

Title: The Small-Scale Structure of Galactic Dark Matter

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Abstract: In my talk I will discuss the relevant astrophysical input for dark matter detection experiments, i.e. the expected distribution of dark matter at the solar position. Based on high resolution N-body simulations I will then show that the formation history of the galactic dark matter halo leaves imprints in the velocity and energy distribution. In the second part of my talk I will focus on the fine-grained dark matter structure and discuss the importance of caustics and streams for detection experiments.

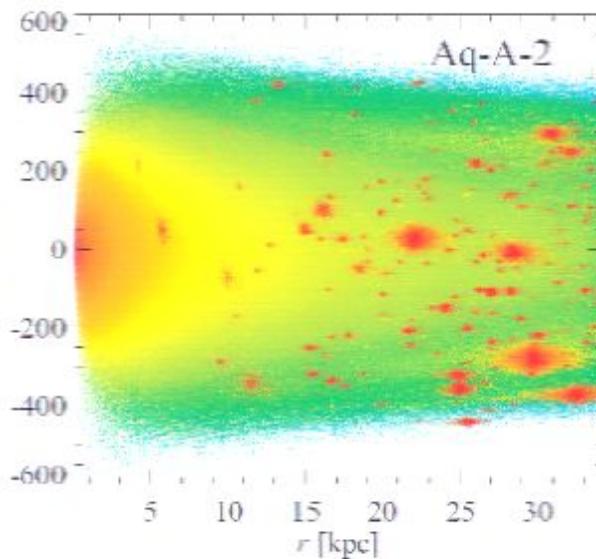
# The Small-Scale Structure of Galactic Dark Matter

**Mark Vogelsberger, Harvard/CfA**

Simon White, Volker Springel, Jesus Zavala,  
Michal Maciejewski, Amina Helmi, Roya Mohayee

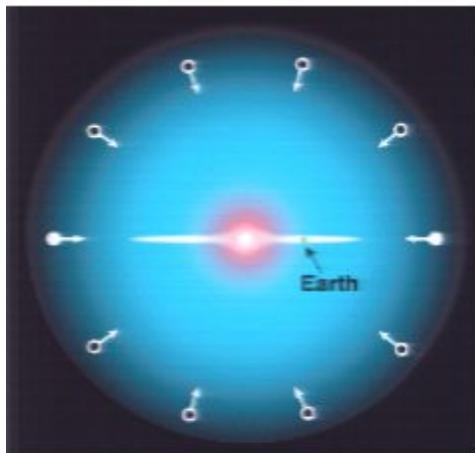
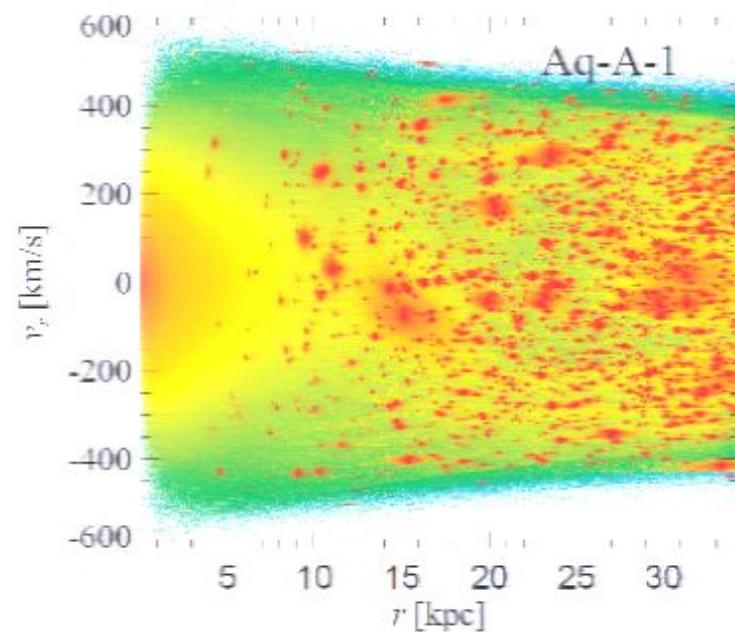
# **Coarse-Grained Structure of $\Lambda$ CDM Halos**

# Halo Phase-Space Structure



Maciejewski et al. (2011)

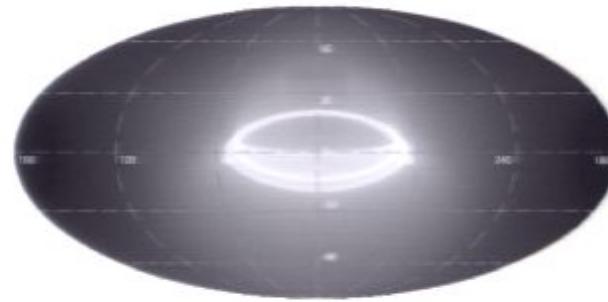
**dark matter  
phase-space  
space structure  
(beyond SHM)**



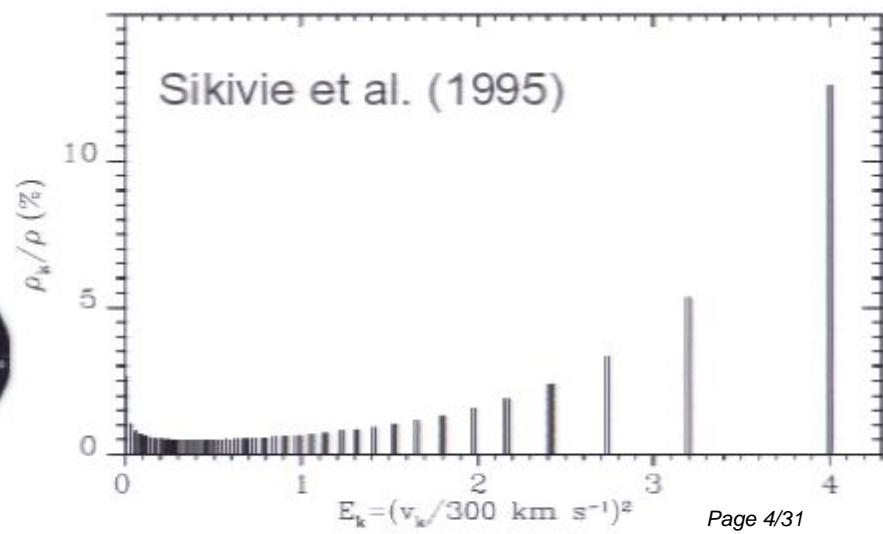
Pirsa: 11090103

Van Bibber (2008)

**Analytic models:**  
→ **massive streams**  
→ **caustic ring model**

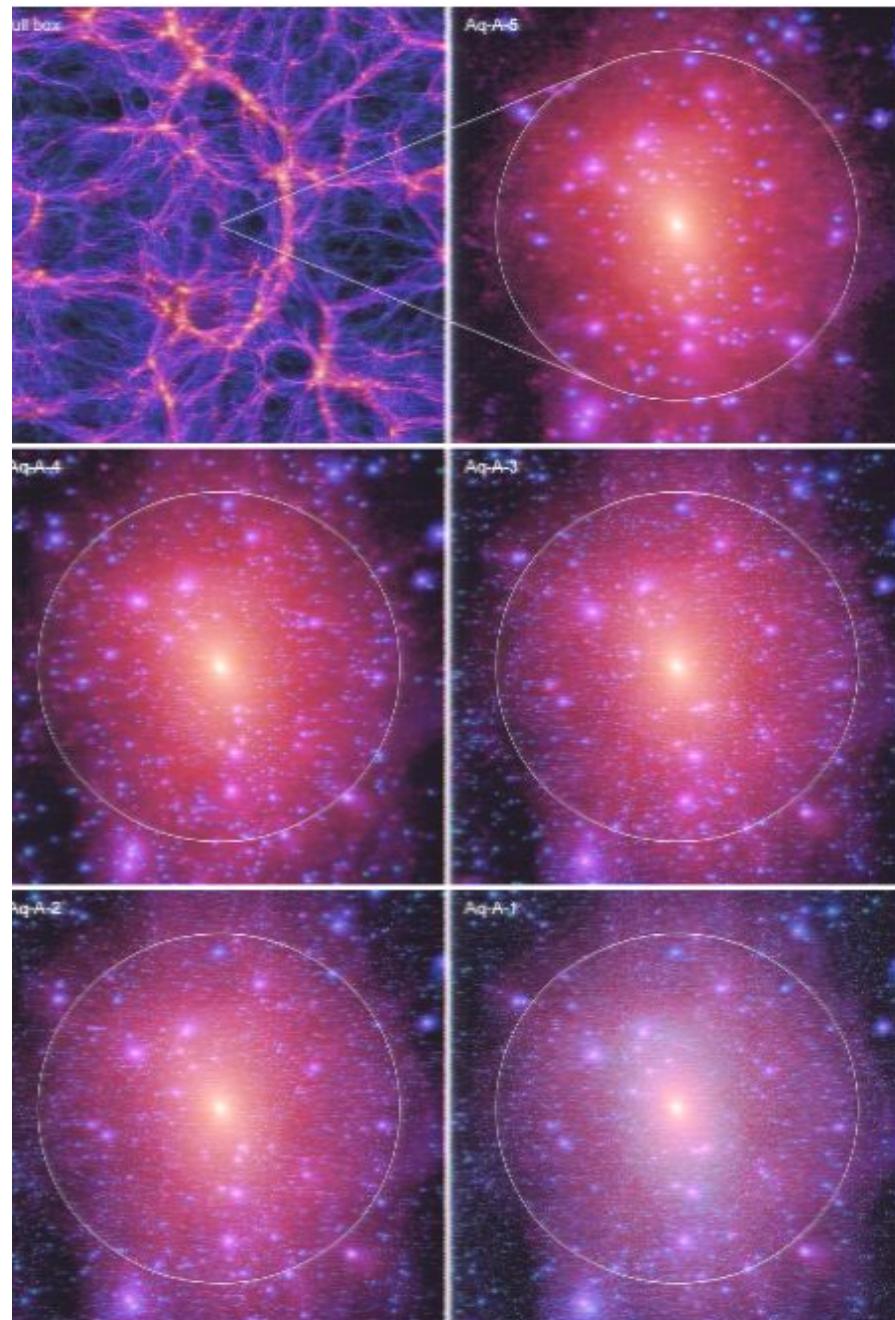


Natarajan & Sikivie (2008)



Sikivie et al. (1995)

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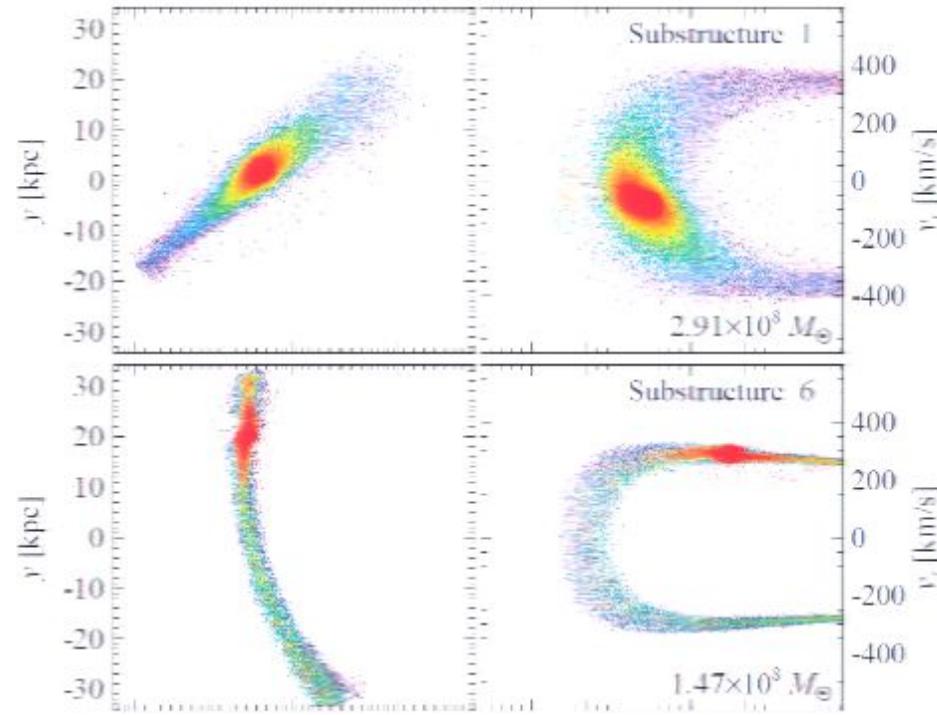
## Aquarius

Springel et al. (2008)

[see also **Via Lactea** by Diemand & Kuhlen]



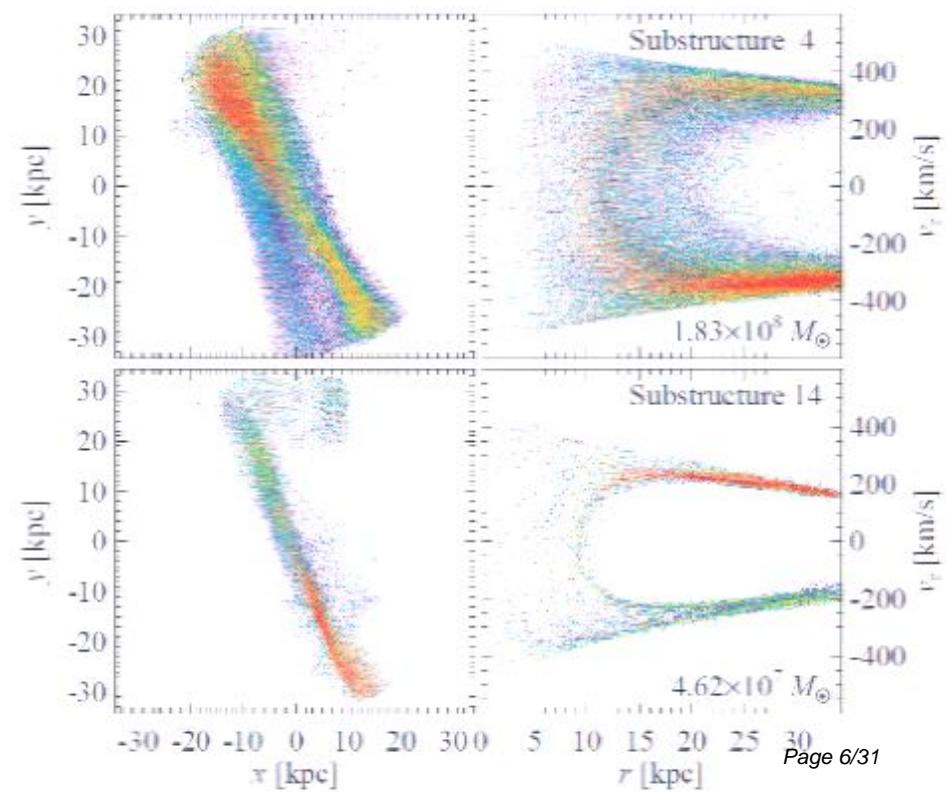
# Phase-Space Structure near the Sun



subhalos and tidal streams

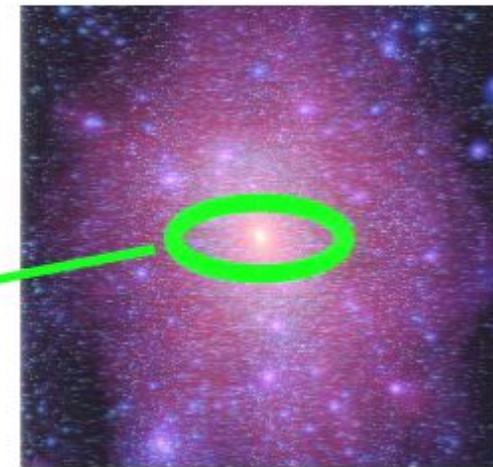
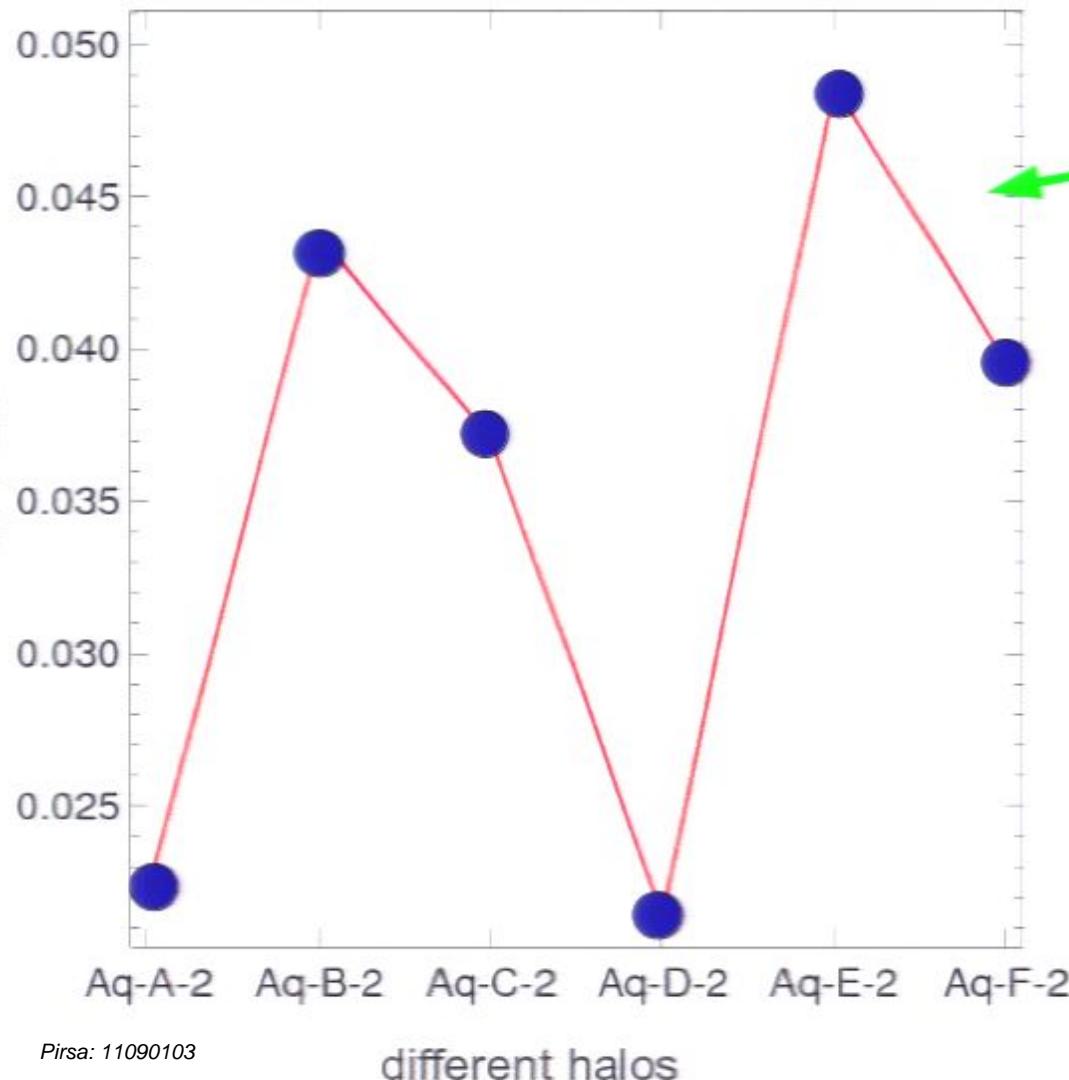
6D structure finding

Maciejewski et al. (2011)

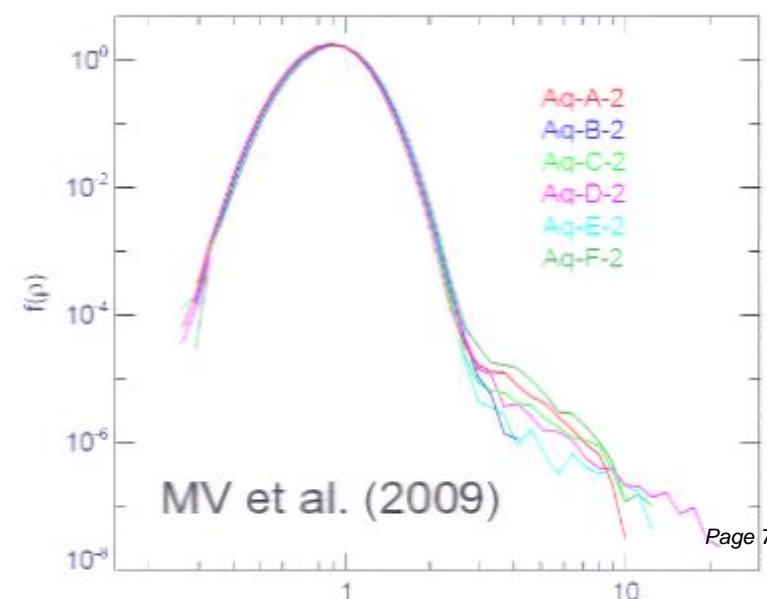


# DM Smoothness near the Sun

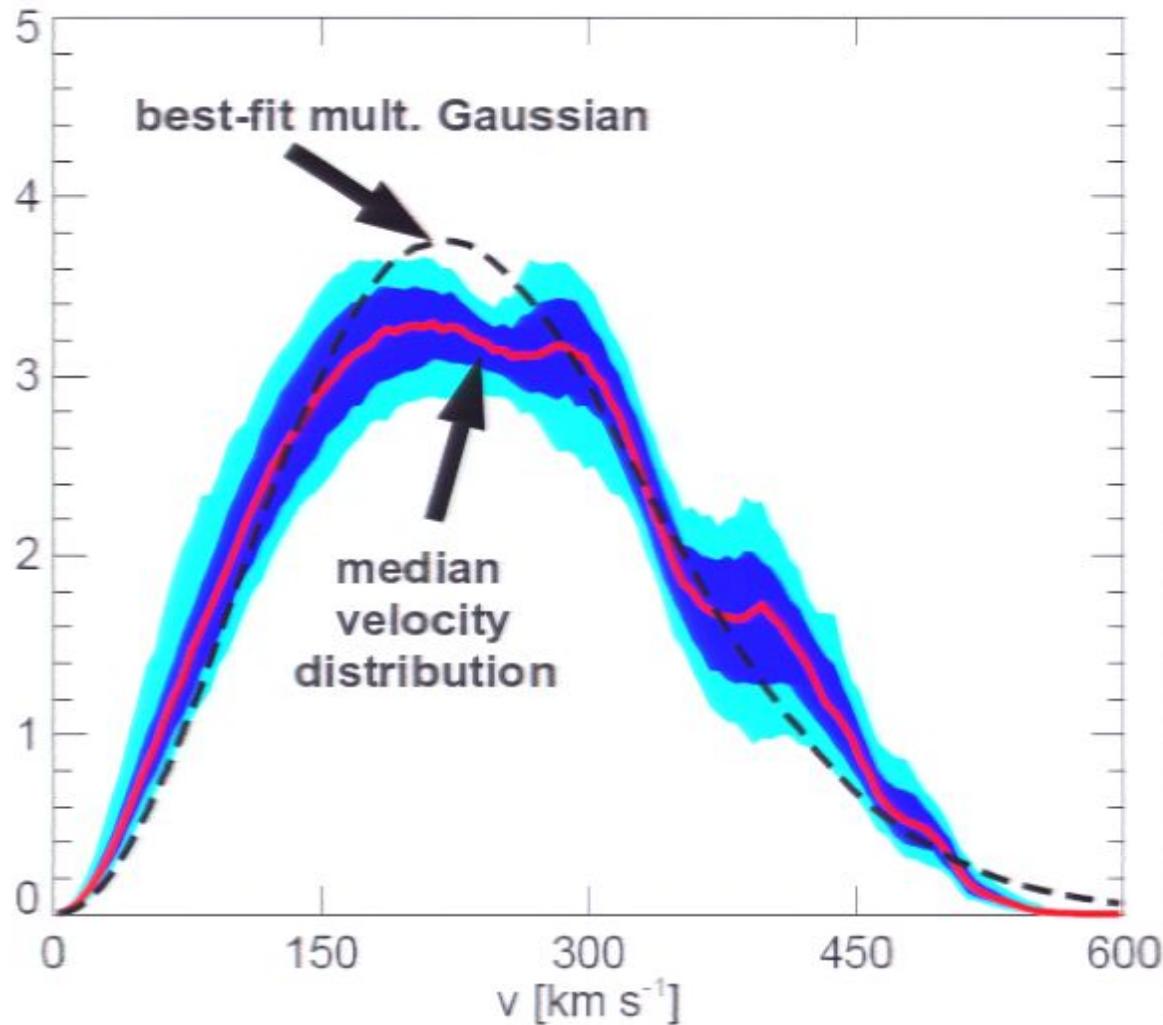
scatter standard deviation < 5%



Chance of hitting a subhalo small:  $\sim 10^{-4}$

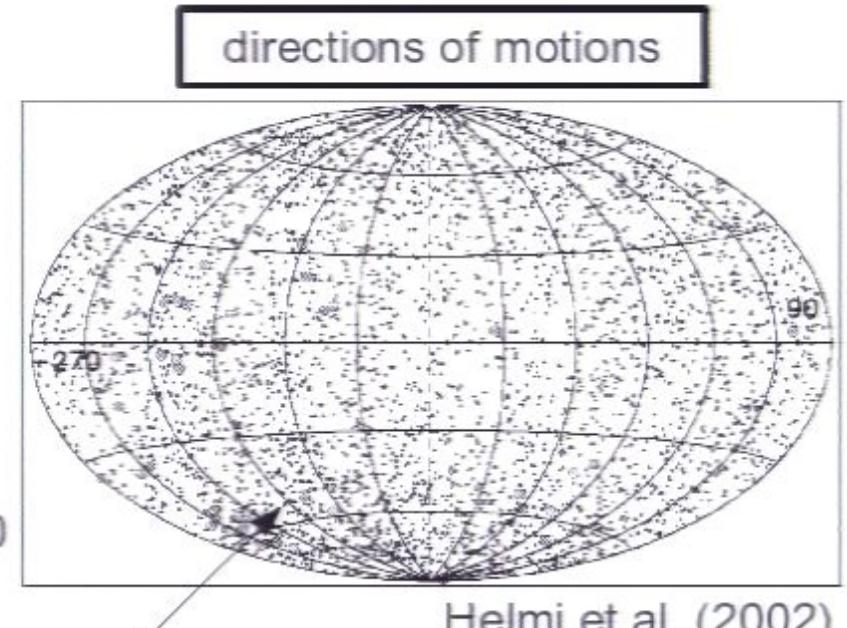


# Local Velocity Structure



velocity space structures at same velocity for given halo

not Maxwellian

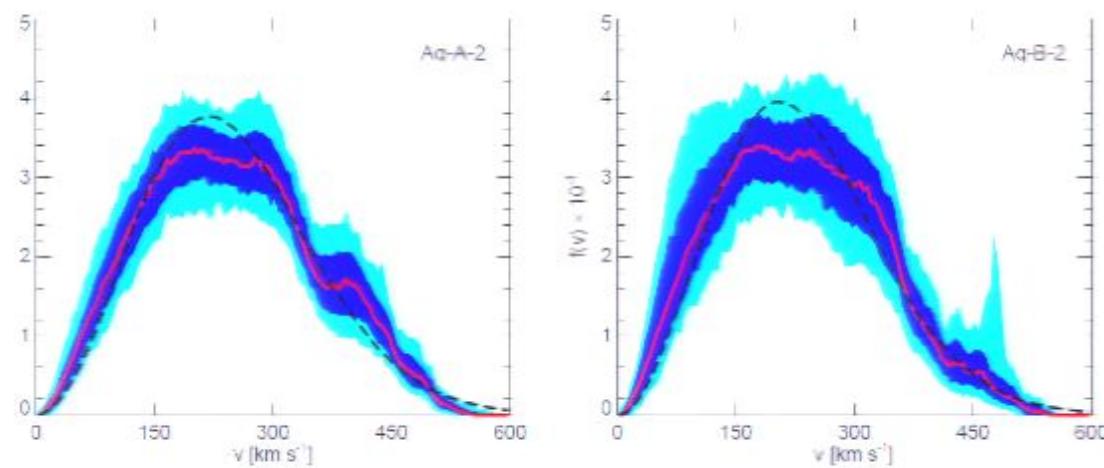


Helmi et al. (2002)

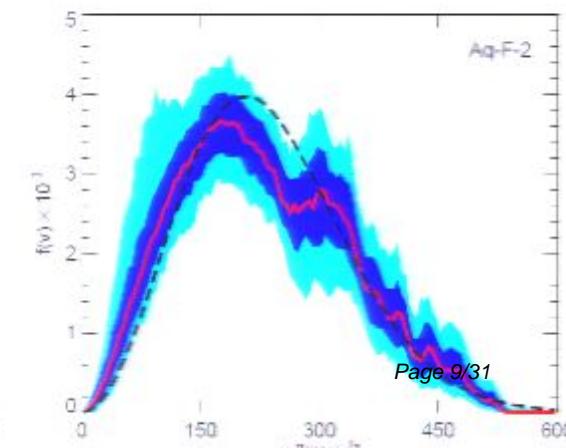
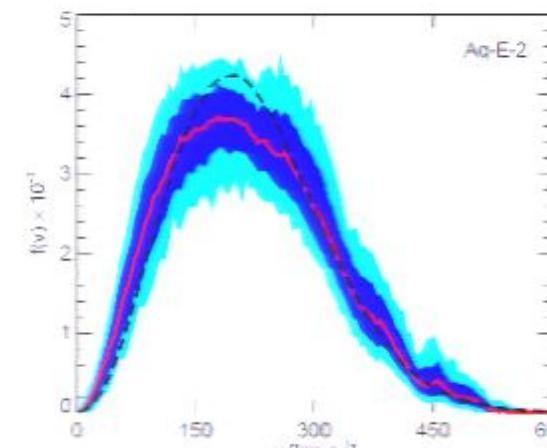
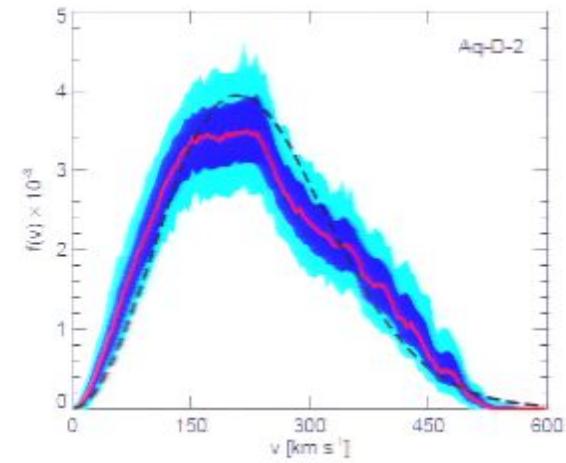
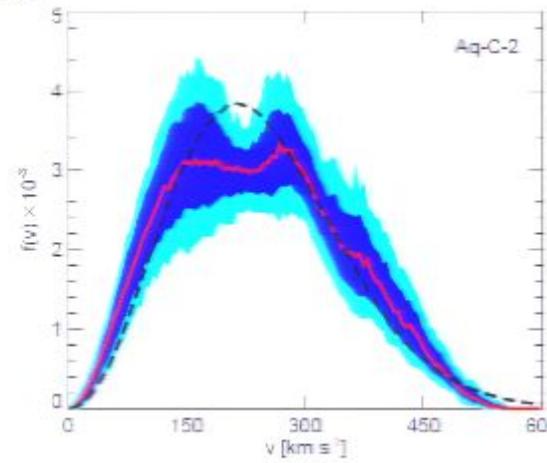
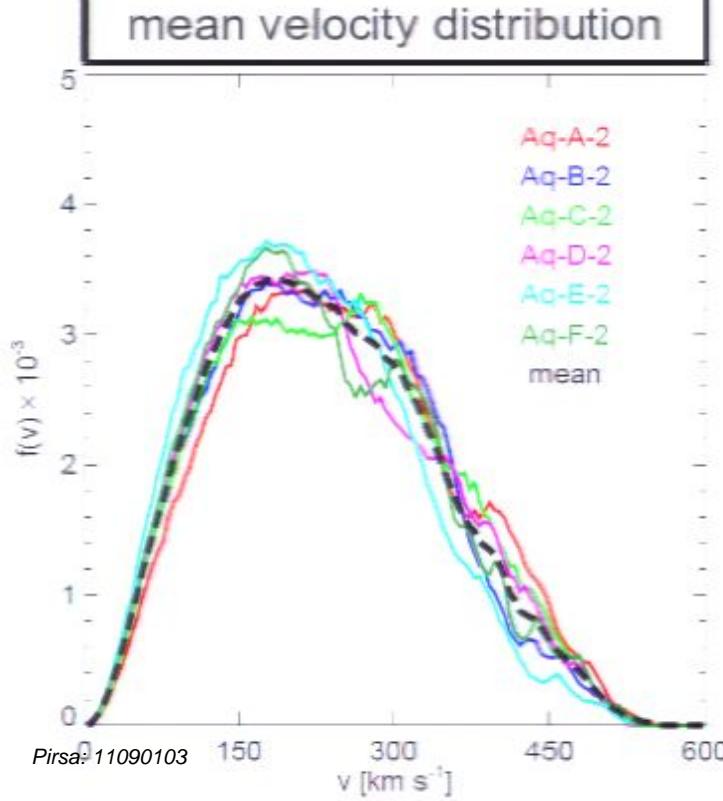
high velocity particles:  
anisotropic distribution  
(→ directional detection)

# Different Halos

features are present in all halos  
but at different velocities



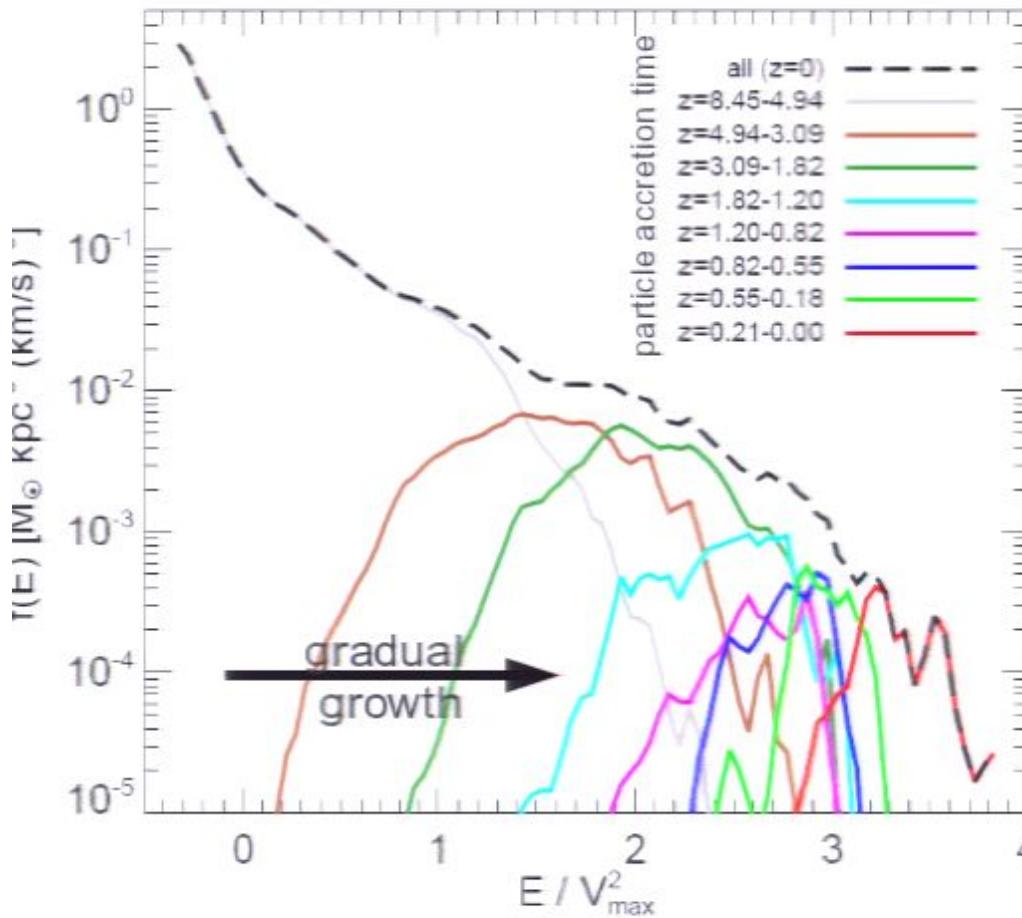
mean velocity distribution



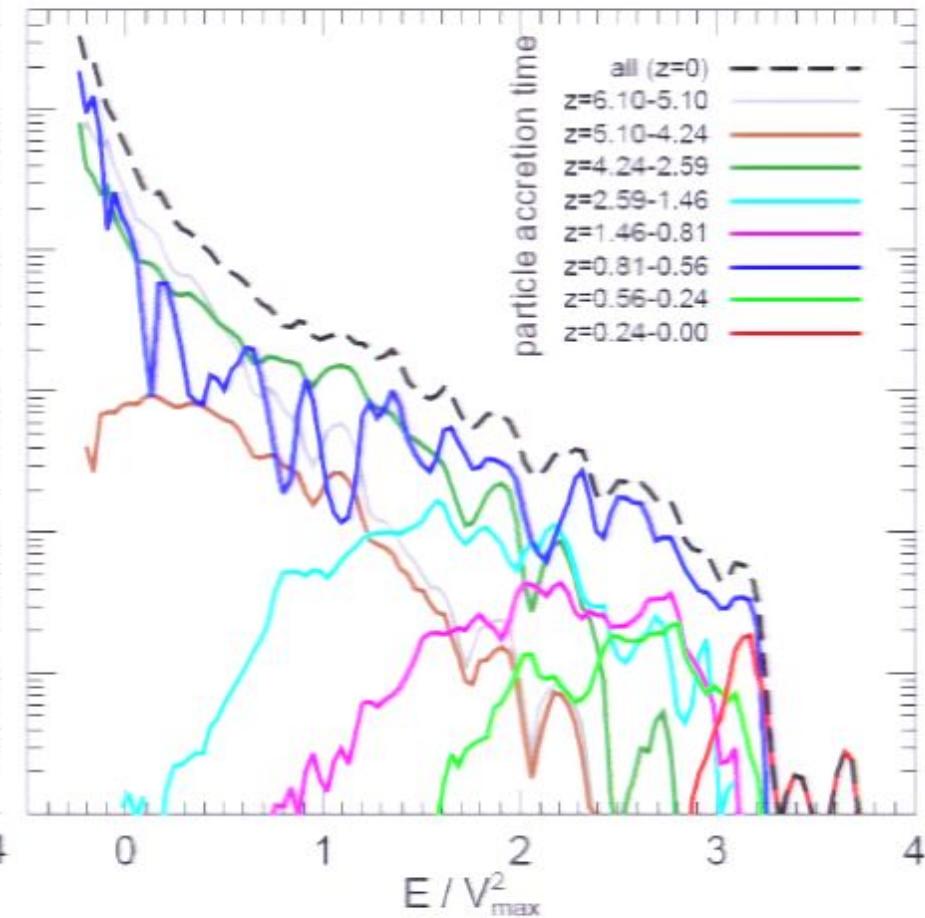
# Phase-Space Density

structure related to formation history

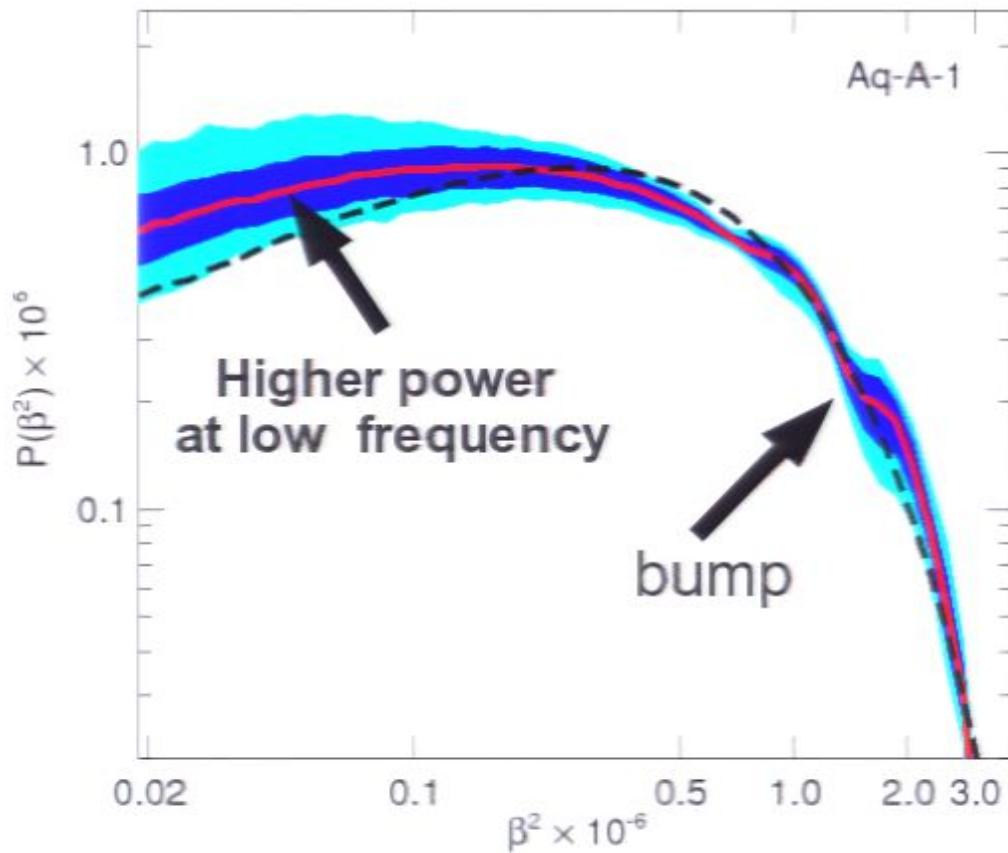
Halo A: quiet formation history



Halo B: active formation history



# Signature in Detector Signal



Axion microwave spectrum

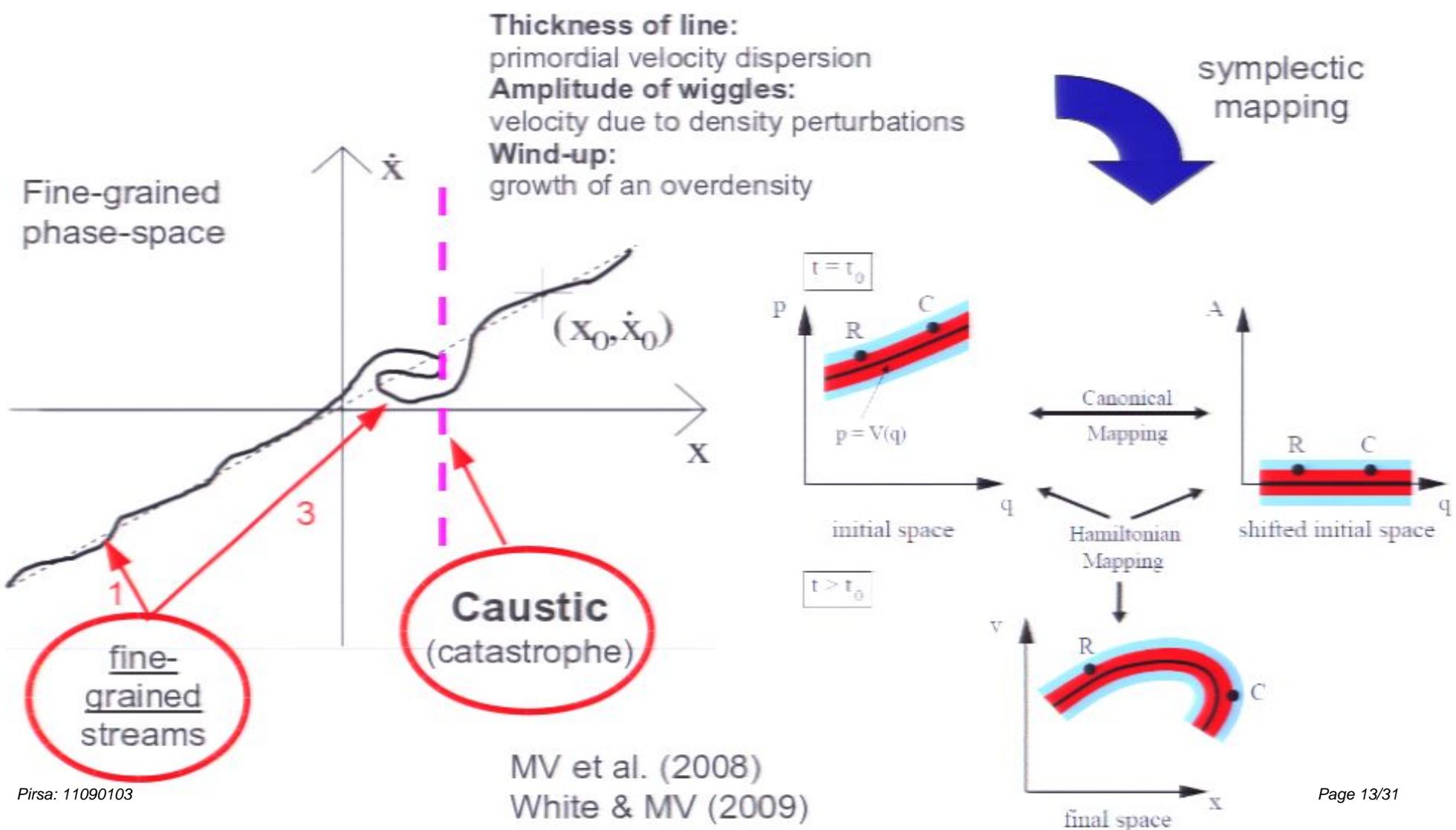
$$\nu_a = 241.8 \left( \frac{m_a}{1\mu\text{eV}/c^2} \right) \left( 1 + \frac{1}{2}\beta^2 \right) \text{MHz}$$

# **Fine-Grained Structure of LCDM Halos**

# CDM – Small Scales

CDM is cold and collisionless

→ CDM restricted to 3D hypersurface in 6D phase-space



# Analytic Estimates

## Self-similar halo formation:

Fillmore & Goldreich (1984), Bertschinger (1985),  
Mohayaee & Salati (2008);  
Mohayaee et al (2006); ...

## Caustic ring model:

Duffy & Sikivie (2008);  
Natarajan & Sikivie (2008);  
Onemli & Sikivie (2007);  
Natarajan & Sikivie (2007);  
Sikivie et al (1997); ...

## General arguments:

Hogan (2001)

### Predictions

- ~100 streams at solar position
- significant annihilation boost (5-100)
- strong caustic rings
- discrete velocity distribution
- distinct caustic structures

How realistic are these models?

# SELF-SIMILAR GRAVITATIONAL COLLAPSE IN AN EXPANDING UNIVERSE<sup>1</sup>

JAMES A. FILLMORE AND PETER GOLDREICH

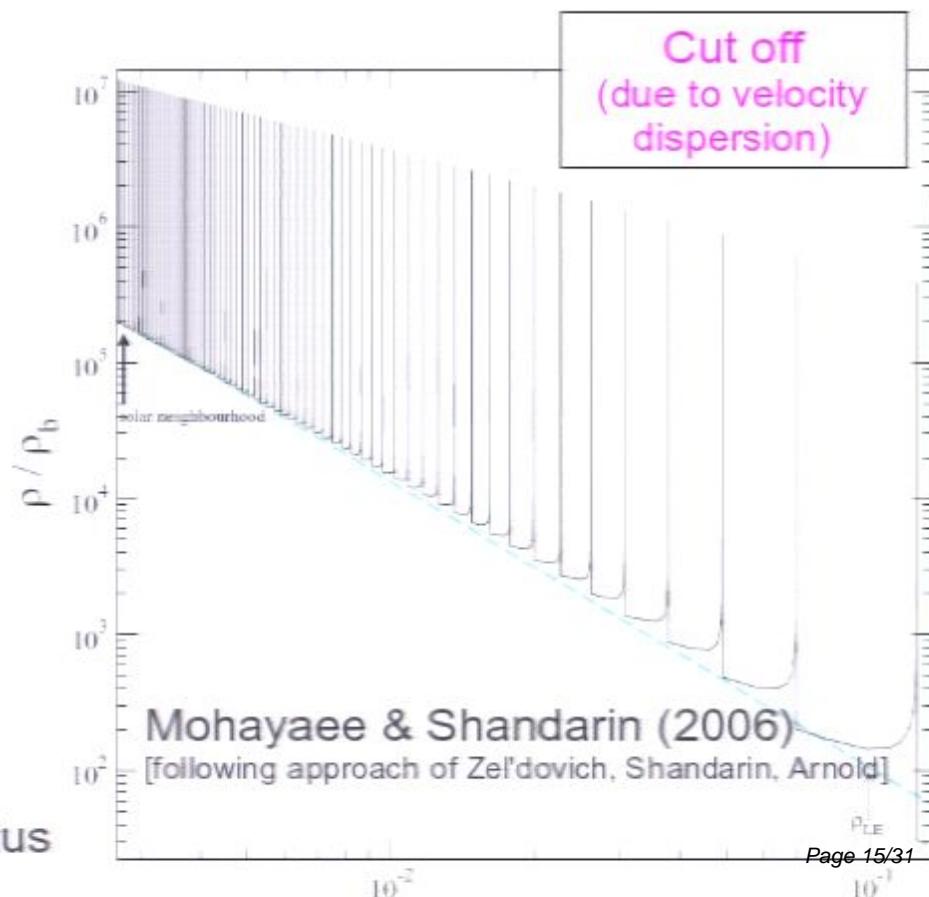
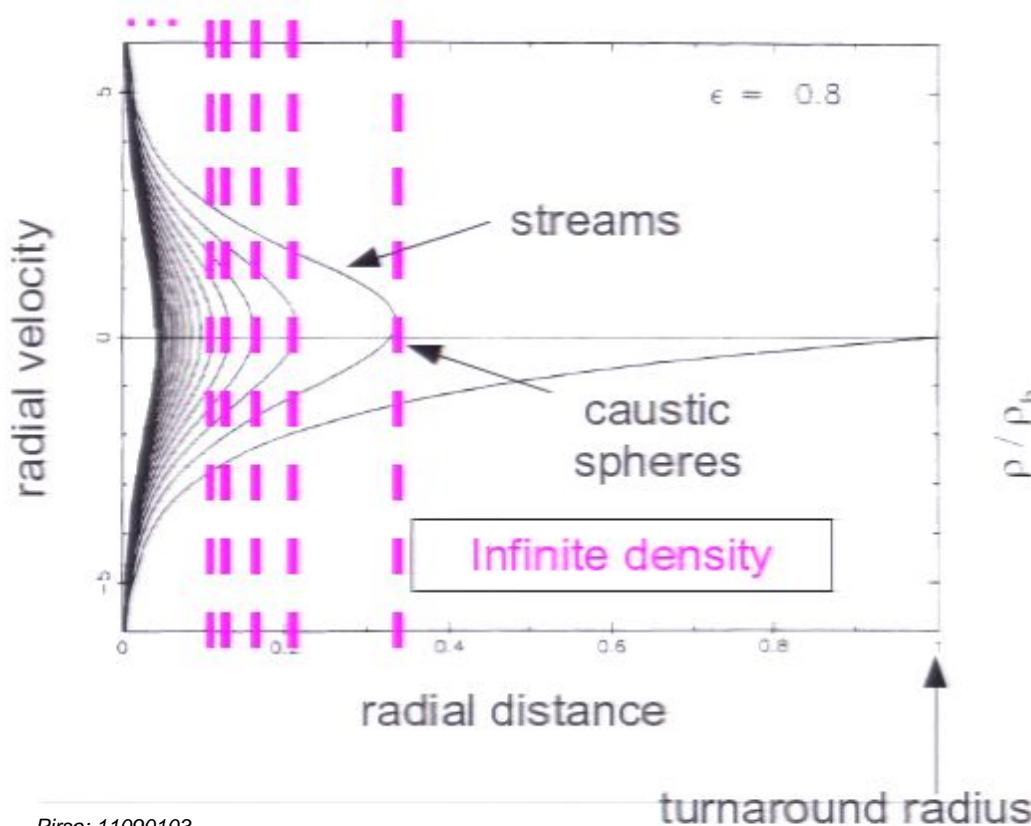
California Institute of Technology

Received 1983 October 10; accepted 1983 December 5

## ABSTRACT

We derive similarity solutions which describe the collapse of cold, collisionless matter in a perturbed Einstein-de Sitter universe. We obtain three classes of solutions, one each with planar, cylindrical, and spherical symmetry. Our solutions can be computed to arbitrary accuracy, and they follow the development of structure in both the linear and nonlinear regimes.

Subject headings: cosmology — relativity

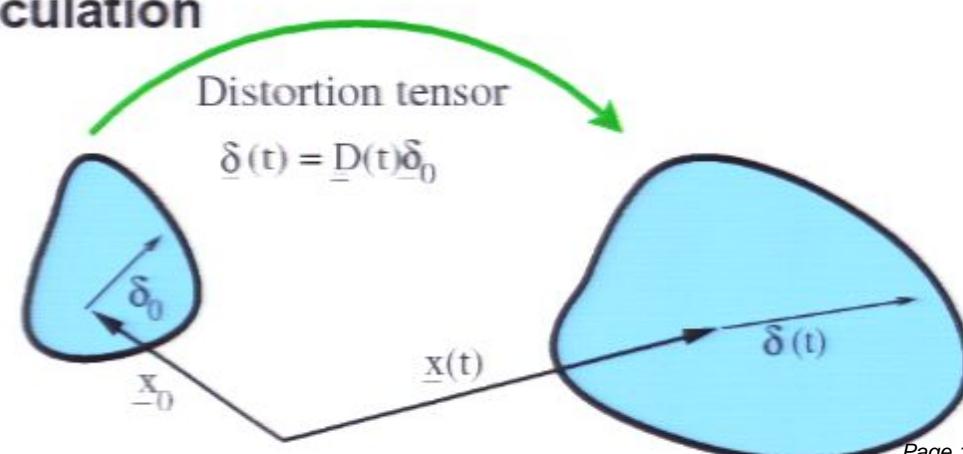


# Resolving Fine-Grained Structures

**Problem:** simulations have too coarse phase-space sampling  
(→ missing many orders of magnitude in mass resolution/particle number)

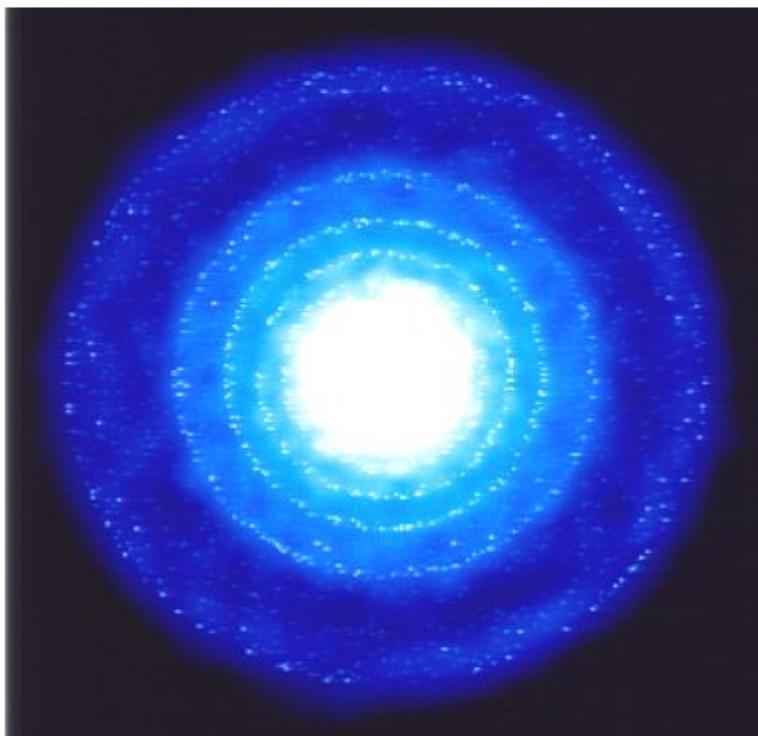
**Solution:** follow the local phase-space evolution  
(→ with a phase-space geodesic deviation equation)

- calculation of stream density
  - identification of caustics
  - Monte-Carlo estimate of intra-stream annihilation
- allows caustic annihilation calculation

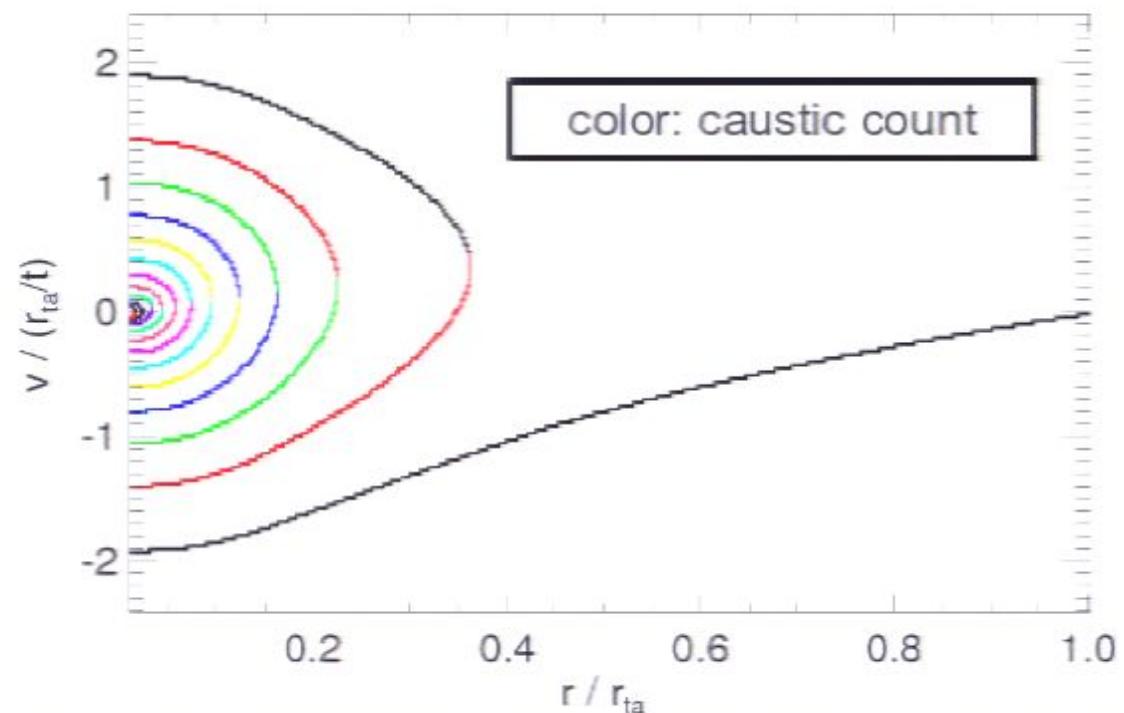


# Caustic Annihilation Radiation: 1D Gravity

annihilation signal

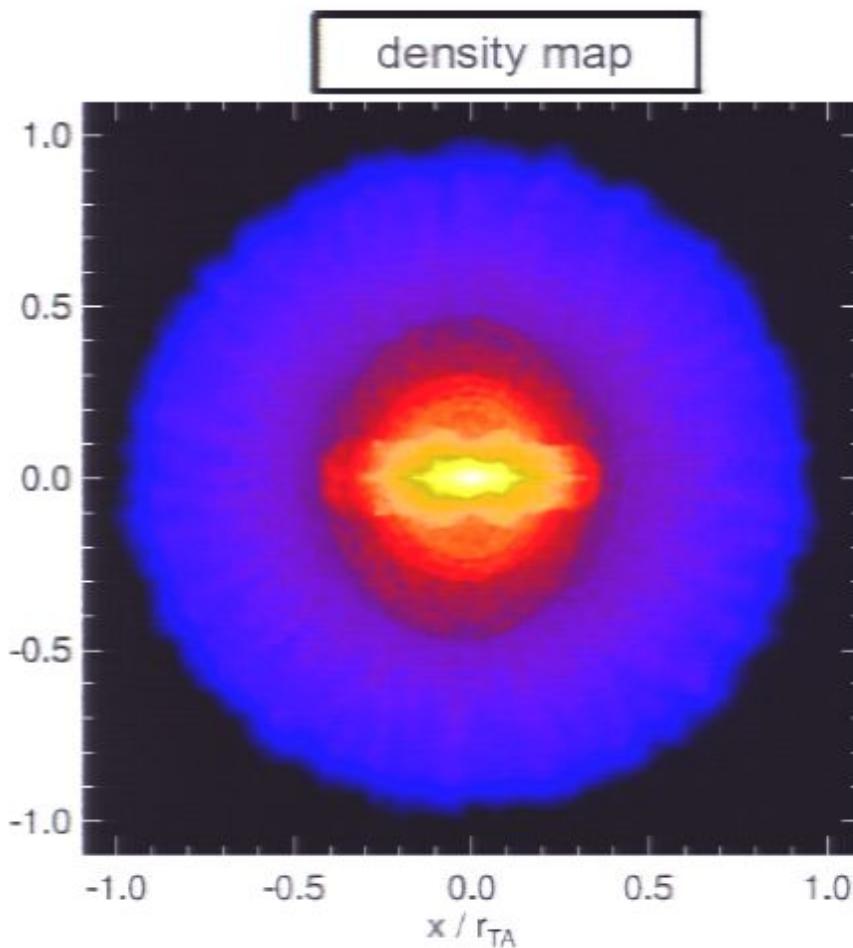


caustic spheres on top of  
smooth annihilation signal

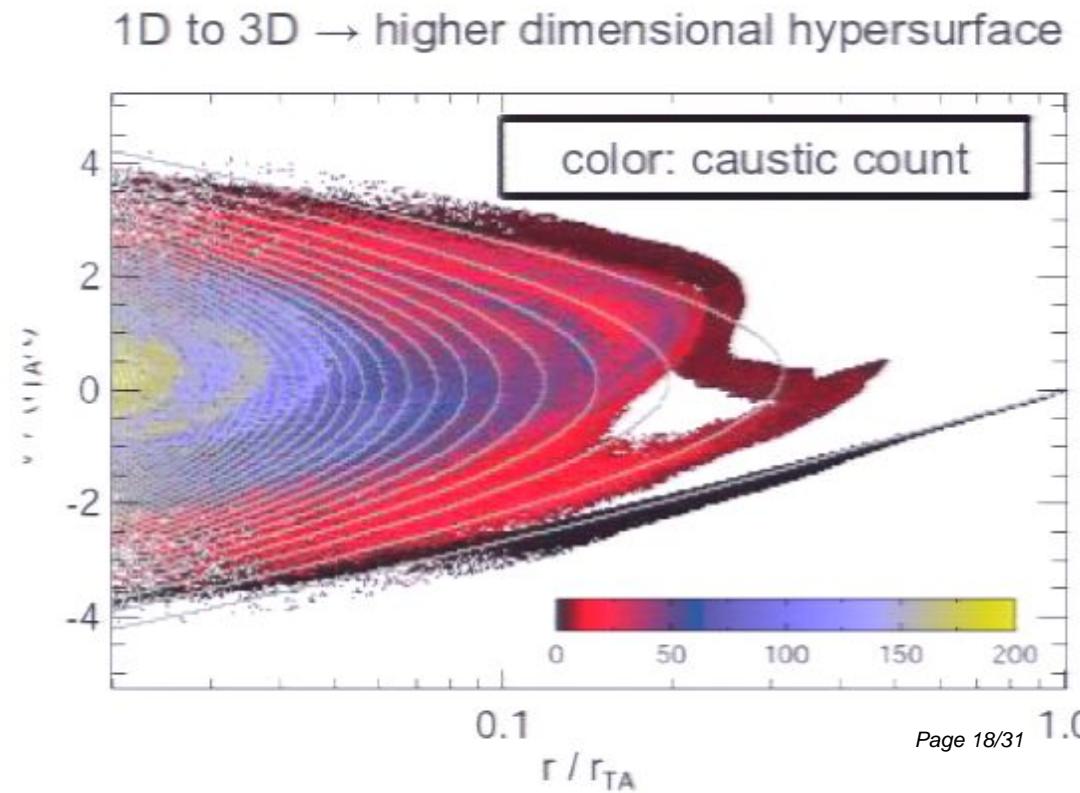


**initial conditions:**  
single density perturbation in an  
otherwise unperturbed EdS universe

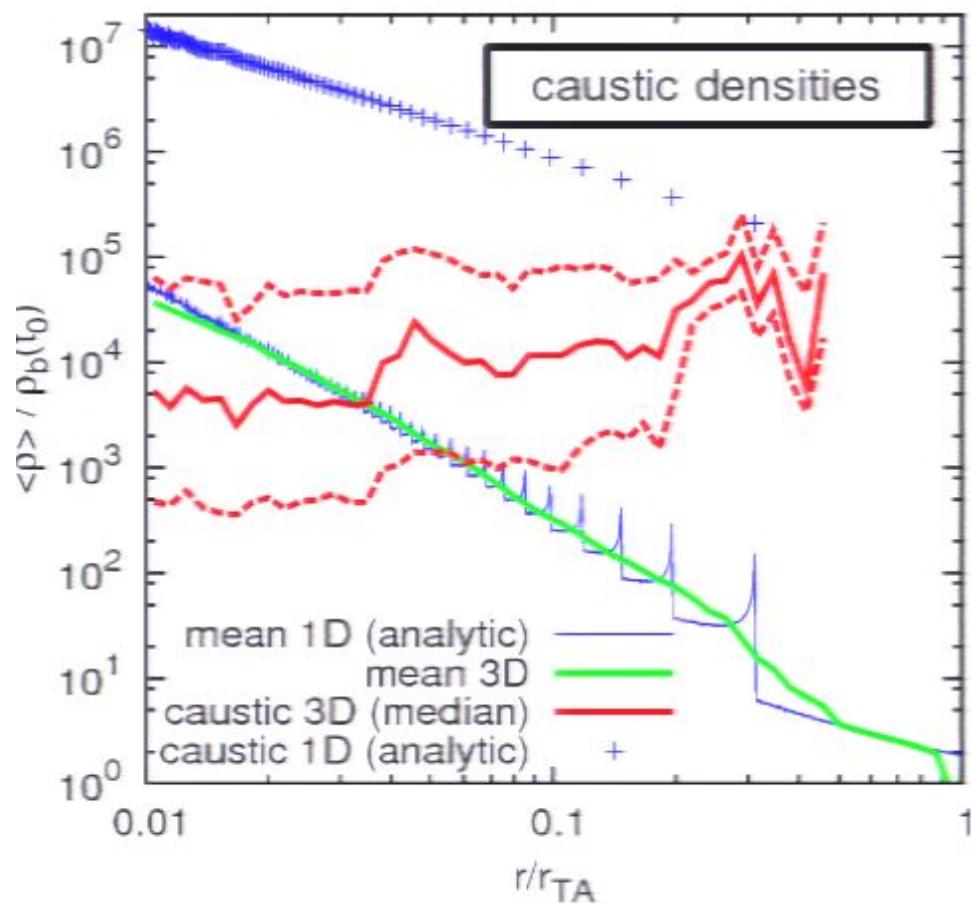
# Collapse of an Isolated Halo in 3D Gravity



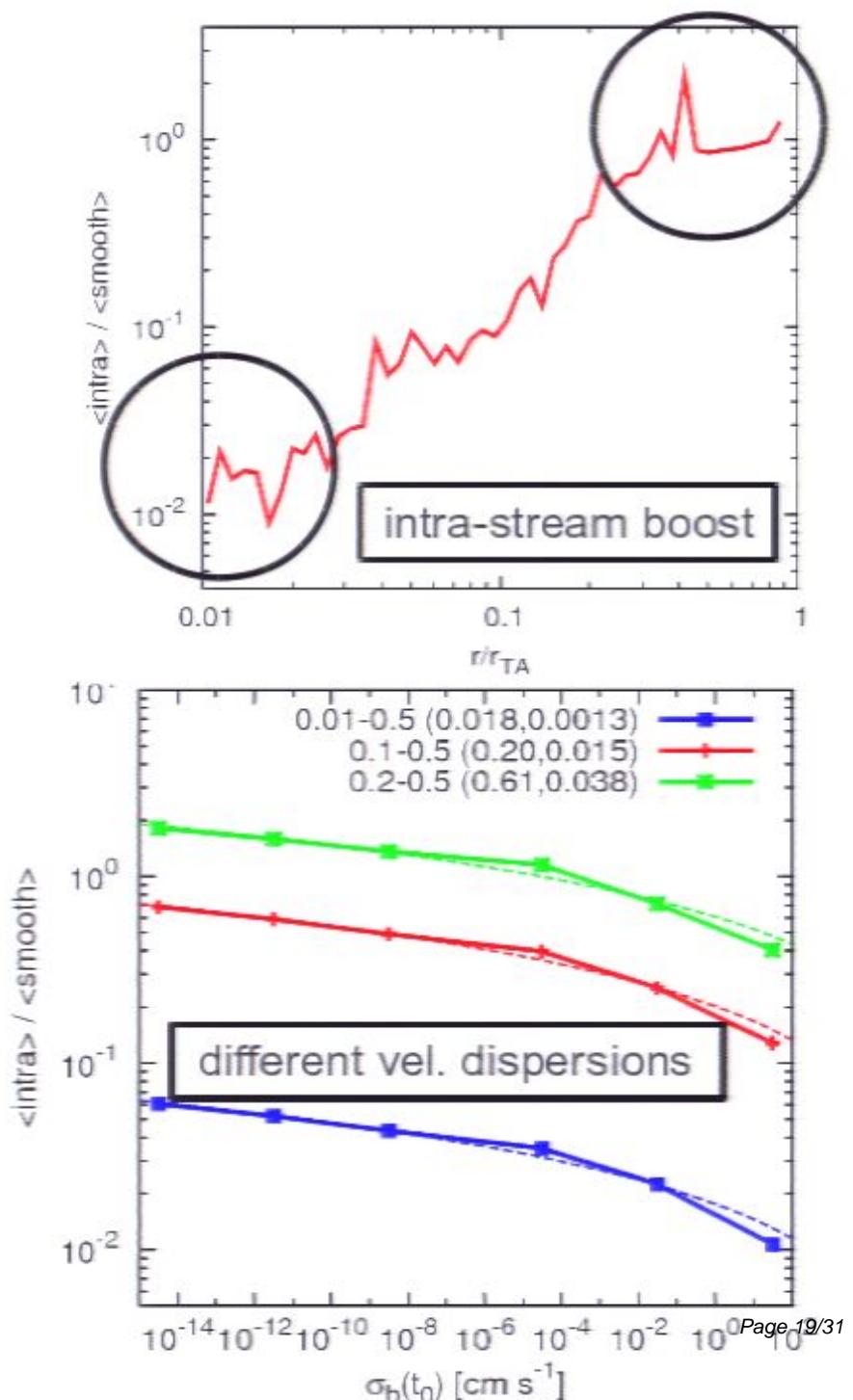
**Instabilities**  
MV et al. (2009)



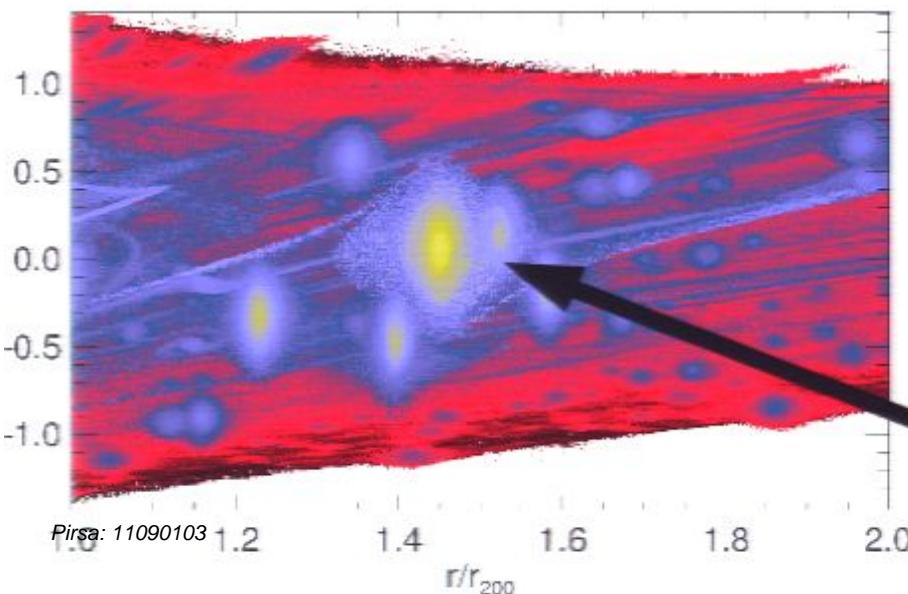
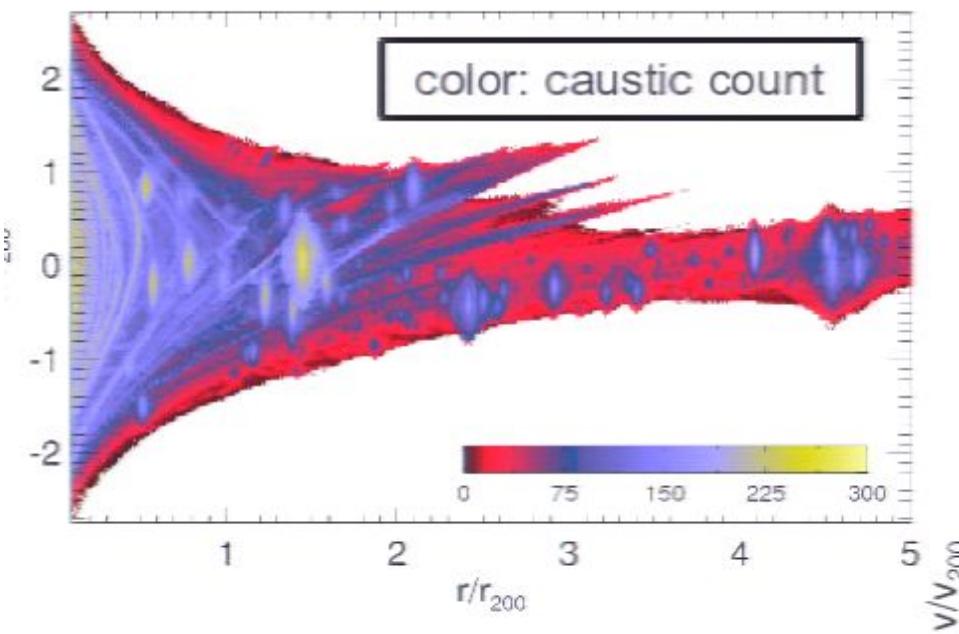
# Caustics in 3D



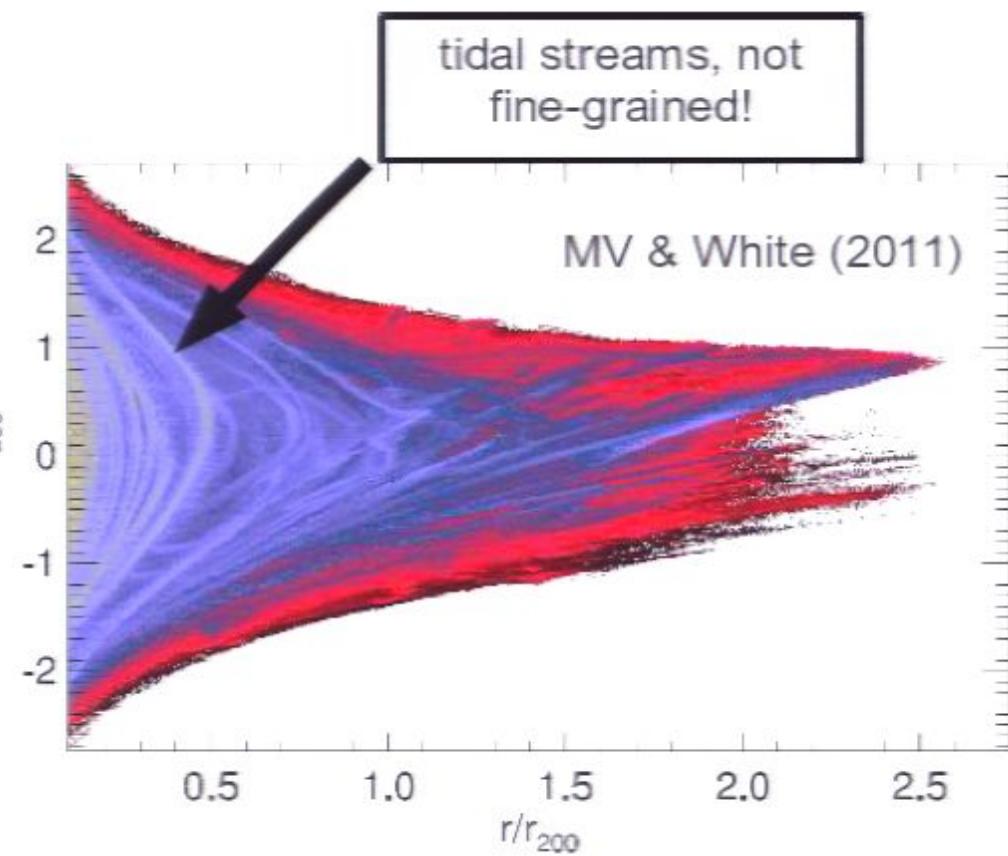
caustic annihilation negligible in inner halo,  
but can boost signal in the outer part



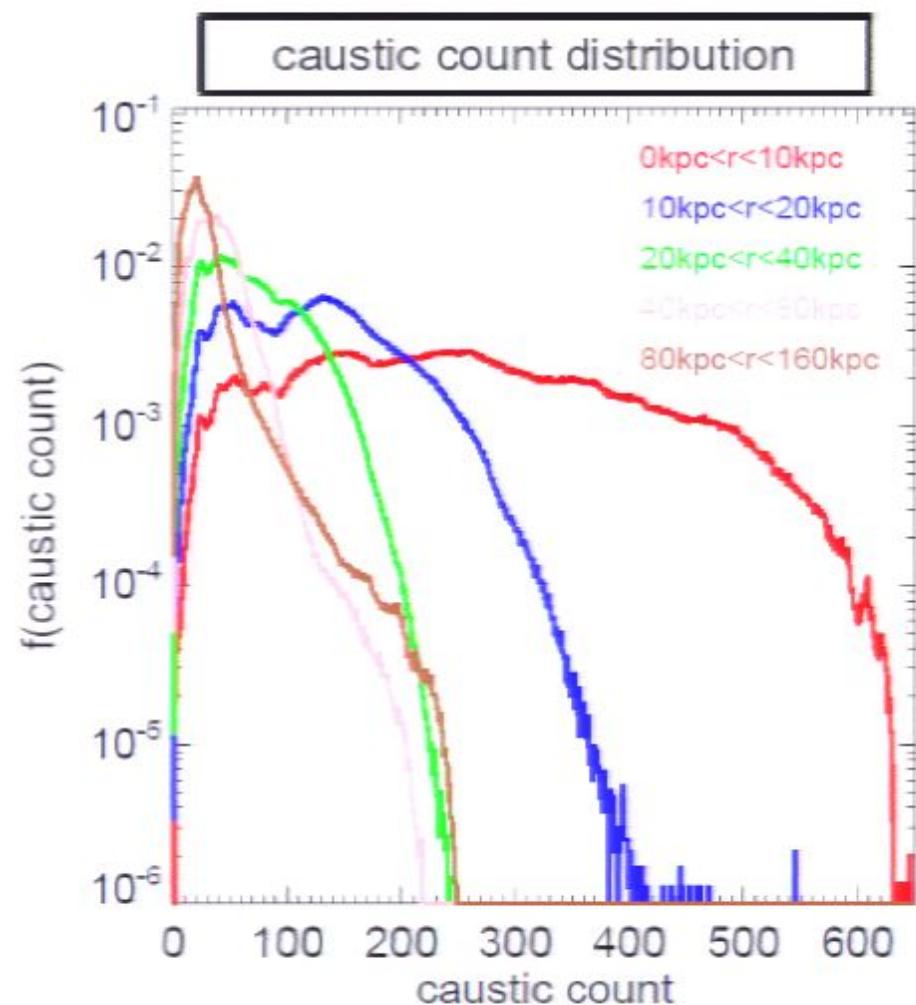
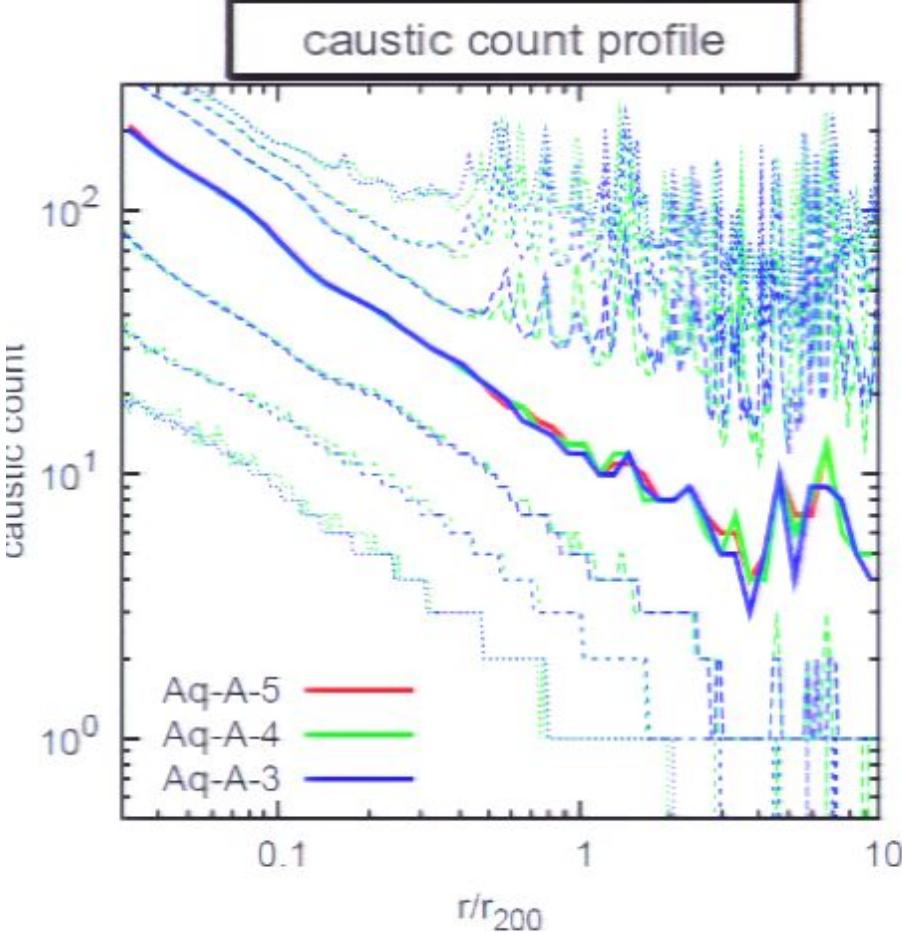
# Fine-Grained Structure of LCDM Halos



results for Milky Way-like DM halo

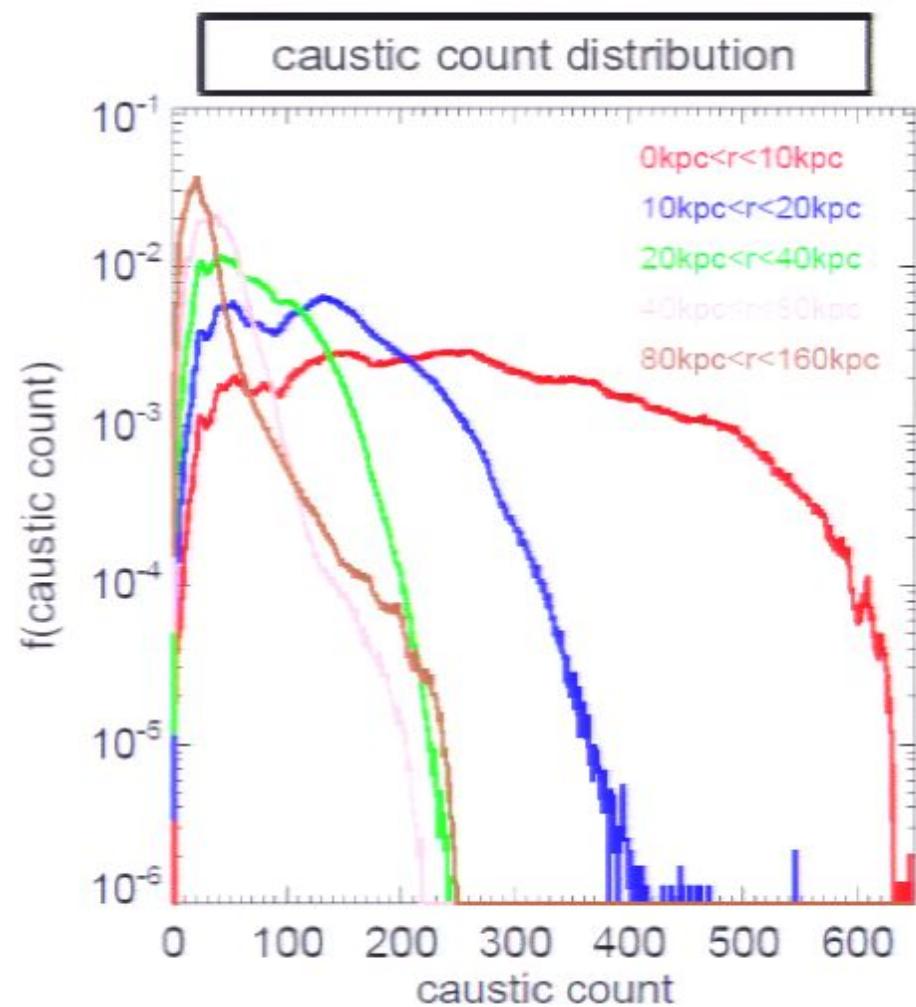
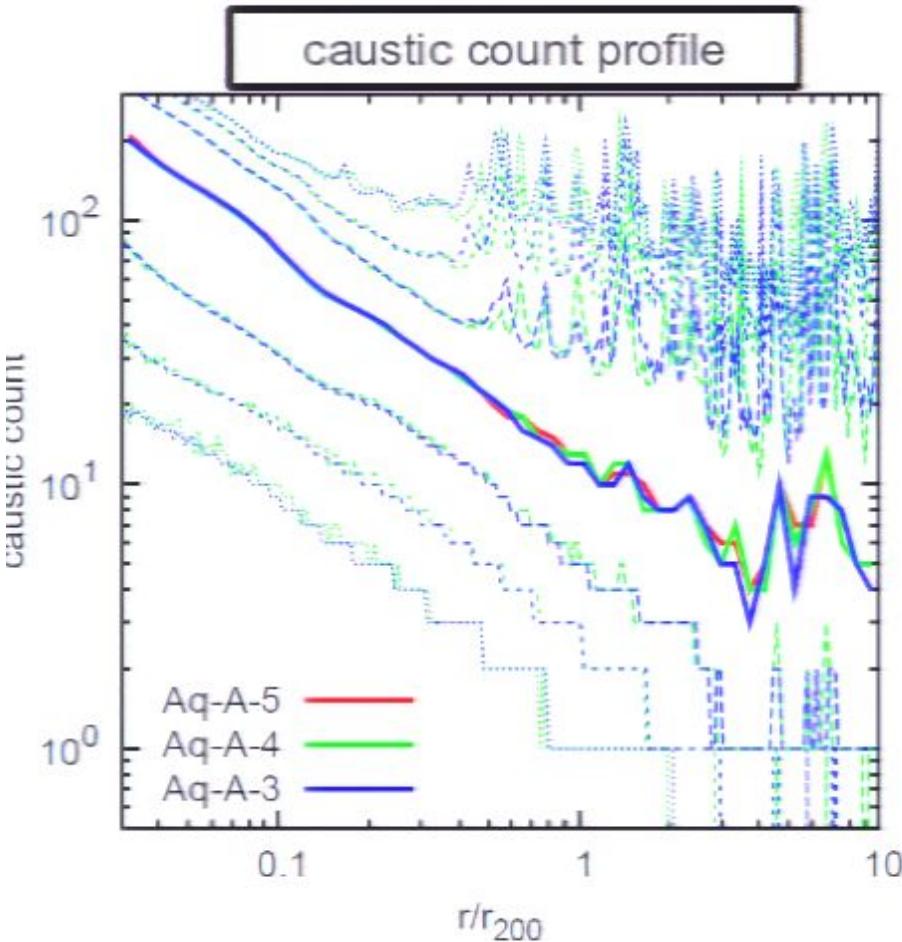


# Caustic Count Distribution



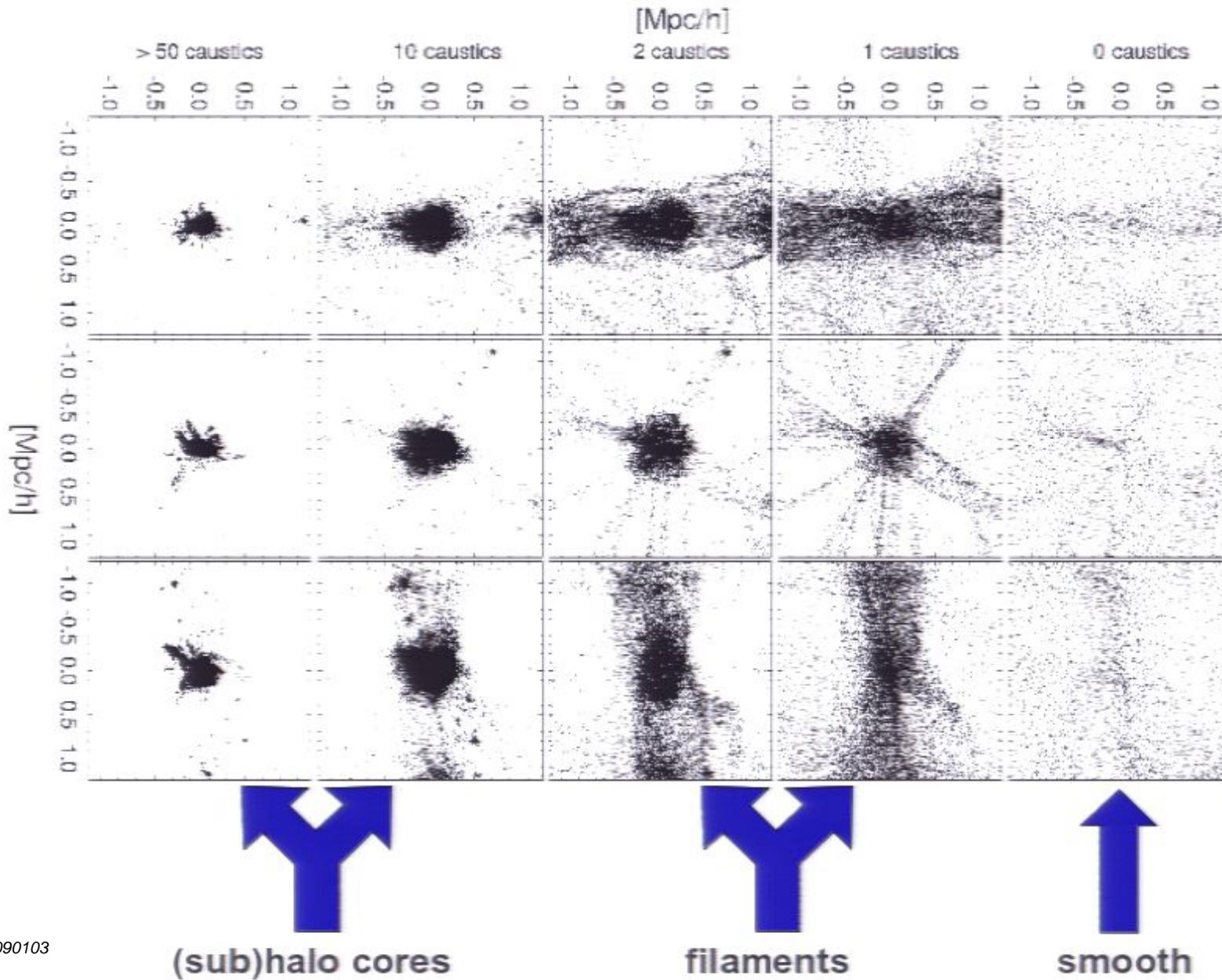
- broad distribution at all radii
- outer part broader due to subhalos
- tracks dynamical age (largest in center)

# Caustic Count Distribution

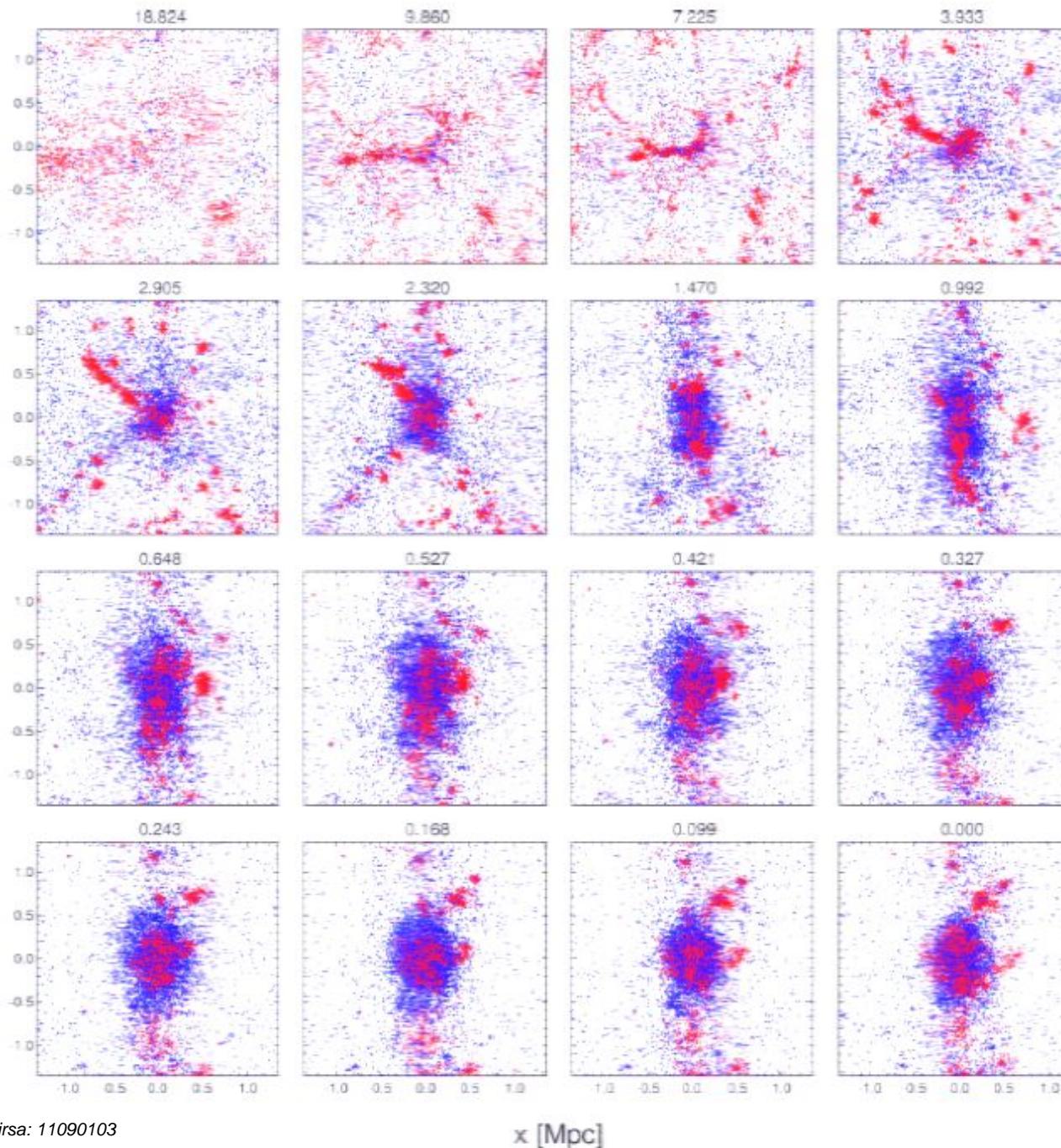


- broad distribution at all radii
- outer part broader due to subhalos
- tracks dynamical age (largest in center)

# Filtering the Cosmic Web



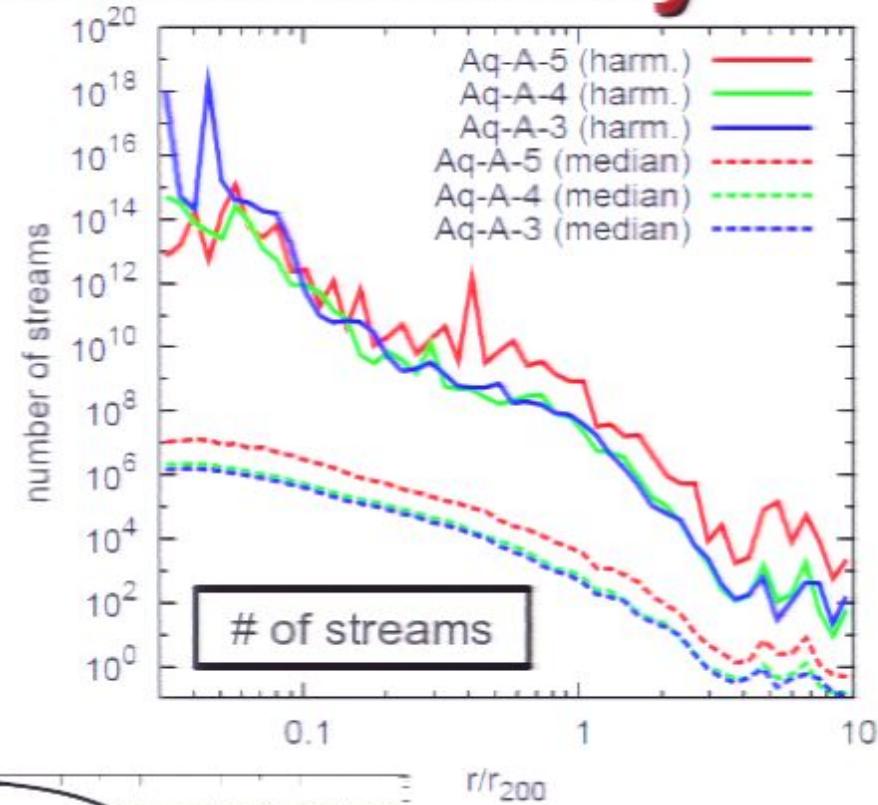
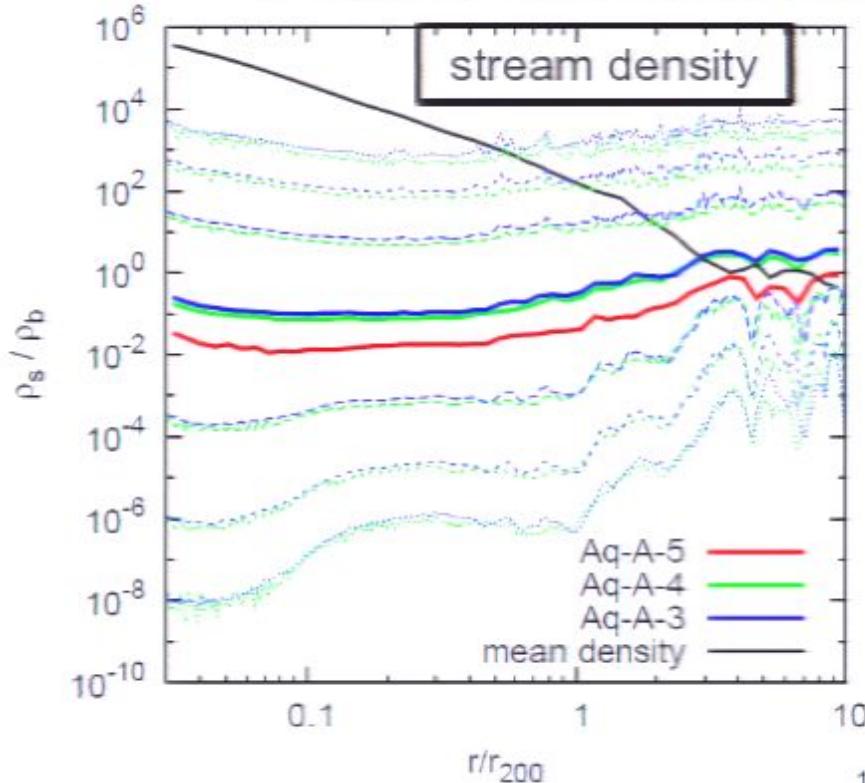
# Origin of high / low Stream Density Regions



low stream density regions:  
stronger mixing in early  
forming objects at high z  
→ strong mixing

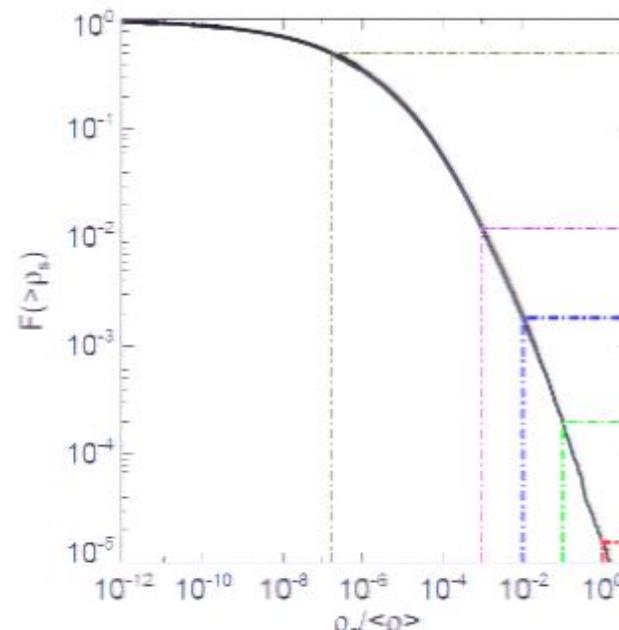
high stream density regions:  
more diffuse, smoothly  
accreted at low z  
→ less mixing

# Fine-Grained Stream Density



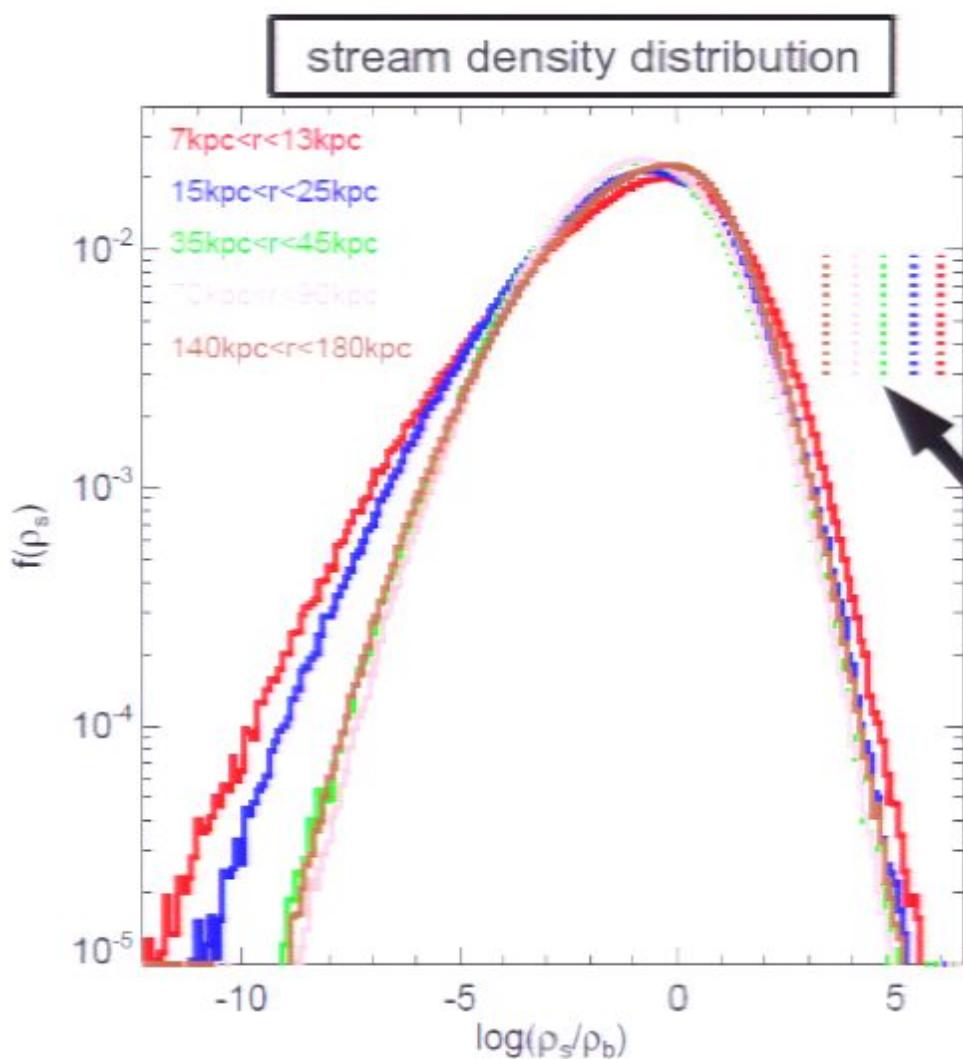
- stream density low
- locally large number of streams

If the dark matter is made of **axions** then a resonant detector should find an energy spectrum where a few tenths of a percent of the total energy density is concentrated in a few very narrow spectral lines.



small amount of high stream density mass

# Fine-Grained Stream Density

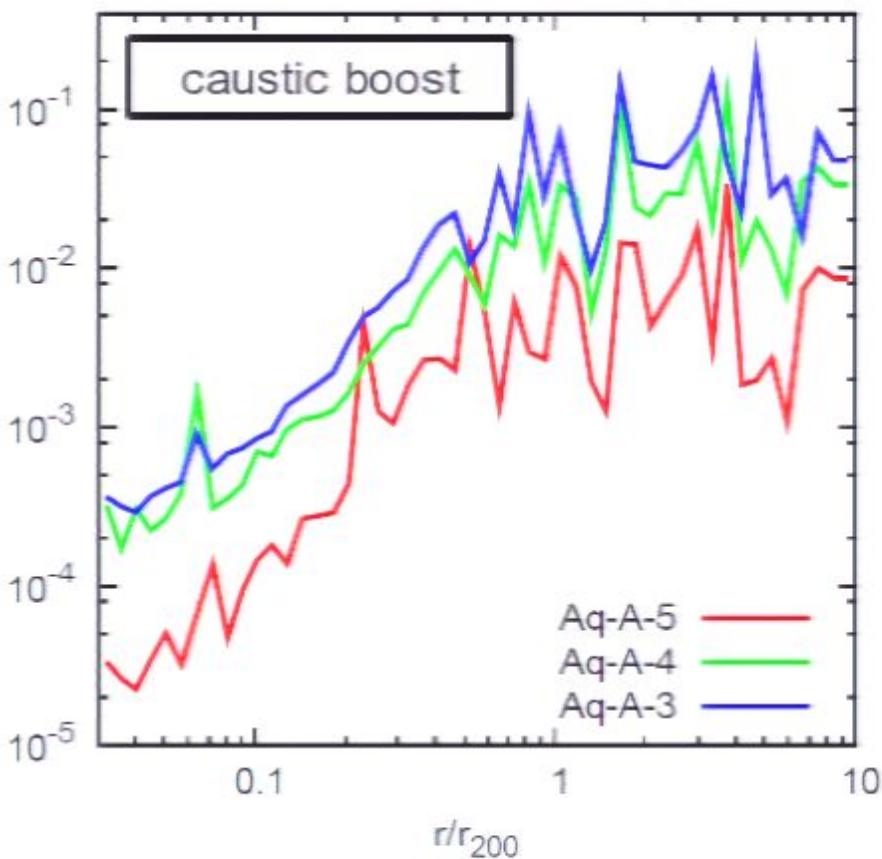


stream density distribution  
in different radial shells:

- very broad distribution
- smaller than local density

mean density in shell

# Local Annihilation Boost Factor



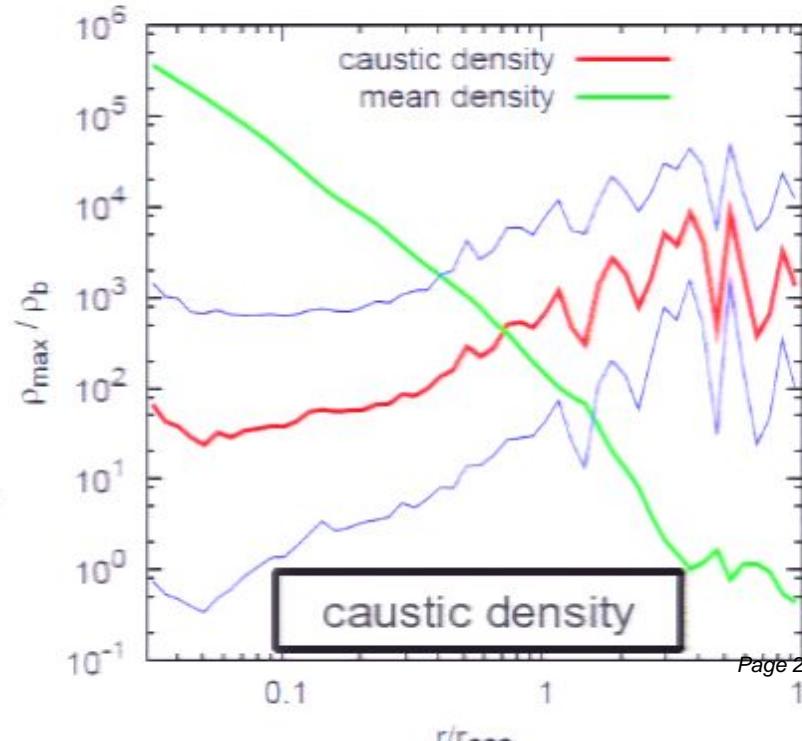
**reason:**

caustic density small compared to mean density

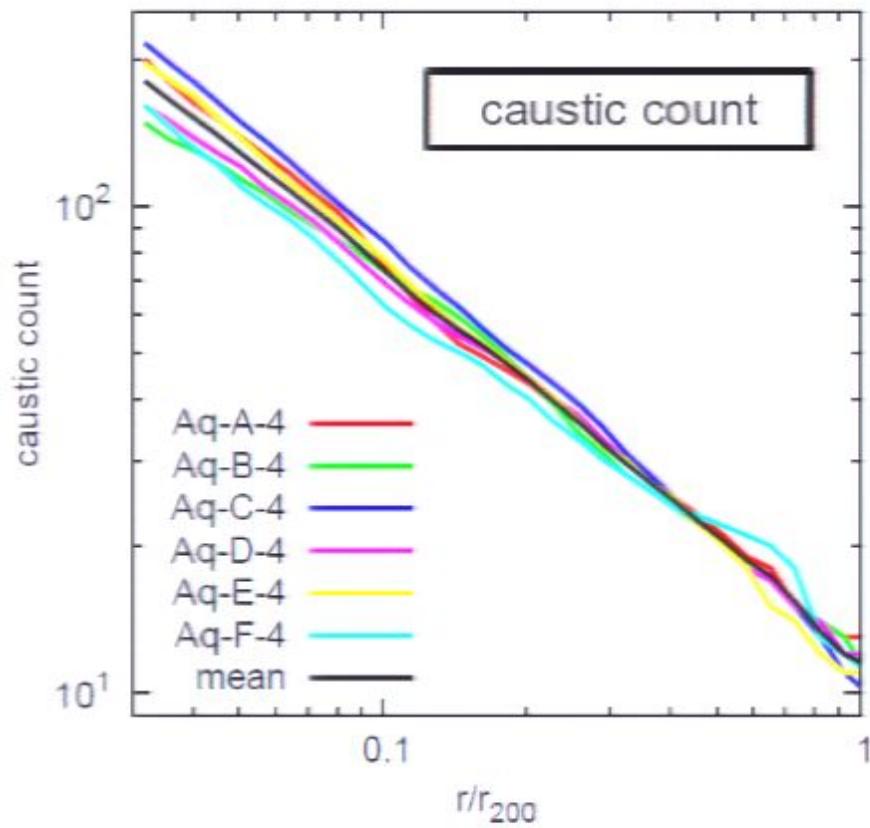
- essentially no boost at solar circle
- no distinct/dense caustic structures



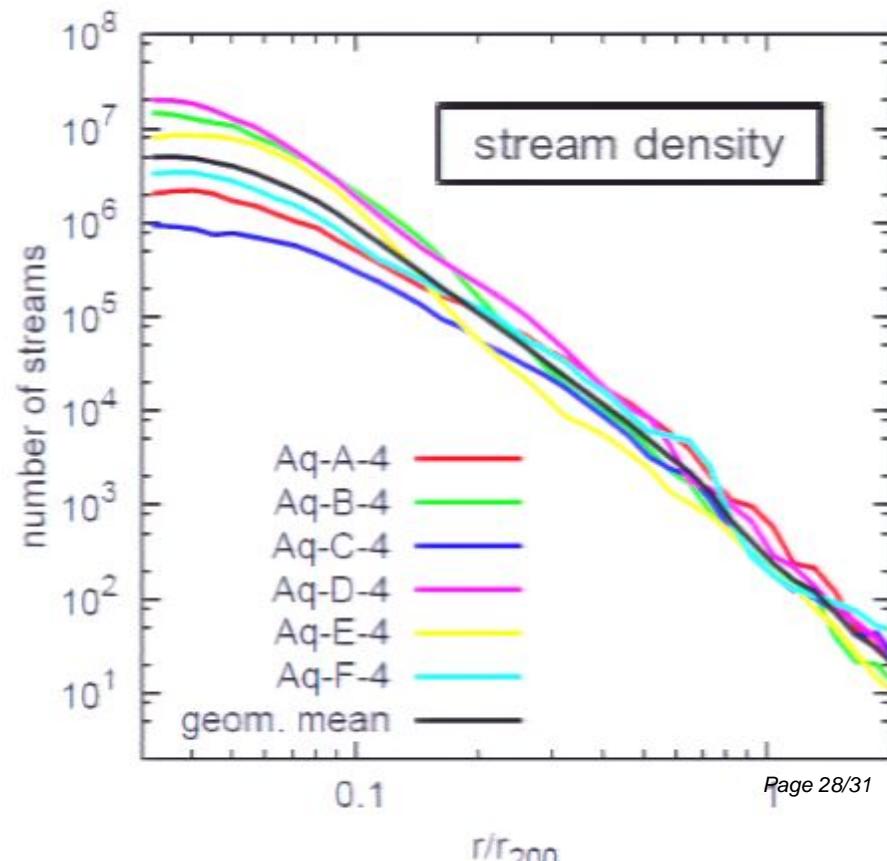
'standard' annihilation rate calculations do not miss a large fine-grained contribution



# Halo-to-Halo Scatter

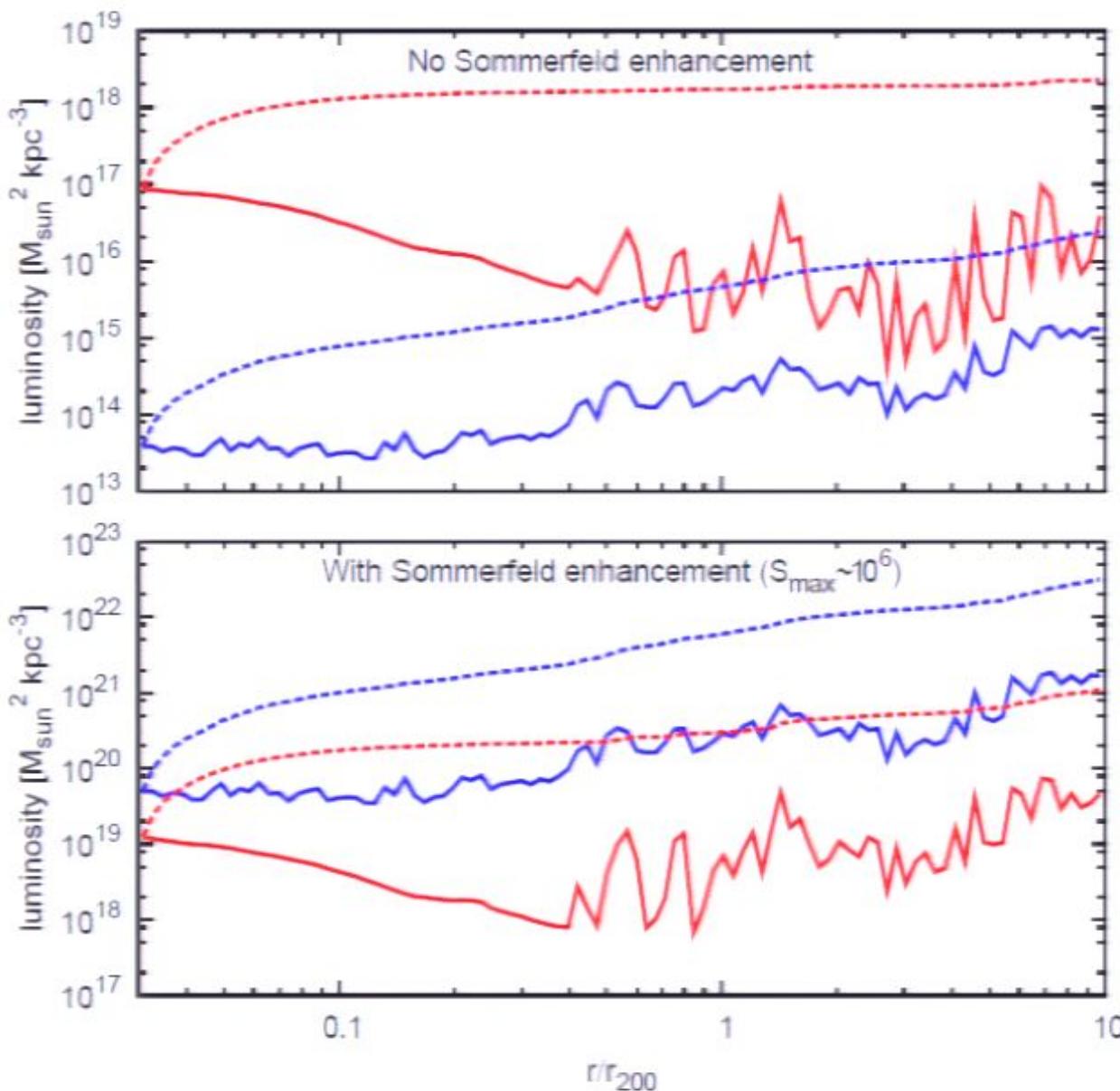


check different halos in same mass range



- there is not much variation
- results pretty universal for that halo mass
- Galactic halo should look similar

# Sommerfeld Enhancement



regions of low velocity dispersion dominate annihilation signal:

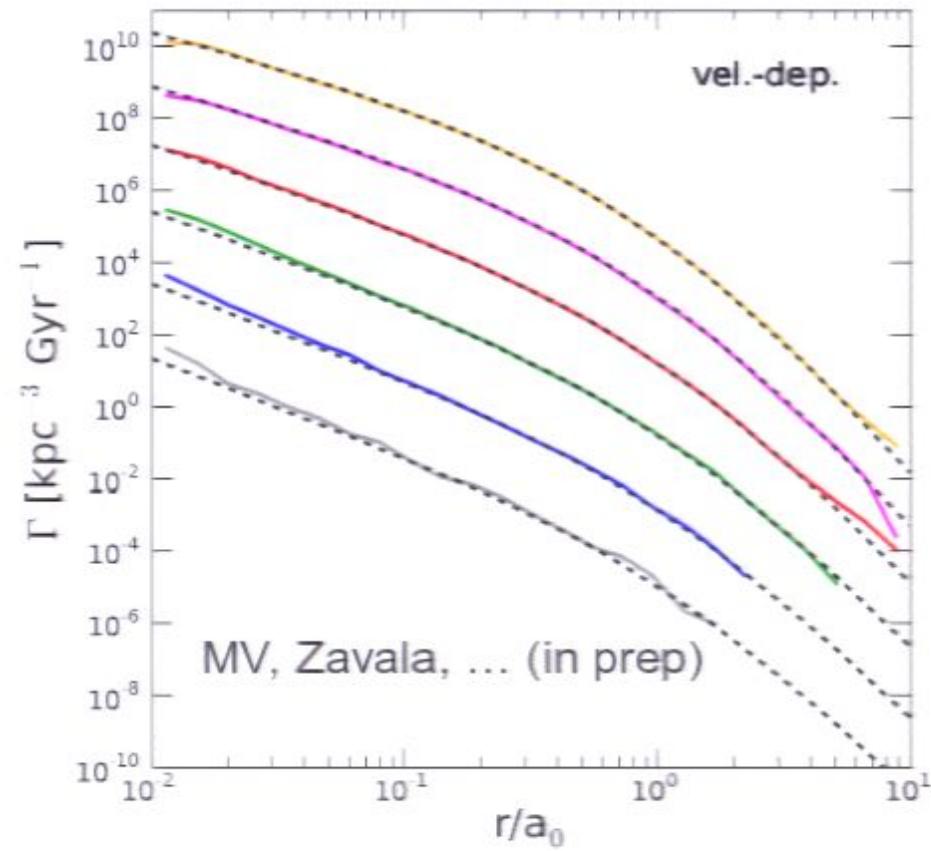
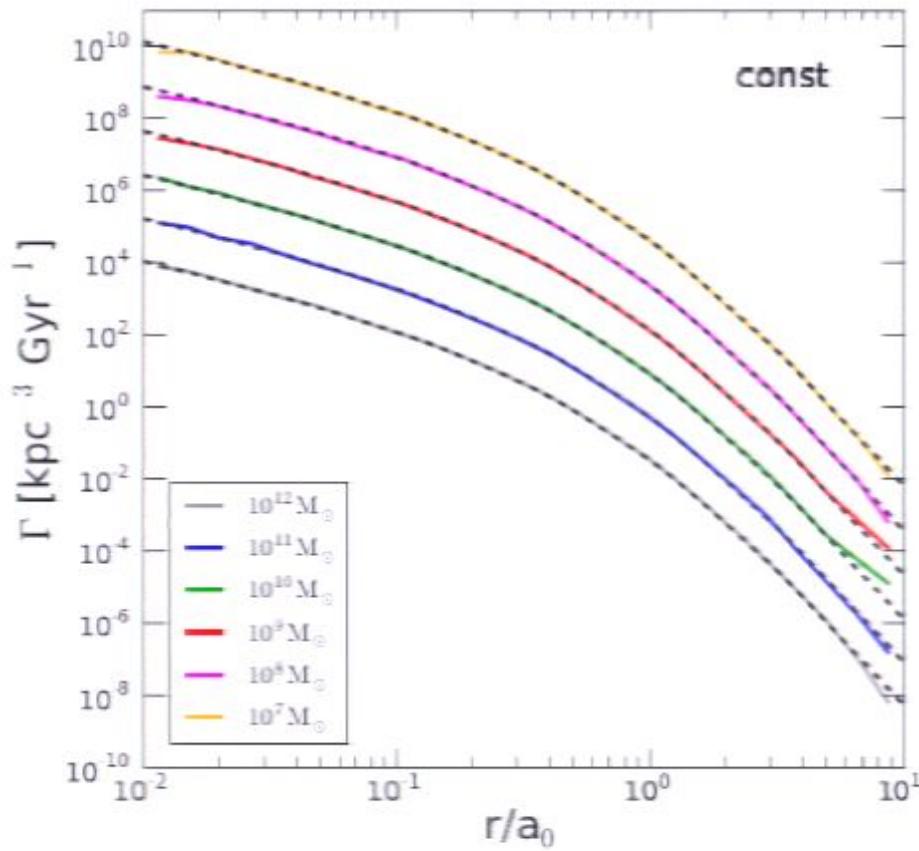
Liouville Theorem:  
→ streams contribute a lot  
→ caustics negligible



in a Sommerfeld-enhanced scenario the fine-grained structure dominates the smooth annihilation signal

red: smooth halo  
blue: streams

# Outlook: Non-Standard N-body



N-body simulations of SIDM, e.g.  $\frac{\sigma_T}{\sigma_{\max}} \approx$

$$\begin{cases} \frac{4\pi}{22.7} \beta^2 \ln(1 + \beta^{-1}) & , \beta < 0.2 \\ \frac{8\pi}{22.7} \beta^2 (1 + 1.5\beta^{1.65})^{-1} & , 0.2 < \beta < 10^3 \\ \frac{\pi}{22.7} (\ln \beta + 1 - \frac{1}{2} \ln^{-1} \beta)^2 & , \beta > 10^3 \end{cases}$$

# Implications

- local DM distribution very grainy [wrong] [<5% deviation from smooth]
- massive streams near the Sun [wrong] [at most 1%]
- discrete velocity distribution [wrong] [smooth distribution]
- Maxwellian/Gaussian velocity distribution [wrong] [~10% deviations]
- Sun might be close to a subhalo [wrong] [chances below ~0.01%]
- ~100 streams near the Sun [wrong] [a lot more due to faster mixing]
- dense caustic structures [wrong] [caustics subdominant in inner halo]
- simulations miss much caustic annihilation [wrong] [<10% even in outskirts]