

Title: Giulio @ 13:30

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Abstract:

# The pure and reversible pictures of Quantum Mechanics

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Giulio Chiribella,  
Perimeter Institute for Theoretical Physics

Workshop "Conceptual Gems of Theoretical Physics",  
Friday October 14 2011, Perimeter Institute

# Plan of the talk

- \* **Prologue: the new view of Quantum Mechanics**
- \* **Physical processes and information flow:  
the language of pictures**
- \* **The causality principle**
- \* **The pure and reversible pictures of Quantum  
Mechanics**

# What did QM give to our culture so far?

- **Complementarity (Bohr, mid '20s)**

Some experiments are incompatible: observing one feature prevents us from observing the other



- **Uncertainty (Heisenberg, 1927)**

We cannot know with arbitrary precision the position and the velocity of a particle

- **Indeterminism (Born, 1926)**

We cannot predict with certainty the outcome of an experiment, no matter how well we know the measured system



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# Old view of QM: a theory of limits

THE **NEGATIVE** VIEW OF QUANTUM MECHANICS:  
theory of limits to knowledge, indetermination,  
imprecision, uncertainty, randomness,  
fuzziness, ...

# Old view of QM: a theory of limits

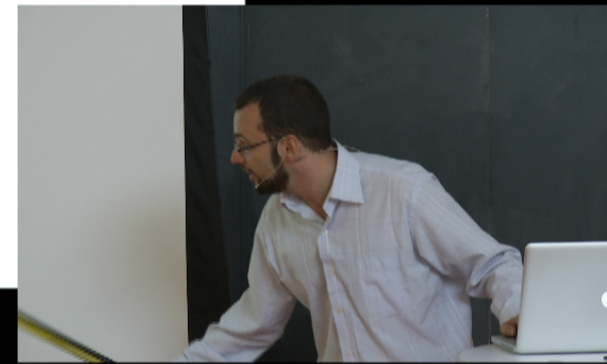
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**Nostalgia**  
of determinism:





# Quantum Information

- **Secure communication (Bennett Brassard '84, Ekert '92)**

The laws of QM guarantee that we can communicate privately

- **Fast computer algorithms (Shor 1997, Grover 1992)**

In the quantum world we can solve problems in less steps than in the classical one

- **State teleportation ('93)**

A finite amount of communication is enough to transfer from one location to another the information contained in a system with an infinite number of possible states



(top, left) Richard Jozsa, William K. Wootters, Charles H. Bennett. (bottom, left) Gilles Brassard, Claude Crépeau, Asher Peres. Photo: André Berthiaume.

# New view of QM: a physical theory of Information

A **POSITIVE** VIEW OF QUANTUM MECHANICS:

theory of new unexpected possibilities for communication, computation, and processing of information.

QM describes not only our **limits in the knowledge of the physical world**, but also, and perhaps most importantly, our **possibilities as information processing agents interacting with it!**

# The game of the lab 1

Imagine you are in a laboratory

There you find many devices: each device transforms an input system in an output system



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# The game of the lab 2

You find that some devices have no  
input:  
they "create" a system in some **state**



# The game of the lab 2

You find that some devices have no input:  
they "create" a system in some **state**



Some other devices have no output:  
they perform **measurements** that  
"destroy" the measured system,  
leaving only an **outcome**,  
with some probability



# Let's play the game

You can now start making experiments:

- prepare a system in some input state





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You can now start making experiments:

- prepare a system in some input state
- transform it, obtaining an output state
- measure the output and see what outcome you get



# Let's play the game

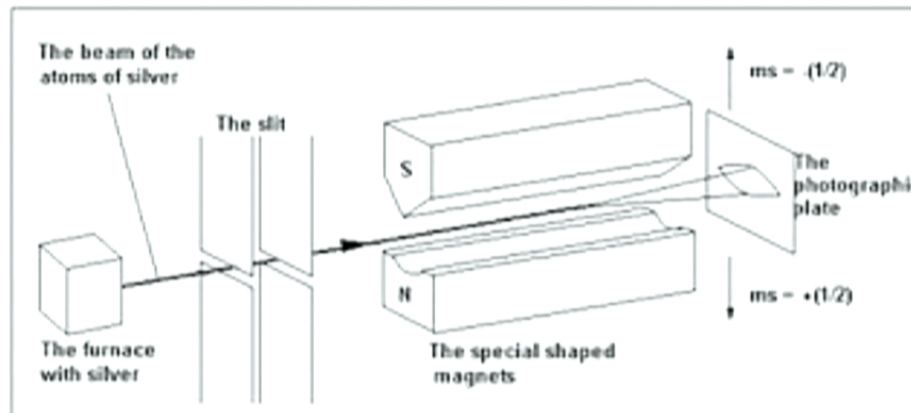
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**Your information about the system is contained in its state and propagates from input to output**

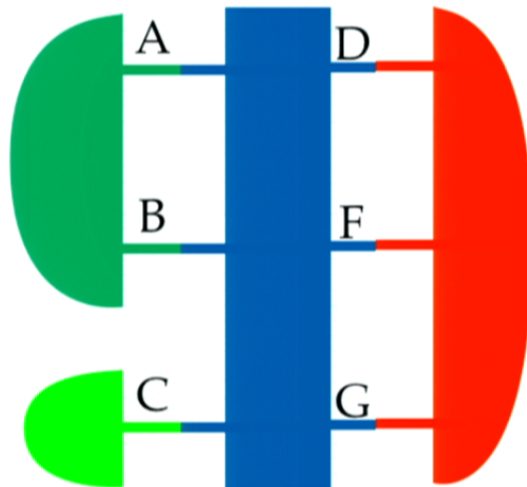
# Example: the Stern-Gerlach experiment



The Stern-Gerlach experiment. On the photographic plate are two clear tracks.



And you can make more complicated experiments...



- prepare A and B together
- prepare C
- transform A, B and C into D, E, and F
- measure everything together

# Non-physics examples

**THE LANGUAGE OF PICTURES  
CAN DESCRIBE MANY SITUATIONS,  
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We make to  
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**Pictures in the bank!**



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## Pictures in the bank!



## Pictures in the kitchen!



## Pictures in the kitchen!



# Reversible processes

A process  is reversible

if there is another process 

such that  = 

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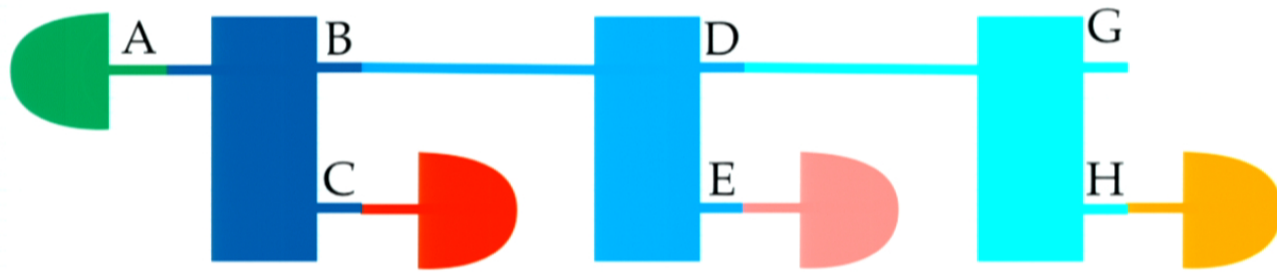
for every possible states  and 

# The causality principle



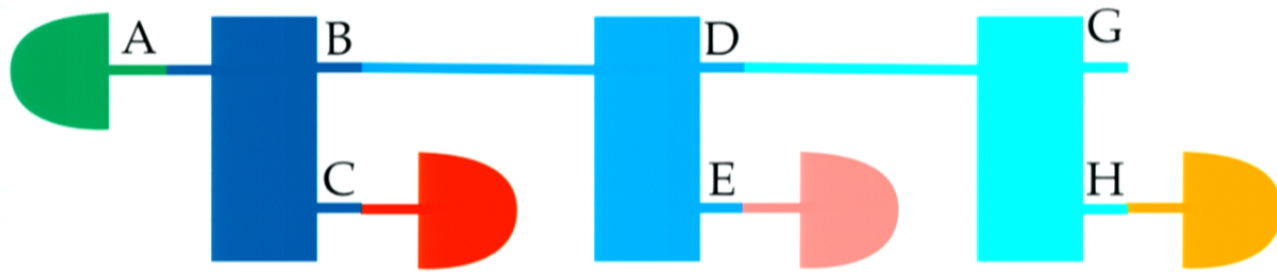
# Causality

Imagine a sequence of measurements, like



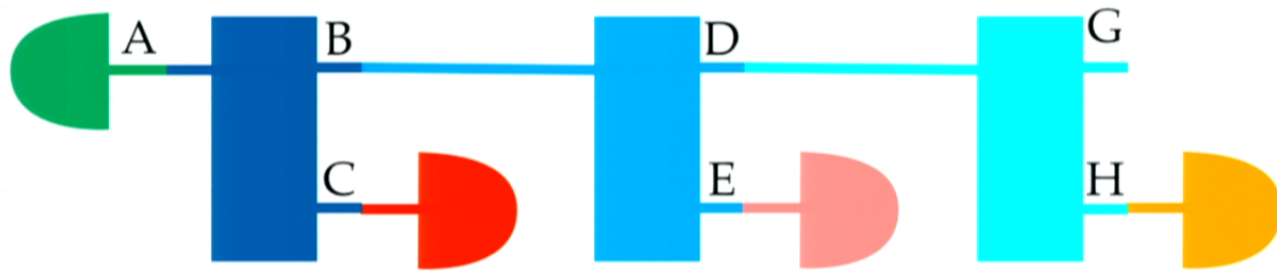
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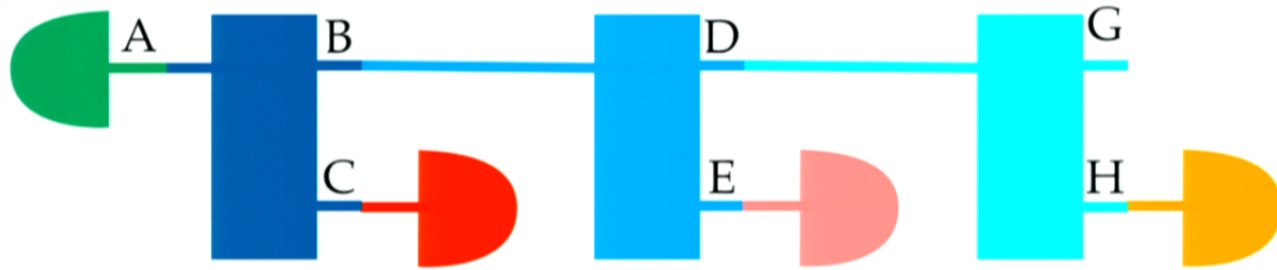
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The causality principle states that the outcome of a measurement at a certain time ("red measurement", here) does not depend on the choice of measurements performed later ("salmon" and "tangerine", here)

# Painting causality

To “discard a system” means to perform a measurement on it and to ignore the outcome.

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The system A has been “destroyed”  
without leaving any information

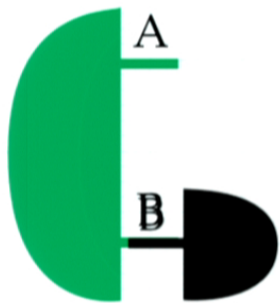
Keeping one,  
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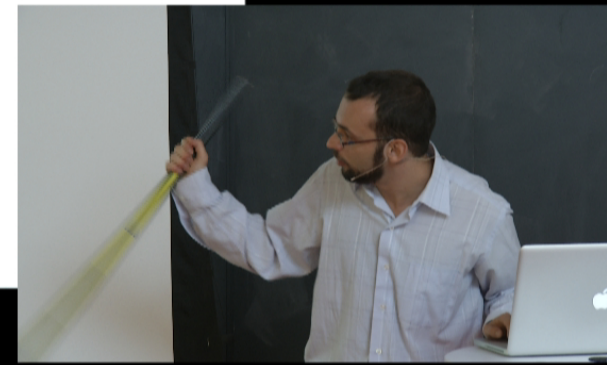
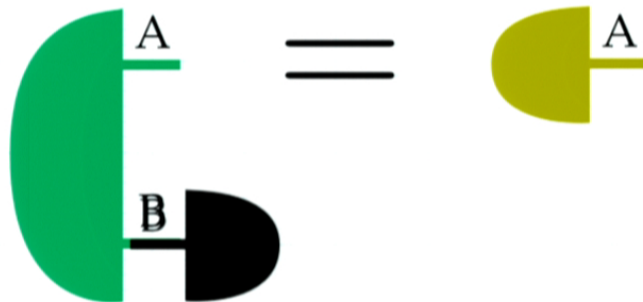
# Keeping one, discarding the other

- Take a state of **A** and **B** together
- Discard **B**



# Keeping one, discarding the other

- Take a state of **A** and **B** together
- Discard **B**
- What remains is a state of **A** alone



# The pure and reversible pictures of Quantum Mechanics

# Pure states

The state describes our information about the system

**Two possibilities:**

- 1) our information is **maximal**:  
there is no way to know the system better.

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“Pure states”



example: polarized light  
(we know exactly  
the polarization)



# Mixed states

2) our information is **not-maximal**:  
the system could be in many different pure states,  
but why don't know which

**"Mixed states"**



example: sunlight  
(the polarization  
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# Purification 1

**Quantum Mechanics has an amazing property:**

# Purification 1

Quantum Mechanics has an amazing property:

Every mixed state  
can be obtained from a pure state  
of two systems together  
by discarding one system



## Purification 2

In other words, **whenever we are ignorant** about a system we can always imagine that our ignorance is due to the fact that **there is some other system** that missed to consider, a system **that completes our information**

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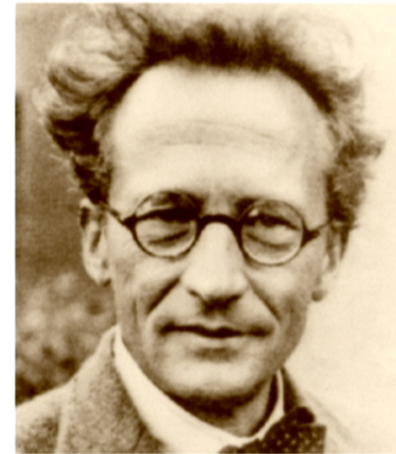
example: sunlight  
each photon is generated by a reaction in the photosphere. Its polarization is random, but if we include the electrons and hydrogen atoms that participate in the reaction, these systems together are in a pure state



# Entanglement

**“The best possible knowledge of a whole does not necessarily include the best possible knowledge of all its parts”**

**“I would not call that one but rather **the** characteristic trait of quantum mechanics, the one that enforces its entire departure from classical lines of thought.”**



**Schrödinger, 1935**

# Purification 3

Purification implies another surprising property:

Every irreversible process  $A \rightarrow B$

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as follows:



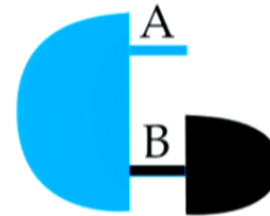


# In summary

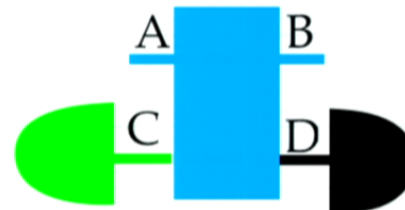
Our actual  
experience:  
ignorance and  
irreversibility



=



=



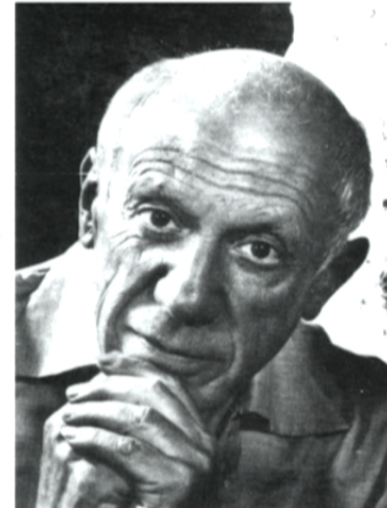
# In summary

Quantum mechanics is a **physical theory of information**:

it reconciles our experience of information-processing agents with a pure and reversible picture of the world

I paint objects  
as I think them, not  
as I see them

**But does this pure and reversible picture  
describe how things actually are?  
Or is it a mere fiction?**



# Two metaphors and a conclusion

# Completing the picture

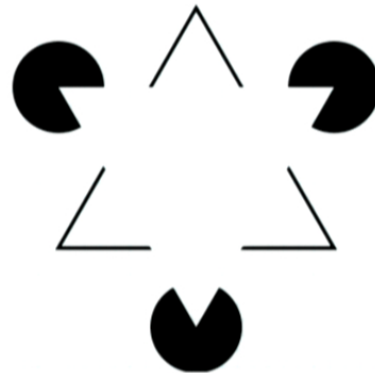
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This process recalls some optical illusions, where our brain completes a picture by imagining shapes that are not in the picture itself:

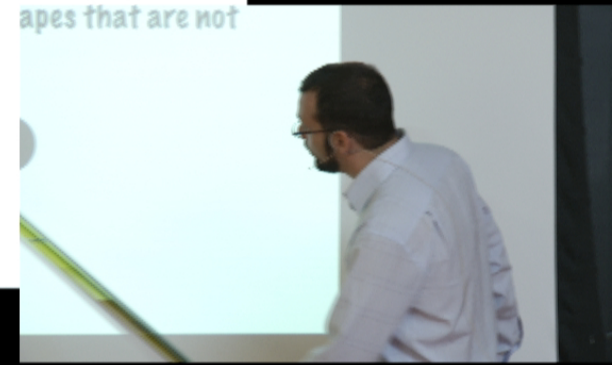
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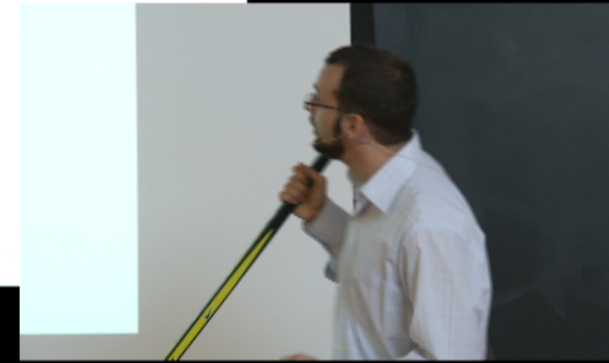


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# Twin systems in narrative

The idea that two systems can be in a pure state together but separately appear in mixed states resonates with the literary theme of the double, which reveals the identity of its twin



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Weronika observes the world through a transparent ball, while the train window reflects the image, alluding to her far apart double, Veronique.

Scene from  
The double life of Véronique  
(1991)



# Conclusion

**Quantum Mechanics is much more than just a theory of limits:**

**It is the physical theory that combines our limited experience of information-processing agents with the possibility of a pure and reversible picture of the world.**



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**Quantum Mechanics is much more than just a theory of limits:**

**It is the physical theory that combines our limited experience of information-processing agents with the possibility of a pure and reversible picture of the world.**

**Whether this picture is fact or fiction, perhaps it is not so important:**

**The cultural richness of Quantum Mechanics is exactly in the possibility to construct new pictures about the world and of our interaction with it.**



# Short bibliography

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**<http://arxiv.org/pdf/0908.1787v1>**
- **C. Brukner,**  
**Questioning the rules of the game,**  
**<http://physics.aps.org/articles/v4/55>**
- **GC, G. M. D'Ariano, and P. Perinotti,**  
**Informational derivation of quantum theory,**  
**<http://arxiv.org/pdf/1011.6451>**

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