

Title: Beyond the Standard Model (Review) - Lecture 13

Date: Mar 01, 2012 09:00 AM

URL: <http://pirsa.org/12030065>

Abstract:



Warped extra-dimensions

ex. Randall-Sundrum model

AdS_{5d}

Warped extra-dimensions

ex. Randall-Sundrum model

AdS_{5d}

AdS metric

$$ds^2 = e^{-2ky} \cdot dx_{4D}^2 + dy^2$$

Warped extra-dimensions

ex. Randall-Sundrum model AdS_{5d}

AdS metric

change coord

$$ds^2 = e^{-2ky} \cdot dx_{4D}^2 + dy^2 = \frac{1}{(kz)^2} \left(dx_{4D}^2 + dz^2 \right)$$
$$z = \frac{e^{ky}}{k}$$

dx_{5D}^2

Warped extra-dimensions

ex. Randall-Sundrum model

AdS_{5d}

AdS metric

change coord

$$ds^2 = e^{-2ky} \cdot dx_{4D}^2 + dy^2 = \frac{1}{(kz)^2} \underbrace{(dx_{4D}^2 + dz^2)}_{dx_{5D}^2}$$

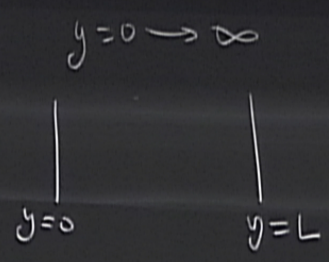
conformally flat

AdS₅ metric
change coord

$$ds^2 = e^{-ky} \cdot dx_{4D}^2 + dy^2 = \frac{1}{(kz)^2} (dx_{4D}^2 + dz^2)$$

\nearrow
 dx_{5D}^2

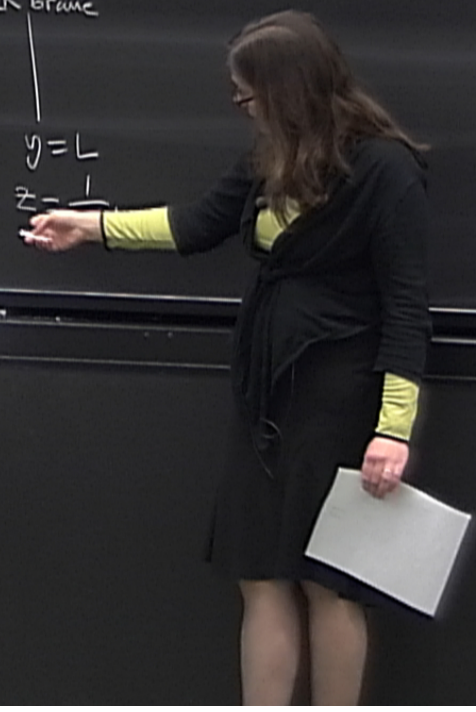
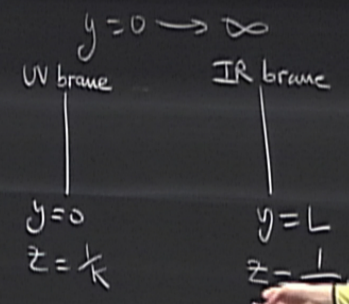
RS slice of AdS₅



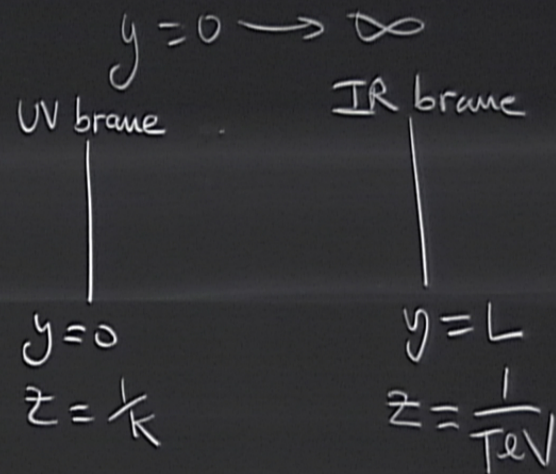
AdS₅ metric
change coord

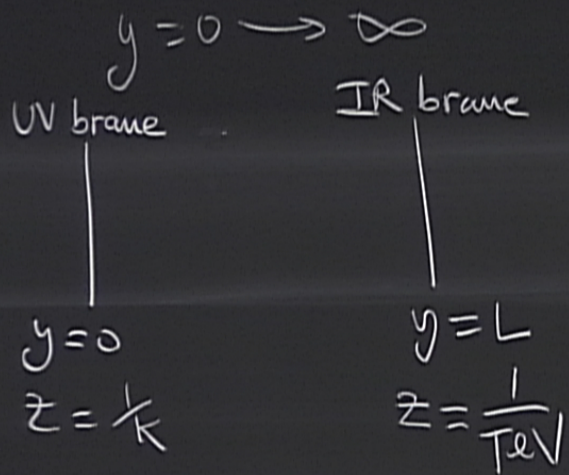
$$ds^2 = e^{-ky} \cdot dx_{4D}^2 + dy^2 = \frac{1}{(Kz)^2} (dx_{4D}^2 + dz^2)$$
$$z = \frac{e^{ky}}{K}$$

RS slice of AdS₅



RS slice of AdS_5





AdS₅

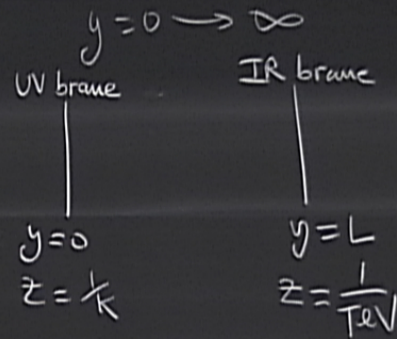
$$M_{\text{pl}}^{\text{SD}} \sim M_{\text{pl}}^{\text{4D}} \sim K \sim \frac{1}{L}$$

change coord $z = \frac{e^{Ky}}{K}$

$$[(Kz)^2] \quad dx_{SD}^2$$

RS slice of AdS_5

$$LED \quad V_{eff}^n M_{SD}^{n+2} \sim M_{4D}^2$$



AdS_5

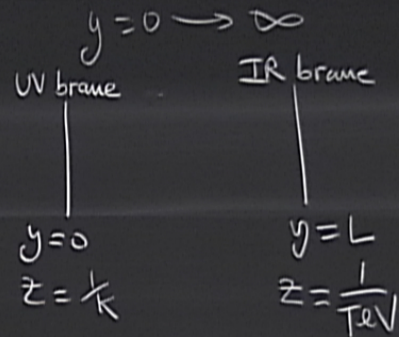
$$M_{Pl}^{SD} \sim M_{Pl}^{4D} \sim K \sim \frac{1}{L}$$

change coord $z = \frac{e^{Ky}}{K}$

$(Kz)^2$
 dx_{5D}^2

RS slice of AdS_5

LED $V_{eff}^n M_{pl}^{n+2} \sim M_{4D}^2$

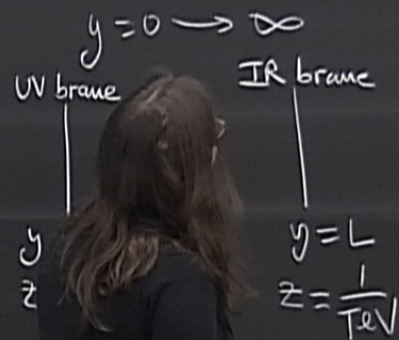


AdS_5

$M_{pl}^{5D} \sim M_{pl}^{4D} \sim K \sim \frac{1}{L}$

RS slice of AdS_5

$$LED \quad V_{vol}^n M_{D}^{n+2} \sim M_{4D}^2$$



AdS_5

$$M_{Pl}^{5D} \sim M_{Pl}^{4D} \sim K \sim \frac{1}{L}$$

solution hierarchy problem
→ Physics is redshifted

$$z = \frac{1}{k}$$

$$z = \frac{1}{TeV}$$

→ Physics is redshifted

Why? local value of energy

$$z = 0$$
$$z = \frac{1}{k}$$

$$z = \frac{1}{TeV}$$

→ Physics is redshifted

Why? local value of energy $g_{00}(y)$

Example: Cosmological redshift


$$z = \frac{1}{k}$$

$$z = \frac{1}{TeV}$$

→ Physics is redshifted

Why? local value of energy $g_{00}(y)$

Example: Cosmological redshift

λ_e, p_e


$$\text{LED Val } M_{\text{D}}^{\text{HD}} \sim M_{\text{4D}}^2$$

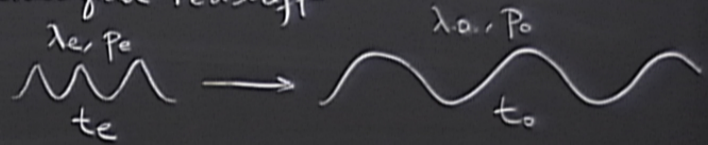
$$y=0 \\ z = \frac{1}{k}$$

$$y=L \\ z = \frac{1}{TeV}$$

Solution hierarchy problem
→ Physics is redshifted

Why? local value of energy $g_{00}(y)$

Example: Cosmological redshift



$$\text{LED Val } M_D^{\text{me}} \sim M_{\text{4D}}^2$$

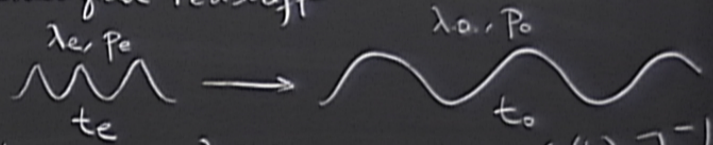
$$y=0 \\ z = \frac{1}{k}$$

$$y=L \\ z = \frac{1}{TeV}$$

Solution hierarchy problem
 \rightarrow Physics is redshifted

Why? local value of energy $g_{00}(y)$

Example: Cosmological redshift



$$\text{FRW } g_{00} = a^2(ct) \rightarrow p_e = p_o \left[\frac{a(t_o)}{a(t_e)} \right]^{-1}$$

$$\text{LED Val } M_D^{\text{int}} \sim M_{4D}^2$$

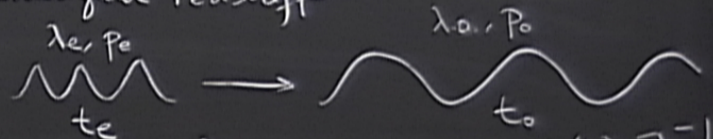
$$y=0 \\ z = \frac{1}{k}$$

$$y=L \\ z = \frac{1}{TeV}$$

Solution hierarchy problem
 \rightarrow Physics is redshifted

Why? local value of energy $g_{00}(y)$
 in RS

Example: Cosmological redshift



$$\text{FRW } g_{00} = a^2(ct) \rightarrow p_e = p_o \left[\frac{a(t_o)}{a(t_e)} \right]^{-1}$$

$$p_e \sqrt{g_{00}^e} = p_o \sqrt{g_{00}^o}$$

LED Val $M_{D}^{11D} \sim M_{4D}^2$

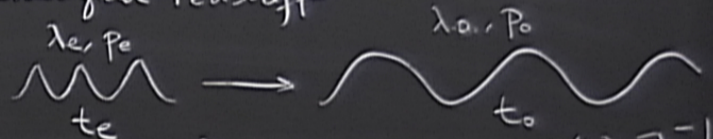
$y=0$
 $z = \frac{1}{k}$

$y=L$
 $z = \frac{1}{TeV}$

Solution hierarchy problem
→ Physics is redshifted

Why? local value of energy $g_{00}(y)$
in RS local measurement of E, \vec{p}
 $g_{00} = e^{-2Ky}$

Example: Cosmological redshift



FRW $g_{00} = a^2(ct) \rightarrow p_e = p_o \left[\frac{a(t_o)}{a(t_e)} \right]^{-1}$
 $p_e \sqrt{g_{00}^e} = p_o \sqrt{g_{00}^o}$

LED Val $M_{D1}^{10} \sim M_{4D}^2$

$y=0$
 $z = \frac{1}{k}$

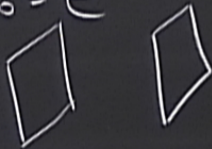
$y=L$
 $z = \frac{1}{TeV}$

Solution hierarchy problem
→ Physics is redshifted

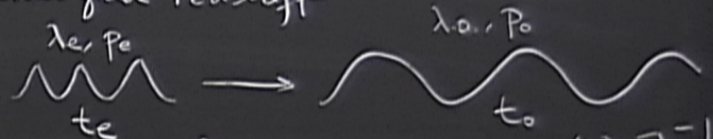
Why? local value of energy $g_{00}(y)$

in RS local measurement of E, \vec{p}

RS redshift $g_{00} = e^{-2Ky}$



Example: Cosmological redshift



FRW

$$g_{00} = a^2(ct) \rightarrow p_e = p_o \left[\frac{a(t_o)}{a(t_e)} \right]^{-1}$$

$$p_e \sqrt{g_{00}^e} = p_o \sqrt{g_{00}^o}$$

LED Val $M_D^{1/2} \sim M_{4D}^2$

$y=0$
 $z = \frac{1}{k}$

$y=L$
 $z = \frac{1}{TeV}$

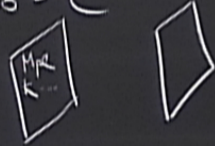
Solution hierarchy problem
→ Physics is redshifted

Why? local value of energy $g_{00}(y)$

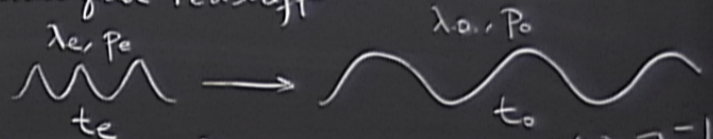
in RS local measurement of E, \vec{p}

RS redshift

$g_{00} = e^{-2ky}$



Example: Cosmological redshift



FRW

$g_{00} = a^2(ct)$
 $p_e \sqrt{g_{00}^e} = p_o \sqrt{g_{00}^o}$

$p_e = p_o \left[\frac{a(t_o)}{a(t_e)} \right]^{-1}$

LED Val $M_D^{1/2} \sim M_{4D}^2$

$y=0$
 $z = \frac{1}{k}$

$y=L$
 $z = \frac{1}{T e V}$

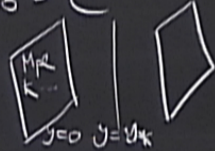
Solution hierarchy problem
→ Physics is redshifted

Why? local value of energy $g_{00}(y)$

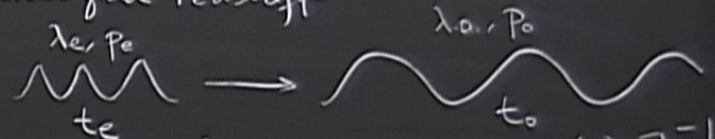
in RS local measurement of E, \vec{p}

RS redshift

$$g_{00} = e^{-2Ky}$$



Example: Cosmological redshift



FRW

$$g_{00} = a^2(ct) \rightarrow p_e = p_o \left[\frac{a(t_o)}{a(t_e)} \right]^{-1}$$

$$p_e \sqrt{g_{00}^e} = p_o \sqrt{g_{00}^o}$$

LED Val $M_{D}^{1/2} \sim M_{4D}^2$

$y=0$
 $z = \frac{1}{k}$

$y=L$
 $z = \frac{1}{TeV}$

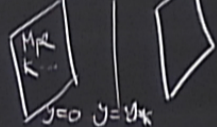
Solution hierarchy problem
→ Physics is redshifted

Why? local value of energy $g_{00}(y)$

in RS local measurement of E, \vec{p}

RS redshift

$g_{00} = e^{-2Ky}$

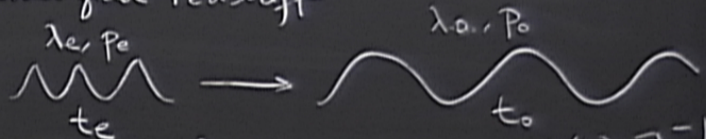


M_{pl} cutoff
→ local cutoff

$\left\{ \begin{array}{l} \frac{M_{pl}}{e^{-Ky=0}} = \frac{\Lambda(y)}{e^{-Ky}} \\ \leftarrow \end{array} \right.$

FRW

Example: Cosmological redshift



$g_{00} = a^2(ct)$
 $p_e \sqrt{g_{00}^e} = p_o \sqrt{g_{00}^o}$

$p_e = p_o \left[\frac{a(t_o)}{a(t_e)} \right]^{-1}$

LED Val $M_D^{16} \sim M_{4D}^2$

$y=0$
 $z = \frac{1}{k}$

$y=L$
 $z = \frac{1}{TeV}$

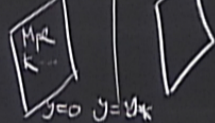
Solution hierarchy problem
→ Physics is redshifted

Why? local value of energy $g_{00}(y)$

in RS local measurement of E, \vec{p}

RS redshift

$g_{00} = e^{-2ky}$

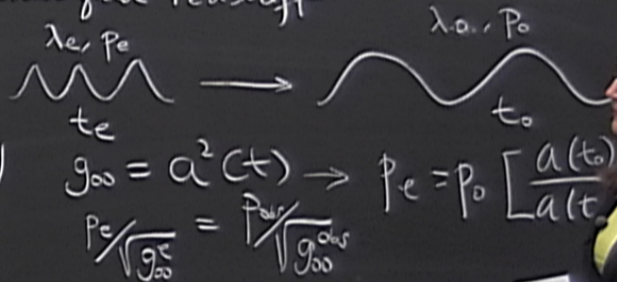


M_{pl} cutoff
→ local cutoff

$\Lambda(y) = e^{-ky} M_{pl}$
 $\frac{M_{pl}}{e^{-ky=0}} = \frac{\Lambda(y)}{e^{-ky}}$

FRW

Example: Cosmological redshift



LED Val $M_{D}^{10} \sim M_{4D}^2$

$y=0$
 $z = \frac{1}{k}$

$y=L$
 $z = \frac{1}{TeV}$

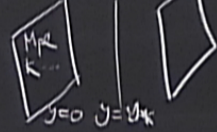
Solution hierarchy problem
→ Physics is redshifted

Why? local value of energy $g_{00}(y)$

in RS local measurement of E, \vec{p}

RS redshift

$g_{00} = e^{-2ky}$



M_{pl} cutoff
→ local cutoff

$\Lambda(y) = e^{-ky} M_{pl}$
 $\frac{M_{pl}}{e^{-ky=0}} = \frac{\Lambda(y)}{e^{-ky}}$

LED Val $M_D^{1/2} \sim M_{4D}^2$

$y=0$
 $z = \frac{1}{k}$

$y=L$
 $z = \frac{1}{TeV}$

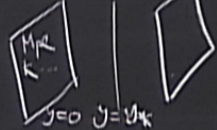
Solution hierarchy problem
→ Physics is redshifted

Why? local value of energy $g_{00}(y)$

in RS local measurement of E, \vec{p}

RS redshift

$g_{00} = e^{-2ky}$



M_{pl} cutoff
→ local cutoff

$\Lambda(y) = e^{-ky} M_{pl}$

$\frac{M_{pl}}{e^{-ky=0}} = \frac{\Lambda(y)}{e^{-ky}}$

Example: Goldberger-Wise mechanism

LED Val $M_{D}^{1/2} \sim M_{4D}^2$

$y=0$
 $z = \frac{1}{k}$

$y=L$
 $z = \frac{1}{TeV}$

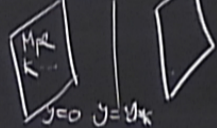
Solution hierarchy problem
→ Physics is redshifted

Why? local value of energy $g_{00}(y)$

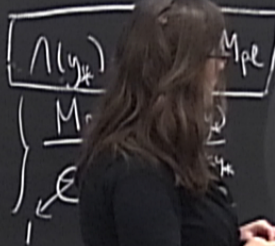
in RS local measurement of E, p

RS redshift

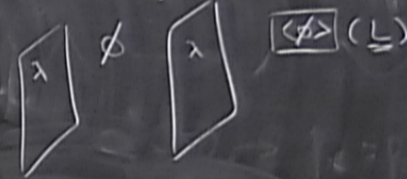
$g_{00} = e^{-2Ky}$



M_{pl} cutoff
→ local cutoff



Goldberger-Wise mechanism



LED Val $M_{D1}^{1/2} \sim M_{4D}^2$

$y=0$
 $z = \frac{1}{k}$

$y=L$
 $z = \frac{1}{TeV}$

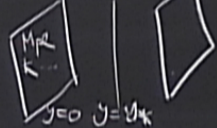
Solution hierarchy problem
→ Physics is redshifted

Why? local value of energy $g_{00}(y)$

in RS local measurement of E, p

RS redshift

$g_{00} = e^{-2ky}$

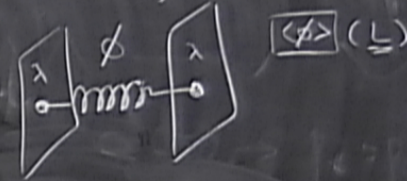


M_{pl} cutoff
→ local cutoff

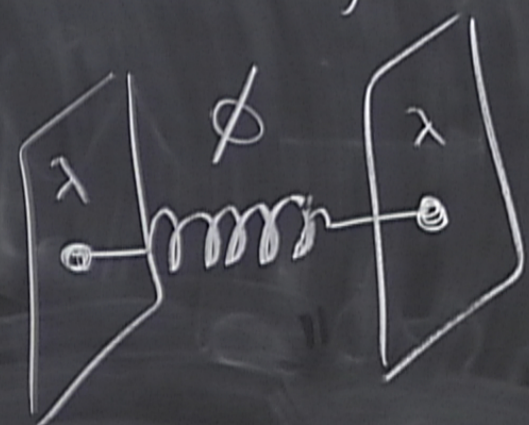
$e^{-ky} M_{pl}$

$\frac{\Lambda(y)}{e^{-ky}}$

Goldberger-Wise mechanism



Goldberger-Krise mechanism



$$\langle \phi \rangle (\underline{L}) \quad KL \sim \mathcal{O}(1)$$
$$V(\phi)^\dagger$$



If we want $\Lambda(y_{\text{TeV}}) \sim \text{TeV}$

y_{TeV}

$$\Lambda(y_*) = e^{-ky_*} M_{\text{pl}}$$
$$\left\{ \begin{array}{l} M_{\text{pl}} \\ e^{-ky=0} \end{array} \right. = \frac{\Lambda(y_*)}{e^{-ky_*}}$$

If we want $\Lambda(y_{\text{TeV}}) \sim \text{TeV}$

$$y_{\text{TeV}} \sim \frac{1}{K} \sim \frac{1}{M_{\text{Pl}}^{\text{SD}}} \sim \frac{1}{M_{\text{Pl}}^{\text{UD}}}$$

$$\Lambda(y_*) = e^{-ky_*} M_{\text{Pl}}$$

$$\left. \begin{aligned} \frac{M_{\text{Pl}}}{e^{-ky=0}} &= \frac{\Lambda(y_*)}{e^{-ky_*}} \end{aligned} \right\}$$

If we want $\Lambda(y_{\text{TeV}}) \sim \text{TeV}$

in Randall-Sundrum
 $y_{\text{TeV}} \sim \frac{1}{k} \sim \frac{1}{M_{\text{Pl}}^{5D}} \sim \frac{1}{M_{\text{Pl}}^{4D}}$

Higgs (ew) physics is stable
it is confined near y_{TeV}

$$\Lambda(y_*) = e^{-ky_*} M_{\text{Pl}}$$
$$\left\{ \begin{array}{l} \frac{M_{\text{Pl}}}{e^{-ky=0}} = \frac{\Lambda(y_*)}{e^{-ky_*}} \end{array} \right.$$

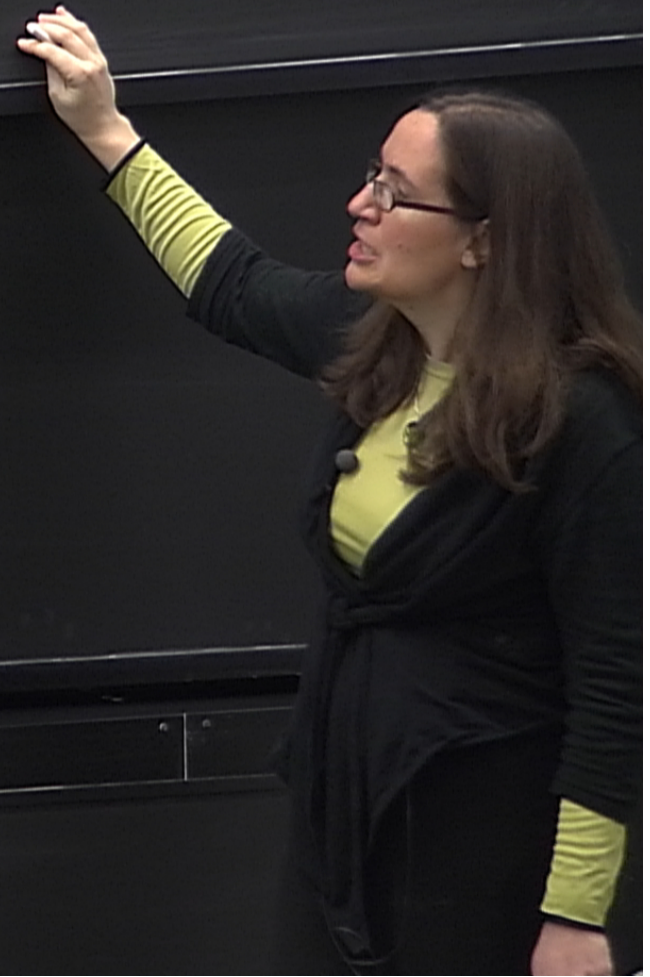
How do we localize fields in RS?

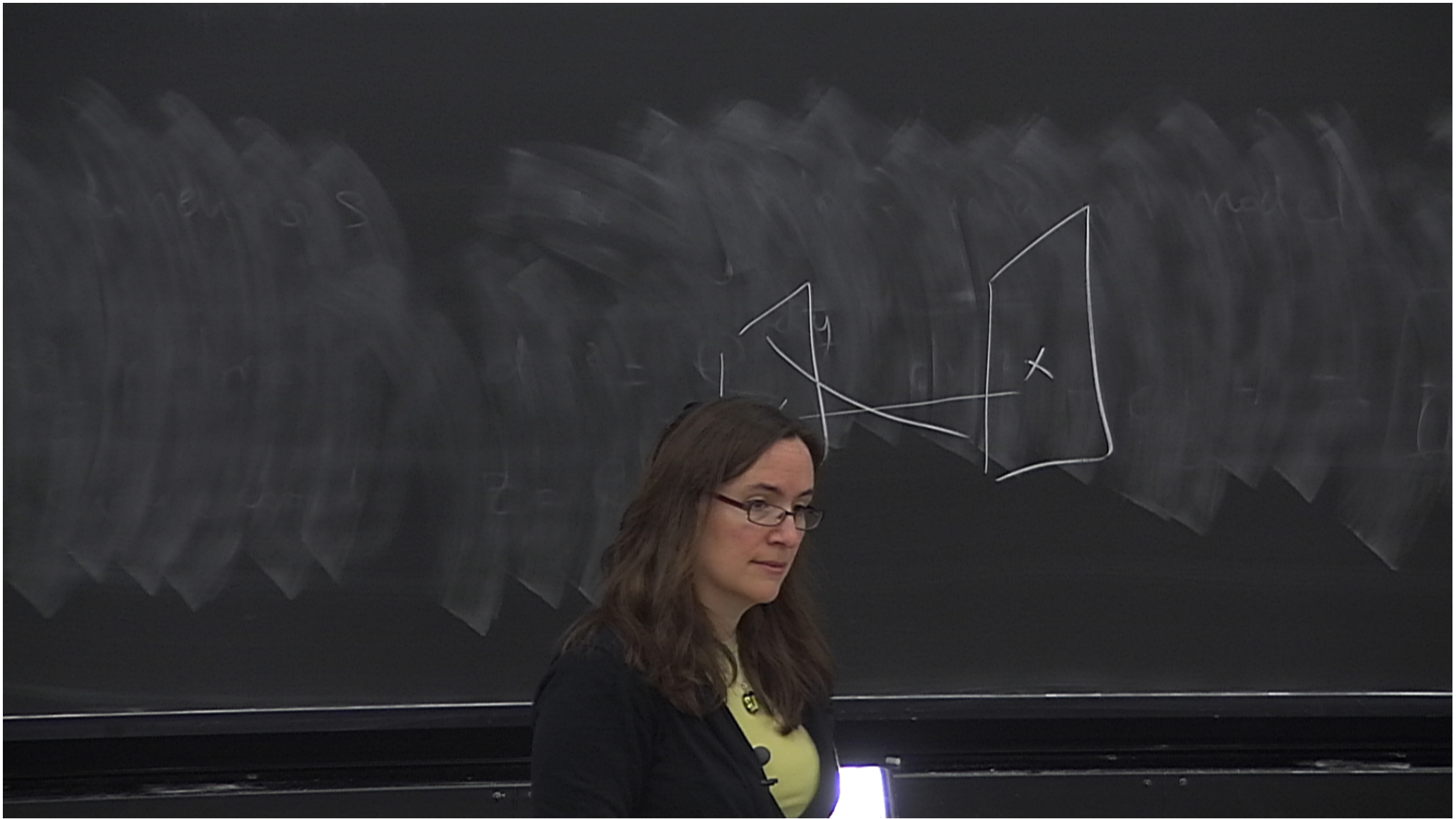
① stuck them on a brane

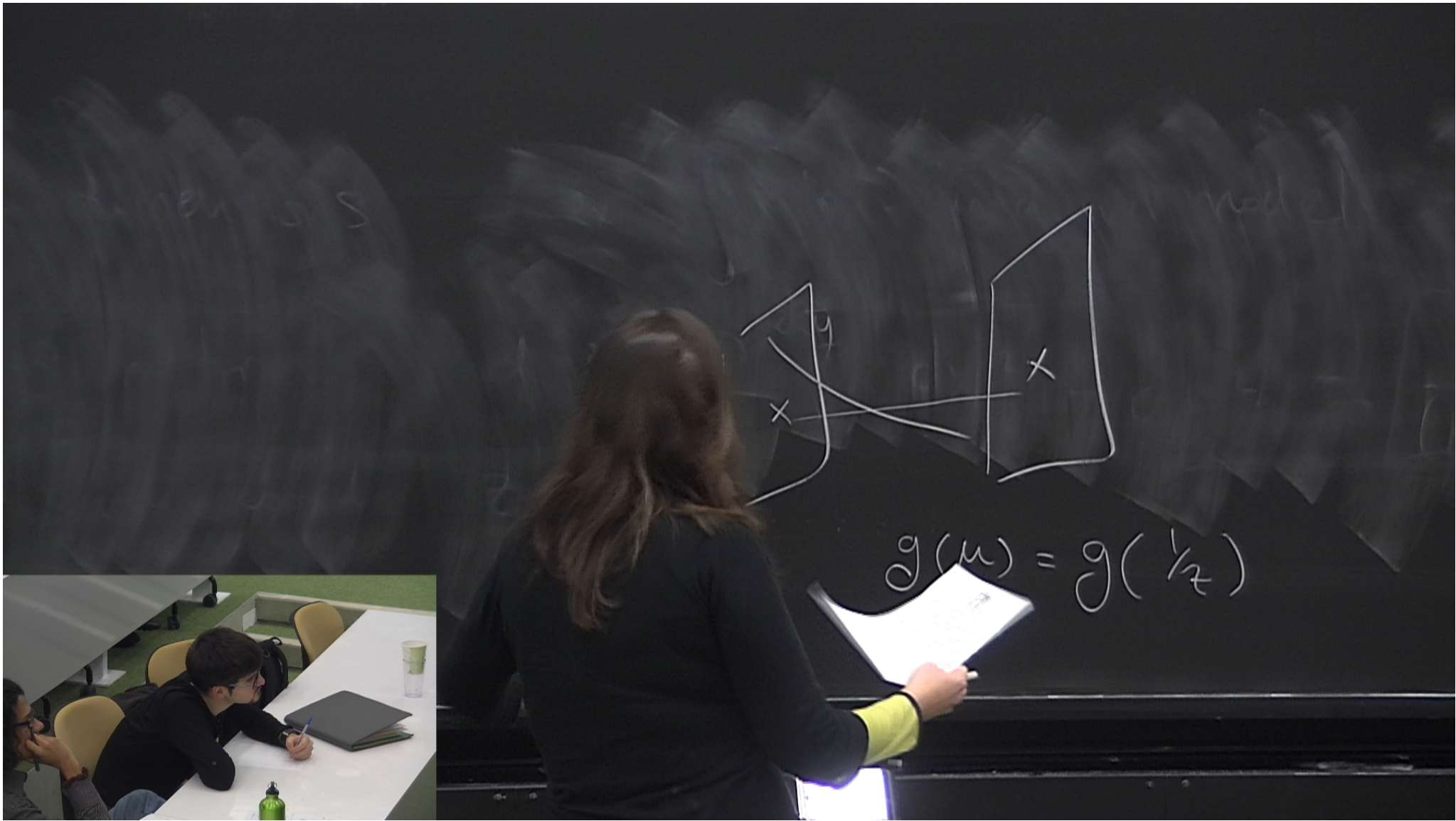
How do we localize fields in RS?

- ① stick them on a brane
- ② use their wavefunction (profile) in the extra dimensions

$$\Lambda_{SD} \sim T_{UV} \sim -T_{IR}$$







Scalar case

$$\Phi(x, y) = \sum_{i=1}^n \phi_i(x, y)$$

Scalar case

$$\Phi(x, y) = \sum_{n=0}^{\infty} \phi_n(x) f_n(y)$$

Scalar case

$$\Phi(x, y) = \sum_{n=0}^{\infty} \phi_n(x) f_n(y)$$

\square_{SD}

$\partial\partial$

EOM $f_n(y)$

$$-\partial_y (e^{-4ky} \partial_y f_n) + M^2 e^{-4ky} f_n = m_n^2 f_n$$

$$\text{LED } V_0 M_{\text{pl}}^{n+2} \sim M_{\text{4D}}^2$$

$$y=0 \\ z = \frac{1}{K}$$

$$y=L \\ z = \frac{1}{T_2 V}$$

$$M_{\text{pl}}^{\text{SD}} \sim M_{\text{pl}}^{\text{4D}} \sim K \sim \frac{1}{L}$$

Solution hierarchy problem
→ Physics is redshifted

Scalar case

$$\Phi(x, y) = \sum_{n=0}^{\infty} \phi_n(x) f_n(y)$$

\square_{SD}

$\partial\partial$

M scalar mass term in bulk
 $\mathcal{L}_{\text{SD}} \supset M^2 \phi^2$

EOM

$$-\partial_y (e^{-4ky} \partial_y f_n) + M^2 e^{-4ky} f_n = m_n^2 e^{-2ky} f_n$$

$$\text{LED } V_{\text{eff}} \sim M_{\text{pl}}^{n+2} \sim M_{\text{4D}}^2$$

$$y=0 \\ z = \frac{1}{K}$$

$$y=L \\ z = \frac{1}{TeV}$$

$$M_{\text{pl}}^{\text{SD}} \sim M_{\text{pl}}^{\text{4D}} \sim K \sim \frac{1}{L}$$

Solution hierarchy problem
→ Physics is redshifted

Scalar case

$$\Phi(x, y) = \sum_{n=0}^{\infty} \phi_n(x) f_n(y)$$

\square_{SD}

M scalar mass term in bulk
 $\mathcal{L}_{\text{SD}} \supset M^2 \phi^2$

EOM $f_n(y)$

$$-\partial_y (e^{-4ky} \partial_y f_n) + \underbrace{M^2}_{\square_{\text{SD}}} e^{-4ky} f_n = m_n^2 e^{-2ky} f_n$$

natural value M

$$\text{LED } V_{eff} \sim M_{pl}^{n+2} \sim M_{4D}^2$$

$$y=0 \\ z = \frac{1}{K}$$

$$y=L \\ z = \frac{1}{TeV}$$

$$M_{pl}^{SD} \sim M_{pl}^{4D} \sim K \sim \frac{1}{L}$$

Solution hierarchy problem
→ Physics is redshifted

Scalar case

$$\Phi(x,y) = \sum_{n=0}^{\infty} \phi_n(x) f_n(y)$$

$$\square_{SD}$$

$$\partial\partial$$

M scalar mass term in bulk
 $\mathcal{L}_{SD} \supset M^2 \phi^2$

EOM $f_n(y)$

$$-\partial_y (e^{-4ky} \partial_y f_n) + M^2 e^{-4ky} f_n = m_n^2 e^{-2ky} f_n$$

natural value M

$$M \sim M_{pl}$$

$$LED \quad V_6^n M_{D7}^{n+2} \sim M_{4D}^2$$

$$y=0 \\ z = \frac{1}{K}$$

$$y=L \\ z = \frac{1}{TeV}$$

$$M_{Pl}^{SD} \sim M_{Pl}^{4D} \sim K \sim \frac{1}{L}$$

Solution hierarchy problem
→ Physics is redshifted

Scalar case

$$\Phi(x,y) = \sum_{n=0}^{\infty} \phi_n(x) f_n(y)$$

$$\square_{SD} \\ \partial\partial$$

M scalar mass term in bulk
 $\mathcal{L}_{SD} \supset M^2 \phi^2$

EOM $f_n(y)$

$$-\partial_y (e^{-4ky} \partial_y f_n) + \underbrace{M^2}_{\sim TeV} e^{-4ky} f_n = \underbrace{m_n^2}_{\sim TeV} e^{-2ky} f_n$$

natural value M
 $M \sim M_{Pl}$

$$\text{LED } V_0 M_{\text{pl}}^{n+2} \sim M_{\text{pl}}^2$$

$$M_{\text{pl}}^{\text{SD}} \sim M_{\text{pl}}^{\text{HD}} \sim K \sim \frac{1}{L}$$

Scalar case

$$\Phi(x, y) = \sum_{n=0}^{\infty} \phi_n(x) f_n(y)$$

$$\square_{\text{SD}} \partial \partial$$

M scalar mass term in bulk
 $\mathcal{L}_{\text{SD}} \supset M^2 \phi^2$

EOM $f_n(y)$

$$\underbrace{-\partial_y (e^{-4ky} \partial_y f_n)}_{M^2 e^{-4ky} f_n} = \underbrace{m_n^2}_{\sim \text{TeV}} e^{-2ky} f_n$$

natural value M
 $M \sim M_{\text{pl}}$



$$\text{LED } V_0 M_{\text{pl}}^{n+2} \sim M_{\text{4D}}^2$$

$$M_{\text{pl}}^{\text{SD}} \sim M_{\text{pl}}^{\text{4D}} \sim K \sim \frac{1}{L}$$

Scalar case

$$\Phi(x, y) = \sum_{n=0}^{\infty} \phi_n(x) f_n(y)$$

$\downarrow m_n$

$$\square_{\text{SD}} \partial \partial$$

M scalar mass term in bulk
 $\mathcal{L}_{\text{SD}} \supset M^2 \phi^2$

EOM $f_n(y)$

$$-\partial_y (e^{-4ky} \partial_y f_n) + M^2 e^{-4ky} f_n = \frac{m_n^2}{\text{TeV}} e^{-2ky} f_n$$

natural value M
 $M \sim M_{\text{pl}}$



LED Vol $M_D \sim M_{4D}$

Scalar case

$$\underline{\phi}(x, y) = \sum_{n=0}^{\infty} \phi_n(x) f_n(y) \quad \square_{5D}$$

$$\hookrightarrow m_n: \square_{4D} \phi_n^2 = -m_n^2 \phi_n^2 \partial \partial$$

M scalar mass term in bulk
 $\mathcal{L}_{5D} \supset M^2 \phi^2$

EOM $f_n(y)$

$$\underbrace{-\partial_y (e^{-4ky} \partial_y f_n)} + \underbrace{M^2 e^{-4ky} f_n} = \underbrace{m_n^2 e^{-2ky} f_n}_{\hookrightarrow \text{TeV}}$$

natural value M
 $M \sim M_{Pl}$



zero modes \rightarrow effective ^{4D} description

zero modes \rightarrow effective ^{4D} description

Case $M=0$ set $m_n = 0$
 $e^{-4ky} \partial_y f_0 = 0$

zero modes \rightarrow effective ^{4D} description.

Case $M=0$ set $m_n=0$

$$e^{-4ky} \quad \partial_y f_0 = 0$$

$$f_0 = C + C' e^{4ky}$$

zero modes \rightarrow effective ^{4D} description

Case $M=0$ set $m_n=0$

$$e^{-4ky} \quad \partial_y f_0 = 0$$

$$f_0 = C + C' e^{4ky}$$

$(++)$ $(+-)$ $(-+)$ $(--)$
UV IR

$(++)$

$$f_0 = Q$$

$(++)$ $(+-)$ $(-+)$ $(--)$
UV IR

$(++)$

$$f_0 = Q$$

imposing normalization

zero modes \rightarrow effective ^{4D} description

Case $M=0$

set $m_n = 0$

$$e^{-4ky} \partial_y f_0 = C''$$
$$f_0 = C + C' e^{4ky}$$

$(++)$ $(+-)$ $(-+)$ $(--)$
UV IR

$(++)$ $f_0 = Q$ imposing normalization
 $(+-)$ $(-+)$ $(--)$

$(++)$ $(+-)$ $(-+)$ $(--)$
UV IR

$(++)$
 $(+-)$ $(-+)$ $(--)$

$$\begin{array}{l} f_0 = Q \\ f_0 = 0 \end{array}$$

imposing normalization
project out
zero mode

$(++)$ $(+-)$ $(-+)$ $(--)$
UV IR

$(++)$
 $(+-)$ $(-+)$ $(--)$

$$\begin{array}{l} f_0 = Q \\ f_0 = 0 \end{array}$$

imposing normalization
project out
zero mode

$(++)$ $(+-)$ $(-+)$ $(--)$
UV IR

$(++)$
 $(+-)$ $(-+)$ $(--)$

$$\begin{array}{l} f_0 = C \\ f_0 = 0 \end{array}$$

→ flat, delocalized
imposing normalization
project out
zero mode

$(++)$ $(+-)$ $(-+)$ $(--)$
UV IR

$(++)$
 $(+-)$ $(-+)$ $(--)$

$$\begin{array}{l} f_0 = C \\ f_0 = 0 \end{array}$$

→ flat, delocalized
imposing normalization
project out
zero mode



$(++)$ $(+-)$ $(-+)$ $(--)$
 UV IR

$(++)$

$(+-)$ $(-+)$ $(--)$

$$f_0 = C$$

$$f_0 = 0$$

flat, delocalized
 imposing normalization

project out
 zero mode



$(++)$ $(+-)$ $(-+)$ $(--)$
UV IR

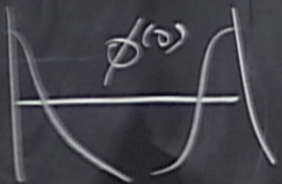
$(++)$

$(+-)$ $(-+)$ $(--)$

$$\begin{aligned} f_0 &= C \\ f_0 &= 0 \end{aligned}$$

flat, delocalized
imposing normalization

project out
zero mode



zero modes \rightarrow effective ^{4D} description.

case $M \neq 0$

$$-\partial_y (e^{-4ky} f_0') = -M^2 e^{-4ky} f_0$$

zero modes \rightarrow effective ^{4D} description.

$$e M \neq 0$$

$$-\partial_y (e^{-4ky} f_0') = -M^2 e^{-4ky} f_0$$

$$f_0 = C_1 e^{2ky(1-\alpha)} + C_2 e^{2ky(1+\alpha)}$$

zero modes \rightarrow effective ^{4D} description.

case $M \neq 0$

$$-\partial_y (e^{-4ky} f_0') = -M^2 e^{-4ky} f_0$$

$$f_0 = C_1 e^{2ky(1-\alpha)} + C_2 e^{2ky(1+\alpha)}$$

$$\alpha = \sqrt{1 + \frac{M^2}{4k^2}}$$

$$f = e^{2ky} (c_1 e^{-2kyx} + c_2 e^{+2kyx})$$

UV BCs

$$y=0$$

$$f_0 = e^{2ky} (c_1 e^{-2kyx} + c_2 e^{+2kyx})$$

UV BCs

$y=0$

$$\left\{ \begin{array}{l} (-) \quad f_0|_{y=0} = 0 \rightarrow C_1 = -C_2 \\ (+) \quad C_1 = C_2 \end{array} \right.$$

$$e^{2ky} (c_1 e^{-2ky\alpha} + c_2 e^{+2ky\alpha})$$

$$\Lambda_{SD} \sim \overline{T_{uv}} \sim -T_{IR}$$

4D Minkowski

$$IR \text{ BCs} \quad (-) \quad f_0|_{IR} = 0$$



$$\Lambda_{SD} \sim \overline{T_{UV}} \sim -T_{IR}$$

4D Minkowski

IR BCs

(-) $f_0|_{IR} = 0 \rightarrow \text{no sols} \rightarrow f_0 = 0$

(+) $f_0'|_{IR} \propto e^{2ky} \left(\alpha \frac{\cosh}{\sinh} + \frac{\sinh}{\cosh} \right)$

$$\Lambda_{SD} \sim \overline{T_{UV}} \sim -T_{IR}$$

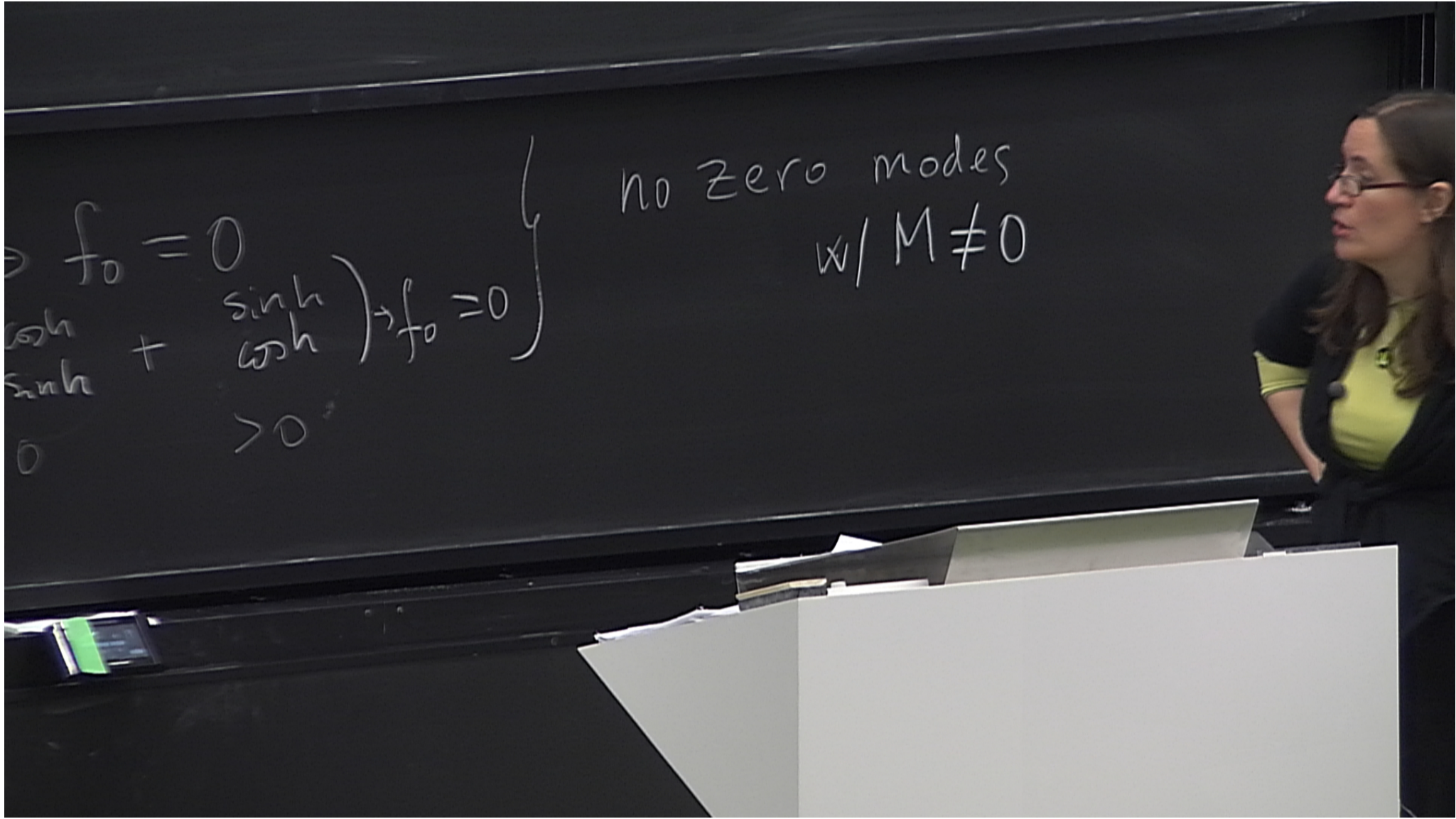
4D Minkowski

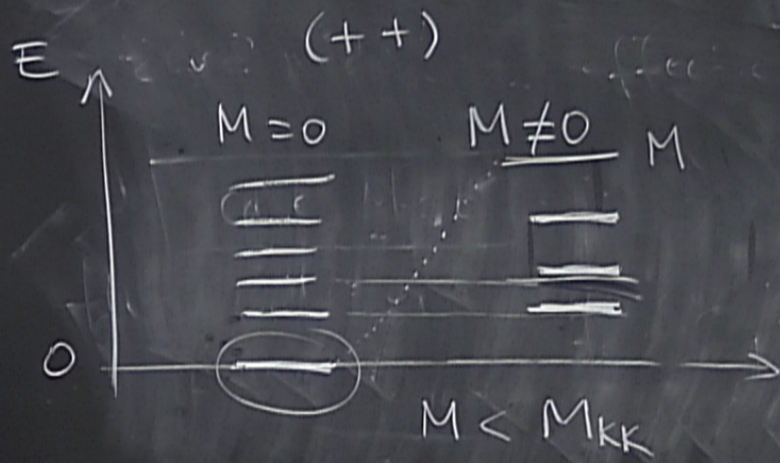
IR BCs

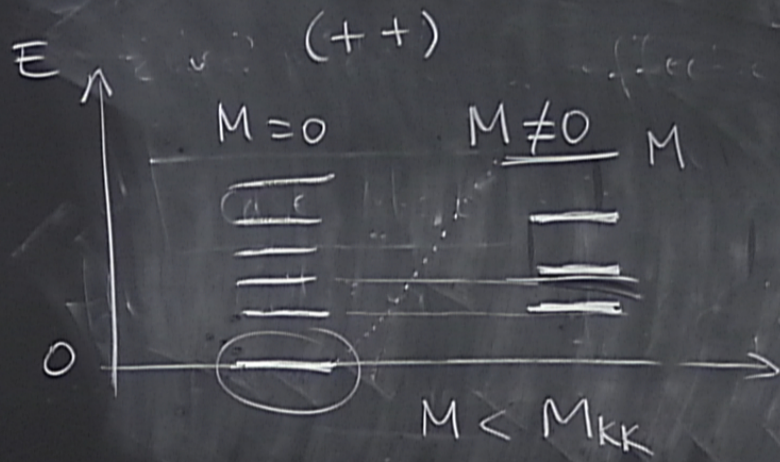
(-) $f_0|_{IR} = 0 \rightarrow \text{no sols} \rightarrow f_0 = 0$

(+) $f_0'|_{IR} \propto e^{2ky} \left(\alpha \frac{\cosh}{\sinh} + \frac{\sinh}{\cosh} \right)$

> 0 > 0







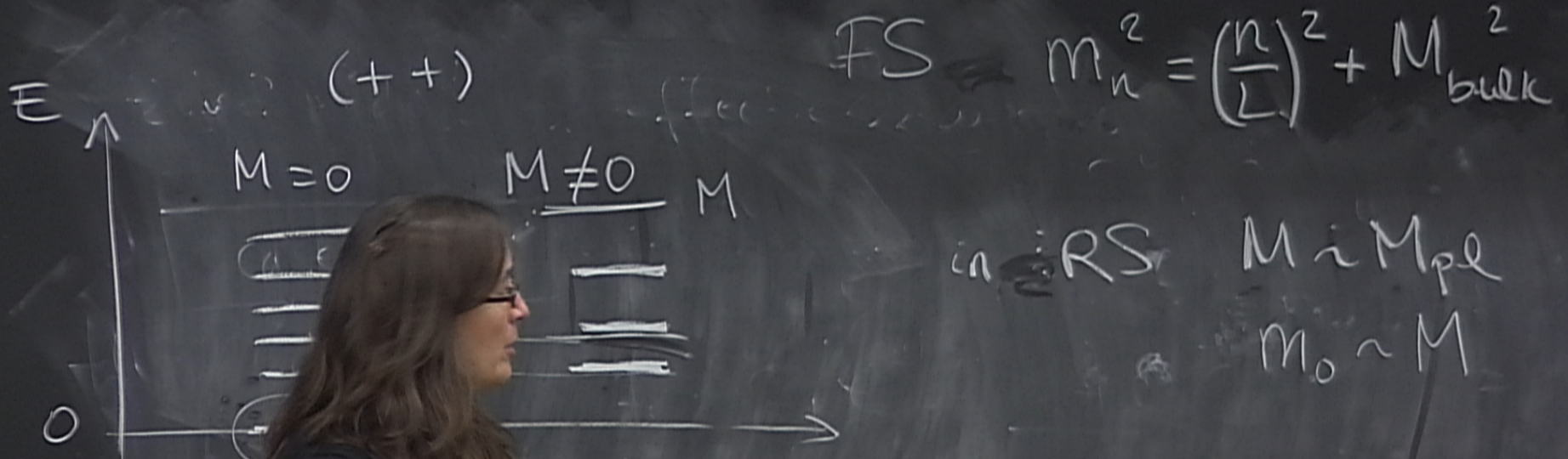
in RS $M \sim M_{pl}$
 $m_0 \sim M$

$$S_{\text{bulk}} + S_{\text{boundary}}$$

$$S_{\text{boundary}} = - \int d^4x dy \sqrt{-g} M_b^2 \phi^2 [\delta(y) - \delta(y - y_{\text{rev}})]$$

$$S_{\text{bulk}} + S_{\text{boundary}}$$

$$S_{\text{boundary}} = - \int d^4x dy \sqrt{-g} M_b^2 \phi^2 [\delta(y) - \delta(y - y_{\text{rev}})]$$



$$FS = m_n^2 = \left(\frac{n}{L}\right)^2 + M_{bulk}^2$$

in RS: $M \sim M_{pl}$
 $m_0 \sim M$

$$S_{\text{bulk}} + S_{\text{boundary}}$$

$$S_{\text{boundary}} = - \int d^d x dy \sqrt{-g} M_b^2 \phi^2 [\delta(y) - \delta(y - y_{\text{rev}})]$$

$$\partial_y f|_b = M_b f|_b$$

$$\Lambda_{SD} \sim \overline{T_{UV}} \sim -T_{IR}$$

4D Minkowski

adds new zero modes

$$f_0 \sim e^{M_b y}$$

M_b

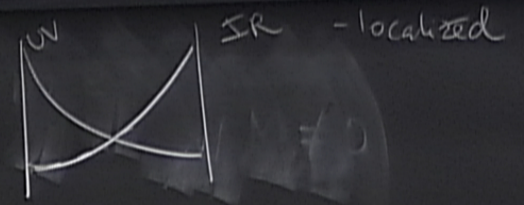
$$\Lambda_{SD} \sim \sqrt{T_{UV}} \sim -T_{IR} \quad \text{4D Minkowski}$$

adds new zero modes

$$f_0 \sim e^{M_b y}$$

$$M_b \geq 0$$

fermions $M_{F/K} \equiv C_f$

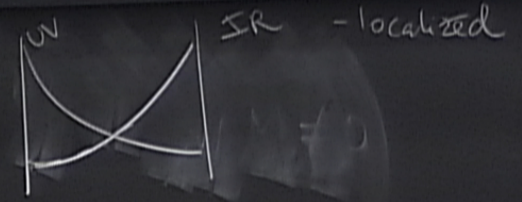


$$\Lambda_{SD} \sim \sqrt{T_{UV} \sim -T_{IR}} \quad 4D \text{ Minkowski}$$

adds new zero modes

$$f_0 \sim e^{M_b y} \quad \geq 0$$

fermions $M_{F/K} \equiv c_f \rightarrow c_f \Big\} = 1/2$ delocalized



$$\Lambda_{SD} \sim \sqrt{T_{UV} \sim -T_{IR}} \quad 4D \text{ Minkowski}$$

adds new zero modes

fermions

$$M_{F/K} \equiv c_f \rightarrow c_f$$

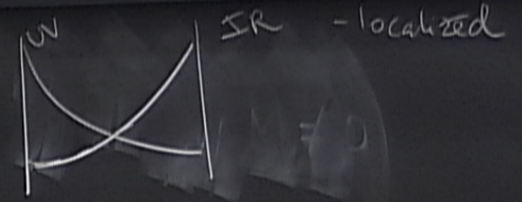
$$f_0 \sim e^{M_b y}$$

$$M_b \geq 0$$

$> 1/2$ UV-localized

$= 1/2$ delocalized

$< 1/2$ IR localized



in RS

① Physics depends position

$$\Lambda(y) = e^{-ky} M_{pl}$$

② zero modes localized anywhere

The Set-up

= where is what
most common

UV

UV localized

- light fermions
- and, i.s., e.g.
- gravitons

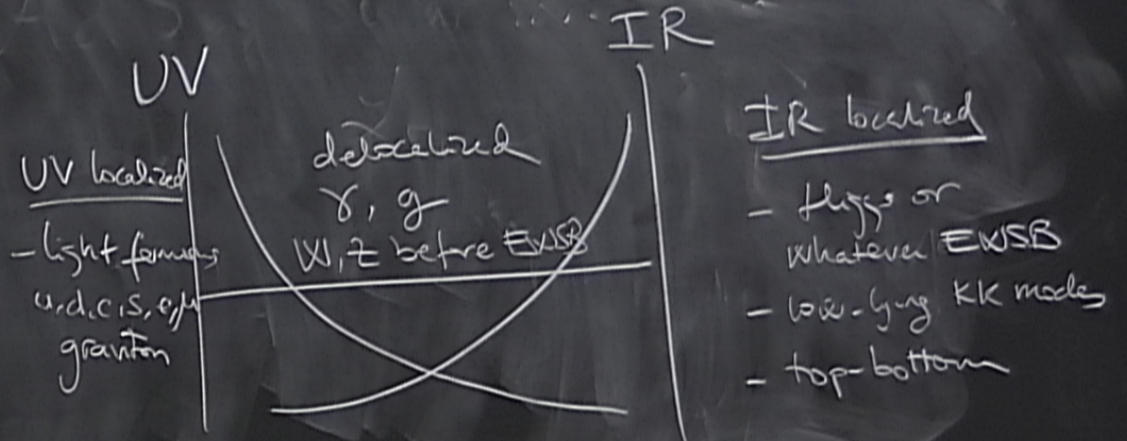
IR

IR localized

- Higgs or whatever EW/SB
- low-lying KK modes
- top-bottom

The Set-up

= where is what
most common



$\Psi_{\text{Kawata}} = H \bar{\Psi}_L \Psi_R$

Frogh - Nielsen

$$A_{SD} \sim \sqrt{T_{UV} \sim -T_{IR}}$$

4D Minkowski

adds new zero modes

fermions $M_{F/K} \equiv 0$

$$f_0 \sim e^{M_b y}$$

$$M_b \geq 0$$

UV-localized

delocalized

IR localized

$$\begin{aligned} > 1/2 \\ = 1/2 \\ < 1/2 \end{aligned}$$

