

Title: Emergent Conformal Violation: Does Inflation Like Fundamental Scalar Fields?

Date: May 11, 2012 03:20 PM

URL: <http://pirsa.org/12050057>

Abstract: We present a new model of inflation which does not rely on fundamental scalar fields. The theory is a conformally invariant gauge field theory minimally coupled to massless fermions. At the beginning of inflation, the conformal symmetry is dynamically broken by a BCS condensation of the fermions, leading to a spontaneous violation of conformal symmetry. A quasi de-Sitter inflationary regime is driven by the interaction between a homogenous plasma dynamo between the gauge, gravitational and condensate field. Unique observational consequences of this model are twofold : (1) The sourcing of B-mode vorticity fluctuations in upcoming CMB powerspectra. (2) A possible inflationary Baryogenesis mechanism connected to the initial conditions of inflation.

## Why another model of Inflation?

- I) We want to obtain inflation from known physical fields.
- II) We would like to address new particle physics connection to inflation.
- III) New predictions for upcoming CMB observations.

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# Does Inflation Like Fundamental Scalars?

Stephon Alexander

Conformal Nature of the  
Universe, PI



DARTMOUTH COLLEGE

in collaboration with Antonino Marciano and  
David Spergel  
based on [arXiv:1107.0318](https://arxiv.org/abs/1107.0318) [hep-th]

# Motivation

## Why another model of Inflation?

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# Roots of Inflation

- Guth (and others) originally proposed inflation by using ideas from:
  - (1) **Condensed Matter Physics:** (Spontaneous symmetry breaking).
  - (2) **Particle Physics:** SU(5) GUT. (Old Inflation)
- This idea did not work (too much anisotropy, bubble nucleation).
- More “improved models” (New Inflation, Slow roll)

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# Slow Roll “Chaotic

RECIPE:



Initial condition: Magically place scalar field at the top.

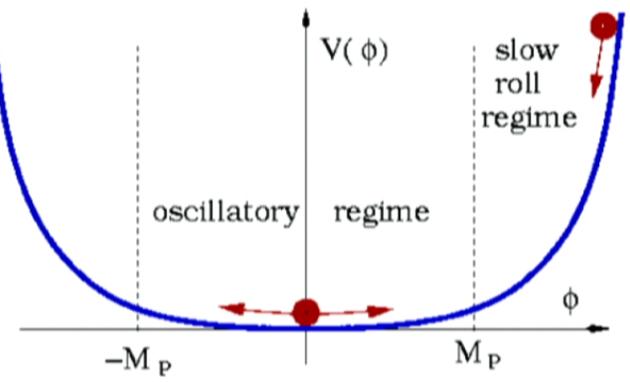
$$S[\phi] \rightarrow \int d^4x \sqrt{-g} \frac{1}{2} (-\partial_\mu \phi \partial^\mu \phi - m^2 \phi^2)$$

Begin: ( $10^{-37}$  sec!)

$$H^2 = \left( \frac{1}{a} \frac{da}{dt} \right)^2 = \frac{1}{3M_{pl}^2} \left( \frac{1}{2} \left( \frac{d\phi}{dt} \right)^2 + \frac{1}{2} m^2 \phi^2 \right)$$

$$\Rightarrow H \approx H_0 = \frac{m_0}{\sqrt{6} M_{pl}}$$

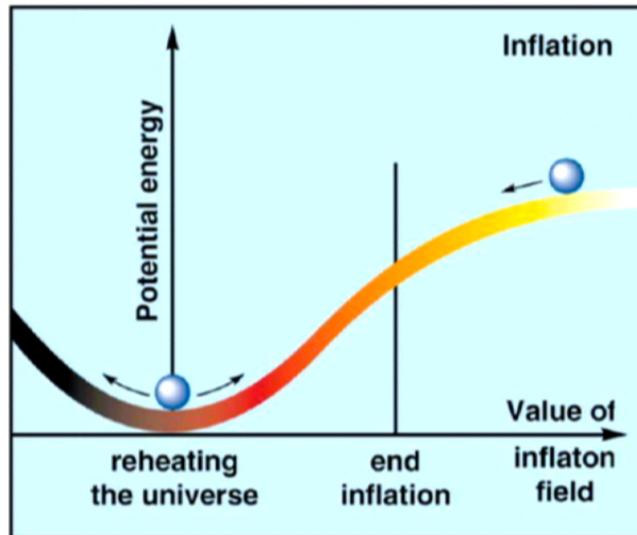
$$\Rightarrow d^2 a / dt^2 \approx H_0^2 a > 0 \rightarrow \text{acceleration! } a \approx a_0 \exp(H_0 t),$$



Chaotic Inflationary Model (Linde 1982)

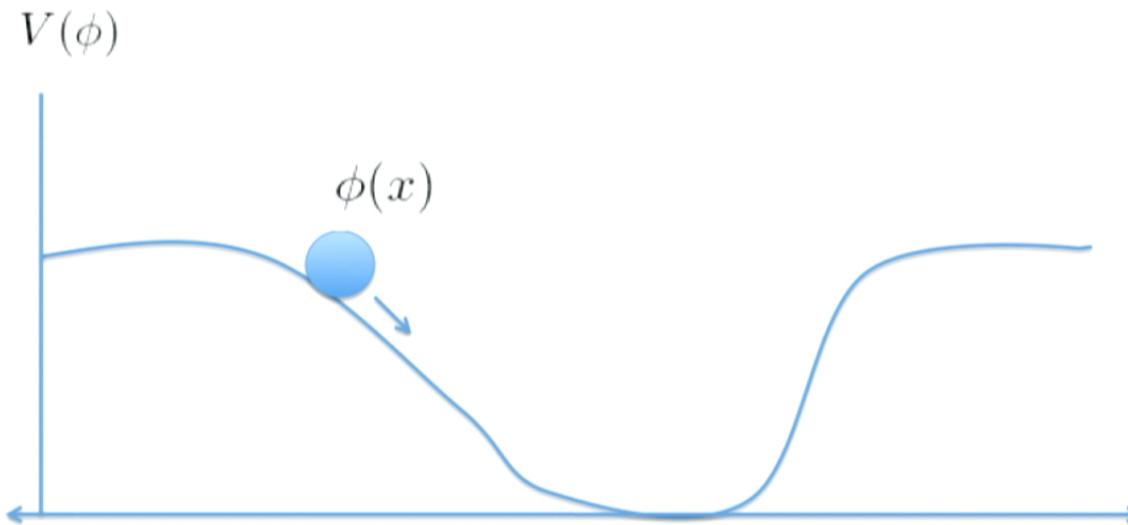
Credit: T. Prokopec

# Scalar Inflation Summary

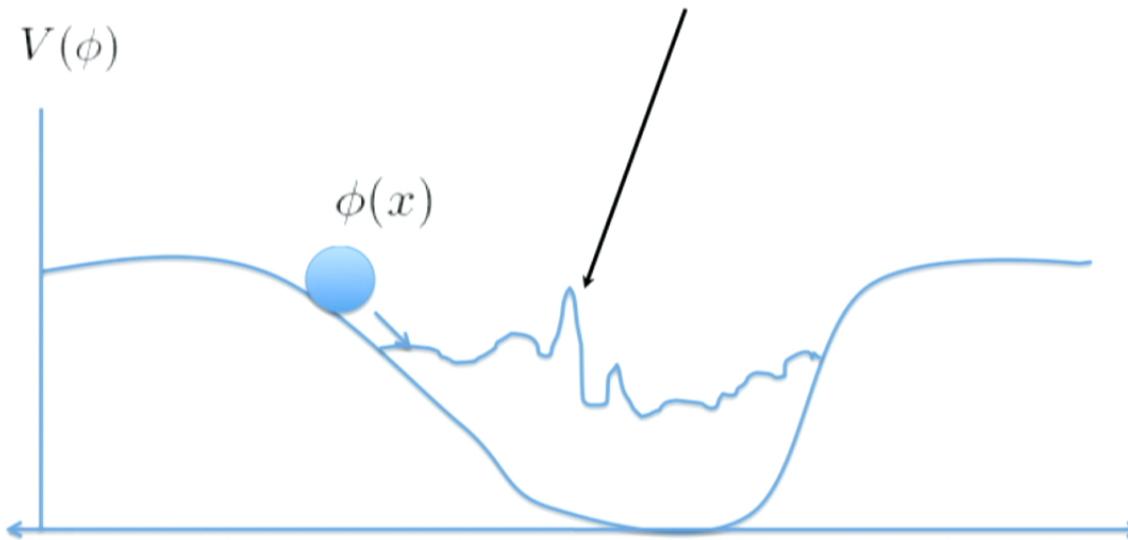


- Two phases:
  - “slow roll” down a mild slope gives inflation
  - Faster fall into lowest energy state and oscillation -> reheating
- Oscillations around minimum potential are damped by particle formation, universe gets reheated

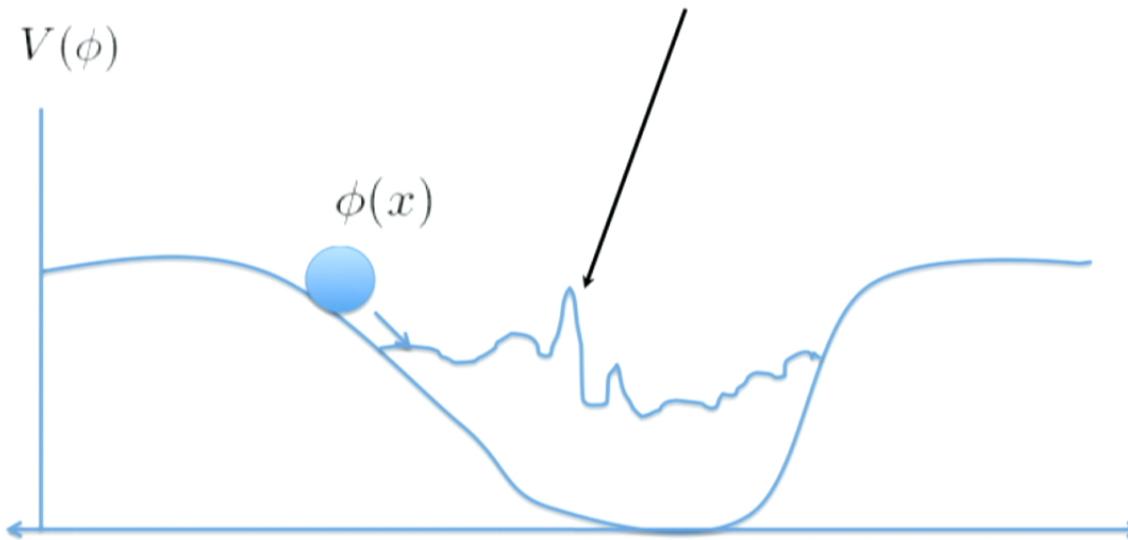
But it is hard to get a field with these properties in our standard model of particle physics



Quantum fluctuations can destroy flatness.



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- What is the identity of the inflaton field?
- Can we find new connections between inflation and the standard model of particle physics, with observable consequences?

Inflation is a great idea waiting for a  
realistic physical model.

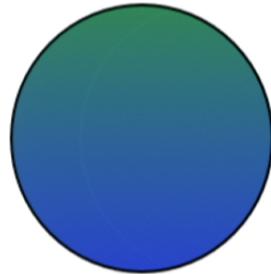
Can inflation return to its roots and connect  
to the Standard Model of Particle  
Physics?

# Vector Inflation

- In '89 Larry Ford proposed a vector field model of inflation. But it suffered from a few problems:
  - I. Vector fields spoil isotropy.
  - II. The “Slow-Roll” conditions were difficult to realize naturally.
  - III. Vector model did not seem to buy anything new.

## Scalar Inflation

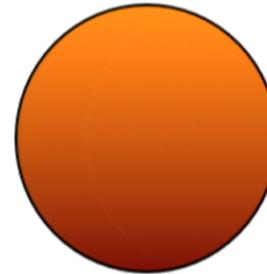
$$\Sigma_0^3$$



$$\{a_0(t_0); \phi_0; V_0; |0\rangle_{BD}\}$$

## Vector Inflation

$$\Sigma_0^3$$



$$\{a_0(t_0); A_0; \psi_0; |\Psi\rangle_{CS}\}$$

## Theoretical framework

$$\tilde{\mathcal{L}} = \text{Tr} \left[ -\frac{1}{4} g_{\alpha\gamma} g_{\beta\delta} F^{\gamma\delta} F^{\alpha\beta} + \frac{1}{4} \frac{\theta}{M_*} F_{\alpha\beta} \tilde{F}^{\alpha\beta} + q A_\mu \mathcal{J}_5^\mu \right]$$

$$S_D = \int d^4x \sqrt{-g} \left[ -i\bar{\psi} \nabla \psi + \frac{3}{M_p^2} (\bar{\psi} \gamma^I \gamma_5 \psi)^2 + q \bar{\psi} \gamma^I e_I^\mu \gamma_5 \psi A_\mu \right]$$

## PARADOX

$$T^\mu{}_\nu = \begin{pmatrix} \rho(t) & & & \\ & -p(t) & & \\ & & -p(t) & \\ & & & -p(t) \end{pmatrix}$$

Massless Yang-Mills is Classically Conformally Invariant

$$Tr[T^\mu{}_\nu] = 0 \rightarrow \text{Gauge Radiation}$$

$$\text{But for inflation } p = -\rho \rightarrow Tr[T^\mu{}_\nu] \neq 0$$

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We Need To Violate Conformal Symmetry  
To Obtain Inflation

Hint: Spontaneous Symmetry Breaking of the Vacuum  
State of Inflation

Given a general massless gauge theory  
there are three forms of anisotropies  
to overcome

$$T_{\nu}^{\mu} = \text{Tr} \left[ -\delta_{\nu}^{\mu} A_{\rho} \mathcal{J}_5^{\rho} + F_{\alpha}^{\mu} F_{\nu}^{\alpha} - \frac{1}{4} \delta_{\nu}^{\mu} g^{\alpha\rho} g^{\beta\sigma} F_{\alpha\beta} F_{\rho\sigma} - A_{\nu} \mathcal{J}_5^{\mu} \right]$$

Isotropic

Electromagnetic  
Anisotropy

Off-diagonal  
Anisotropy

# Isotropy or Not?

**Claim:** The purely isotropic part of gauge field-current interaction dominates energy momentum tensor self-consistently.

$$\mathcal{J} \equiv \text{Tr}[A_\mu \mathcal{J}_5^\mu]$$

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## ISOTROPY: EXTENDED U(1) SYMMETRY

Large anisotropies resolved by having  $N$  copies of gauge fields randomly oriented on initial time hypersurface.

$$\rightarrow T_{ij} = \sum_{A=1}^N A_{(i}^A \mathcal{J}_{j)}^A \simeq \frac{N}{3} A \cdot \mathcal{J} \delta_j^i + O(1) \sqrt{N} A \cdot \mathcal{J}$$

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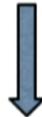
## Gauge Field Amplification

$$\eta^{\gamma\beta} \partial^\alpha F_{\alpha\beta} + \varepsilon^{\gamma\alpha\mu\nu} F_{\mu\nu} \partial_\alpha \theta / (4M_*) + a^4 \mathcal{J}^\gamma = 0$$

$$\ddot{A}_h + k^2 A_h = -h k A_h \dot{\theta} / M_* + a^4 \mathcal{J}_h$$

 Chern-Simons Source

Fermion Current



$$\sqrt{2} \mathcal{J}_h = \mathcal{J}_1 + hi\mathcal{J}_2 = (\bar{\psi} (\gamma_1 + hi\gamma_2) \gamma_5 \psi) / a$$

# Einstein Equations

$$g_{\mu\nu} = a^2(\eta) \text{diag}[-1, 1, 1, 1] + \delta a^2(\eta) g_{\mu\nu}^{(1)}$$

$$3 \frac{\dot{a}^2}{a^4} = \frac{8\pi G}{a^4} (E_+ E_- + B_+ B_-) + 8\pi G (A_+ \mathcal{J}_- + A_- \mathcal{J}_+).$$

Key Insight:  $A, J \sim \text{Constant}$

$$A \sim a(\eta) A_0 \quad J \sim \frac{J_0}{a(\eta)}$$

Inflation  $\Rightarrow a(\eta)/a_0 = (1 - H\eta)^{-1} = \exp Ht.$

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## Solutions for the vector fields

$$A(\eta, k)_- = A_-^0 \cosh(\beta_k \eta) + \tilde{A}_-^0 \sinh(\beta_k \eta) + \Xi[H, \beta, \tilde{J}_-, \eta]$$

$$\text{with } \Xi[H, \beta, \tilde{J}_-, \eta] = \frac{\tilde{J}_-}{2H^2(1-H\eta)} + \frac{\beta \tilde{J}_-}{4H^3} \Psi(x) \Big|_{x=-\frac{\beta}{H}(1-H\eta)}^{x=\frac{\beta}{H}(1-H\eta)}$$

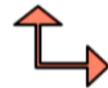
$$\Psi(x) = e^x \int_{\infty}^x \frac{e^{-t}}{t} dt$$

the leading contribution grows as the conformal factor  $\Xi \simeq \tilde{J}_0^+ / [2H^2(1-H\eta)]$

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## dS inflationary phase

Consistency  
Condition

$$M_p^2 H^2 \simeq 2 \frac{\tilde{J}_- \tilde{J}_+}{H^2}$$

Initial conditions:  $A_-^0 \simeq A_+^0 < 10^{-5} M_p$        $\mathcal{J}_+(\eta_0) \simeq \mathcal{J}_-(\eta_0) \simeq 10^{-30} M_p^3$

# Sakharov Conditions and Inflation

(S.A, Peskin, Sheikh-Jabbari PRL 05, Lyth et. al JCAP 06)

- Baryon Violation: Global Chiral Anomaly
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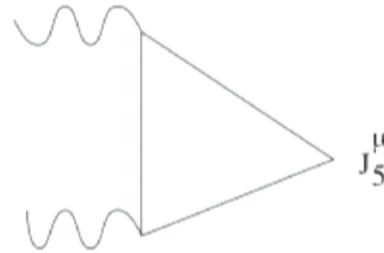
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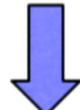
# Baryon Asymmetry

- Recall the Anomaly

Diagram:



$$\partial_\mu J^\mu = F_{\alpha\beta} F_{\mu\nu} \epsilon^{\alpha\beta\mu\nu} / (32\pi^2) \sim \vec{E} \cdot \vec{B}$$



Fermion number

Chern-Simons

$$n = \int_0^{H^{-1}} d\eta k (\dot{A}_+ A_+ - \dot{A}_- A_-) \longrightarrow \text{Condition for Inflation!}$$

- Gauge Field gets converted into Fermions through the triangle anomaly.

$$n/s \sim 10^{-10}$$


Observations  
(WMAP and BBN)

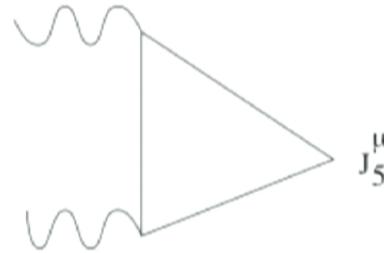
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# End of inflation

$$S = S_D + \int_{\mathcal{M}_4} d^4x \sqrt{-g} \left[ \frac{M_p^2 R}{8\pi} - \frac{1}{2} \partial_\mu \theta \partial^\mu \theta + m^2 \theta^2 - \frac{1}{4} \text{Tr}[F_{\alpha\beta} F^{\alpha\beta}] + \frac{\theta}{4M_*} \text{Tr}[F_{\alpha\beta} \tilde{F}^{\alpha\beta}] + q \text{Tr}[A_\mu \mathcal{J}_5^\mu] \right]$$

The slow-roll condition is violated when the scalar reaches the minimum of the potential

$$\epsilon = \frac{M_p^2}{2} \left( \frac{V'(\theta)}{V(\theta)} \right)^2 \geq 1$$

$$\ddot{A}(\eta, k)_h + k^2 A(\eta, k)_h = -h k A(\eta, k)_h \dot{\theta} / M_* + a^3 J_h$$

$$\theta = \frac{M_p}{3\pi m t} \sin(mt)$$

[Lev Kofman, Andrei D. Linde, Alexei A. Starobinsky PRL 1994](#)

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$$\ddot{A}(\eta, k)_h + k^2 A(\eta, k)_h + \Phi_0 \sin(mt) A(\eta, k)_h + a^3 J_h = 0$$

CP asymmetric parametric resonance for A in

$$\Phi_0 = \frac{k M_p}{3\pi M_* t}$$

ABJ anomaly and decay of gauge fields into fermions

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## Fermion Dynamics

$$(i\cancel{D} - e\cancel{A}) \Psi(\vec{x}, \eta) = 0$$

Densitize  $\Psi = \sqrt[4]{-g} \psi, \quad \bar{\Psi} = \sqrt[4]{-g} \bar{\psi}$

$$\psi(\vec{x}, \eta) = \frac{\Psi(\vec{x}, \eta)}{a^2(\eta)} = \sum_{r \vec{p}} \frac{1}{\sqrt{2V\omega_{\vec{p}}}} \left[ \frac{c_r(\vec{p})}{a^2(\eta)} u_r(\vec{p}) e^{-ip \cdot x} + \frac{d_r^*(\vec{p})}{a^2(\eta)} v_r(\vec{p}) e^{ip \cdot x} \right],$$

$$J \sim \frac{1}{a^4}$$

## Functional Schrodinger Equation

(Jackiw, Ratra, Kiefer)

$$H(\eta) |\Xi\rangle = -i \frac{\partial}{\partial \eta} |\Xi\rangle$$

$$\begin{aligned} H(\eta) &= \int d^3x \sqrt{{}^{(3)}g} \mathcal{H}(\vec{x}, \eta) = \\ &= a^3(\eta) \sum_{r\vec{p}} \omega_{\vec{p}} [c_r^\dagger(\vec{p}) c_r(\vec{p}) + d_r^\dagger(\vec{p}) d_r(\vec{p})] \end{aligned}$$

Excited Bunch-Davies Vacuum

$$\longrightarrow |\Xi\rangle = \prod_{\vec{p}} e^{-\frac{1}{2}[\xi_{r\vec{p}} \xi_{r\vec{p}}^* + \eta_{r\vec{p}} \eta_{r\vec{p}}^*]} |\xi_{\vec{p}}, \eta_{\vec{p}}\rangle$$

$$|\xi_{\vec{p}}, \eta_{\vec{p}}\rangle = e^{c_r^\dagger(\vec{p}) \xi_{r\vec{p}} + d_r^\dagger(\vec{p}) \eta_{r\vec{p}}} |0\rangle_{BD}$$

$${}_{BD} \langle \xi_{\vec{p}}^*, \eta_{\vec{p}}^* | = \langle 0 | e^{c_r(\vec{p}) \xi_{r\vec{p}}^* + d_r(\vec{p}) \eta_{r\vec{p}}^*}$$

Coupling of fermions  
to geometry requires  
state's phase to  
depend on scale factor

$$\xi_{r \vec{p}}(\eta) = i \xi_r^{(0)} a^2(\eta) \frac{a_0 \omega_{\vec{p}}}{2H}$$

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$$|\Xi_a\rangle = \prod_{\vec{p}} |\xi_{\vec{p}} a^2\rangle$$

Coherent  
Bunch-Davies vacuum state



$$\langle \Xi | \mathcal{J}^\mu | \Xi \rangle \simeq \frac{J^\mu}{a}$$

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# Outlooks and conclusions

1) Can Dark Matter be addressed in this model?

$$SU(2) \times U(1)_Y \times U(1)'^n$$

$$\mathcal{L}_{NC}^{SM} = g \mathcal{J}^{\mu}_{em} A_{\mu} + g_1 \mathcal{J}^{\mu}_1 Z_{1\mu}^0$$

$$\mathcal{L}_{NC} = g \mathcal{J}^{\mu}_{em} A_{\mu} + \sum_{\alpha=1}^{n+1} g_{\alpha} \mathcal{J}^{\mu}_{\alpha} Z_{\alpha\mu}^0$$

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(Work in progress with J. Magueijo, A. Marciano, J. Noeller)

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