

Title: Quantum Computation and Simulation: Recent Progress in the Trapped Ion System

Date: Feb 22, 2012 04:00 PM

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Abstract: In this talk, I will briefly review the recent progress on quantum computation and simulation in the trapped ion system, with particular emphasis on the idea of scaling (how to scale up the number of qubits). I will discuss ideas towards large-scale quantum computation/simulation based on the network approach or the use of transverse phonon modes in anharmonic traps and then review the recent experimental progress along this direction. At the end of the talk, I will also briefly mention recent activities in Tsinghua-Michigan Joint Institute for quantum information.

Quantum Computation and Simulation: Recent Progress in the Trapped Ion System

Luming Duan

**Department of Physics, University of Michigan
& Center for Quantum Information, Tsinghua University**



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Why do we need a quantum computer?

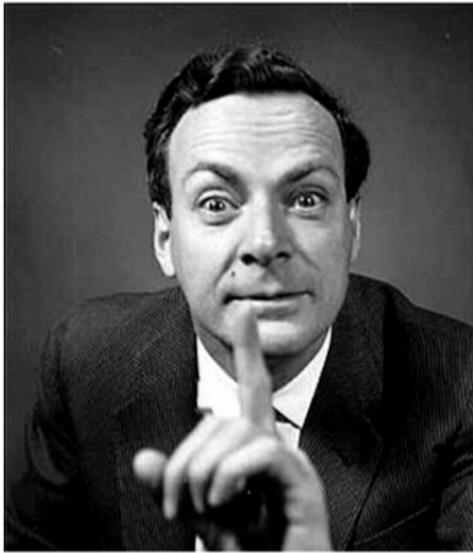


Why do we need a quantum computer?



Limit of a classical computer:

◆ Integration limit



Richard Feynman

“We have plenty of room at the bottom”

But,

Quantum Mechanics!

Limit of a classical computer:

◆ Principle limit

Some problems are hard! (NP)

Exponential scaling

Limit of a classical computer:

◆ Principle limit

Some problems are hard! (NP)

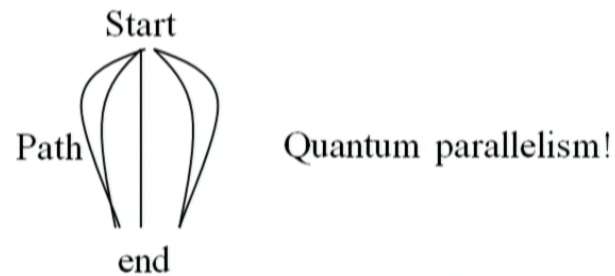
Exponential scaling

Physical example: strongly correlated system

Go to a quantum computer!!!

Possible exponential speedup

$$|\Psi\rangle = \sum_{i_1, i_2, \dots, i_n} c_{i_1, i_2, \dots, i_n} |i_1, i_2, \dots, i_n\rangle$$



Example: Shor's factorization.



How to build a quantum computer?

Requirements:

- ◆ A scalable system of qubits
- ◆ Good isolation and precise control of individual qubits
- ◆ Controllable interaction between qubits

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Candidate physical systems

AMO systems

- ✓ Trapped ions
- ✓ Neutral atoms
- ✓ Photons

Solid-state systems

- ✓ Quantum dots
- ✓ Superconducting qubits
- ✓ Nuclear spins

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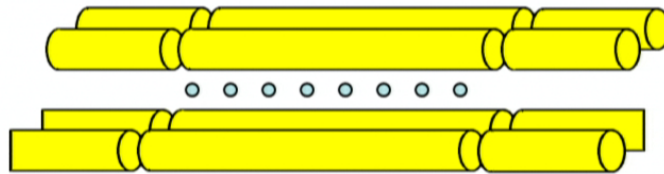
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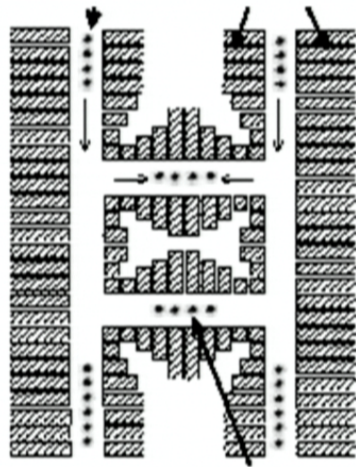


Linear Paul trap



How to scale up the system

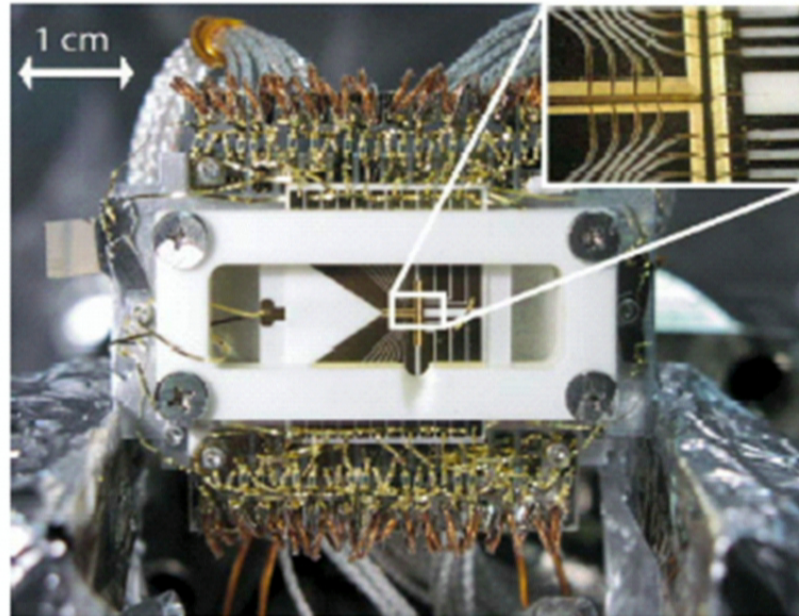
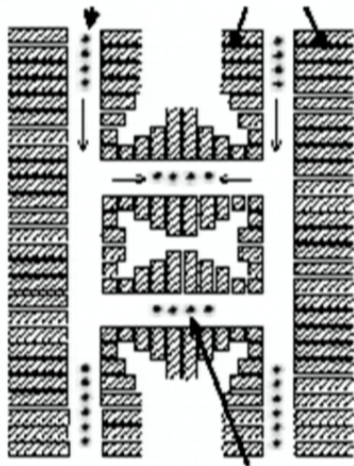
1. Ion shuttling:



Kielpinski, Monroe, Wineland,
Nature 417, 709 (2002)

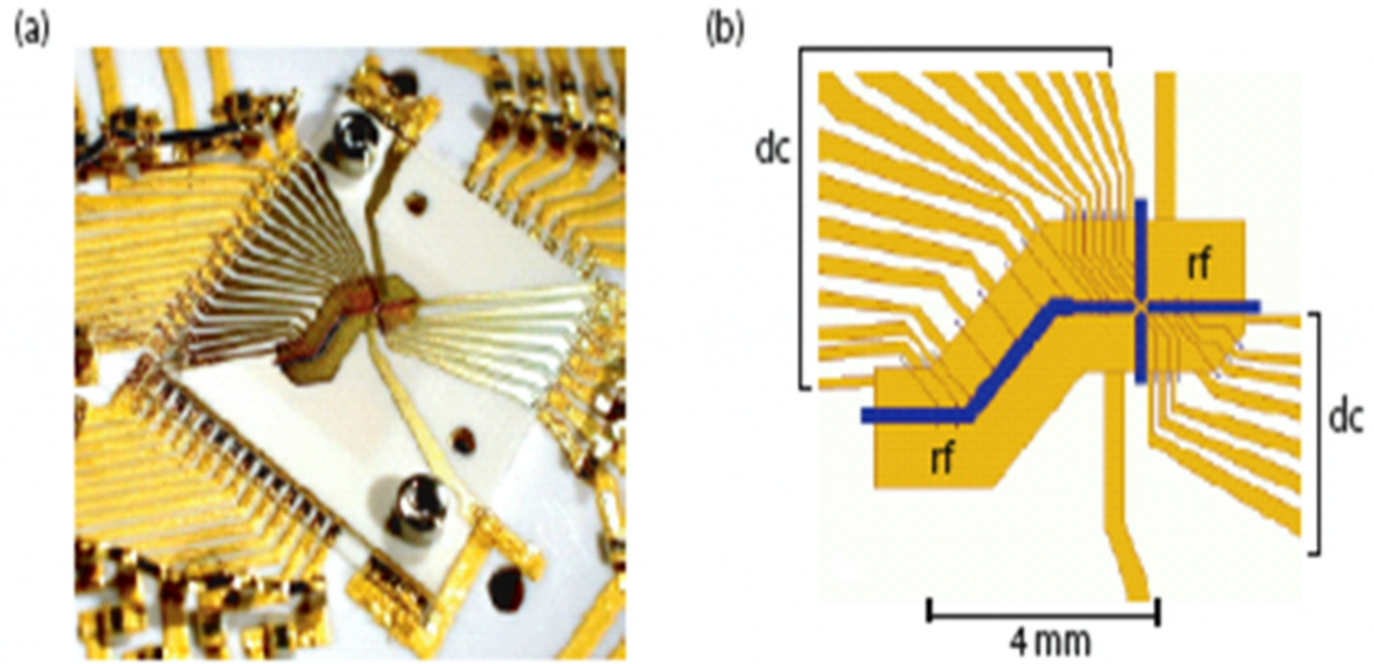
How to scale up the system

1. Ion shuttling:



Kielpinski, Monroe, Wineland,
Nature 417, 709 (2002)

More advanced traps



Wineland NIST group, chip trap, 2009

How to scale up the system

- **Quantum network approach through probabilistic photon coupling**

[Duan](#), [Blinov](#), [Moehring](#), [Monroe](#), QIC 2003

Duan and Monroe, Rev Mod Phys. (2010).

- **Transverse mode ion computation in anharmonic ion traps**

Zhu, Monroe, Duan, PRL, 2006

[G.-D. Lin](#), [S.-L. Zhu](#), [Islam](#), [Kim](#), [Chang](#), [Korenblit](#), [Monroe](#), [Duan](#), EPL, 2009

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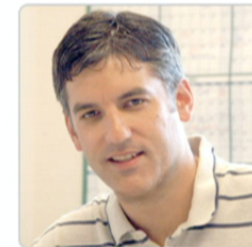
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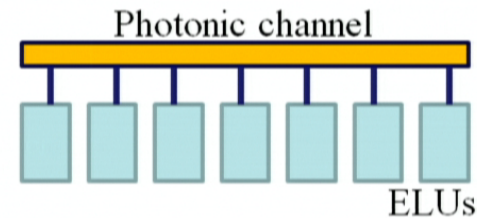
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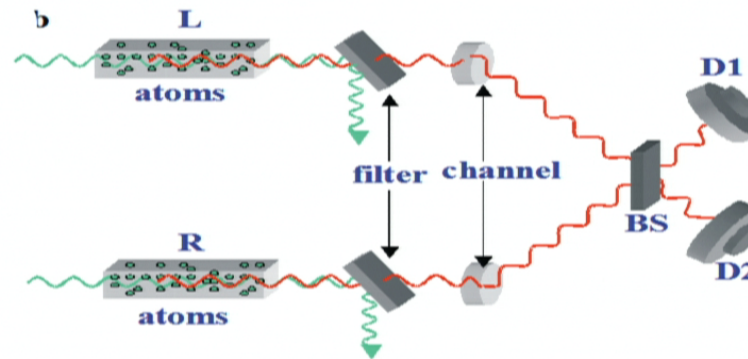
MUSIQC team (IARPA)

Modular Universal Scalable Ion-trap Quantum Computer



Inspiration from the DLCZ protocol

Duan, Lukin, Cirac, Zoller, (DLCZ), Nature 2001

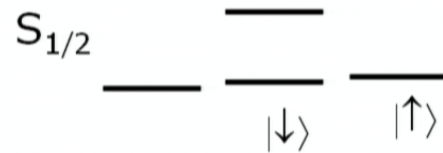
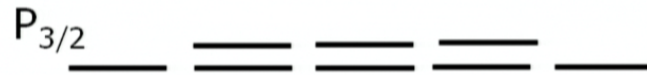


Experimental implementation:

Caltech group
Harvard group
Stanford group
Heidelberg group

Georgia Tech
USTC group
MIT group
Marx-Planck Institute

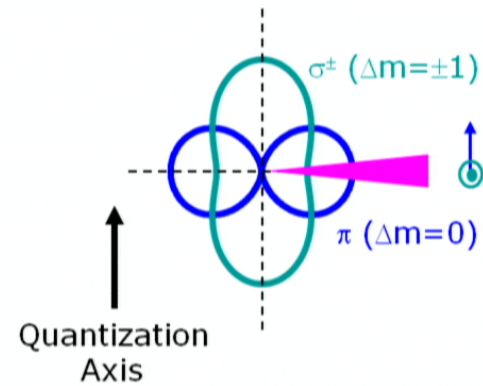
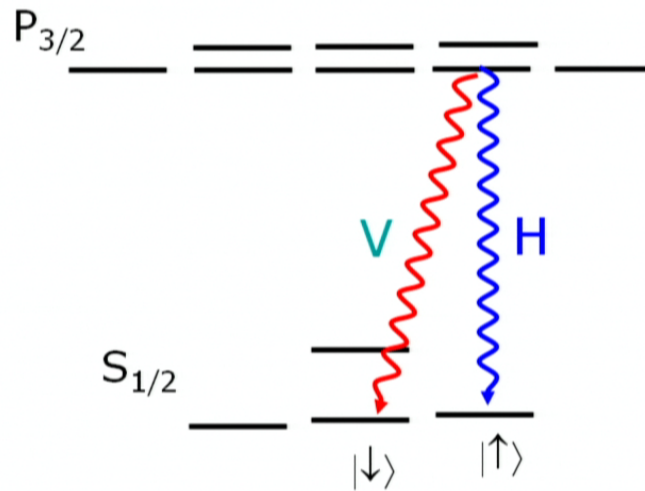
Experimental entanglement between 1 ion and 1 photon



Blinov, Moehring, Duan, Monroe
Nature 428, 153 (2004).



Experimental entanglement between 1 ion and 1 photon

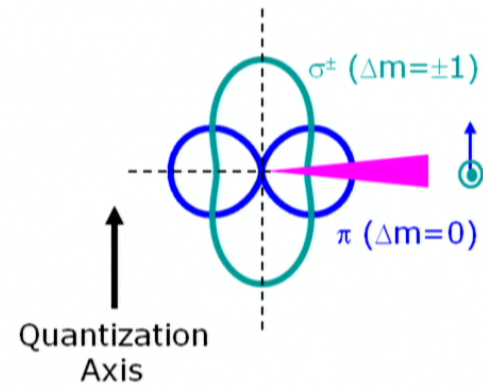
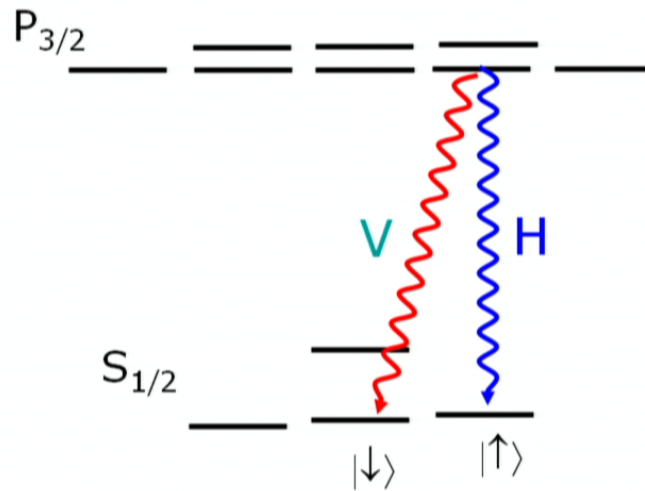


$$|\psi\rangle = |\downarrow\rangle|V\rangle + |\uparrow\rangle|H\rangle$$

Blinov, Moehring, Duan, Monroe
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Experimental entanglement between 1 ion and 1 photon



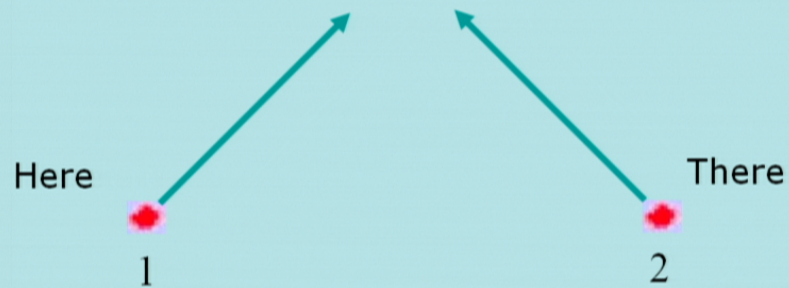
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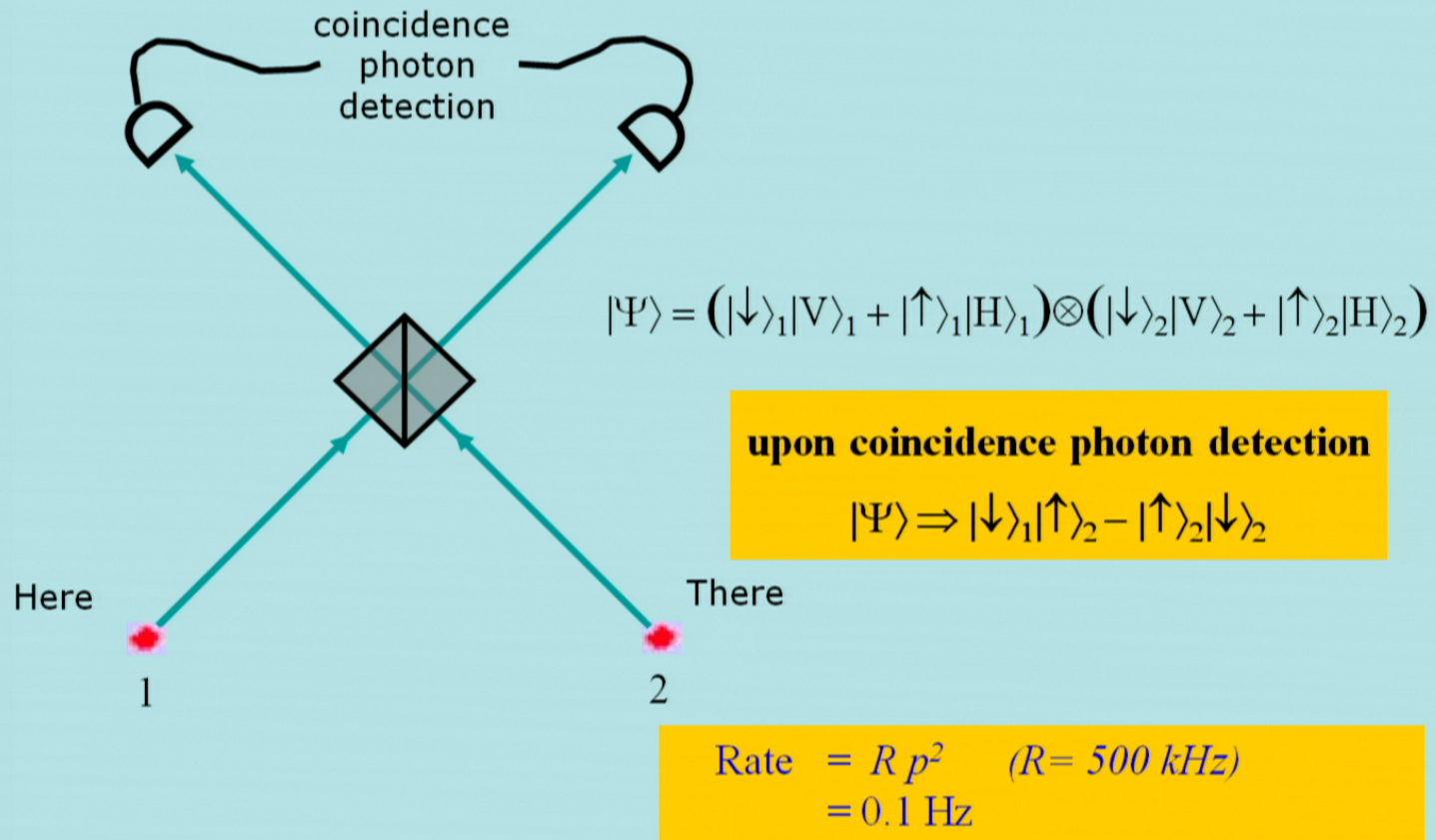


Probabilistic entanglement between two remote ions

$$|\Psi\rangle = (|\downarrow\rangle_1|V\rangle_1 + |\uparrow\rangle_1|H\rangle_1) \otimes (|\downarrow\rangle_2|V\rangle_2 + |\uparrow\rangle_2|H\rangle_2)$$



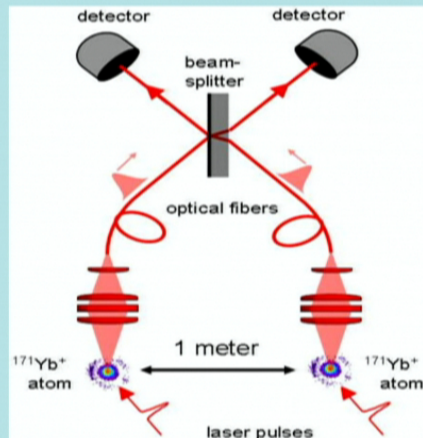
Probabilistic entanglement between two remote ions



Entanglement of remote ions:

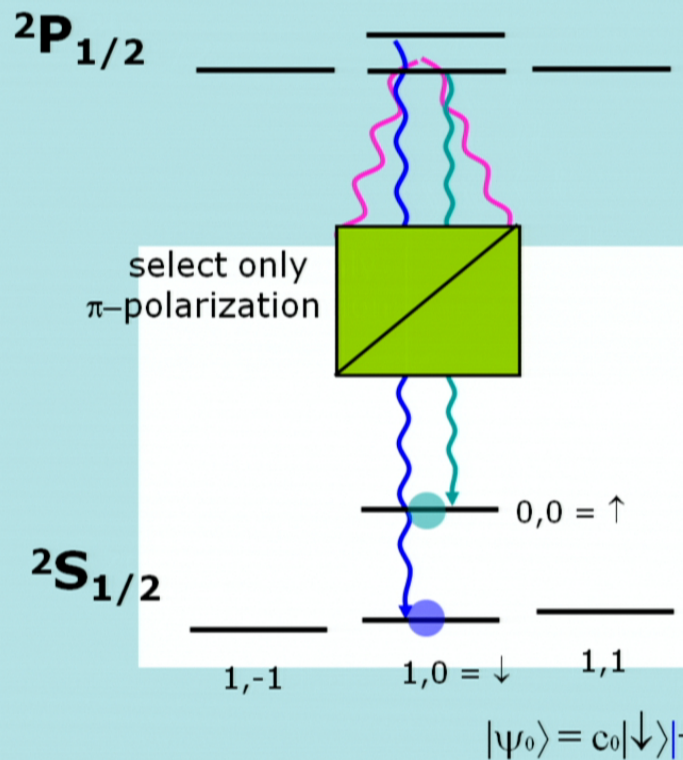
D. L. Moehring, P. Maunz, S. Olmschenk, K. C. Younge, D. N. Matsukevich, L.-M. Duan, and C. Monroe, Nature 449, 68 (2007).

Entanglement fidelity: 87(2)%



Probabilistic ion Gate (Duan et al, PRA, 2006)

Frequency Qubit



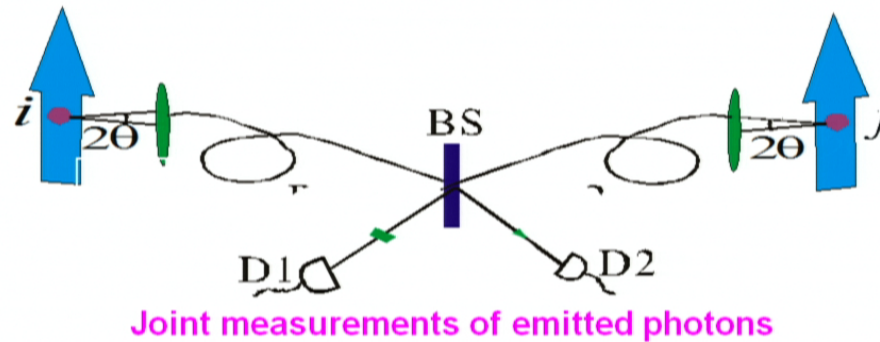
Given photon is emitted into polarizer

$$|\psi\rangle = c_0|\downarrow\rangle|\text{blue}\rangle + c_1|\uparrow\rangle|\text{green}\rangle$$

Keep track of information of the initial state !!

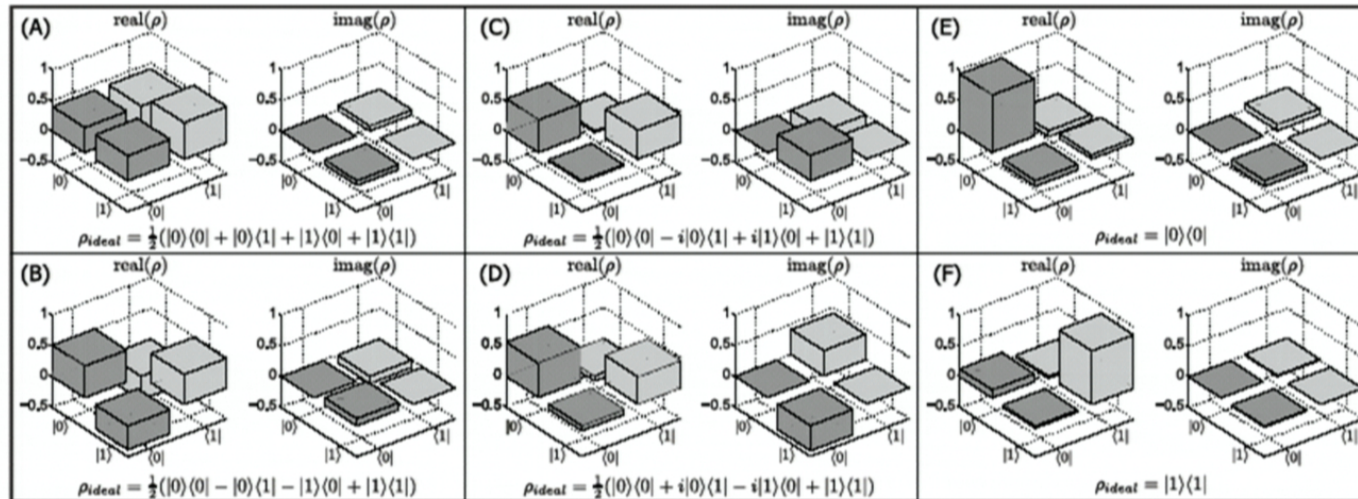
Probabilistic gates on remote ion qubits

Duan et al., PRA, 2006



- ✓ ions in arbitrary initial states
- ✓ probabilistic ZZ gate (projection to $|01\rangle$ and $|10\rangle$ subspace)
- ✓ Probabilistic ZZ is a gate that is universal and efficient for quant. Computation

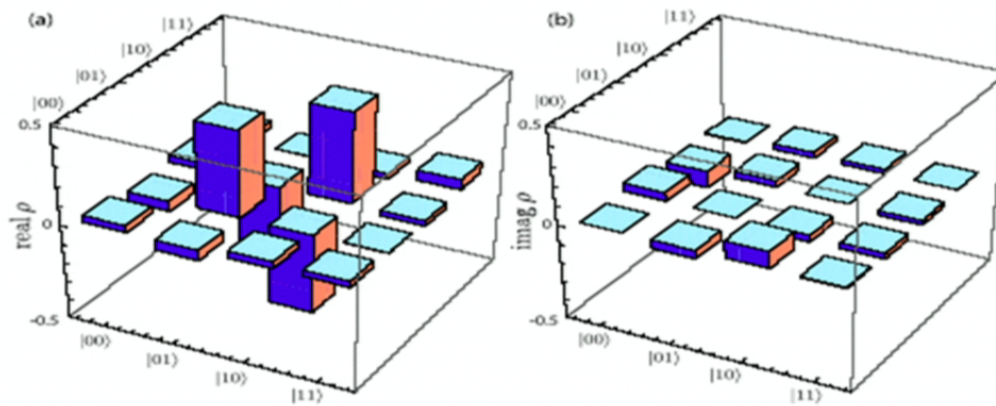
Quantum teleportation between remote ions



Average fidelity of teleported state: $90 \pm 2\%$.

S. Olmschenk, D. N. Matsukevich, P. Maunz, D. Hayes, L.-M. Duan, C. Monroe
[arXiv:0907.5240](https://arxiv.org/abs/0907.5240), Science, 2009

Experimental demonstration of a remote gate

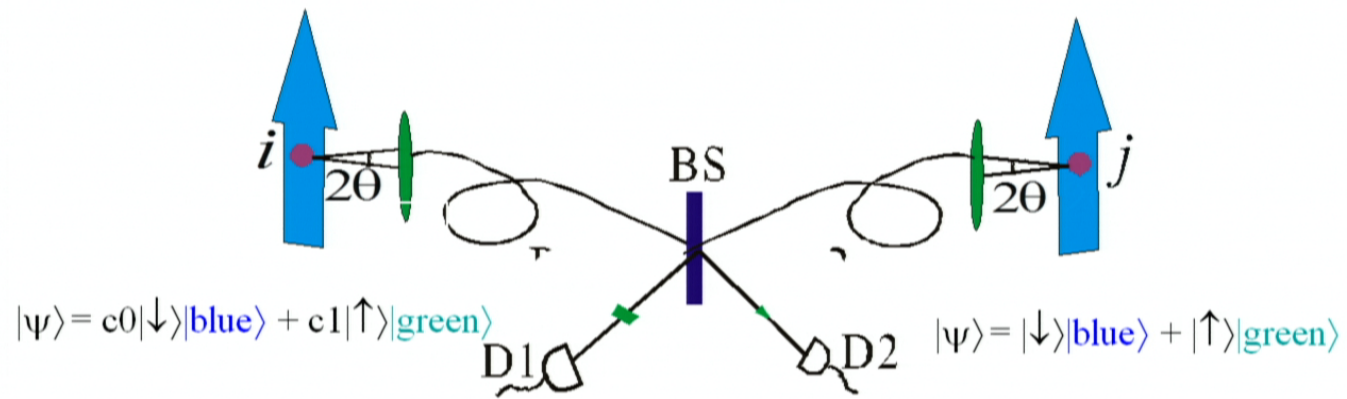


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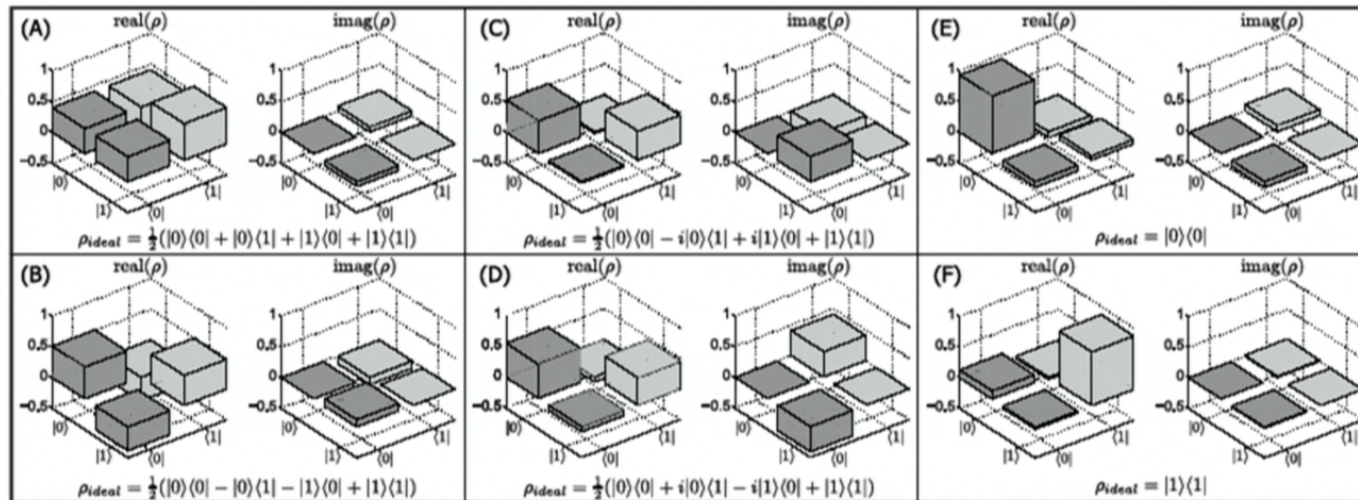
[P. Maunz](#), [S. Olmschenk](#), [D. Hayes](#), [D. N. Matsukevich](#), [L.-M. Duan](#), [C. Monroe](#),
[arXiv:0902.2136](#), PRL, 2009

Teleportation of ion states

$$|\psi\rangle = c_0|\downarrow\rangle + c_1|\uparrow\rangle$$



Quantum teleportation between remote ions



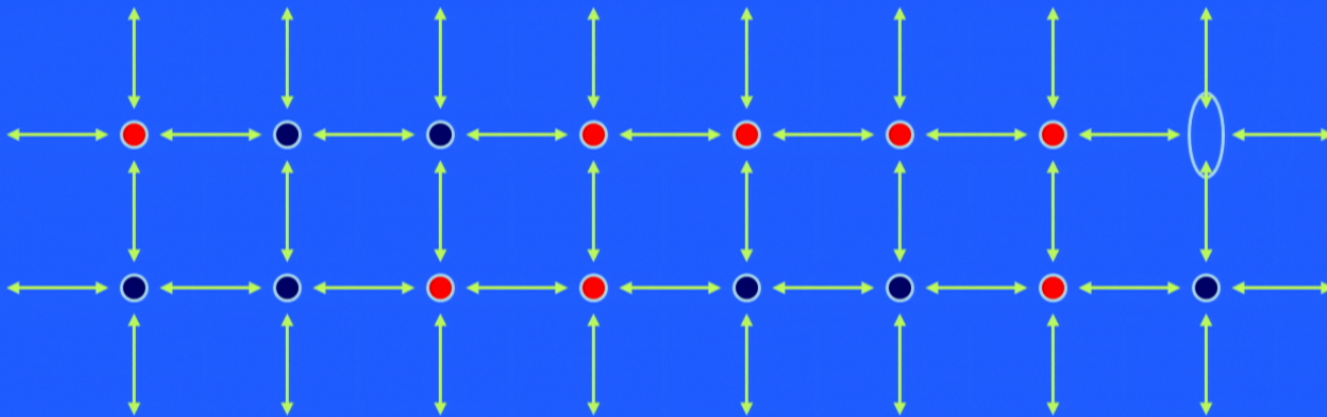
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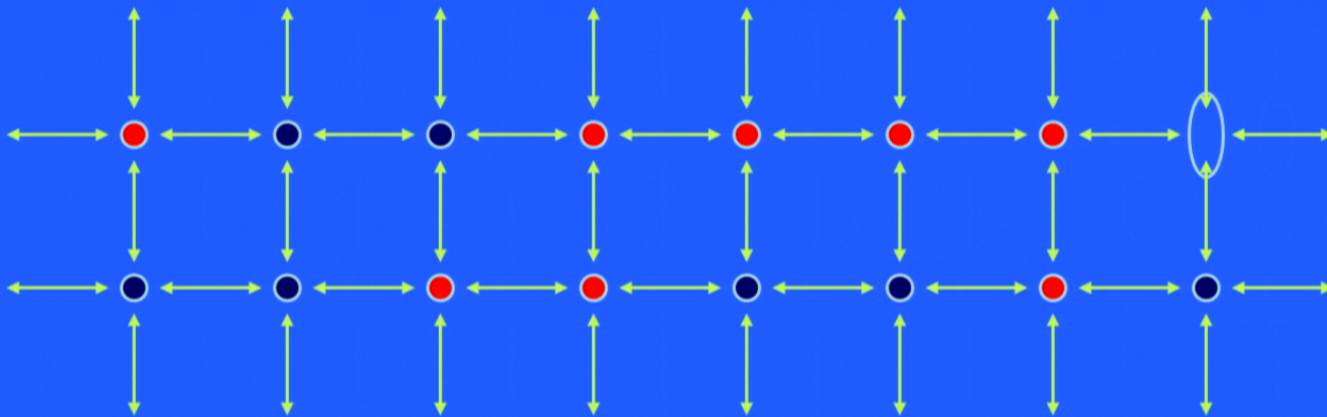
Quantum computing with probabilistic ion-photon gate

Duan and Raussendorf, Phys. Rev. Lett. 95, 080503 (2005)



Quantum computing with probabilistic ion-photon gate

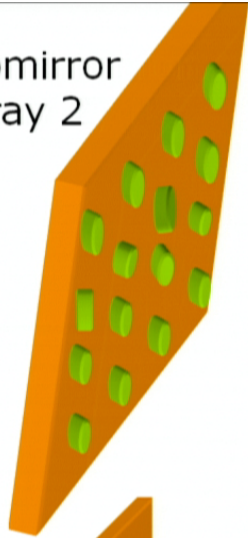
Duan and Raussendorf, Phys. Rev. Lett. 95, 080503 (2005)



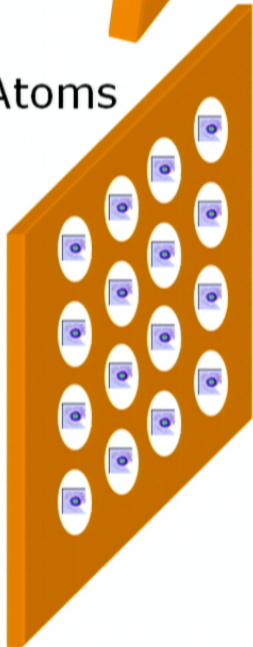
Efficient scaling with probabilistic gates:

$$M \propto n \ln(n/\varepsilon) \left(\frac{2}{p}\right)^{\log_2(4/p)+2}$$

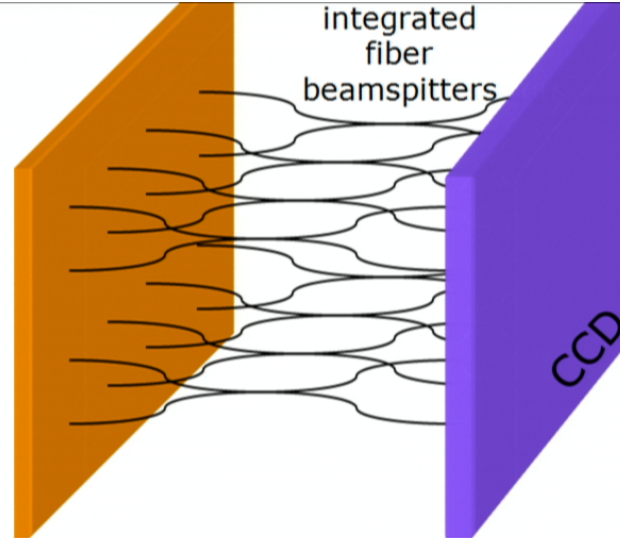
micromirror
array 2



Atoms



integrated
fiber
beamsplitters



CCD

micromirror
array 1



Monroe, Kim etc.

How to scale up the system

- **Quantum network approach through probabilistic photon coupling**

[Duan](#), [Blinov](#), [Moehring](#), [Monroe](#), QIC 2003

Duan and Monroe, Rev Mod Phys. (2010).

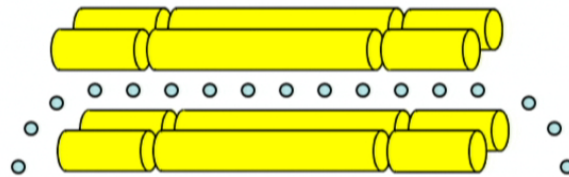
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Zhu, Monroe, Duan, PRL, 2006

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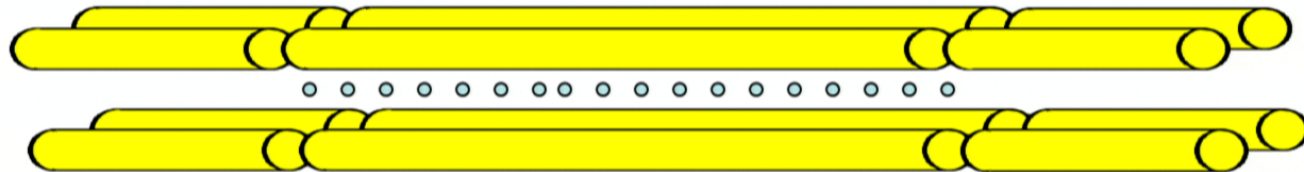
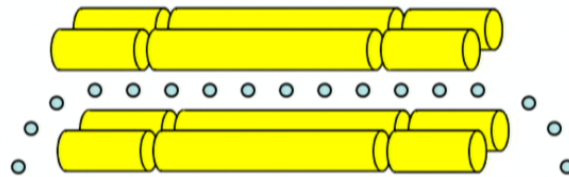
Scale up in a single linear trap

What is the difficulty?



Scale up in a single linear trap

What is the difficulty?



Scale up in the linear trap

The real problems:

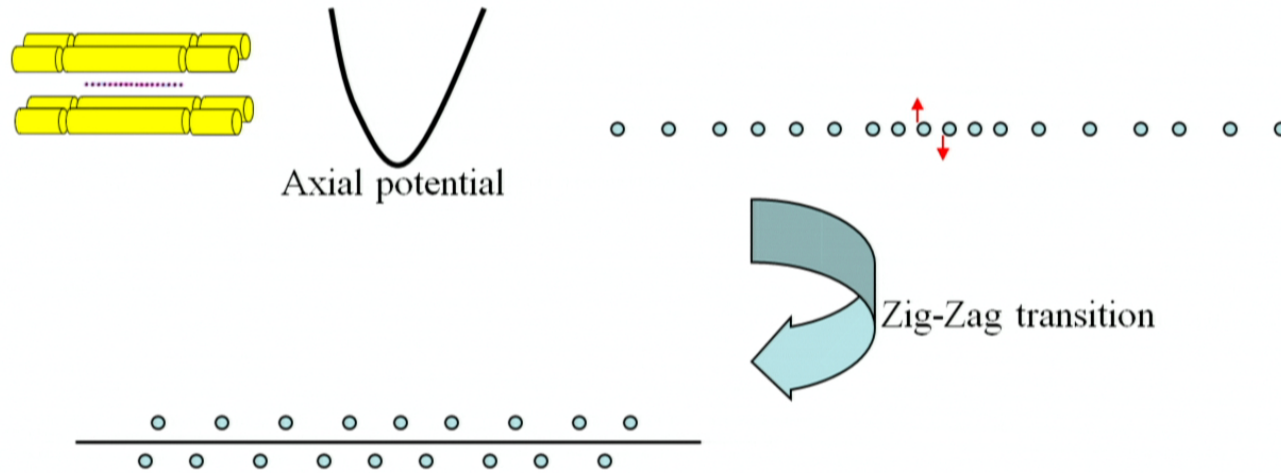
1. Chain instability due to structural phase transition



Scale up in the linear trap

The real problems:

1. Chain instability due to structural phase transition



Scale up in the linear trap

Solutions to all the problems:

[G.-D. Lin](#), [S.-L. Zhu](#), [Islam](#), [Kim](#), [Chang](#), [Korenblit](#), [Monroe](#), [Duan](#)

[arXiv:0901.0579](#), EPL, 2009

Scale up in the linear trap

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[arXiv:0901.0579](#), EPL, 2009

An Uniform Ion Trap

Design of a large-scale uniform trap



No sideband cooling

Solution to Problem 2: Sideband cooling

We require no sideband cooling for the gates

Only Doppler Cooling!

No sideband cooling

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Thermal vibration outside of the Lamb-Dicke limit

No sideband cooling

Solution to Problem 2: Sideband cooling

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Thermal vibration outside of the Lamb-Dicke limit

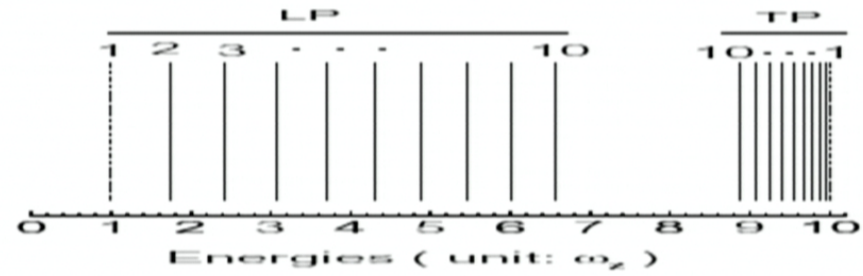
We use transverse photon modes instead of the axial ones



Stronger confinement leads to more robustness to vibrational noise

Transverse phonon modes

Phonon mode structure:



Multi-mode quantum gates

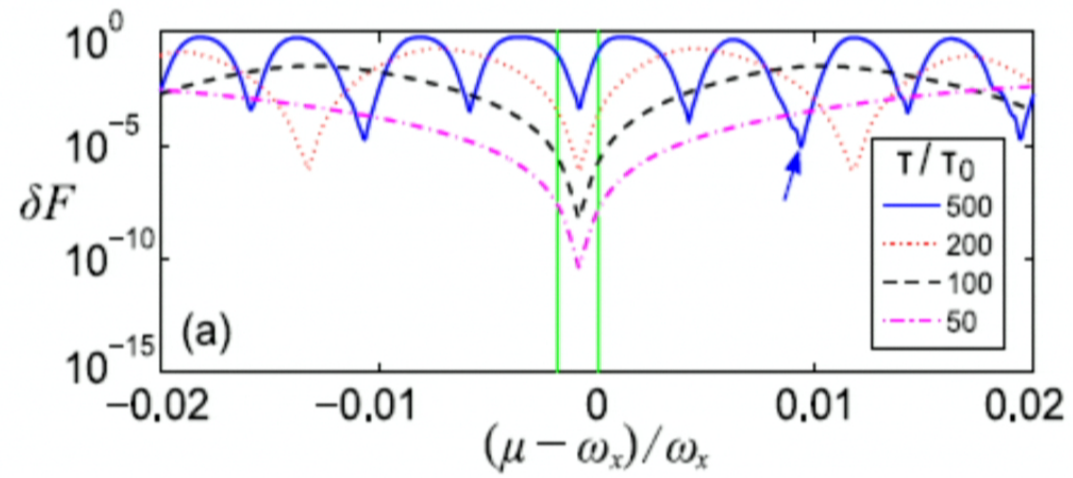
Solution to Problem 3: multiple phonon modes



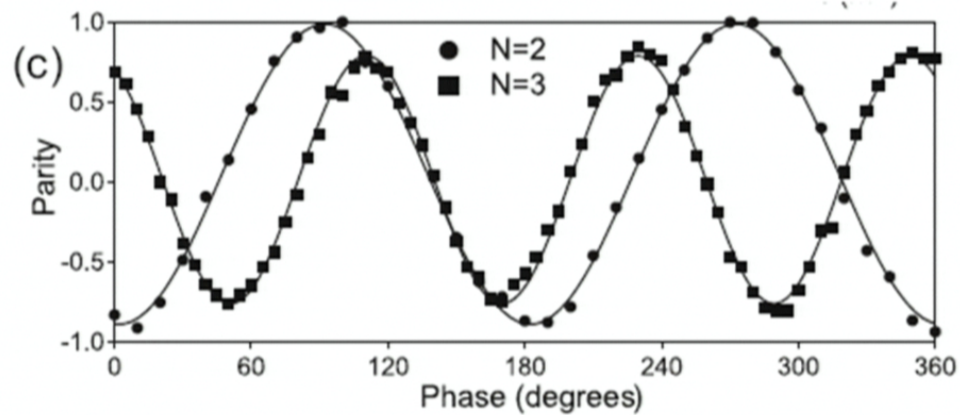
- Through laser pulse control, high-fidelity Quantum gates can be achieved with involvement of all phonon modes
- The required control can be pretty simple

Laser control for the gate

The gate infidelity



Experimental demonstration of transverse mode quantum gate



Fidelity: $F_2 > 96\%$, $F_3 > 84\%$

K. Kim, M.-S. Chang, R. Islam, S. Korenblit, L.-M. Duan, C. Monroe
[arXiv:0905.0225](https://arxiv.org/abs/0905.0225), PRL (2009).

Quantum Simulation

Solve fundamental many-body models: (important for new materials)

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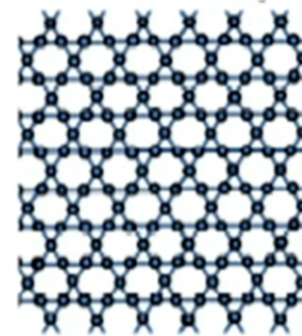
Examples:

Hubbard model (relevant for high-Tc physics)

$$H_{weak} = t \sum_{\langle i,j \rangle} a_{i\sigma}^+ a_{j\sigma} + u \sum_i a_{i\uparrow}^+ a_{i\downarrow}^+ a_{i\downarrow} a_{i\uparrow}$$

Frustrated magnetic model

$$H_0 = J \sum_{\langle i,j \rangle} S_i \cdot S_j$$



Examples of simulation with ultracold atoms

Bose-Hubbard model:

Jaksch, Gardiner, Cirac, Zoller, PRL 1998.
Bloch's group, Nature (2002)

Quantum magnetic model:

Duan, Demler, Lukin, PRL (2003).
Bloch's group, Nature (2007);

Fermion Hubbard model:

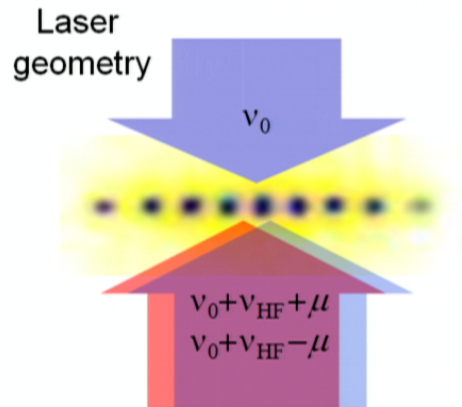
under weak interaction

Hofstadter, Cirac, Zoller, Demler, Lukin, PRL 2003

under strong interaction

Duan, PRL (2005).
Ketterle's group, Nature (2007).

Quantum Simulation with trapped ions



$$H = \sum_{i < j} J_{i,j} \sigma_x^{(i)} \sigma_x^{(j)} + B \sum_i \sigma_y^{(i)}$$

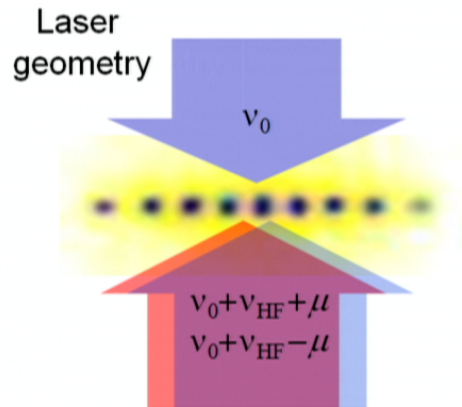
$$J_{i,j} = \Omega_i \Omega_j \frac{\hbar (\delta k)^2}{2M} \sum_m \frac{b_{i,m} b_{j,m}}{\mu^2 - \omega_m^2}$$

μ = laser detuning

μ controls range and form of interaction

Porras, Ciriac, PRL, 2004
Zhu, Monroe, Duan, PRL, 2006

Quantum Simulation with trapped ions



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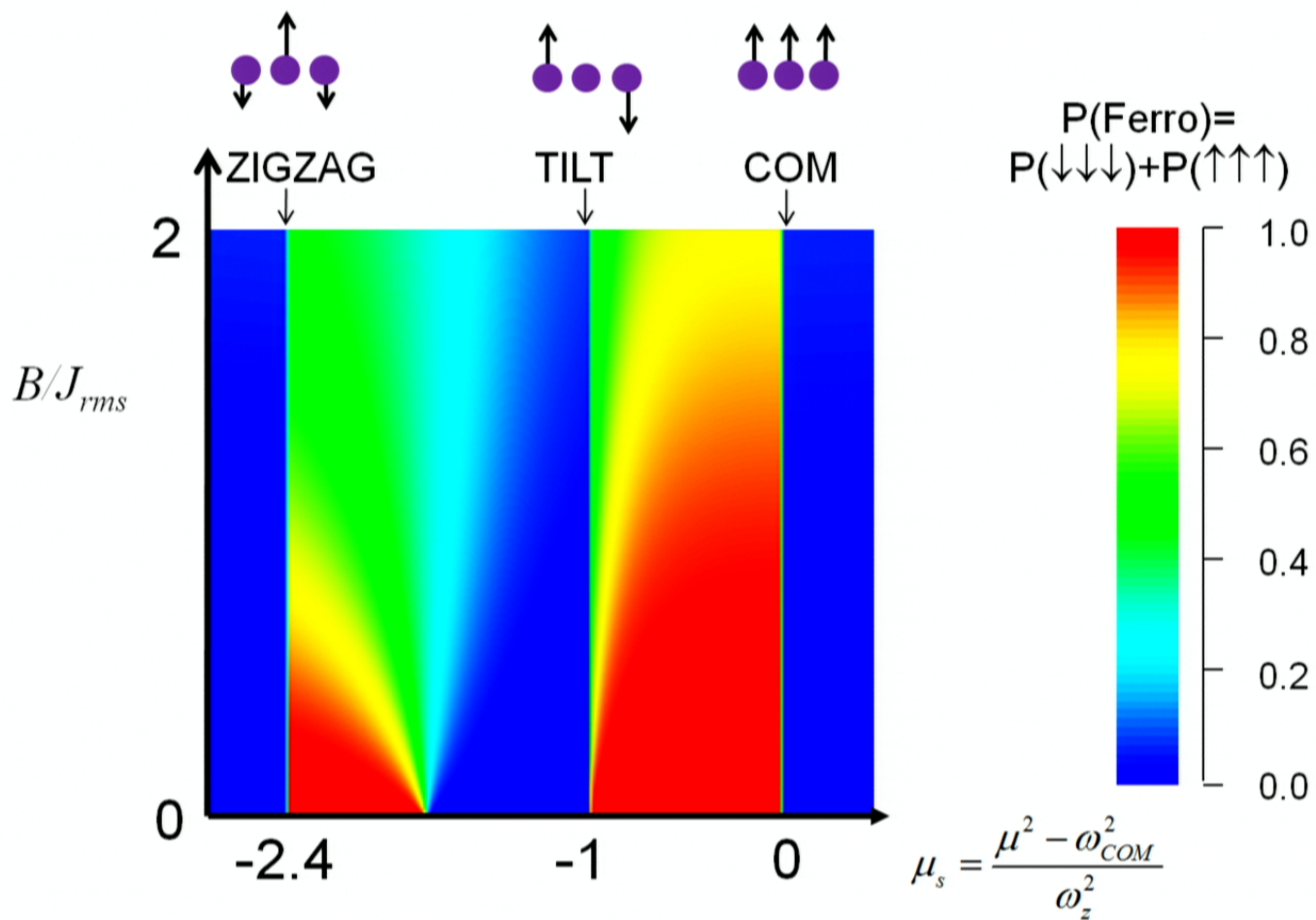
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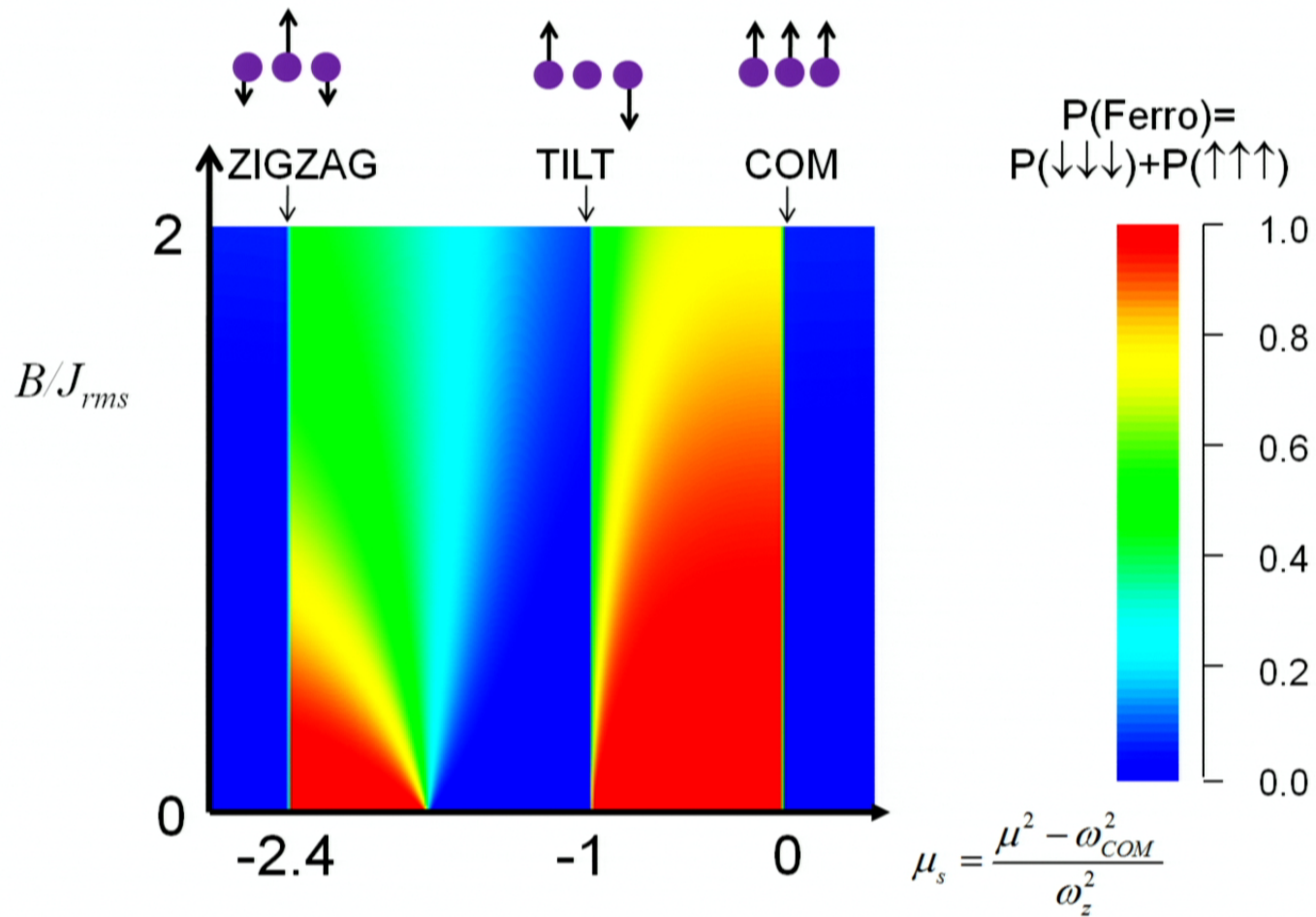
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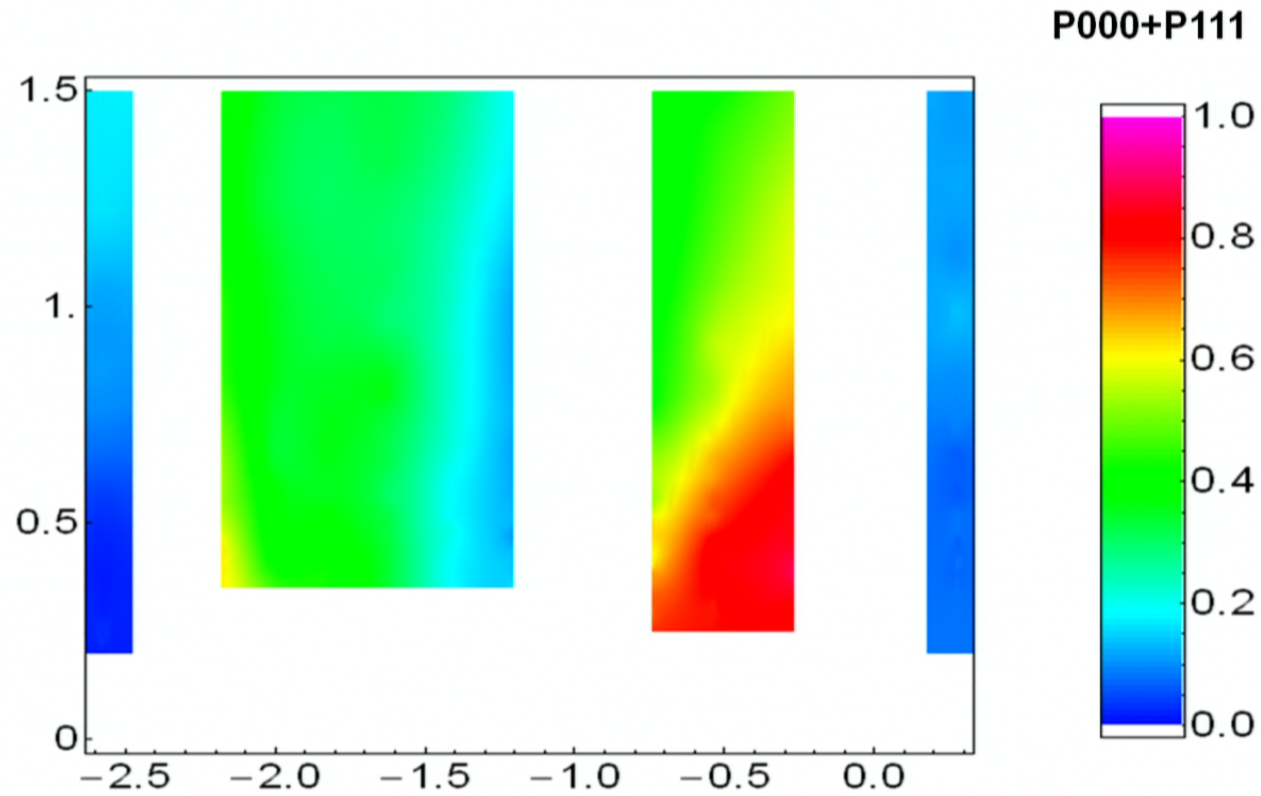
3-ion "phase diagram"



3-ion "phase diagram"

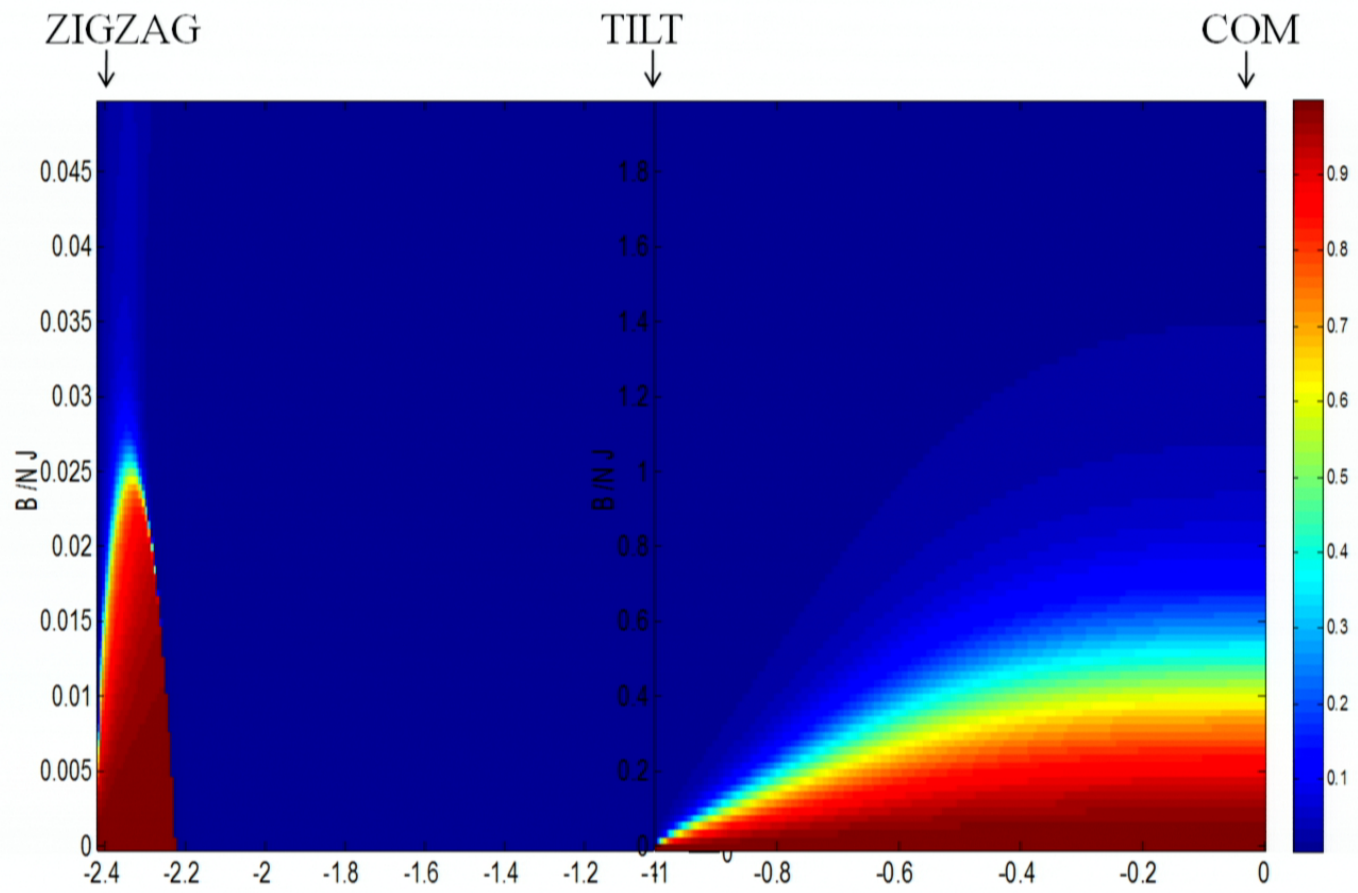


Experimental Phase Diagram (PMT) with P000+P111

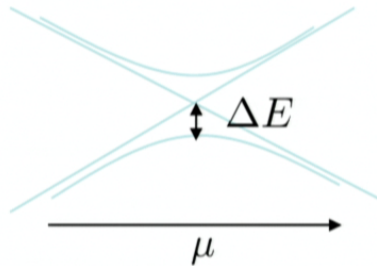


Kim, Chang, Korenblit, Islam, Edwards, Freericks, Lin, Duan, Monroe,
Nature 465, 590 (2010).

9-ion phase diagram



Exponentially sharp phase boundary



$$\Delta E \sim \left(\frac{B}{NJ}\right)^{\frac{N-1}{2}}$$



清华大学
Tsinghua University



交叉信息研究院
Institute for Interdisciplinary
Information Sciences



量子信息中心
Center for Quantum Information

Mission of CQI

- **A world-class research center for quantum information**
- Vibrant research culture with generous support
- International: more than half faculty are of non-Chinese origin
- Independence of junior faculty
- Interdisciplinary and integrated



量子信息中心
Center for Quantum Information



Andrew YAO

ITCS: Strong theoretical computer science program

Experimental QI platform:

- ✓ Trapped ion quantum computation
- ✓ Photonic quantum network at the telecom
- ✓ Atom-Photon Quantum interface
- ✓ Ultracold atom quantum simulator



Amy WANG



Bo Zheng



Duan LM



Kihwan Kim



Zhe Zhang



Chong Zu



Ke Liu

Center for Quantum Information



5
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Center for Quantum Information



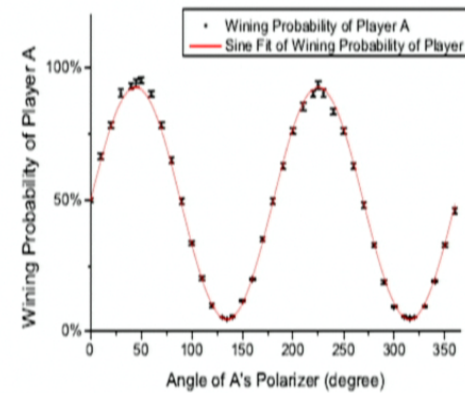
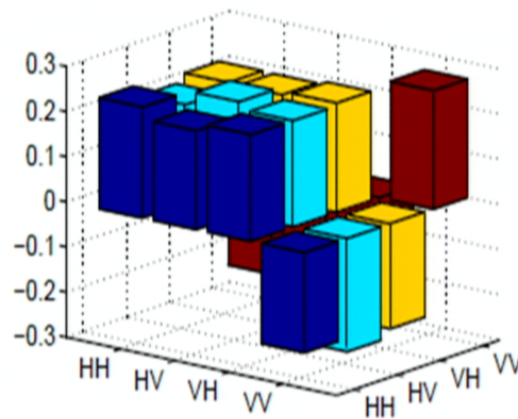
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$$(|00\rangle_{ab} + |01\rangle_{ab} + |10\rangle_{ab} - |11\rangle_{ab}) / 2$$

Demonstration of
quantum game

NJP (2012)





量子信息中心
Center for Quantum Information



Giulio Chiribella



Alioscia Hamma

New Members



Hongcheng Jiang



Xiongfeng Ma



清华大学
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交叉信息研究院
Institute for Interdisciplinary
Information Sciences



量子信息中心
Center for Quantum Information

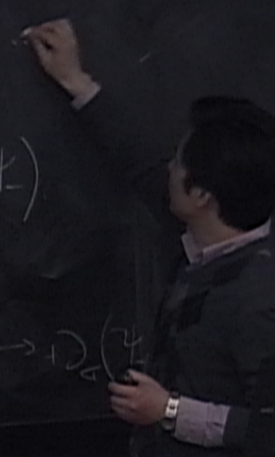
Actively recruiting:

- Faculty, Research Faculty, and Postdoctoral fellows!
- Visitor Program, Faculty/student exchange

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More information: <http://iiis.tsinghua.edu.cn/en/>

$$\begin{aligned}
 & + s_{T-} \cdot \underbrace{2_{T-} + 2_{T-} \cdot s_{(2_{T-})}}_{\text{---}} \\
 & + 2_{-} (7_{+} s_{7_{+}}) \quad - 2_{+} \cdot s_{7_{-}} + 2_{+} (7_{-} s_{7_{-}}) \\
 & 2_{-} \cdot s_{7_{-}} + 2_{-} (7_{+} s_{7_{+}}) + 2_{+} (7_{-} s_{7_{-}}) \\
 & \quad - 2_{+} (7_{+} s_{7_{+}}) + 2_{-} (7_{-} s_{7_{-}})
 \end{aligned}$$



$$\begin{aligned}
 & + s_{\tau} \cdot \underbrace{2_{\tau} \tau_{-} + \tau_{-} \cdot s(2_{\tau} \tau_{-})}_{\text{---}} \bigg) \frac{1}{\tau} \cdot \frac{1}{\tau} \\
 & + 2_{-} (\tau_{+} s \tau_{+}) \quad - 2_{\tau} \cdot s_{\tau} \tau_{-} + \tau_{-} (\tau_{-}) \\
 & \tau_{-} \cdot s_{\tau} \tau_{-} + 2_{-} (\tau_{+} s \tau_{+}) + 2_{\tau} (\tau_{-}) \\
 & - 2_{\tau} (\tau_{+} s \tau_{+}) + 2_{\tau} (\tau_{-} s \tau_{-}) + 2_{-} (\tau_{-})
 \end{aligned}$$

$$\begin{aligned}
 & + s_7 \cdot 2_7 + 7_7 \cdot s(2_7) \\
 & + 2_7(7_7 s_7) = 2_7 \cdot s_7 + 2_7(7_7 s_7) \\
 & 7_7 \cdot s_7 + 2_7(7_7) + 2_7(7_7 s_7) \rightarrow + 2_7(7_7 s_7) + 2_7(\checkmark)
 \end{aligned}$$

