

Title: Beyond the Standard Model (Review) - Lecture 10

Date: Feb 27, 2012 09:00 AM

URL: <http://pirsa.org/12020091>

Abstract:

maintain stabilized EW scale \rightarrow soft breaking

\rightarrow gaugino masses $M \lambda \lambda$

scalar partner mass

trilinear scalar

$$M^2 \phi^2$$
$$A \phi^3$$

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{MSSM}}$$

$\mathcal{O}(100)$

not successful
eff. theory

maintain stabilization ew scale \rightarrow soft breaking

- \rightarrow gaugino masses $M \lambda \lambda$
- scalar partner mass
- trilinear scalar

$$m^2 \phi^2$$
$$A \phi^3$$

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{MSSM}}$$

$\mathcal{O}(100)$

not successful
eff thg

el sysy @ high-E \rightarrow reduce # p

SUSY

maintain stabilization ew scale \rightarrow soft breaking

$\left\{ \begin{array}{l} \text{gaugino masses } M \lambda \lambda \\ \text{scalar partner mass } m^2 \\ \text{trilinear scalar } A \phi \end{array} \right.$

Understand, model SUSY @ high-E \rightarrow reduce # parameters

UV-completion to Left

Understand, model SUSY @ high-E \rightarrow reduce # parameters

UV-completion to Left

SUSY model building

Spontaneous SUSY

$\mathcal{L}_{\text{SUSY}}$ but $\langle \phi \rangle$

SUSY $Q|0\rangle = \bar{Q}|0\rangle = 0$

$\langle Q, \bar{Q} \rangle = 26 \mu \text{P}^M \rightarrow$

Understand, model SUSY @ high-E \rightarrow reduce # parameters

UV-completion to Left

SUSY model building

Spontaneous SUSY

$\mathcal{L}_{\text{SUSY}}$ but $\neq 0$

$$\text{SUSY} \quad Q|0\rangle = \bar{Q}|0\rangle = 0$$

$$\{Q, \bar{Q}\} = 2\epsilon_{\mu\nu} P^M \xrightarrow{\epsilon_{\mu\nu} \bar{\epsilon}_{\mu\nu}} P^M = \frac{1}{4} \bar{\epsilon}^M \{Q, \bar{Q}\}$$

$$P^0 = \frac{1}{4} \{Q_1 \bar{Q}_1 + \bar{Q}_1 Q_1 + Q_2 \bar{Q}_2 + \bar{Q}_2 Q_2\}$$

$\mathcal{N} > 1$ $\mathcal{N} = 1$ matter sector } \rightarrow SUSY XDIMS
 $\mathcal{N} = 2$ gauge sector }
 $\mathcal{N} = 4 \rightarrow$ Landau poles

$\mathcal{N} < 1$

$\mathcal{N} = 1$

$\mathcal{N} = 1$ matter sector } \rightarrow SUSY XDIMS
 $\mathcal{N} = 2$ gauge sector }
 $\mathcal{N} = 4 \rightarrow$ random poles

$$\langle 0 | \overset{P^0}{H} | 0 \rangle = \frac{1}{4} \left\{ \underbrace{\langle 0 | Q \bar{Q} | 0 \rangle}_{\text{norm of } Q} + \dots \right\} = \frac{1}{4} (\| Q$$

$\mathcal{N} = 1$ matter sector } \rightarrow SUSY XDIMS
 $\mathcal{N} = 2$ gauge sector }
 $\mathcal{N} = 4 \rightarrow$ random poles

$$\langle 0 | \overset{P^0}{\mathbb{1}} | 0 \rangle = \frac{1}{4} \left\{ \underbrace{\langle 0 | Q \bar{Q}_i | 0 \rangle}_{\text{norm of } Q_i} + \dots \right\} = \frac{1}{4} \left(\overset{>0}{\| \bar{Q}_i | 0 \rangle \|^2} + \dots \right) \geq 0$$

$N=1$ matter sector } \rightarrow SUSY XDIMS
 $N=2$ gauge sector }
 $N=4 \rightarrow$ random poles

$$\langle 0 | \overset{P^0}{H} | 0 \rangle = \frac{1}{4} \{ \underbrace{\langle 0 | Q \bar{Q}_1 | 0 \rangle}_{\text{norm of } Q_1} + \dots \} = \frac{1}{4} (\| \bar{Q}_1 | 0 \rangle \|^2 + \dots) \geq 0$$

\downarrow if SUSY
 $\langle 0 | H | 0 \rangle \geq 0 \rightarrow$
 no non-perturbative effects



$N=1$ matter sector } \rightarrow SUSY XDIMS
 $N=2$ gauge sector }
 $N=4 \rightarrow$ random poles

\downarrow if SUSY
 $\langle 0|H|0\rangle \geq 0 \rightarrow \langle 0|V|0\rangle \geq 0$
 norm of Q_i
 no non perturbative effects



$N=1$ matter sector } \rightarrow SUSY XDIMS
 $N=2$ gauge sector }
 $N=4 \rightarrow$ random poles

\downarrow if SUSY
 $\langle 0 | H | 0 \rangle \geq 0 \rightarrow \langle 0 | V | 0 \rangle = 0$
 no non perturbative effects instantons
 norm of Q_i



$W=4 \rightarrow$ random poles

$$\langle 10 \rangle = \frac{1}{4} \{ \underbrace{\langle 0 | Q \bar{Q} | 0 \rangle + \dots}_{\text{norm of } Q} \} = \frac{1}{4} (\overset{>0}{\| \bar{Q} | 0 \rangle \|^2 + \dots }) \geq 0$$

f SUSY

$$\langle 10 \rangle \geq 0 \rightarrow \langle 0 | V | 0 \rangle = 0$$

no non perturbative effects instantons

chiral, vector superm

$$\langle 0 | H | 0 \rangle = \frac{1}{4} \{ \underbrace{\langle 0 | Q \bar{Q} | 0 \rangle}_{\text{norm of } Q} + \dots \} = \frac{1}{4} (\| \bar{Q} | 0 \rangle \|^2 + \dots) \geq 0$$

↓ if SUSY

$$\langle 0 | H | 0 \rangle \geq 0 \rightarrow \langle 0 | V | 0 \rangle = 0$$

no non perturbative effects instantons

chiral, vector supermultiplets
 $V = FF^* + \frac{1}{2} D^2$

$$\langle 0 | \overset{p^0}{H} | 0 \rangle = \frac{1}{4} \{ \underbrace{\langle 0 | Q \bar{Q} | 0 \rangle}_{\text{norm of } Q} + \dots \} = \frac{1}{4} (\| \bar{Q} | 0 \rangle \|^2 + \dots) \geq 0$$

\downarrow if SUSY
 $\langle 0 | H | 0 \rangle \geq 0 \rightarrow \langle 0 | V | 0 \rangle = 0$
 no non perturbative effects instantons

chiral, vector supermultiplets
 $V = FF^* + \frac{1}{2} D^2$
 auxiliary fields

$\langle O_1 \rangle \neq 0 \rightarrow \langle O_2 \rangle = 0$
no non perturbative effects instantons

auxiliary fields $\rightarrow \langle F \rangle$ or $\langle D \rangle$

if SUSY global \rightarrow Spont SUSY \rightarrow ~~GB~~ Goldstino

$$\langle 0|H|0\rangle = \frac{1}{4} \{ \underbrace{\langle 0|Q\bar{Q}|0\rangle}_{\text{norm of } Q} + \dots \} = \frac{1}{4} (\| \bar{Q} |0\rangle \|^2 + \dots) \geq 0$$

↓ if SUSY

$$\langle 0|H|0\rangle \geq 0 \rightarrow \langle 0|V|0\rangle = 0$$

no non perturbative effects instantons

chiral, vector supermultiplets

$$V = FF^* + \frac{1}{2}D^2$$

auxiliary fields $\rightarrow \langle F \rangle$ or $\langle D \rangle \neq 0$

if SUSY global \rightarrow Spont SUSY \rightarrow ~~GB~~ Goldstino

ex bosonic symm $SU(2) \rightarrow U(1) \rightarrow 2GBs$

if SUSY gauge (

$$\langle 0|H|0\rangle = \frac{1}{4} \left\{ \langle 0|Q\bar{Q}, 10\rangle + \dots \right\} = \frac{1}{4} (\| \bar{Q}, 10 \|^2 + \dots) \geq 0$$

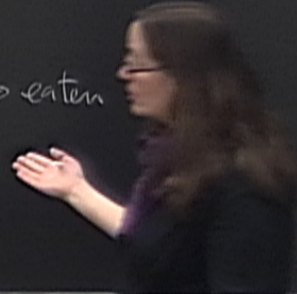
\downarrow if SUSY
 $\langle 0|H|0\rangle \geq 0 \rightarrow \langle 0|V|0\rangle = 0$
no non perturbative effects instantons

chiral, vector supermultiplets
 $V = FF^* + \frac{1}{2}D^2$
 auxiliary fields $\rightarrow \langle F \rangle$ or $\langle D \rangle \neq 0$

if SUSY global \rightarrow Spont SUSY \rightarrow ~~GB~~ Goldstino

ex bosonic symm $SU(2) \rightarrow U(1) \rightarrow 2GBs$ ^{if gauge} \rightarrow would-be GB \rightarrow eaten

if SUSY gauge (SUGRA)



$$\langle 0|H|0\rangle = \frac{1}{4} \{ \langle 0|Q\bar{Q}, 10\rangle + \dots \} = \frac{1}{4} (\| \bar{Q}, 10 \|^2 + \dots) \geq 0$$

if SUSY

$$\langle 0|H|0\rangle \geq 0 \rightarrow \langle 0|V|0\rangle = 0$$

no non perturbative effects instantons

chiral, vector supermultiplets

$$V = FF^* + \frac{1}{2}D^2$$

auxiliary fields $\rightarrow \langle F \rangle$ or $\langle D \rangle \neq 0$

if SUSY global \rightarrow Spont SUSY \rightarrow ~~GB~~ Goldstino

ex. bosonic symm $SU(2) \rightarrow U(1) \rightarrow 2GBs$ ^{if gauge} \rightarrow would-be GB \rightarrow eaten

if SUSY gauge (SUGRA) \rightarrow goldstini eaten

$$\langle 0|H|0\rangle = \frac{1}{4} \{ \langle 0|Q\bar{Q}, |0\rangle + \dots \} = \frac{1}{4} (\|Q|0\rangle\|^2 + \dots)$$

↓ if SUSY

$$\langle 0|H|0\rangle \geq 0 \rightarrow \langle 0|V|0\rangle = 0$$

no non-perturbative effects instantons

chiral, vector supermultiplet
 $V = FF^* + \frac{1}{2}D^2$
 auxiliary field

if SUSY global \rightarrow spontaneous SUSY \rightarrow goldstini

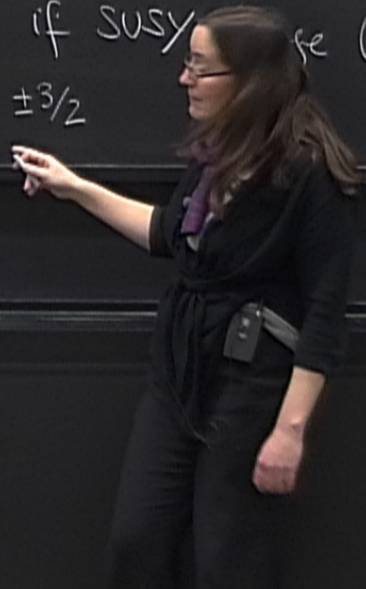
SUGRA
 graviton $s=2$
 \oplus
 gravitino $s=3/2$

ex. bosonic symm $SU(2) \rightarrow U(1) \rightarrow 2GBs$ if gauge would-be GB \rightarrow eaten

if SUSY broken (SUGRA) \rightarrow goldstini eaten by gravitino $\pm 3/2$

$\{Q, \bar{Q}\} \mathcal{N}=1$

Q_2



$\langle OTHIO \rangle \geq 0 \rightarrow \langle OIVIO \rangle \neq 0$
 no non perturbative effects instantons

auxiliary fields $\rightarrow \langle F \rangle$

if SUSY global \rightarrow Spont SUSY \rightarrow ~~GB~~ Goldstino $\pm 1/2$

ex. bosonic symm $SU(2) \rightarrow U(1) \rightarrow 2GBs$ ^{if gms} \rightarrow would be eaten

if SUSY gauge (SUGRA) \rightarrow goldstini eat gravitino $\pm 3/2$ $\pm 1/2$

SUGRA
 graviton \oplus $s=2$
 gravitino $s=3/2$

$$\langle 0|H|0\rangle \geq 0 \rightarrow \langle 0|V|0\rangle = 0$$

no non perturbative effects instantons

$$V = FF^* + \frac{1}{2}D^2$$

auxiliary fields $\rightarrow \langle F \rangle$ or $\langle D \rangle \neq 0 \rightarrow$ SUSY

if SUSY global \rightarrow Spont SUSY \rightarrow ~~GB~~ Goldstino $\pm 1/2$

SUGRA

graviton $s=2$

\oplus

gravitino $s=3/2$

ex bosonic symm $SU(2) \rightarrow U(1) \rightarrow 2GBs$ ^{if gauge} \rightarrow would be GB \rightarrow eaten

if SUSY gauge (SUGRA) \rightarrow goldstini eaten by gravitino $\pm 3/2$ $\pm 1/2$

$s=1$ massless $(\pm 1, 0)$

\uparrow Transverse \downarrow Long

$$\langle 0|H|0\rangle \geq 0 \rightarrow \langle 0|V|0\rangle = 0$$

no non perturbative effects instantons

$$V = FF^* + \frac{1}{2}D^2$$

auxiliary fields $\rightarrow \langle F \rangle$ or $\langle D \rangle \neq 0 \rightarrow$ SUSY

if SUSY global \rightarrow Spont SUSY \rightarrow ~~GB~~ goldstino $\pm 1/2$

SUGRA

graviton $s=2$

\oplus

gravitino $s=3/2$

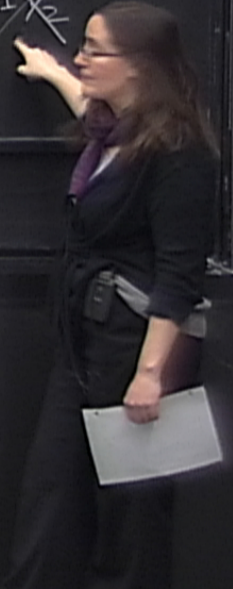
ex bosonic symm $SU(2) \rightarrow U(1) \rightarrow 2GBs$ ^{if gauge} \rightarrow would be GB \rightarrow eaten

if SUSY gauge (SUGRA) \rightarrow goldstini eaten by gravitino $\pm 3/2$ \oplus $\pm 1/2$

$s=1$ massless $(\pm 1, \cancel{0})$

\downarrow Transverse \downarrow Long

$s=3/2, \pm 3/2, \cancel{\pm 1/2}$



$$\langle 0|H|0\rangle \geq 0 \rightarrow \langle 0|V|0\rangle = 0$$

no non perturbative effects instantons

$$V = FF^* + \frac{1}{2}D^2$$

auxiliary fields $\rightarrow \langle F \rangle$ or $\langle D \rangle \neq 0 \rightarrow$ SUSY

if SUSY global \rightarrow Spont SUSY \rightarrow ~~GB~~ goldstino $\pm 1/2$

SUGRA

graviton $s=2$

\oplus

gravitino $s=3/2$

ex bosonic symm $SU(2) \rightarrow U(1) \rightarrow 2GBs$ ^{if gauge} \rightarrow would be GB \rightarrow eaten

if SUSY gauge (SUGRA) \rightarrow goldstini eaten by gravitino

$\pm 3/2$ $\oplus 1/2$ $E(x^M)$

$s=1$ massless $(\pm 1, \pm 1)$

\swarrow Trans \searrow Long

$s=3/2, \pm 3/2, \pm 1/2$

superhiggs mech \uparrow goldstini

Understand model susy @ high-E \rightarrow reduce # parameters
 UV-completion to Left
 SUSY model building

Define $\text{STr } M^2 \equiv \sum_i (-1)^{J_i} (2J_i + 1) M_i^2 C_i$

\uparrow
 supertrace

$C_i^{\text{bosons}} = \begin{cases} 1 & \text{R} \\ 2 & \text{I} \end{cases}$

$C_i^{\text{ferm}} = \begin{cases} 1 & \text{Majorana} \\ 2 & \text{Dirac} \end{cases}$

SUGRA ex
 graviton $s=2$
 \oplus
 gravitinos $s=3/2$

Understand model susy @ high-E \rightarrow reduce # parameters
 UV-completion to Left
 SUSY model building

Define $\text{STr } M^2 \equiv \sum_i (-1)^{J_i^{\text{spin}}} (2J_i + 1) M_i^2 C_i$

\uparrow
 Supertrace

$C_i^{\text{bosons}} = \begin{cases} 1 & \text{R} \\ 2 & \text{C} \end{cases}$

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SUGRA
 graviton $s=2$
 \oplus
 gravitinos $s=3/2$

after

$$\langle 0|H|0\rangle \geq 0 \rightarrow \langle 0|V|0\rangle = 0$$

no non-perturbative effects instantons

$$V = FF^* + \frac{1}{2}D^2$$

auxiliary fields $\rightarrow \langle F \rangle$ or $\langle D \rangle \neq 0 \rightarrow$ SUSY

SUGRA
 graviton $s=2$
 ⊕
 gravitino $s=3/2$

ex bosonic symm $SU(2) \rightarrow U(1)$ — 2GBs $\xrightarrow{\text{if gauge}}$ would be GB \rightarrow eaten

if SUSY gauge (SUGRA) \rightarrow goldstini eaten by gravitino
 $\pm 3/2$ $\pm 1/2$ $E(X^M)$

$S=1$ massless $(\pm 1, 0)$
 Transverse Long
 $S=3/2, \pm 3/2, \pm 1/2$
 superhiggs mech \uparrow goldstini

after a long derivation SUSY spontaneously broken

$$S \text{Tr} M^2 = 2 \frac{g^2}{\alpha} \text{Tr}(T^a) \langle D^a \rangle$$

\swarrow gauge interactions
 \searrow generators
 \leftarrow D-term

$\langle OIPI \rangle = 0 \rightarrow \langle OIPI \rangle \neq 0$
 no non perturbative effects instantons

auxiliary fields $\rightarrow \langle F \rangle$ or $\langle D \rangle \neq 0 \rightarrow$ SUSY

SUGRA
 graviton \oplus $s=2$
 gravitino $s=3/2$

ex bosonic symm $SU(2) \rightarrow U(1) \rightarrow 2GBs \xrightarrow{\text{if gauge}} \text{would-be GB} \rightarrow \text{eaten}$

if SUSY gauge (SUGRA) \rightarrow goldstini eaten by gravitino
 $\pm 3/2$ $\oplus \pm 1/2$ $\epsilon(x^M)$

$s=1$ massless (± 1)
 $s=3/2, \pm 3/2, \pm 1/2$
 superhiggs mech \uparrow goldstini

after a long derivation SUSY spontaneously broken

$$S \text{Tr} M^2 = \sum_a g_a^2 \text{Tr}(T_a) \langle D^a \rangle$$

\swarrow gauge interactions \searrow generators \nwarrow D-term

$$\langle 0|H|0\rangle \geq 0 \rightarrow \langle 0|V|0\rangle = 0$$

no non-perturbative effects instantons

current, vector supermultiplet

$$V = FF^* + \frac{1}{2}D^2$$

auxiliary fields $\rightarrow \langle F \rangle$ or $\langle D \rangle \neq 0 \rightarrow$ SUSY

- 1 Majorana
- 2 Dirac

SUGRA

ex bosonic symm $SU(2) \rightarrow U(1) \rightarrow 2GBs \xrightarrow{\text{if gauge}} \text{would be GB} \rightarrow \text{eaten}$

if SUSY gauge (SUGRA) \rightarrow goldstini eaten by gravitino

$\pm 3/2$ $\left(\pm 1/2 \right)$ $E(x^M)$

$S=1$ massless $\left(\pm 1 \right)$

$S=3/2, \pm 3/2, \pm 1/2$

superhiggs mech \uparrow goldstini

after a long derivation SUSY spont broken

SUSY $\rightarrow \text{STr } M^2 = 0$

SUSY $\langle F \rangle \neq 0 \rightarrow \text{STr } M^2 = 0$

SUSY $\langle D \rangle \neq 0 \rightarrow$

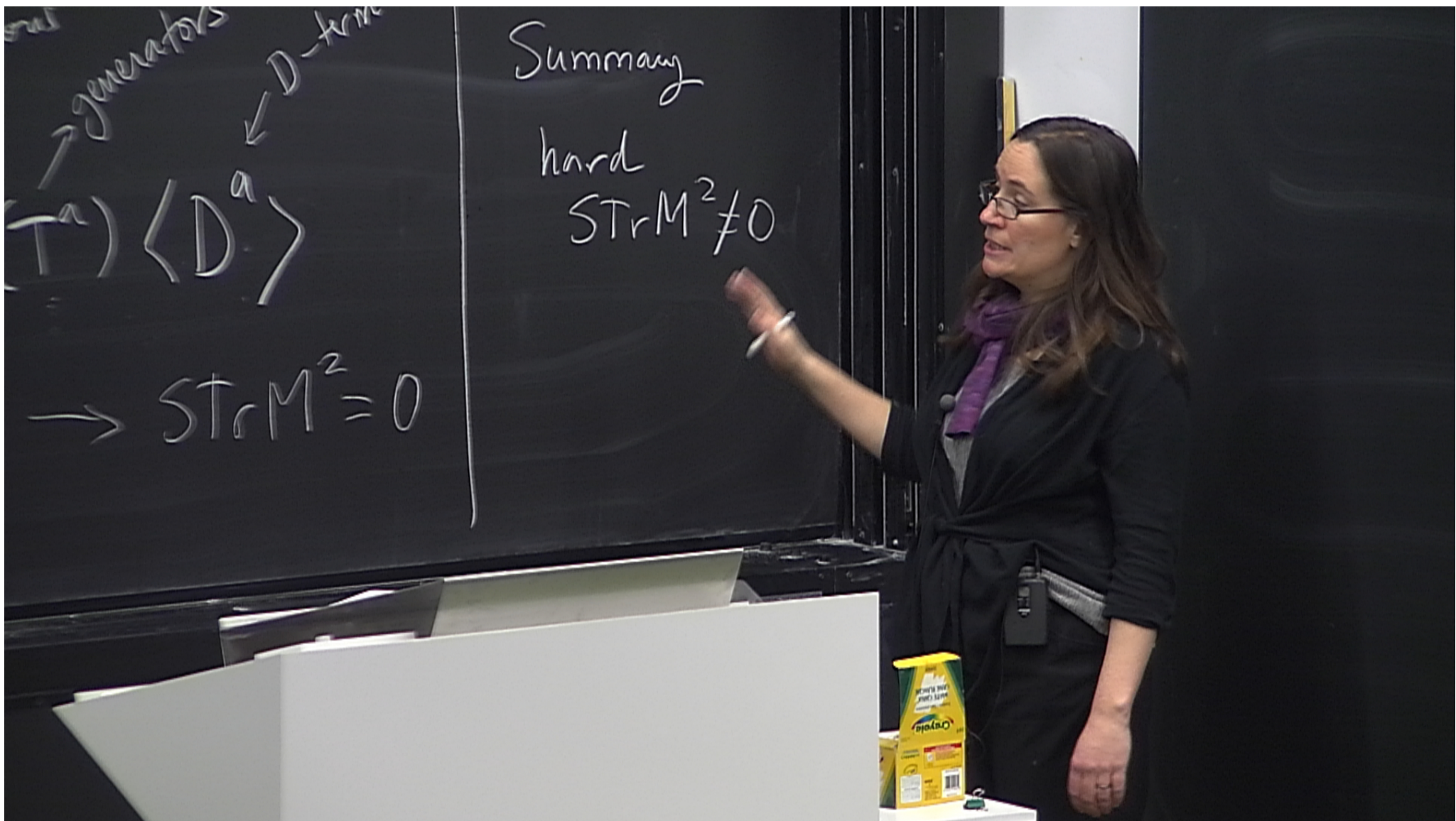
$$\text{STr } M^2 = \sum_a g_a^2 \text{Tr}(T^a) \langle D^a \rangle$$

gauge interactions \rightarrow generators $\leftarrow D$ -term

non abelian $\text{Tr}(T^a) = 0$

abelian and gauge \rightarrow anomaly cancellation $\text{Tr}(T^a) = 0$





$$\langle 0|H|0\rangle \geq 0 \rightarrow \langle 0|V|0\rangle = 0$$

no non perturbative effects instantons

$$V = FF^* + \frac{1}{2}D^2$$

auxiliary fields $\rightarrow \langle F \rangle$ or $\langle D \rangle \neq 0 \rightarrow$ SUSY

SUGRA
 graviton $s=2$
 ⊕
 gravitino $s=3/2$

ex. bosonic symm $SU(2) \rightarrow U(1)$ — 2GBS $\xrightarrow{\text{if gauge}}$ would be GB \rightarrow eaten

if SUSY gauge (SUGRA) \rightarrow goldstini eaten by gravitino
 $\pm 3/2$ (⊕ $\pm 1/2$) $\Sigma(X^M)$

$S=1$ massless (⊕ ± 1 , ⊖ ± 1)
 Trivial Long

$S=3/2$, $\pm 3/2$ (⊕ $\pm 1/2$)
 Super-Higgs mech \uparrow goldstini

after a long derivation SUSY spontaneously broken

Sum rule

$$\text{SUSY} \rightarrow \text{STr } M^2 = 0$$

$$\text{SUSY } \langle F \rangle \neq 0 \rightarrow \text{STr } M^2 = 0$$

$$\text{SUSY } \langle D \rangle \neq 0 \rightarrow \left. \begin{array}{l} \text{non abelian } \text{Tr}(T^a) = 0 \\ \text{abelian and gauge} \rightarrow \text{anomaly cancellation } \text{Tr}(T^a) = 0 \end{array} \right\} \rightarrow \text{STr } M^2 = 0$$

$$\text{STr } M^2 = \sum_a \frac{1}{a} g_a^2 \text{Tr}(T^a) \langle D^a \rangle$$

\downarrow gauge interactions \rightarrow generators \leftarrow D-term

Summary
 hard $\text{STr } M^2 \neq 0$

$$\langle 0|H|0\rangle \geq 0 \rightarrow \langle 0|V|0\rangle = 0$$

no non perturbative effects instantons

$$V = FF^* + \frac{1}{2}D^2$$

auxiliary fields $\rightarrow \langle F \rangle$ or $\langle D \rangle \neq 0 \rightarrow$ SUSY

SUGRA
 graviton $s=2$
 ⊕
 gravitino $s=3/2$

ex. bosonic symm $SU(2) \rightarrow U(1)$ — 2GBS $\xrightarrow{\text{if gauge}}$ would be GB \rightarrow eaten

if SUSY gauge (SUGRA) \rightarrow goldstini eaten by gravitino
 $\pm 3/2$ (⊕ $\pm 1/2$) $\epsilon(x^M)$

$s=1$ massless (⊕ ± 1 , ⊖ ± 1)
 Trivial Long

$s=3/2, \pm 3/2$ (⊕ $\pm 1/2$)
 super-Higgs mech \uparrow goldstini

after a long derivation SUSY spontaneously broken

Sum rule

$$\text{SUSY} \rightarrow \boxed{\text{STr } M^2 = 0}$$

$$\text{SUSY } \langle F \rangle \neq 0 \rightarrow \text{STr } M^2 = 0$$

$$\text{SUSY } \langle D \rangle \neq 0 \rightarrow \begin{matrix} \text{non abelian } \text{Tr}(T^a) \neq 0 \\ \text{abelian and gauge} \rightarrow \text{anomaly cancellation } \text{Tr}(T^a) = 0 \end{matrix} \left. \vphantom{\begin{matrix} \text{non abelian } \text{Tr}(T^a) \neq 0 \\ \text{abelian and gauge} \rightarrow \text{anomaly cancellation } \text{Tr}(T^a) = 0 \end{matrix}} \right\} \rightarrow \text{STr } M^2 = 0$$

$$\text{STr } M^2 = \sum_a g_a^2 \text{Tr}(T^a) \langle D^a \rangle$$

\downarrow gauge interactions \rightarrow generators \leftarrow D-term

Summary

hard $\text{STr } M^2 \neq 0$

problem

$$\text{STr} M^2 = 0$$

← everybody

⊕ conservation e.g. L_e

$$\text{STr} M^2 = 0 \rightarrow m_{e_L}^2 + \tilde{m}_{e_R}^2 + m_{\nu}^2 = 2m_e^2$$

$$C_i = \left. \begin{matrix} \\ \\ \end{matrix} \right\} \mathbb{C} \quad C_i = \left. \begin{matrix} \\ \\ \end{matrix} \right\} \mathbb{Z} \text{ Dirac}$$

problem $\text{STr} M^2 = 0$ \oplus conservation e.g. L_e
 ← everybody
 (scalars)²

$$\text{STr} M^2 = 0 \rightarrow m_{\tilde{e}_L}^2 + \tilde{m}_{eR}^2 + m_{\tilde{\nu}_\tau}^2 = 2 m_e^2$$

Define $\text{STr } M^2 \equiv \sum_i (-1)^{J_i^{\text{spin}}} (2J_i + 1) M_i^2$ C_i

↑
supertrace

$$C_i^{\text{bosons}} = \begin{cases} 1 & \mathbb{R} \\ 2 & \mathbb{C} \end{cases} \quad C_i^{\text{ferm}} = \begin{cases} 1 & \text{Majorana} \\ 2 & \text{Dirac} \end{cases}$$

problem $\text{STr } M^2 = 0$ \oplus conservation of L_e
← everybody

$$(\text{scalars})^2 - (\text{fermions})^2 = 0$$

$$\text{STr } M^2 = 0 \rightarrow m_{eL}^2 + \tilde{m}_{eR}^2 + m_{\nu}^2 = 2m_e^2$$

↑
Supertrace

$$C_i^{\text{bosons}} = \begin{cases} 1 & \text{IR} \\ 2 & \text{F} \end{cases}$$

$$C_i^{\text{ferm}} = \begin{cases} 1 & \text{Majorana} \\ 2 & \text{Dirac} \end{cases}$$

problem

$$\text{STr} M^2 = 0$$

← everybody

⊕ conservation e.g. L_e

$$(\text{scalars})^2 - (\text{fermions})^2 = 0$$

$$\text{STr} M^2 = 0 \rightarrow$$

$$m_{\tilde{e}_L}^2 + \underbrace{\tilde{m}_{\tilde{e}_R}^2 + m_{\tilde{\nu}}^2}_{\text{+ extra contrib}} = 2 m_e^2$$

only MSSM

graviton
 \oplus $s=2$
gravitino
 $s=3/2$

if SUSY gauge (SUGRA) \rightarrow goldstini eaten

add a new sector to the MSSM

- ① $\text{Str } M^2$ tree level statement
- ② $\text{Str } M^2$

if SUSY gauge (SUGRA) \rightarrow goldstini eaten by gravitino
2GBS \rightarrow would be GB \rightarrow eaten

add a new sector to the MSSM

- ① $\text{Str} M^2 = 0$ tree level statement
- ② $\text{Str} M^2 = (\text{bosons})^2 - (\text{fermions})^2$, masses of $\dots \leq$ SUSY partner

tree level statement

$$(\text{bosons})^2 - (\text{fermions})^2$$

$$\tilde{H}, \lambda$$

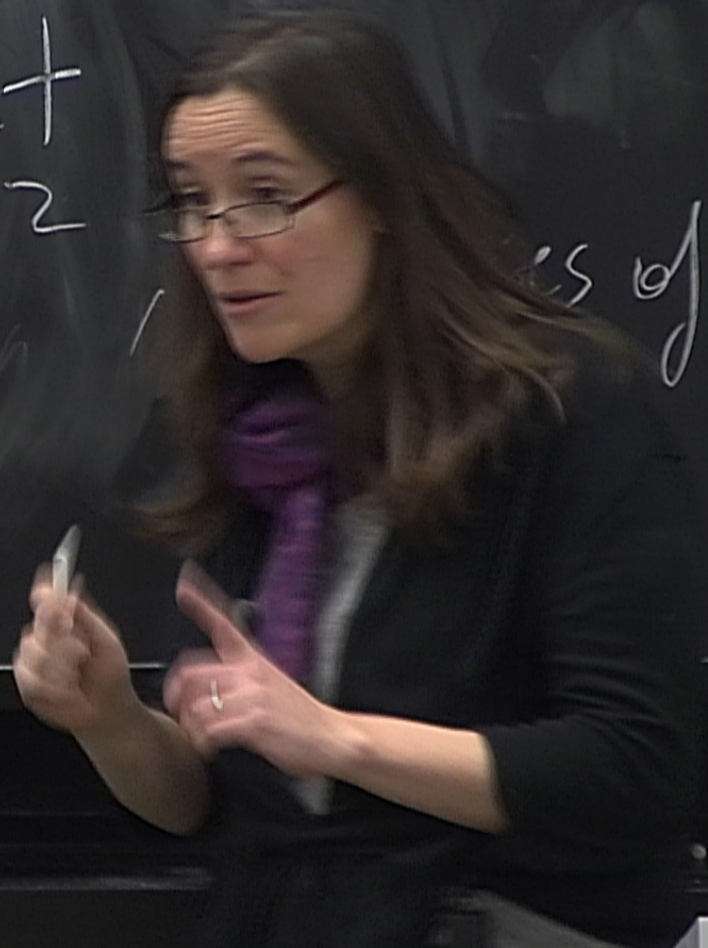
all S

tree level statement

$$(bosons)^2 - (fermions)^2$$

$$\tilde{H}, \lambda$$

es of all S



tree level statement

$$(bosons)^2 - (fermions)^2$$

$$\tilde{H}, \lambda$$

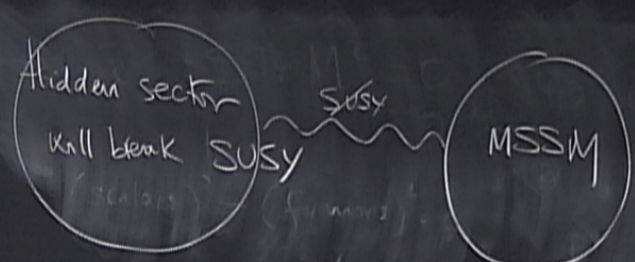
masses of all S

Supertrace

1

$$C_i^{\text{bosons}} = \begin{cases} 1 & \text{IR} \\ 2 & \text{D} \end{cases}$$

$$C_i^{\text{ferm}} = \begin{cases} 1 & \text{Majorana} \\ 2 & \text{Dirac} \end{cases}$$



variation e.g. L_e

$$\text{Tr} M^2 = 0 \rightarrow m_{\tilde{e}_L}^2 + \tilde{m}_{e_R}^2 + m_{\nu}^2 = 2m_e^2 + \text{extra constants}$$

only MSSM

- ① $\text{Str} M^2 = 0$ tree level statement
- ② $\text{Str} M^2 = (\text{bosons})^2 - (\text{fermions})^2$,
 \tilde{q}, \tilde{e} \tilde{H}, λ

masses of all SM \ll SUSY partners \rightarrow expect $\text{Str} M^2 > 0$

SUSY model

- ① content hidden sector
- ② mediation SUSY to MSSM sector

SUSY parameter $\langle \lambda \lambda \rangle \neq 0$
 Γ, D , gaugino mediation

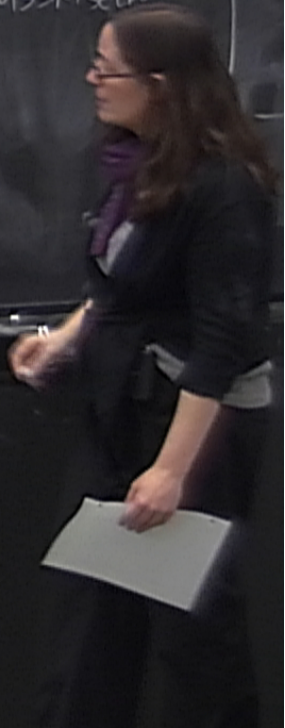
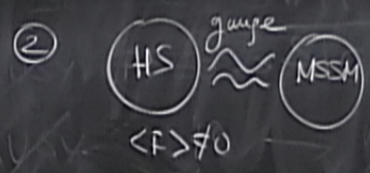
fem = $\left\{ \begin{array}{l} 1 \text{ Majorana} \\ 2 \text{ Dirac} \end{array} \right.$

② $\text{Tr} M^2 = (\text{bosons})^2 - (\text{fermions})^2$, masses of all SM
 \tilde{q}, \tilde{e} \tilde{H}, λ

MSSM
 $\sum_R^2 + m_{\tilde{\nu}}^2 = \sum m_e^2 + \text{extra}$
 trace contrib

for SUSY model

- ① content hidden sector
- ② mediation SUSY to MSSM sector
- ③ gaugino med



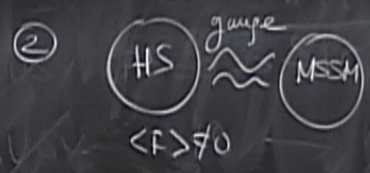
fem = {
 1 Majorana
 2 Dirac

② $\text{Tr} M^2 = (\text{bosons})^2 - (\text{fermions})^2$, masses of all SM
 $\tilde{g}, \tilde{e}, \tilde{H}, \lambda$

MSSM
 $\sum_R + m_{\tilde{\nu}}^2 = \sum_L m_e^2 + \text{extra}$
 trace constant

for SUSY model

- ① content hidden sector
- ② mediation SUSY to MSSM sector
- ③ gaugino med $\langle \lambda \lambda \rangle \neq 0$

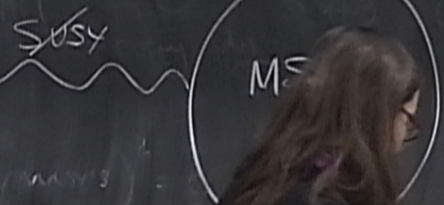


Super trace

$$C_i^{\text{bosons}} = \begin{cases} 1 & \mathbb{R} \\ 2 & \mathbb{C} \end{cases}$$

$$C_i^{\text{ferm}} = \begin{cases} 1 & \text{Majorana} \\ 2 & \text{Dirac} \end{cases}$$

den sector
|| break SUSY
(scalars)



① $\frac{1}{M_{\text{pl}}}$ SUGRA

② med gauge $\frac{g^2}{16\pi^2}$ GMSB

③ $\langle \lambda \lambda \rangle \neq 0$

Supertrace

$$C_i^{\text{bosons}} = \begin{cases} 1 & \text{IR} \\ 2 & \text{E} \end{cases}$$

$$C_i^{\text{ferm}} = \begin{cases} 1 & \text{Majorana} \\ 2 & \text{Dirac} \end{cases}$$

den sector
11 brak SU
(scalars)

usy

MSSM

① $\frac{1}{M_{pl}}$ SUGRA

② med gauge $\frac{g^2}{16\pi^2}$ GMSB

③ $\langle \lambda \lambda \rangle \neq 0$ $\frac{1}{M_{pl}}$ \tilde{g} MSB

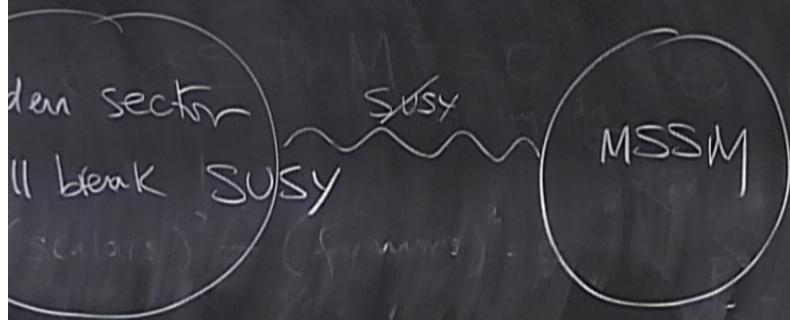
④ Anomaly med

= 21

Super trace

$$C_i^{\text{bosons}} = \begin{cases} 1 & \text{IR} \\ 2 & \text{F} \end{cases}$$

$$C_i^{\text{ferm}} = \begin{cases} 1 & \text{Majorana} \\ 2 & \text{Dirac} \end{cases}$$

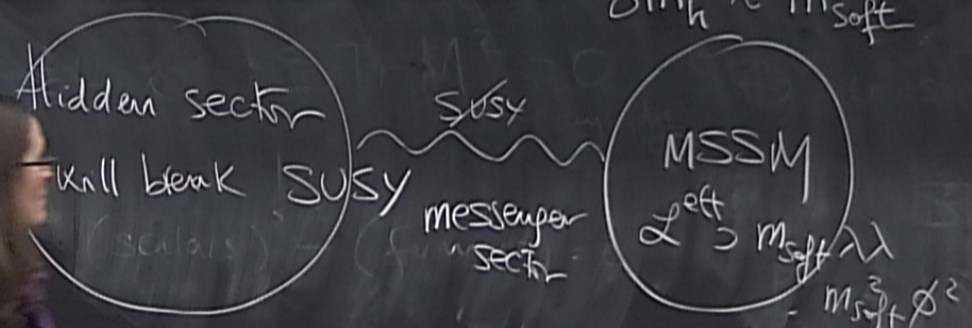


- ① $\frac{1}{M_{\text{pl}}}$ SUGRA
- ② med gauge $\frac{g^2}{16\pi^2}$ GMSB
- ③ $\langle \lambda \lambda \rangle \neq 0$ $\frac{1}{M_{\text{pl}}}$ \tilde{g} MSB
- ④ Anomaly med extra dims

Supertrace

$$C_i^{\text{bosons}} = \begin{cases} 1 & \mathbb{R} \\ 2 & \mathbb{C} \end{cases}$$

$$\Delta M_h^2 \sim M_{\text{soft}}^2$$



- ① $\frac{1}{M_{\text{pl}}}$ SUGRA
- ② med gauge $\frac{g^2}{16\pi^2}$
- ③ $\langle \lambda \lambda \rangle \neq 0$ $\frac{1}{M_{\text{pl}}}$
- ④ Anomaly med extra dim \rightarrow superconform