

Title: Astrophysical Constraints on Dark Matter Annihilation with Sommerfeld Enhancement

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Abstract: Dark matter models with an annihilation cross section enhanced by a Sommerfeld mechanism have been proposed in the past years to explain a number of observed anomalies, such as the excess of high energy positrons in cosmic rays reported by PAMELA. However, this enhancement can not be arbitrarily large without violating a number of astrophysical measurements. In this talk, I will discuss the degree to which these measurements can constrain Sommerfeld-enhanced models. In particular, I will talk about constraints coming from the observed abundance of dark matter and the extragalactic background light measured at multiple wavelengths.

# Astrophysical constraints on dark matter annihilation with Sommerfeld enhancement



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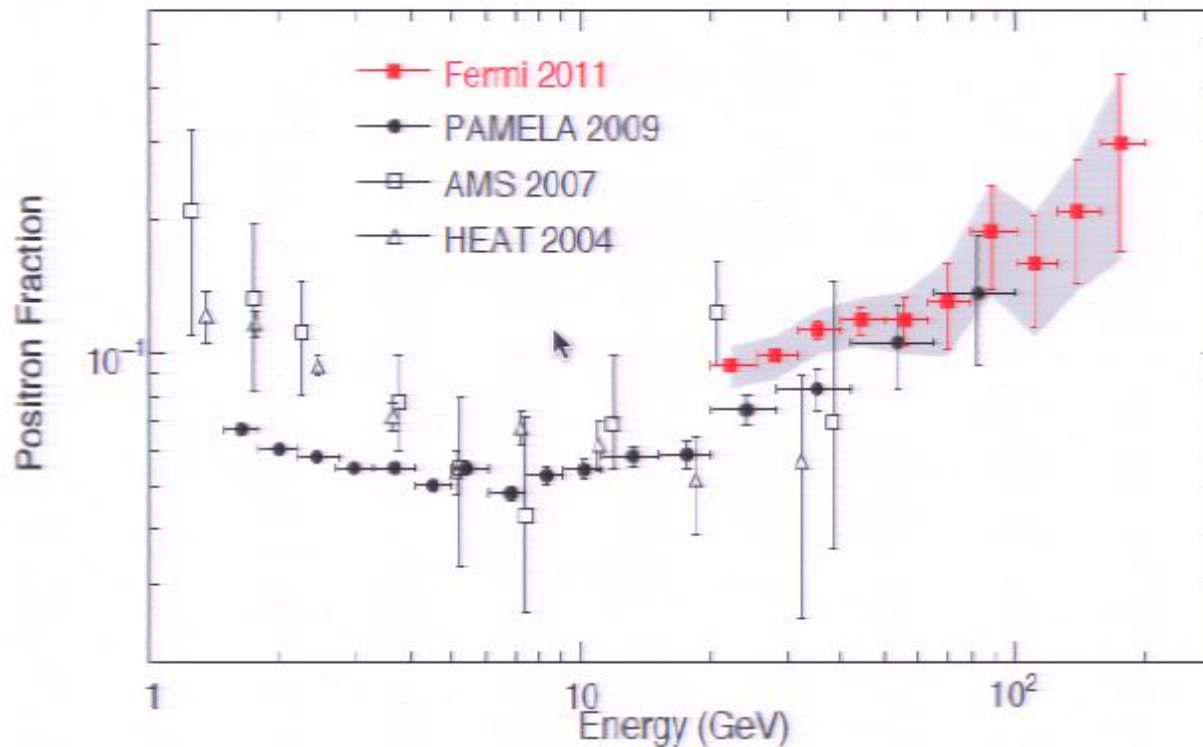
Papers: PRD, 81, 083502 ([0910.5221](#)), PRD, 83, 123513 ([1103.0776](#))

# Outline

- **Sommerfeld enhancement (brief motivation and description)**
- **Relic density constraints**
- **CMB constraints**
- **DM annihilation in halos and the Extragalactic Background Light (X- and Gamma-rays)**
- **EBL constraints**

# Why boosting DM annihilation?

PAMELA and Fermi e+ excess (E>10GeV)  
Ackermann et al. 2011



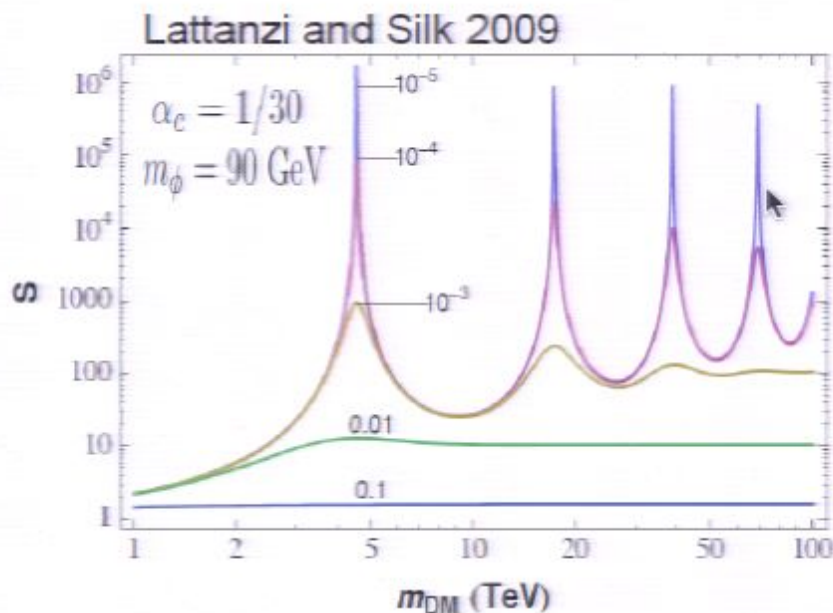
## The case for DM annihilation

- WIMP annihilation can explain cosmic ray anomalies but: **large cross section**  $BF > O(100)$  over thermal relic value:  $3 \times 10^{-26} \text{cm}^3 \text{s}^{-1}$  (e.g. Bergström et al. 2009) and **annihilation mainly to leptons, proton/antiproton channel suppressed** (PAMELA data).
- A new force carrier ( $m_\phi \sim \text{GeV}$ ) acting between the annihilating WIMPs enhances the cross section via a **Sommerfeld mechanism** (Hisano et al. 2004, Arkani-Hamed et al. 2009, ..). If  $m_\phi < 2m_p$ , then decay into antiprotons is kinematically forbidden.

# Sommerfeld enhancement

Simplified case, a scalar boson as a force carrier, Yukawa potential

$$\frac{1}{m_\chi} \frac{d^2 \Psi(r)}{dr^2} + V(r) \Psi(r) = -m_\chi \beta^2 \Psi(r) \quad V(r) = -\frac{\alpha_c}{r} e^{-m_\phi r}$$



$$\sigma = \sigma_0 S_k \quad S_k = \frac{|\psi_k(0)|^2}{|\psi_k^{(0)}(0)|^2}$$

Coulomb approximation ( $m_\phi \rightarrow 0$ ):

$$S = \frac{\pi \alpha_c}{\beta} \left(1 - e^{-\pi \alpha_c / \beta}\right)^{-1}$$

$$S(\beta) \propto 1/\beta \quad \text{if } \beta \ll \pi \alpha_c$$

General behaviour:

1) if  $\beta^2 \gg m_\phi \alpha_c / m_\chi \rightarrow$  Coulomb case

2) if  $\beta^2 \ll m_\phi \alpha_c / m_\chi \rightarrow$  bound states if  $m_\chi = 4m_\phi n^2 / \alpha$

3) Close to "resonances"  $\rightarrow S(\beta) \propto 1/\beta^2$

4) Saturation at very low velocities, finite life time of the bound states

# Relic density constraints

Boltzmann equation: 
$$\frac{dn_\chi}{dt} + 3Hn_\chi = -\langle\sigma v\rangle \left( n_\chi^2 - (n_\chi^{EQ})^2 \right)$$

Thermal average:  $x_\chi = m_\chi/T_\chi$

$$\langle\sigma v\rangle = \langle\sigma v\rangle_S \left( \frac{x^{3/2}}{2\pi^{1/2}} \int_0^1 S(\beta) \beta^2 e^{-x\beta^2/4} d\beta \right) = \langle\sigma v\rangle_S \mathcal{S}(x_\chi)$$

Note that:

$$S(\beta) \propto 1/\beta \quad \rightarrow \quad \mathcal{S}(x_\chi) \propto x_\chi^{1/2} \propto 1/\sigma_{vel}$$

$$S(\beta) \propto 1/\beta^2 \quad \rightarrow \quad \mathcal{S}(x_\chi) \propto x_\chi \propto 1/\sigma_{vel}^2$$

Dark matter abundance:  $\Omega_\chi h^2 = \Omega_{DM} h^2 \sim 0.1143$

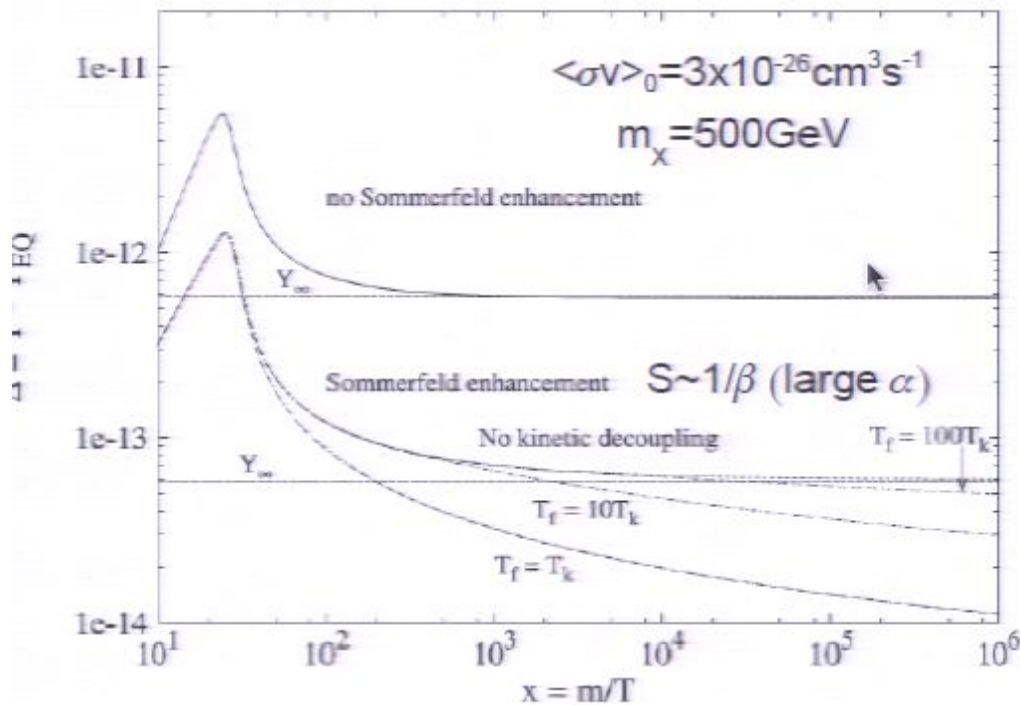
**Kinetic decoupling:** after freeze-out, scattering with SM particles keep  $T_\chi = T$ , after kinetic decoupling  $T_\chi$  drops as  $1/a^2$  ("colder" than radiation):

$$x_\chi = x \quad \text{for } t < t_{KD}$$

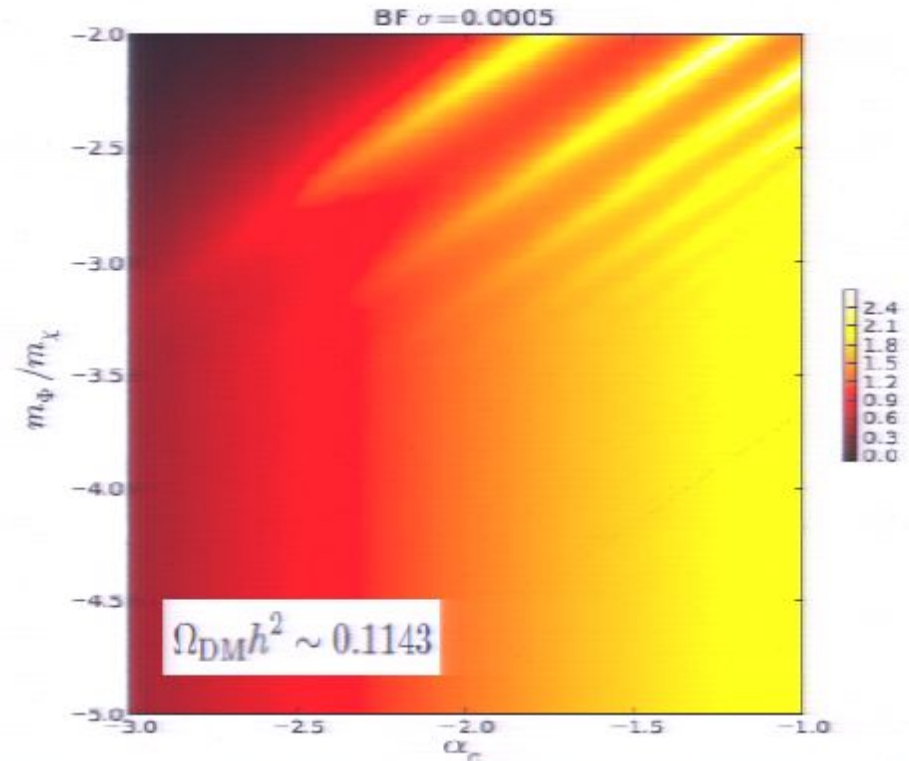
$$x_\chi = x^2/x_{KD} \quad \text{for } t > t_{KD}$$

# Relic density constraints

Dent et al. 2010



Zavala et al. 2010



- If  $S \sim 1/\sigma$  then  $Y \sim 1/\ln x$  for  $x > x_{kd}$
- If  $S \sim 1/\sigma^2$  then  $Y \sim 1/x$  for  $x > x_{kd}$
- $\langle \sigma v \rangle_0$  needs to be lower than the case without enhancement (a factor of a few) to give the correct relic density
- Kinetic decoupling temperature is a relevant parameter, the larger it is, the stronger the suppression on the relic density

BF (relative to  $\langle \sigma v \rangle_0 = 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$ )  $< 100$   
for  $\alpha < 10^{-2}$ ,  $m_\psi/m_\chi < 10^{-3}$ ,  $m_\chi \sim 100 \text{ GeV}$ ,  $T_{kd} = 8 \text{ MeV}$

$$\text{BF} = \frac{\langle \sigma v \rangle_0^{\Omega_{DM}} S(\sigma_{\text{vel,h}})}{3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}}$$

Feng et al. 2010, "maximal" BF up to  $m_\chi \sim 3 \text{ TeV}$  is  $< 300$

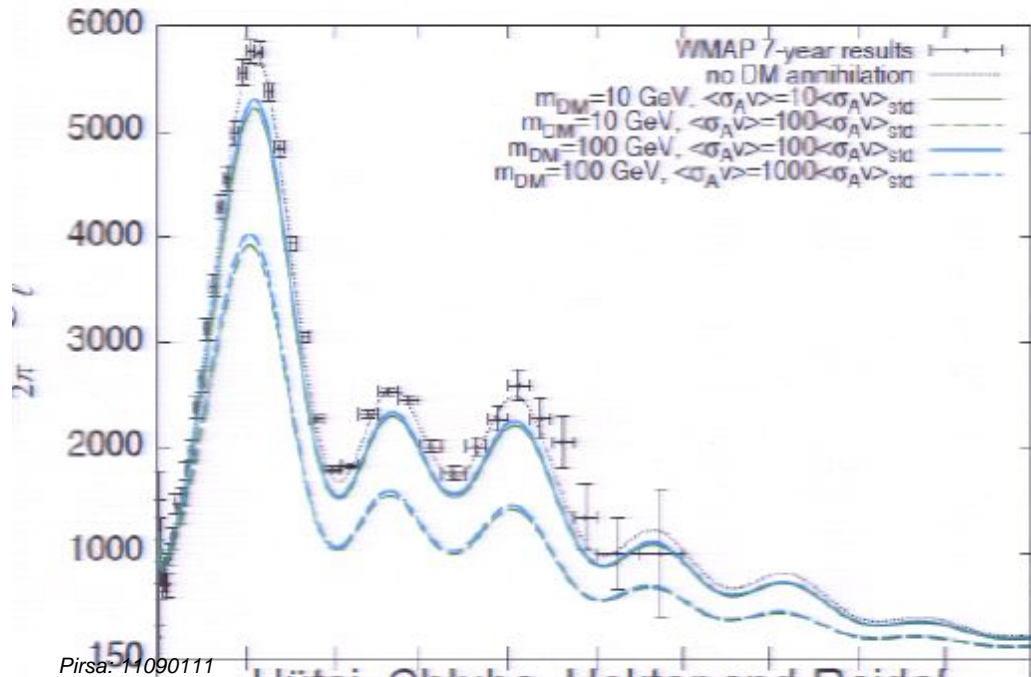
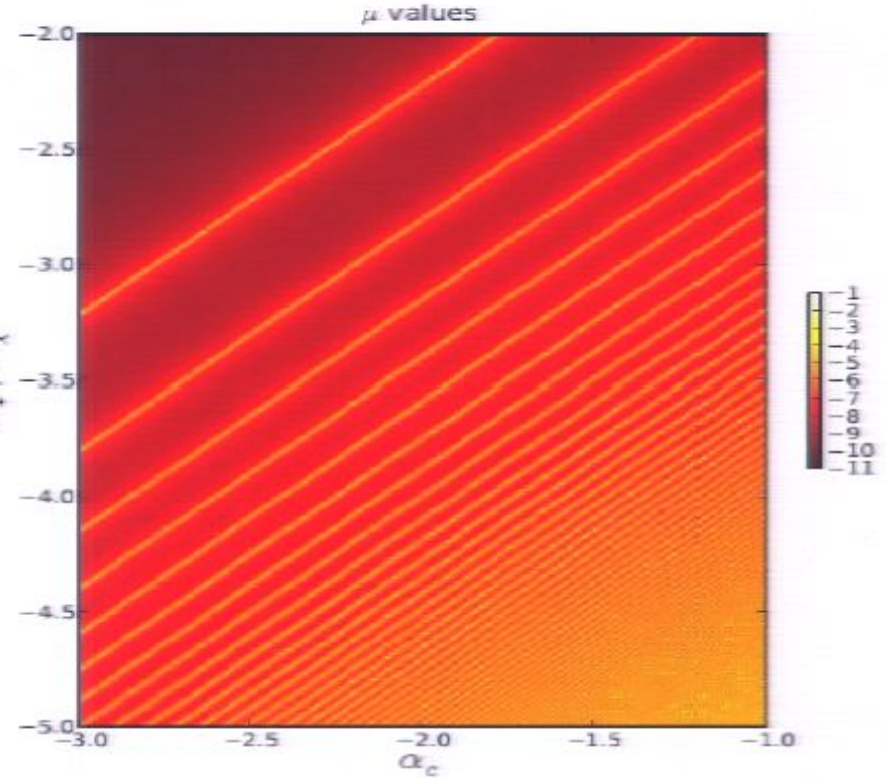
# CMB constraints

Zavala et al. 2010

**CMB energy spectrum:** energy injection at  $10^4 < z < 10^6$  effectively produces a Bose-Einstein energy spectrum with chemical potential  $\mu$  instead of a pure black body spectrum (Illarionov and Sunyaev 1975). Limit by COBE/FIRAS  $|\mu| < 9 \times 10^{-5}$ . "f" is the fraction that ionizes and heats the IGM.

$$\mu = 1.4 \frac{\delta \rho_\gamma}{\rho_\gamma} = 1.4 \int_{t_1}^{t_2} \frac{\dot{\rho}_\gamma}{\rho_\gamma} dt = 1.4 \int_{t_1}^{t_2} \frac{f m_\chi \langle \sigma v \rangle n_\chi^2}{\rho_{\gamma,0} a^{-4}} dt,$$

Injection at  $10^3 < z < 10^4$  produces a y-type distortion to the CMB (Hannestad and Tram 2011). Both are **weak constraints**.



**CMB power spectrum:** e.g. Slatyer et al. 2009, limits based on WMAP5:

$$\frac{\lim_{v \rightarrow 0} \langle \sigma v \rangle}{3 \times 10^{-26} \text{cm}^3/\text{s}} \lesssim \frac{120}{f} \left( \frac{m_\chi}{1 \text{TeV}} \right)$$

$f \sim 0.25$  for annihilation into SM particles, except electrons ( $f \sim 0.7$ ) and neutrinos ( $f \sim 0$ )



# Cosmic background radiation from dark matter annihilation

- Energy of photons per unit area, time, solid angle and energy range received by an observer located at  $z=0$ .

$$I = \frac{1}{4\pi} \int \mathcal{E}(E_0(1+z), z) \frac{dr}{(1+z)^4} e^{-\tau(E_0, z)}$$

- Contribution from all dark matter structures along the line of sight of the observer (assumption: no contribution from unclustered DM).
- The volume emissivity of photons (energy of photons produced per unit volume, time and energy range) can be written as:

$$\mathcal{E} = \frac{f_{\text{WIMP}}}{2} E \rho_\chi(\vec{x})^2$$

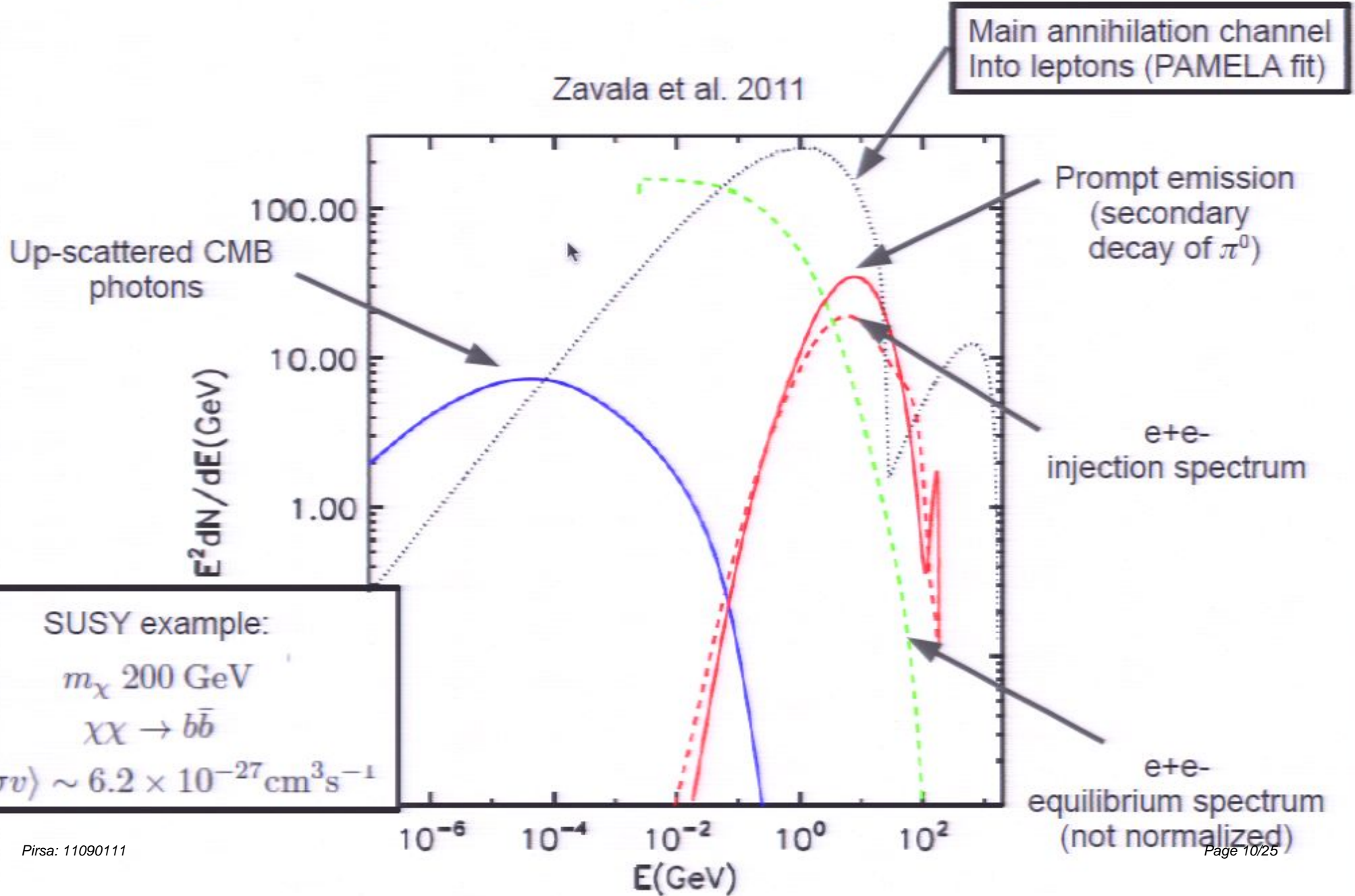
- Properties of dark matter as a particle:

$$f_{\text{WIMP}} = \frac{dN}{dE} \frac{\langle \sigma v \rangle}{m_\chi^2}$$

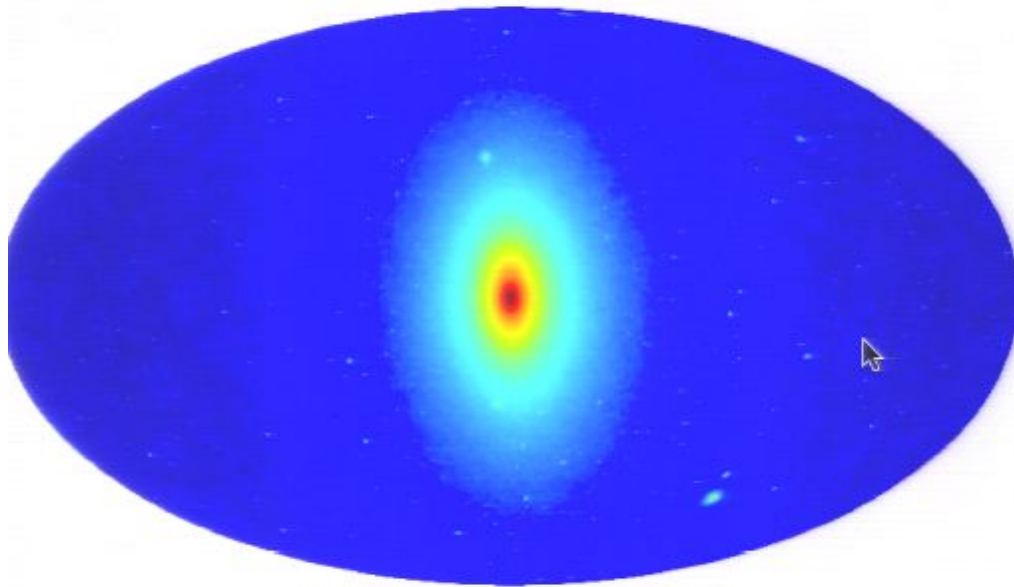
- The density squared dependence is connected to the gravitational interactions of dark matter.

# Photon yield

Zavala et al. 2011



# Annihilation in DM halos



Virgo Consortium's Aquarius Project

MW-like halo

$m_{DM} \sim 1500 M_{\text{sun}}$  (Springel et al. 2008)

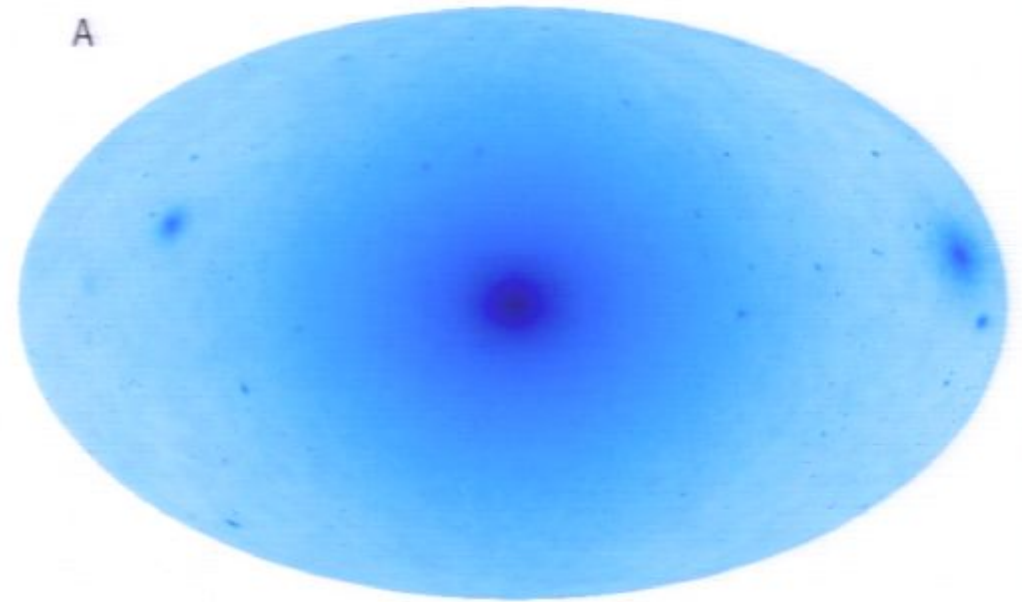
14  18  
log S ( $M_{\text{sun}}^2 \text{kpc}^{-2} \text{sr}^{-1}$ )

Via-Lactea II simulation

MW-like halo

$m_{DM} \sim 4100 M_{\text{sun}}$  (Kuhlen et al. 2009)

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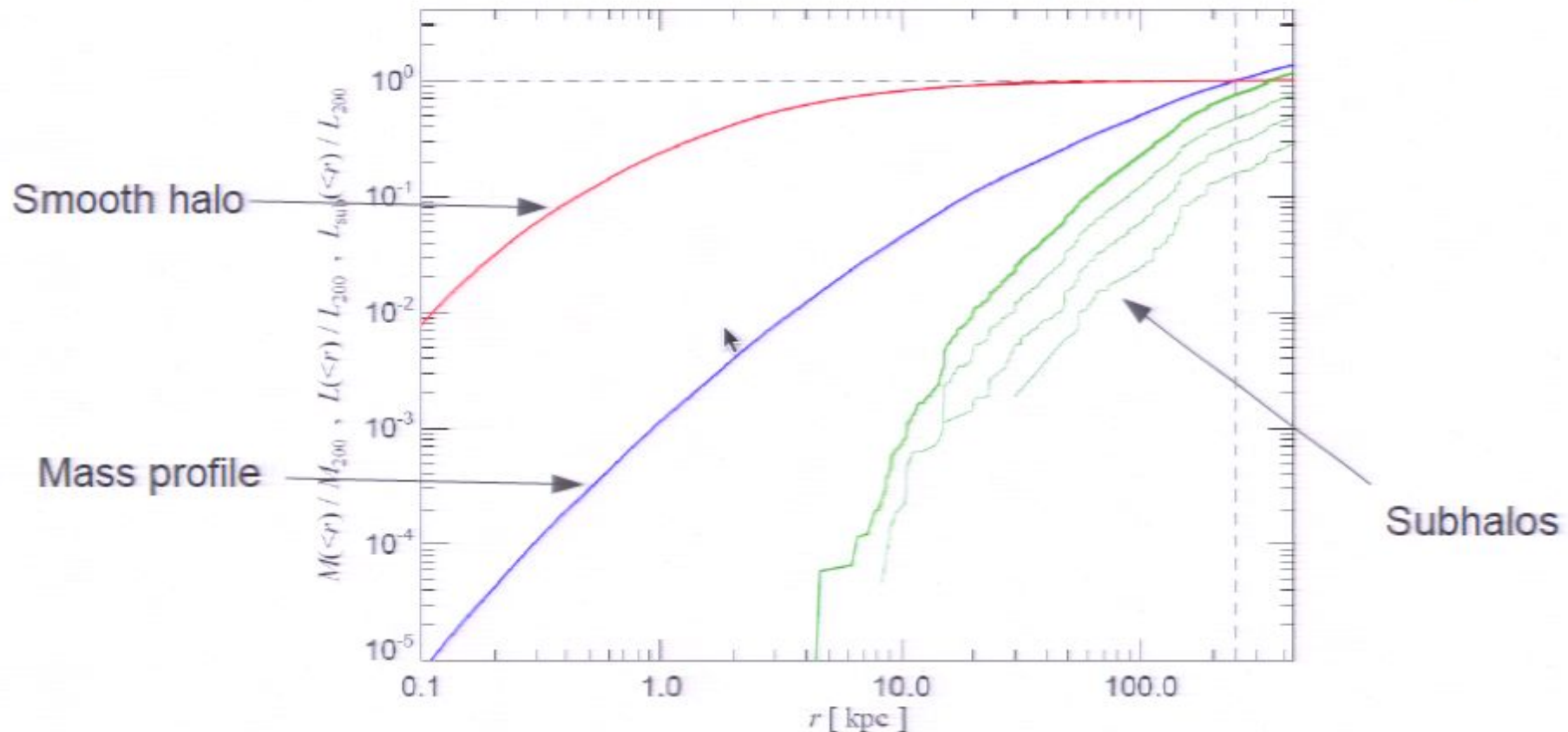


- Total luminosity of a smooth DM halo (formula roughly agrees with summation over particle densities):

$$L'_h = \int \rho_{\text{NFW}}^2(r) dV = \frac{1.23 V_{\text{max}}^4}{G^2 r_{\text{max}}}$$

Keep in mind: uncertainty on the DM density profile (+effects of baryons)

# Annihilation in DM halos (substructure)



Springel et al. 2008

- **Substructures within halos have a dominant role for external observers.** Their contribution to the total luminosity is uncertain  $\sim 2 - 2000$  times the contribution of the smooth component for a MW-like halo (once their minimum mass is extrapolated to  $\sim$ Earth mass).

# Millennium-II (Boylan-Kolchin et al. 2009)

Same cosmology as Millennium I

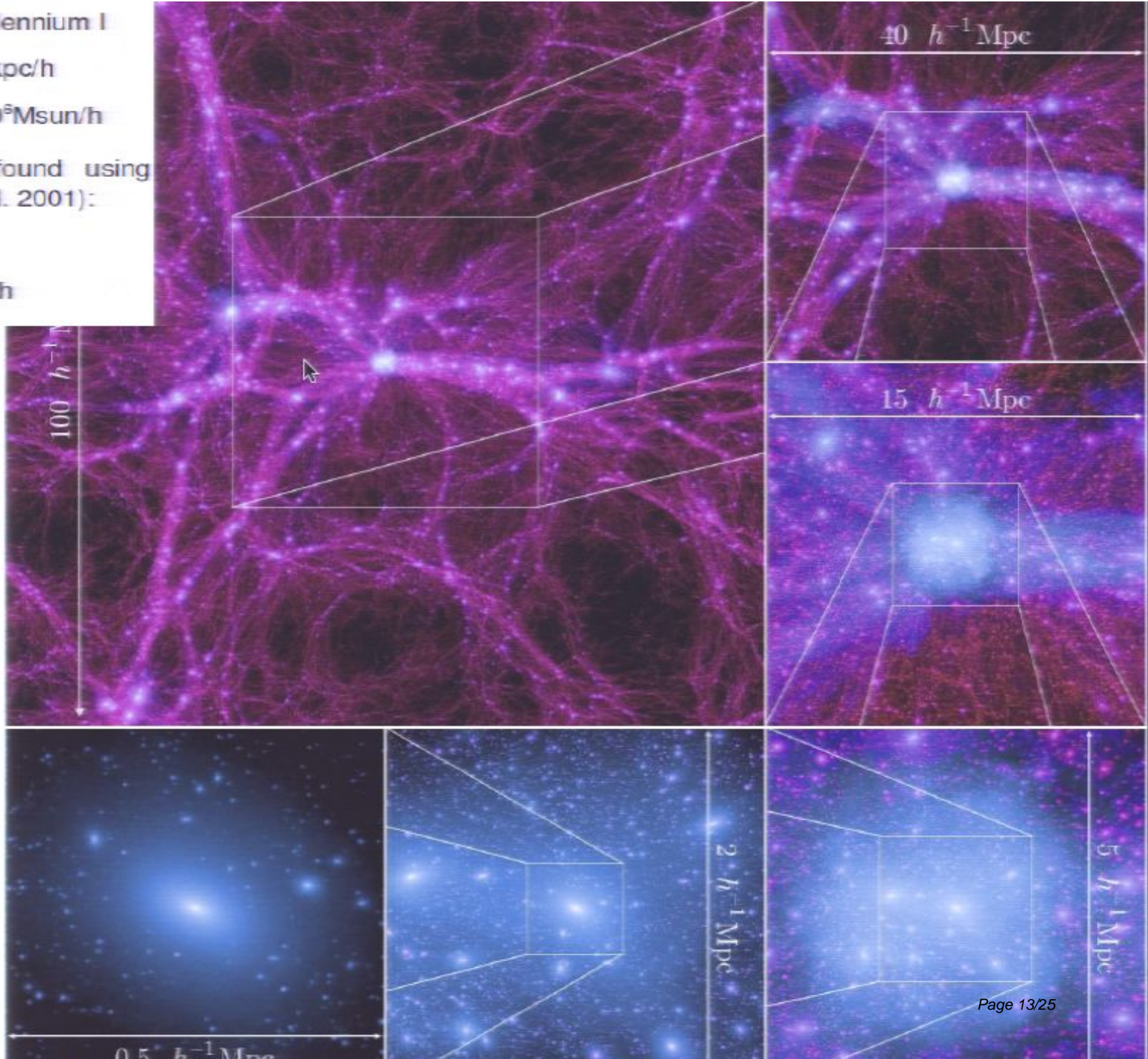
100 Mpc/h box and  $\epsilon=1\text{kpc/h}$

$N_p=2160^3$ ,  $m_{DM}=6.89\times 10^6\text{Msun/h}$

Bound substructures found using  
SUBFIND (Springel et al. 2001):

$11\times 10^6$  subs at  $z=0$

$M_{sb}(\text{min})\sim 1.4\times 10^8\text{Msun/h}$



Same cosmology as Millennium I

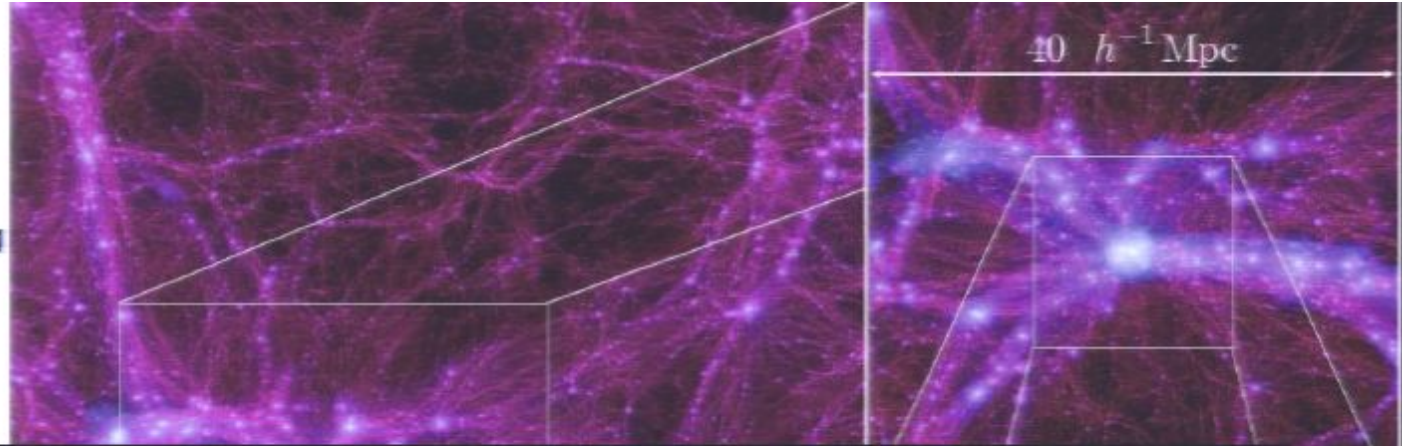
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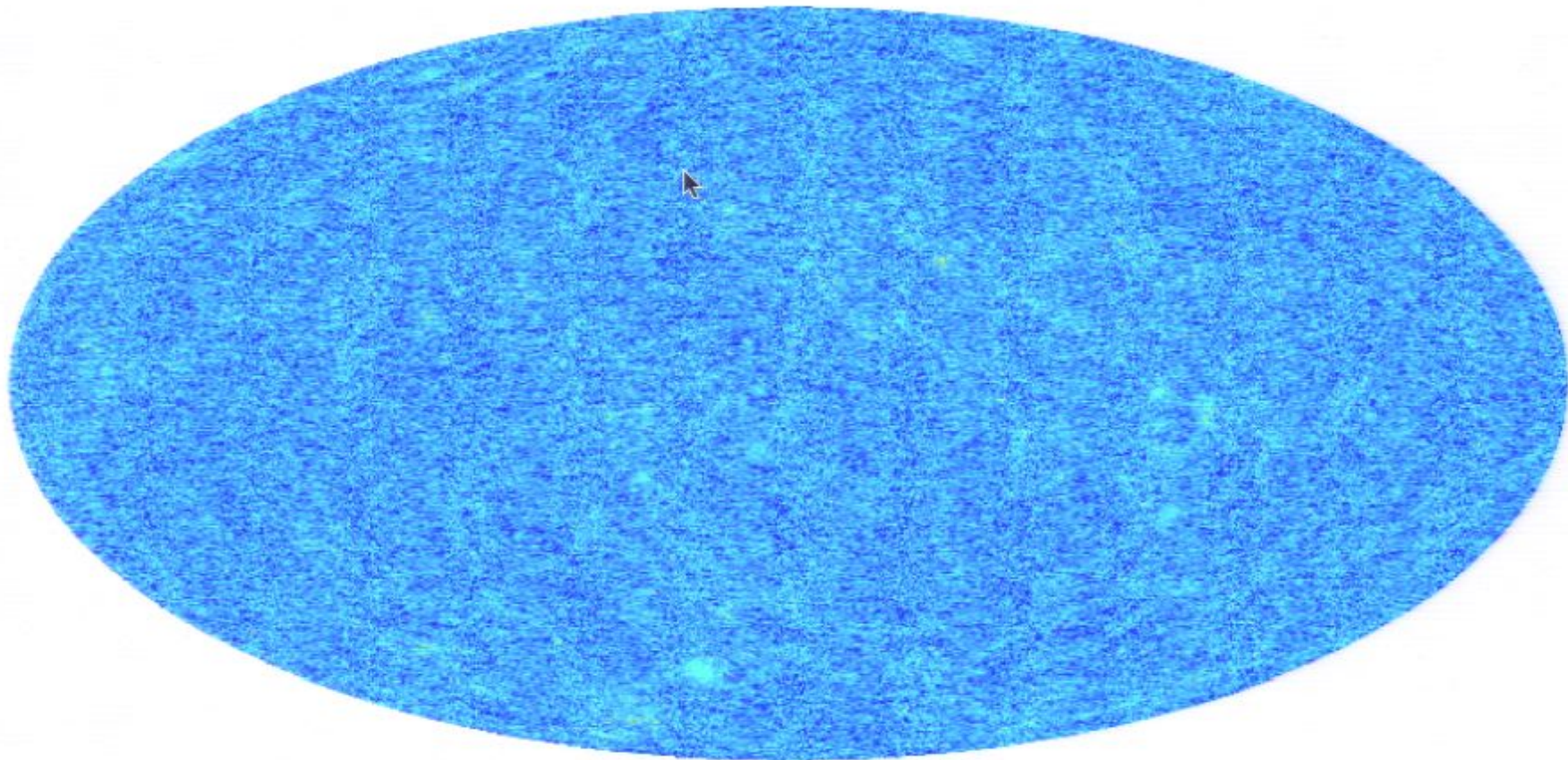


## All-sky maps

- Simulation of the past light cone with resolved DM halos and subhalos as sources (assuming scaling law for luminosity, NFW profile)
- Spatial distribution and temporal evolution given by MS-II
- Extrapolation to unresolved sources down to earth masses (two orders of magnitude uncertainty)
- Photon yield given as input from a particle physics model
- Sommerfeld enhancement included as a  $S(\sigma_{\text{vel}})$  function

Millennium-II Sinhalese  
(Boylan-Kolchin et al. 2009)

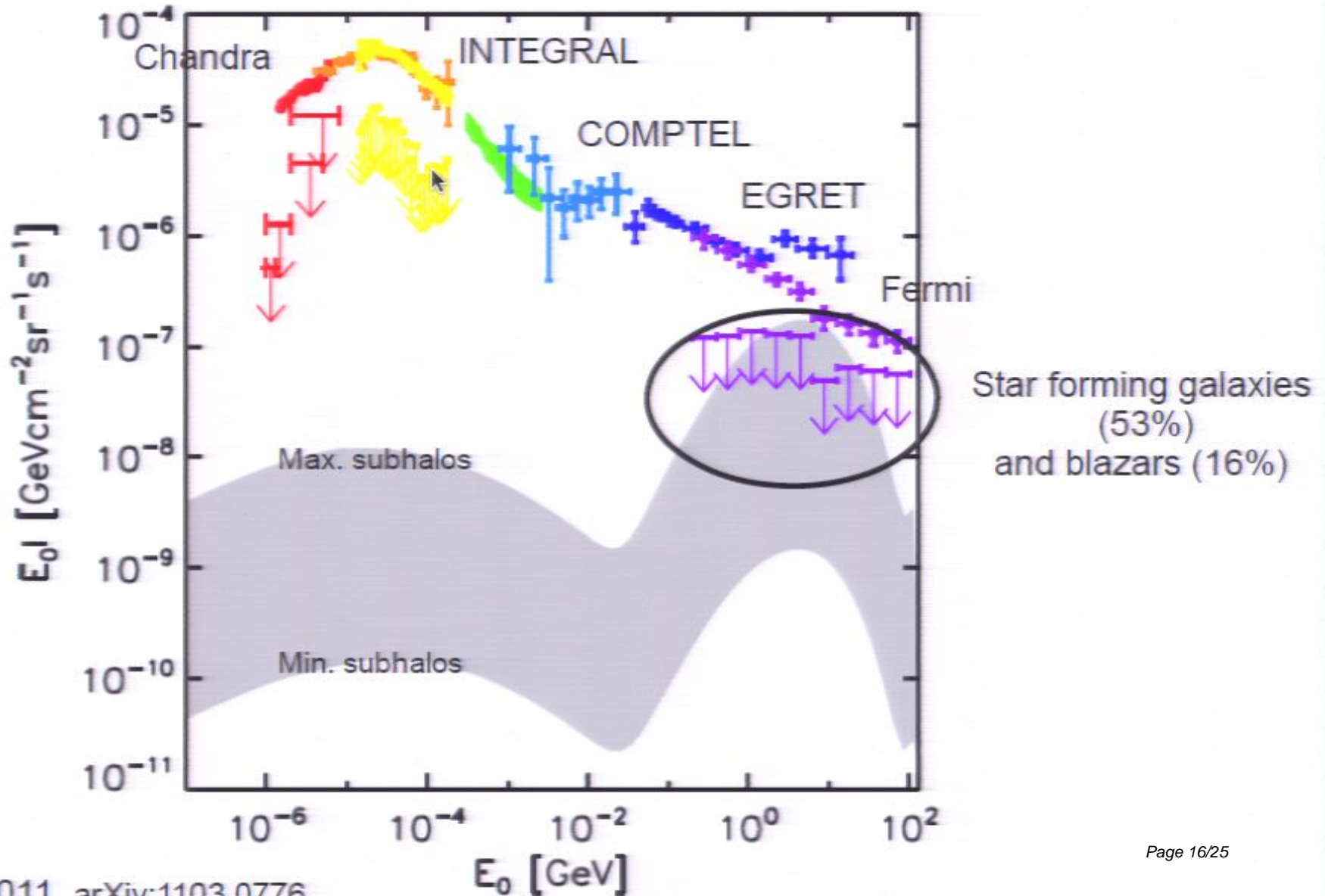
# All-sky maps (resolved structures up to $z \sim 10$ , $E=10\text{GeV}$ )



-11.  -9.0  $\text{Log}(I_{\gamma,e})$   
 $N_{\text{pix}} = 12(512)^2 \sim 3 \times 10^6$       ang. res.  $\sim 0.115^\circ$

# Isotropic component (example)

$$m_\chi \sim 200 \text{ GeV}, \chi\chi \rightarrow b\bar{b} \text{ and } \langle\sigma v\rangle \sim 6.2 \times 10^{-27} \text{ cm}^3 \text{ s}^{-1}$$



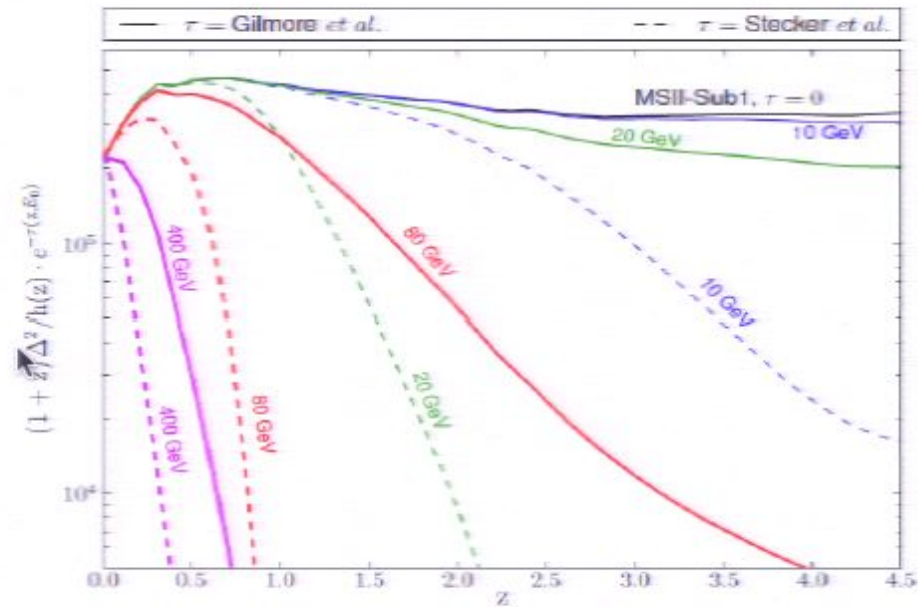


# Constraints on particle physics models

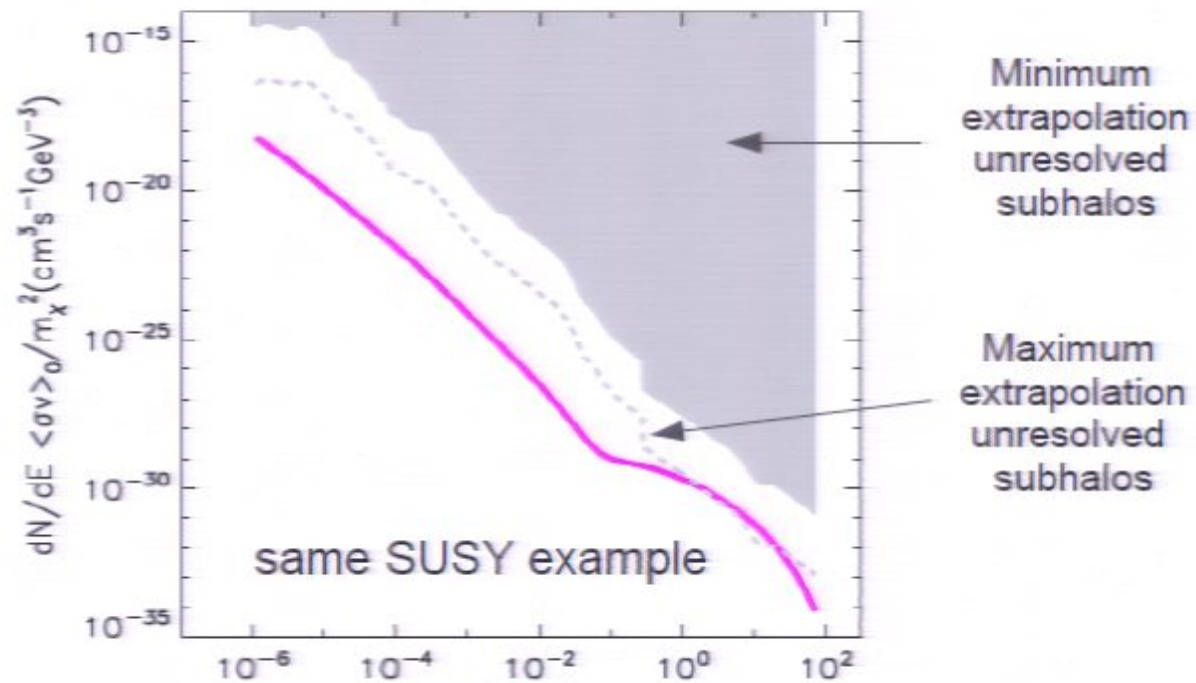
“factoring out” the astrophysical part of the signal

$$\Gamma(E_0) = \frac{c}{8\pi} E_0 f_{\text{WIMP}}(E_0(1+z^*)) \int \frac{\rho_\chi^2(\vec{x}, z) e^{-\tau(E_0, z)}}{(1+z)^3 H(z)} dz$$

$z^* < 4$  for X-rays  
 $z^* < 1$  for  $E > 10 \text{ GeV}$

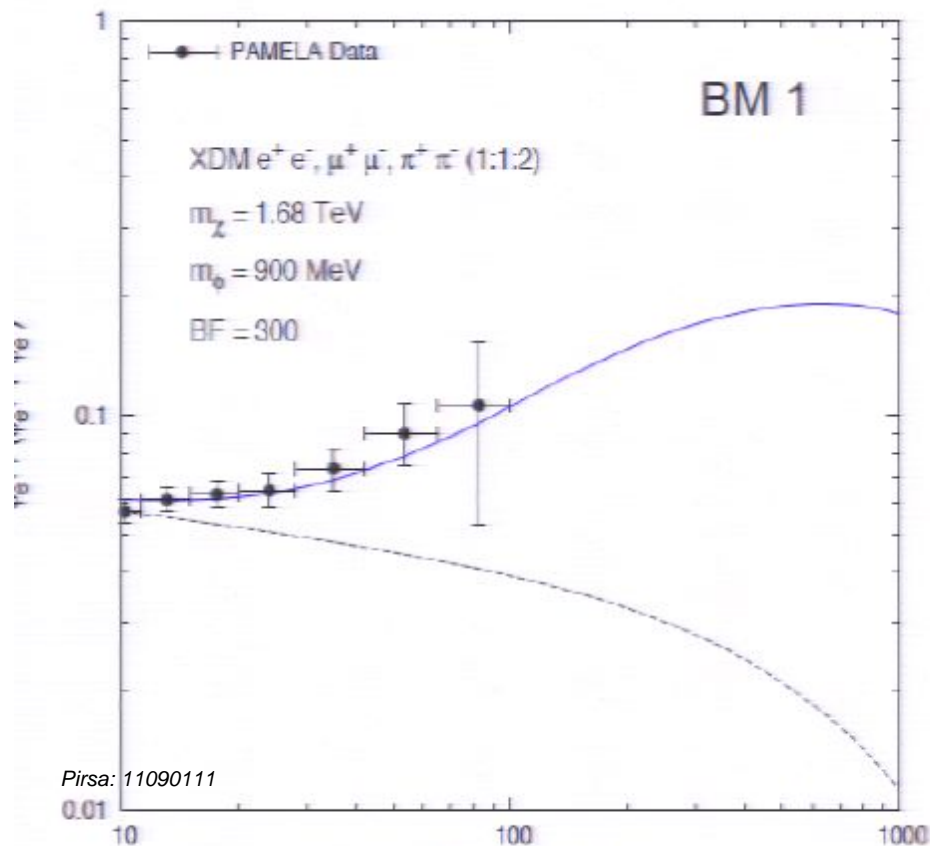


Fermi collaboration  
 Abdo et al. 2010



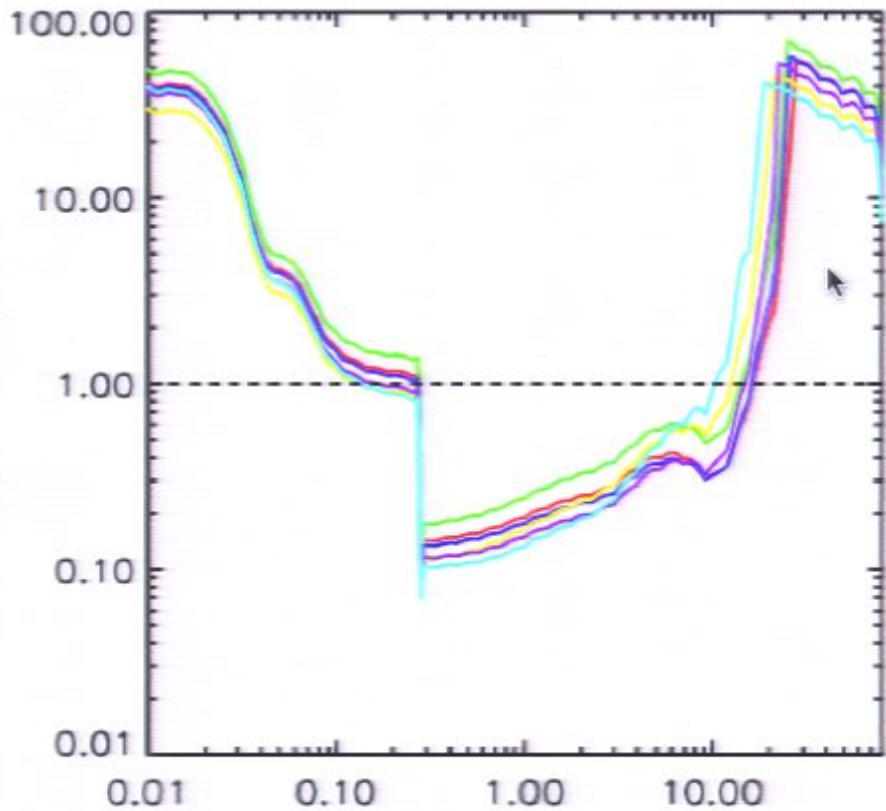
# Sommerfeld-enhanced models fitting the cosmic ray excesses (Finkbeiner et al. 2011)

Benchmark no.	Annihilation Channel	$m_\phi$ (MeV)	$m_\chi$ (TeV)	$\alpha_c$	$\delta$ (MeV)	$\frac{S_{\max}(\sigma v)_0}{3 \times 10^{-26} \text{cm}^3 \text{s}^{-1}}$
1	1:1:2 $e^\pm : \mu^\pm : \pi^\pm$	900	1.68	0.04067	0.15	530
2	1:1:2 $e^\pm : \mu^\pm : \pi^\pm$	900	1.52	0.03725	1.34	360
3	1:1:1 $e^\pm : \mu^\pm : \pi^\pm$	580	1.55	0.03523	1.49	437
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5	1:1 $e^\pm : \mu^\pm$	350	1.33	0.02643	1.10	339
6	$e^\pm$ only	200	1.00	0.01622	0.70	171



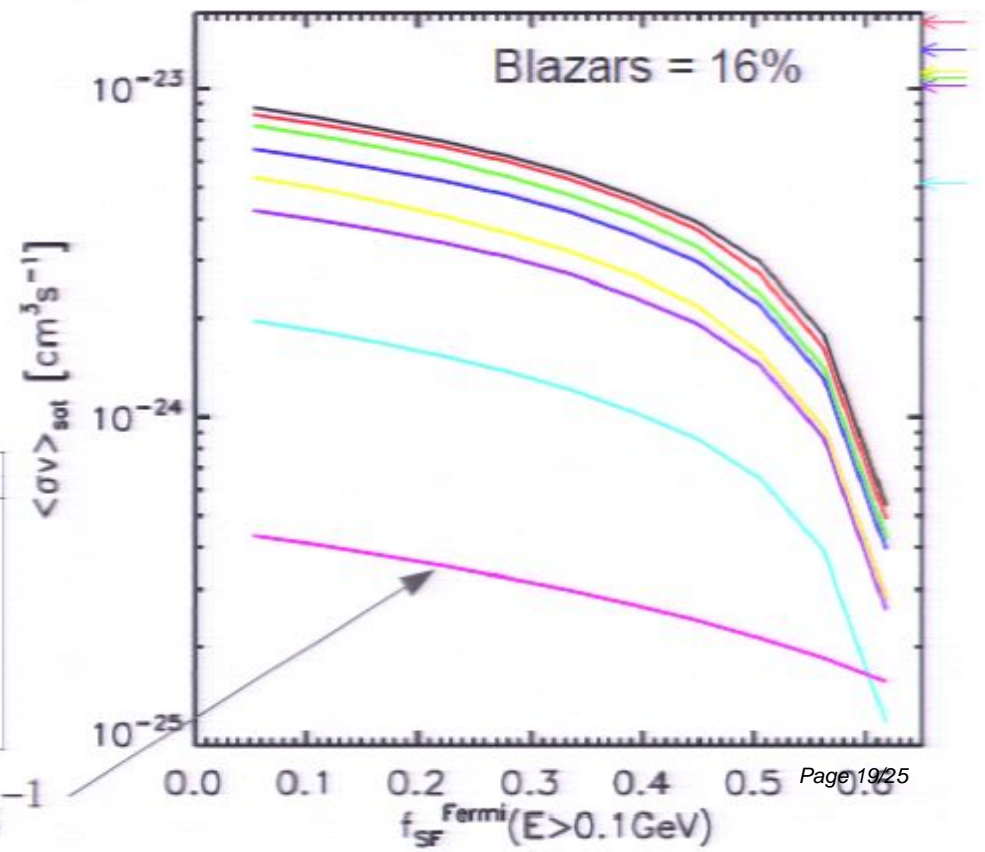
- New force carrier in the “dark sector”
- Annihilation cross section enhanced by a Sommerfeld mechanism:
 
$$\langle \sigma v \rangle = \langle \sigma v \rangle_0 S(\sigma_{\text{vel}})$$
- Correct relic density
- Fit to the cosmic ray excesses measured by PAMELA and Fermi
- Allowed by bounds on  $S_{\max}$  from the CMB
- IC contribution dominates the photon yield

# Sommerfeld-enhanced models fitting the cosmic ray excesses



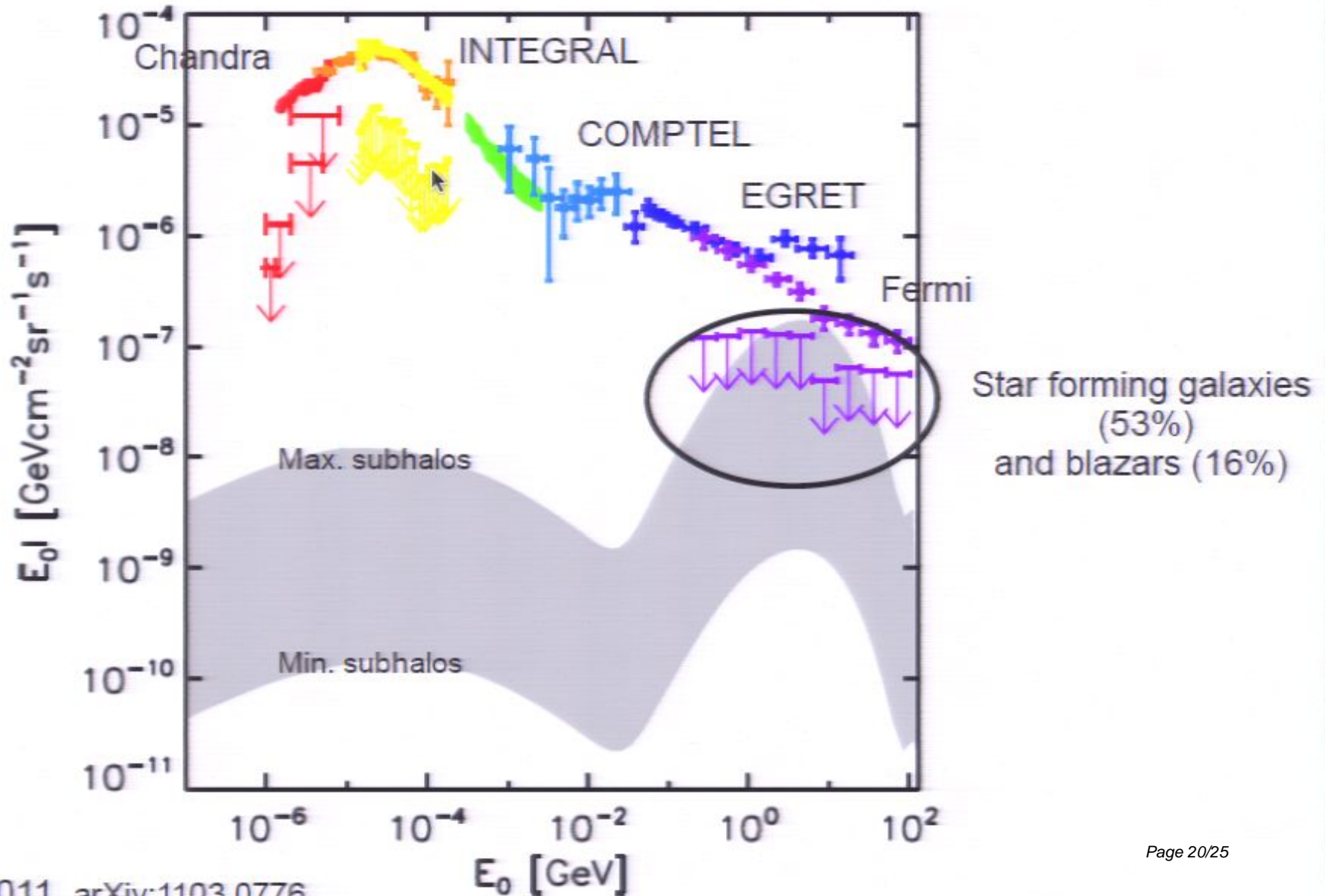
- Minimum contribution from subhalos
- SFG = 53% of EGB ( $E > 1 \text{ GeV}$ )
- Blazars = 16% of EGB ( $E > 1 \text{ GeV}$ )

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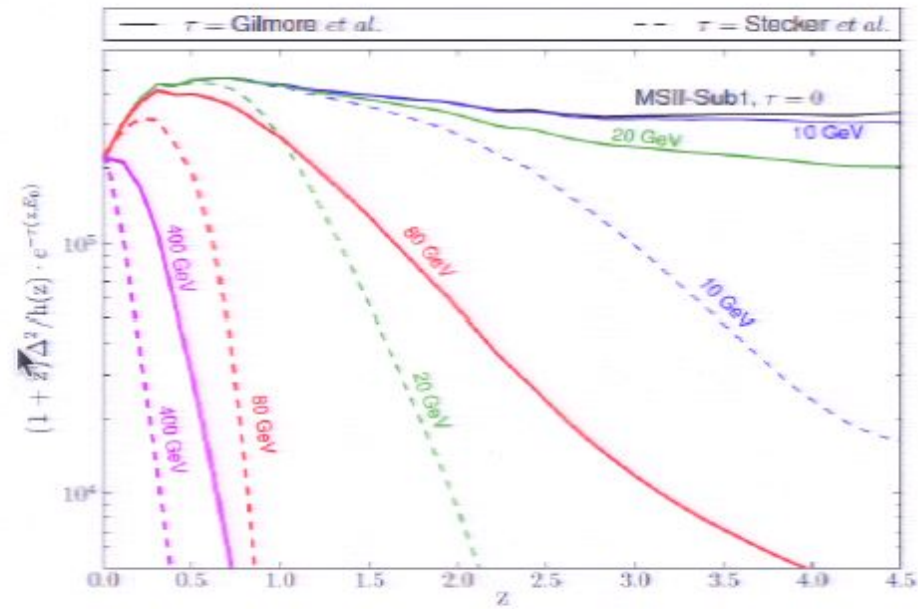


# Constraints on particle physics models

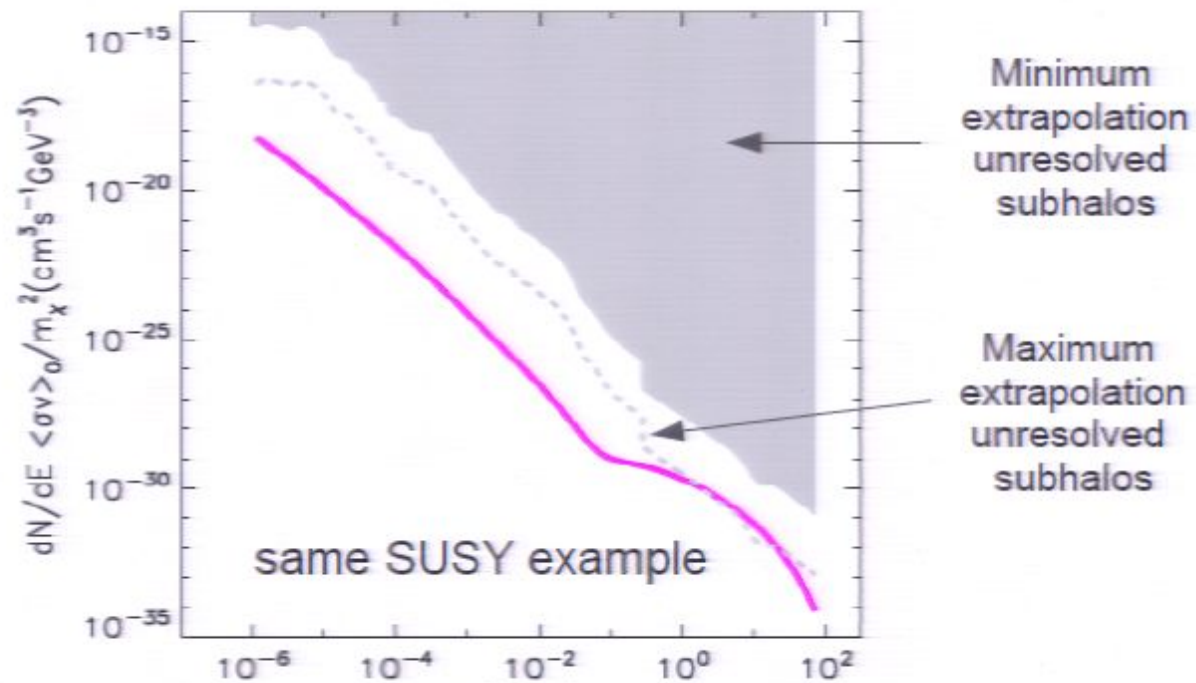
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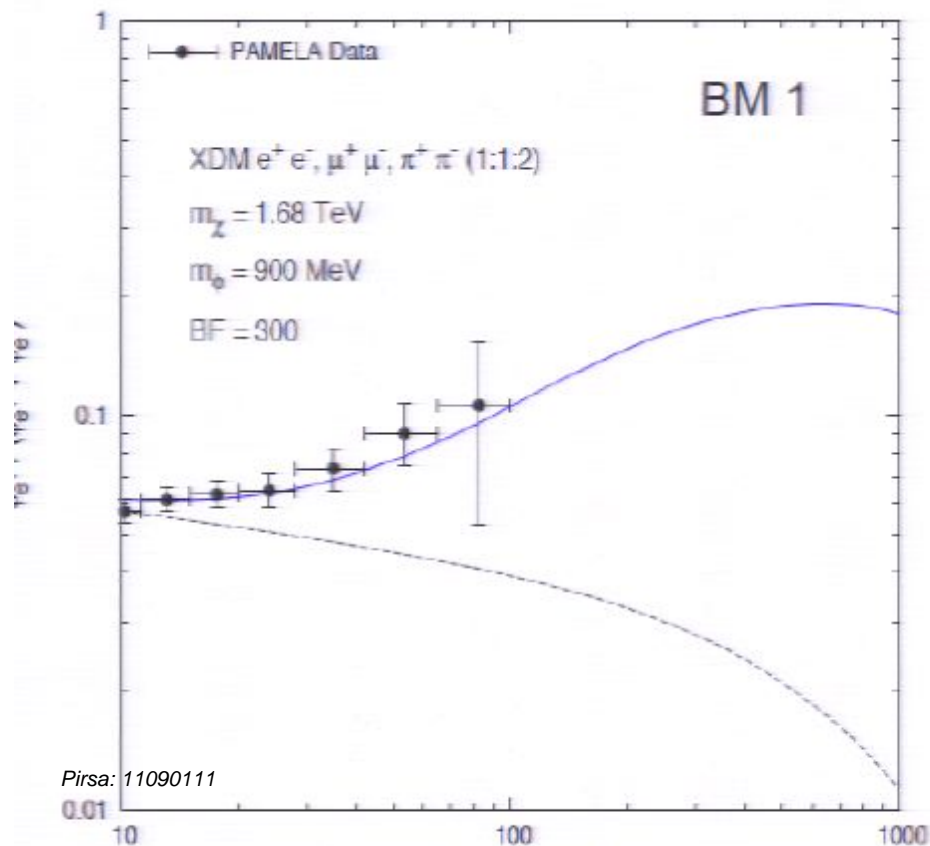


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 Abdo et al. 2010



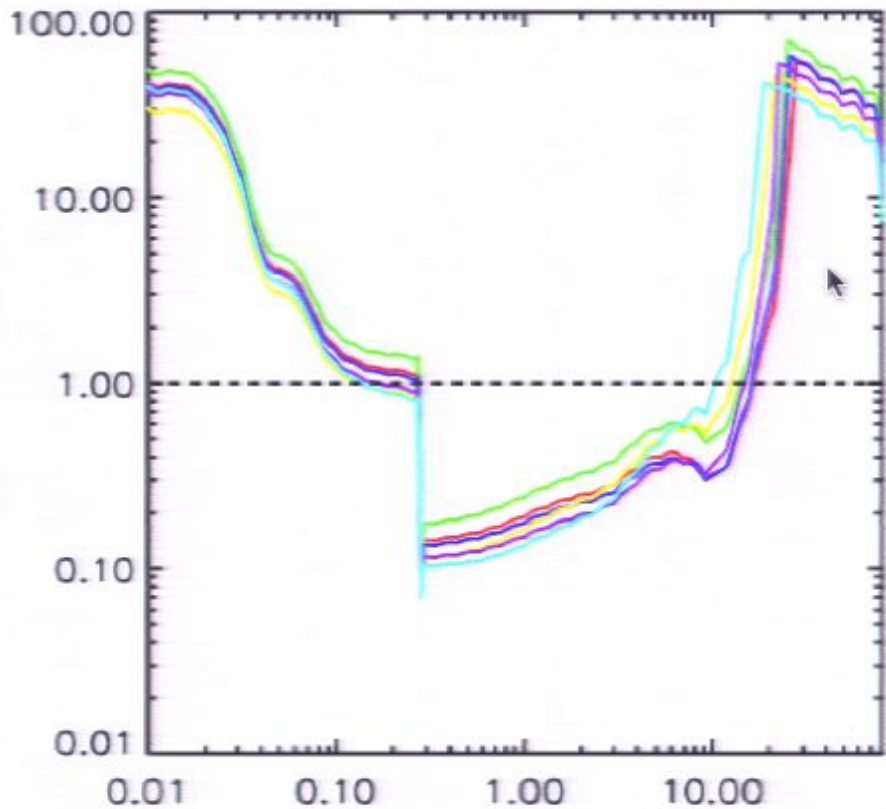
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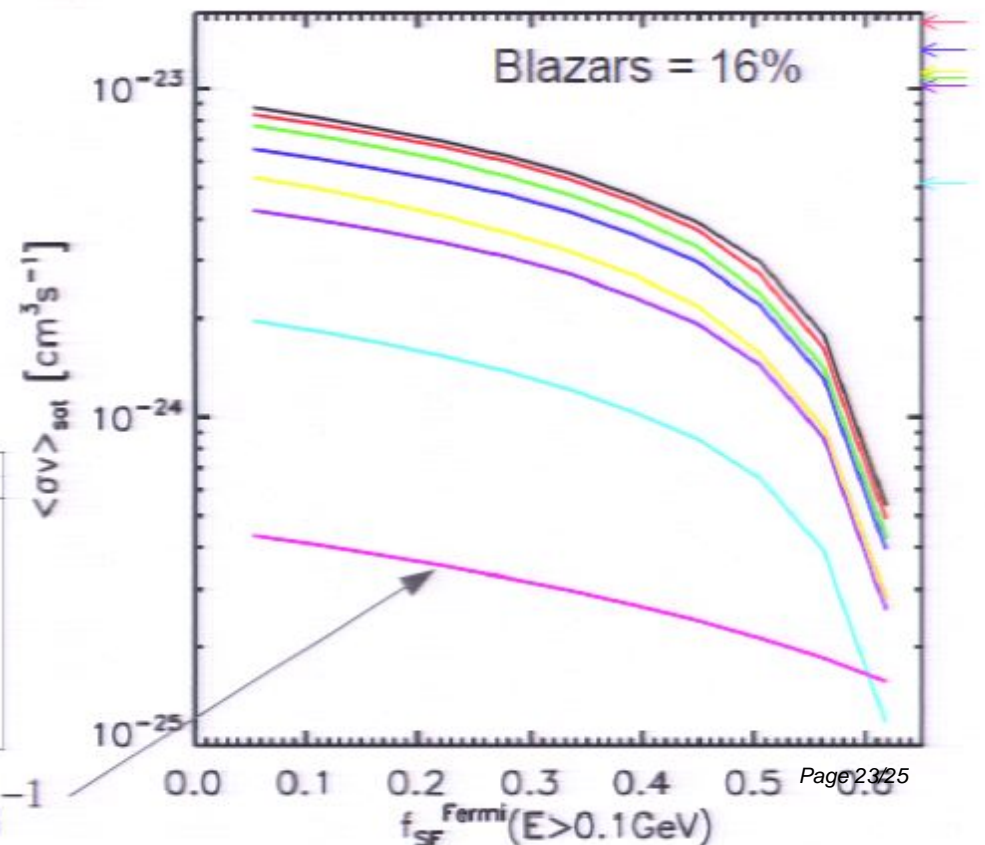
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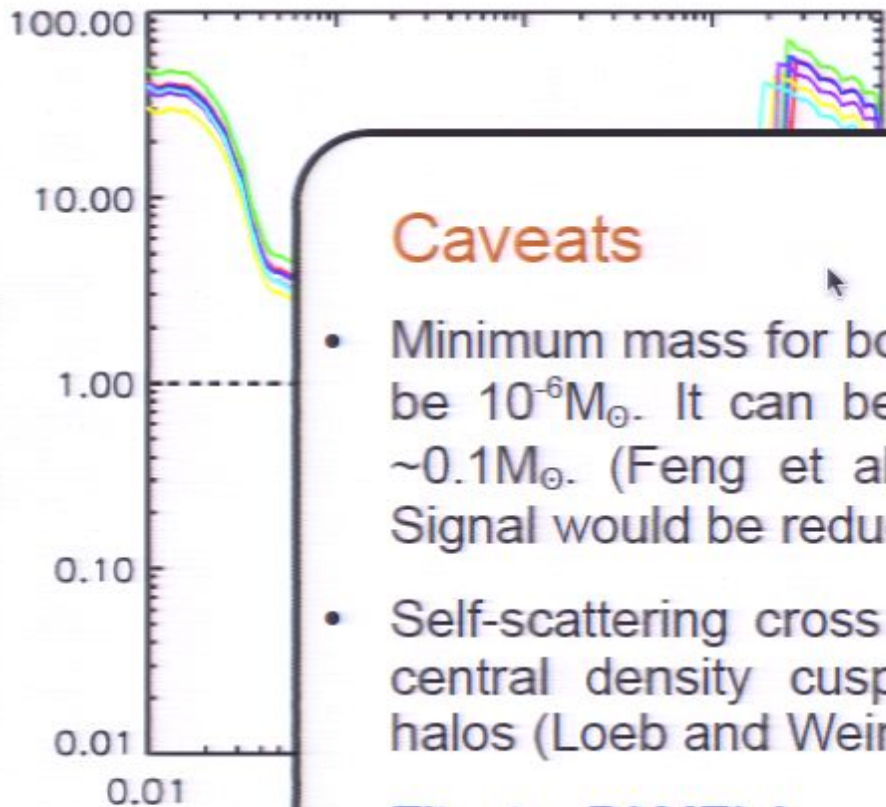


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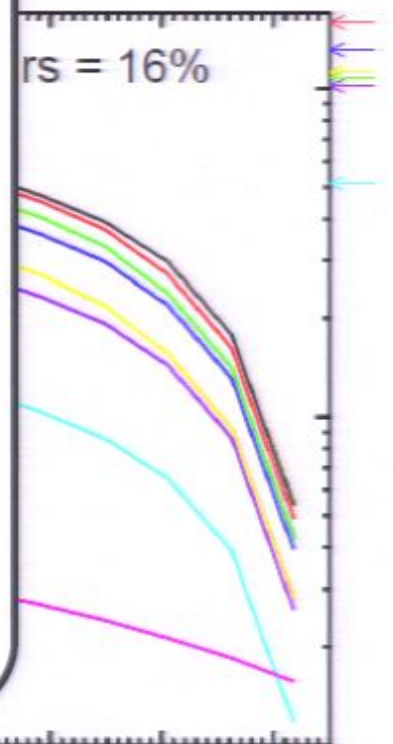
# Sommerfeld-enhanced models fitting the cosmic ray excesses



- Minimum contribution from subhalos
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## Caveats

- Minimum mass for bound halos was assumed to be  $10^{-6} M_{\odot}$ . It can be higher for these models  $\sim 0.1 M_{\odot}$ . (Feng et al. 2010, Bringmann 2009). Signal would be reduced by a factor of  $\sim 2$ .
- Self-scattering cross section could deplete the central density cusps and disrupt low-mass halos (Loeb and Weiner 2011).
- Fits to PAMELA positron excess taking into account local substructure weakens the constraints (Tracy's talk).



benchmark no.	Annihilation Channels
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2	1:1:2 $e^{\pm} : \mu^{\pm}$
3	1:1:1 $e^{\pm} : \mu^{\pm}$
4	1:1:1 $e^{\pm} : \mu^{\pm}$
5	1:1 $e^{\pm} : \mu^{\pm}$
6	$e^{\pm}$ only



# Summary and Conclusions

- Sommerfeld-enhanced models can explain the cosmic-ray anomalies, but they need to be consistent with independent astrophysical constraints: correct relic abundance and CMB already constrain the boost factor to be less ~ few hundred.
- We have obtained predictions from the simulated all-sky maps of the cosmic X- and gamma-ray background from DM annihilation including:
  - Photon yield given by a WIMP model (in situ photons and up-scattered photons of the CMB). Model-independent, can be used for Sommerfeld-enhanced models.
  - Dark matter spatial distribution using Millennium-II simulation, uncertainty of ~2 orders of magnitude in extrapolation to unresolved structures.
- Isotropic component constrained by observations of the cosmic background, and contributions from blazars and star forming galaxies: **although is not as clean as the CMB, it is a powerful tool to constrain the intrinsic properties of dark matter.**