

Title: Beyond the Standard Model (Review) - Lecture 4

Date: Feb 16, 2012 09:00 AM

URL: <http://pirsa.org/12020067>

Abstract:

Breaking

① explicit

② spontaneous

# Breaking

$$L = L_{\text{sym}} + L_{\text{sym}}$$

① explicit  $\nearrow$  approximate  $L_{\text{sym}}$  is a perturbation

② Spontaneous

approximate  $\mathcal{L}_{\text{sym}}$  is a perturbation of  $\mathcal{L}_{\text{sym}}$   $\mathcal{L}_{\text{sym}} = m_f \hat{q} \hat{q}$



approximate  $\mathcal{L}_{\text{sym}}$  is a perturbation of  $\mathcal{L}_{\text{sym}}$   $\mathcal{L}_{\text{sym}} = m_f \bar{\psi} \psi$

accidental  $\mathcal{L}_{\text{SM}} = \mathcal{L}_{\text{QED}} + \mathcal{L}_{\text{weak}}$   
CP CP

SSB → global  
→ local

Goldstone Theorem: one massless dof per br  
continuous }  
global }

Goldstone Theorem: one massless dof per broken generator  
continuous }  
global }

Goldstone Theorem: one massless dof per broken generator

continuous }  
global }

-example QCD  $N_f$  massless flavors

Goldstone Theorem: one massless dof per broken generator

continuous }  
global }

-example QCD  $N_f$  massless flavors

chiral  
symm

$SU(N_f)_L \times S$

Goldstone Theorem: one massless dof per broken generator

continuous }  
global }

-example QCD  $N_f$  massless flavors

chiral  
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$SU(N_f)_L \times SU(N_f)_R$

Goldstone Theorem: one massless dof per broken generator

continuous }  
global }

-example QCD  $N_f$  massless flavors

chiral  
symm

$SU(N_f)_L \times SU(N_f)_R$

4

one massless dof per broken generator

-example QCD  $N_f$  massless flavors

chiral  
symm

$SU(N_f)_L \times SU(N_f)_R$

$$\psi_i^{L,R} \rightarrow e^{i\theta^a T^a} \psi_i^{L,R}$$

$$\theta = \theta^a T^a$$

Theorem: one massless dof per broken generator

conserved }  
label }

-example QCD  $N_f$  massless flavors

chiral  
symm  $SU(N_f)_L \times SU(N_f)_R$

$$\langle \bar{u}u + \bar{d}d \rangle \neq 0$$

$$\psi_i^{L,R} \rightarrow e^{i\theta^{L,R}} \psi_i^{L,R}$$

$$\theta = \theta_{L,R}^a T^a$$

Theorem: one massless dof per broken generator

conserved }  
abel

-example QCD  $N_f$  massless flavors

$\bar{\psi}\psi$

chiral  
symm

$SU(N_f)_L \times SU(N_f)_R$

$\langle \bar{u}u + \bar{d}d \rangle \neq 0$

$\rightarrow SU(N_f)_V$

$V \rightarrow$

$$\psi_i^{L,R} \rightarrow e^{i\theta^{L,R}} \psi_i^{L,R}$$

$$\theta = \theta_{L,R}^a T^a$$

Theorem: one massless dof per broken generator

$$\psi_i^{L,R} \rightarrow e^{i\theta^{L,R}} \psi_i^{L,R}$$

flavors }  
global }

-example QCD  $N_f$  massless flavors

$$\theta = \theta_{L,R}^a T_{L,R}^a$$

$\bar{\psi}\psi$

chiral  
symm

$$SU(N_f)_L \times SU(N_f)_R$$

$$\langle \bar{u}u + \bar{d}d \rangle \neq 0$$

$$\rightarrow SU(N_f)_V$$

$$V = L + R$$

# of generators  $SU(N) \rightarrow N^2 - 1$

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$$\text{broken generators} = 2 \cdot (N_f^2 - 1) - (N_f^2 - 1) = N_f^2 - 1$$

u, d, s  $N_f = 3$  # Goldstone bosons = 8

u, d  $N_f = 2$  # GB =

# of generators  $SU(N) \rightarrow N^2 - 1$

$$\text{broken generators} = 2 \cdot (N_f^2 - 1) - (N_f^2 - 1) = N_f^2 - 1$$

u, d, s  $N_f = 3$  # Goldstone bosons = 8

u, d  $N_f = 2$  # GB = 3

$$\rightarrow N^2 - 1$$

$$(N_f^2 - 1) = N_f^2 - 1$$

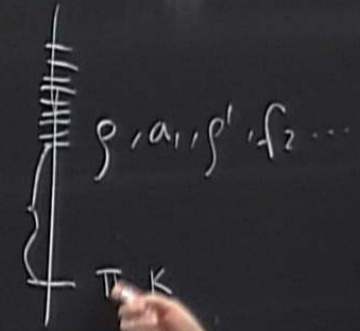
# Goldstone bosons = 8

# GB = 3

QCD

perturbative  $q, \bar{q}, g$

mesons, baryons

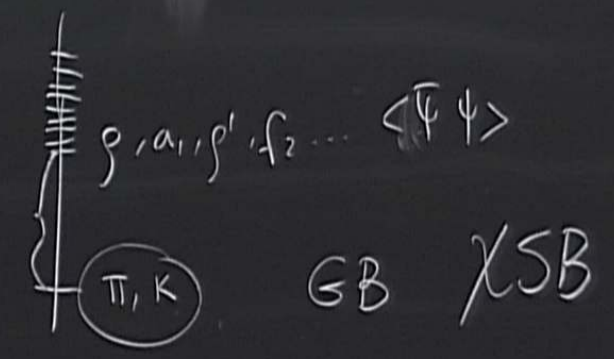


$24$   
 the bosons = 8 + K's  
 = 3  $(\pi^0, \pi^+, \pi^-)$

QCD

perturbative  $g, \bar{q}, q$

mesons, baryons



SB  $\rightarrow$  global  
 $\rightarrow$  local

Goldstone Theorem: one massless dof per broken ge

continuous }  
 global }

-example QCD  $N_f$  massless



$\bar{\psi}\psi$

chiral symm SUCN

$\langle \bar{u}u + \bar{d}d \rangle \neq 0$

u, d  $N_F = 2$  # GB = 3  $\pi^0, \pi^+, \pi^-$

global  $\rightarrow$  approximate global

$m = 0$  GB  $\rightarrow$   $m \neq 0$  PGB

$m_{\text{PGB}} \ll m_{\text{sector}}$

u,d  $N_F = 2$  # GB = 3  $(\pi^0, \pi^+, \pi^-)$

global  $\rightarrow$  approximate global  $m_{u,d,s} \neq 0$

$m=0$  GB  $\rightarrow$   $m \neq 0$  PGB  
 $m_{PGB} \ll m_{sector}$

$m \bar{u} u$

$GB = 3 \quad (\pi^0, \pi^+, \pi^-)$

$\{ \pi, K \} \quad GB \quad \chi SB$

$m_{u.d.s} \neq 0$

$m_u \bar{u}_L u_R$   
 $SU(2)_L \quad 2 \quad 1$

~~$\mathcal{L} \supset m \bar{u}_L u_R$~~

$U(1)$

sector

$\pi^+, \pi^0, \pi^-$

$\pi, K$  GB  $\chi$ SB

$m_u \bar{u}_L u_R$   
 $SU(2)_L$  2 1

~~$\mathcal{L} \supset m \bar{u}_L u_R$~~

$y \bar{u}_L H u_R$  singlet  $SU(2)_L$   
 $\rightarrow \begin{pmatrix} y_u \\ y_d \end{pmatrix} \bar{u}_L u_R$

u,d  $N_f = 2$  # GB = 3  $(\pi^0, \pi^+, \pi^-)$

global  $\rightarrow$  approximate global

$m_{u,d,s} \neq 0$

$m_u \bar{u}_L u_R$   
 $SU(2)_L$       2      1

$m=0$  GB  $\rightarrow$   $m \neq 0$  PGB

$m_{PGB} \ll m_{sector}$

$m_{u,d,s} \ll m_c, m_t, m_b$

u,d  $N_f = 2$  # GB = 3  $(\pi^0, \pi^+, \pi^-)$

global  $\rightarrow$  approximate global

$m_{u,d,s} \neq 0$

GB  $\rightarrow m \neq 0$  PGB

$m_{\text{PGB}} \ll m_{\text{sector}}$

$< m_c, m_t, m_b$

$m_u \bar{u}_L u_R$   
 $SU(2)_L$       2      1

+  $\rho$  1370 MeV  
-  $\pi, K$

$W, Z$  massless spin 1 dof

$W, Z$

massless spin 1

dof 2

massive

//

//

3 = 2 transv + 1 longitud

$W, Z$	massless	spin 1	dof	2
	massive	"	"	3 = 2 transv + <span style="border: 1px solid black; padding: 2px;">1 longitud</span>
$SU(2)_L \times U(1)_Y \rightarrow U(1)_{em}$			3 GB	would-be GB $\rightarrow$ ea

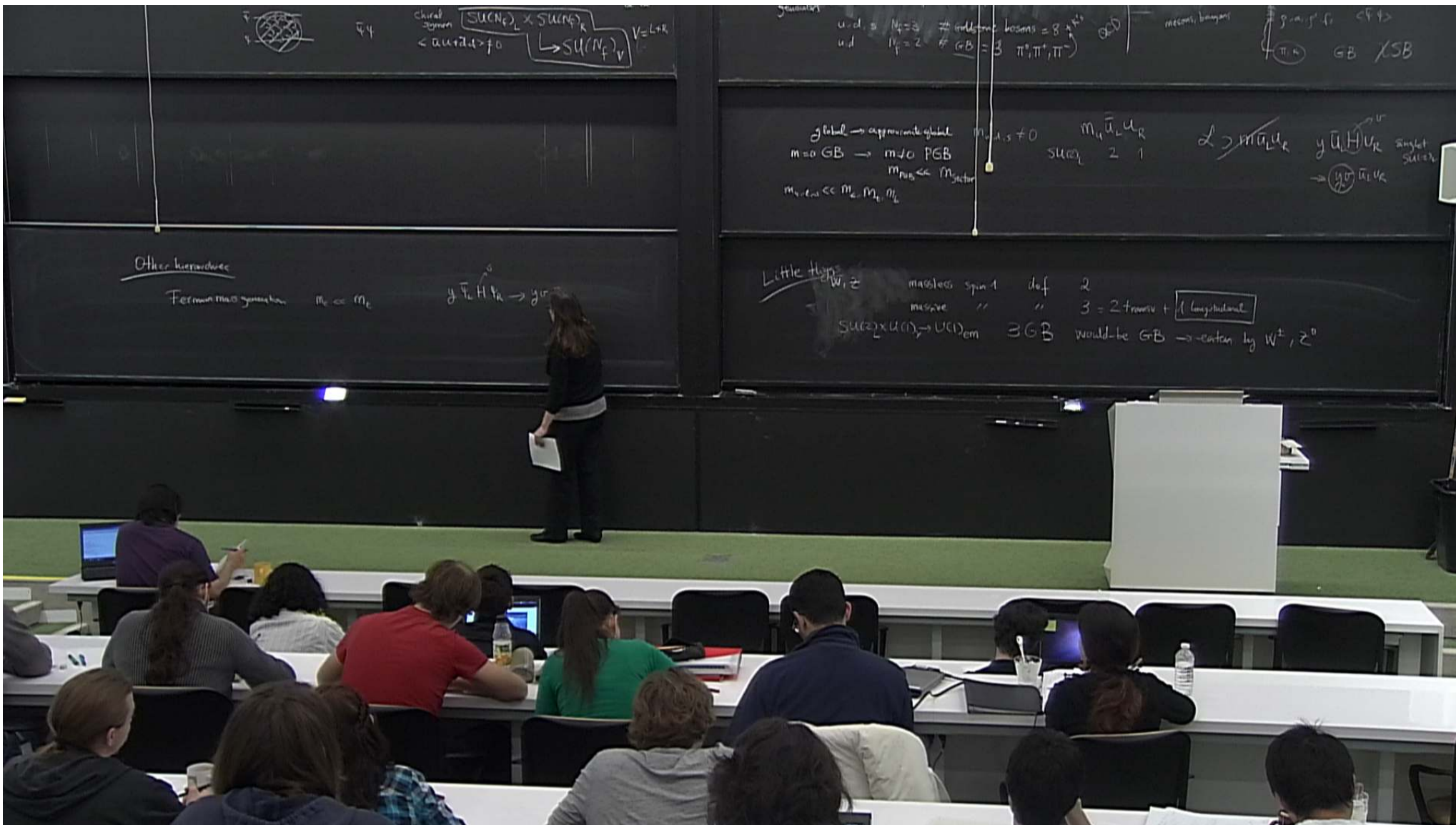
Spin 1	dof	2	
"	"	3	= 2 transv + 1 longitudinal
em	3 GB		would-be GB $\rightarrow$ eaten by $\gamma^\pm, Z^0$

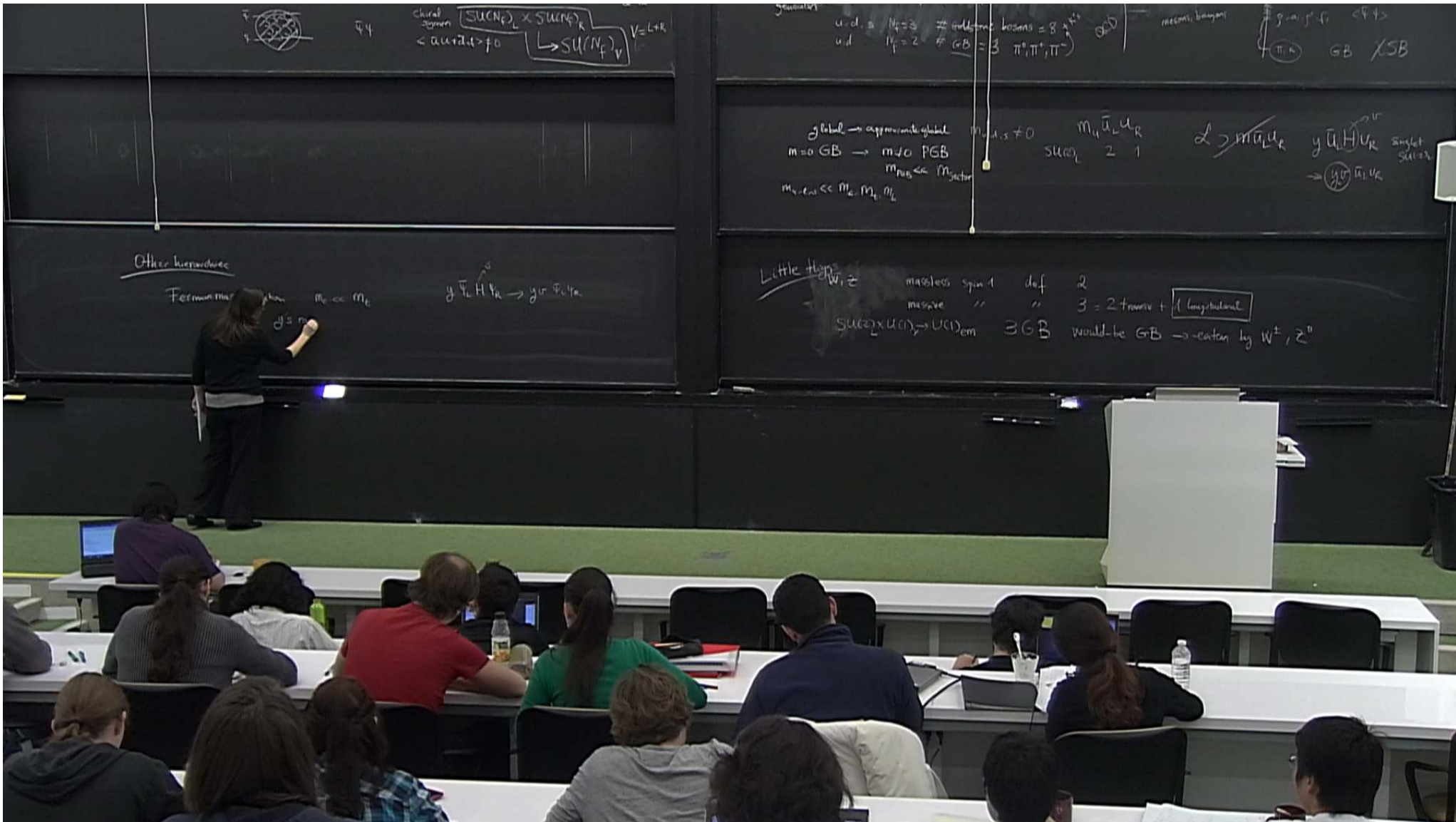


Spin 1	dof	2	
//	//	3 = 2 transv +	1 longitudinal
em	3 GB	would-be GB $\rightarrow$ eaten by $W^\pm, Z^0$	



Spin 1	dof	2
//	//	3 = 2 transv + 1 longitudinal
em	3 GB	would-be GB $\rightarrow$ eaten by $W^\pm, Z^0$





$$m_e \ll m_t$$

range many orders of magnitude

natural?  $\mathcal{L}_{tree} \supset y_e y_t$

$$y \bar{\Psi}_L H \Psi_R \xrightarrow{\sigma} y_U \bar{\Psi}_L \Psi_R$$

stable under rad. corrections?

$$m_e \ll m_t$$

change many orders of magnitude  
L tree  $\supset y_e y_t$

$$y \bar{\Psi}_L H \Psi_R \rightarrow y \nu \bar{\Psi}_L \Psi_R$$

$$\delta m_f \propto m_f$$

Stable under rad. corrections?

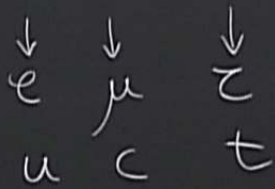
Symms global acts different way families  $\rightarrow$  Horizontal symm

$\downarrow$   $\downarrow$   $\downarrow$   
e  $\mu$   $\tau$   
u c t

Froggat-Nielsen mechanism

$y \bar{\Psi}_L + \Psi_R$

Symms global acts different way families  $\rightarrow$  Horizontal symms



Froggat-Nielsen mechanism

$$y \bar{\Psi}_L + \Psi_R \begin{pmatrix} \Phi \\ 1 \end{pmatrix}$$



acts different way families  $\rightarrow$  Horizontal symm

$\downarrow$   $\downarrow$   
 $\mu$   $\tau$   
 $c$   $t$

sees mechanism

$$y \bar{\Psi}_L + H \Psi_R \left( \begin{array}{c} \langle \bar{\Phi} \rangle \\ \Lambda \end{array} \right) \textcircled{c}$$

$\rightarrow$  # depends on family

$S=1$  gauge

$S=1/2$  chiral

$S=0$

??



$$\Delta m^2 \propto \Lambda_{NP}^2$$

gives different way

$$\Delta m^2 \propto \Lambda_{NP}^2 \rightarrow \text{Higgs heavy}$$

PEWT

→ Higgs heavy

PEWT

$$m_h \lesssim 130 \text{ GeV}$$

direct searches

$$m_h \gtrsim 115 \text{ GeV}$$

LHC

' "

$$m_h \lesssim 140 \text{ GeV}$$

Higgs  
is light

may out Desert

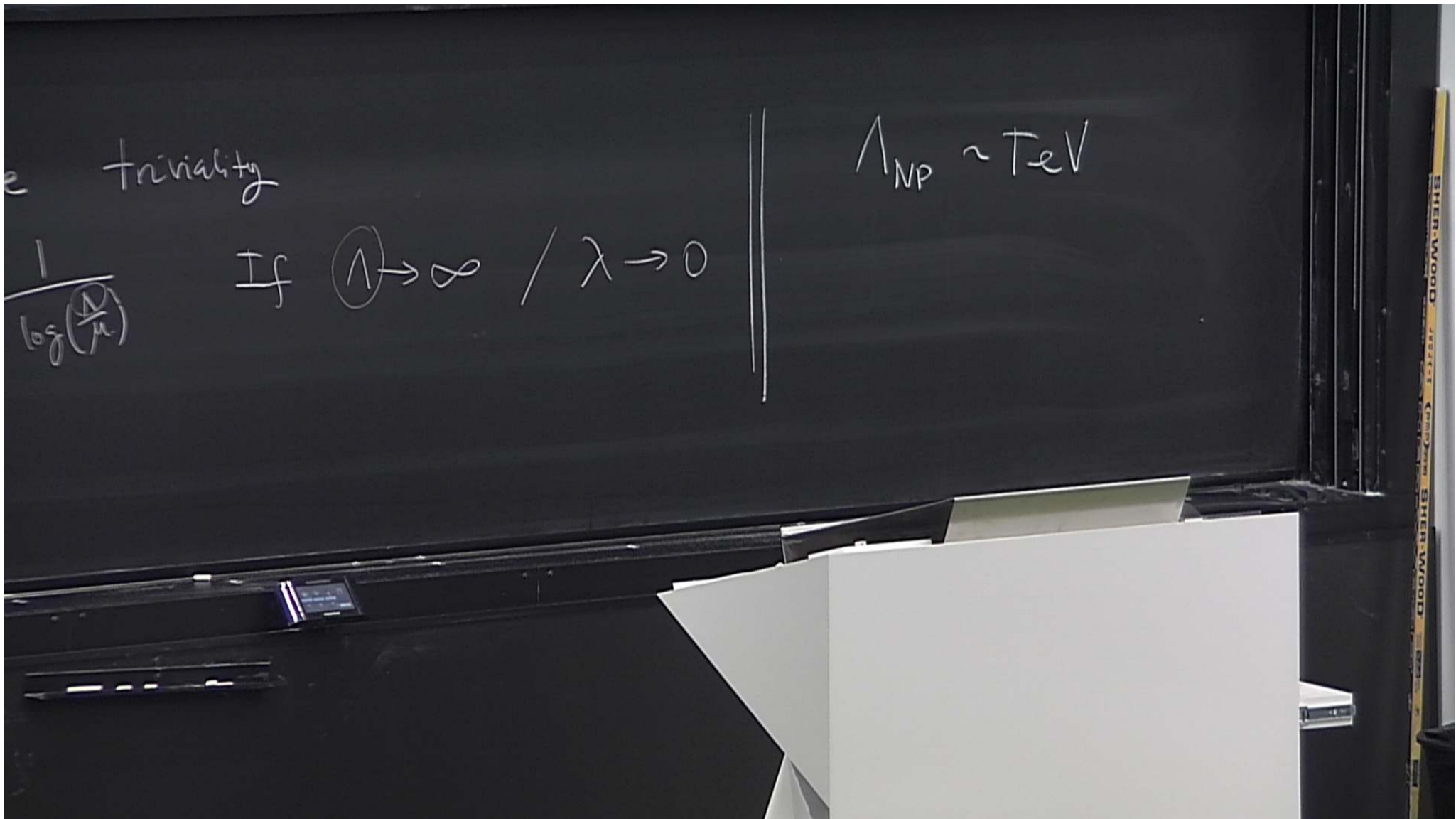
not possible triviality

$$m^2 h^2 + \lambda h^4$$

$v \neq 0$   $\nearrow$

$$\lambda(\mu) \stackrel{(\ominus)}{\approx} \frac{1}{\log\left(\frac{\Lambda}{\mu}\right)}$$

If  $\Lambda \rightarrow \infty$  /  $\lambda \rightarrow 0$



e triviality

$$\frac{1}{\log(\frac{\Lambda}{\mu})}$$

If  $\Lambda \rightarrow \infty$  /  $\lambda \rightarrow 0$

$$\Lambda_{NP} \sim TeV$$

$S=1$  gauge

$S=1/2$  chiral

$S=0$

??  
0

→

$$\Delta m^2 \propto \Lambda_{NP}^2$$

→

Higgs heavy

PE  
dire  
LHC

No Higgs  $\rightarrow$  Technicolor

Dimensional transmuta

chricolor

Dimensional transmutati

Scale inv  
Class



b

$$\Lambda_{\text{QCD}} \sim \mu / g_{\text{QCD}}(\mu) \sim \mathcal{O}(1)$$

$$\Lambda_{\text{NP}} \sim \text{TeV}$$

$$\Lambda_{\text{QCD}} \sim \mu / g_{\text{QCD}}(\mu) \sim \mathcal{O}(1)$$