

Title: Decoupling the Gravity Multiplet from Supergravity

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Abstract: The full machinery of supergravity (SUGRA) is required to fully understand many supersymmetric models. For the purpose of understanding phenomenology at colliders and in cosmology, the main concern is to ascertain the effects of SUGRA on the vacuum structure and particle spectrum. Practical calculations often require cumbersome manipulations of component field terms involving the full gravity multiplet. In this talk I will present an alternative gauge fixing for conformal SUGRA which decouples these gravity complications from SUGRA computations. This yields a simplified tree-level action for the matter fields in SUGRA which can be expressed compactly in terms of superfields and a modified conformal compensator. As a concrete application I will finally show the example of the mass spectrum of goldstini arising from a general admixture of F-term, D-term, and almost no-scale supersymmetry breaking.

SIMPLIFIED FRAMEWORK  
FOR SUGRA  
CALCULATIONS

$$\mathcal{L}_{EH} = -$$



adding a comp

$$\mathcal{L} = -\frac{1}{R}$$

# DECOUPLING THE GRAVITY MULTIPLY FROM SUPERGRAVITY

Based on:

Chung, FDE, Thaler

2600



## Motivation

Global SUSY  $\rightarrow$  superspace  $x^\mu, \theta_\alpha$

Gravity SUGRA  $\rightarrow$  superspace picture complicated

# DECOUPLING THE GRAVITY MULTIPLY FROM SUPERGRAVITY

Based on:

Cheng, FDE, Thaler

1104.2538, 1104.2600

SIMPLIFIED FRAMEWORK  
FOR SUGRA  
CALCULATIONS

Kaku et al ( $\sim 1978$ )

Bianchi SUGRA  $\implies$  gauge fixing of  
conformal SUGRA

$$\mathcal{L}_{EH} = -\frac{1}{2} R$$

no-scale invariant  
 $g_{\mu\nu} \rightarrow e^{-2\lambda(x)} g_{\mu\nu}$

$$\mathcal{L}_{EH} = -\frac{1}{2} R$$



adding a compensator field  $\varphi$

$$\mathcal{L} = -\frac{1}{2} R \varphi^2 + (\partial_\mu \varphi)^2$$

$\eta$ -scale invariant  
 $g_{\mu\nu} \rightarrow e^{-2\lambda(x)} g_{\mu\nu}$



$$\chi_{EH} = -\frac{1}{2}$$



adding a compensator field  $\varphi$

$$\mathcal{L} = -\frac{1}{12} R \varphi^2 + (\partial_\mu \varphi)^2$$

$$g_{\mu\nu} \rightarrow e^{-2\lambda(x)} g_{\mu\nu}$$

$$\varphi \rightarrow e^{\lambda(x)} \varphi \quad \text{G.F.} \quad \varphi = \sqrt{6}$$

Kaku et al ( $\sim 1978$ )

Binaria SUGRA  $\implies$  gauge fixing of  
conformal SUGRA

Extra symmetries:

- \* dilatation  $\hat{D}$
- \* dual rotation  $\hat{A}$
- \* conformal SUSY  $\hat{S}$
- \* special conf.  $K_n$

$\alpha = \frac{1}{12} \kappa^2 + (\partial_\mu \varphi)$

Kaku et al (~1978)

Binaria SUGRA  $\implies$  gauge fixing of  
conformal SUGRA

Extra symmetries:

- \* dilatation  $\hat{D}$
- \* dual rotation  $\hat{A}$
- \* conformal SUSY  $\hat{S}$
- \* special conf.  $K_\mu$

+

conformal  
compensator

$\Phi$

$$\mathcal{L} = -3 \int d^4x e^{-K/3} \Phi^\dagger \bar{\Phi} + \int d^2\theta \Phi^3 W + \frac{1}{4} \int d^4x F_{ab} W^{ab} + h.c.$$

+ ...

Example

$$L = \dots$$

$$\mathcal{L} = -3 \int d^4x e^{-K/3} \Phi^\dagger \Phi + \int d^2\theta \Phi^3 W + \frac{1}{4} \int d^4x F_{ab} W^{\dot{a}b} W_{ab} + h.c.$$

+  
o o o o o

Kugo &  
Vasiliev  
NPB 226 (1983)

$$\mathcal{L} = -3 \int d^4 \theta e^{-K/3} \Phi^\dagger \Phi + \int d^2 \theta \Phi^3 W + \frac{1}{4} \int d^4 \theta F_{ab} W^{ab} W_{ab} + h.c.$$

⊙: global susy  
superspace

⊙⊙⊙⊙ = graviton  
gravitino  
auxiliary fields

Kugo &  
Uehara  
NPB 226 (1983)

$$\underline{\Phi} = \{ \sigma, \sigma \mathcal{G}_2, \sigma F_\phi \} :$$

$$\hat{D}, \hat{A} : \sigma \rightarrow e^\lambda \sigma$$

$$\hat{S} : \mathcal{G}_2 \rightarrow \mathcal{G}_2 - \mathcal{K}_2$$

$$\lambda \in \mathcal{F} \implies \sigma \text{ and } \mathcal{G}_2$$

one  
PURE GAUGE  
MODE

\* special conf.  $K_M$

$$\sigma = 1$$
$$g_2 = 0$$

$\Rightarrow$

$$\boxed{\Phi = 1 + \sigma^2 F_\phi}$$



$$\bar{\rho} = 1 + \sigma^2 F_p$$

00000 : 1)  $\frac{C}{3} \frac{R}{2}$   $C$  scalar function of matter fields

$$\langle C \rangle = -3$$

$$\langle C_L \rangle = \langle C_T \rangle = 0$$

$$\bar{\mathcal{L}} = 1 + \mathcal{O}^2 F_p$$

00000 : 1)  $\frac{C}{3} \frac{R}{2}$   $C$  scalar function of matter fields

$$\langle C \rangle = -3 \implies \text{RS gravitino } \checkmark$$

$$\langle C_+ \rangle = \langle C_- \rangle = 0$$

---

2)  $i \sum \sigma^{\mu\nu} \partial_\nu \Psi_\mu$

$\sum_\alpha$  fermionic function of matter fields

$$1) \quad \frac{C}{3} \quad \frac{R}{2}$$

$C$  scalar function of matter fields

$$\langle C \rangle = -3 \implies \text{Dirac quantization}$$

$$\langle C_1 \rangle = \langle C_2 \rangle =$$

$$2) \quad i \sum_{\alpha} \sigma^{\mu\nu} \partial_{\nu} \Psi_{\mu}$$

$\sum_{\alpha}$  fermions

matter fields

$$3) \quad Z^+ \Psi^{\mu} J_{\mu\nu} \Psi^{\nu}$$



$$\bar{\Phi} = 1 + \mathcal{O}^2 F_p$$

$$00000 : 1) \frac{C}{3} \frac{R}{2} \quad C \text{ scalar function of matter fields}$$

$$\langle C \rangle = -3 \implies \text{RS gravitons } \checkmark$$

$$\langle C_1 \rangle = \langle C_2 \rangle = 0$$

$$\langle K_i \rangle \chi^i$$

$$2) i \sum \sigma^{\mu\nu} \partial_\nu \Psi_\mu$$

$\sum_\alpha$  fermionic function of matter fields

$$3) z^+ \Psi^\mu \sigma_{\mu\nu} \Psi^\nu$$

$$\text{Arg}(z) = 0$$

\* special conf.  $K_M$

KV gauge

NPB 222  
(1983)

$$C = -3$$

$$\xi = 0$$

$$\text{Avg}(\varepsilon) = 0$$

to all orders in the fields

\* special conf.  $K_M$

(150)

$$C = -3$$

$$\xi = 0$$

$$\text{Avg}(\varepsilon) = 0$$

to all orders in the fields

Decouples: graviton  
gravitino

\* special conf.  $K_{\mu}$

(150)

$$C = -3$$

$$\xi = 0$$

$$\text{Avg}(\varepsilon) = 0$$

to all orders in the fields

Decouples: graviton  
gravitino

They did not decouple  $b_{\mu}$

- \* dual rotation
- \* conformal SUSY  $\hat{S}$
- \* special conf.  $K_\mu$

$\Phi \Rightarrow$  weight 1

KV gauge

NPB 222  
(1983)

$$C = -3$$

$$\mathcal{Q} = 0$$

$$A_{\mu\nu}(\varepsilon) = 0$$

$$D_\mu \sigma = \partial_\mu \sigma - \frac{i}{2} \sigma b_\mu$$

$$\mathcal{L} = \{ \sigma, \sigma^2, \sigma F_\phi \}$$



asymptotically

$C = -3, \bar{\phi} = 0, Z \text{ real} \Rightarrow$  to linear order  
in the field fluctuation



$$\mathcal{L} = -3 \int d^4x e^{-K/3} \Phi^\dagger \Phi + \int d^2\theta \Phi^3 W + \frac{1}{4} \int d^4x \text{tr} F_{ab}^2 + \text{h.c.}$$

+ 000000

$$\Phi = \exp\left[\frac{\langle K \rangle}{2} - i \text{Arg}(K\Lambda)\right] \exp\left[\frac{\langle K_i \rangle X^i}{3}\right] (1 + \theta^2 F_\phi)$$

Kugo &

Uelare

NPB 226 (1983)

- \* dual rotation  $\mathbb{1}$  +
- \* conformal SUSY  $\hat{S}$
- \* special conf.  $K_\mu$

$\mathbb{I} \Rightarrow$  weight 1

$$C = -3$$

$$\mathcal{Q} = 0$$

$$A_{\mu\nu}(\varepsilon) = 0$$

$$D_\mu \sigma = \partial_\mu \sigma - \frac{i}{2} \sigma b_\mu$$

$$\mathbb{I} = \{ \sigma, \sigma^\dagger, \sigma F_\phi \}$$

$$\mathbb{I} = W^{-1/3} \tilde{\mathbb{I}} \quad \tilde{\mathbb{I}} = \{ 1, G_i \chi^i, F_\phi \}$$

$$\mathcal{L} = -3 \int d^4x e^{-K/3} \Phi^\dagger \Phi + \int d^2\theta \Phi^3 W + \frac{1}{4} \int d^4x \text{tr} F_{ab}^2 + \text{h.c.} + \mathcal{O}\left(\frac{1}{M_{\text{Pl}}}\right)$$

$$\Phi = \exp\left[\frac{\langle K \rangle}{2} - i \text{Arg}(W)\right] \exp\left[\frac{\langle K_i \rangle X^i}{3}\right] \left(1 + \theta^2 \frac{F}{\phi}\right)$$

Kugo &  
Uehara

NPB 226 (1983)

$$\mathcal{L} = -3 \int d^4x e^{-K/3} \Phi^\dagger \Phi + \int d^2\theta \Phi^3 W + \frac{1}{4} \int d^2\theta_{ab} W^{ab} W_{ab} + h.c.$$

$+ \mathcal{O}\left(\frac{1}{M_{Pl}}\right)$ 

 $m_{3/2}$  effect
 
 $\langle F_\phi \rangle = m_{3/2}$

1104.2538

$$\Phi = \exp\left[\frac{\langle K \rangle}{2} - i \text{Arg}(W)\right] \exp\left[\frac{\langle K_i \rangle X^i}{3}\right] (1 + \theta^2 F_\phi)$$

$C = -3, \xi = 0, \Xi$  real  $\Rightarrow$  to linear order  
in the field fluctuation

$$b_n = 0 + \mathcal{O}\left(\frac{1}{M_{pl}}\right)$$

$C = -3$  to all order

$\sigma$ : lowest component of chiral S.F.

$\Downarrow$   $\sigma$  function  
 $X^i \quad X^{+\bar{j}}$

$C = -3, \xi = 0, Z \text{ real} \Rightarrow$  to linear order  
in the field fluctuation

$$b_m = 0 + \mathcal{O}\left(\frac{1}{M_{pl}}\right)$$

$C = -3$  to all order

$\sigma$ : lowest component of chiral s.f.

$\Downarrow$   $\sigma$  function  
 $X^i \quad X^{+\bar{j}}$

$$D_m \sigma = \partial_m \sigma - \frac{i}{2} b_m \sigma \Rightarrow \text{chiral}$$

$C = -3, \xi = 0, \Xi$  real  $\Rightarrow$  to linear order  
in the field fluctuation

$$b_m = 0 + \mathcal{O}\left(\frac{1}{M^2}\right)$$

$C = -3$  to all order

$\sigma$ : lowest component of chiral S.F.

$\Rightarrow$   $\sigma$  function  
 $X^i \quad X^{+\bar{j}}$

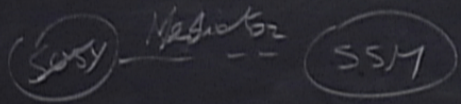
$$D_m \sigma = \partial_m \sigma - \frac{i}{2} \cancel{b_m} \sigma \Rightarrow \text{chiral}$$



Goldstein spectrum

Goldstein

Cherry, Nonuma, Thaler  
1002.1367



Goldstern spectrum

Goldstern

Cheng, Nima, Taler  
1002.1367

(Susy) Residuals

(Susy)

# Goldstini spectrum

Goldstini

Cheng, Nunez, Polchinski  
1002.1967

(SUSY)  $\xrightarrow{\text{Mediate}}$  (SSM)

(SUSY)

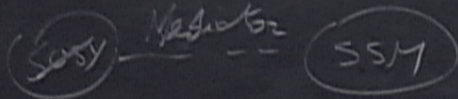
$N$  ~~SUSY~~ sequestered

$SUSY^N \xrightarrow{\text{gravity}} SUGRA$

# Goldstini spectrum

Goldstini

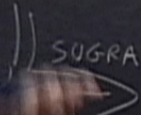
Cheng, Nilles, Todor  
1002.1867



$N$  ~~SUSY~~ sequestered

$SUSY^N \xrightarrow{\text{gravity}} SUGRA$

$N$  Goldstini



- one eaten by  $\Upsilon_\mu$
- $N-1$  Goldstini in the spectrum

# Goldstini spectrum

Goldstini

Cheng, Nunez, Thaler  
1002.1367

Factor

SSM

$N$  ~~SUSY~~ sequestered

$$m_{\frac{3}{2}} = 2 m_{\frac{3}{2}}$$

SUSY<sup>N</sup>

gravity

SUGRA

$$\langle K_i \rangle \neq 0$$

Goldstini

SUGRA

- one eaten by  $\Psi_{\mu}$
- $N-1$  Goldstini in the spectrum

Goldstini spectrum

$$Q = X^\dagger X$$
$$W = \mu^2 X$$

Goldstini

Cheng, Nussler, Pospelov  
1002.1367

$$\mathcal{L} = \int d^4x \phi^\dagger \not{\partial} \phi + X^\dagger X +$$
$$+ \int d^3x \phi^3 \mu^2 X$$

$$m_{3/2} = 2 m_{3/2}$$
$$\langle K_\mu \rangle \neq 0$$

