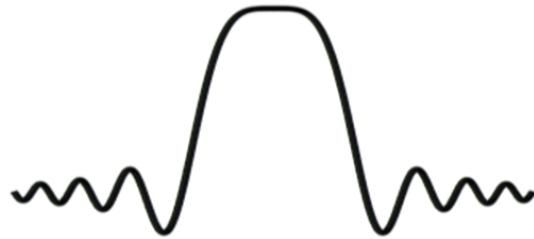
$$K = \frac{1}{4} \left( b\sigma + \frac{1}{b\sigma} \right)^2$$

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# phase matching

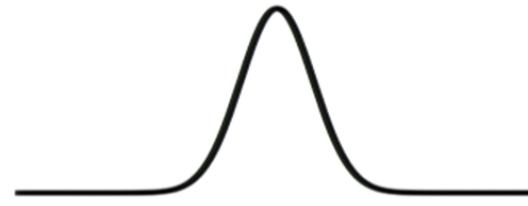


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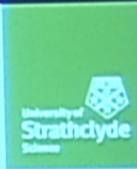
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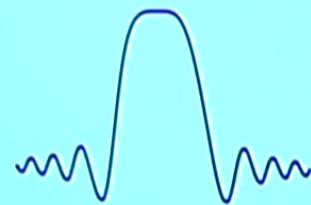
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## phase matching

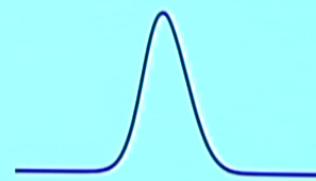


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$$K = ?$$

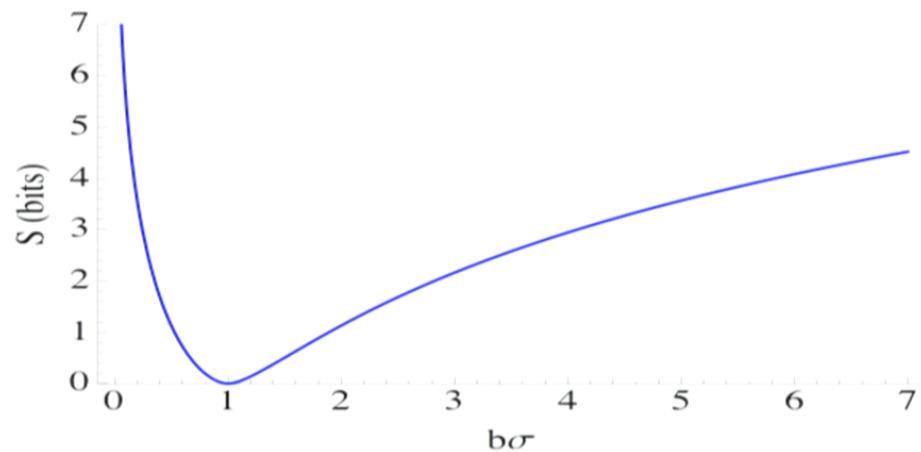
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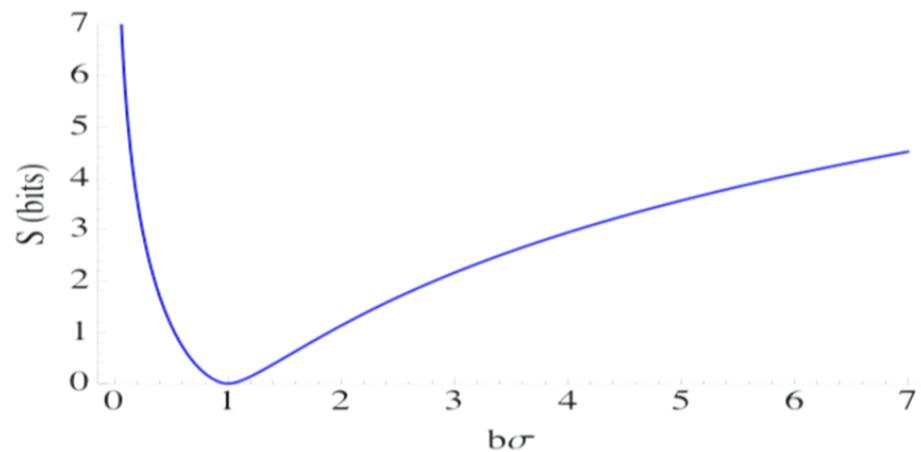
shared information



$$S(K) = \lim_{\alpha \rightarrow 1} H_\alpha$$



shared information



$$S(K) = \lim_{\alpha \rightarrow 1} H_\alpha$$



# non-ideal detection

- cross talk
- accidentals
- dark counts
- turbulence
- ...

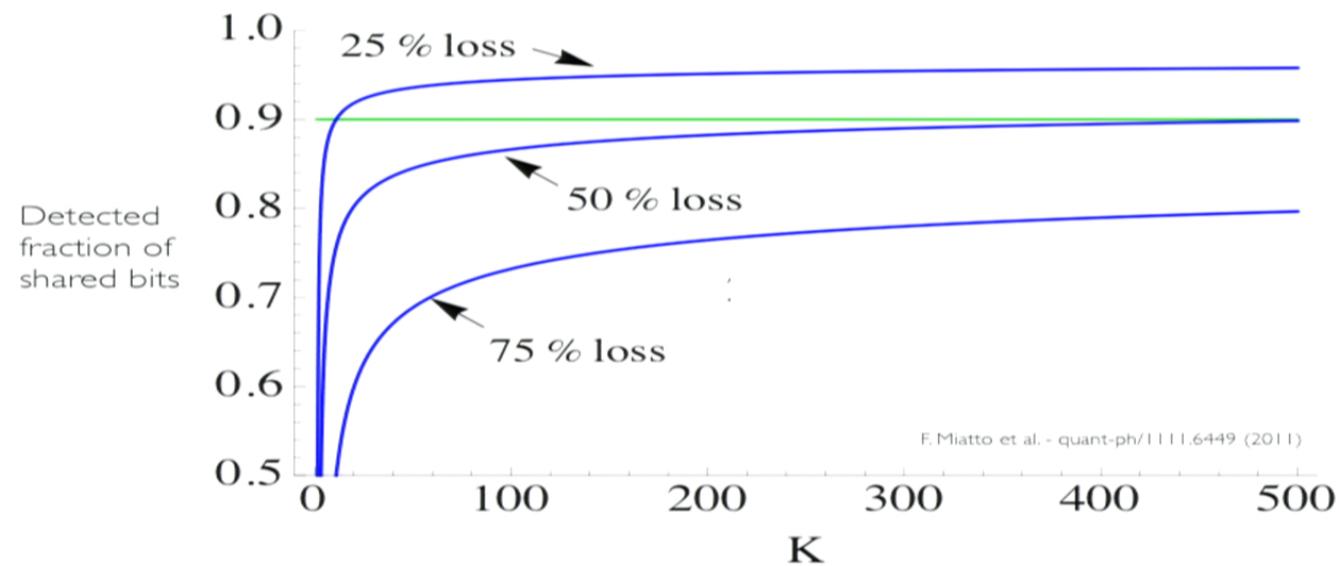


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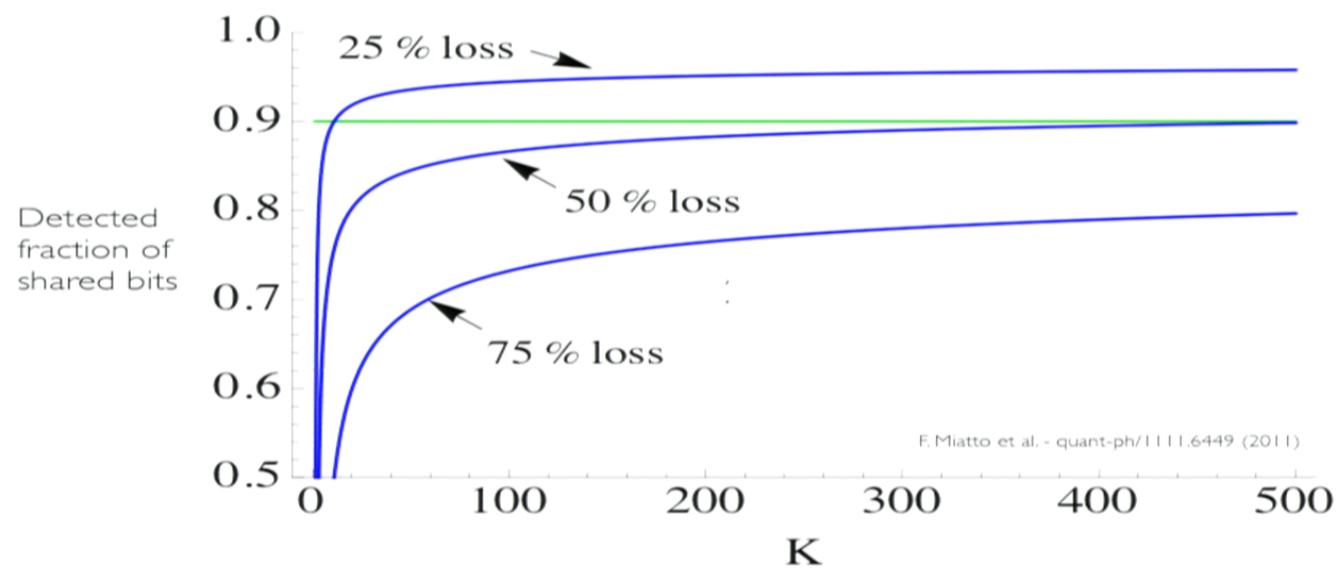


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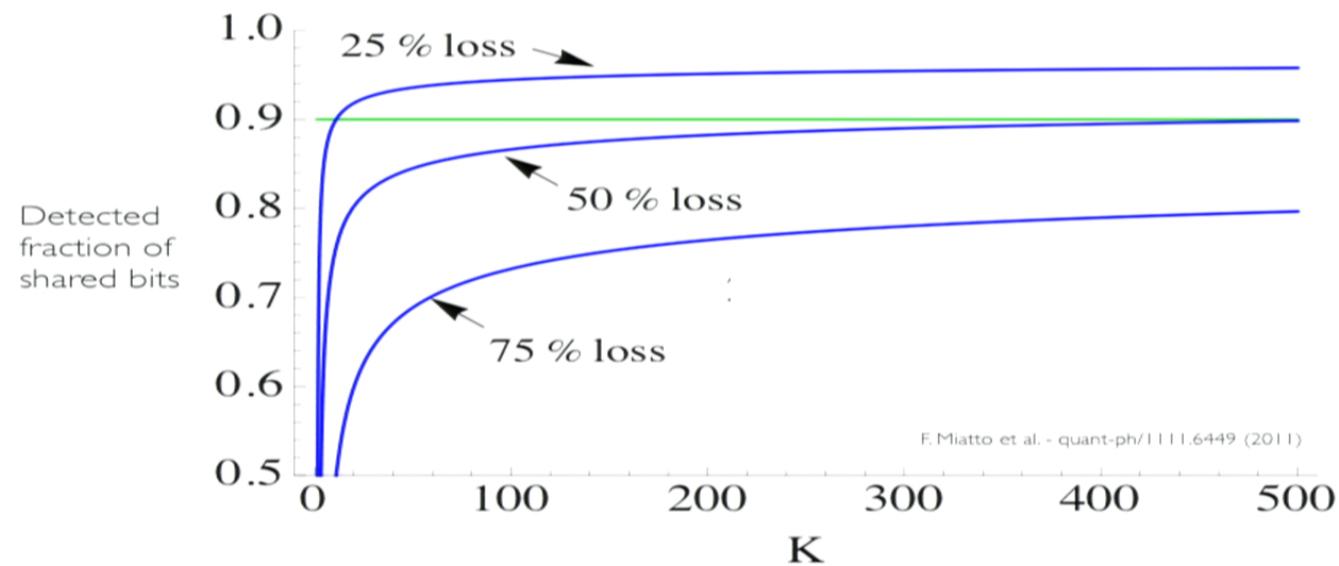


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## non-ideal detection

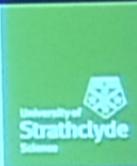


# non-ideal detection

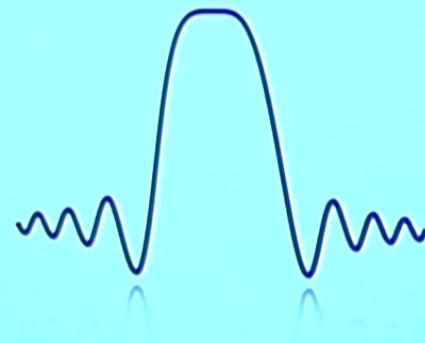


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however...



The phase matching function is not a Gaussian

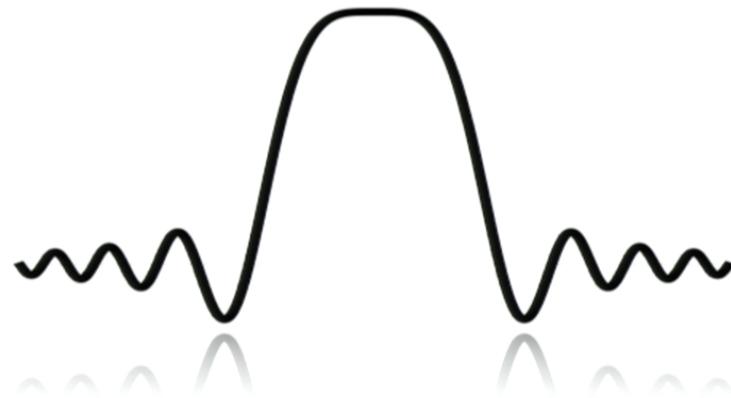


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however...

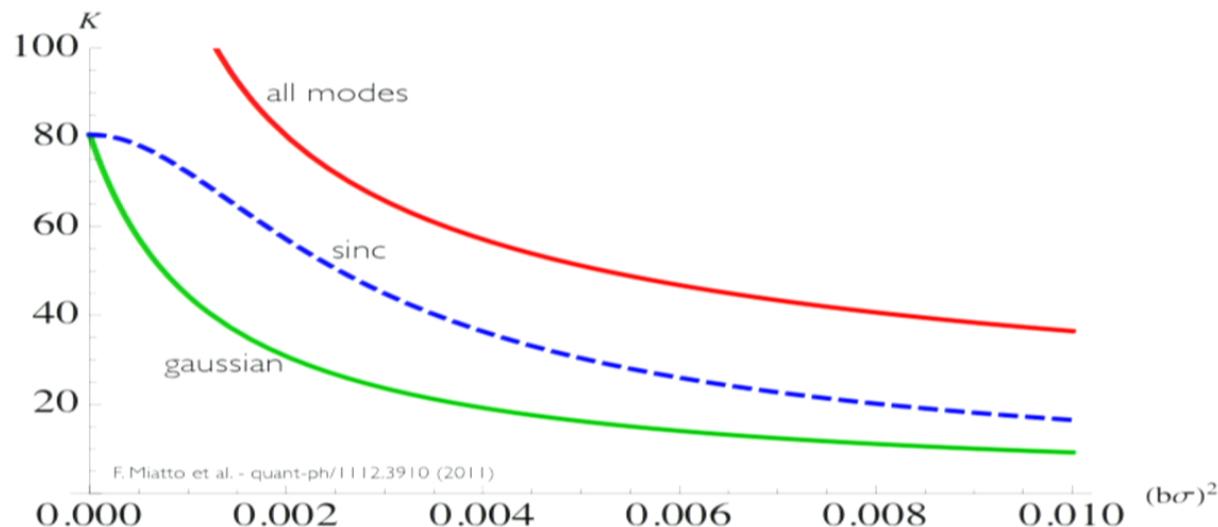


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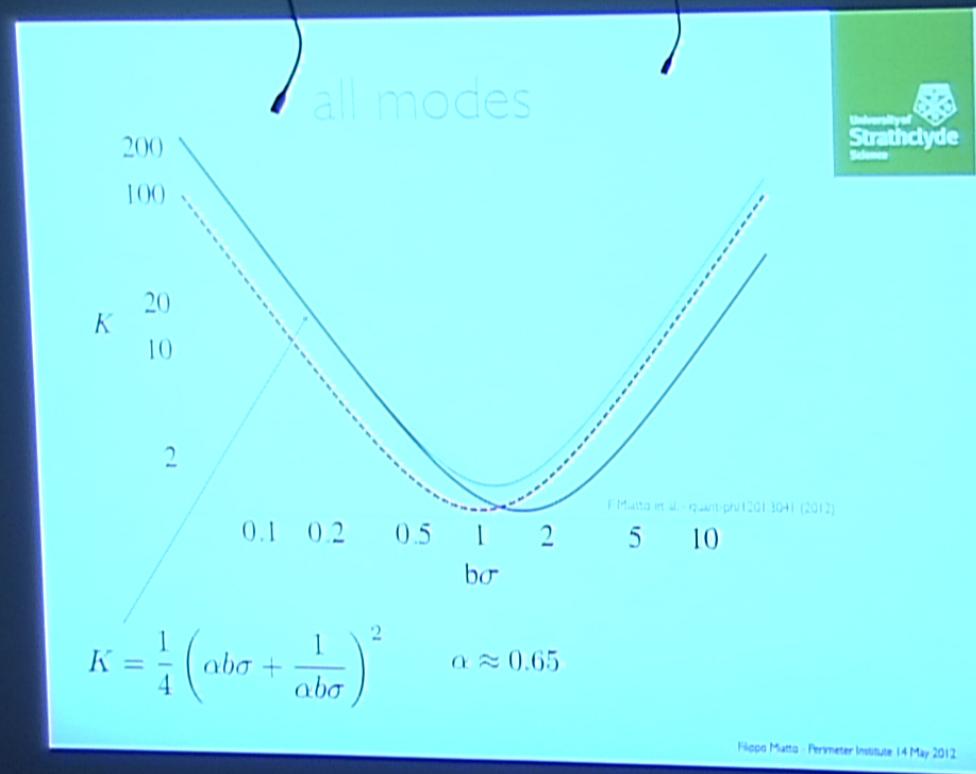
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# sinc phase matching ( $p = 0$ )

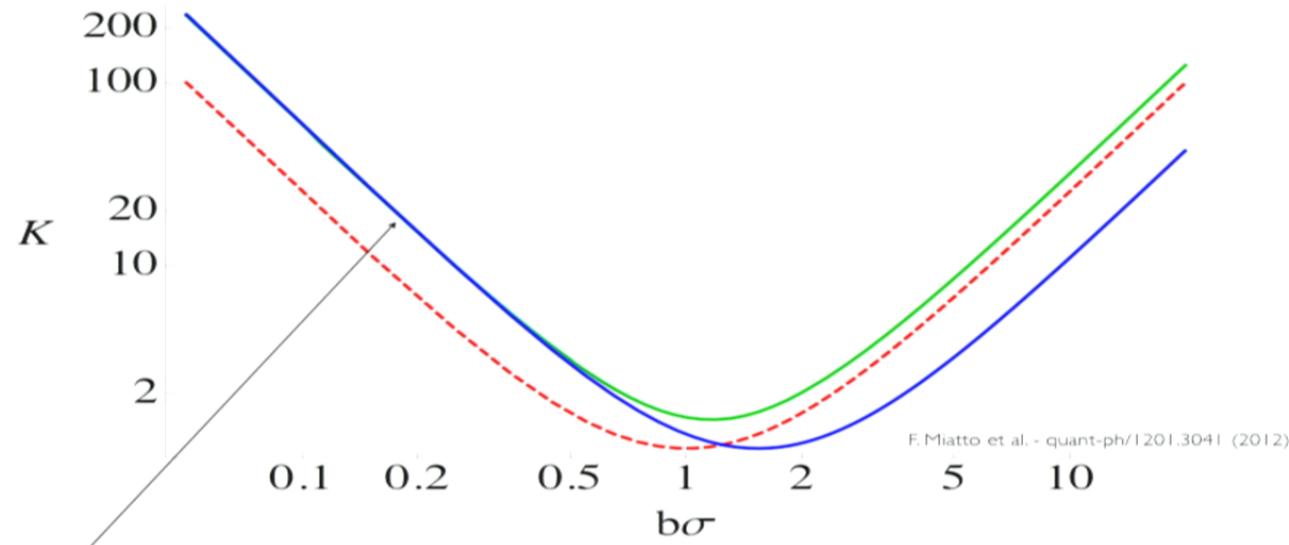


F. Miatto et al. - quant-ph/1112.3910 (2011)

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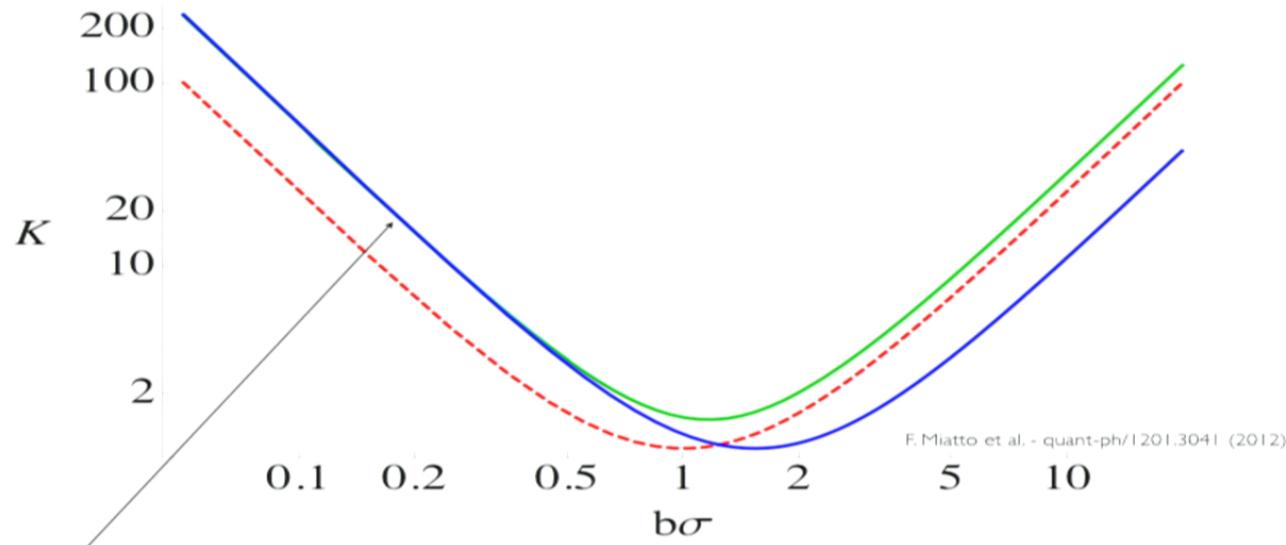
all modes



$$K = \frac{1}{4} \left( \alpha b\sigma + \frac{1}{\alpha b\sigma} \right)^2 \quad \alpha \approx 0.65$$

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all modes



$$K = \frac{1}{4} \left( \alpha b\sigma + \frac{1}{\alpha b\sigma} \right)^2 \quad \alpha \approx 0.65$$

F. Miatto et al. - quant-ph/1201.3041 (2012)

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however...



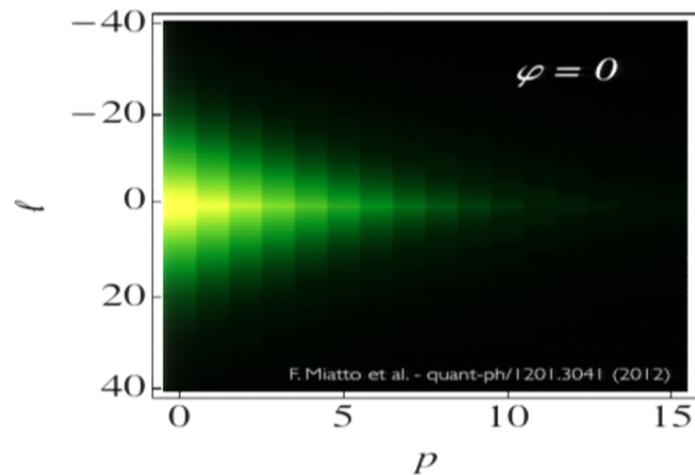
The photons can be phase-mismatched



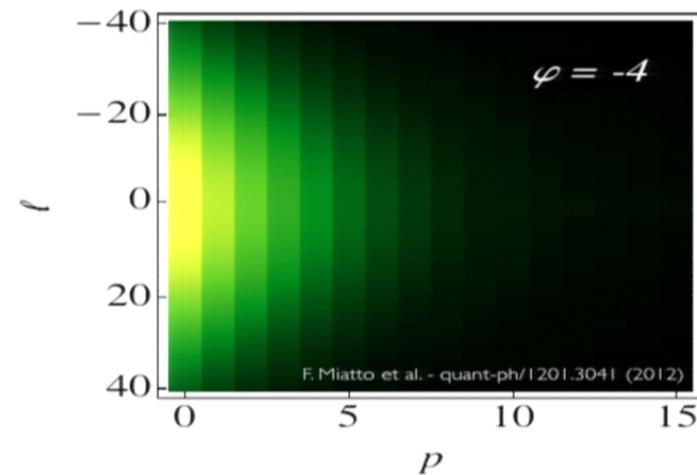
# general Schmidt weights



$K \approx 232$



$K \approx 425$

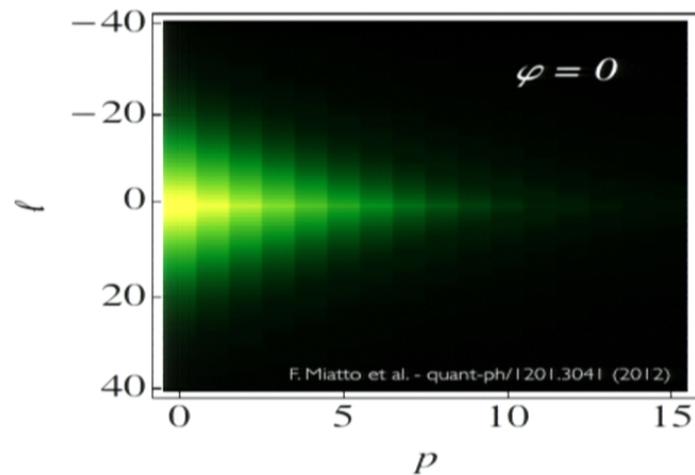


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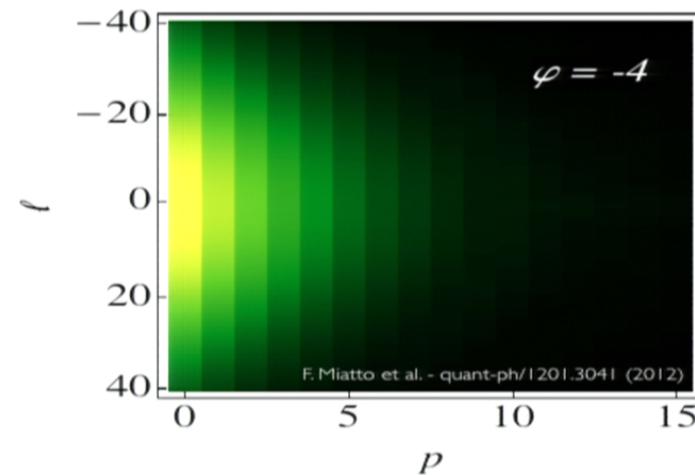
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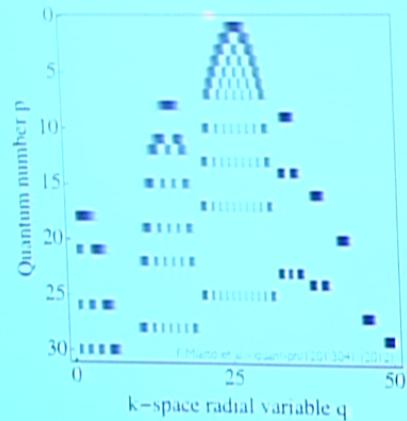


$K \approx 425$



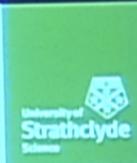
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## general Schmidt modes

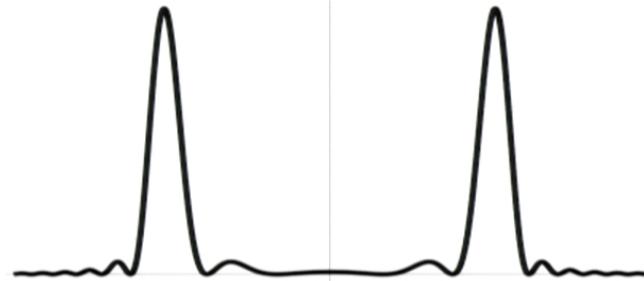
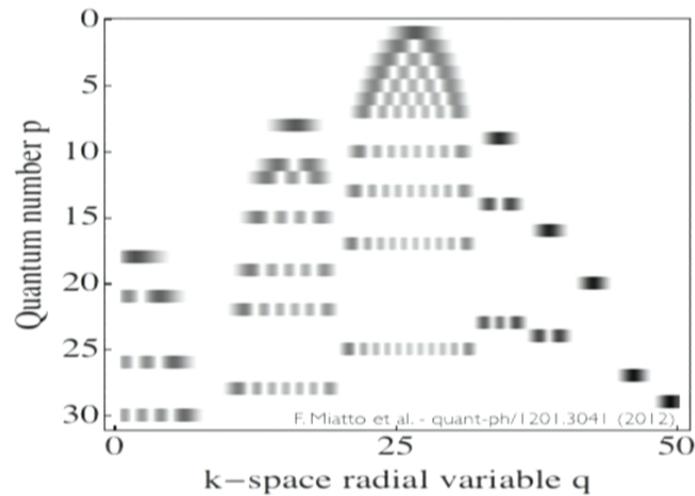


$$p \sim (r, m)$$

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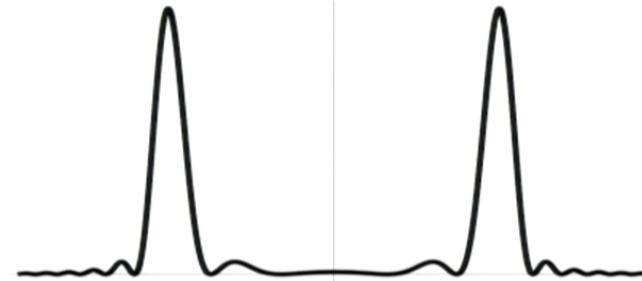
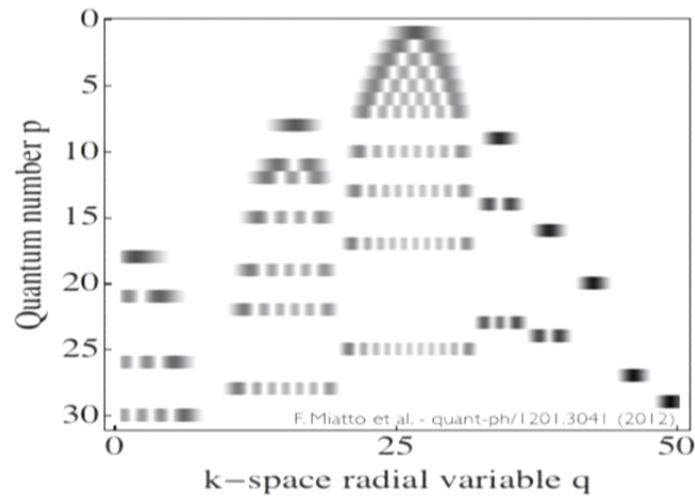
# general Schmidt modes



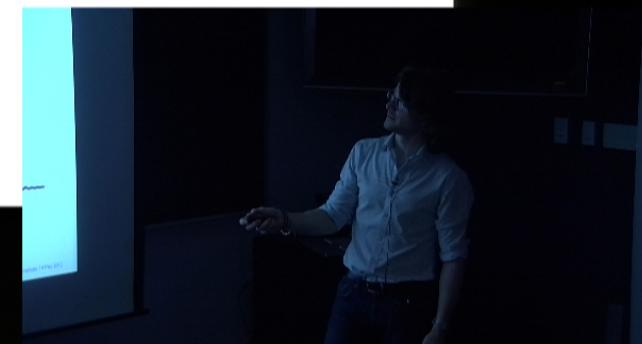
$$p \sim (r, m)$$

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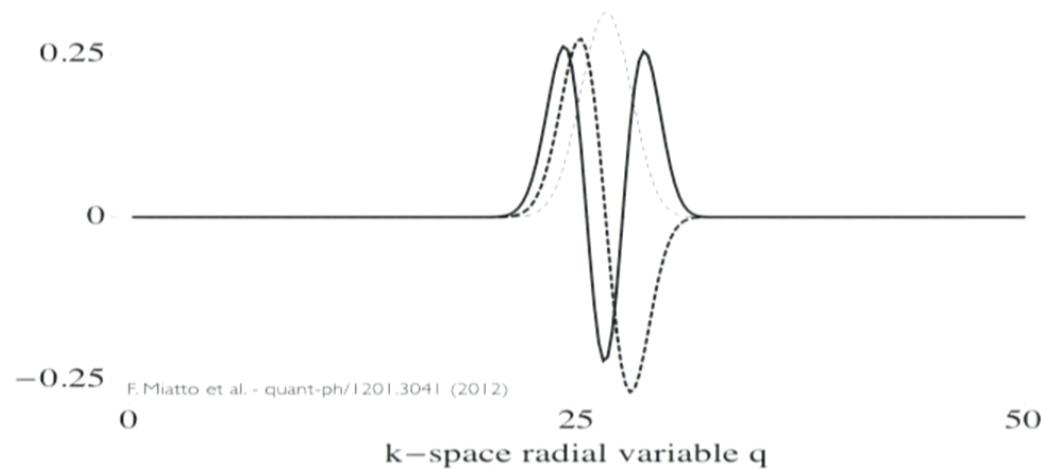
# general Schmidt modes



$$p \sim (r, m)$$

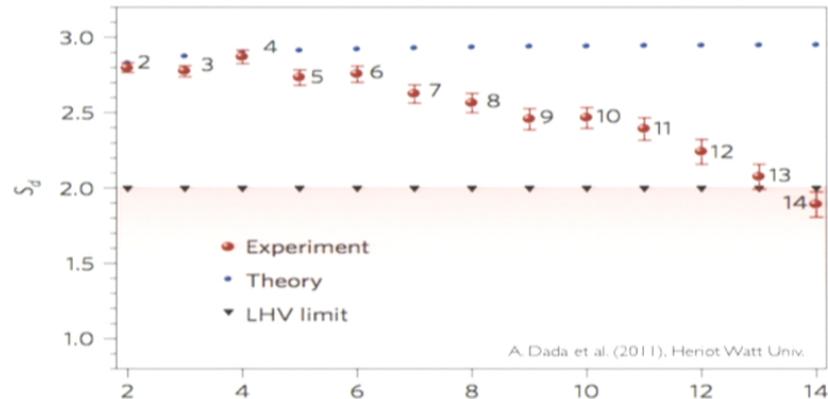


# general Schmidt modes



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nature  
physics

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PUBLISHED ONLINE: 8 MAY 2011 | DOI:10.1038/NPHYS1996

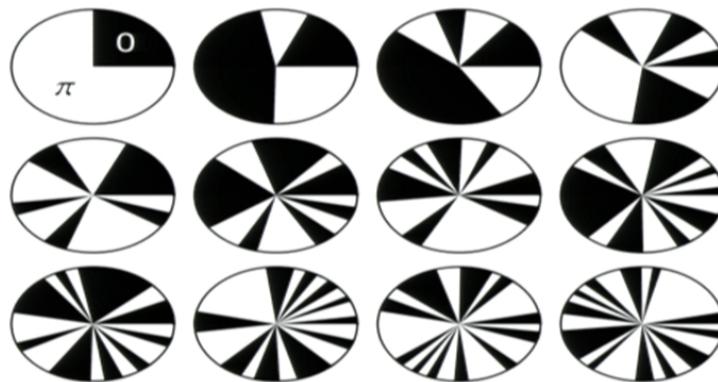
## Experimental high-dimensional two-photon entanglement and violations of generalized Bell inequalities

Adetunmise C. Dada<sup>1\*</sup>, Jonathan Leach<sup>2</sup>, Gerald S. Buller<sup>1</sup>, Miles J. Padgett<sup>2</sup> and Erika Andersson<sup>1</sup>

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J. Opt. 13 (2011) 064008 (8pp)

JOURNAL OF OPTICS

doi:10.1088/2040-8978/13/6/064008

## High-dimensional entanglement with orbital-angular-momentum states of light

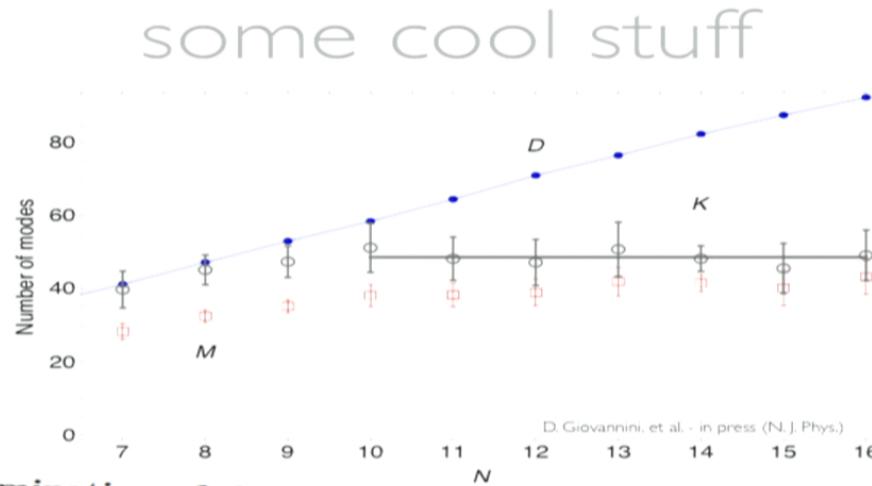
Bart-Jan Pors<sup>1</sup>, Filippo Miatto<sup>1,2,4</sup>, G W 't Hooft<sup>1,3</sup>, E R Eliel<sup>1</sup> and  
J P Woerdman<sup>1</sup>

<sup>1</sup> Huygens Laboratory, Leiden University, PO Box 9504, 2300 RA Leiden, The Netherlands

<sup>2</sup> Dipartimento di Fisica 'Galileo Galilei', University of Padua, via Marzolo,  
8, I-35131 Padova, Italy

<sup>3</sup> Philips Research Laboratories, 5656 AE, Eindhoven, The Netherlands

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## Determination of the dimensionality of bipartite orbital-angular-momentum entanglement using multi-sector phase masks

D. Giovannini<sup>1</sup>, F. M. Miatto<sup>2</sup>, J. Romero<sup>1,2</sup>,  
S. M. Barnett<sup>2</sup>, J. P. Woerdman<sup>3</sup>, M. J. Padgett<sup>1</sup>

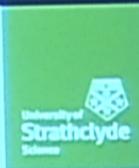
<sup>1</sup> School of Physics and Astronomy, SUPA, University of Glasgow, Glasgow G12 8QQ, United Kingdom

<sup>2</sup> Department of Physics, SUPA, University of Strathclyde, Glasgow G4 0NG, United Kingdom

<sup>3</sup> Huygens Laboratory, Leiden University, PO Box 9504, 2300 RA Leiden, The Netherlands



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## Transport of orbital-angular-momentum entanglement through a turbulent atmosphere

Bart-Jan Pors,<sup>1,\*</sup> C. H. Monken,<sup>1,2</sup> Eric R. Eliel,<sup>1</sup> and J. P. Woerdman<sup>1</sup>

<sup>1</sup>Huygens Laboratory, Leiden University, P.O. Box 9504, 2300 RA Leiden, The Netherlands

<sup>2</sup>Departamento de Física, Universidade Federal de Minas Gerais, Caixa Postal 702, Belo Horizonte, MG 30161-970, Brazil

\*pors@mpphys.leidenuniv.nl

**Abstract:** We demonstrate experimentally how orbital-angular-momentum entanglement of two photons evolves under the influence of atmospheric turbulence. Experimental results are in excellent agreement with our theoretical model, which combines the formalism of two-photon coincidence detection with a Kolmogorov description of atmospheric turbulence. We express the robustness to turbulence in terms of the dimensionality of the measured correlations. This dimensionality is surprisingly robust: scaling up our system to real-life dimensions, a horizontal propagation distance of 2 km seems viable.

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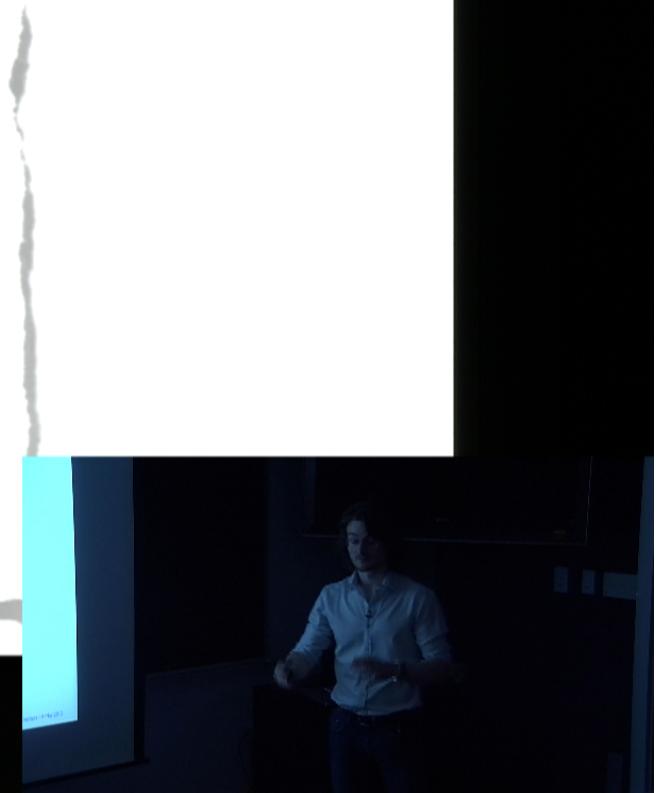
<sup>1</sup>Huygens Laboratory, Leiden University, P.O. Box 9504, 2300 RA Leiden, The Netherlands

<sup>2</sup>Departamento de Física, Universidade Federal de Minas Gerais, Caixa Postal 702, Belo Horizonte, MG 30161-970, Brazil

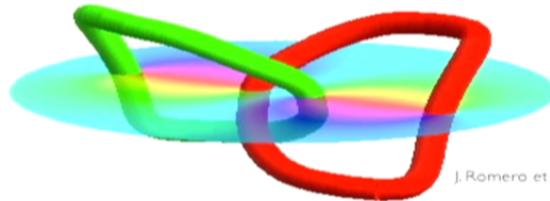
[pors@molphys.leidenuniv.nl](mailto:pors@molphys.leidenuniv.nl)

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J.Romero et al (2011), Glasgow Univ.

PRL 106, 100407 (2011)

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11 MARCH 2011

### Entangled Optical Vortex Links

J. Romero,<sup>1,2</sup> J. Leach,<sup>1</sup> B. Jack,<sup>1</sup> M. R. Dennis,<sup>3</sup> S. Franke-Arnold,<sup>1</sup> S. M. Barnett,<sup>2</sup> and M. J. Padgett<sup>1</sup>

<sup>1</sup>School of Physics and Astronomy, SUPA, University of Glasgow, Glasgow G12 8QQ, United Kingdom

<sup>2</sup>Department of Physics, SUPA, University of Strathclyde, Glasgow G4 0NG, United Kingdom

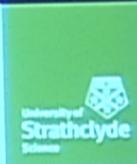
<sup>3</sup>H. H. Wills Physics Laboratory, University of Bristol, Bristol BS8 1TL, United Kingdom

(Received 15 June 2010; revised manuscript received 9 November 2010; published 11 March 2011)

Optical vortices are lines of phase singularity which percolate through all optical fields. We report the entanglement of linked optical vortex loops in the light produced by spontaneous parametric down-conversion. As measured by using a Bell inequality, this entanglement between topological features extends over macroscopic and finite volumes. The entanglement of photons in complex three-dimensional topological states suggests the possibility of entanglement of similar features in other quantum systems describable by complex scalar functions, such as superconductors, superfluids, and Bose-Einstein condensates.

Filippo Miatto - Perimeter Institute | 4 May 2012

## conclusions



- high dimensional spatial entanglement of thousands of modes has been reached
- it is relatively easy to produce, control and measure
- if combined with high dimensional temporal entanglement it can yield vast Hilbert spaces to play with
- down-conversion still has some mysteries, which could bear potential further benefits
- There is a lot of room to play with tests of QM, implementations of QI protocols, communications, cryptography

Ricardo Matto - Perimeter Institute, 14 May 2012

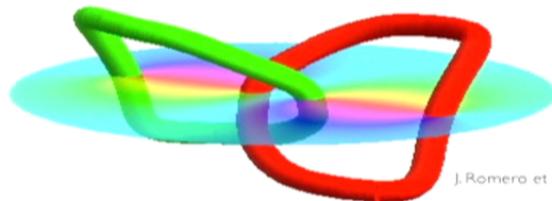
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Filippo Miatto - Perimeter Institute | 4 May 2012

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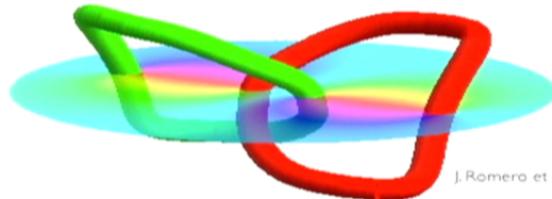
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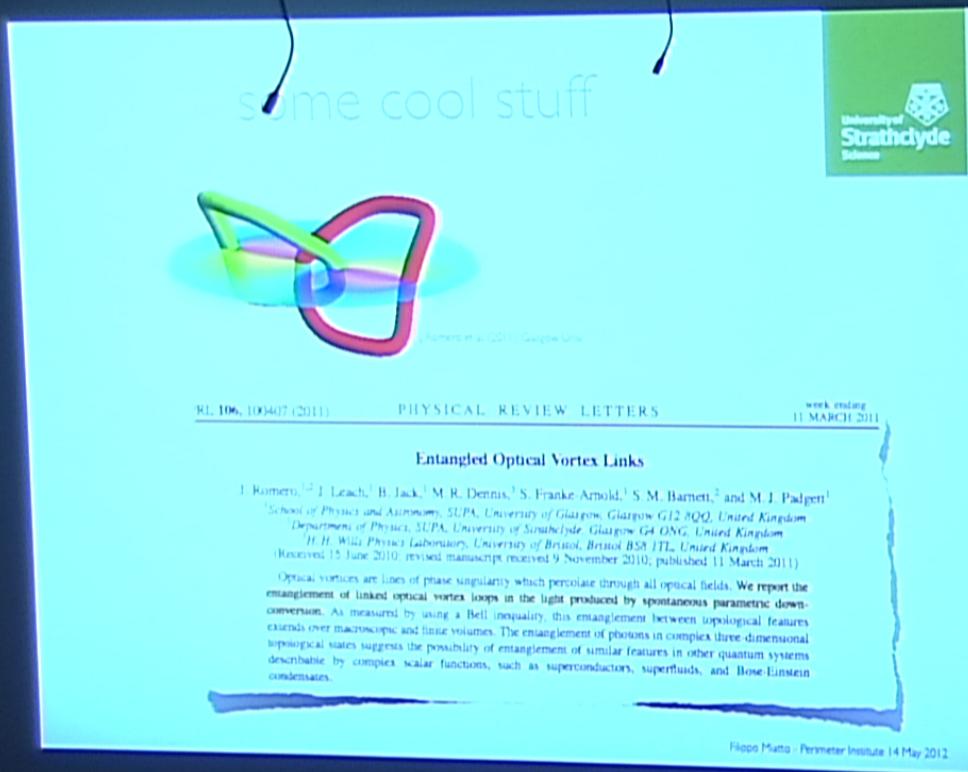
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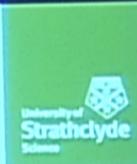
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Rieppi Matto - Perimeter Institute (4 May 2012)

