

Title: Dark Matter Annihilation: From High Redshift to the Galactic Center

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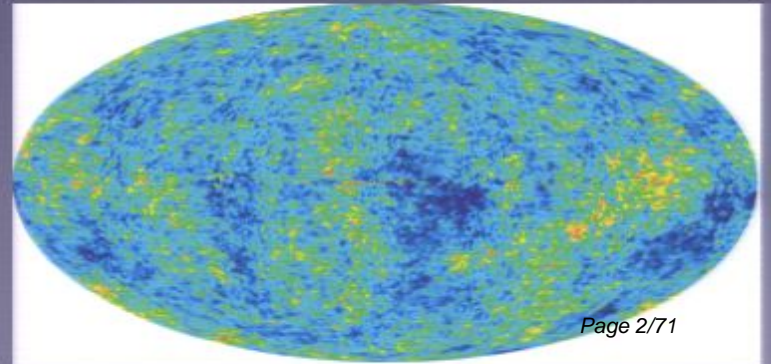
Abstract: The existence of dark matter is hardly in doubt, yet astrophysicists continue to search in vain for any non-gravitational signals of it. In the case of weakly interacting massive particle (WIMP) models, ongoing annihilation or decay of WIMPs to Standard Model particles could provide observable signals, e.g. as excess gamma rays in the center of the Milky Way or as excess ionization at high redshift.

I will present our latest results on the most rigorous constraint from astrophysics: the effect of WIMP annihilation on the ionization history of the Universe, as recorded in the CMB.

Searching for Dark Matter in the CMB: A Compact Parameterization of Energy Injection from New Physics

Doug Finkbeiner, Silvia Galli, Tongyan Lin, &
Tracy Slatyer

arXiv:1109.????



What astronomical / cosmological signals might come from dark matter?

- PAMELA positrons
- Fermi e^+e^-
- INTEGRAL 511 keV line(?)
- Excess microwaves/gammas in GC, dwarf galaxies, diffuse background...
- Effects on the CMB?

Motivation for looking at the CMB

- The CMB, together with LSS and SNe Ia, provides persuasive evidence of the existence of dark matter.
- This evidence comes from things like $H(z)$, d_A , and the growth of structure. This can tell us about CDM/HDM, but little about the particle nature of the DM.
- If the DM is a WIMP and if the WIMP annihilates appreciably, then there is more to be learned from the CMB!

The CMB originates at the time of “last scattering,” when the Universe first becomes transparent.

($z \approx 1100$ $t \approx 380,000$ yr)

- WIMP annihilation (or decay) can inject high-energy particles and photons into the gas at $z \sim 100-1000$.
- This energy modifies the “recombination” history of the Universe (really, *ionization fraction* as a function of time).
- The CMB power spectrum is sensitive to this change in the ionization history.

By measuring the CMB we can:

- Search for departures from the “standard recombination” scenario,
- Place limits on energy injection at $z=100-1000$,
- Translate these limits to exclusions in WIMP parameter space (e.g. the cross-section / mass plane, etc.)

Note that these results are quite robust -- we understand recombination and the CMB *quite well*, and the measurements are good and rapidly improving!

There is less “wobble room” in CMB constraints at $z=100-1000$ than constraints based on e.g. annihilation in late-time halos.

Selected key papers:

2004: Chen & Kamionkowski - calculated effect of DM decay on recombination history. (to explain high tau in WMAP I)

2005: Padmanabhan & Finkbeiner - repeated calculation for WIMP annihilation, obtained limits from WMAP.

2009: Galli, Iocco, Bertone, & Melchiorri - computed limits from WMAP 5 on Sommerfeld-enhanced DM.

2009: Slatyer, Padmanabhan, & Finkbeiner - careful calculation of deposition efficiency of WIMP annihilation energy as a function of z , $f(z)$. Computed actual limits for 42 benchmark WIMP masses / annihilation channels.

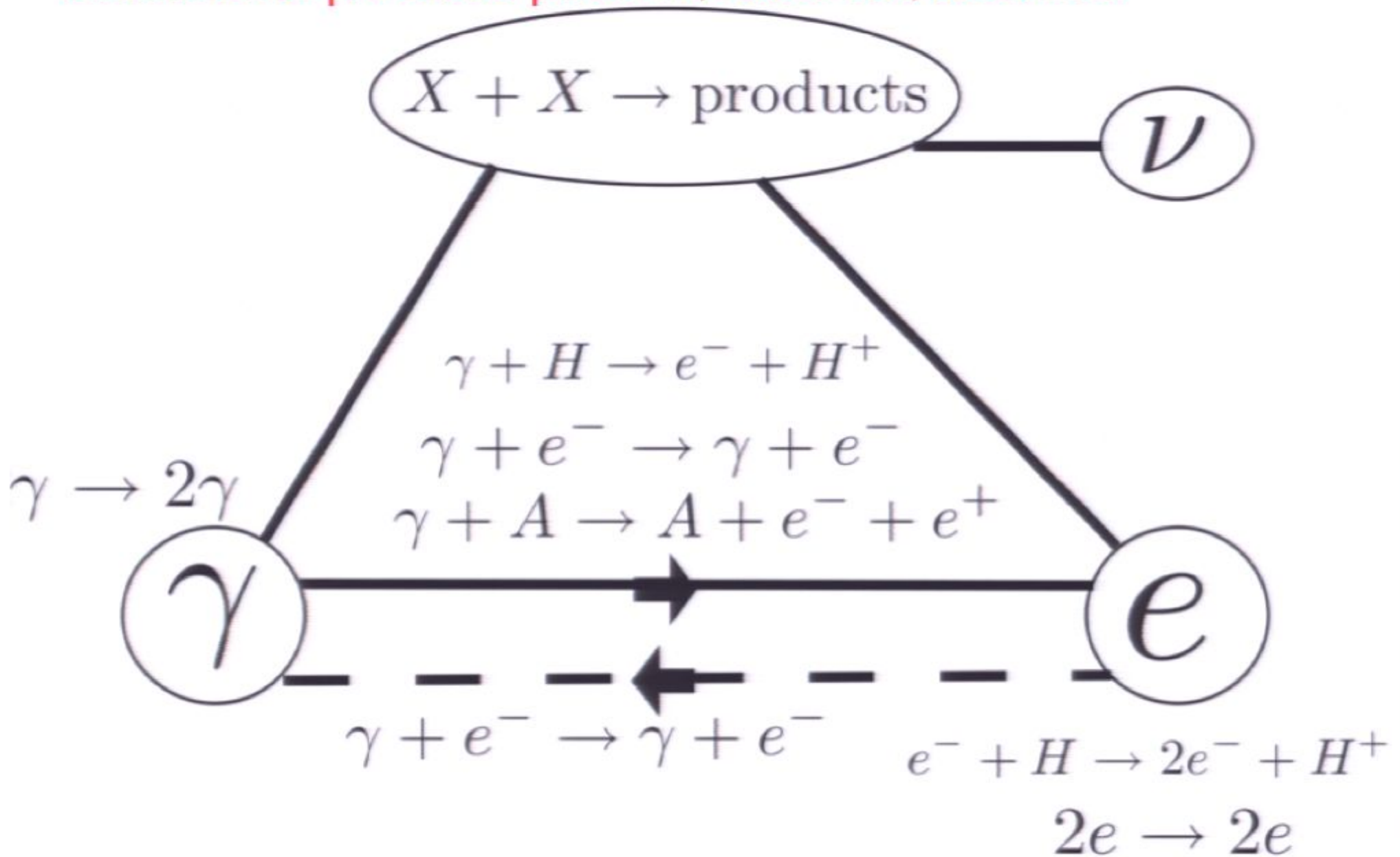
Recent papers:

2011: Hütsi, Chluba, Hektor, & Raidal - Focus on light DM case, generate $f(z)$ curve appropriate for light WIMPs, use WMAP 7.

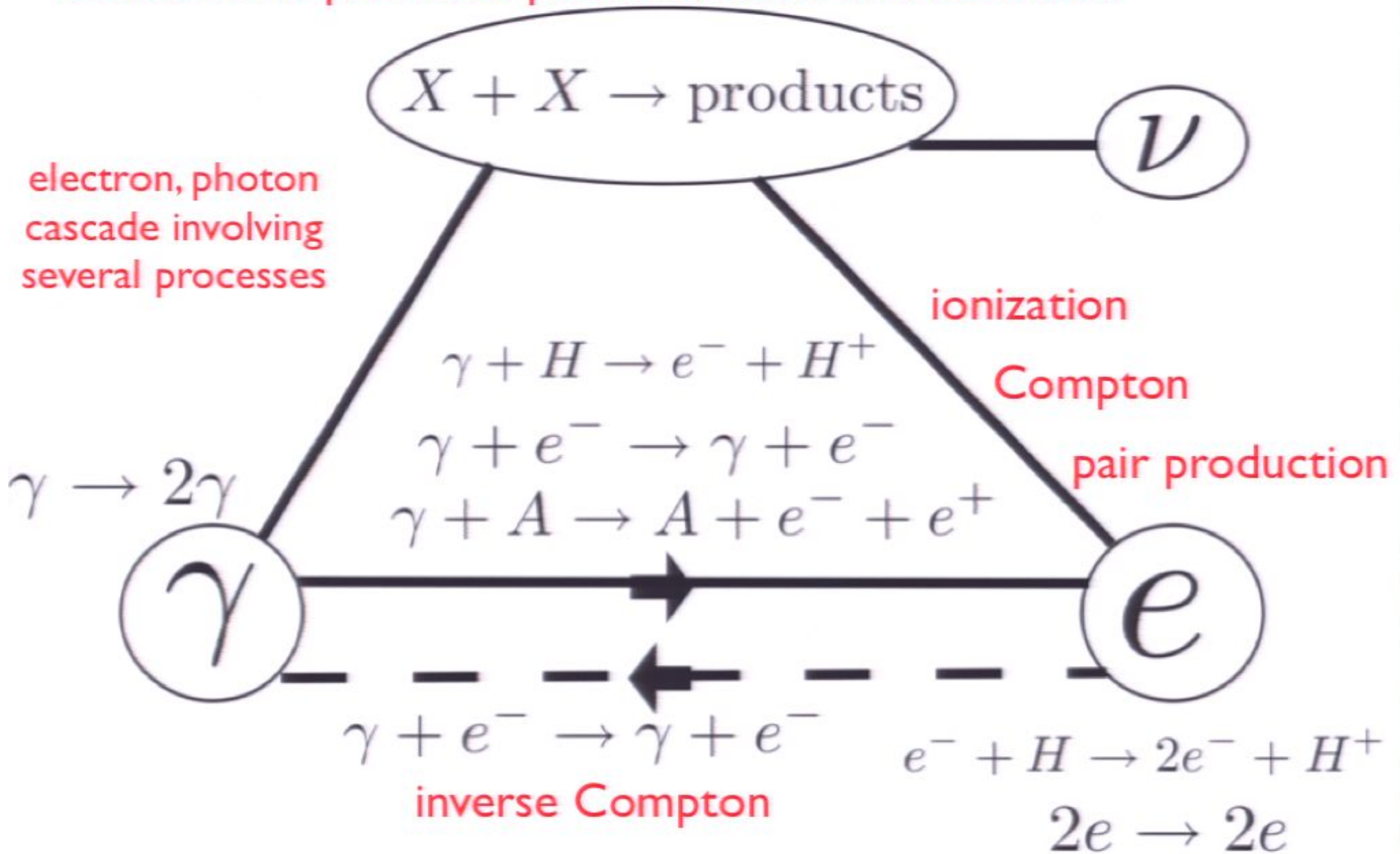
2011: Galli, Iocco, Bertone, & Melchiorri - derive latest limits from WMAP 7 and ACT, use $f(z)$ from Slatyer et al.

2011: Finkbeiner, Galli, Lin, & Slatyer - introduce PCA formalism for robust model-independent constraints.

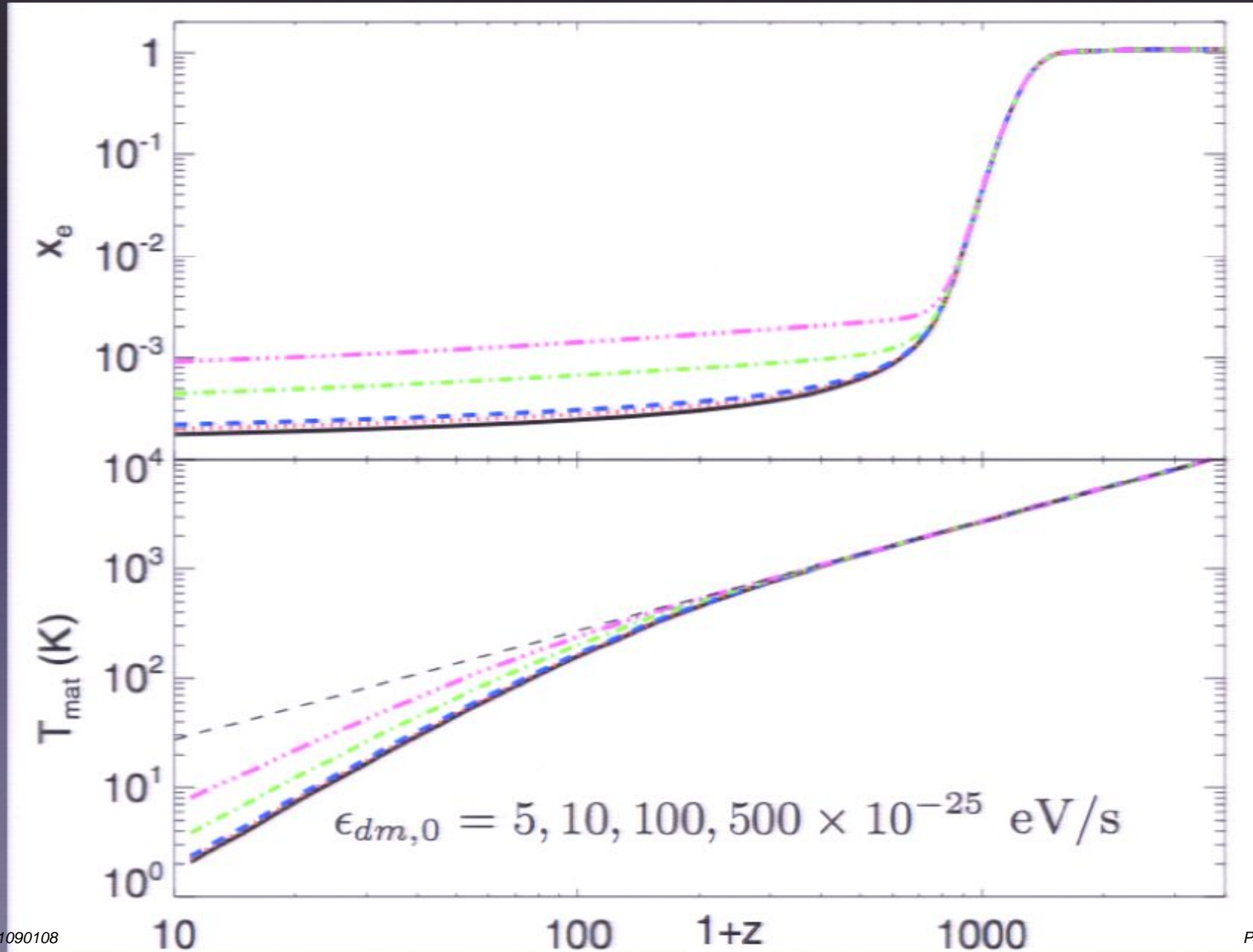
Annihilation produces photons, electrons, neutrinos



Annihilation produces photons, electrons, neutrinos

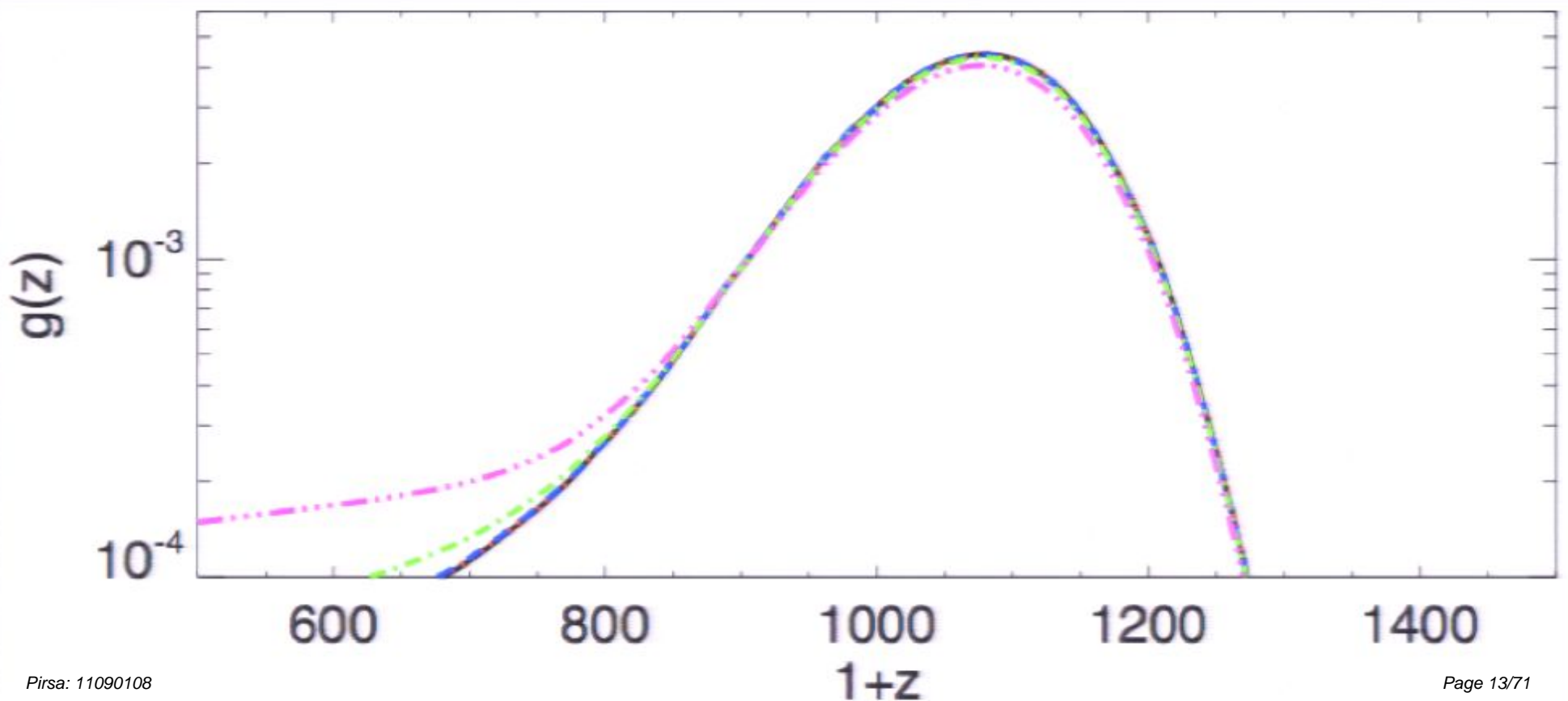


Ionization fraction (x_e) and gas temperature change...



... and this changes the visibility function ...
(= the distribution function of the last scattering redshift of CMB photons)

$$g(z) \equiv \tau'(z)e^{-\tau(z)}$$




What effect does this change in $g(z)$ have?

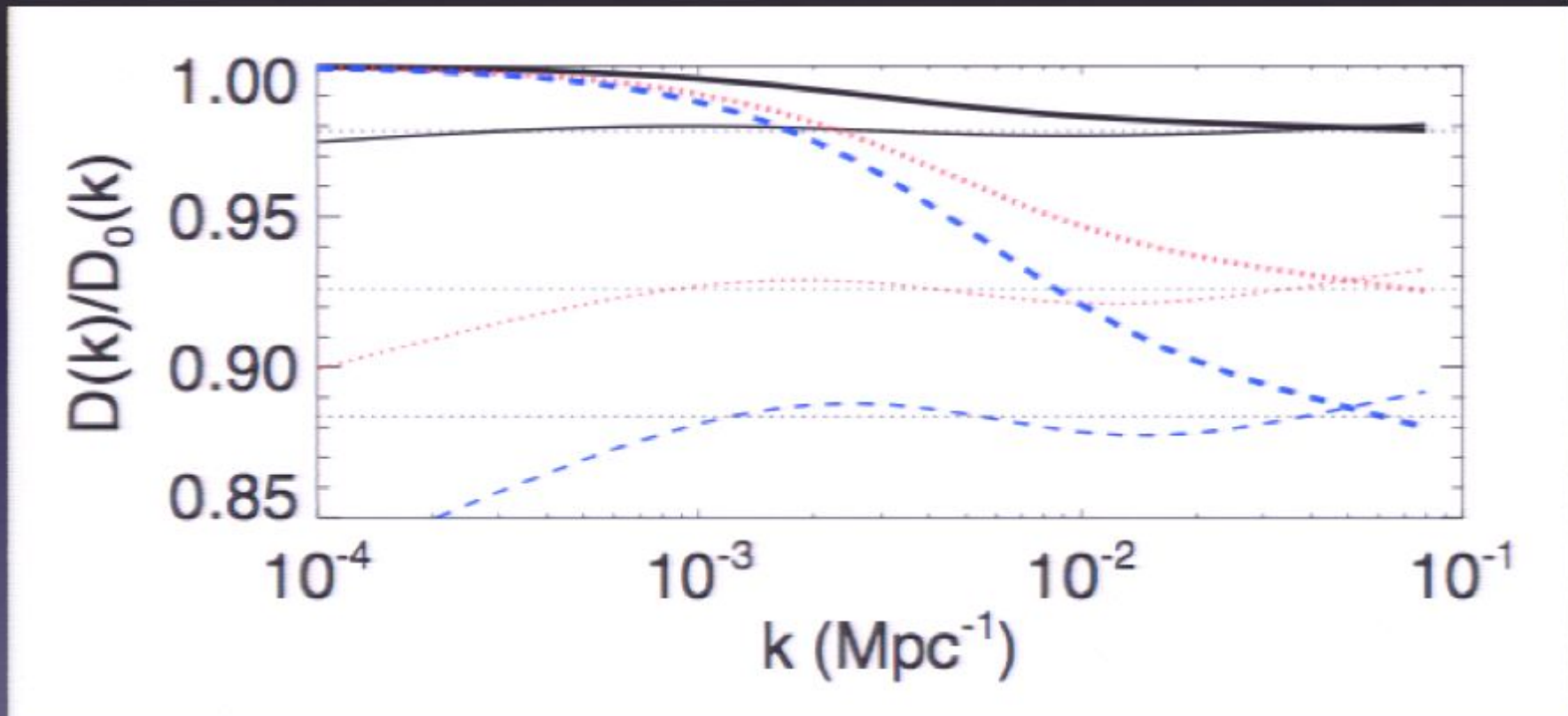
$$C_l = 4\pi A \int_0^\infty d(\ln k) k^{n_s} D^2(k) T^2(k)$$

$T(k) \sim \text{constant}$, $D(k)$ = damping function, k = wavenumber

$$D(k) = \int dz g(z) \exp\left(-\frac{k^2}{k_D^2(z)}\right)$$

$$\frac{1}{k_D^2} = \int_z^\infty dz \frac{c}{H^2(z)} \frac{1}{6(1+R)\tau'(z)} \left[\frac{R^2}{(1+R)} + \frac{16}{15} \right]$$


What effect does this change in $g(z)$ have?



Changing $g(z)$ mostly changes $D(k)/D_0(k)$.

The CMB gets damped like $k^{-\alpha}$


$$n_s \rightarrow n_s + 2\alpha$$

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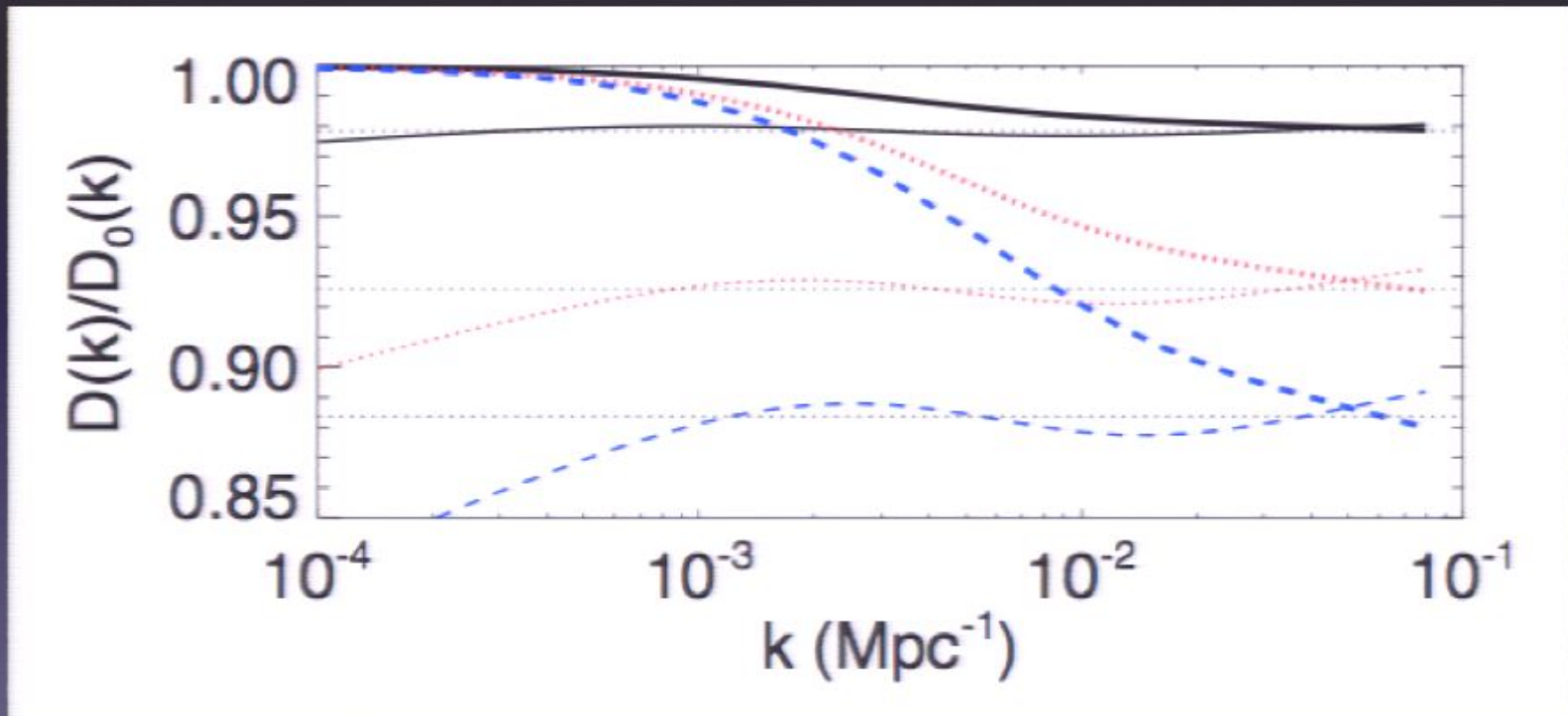
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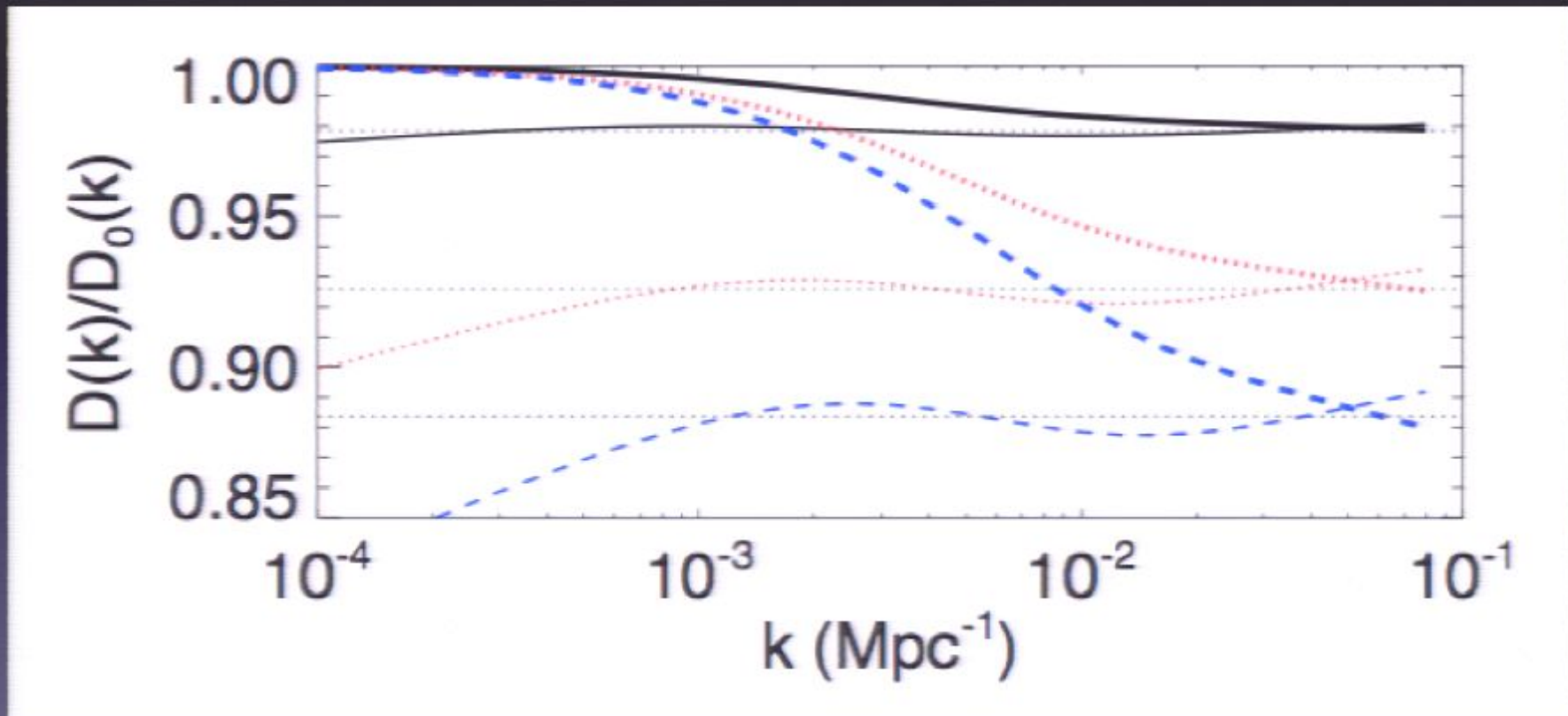
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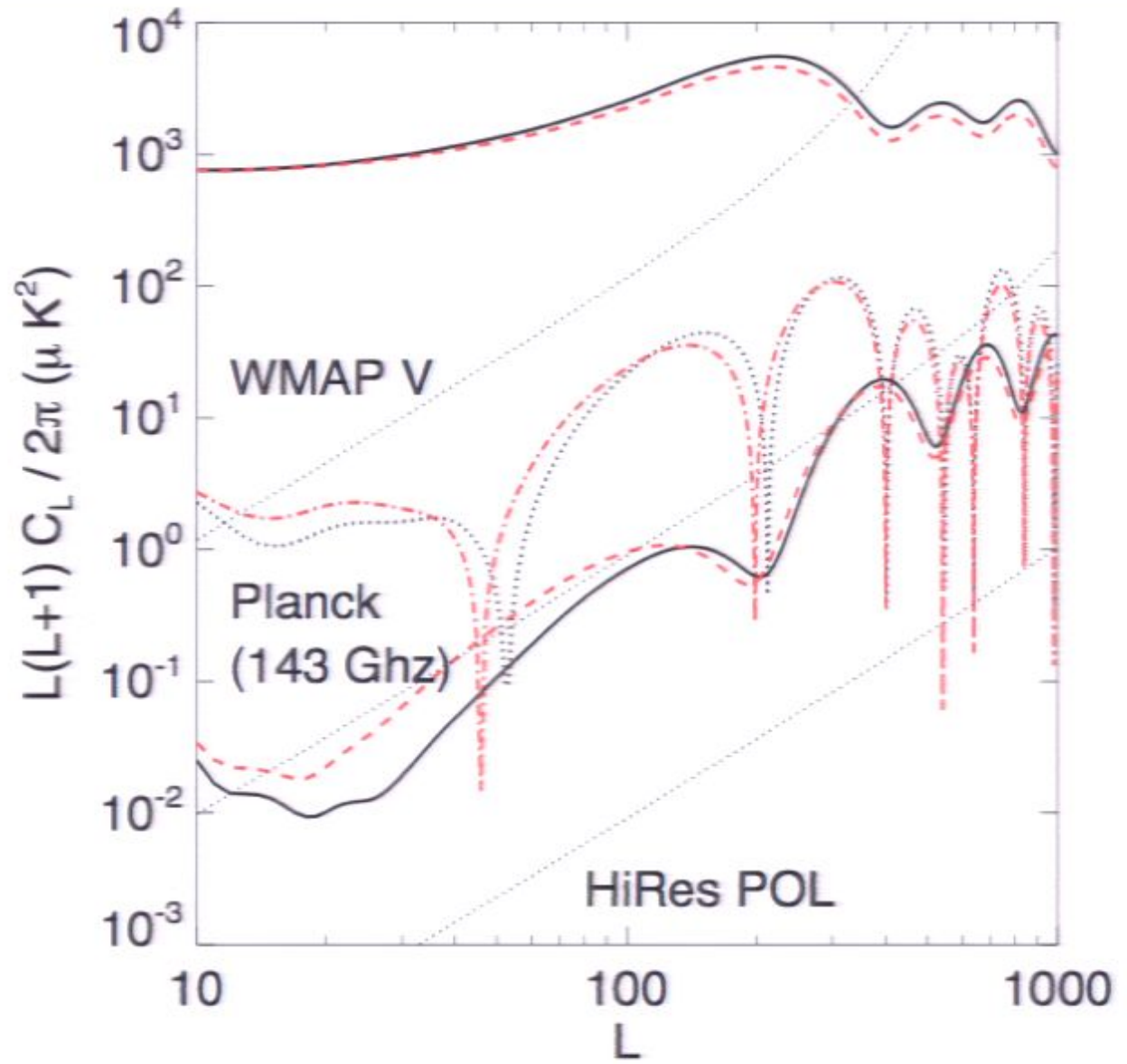


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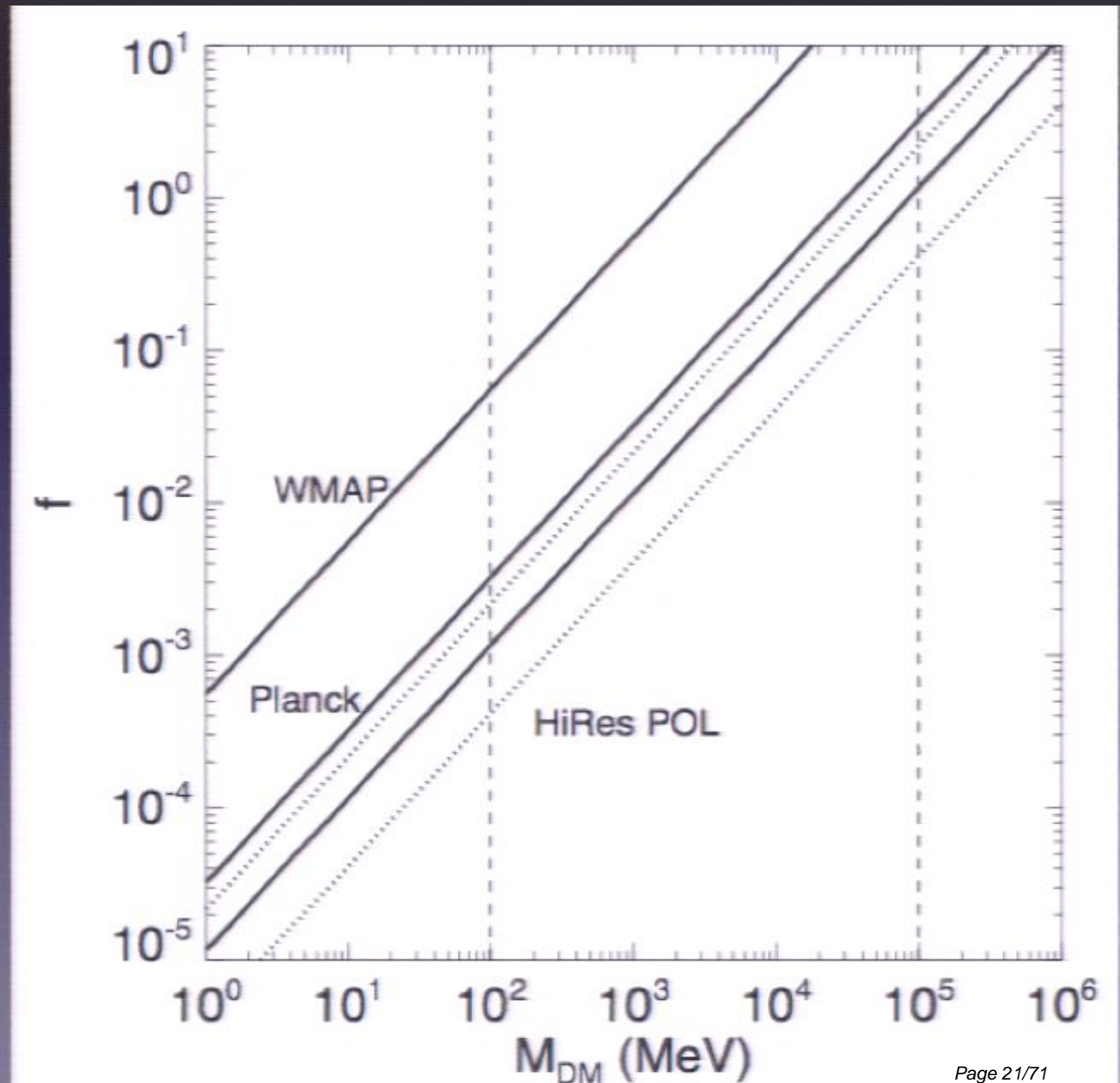
... and increased scattering at $z \sim 600$ modifies the power spectrum.



Constraints in f / M
plane. (for thermal
relic Xsec)

f is a “fudge factor”
parameterizing
energy deposition
efficiency.

$f = 1$ is “on the spot”
approximation



Cosmology



$$\left(\frac{dE}{dt dV} \right)_{\text{ann}} = p_{\text{ann}}(z) c^2 \Omega_{\text{DM}}^2 \rho_c^2 (1+z)^6$$

$$p_{\text{ann}} = f(z) \langle \sigma v \rangle / m_{\text{DM}}$$



Dark matter model

But what value does f have?

f depends on WIMP mass, annihilation channels, etc.

If all energy is immediately deposited in the gas, $f = 1$.

Any energy to neutrinos, gamma-ray background, etc., $f < 1$.

Values from $0.2 < f < 0.7$ are typical.

PAMELA positrons (Adriani+ 2010):

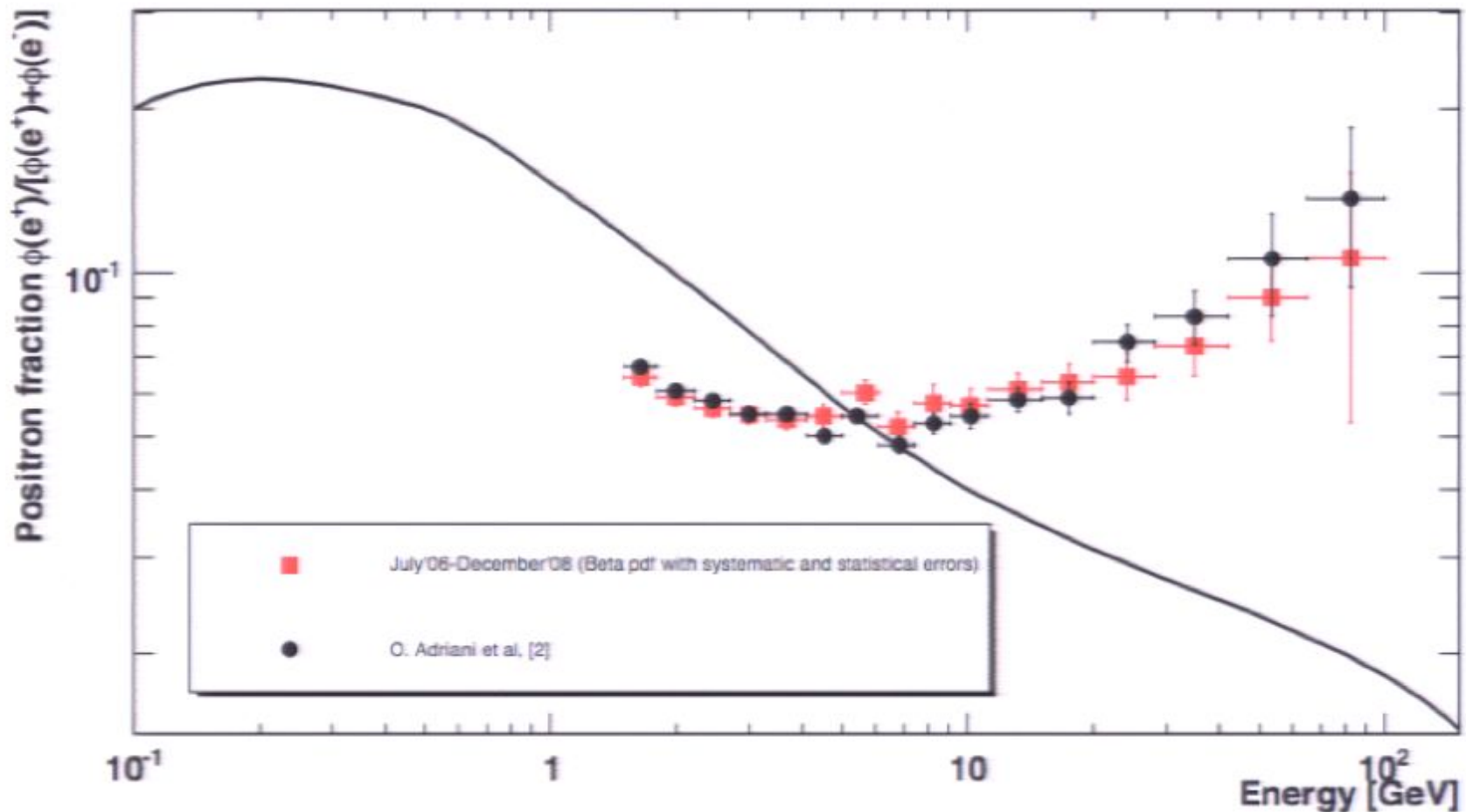


Figure 11: The positron fraction R obtained using a beta-fit with statistical and systematic errors summed in quadrature (red), compared with the positron fraction reported in [2] (black). The solid line shows a calculation by Moskalenko & Strong [40] for pure secondary production of positrons during the propagation of cosmic-rays in the galaxy.

Also built into f is any enhancement to the annihilation cross section.

For example, Sommerfeld-enhanced models motivated by the PAMELA positron spectrum can have $f \gg 1$.

Can these models be ruled out with WMAP?

Accurate calculations of f for benchmark models: The “SPF factor” paper...

CMB Constraints on WIMP Annihilation: Energy Absorption During the Recombination Epoch

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²*Physics Division, Lawrence Berkeley National Laboratory, 1 Cyclotron Rd., Berkeley, CA 94720, USA*

³*Harvard-Smithsonian Center for Astrophysics, 60 Garden St., Cambridge, MA 02138, USA*

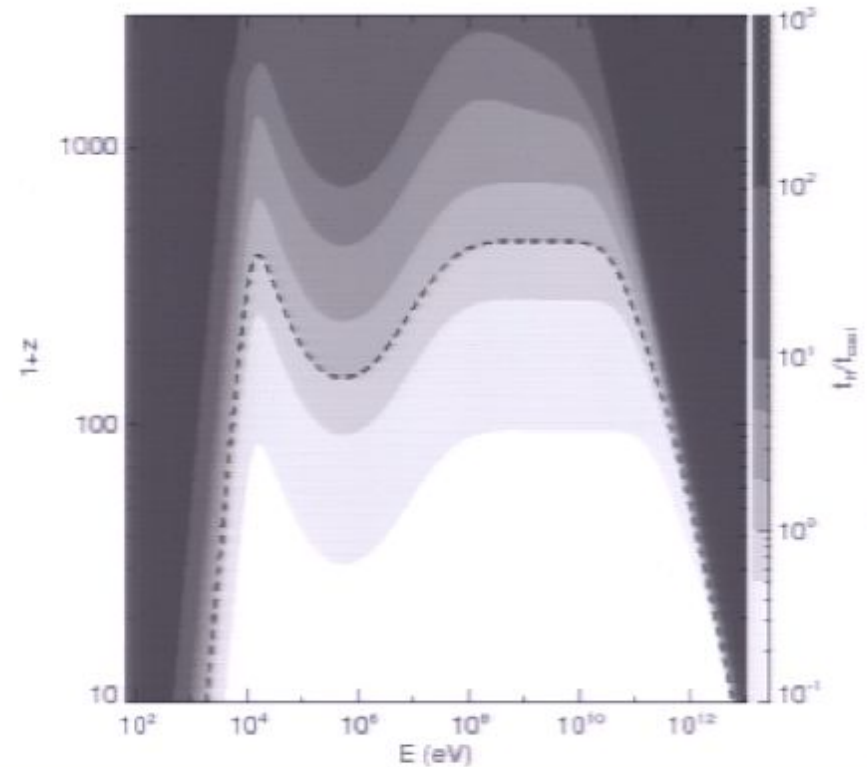
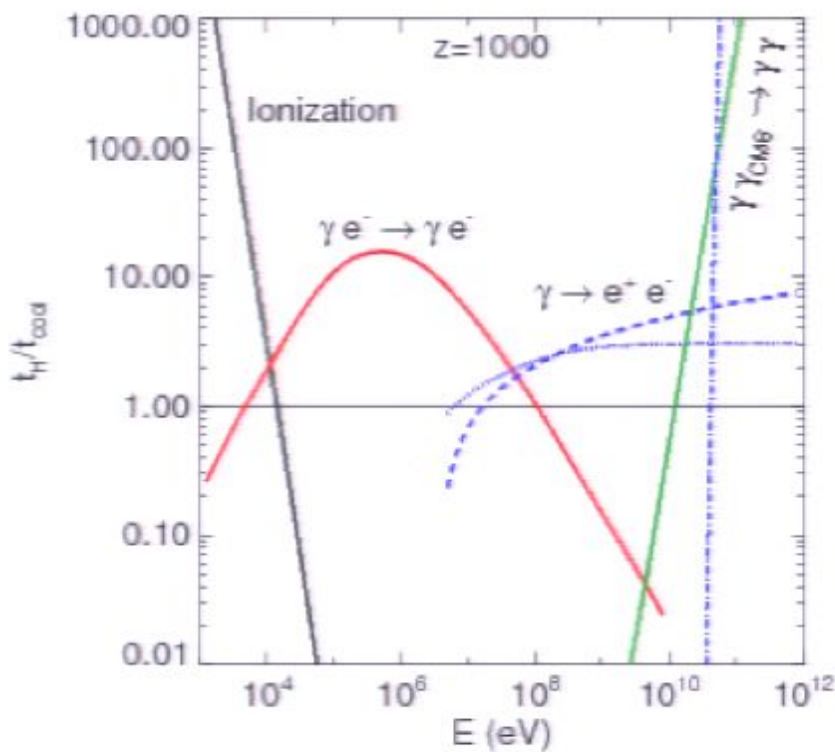
We compute in detail the rate at which energy injected by dark matter annihilation heats and ionizes the photon-baryon plasma at $z \sim 1000$, and provide accurate fitting functions over the relevant redshift range for a broad array of annihilation channels and DM masses. The resulting perturbations to the ionization history can be constrained by measurements of the CMB temperature and polarization angular power spectra. We show that models which fit recently measured excesses in 10-1000 GeV electron and positron cosmic rays are already close to the 95% confidence limits from WMAP. The recently launched Planck satellite will be capable of ruling out a wide range of DM explanations for these excesses. In models of dark matter with Sommerfeld-enhanced annihilation, where $\langle\sigma v\rangle$ rises with decreasing WIMP velocity until some saturation point, the WMAP5 constraints imply that the enhancement must be close to saturation in the neighborhood of the Earth.

Energy transfer from electrons to photons is efficient.

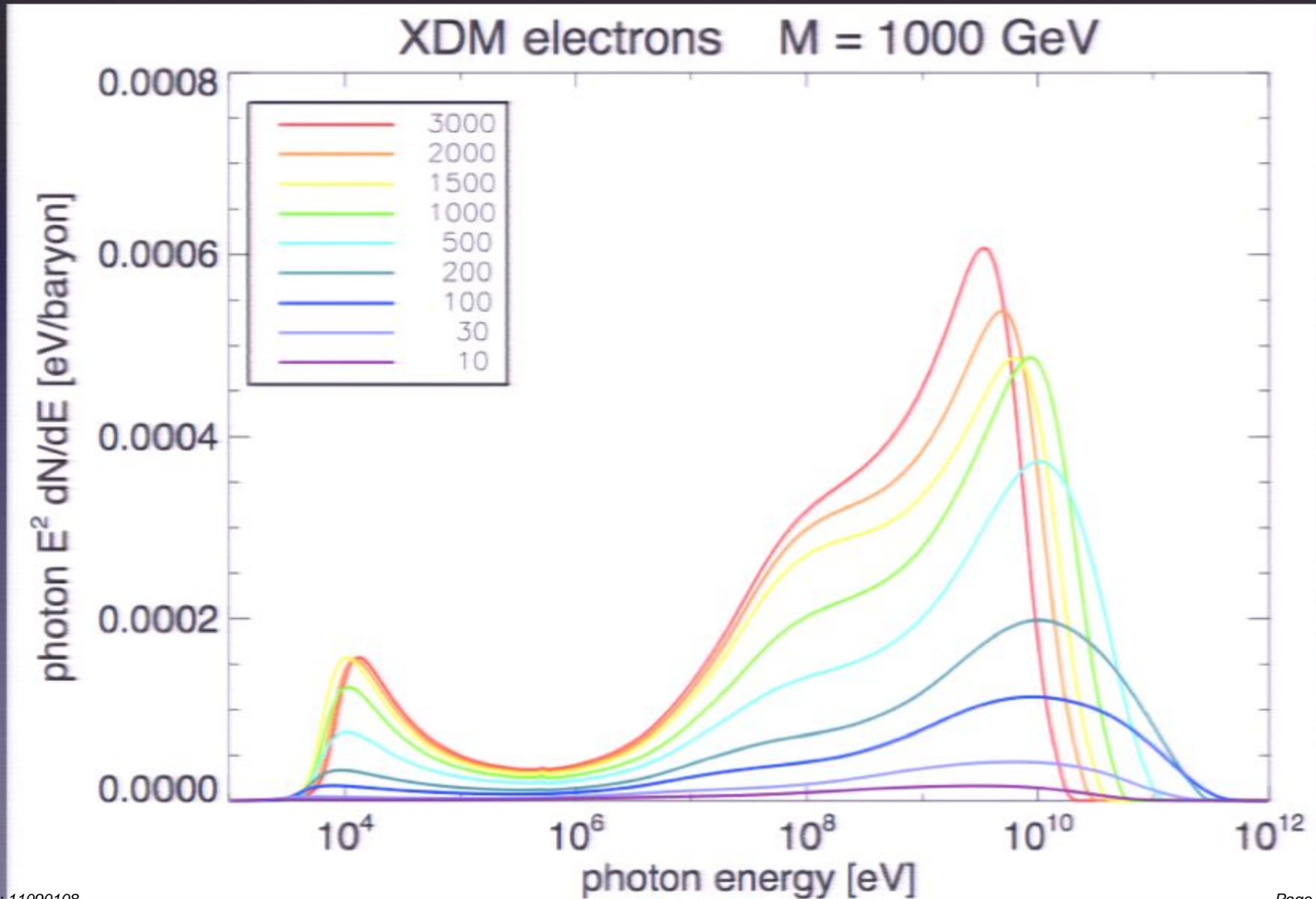
(i.e. essentially instantaneous)

We are mainly concerned with the fate of high energy photons.

There is a z-dependent transparency window:



Annihilation photons not yet thermalized

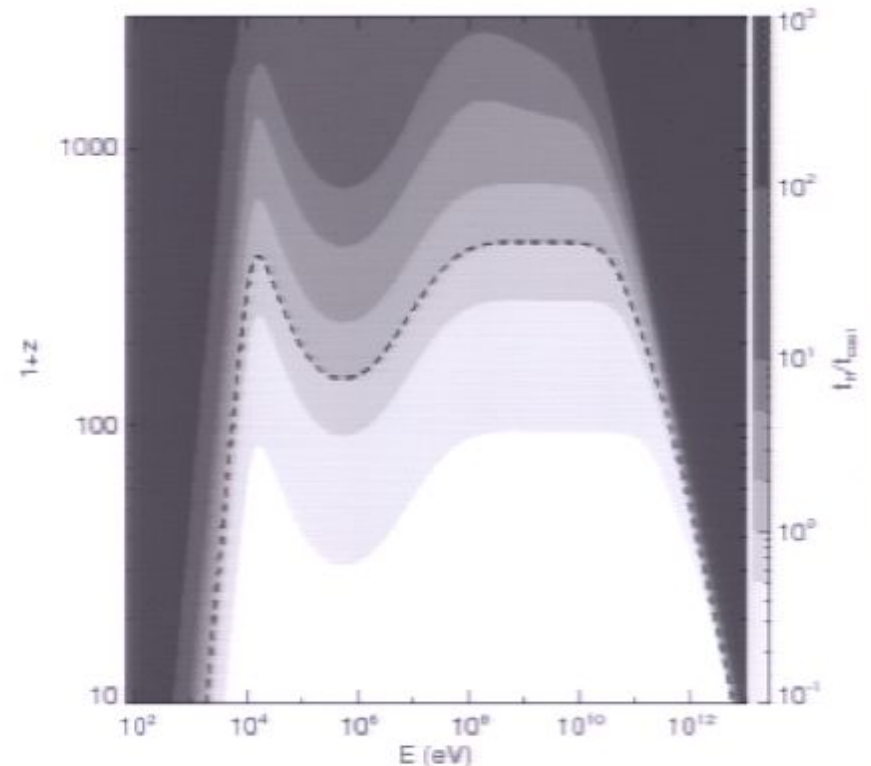
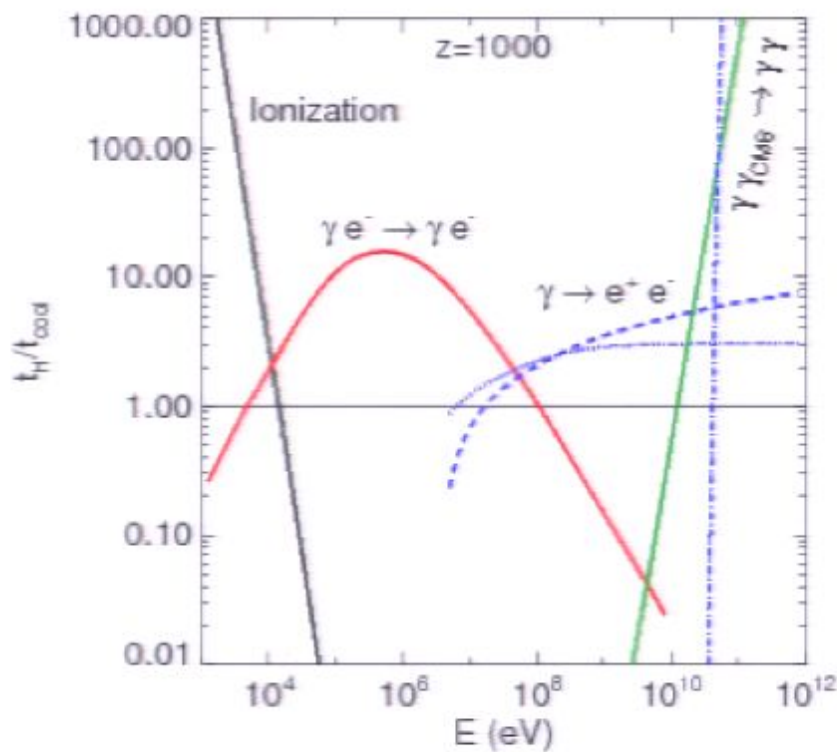


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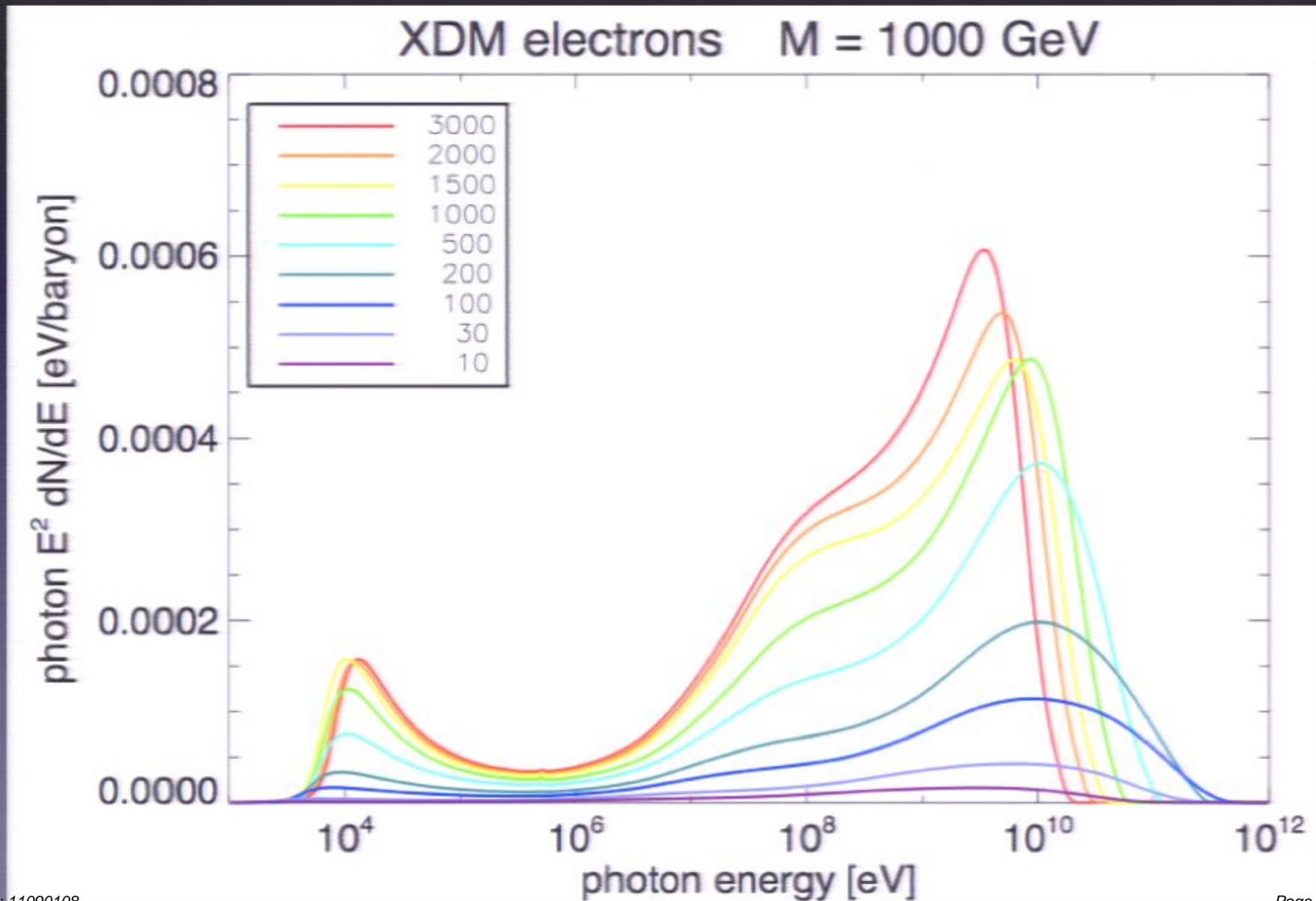
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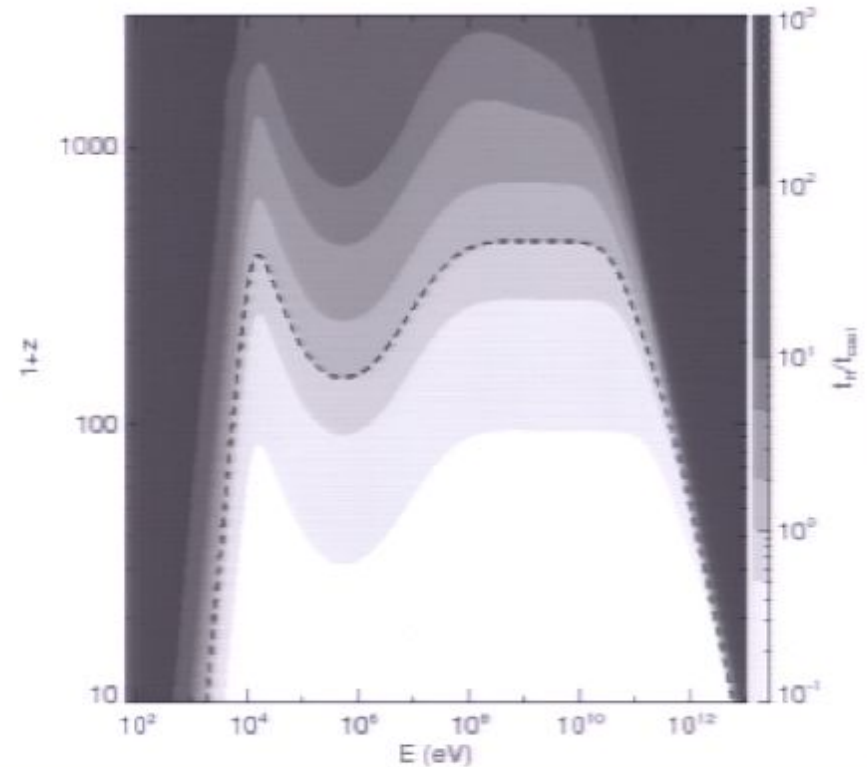
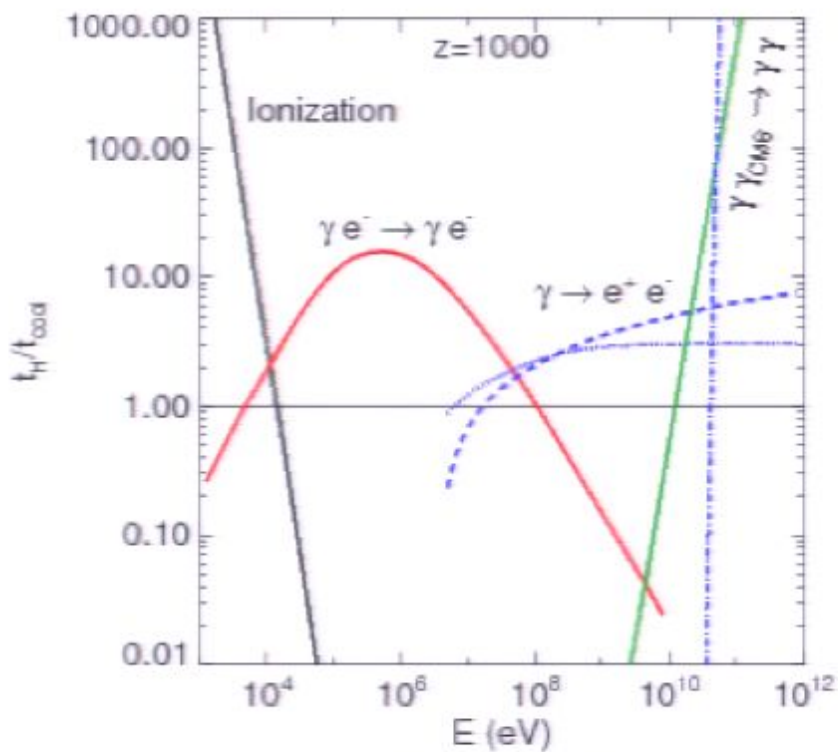


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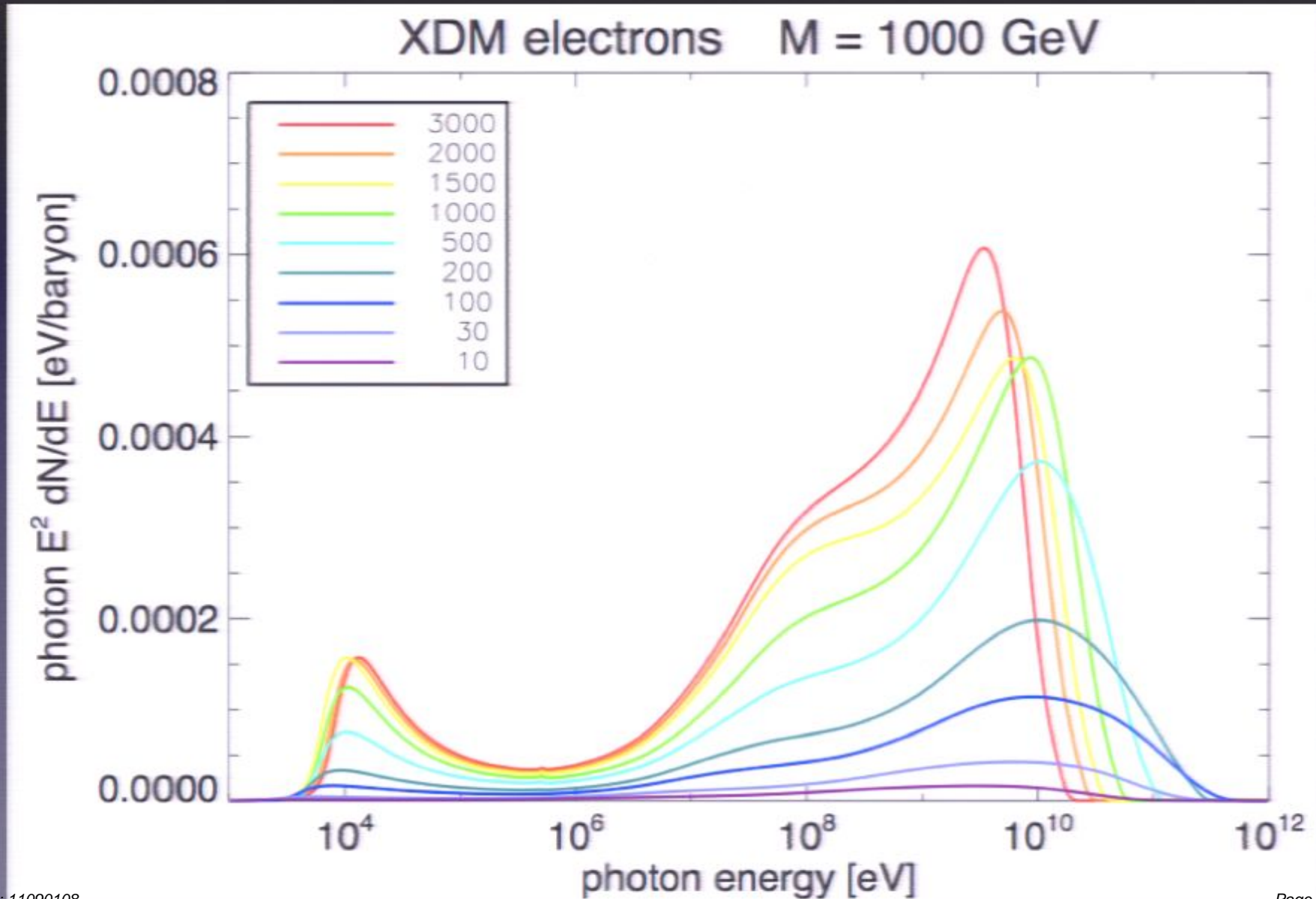


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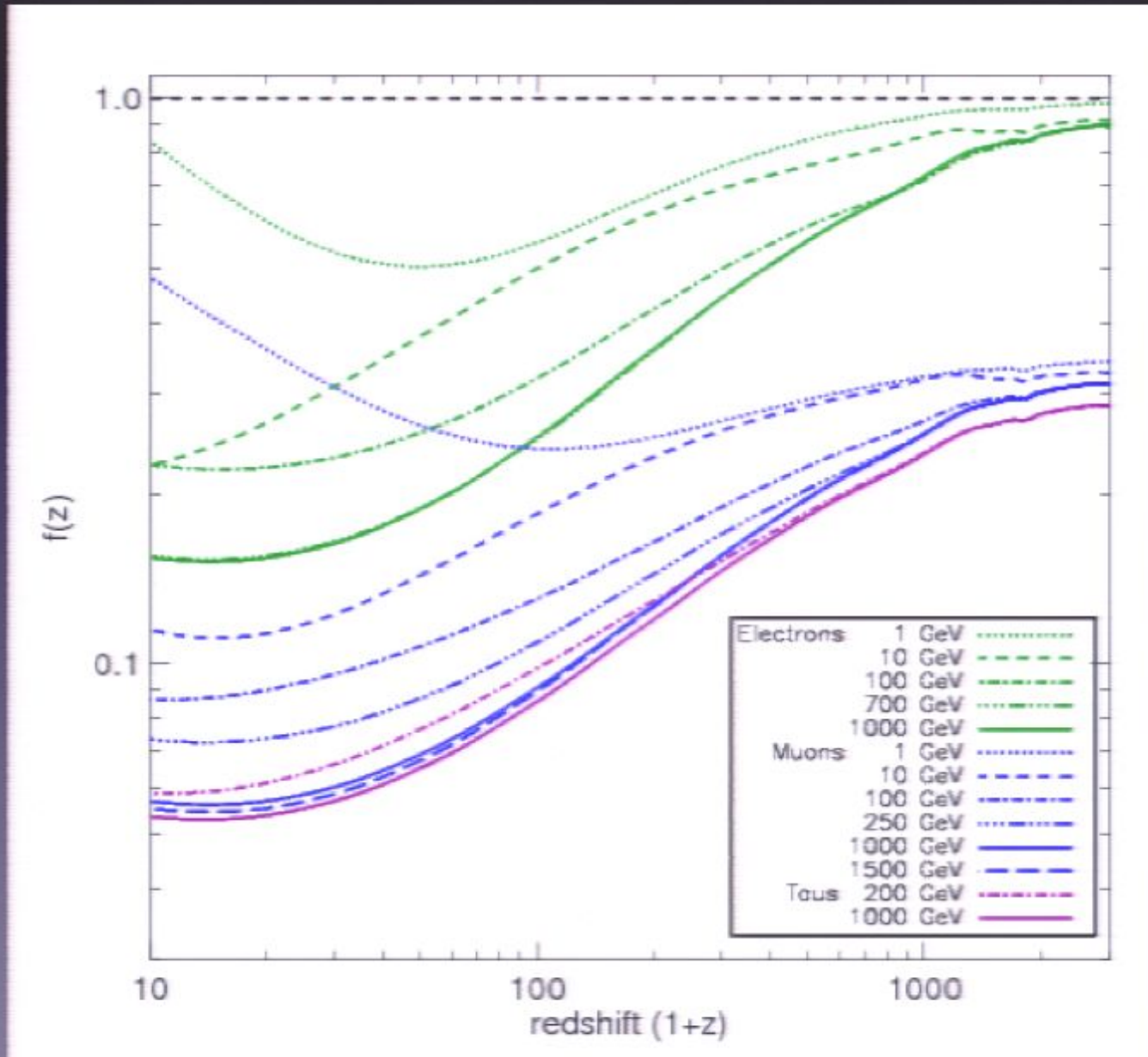
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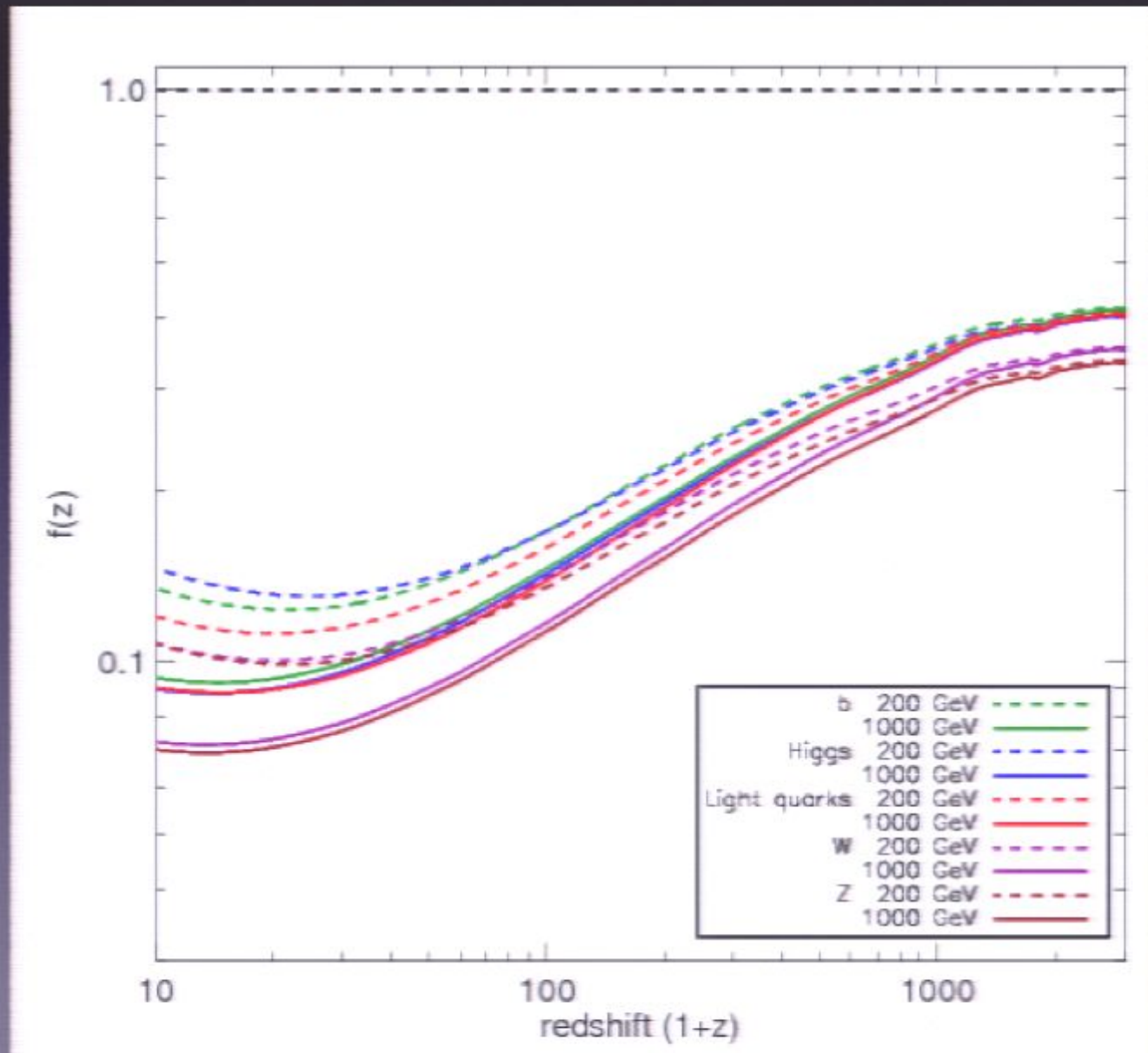
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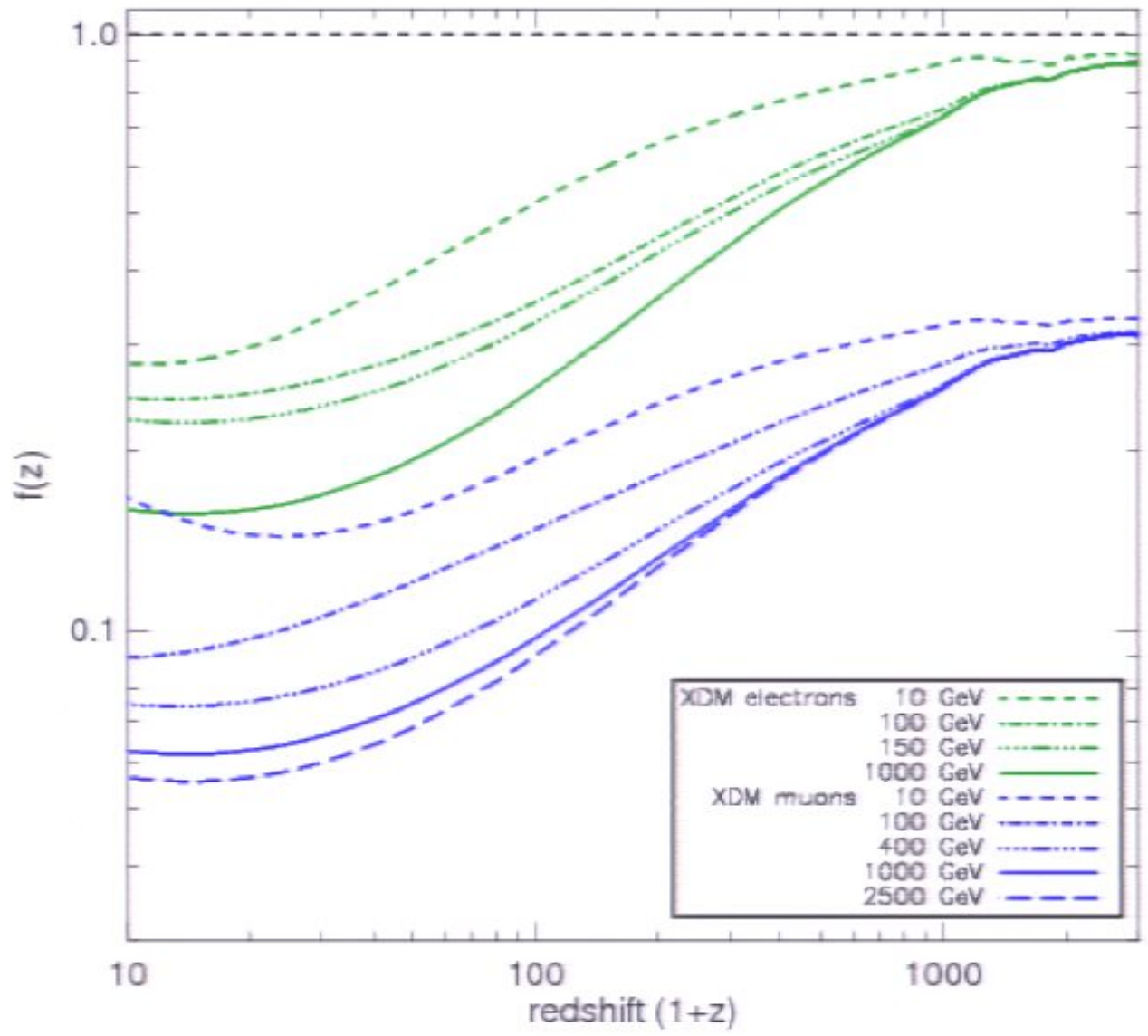
The Slatyer-Padmanabhan-Finkbeiner (SPF) factor, f :



The Slatyer-Padmanabhan-Finkbeiner (SPF) factor.

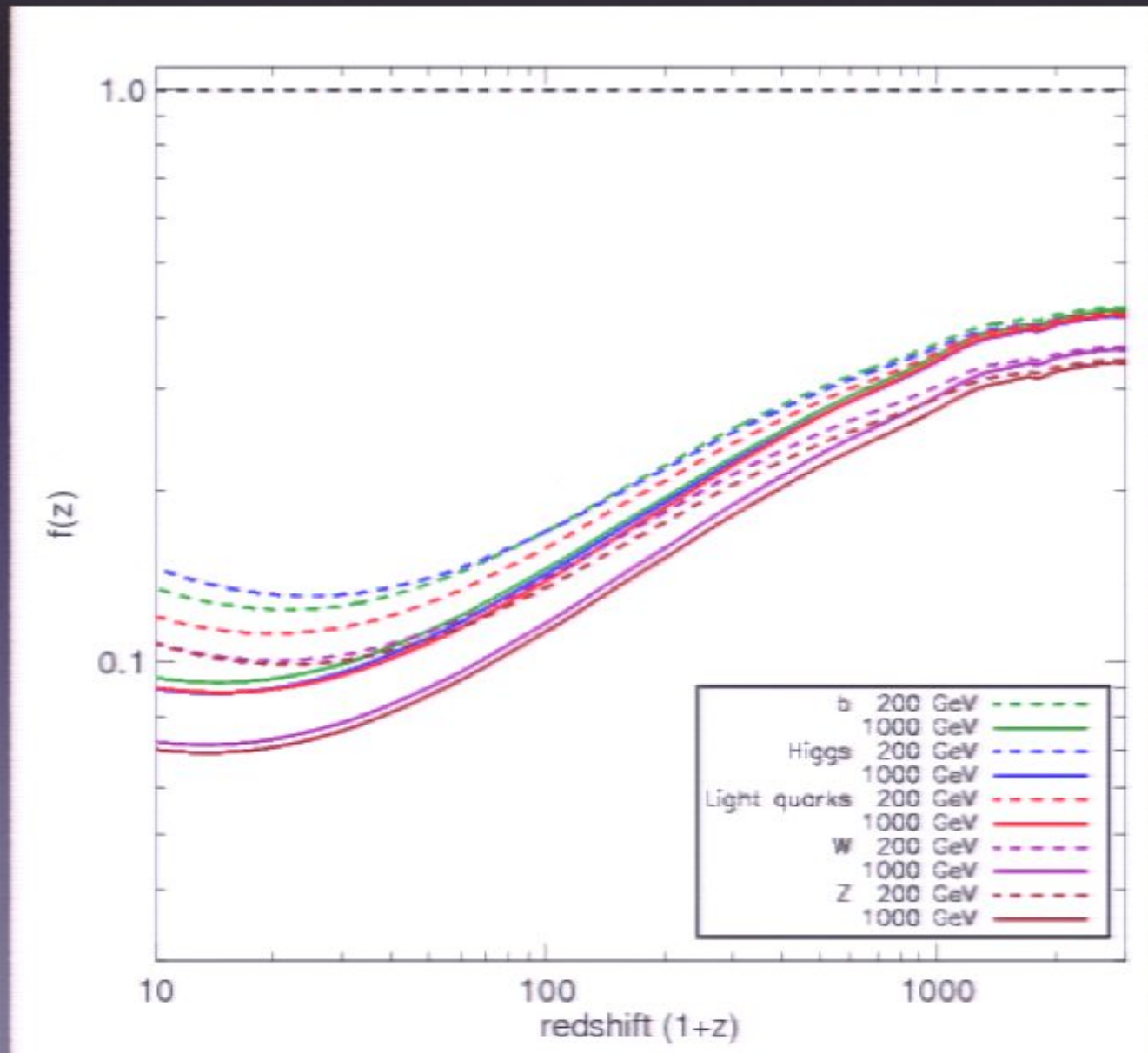


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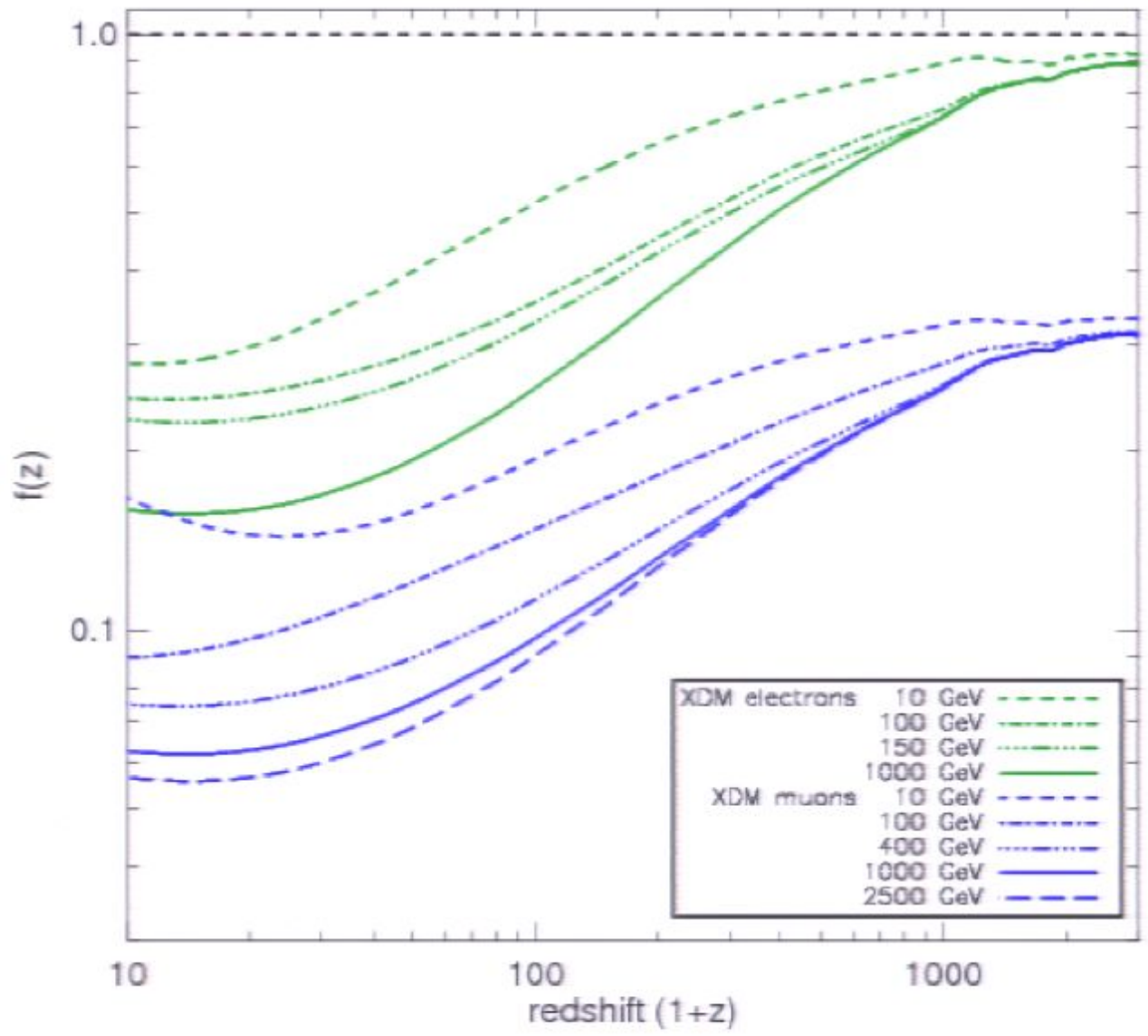


Here, "XDM" just means annihilates through a new light state, which then decays.

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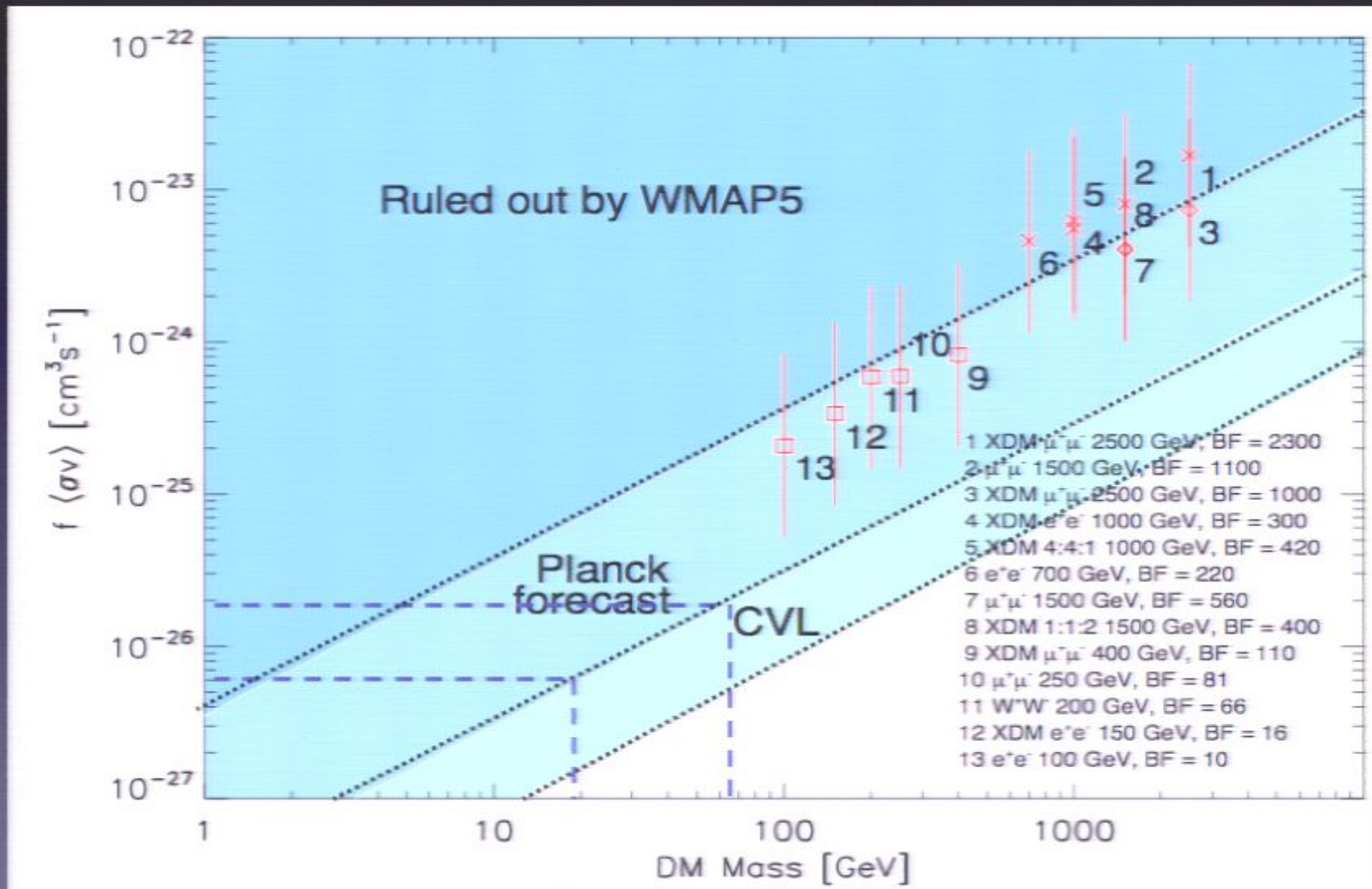
Here, “XDM” just means annihilates through a new light state, which then decays.

$$f(z) = F(1+z)^{\alpha} \left(\left(\frac{1+z}{z_0} \right)^{\gamma} + \left(\frac{1+z}{z_0} \right)^{-\gamma} \right)^{\beta} \exp \left(\frac{\delta}{1 + ((1+z)/1100)^{\eta}} \right). \quad (\text{A1})$$

These fits are accurate to within 1% between $z = 300 - 1200$ for all channels. These fits remain accurate to $< 5\%$ between $z = 170$ and $z = 1470$, but outside this range they may perform very poorly.

| Channel | DM mass (GeV) | f_{mean} | $f(z=2500)$ | a | b | c | F | α | β | γ | δ | η | $z\eta$ |
|--|---------------|-------------------|-------------|--------|----------|--------|--------|----------|---------|----------|----------|----------|-----------|
| Electrons $\chi\chi \rightarrow e^+e^-$ | 1 | 0.92 | 0.98 | 0.5069 | 51.8802 | 2.2828 | 0.1140 | 0.4099 | -0.5634 | 0.6445 | 0.0043 | -5.1992 | 150.3970 |
| | 10 | 0.84 | 0.91 | 0.0715 | 0.0078 | 6.7906 | 0.0864 | 0.4028 | -0.2453 | 1.1481 | 0.0488 | -4.1911 | 166.4426 |
| | 100 | 0.69 | 0.89 | 0.2207 | 14.5754 | 3.1748 | 0.0676 | 0.3745 | -0.1973 | 0.9745 | 0.0682 | -13.0681 | 322.3401 |
| | 700 | 0.70 | 0.89 | 0.1627 | 13.3065 | 2.8822 | 0.0841 | 0.3698 | -0.5719 | 0.5410 | 0.0528 | -12.3998 | 663.9780 |
| | 1000 | 0.70 | 0.89 | 0.1615 | 13.3421 | 2.8416 | 0.0701 | 0.3696 | -0.3077 | 0.7263 | 0.0469 | -12.9124 | 678.7171 |
| Muons $\chi\chi \rightarrow \mu^+\mu^-$ | 1 | 0.32 | 0.34 | 0.2396 | 133.1654 | 3.0272 | 0.0602 | 0.3284 | -0.4350 | 0.5484 | -0.0094 | -4.7619 | 97.2662 |
| | 10 | 0.31 | 0.33 | 0.1092 | 8.7012 | 3.4240 | 0.0650 | 0.3258 | -0.3532 | 0.7324 | -0.0429 | 4.5242 | 179.1545 |
| | 100 | 0.26 | 0.31 | 0.0844 | 6.8923 | 4.0583 | 0.0441 | 0.2985 | -0.3359 | 0.6027 | 0.0303 | -14.5100 | 485.1301 |
| | 250 | 0.25 | 0.31 | 0.0725 | 12.4318 | 3.2776 | 0.0557 | 0.2930 | -0.7418 | 0.3300 | 0.0646 | -10.3133 | 823.4443 |
| | 1000 | 0.24 | 0.31 | 0.0662 | 12.9396 | 2.9742 | 0.0514 | 0.2925 | -0.6312 | 0.5611 | 0.0575 | -10.5586 | 947.3654 |
| | 1500 | 0.24 | 0.31 | 0.0646 | 13.0970 | 2.9112 | 0.0553 | 0.2926 | -0.7359 | 0.5133 | 0.0573 | -10.5603 | 952.6785 |
| Tau $\chi\chi \rightarrow \tau^+\tau^-$ | 200 | 0.23 | 0.28 | 0.0577 | 7.5935 | 3.5566 | 0.0341 | 0.2860 | -0.0818 | 1.4385 | 0.0573 | -8.8065 | 935.1002 |
| | 1000 | 0.23 | 0.29 | 0.0529 | 12.7237 | 2.9838 | 0.0565 | 0.2865 | -0.3265 | 0.4640 | 0.0562 | -10.5471 | 934.1133 |
| XDM electrons $\chi\chi \rightarrow \phi\phi$ followed by $\phi \rightarrow e^+e^-$ | 10 | 0.88 | 0.92 | 0.2419 | 2.7143 | 4.1521 | 0.0908 | 0.4080 | -0.2529 | 1.1047 | 0.0081 | -0.9440 | 149.6370 |
| | 100 | 0.73 | 0.89 | 0.2427 | 10.4821 | 3.6656 | 0.0792 | 0.3787 | -0.3787 | 0.6703 | 0.0418 | -13.7399 | 296.5718 |
| | 150 | 0.70 | 0.89 | 0.2226 | 12.5182 | 3.3474 | 0.0686 | 0.3748 | -0.2138 | 0.7970 | 0.0603 | -11.9976 | 292.5551 |
| | 1000 | 0.70 | 0.89 | 0.1655 | 13.1537 | 2.9302 | 0.0727 | 0.3697 | -0.3598 | 0.6831 | 0.0486 | -12.7614 | 675.8390 |
| XDM muons $\chi\chi \rightarrow \phi\phi$ followed by $\phi \rightarrow \mu^+\mu^-$ | 10 | 0.32 | 0.33 | 0.1464 | 23.7835 | 2.7952 | 0.0569 | 0.3250 | -0.4137 | 0.6546 | 0.0370 | -3.1624 | 173.1706 |
| | 100 | 0.27 | 0.31 | 0.0809 | 2.5357 | 4.7587 | 0.0457 | 0.3035 | -0.3322 | 0.8392 | 0.0179 | -13.3422 | 321.8945 |
| | 400 | 0.25 | 0.31 | 0.0741 | 11.3064 | 3.3949 | 0.0402 | 0.2937 | -0.2579 | 0.6965 | 0.0505 | -10.3800 | 774.7615 |
| | 1000 | 0.25 | 0.31 | 0.0617 | 12.5196 | 3.1133 | 0.0418 | 0.2925 | -0.3294 | 0.7487 | 0.0541 | -10.6936 | 939.3080 |
| | 2500 | 0.24 | 0.31 | 0.0556 | 13.0389 | 2.9349 | 0.0522 | 0.2926 | -0.6537 | 0.5413 | 0.0566 | -10.5987 | 952.4342 |
| XDM tau $\chi\chi \rightarrow \phi\phi, \phi \rightarrow \tau^+\tau^-$ | 200 | 0.22 | 0.27 | 0.0604 | 6.6206 | 3.6373 | 0.0333 | 0.2861 | -0.0610 | 1.0364 | 0.0548 | -8.7336 | 638.6944 |
| | 1000 | 0.22 | 0.27 | 0.0534 | 11.2208 | 3.1869 | 0.0424 | 0.2841 | -0.4351 | 0.6734 | 0.0542 | -10.5137 | 911.3169 |
| XDM pions $\chi\chi \rightarrow \phi\phi$ followed by $\phi \rightarrow \pi^+\pi^-$ | 100 | 0.22 | 0.25 | 0.0607 | 1.4685 | 5.0403 | 0.0394 | 0.2881 | -0.2700 | 0.8445 | 0.0137 | -12.6965 | 304.5202 |
| | 200 | 0.21 | 0.25 | 0.0674 | 6.0060 | 4.1253 | 0.0363 | 0.2825 | -0.1722 | 0.7910 | 0.0323 | -13.6145 | 477.7644 |
| | 1000 | 0.20 | 0.25 | 0.0515 | 12.3319 | 3.1745 | 0.0382 | 0.2762 | -0.3601 | 0.6781 | 0.0517 | -10.8809 | 1030.3075 |
| | 1600 | 0.20 | 0.25 | 0.0481 | 12.6927 | 3.0715 | 0.0428 | 0.2760 | -0.5297 | 0.5865 | 0.0547 | -10.7564 | 1026.1082 |
| | 2500 | 0.20 | 0.25 | 0.0463 | 12.9871 | 2.9688 | 0.0480 | 0.2762 | -0.6968 | 0.5217 | 0.0566 | -10.6509 | 1025.4334 |
| W bosons $\chi\chi \rightarrow W^+W^-$ | 200 | 0.29 | 0.35 | 0.1013 | 19.1565 | 2.9322 | 0.0395 | 0.3076 | -0.0895 | 1.1093 | 0.0377 | -13.2287 | 446.3091 |
| | 300 | 0.29 | 0.35 | 0.0906 | 15.7616 | 3.0067 | 0.0388 | 0.3053 | -0.0855 | 1.0564 | 0.0389 | -13.1812 | 528.0555 |
| | 1000 | 0.28 | 0.35 | 0.0711 | 10.6406 | 3.1935 | 0.0415 | 0.3025 | -0.2151 | 0.8366 | 0.0516 | -10.6585 | 782.1619 |
| Z bosons $\chi\chi \rightarrow ZZ$ | 200 | 0.28 | 0.34 | 0.0998 | 20.7336 | 2.8932 | 0.0392 | 0.3043 | -0.1088 | 1.0375 | 0.0359 | -13.3227 | 447.9354 |
| | 1000 | 0.27 | 0.33 | 0.0689 | 10.6396 | 3.2027 | 0.0407 | 0.2988 | -0.2263 | 0.7934 | 0.0514 | -9.9893 | 773.0394 |
| Higgs bosons $\chi\chi \rightarrow h\bar{h}$ | 200 | 0.34 | 0.40 | 0.1313 | 24.2160 | 2.8491 | 0.0479 | 0.3205 | -0.2349 | 0.7599 | 0.0297 | -13.5576 | 388.8721 |
| | 1000 | 0.32 | 0.40 | 0.0877 | 10.9586 | 3.1982 | 0.0430 | 0.3133 | -0.1570 | 0.8487 | 0.0490 | -9.8120 | 616.1287 |
| b quarks $\chi\chi \rightarrow b\bar{b}$ | 200 | 0.35 | 0.41 | 0.1244 | 20.6286 | 2.8789 | 0.0467 | 0.3217 | -0.1873 | 0.8494 | 0.0345 | -13.3583 | 383.5586 |
| | 1000 | 0.33 | 0.41 | 0.0917 | 11.6611 | 3.1846 | 0.0425 | 0.3149 | -0.1246 | 0.9724 | 0.0467 | -9.8366 | 635.3590 |
| Light quarks $\chi\chi \rightarrow u\bar{u}, d\bar{d}$ (50 % each) | 200 | 0.34 | 0.40 | 0.1129 | 18.5996 | 2.9221 | 0.0432 | 0.3174 | -0.1218 | 0.9244 | 0.0361 | -13.1747 | 430.2257 |
| | 1000 | 0.32 | 0.40 | 0.0882 | 12.3648 | 3.1280 | 0.0434 | 0.3135 | -0.1700 | 0.9101 | 0.0490 | -9.8913 | 674.5797 |

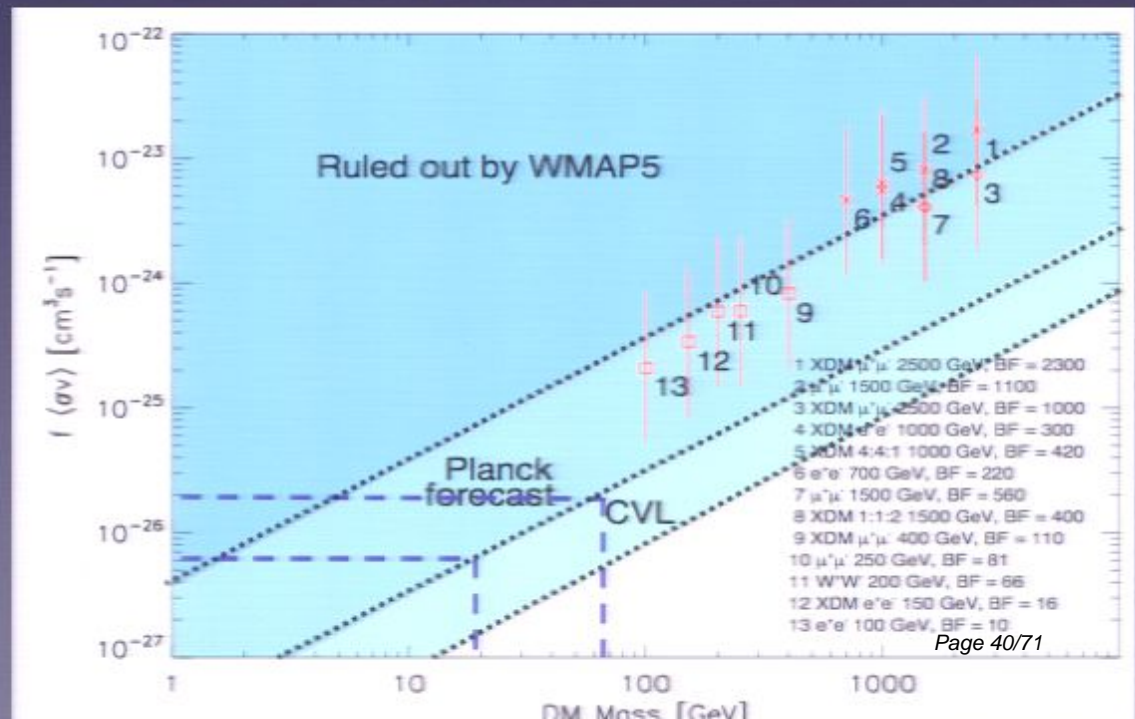
Benchmark models that fit PAMELA and/or Fermi



Note that the PAMELA - constrained models fall along the edge of the ruled-out region.

They all have \sim the same injection power. The CMB is approximately sensitive to injection power.

>> There must be a more general way to do this!



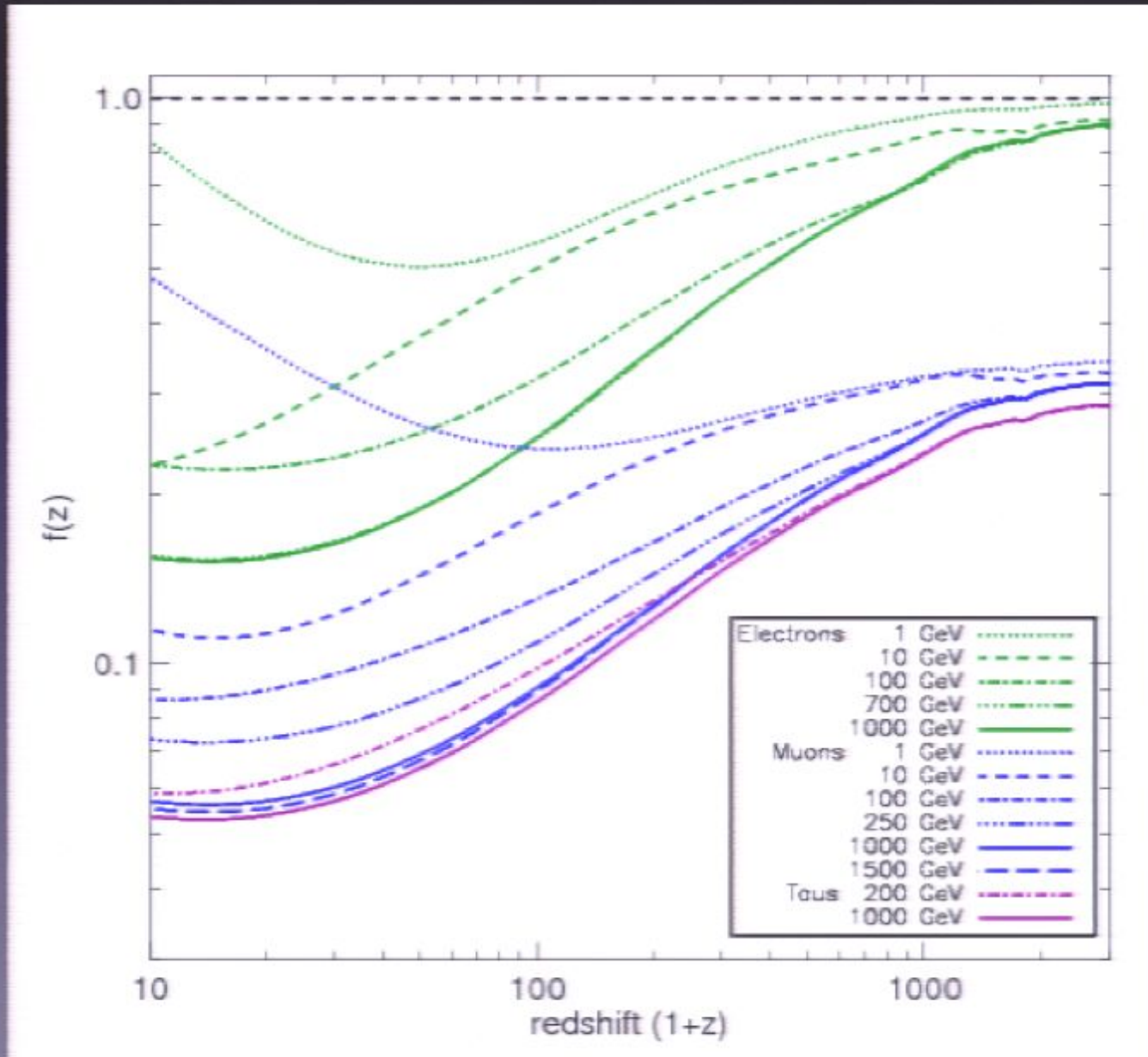
Recent work with Galli, Lin, & Slatyer (2011)

Idea: The energy injection is already constrained to be small, so we can linearize the problem and perturb about a fiducial model, i.e. the standard cosmology with no extra energy injection.

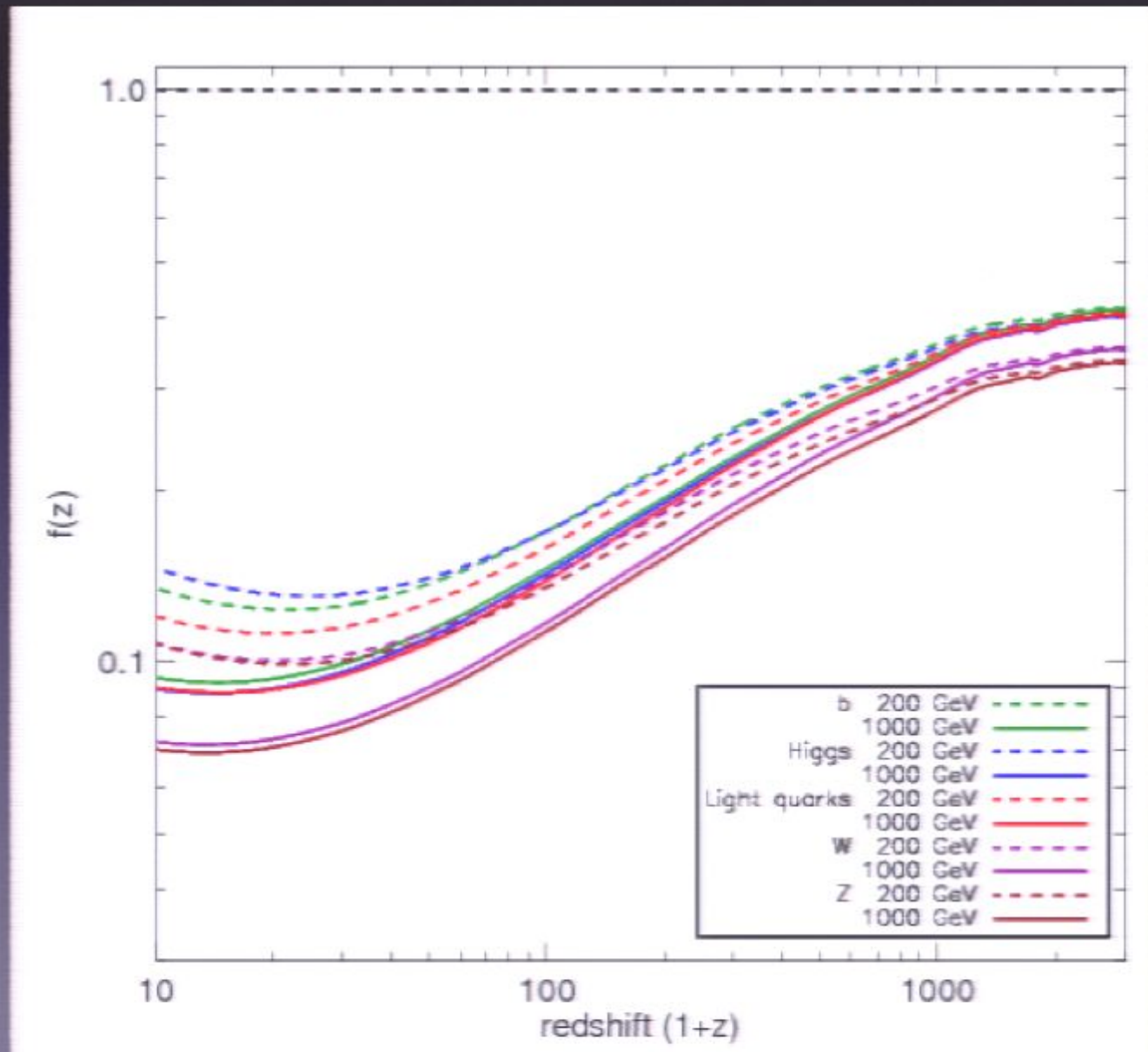
Various energy injection functions, $f(z)$, perturb the C_l spectrum in a small dimension subspace, allowing us to describe arbitrary (smooth, non-negative) energy injection with only a few numbers.

We can work out degeneracies, detectability, etc., by considering a few generic parameters.

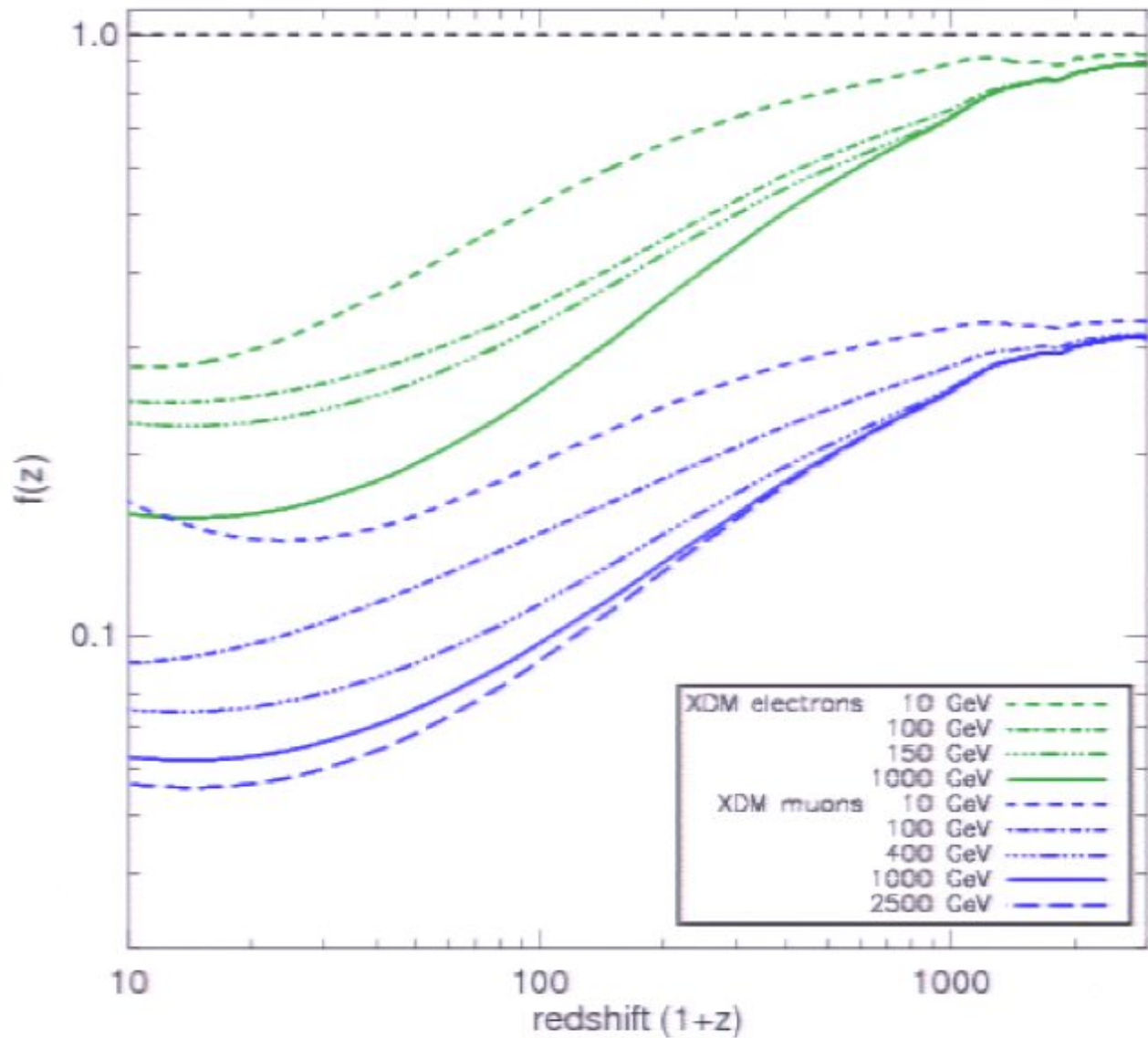
The Slatyer-Padmanabhan-Finkbeiner (SPF) factor, f :



The Slatyer-Padmanabhan-Finkbeiner (SPF) factor.



The Slatyer-Padmanabhan-Finkbeiner (SPF) factor.



Here, "XDM" just means annihilates through a new light state, which then decays.

Recent work with Galli, Lin, & Slatyer (2011)

Idea: The energy injection is already constrained to be small, so we can linearize the problem and perturb about a fiducial model, i.e. the standard cosmology with no extra energy injection.

Various energy injection functions, $f(z)$, perturb the C_l spectrum in a small dimension subspace, allowing us to describe arbitrary (smooth, non-negative) energy injection with only a few numbers.

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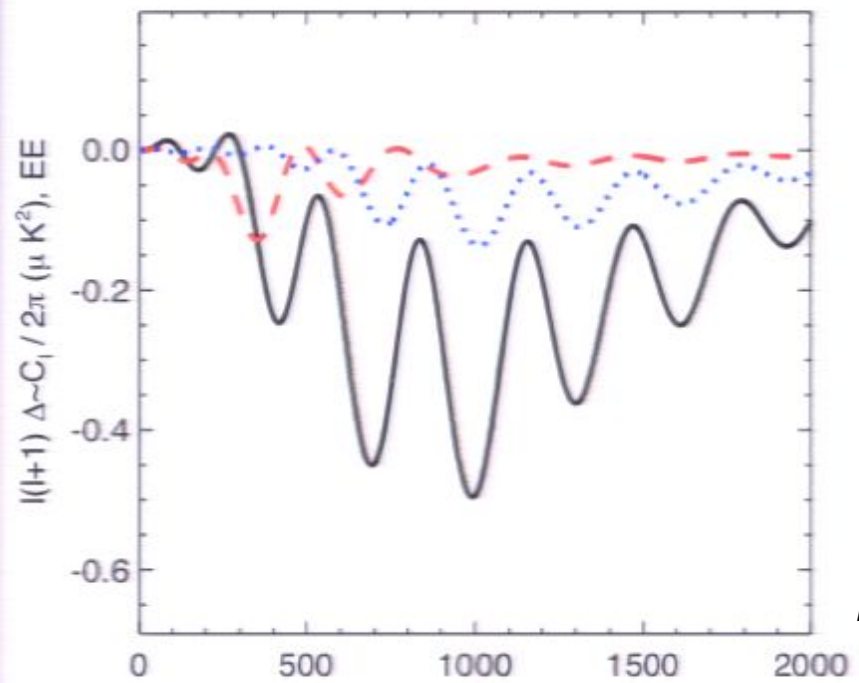
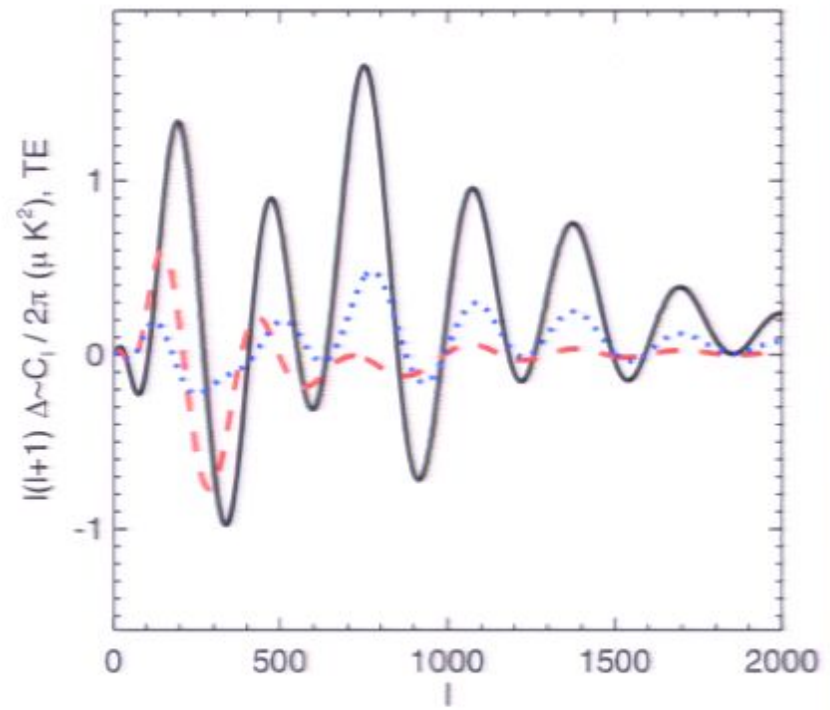
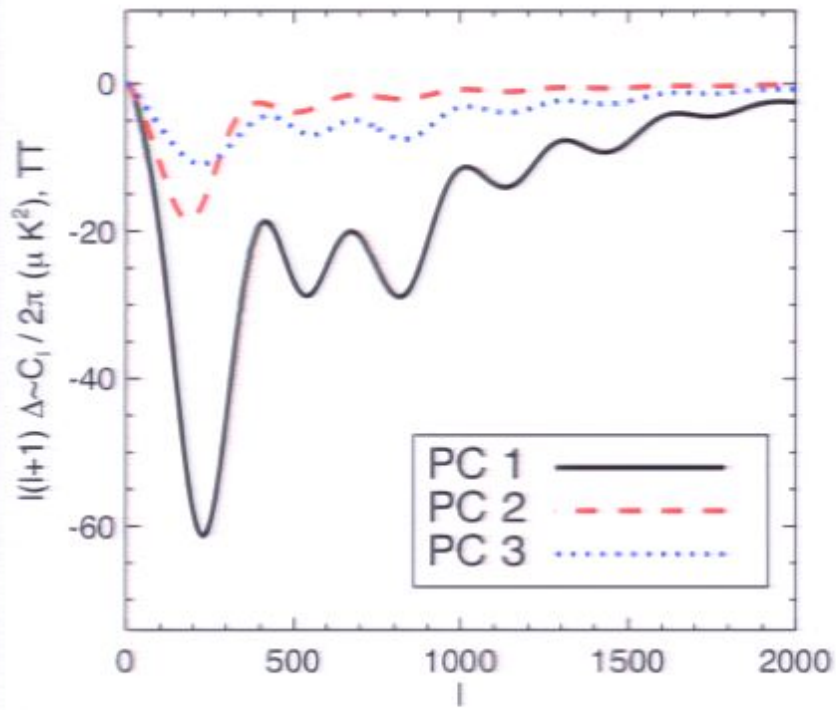
What basis to use in Delta C_l (“delta power spectrum”) space?

Or equivalently, $f(z)$ space?

We can consider the effect of a delta function energy injection at some redshift. This maps to a vector in ΔC_l space.

Now find Principle Components, map back to $f(z)$ space.

This gives you the components that provide most of the variance in ΔC_l .

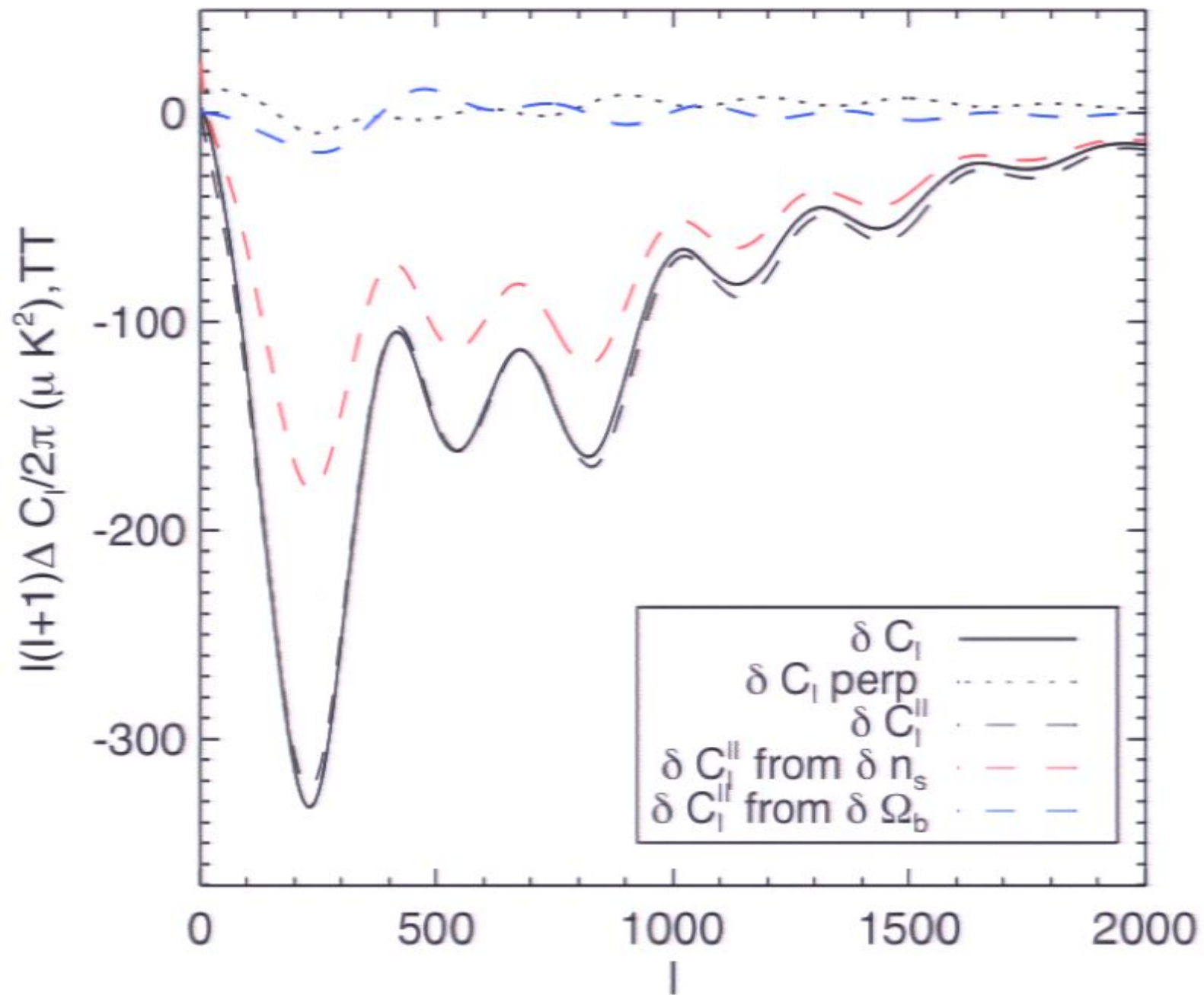


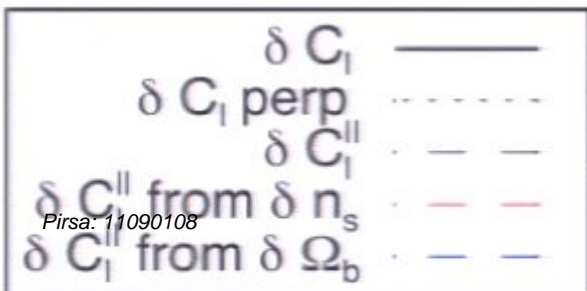
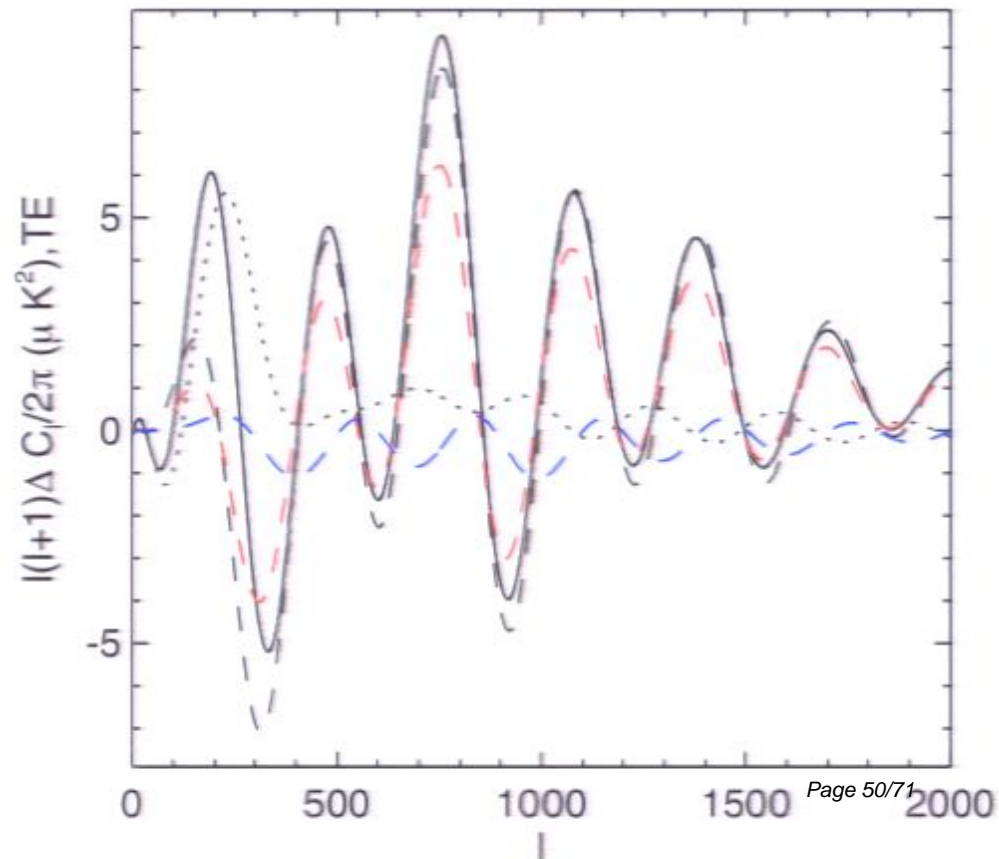
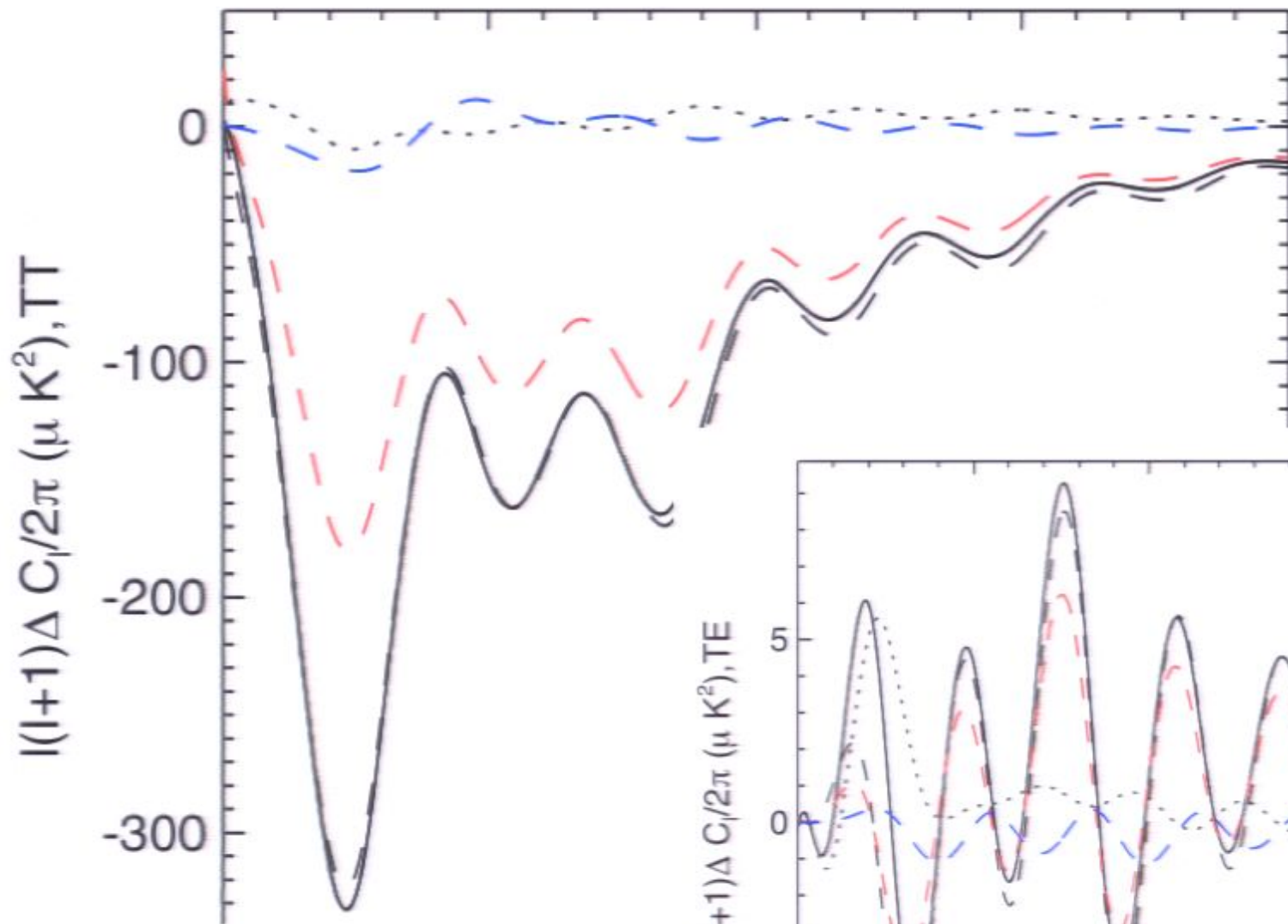
However -- we care about *detectability*, not variance.

Given the expected uncertainties (both cosmic variance and measurement noise), how detectable are each of these components?

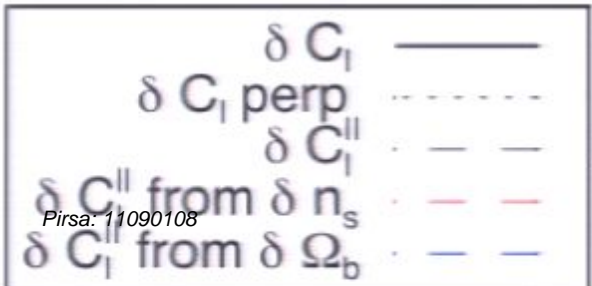
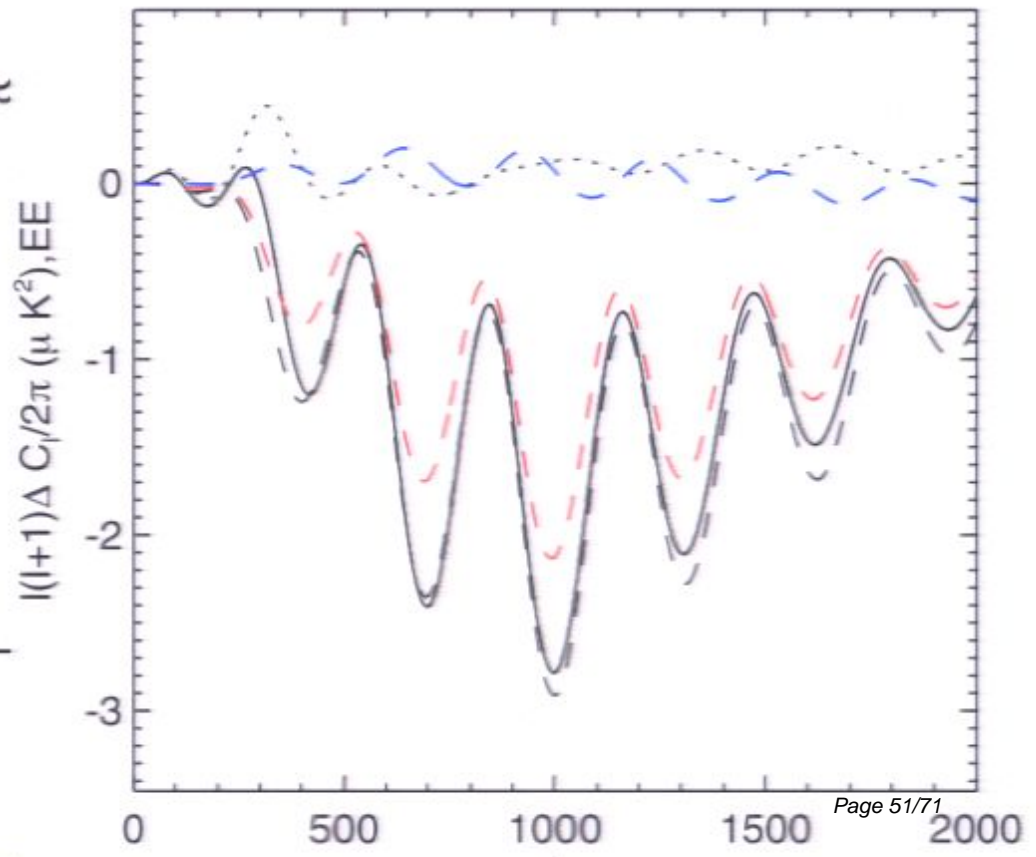
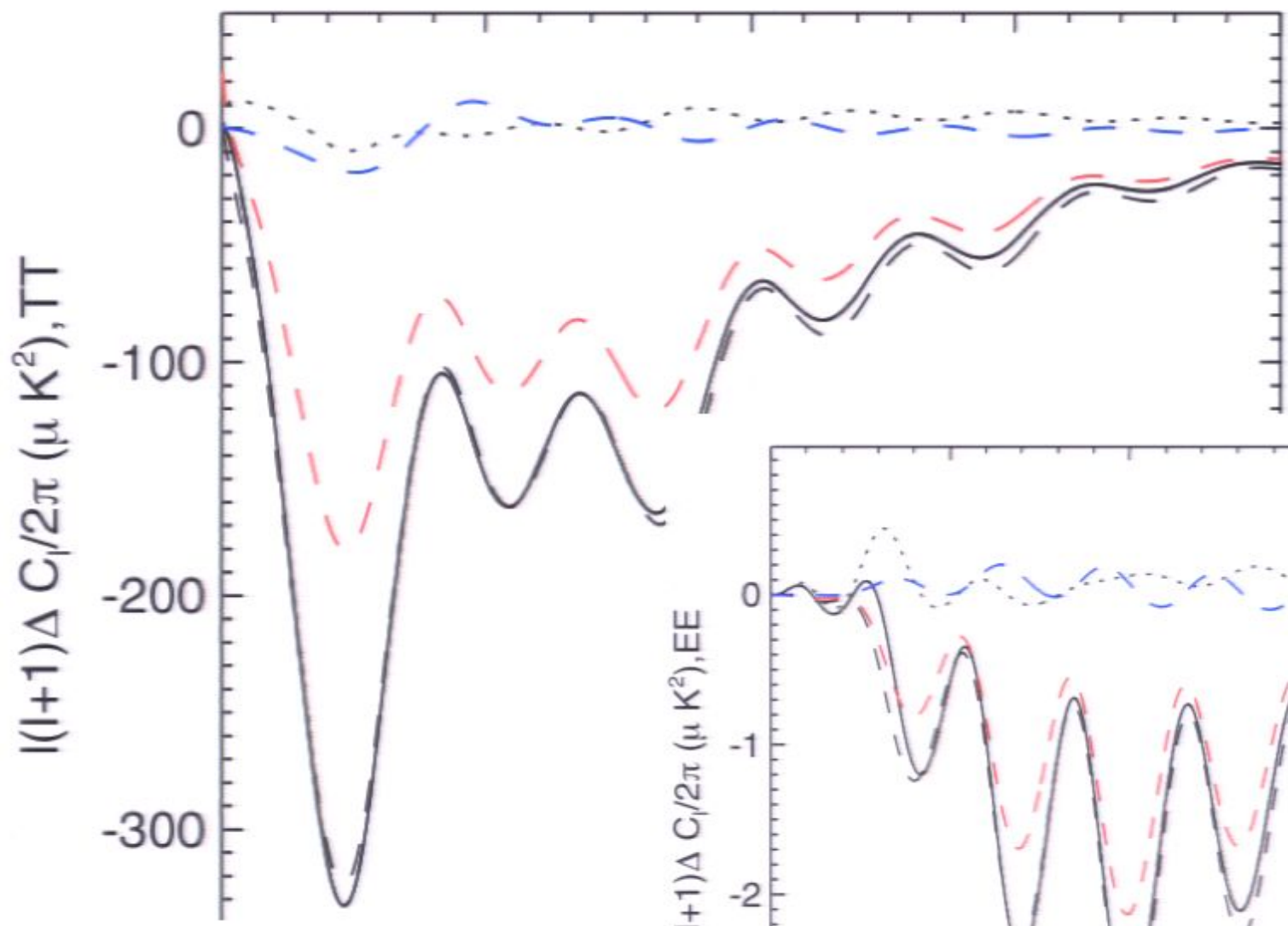
Also -- what about degeneracies with cosmological parameter variations? (especially n_s)

To illustrate this problem, we take a toy (constant f) model, and project out the directions in ΔC_l space corresponding to the cosmological parameters.





500



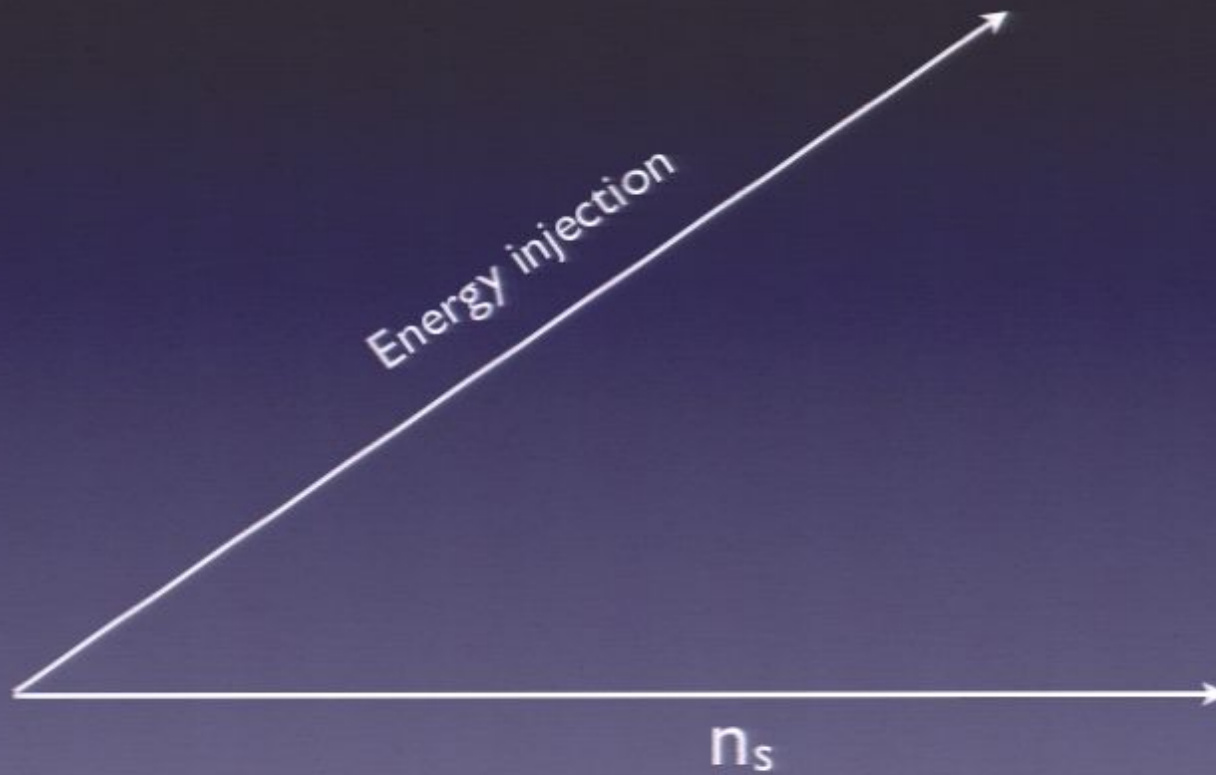
500

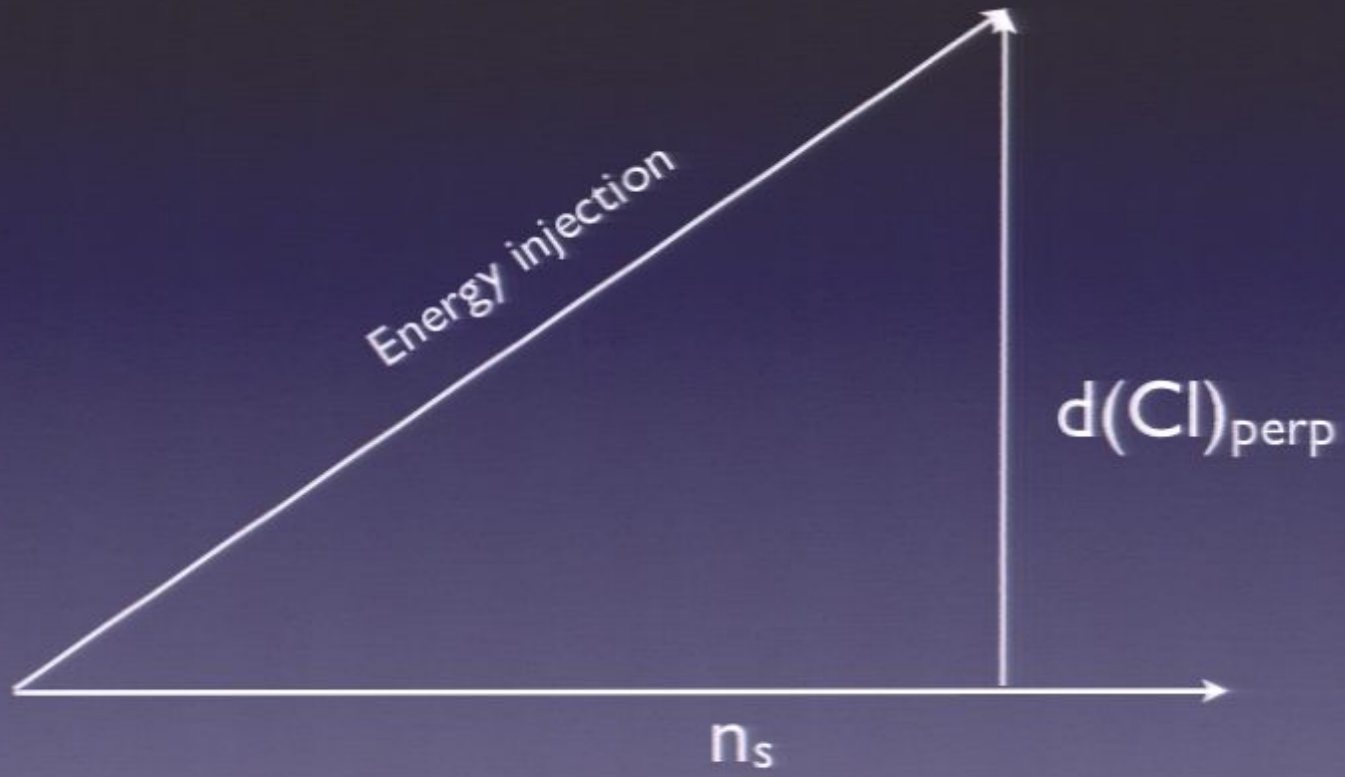
It is not correct to simply project in ΔC_l space.

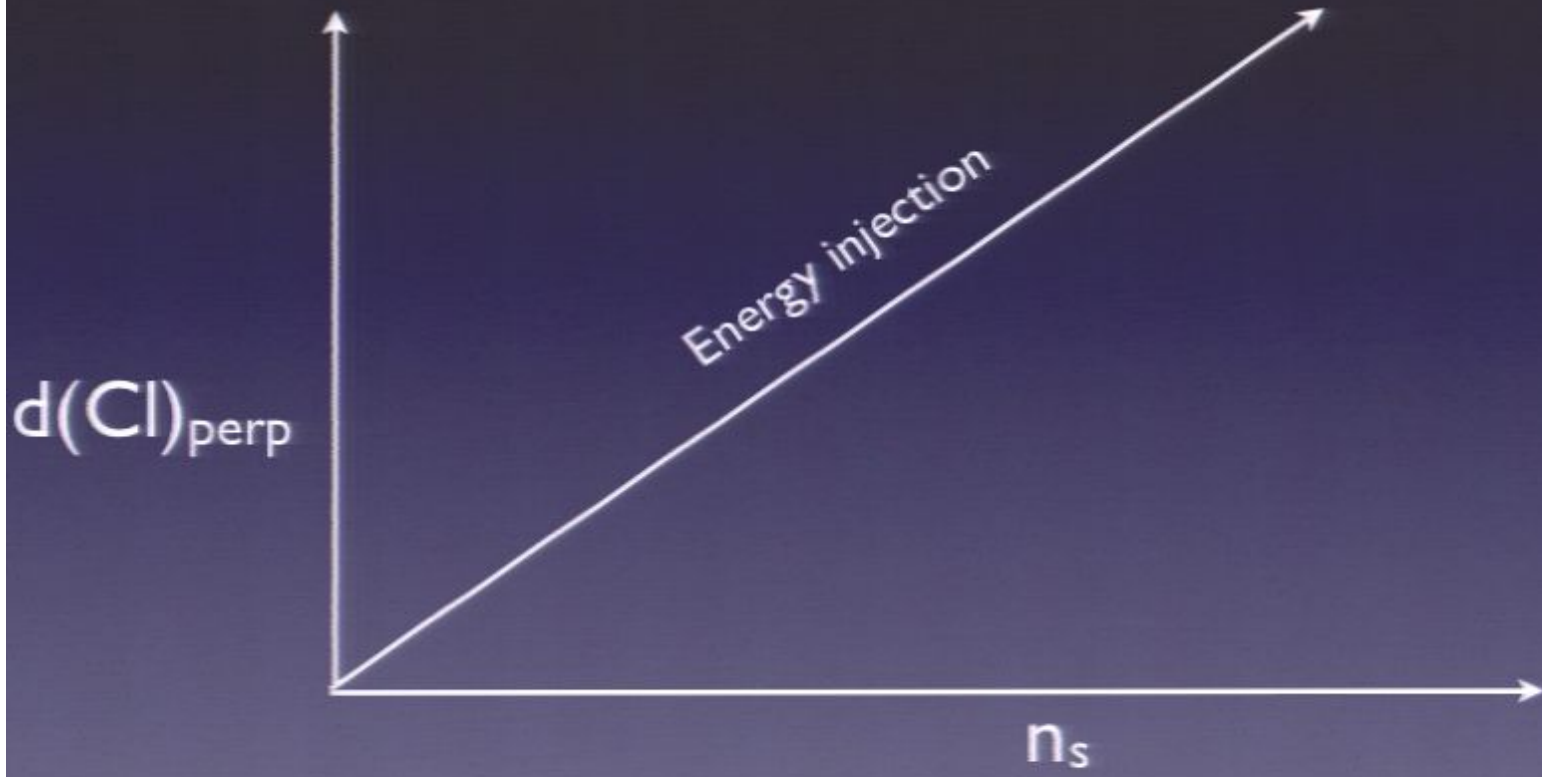
We must *marginalize* over the cosmological parameters (“nuisance parameters!”) taking account of the uncertainty at each l . Doing this, we find a basis for perturbations in ΔC_l corresponding to injection histories $f(z)$.

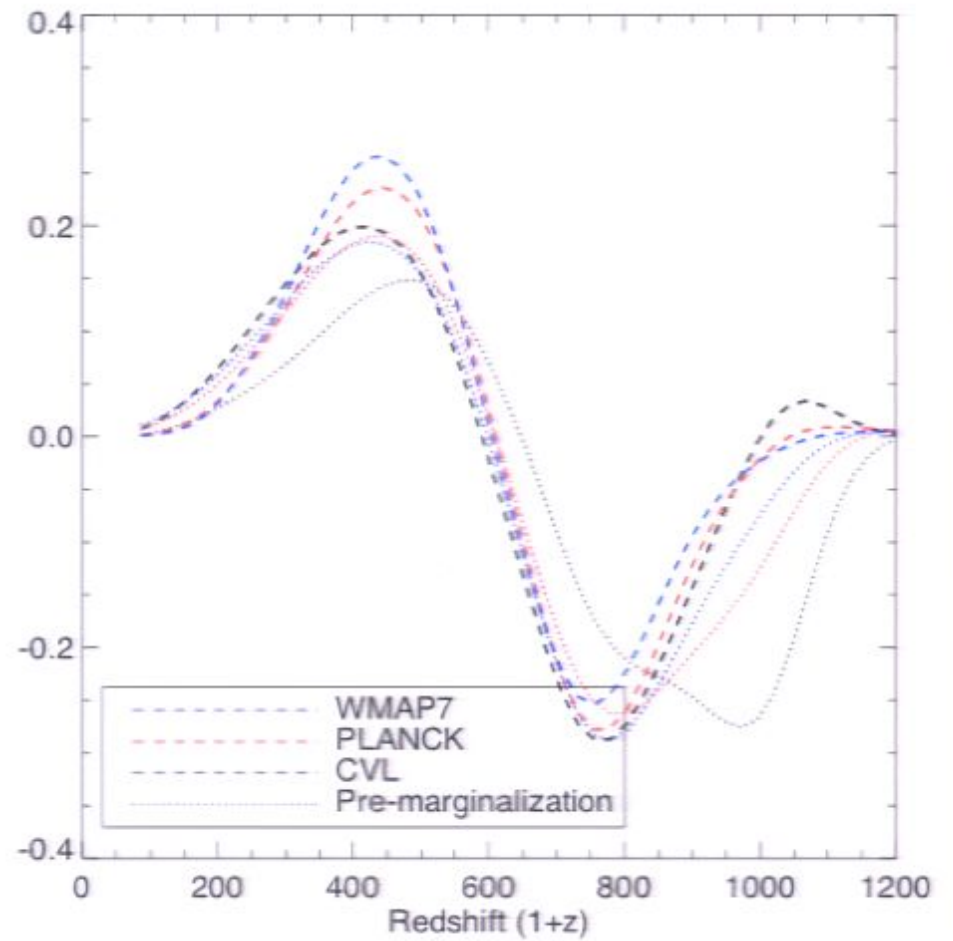
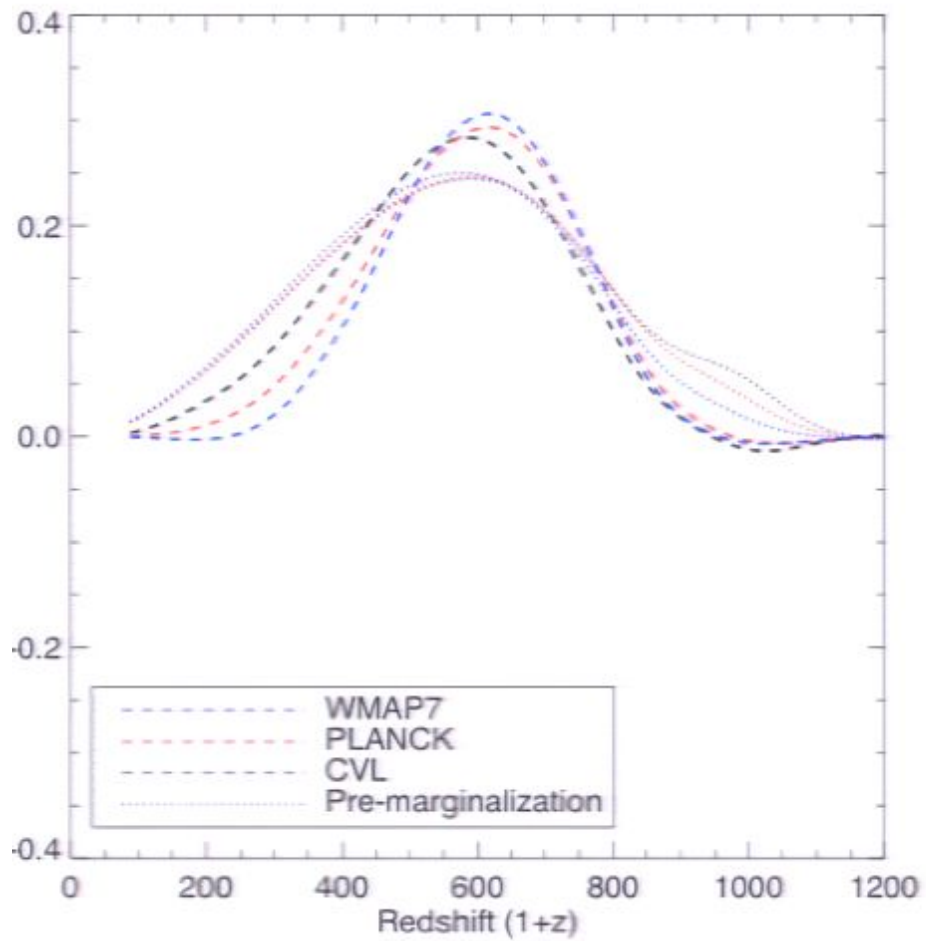
Think of perturbations as vectors in
power-spectrum space.

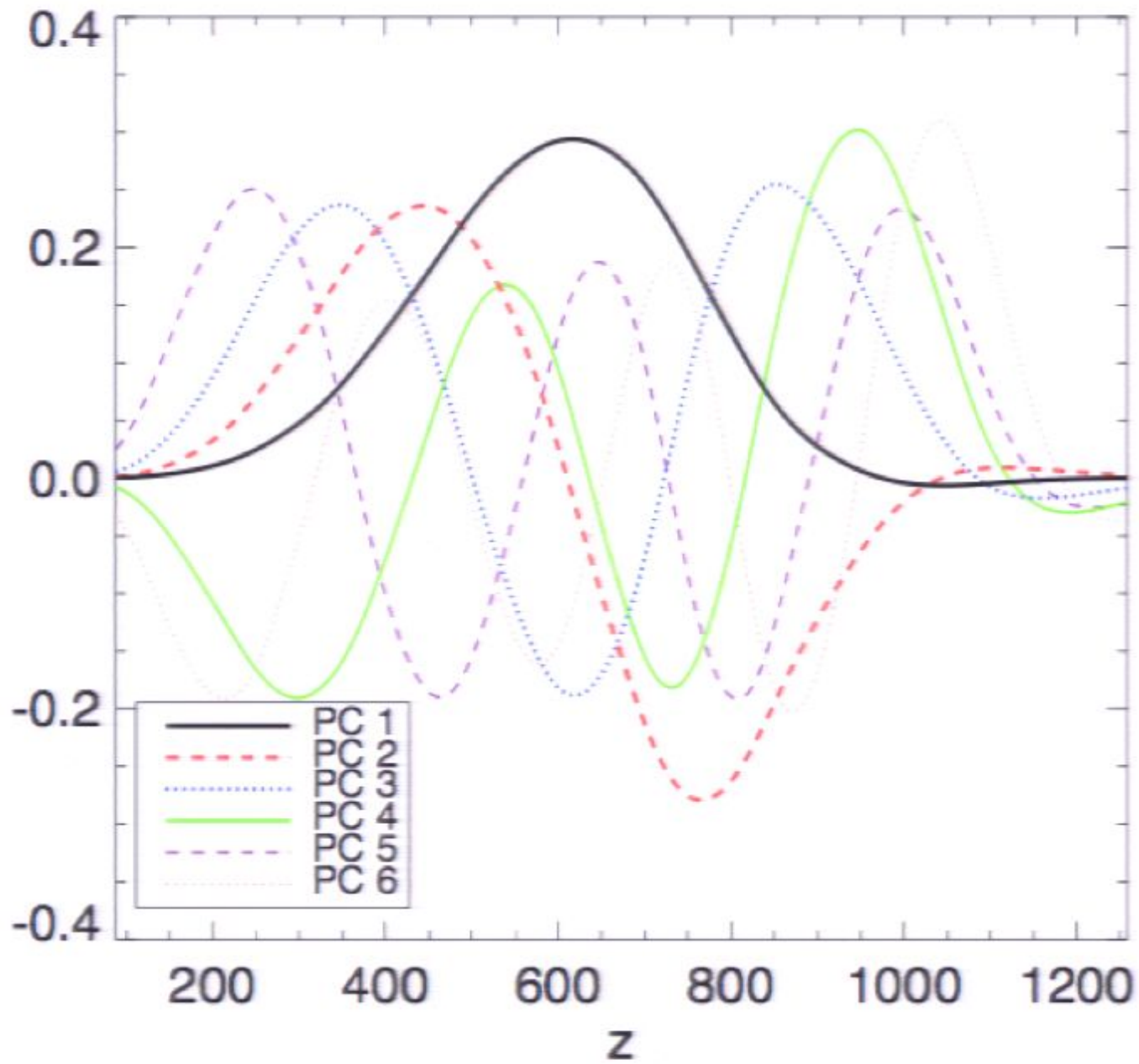


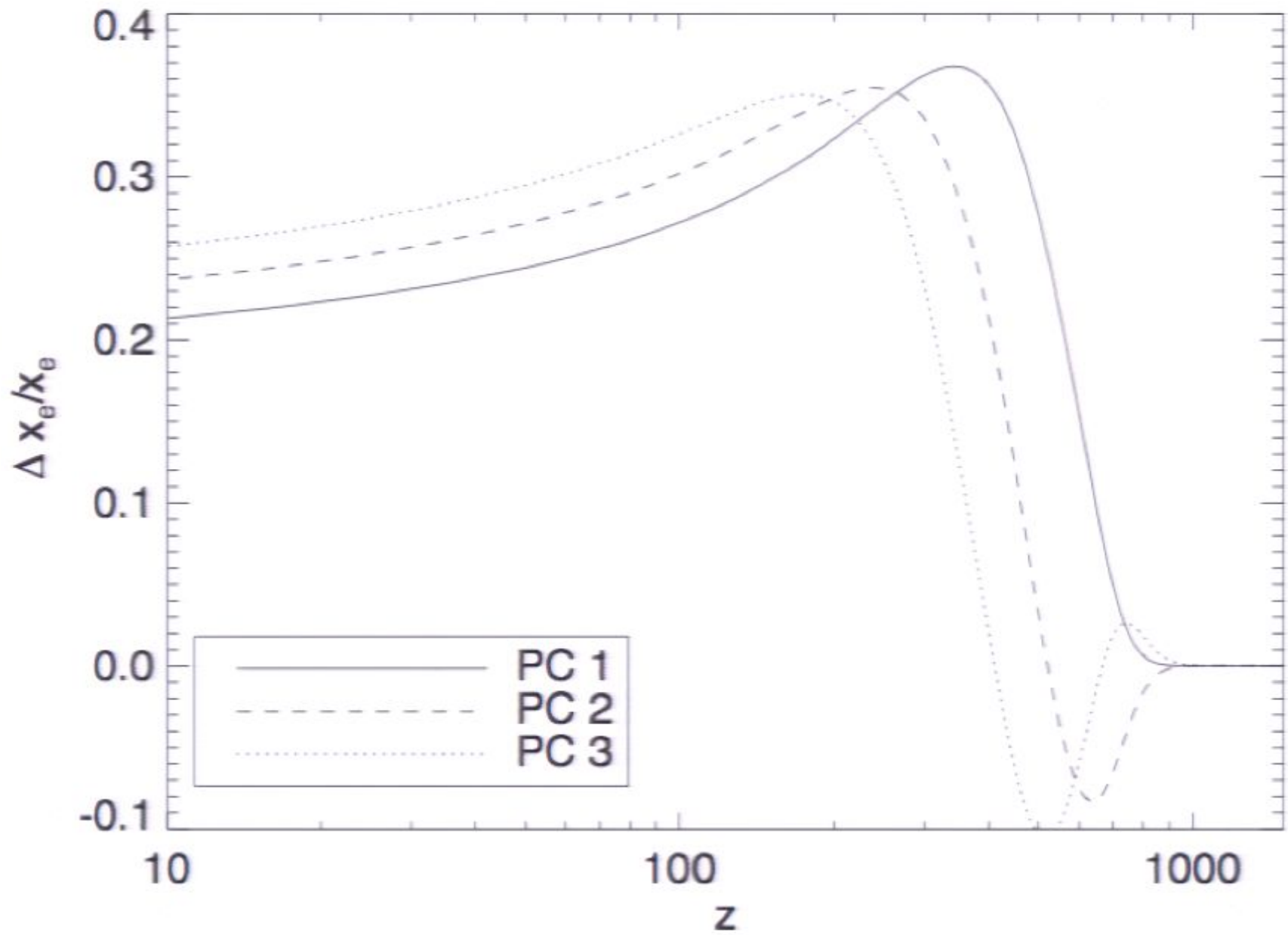










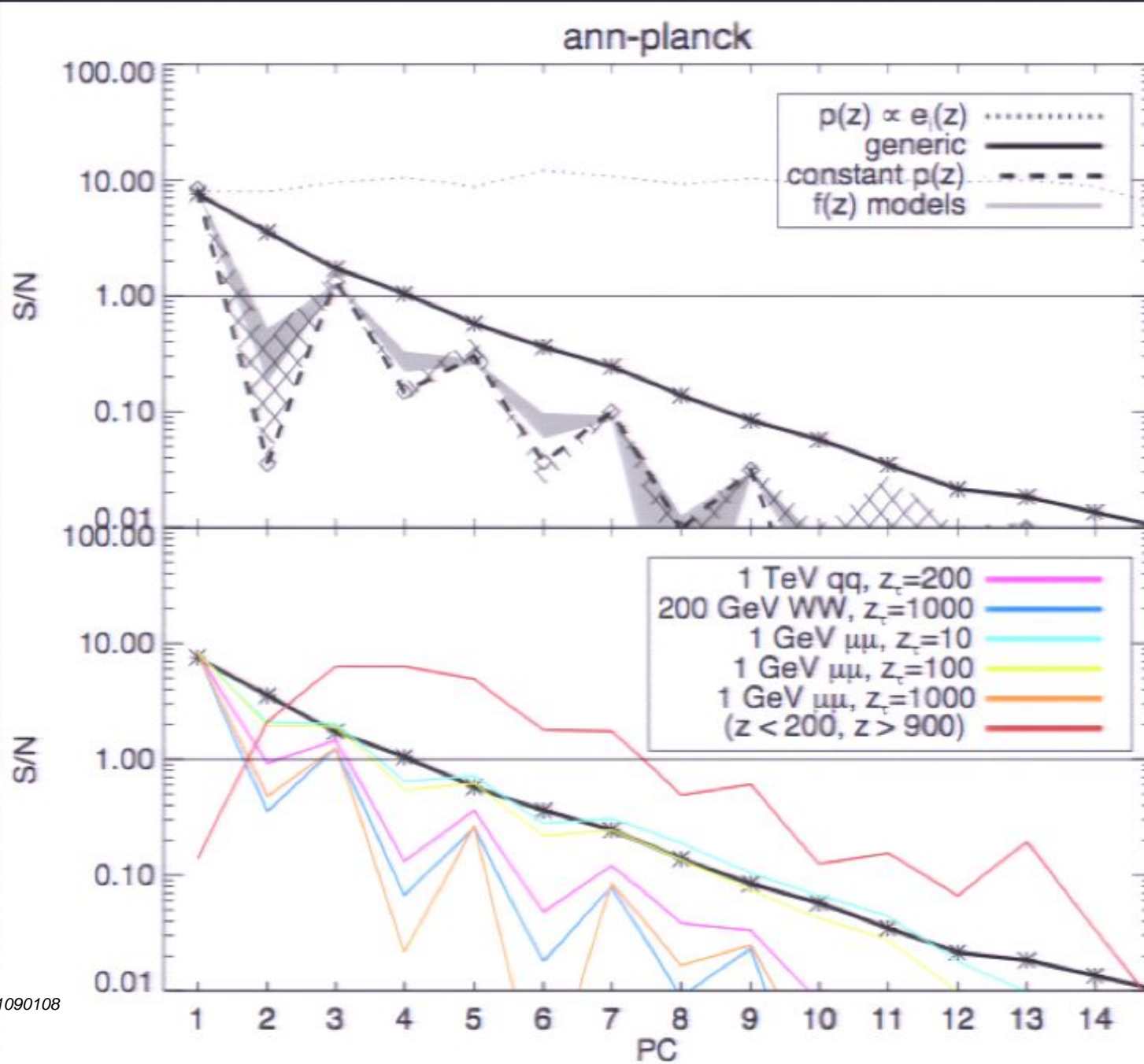


Detectability:

The most optimistic assumption is that WMAP5 barely missed detecting this signal at 2 sigma.

So assume $f(z) = \text{constant}$ at the maximum annihilation power allowed by WMAP5.

Preliminary!



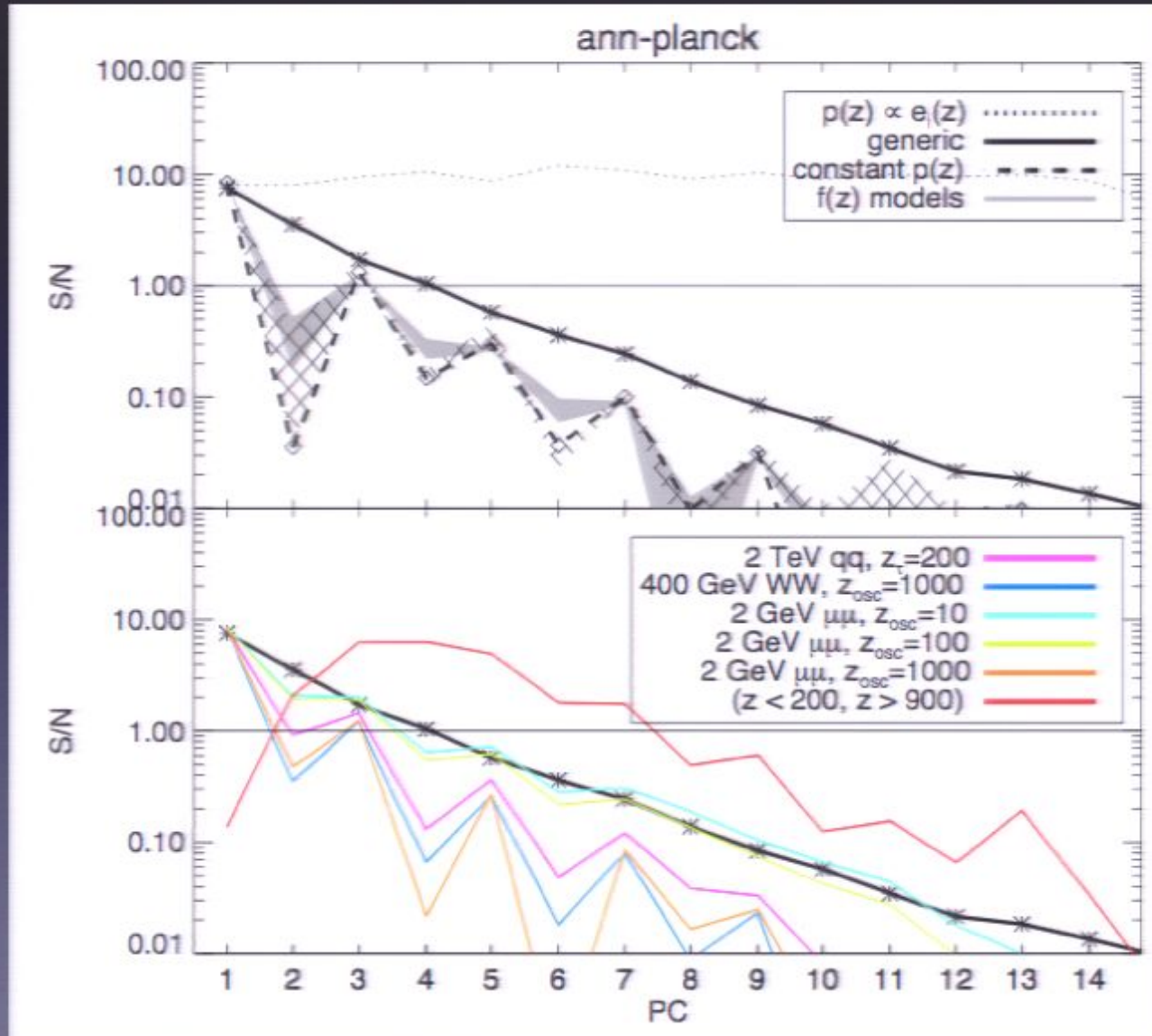
Bottom line:

- Planck may detect *one* PC at high confidence, worth trying first 3. Let's call these $\epsilon_1, \epsilon_2, \epsilon_3...$
- CV - limited mission could go for ~ 5 .
- These parameters are *simple* to measure. Just take dot product (including covariance matrix) of measured ΔC_l with ΔC_l principle components; this measures $\epsilon_1, \epsilon_2, \epsilon_3$.
- Predict $\epsilon_1, \epsilon_2, \epsilon_3$ for your favorite DM model.
Compare.

This works for decay also

Assume appropriate redshift dependence

Marginalize, etc... to get PCs for decay.



Preliminary!

Markov chain Monte Carlo (MCMC)

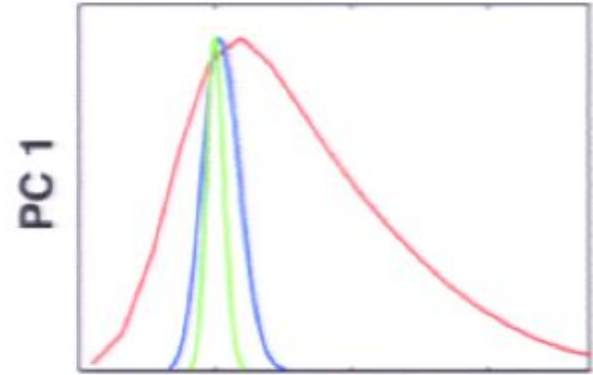
The Fisher matrix analysis assumes linearity and Gaussian likelihood. These are good approximations, but as we can compute the likelihood numerically with a Markov chain.

Preliminary!

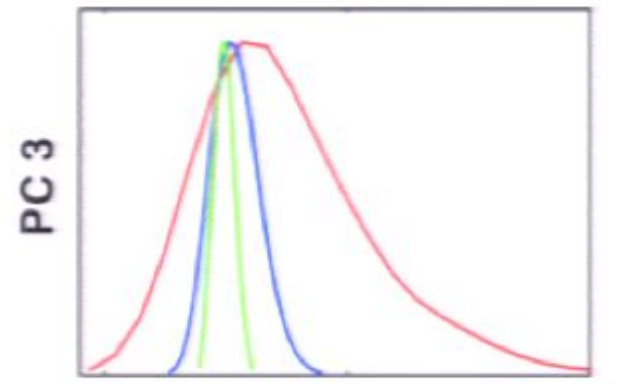
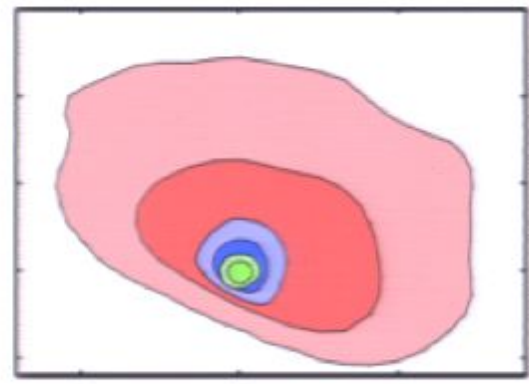
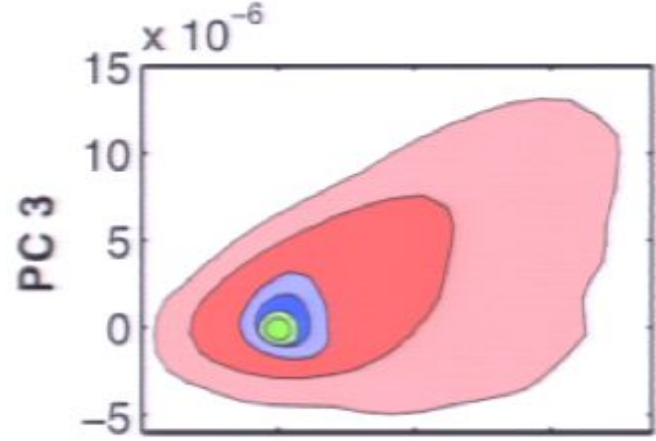
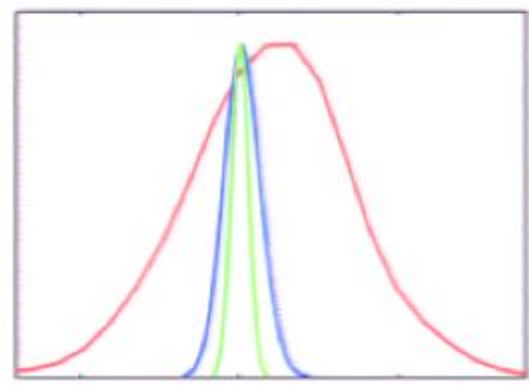
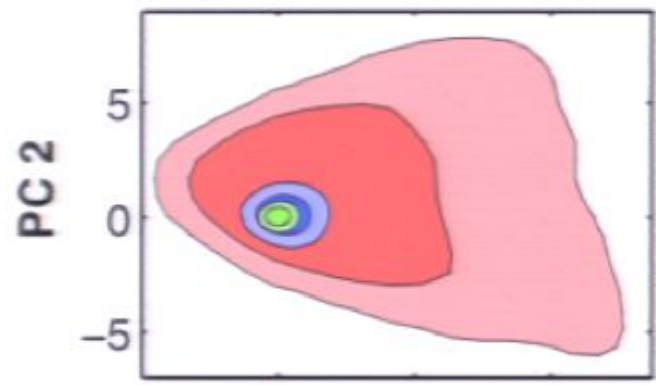
WMAP 7

Planck

CVL



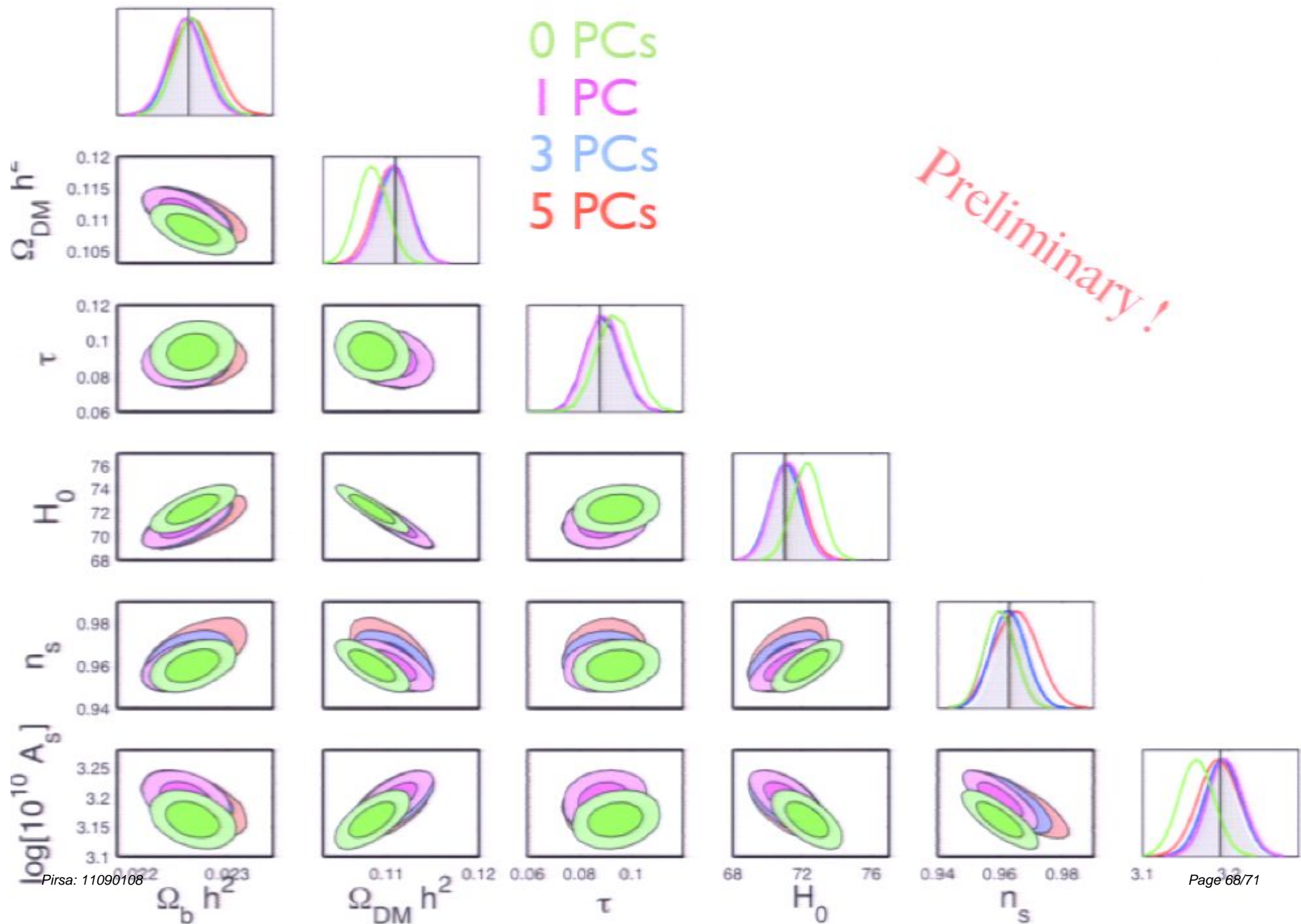
$\times 10^{-6}$

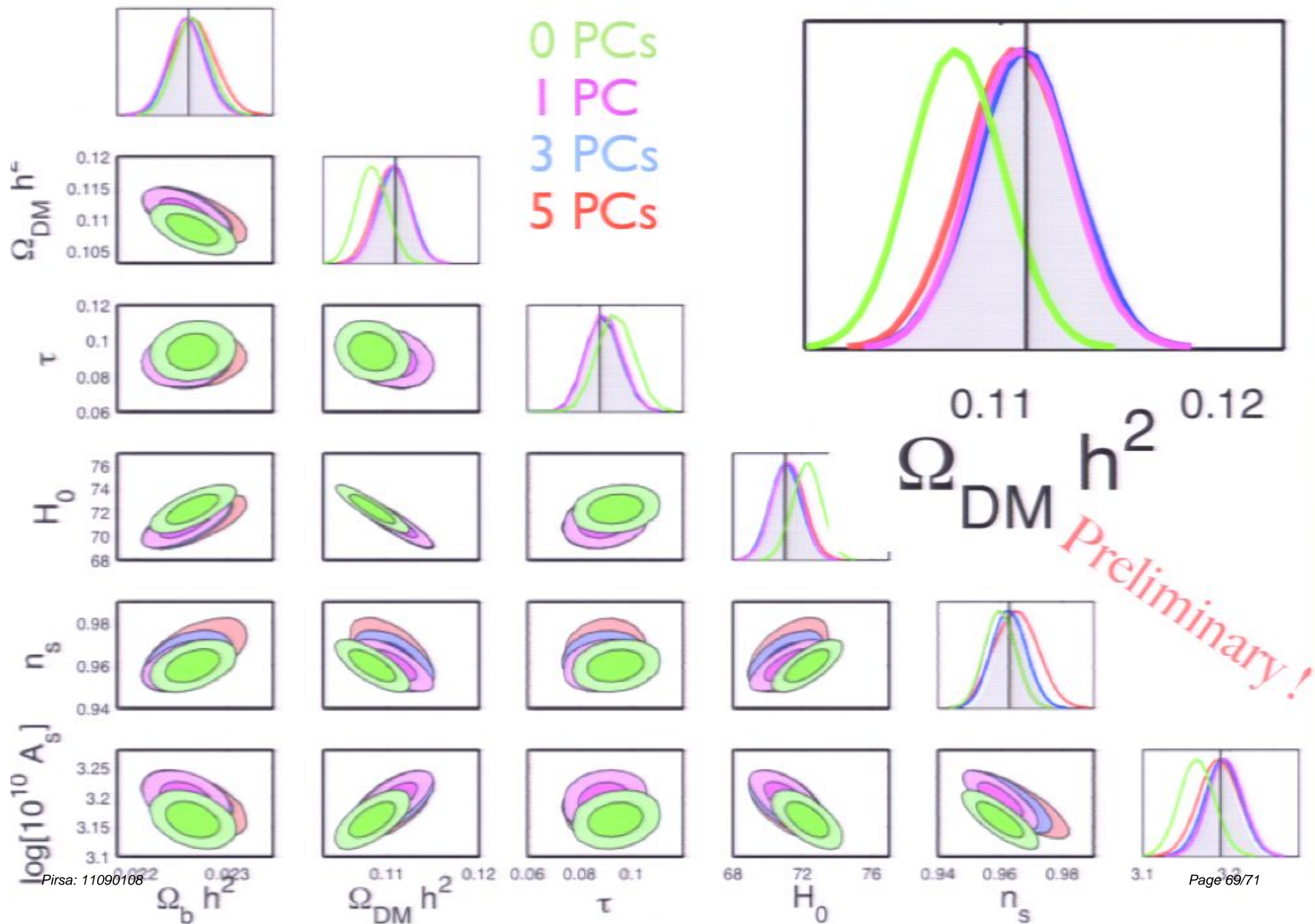


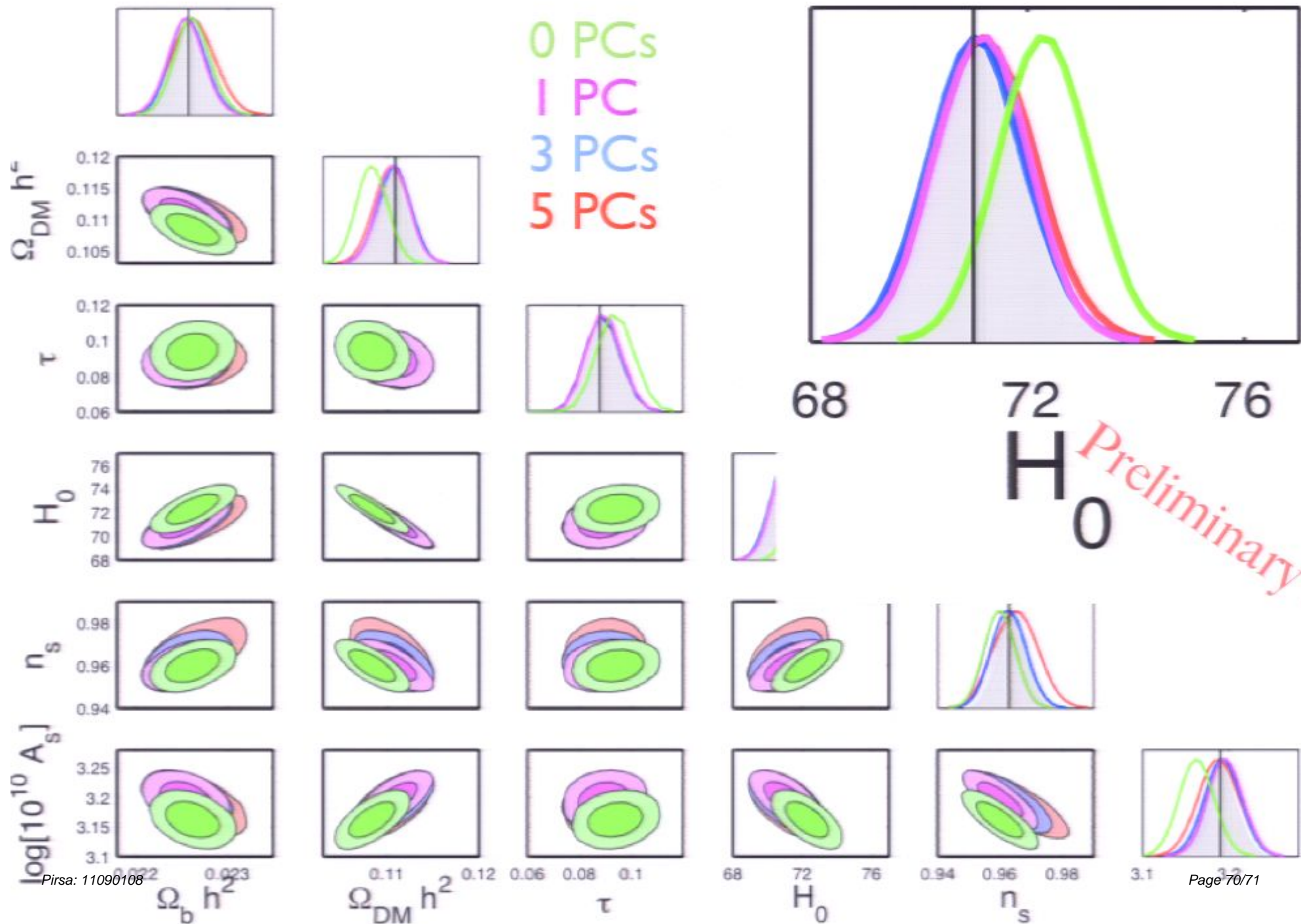
Markov chain Monte Carlo (MCMC)

We can also use MCMC to compute the bias in the cosmological parameters caused by neglect of energy injection.

We find the Fisher matrix-based estimates were good to ~ 10%.







Conclusions:

- A general energy injection at $z \sim 100-1000$ can be parameterized in a general way, yielding only 1 (or maybe 3 or 5) parameters to measure, after accounting for degeneracies with cosmological parameters.
- Neglect of these parameters (assuming $\epsilon_1, \epsilon_2, \epsilon_3 = 0$) will bias the cosmological parameter fits -- often by > 1 sigma.
- If you want to know n_s (with correct error bars) you should make sure to marginalize over $\epsilon_1, \epsilon_2, \epsilon_3$.