

Title: Physics in Nature Presentation: Surface Tension in Nature

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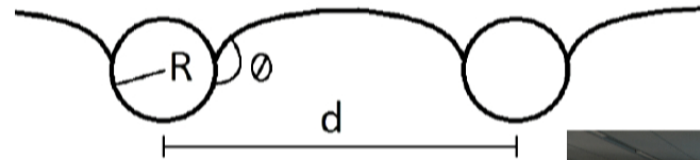
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Abstract:

Surface Tension in Nature



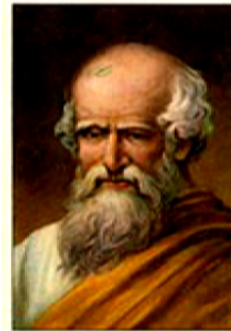
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PSI Presentations
August 19 2011



What is surface tension?

- Archimedes' principle fails to explain why some small objects more dense than water can float.

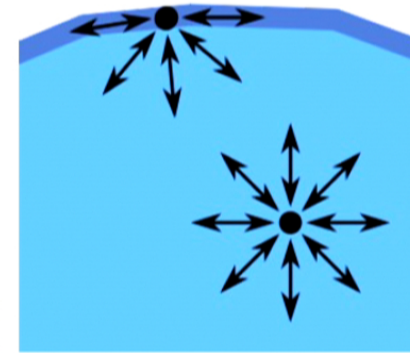
?



(Buoyant force) = (Weight of displaced fluid)
< (Weight of object)

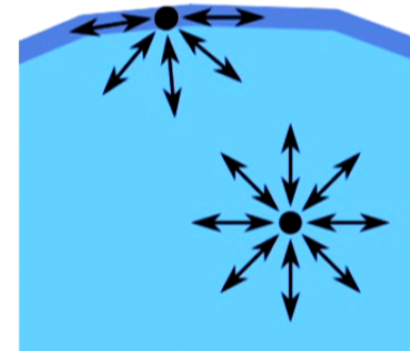
What is surface tension?

- Intermolecular attractive forces, such as Hydrogen bonding in the case of water, cause the molecules on the surface to be attracted into the fluid.
- This causes the fluid to stay together, and retain a smooth boundary.
- Surface tension can also be interpreted in terms of minimizing surface energy.



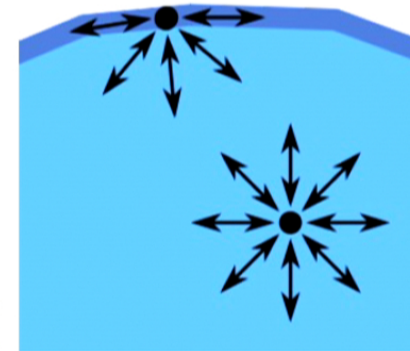
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Surface tensions of common liquids

- Surface tension has dimensions
(Force)/(Length) = (Energy)/(Length²)



Water
~0.07 N/m



Mercury
~0.5 N/m

Water Striders

- More dense than water
- Float due to surface tension acting on long legs



- Weight $\sim \rho g(\text{Length})^3$
- Surface tension forces $\sim \sigma(\text{Length})$
- Need L smaller than $\sim \sqrt{(\sigma/\rho g)}$

Propulsion

- Some beetle larvae bend, creating a difference in the front and rear horizontal components of surface tension.
- Small boats with no moving parts can emit electrical pulses to alter the surface tension
- Applying soap to one end of a floating object will propel it in the opposite direction



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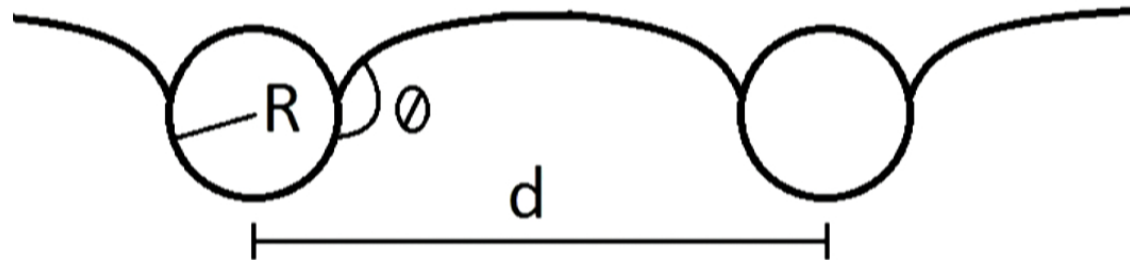
Capillary Attraction



“Cheerios Effect” - Similar objects floating on a fluid tend to be attracted to each other.



Capillary Attraction



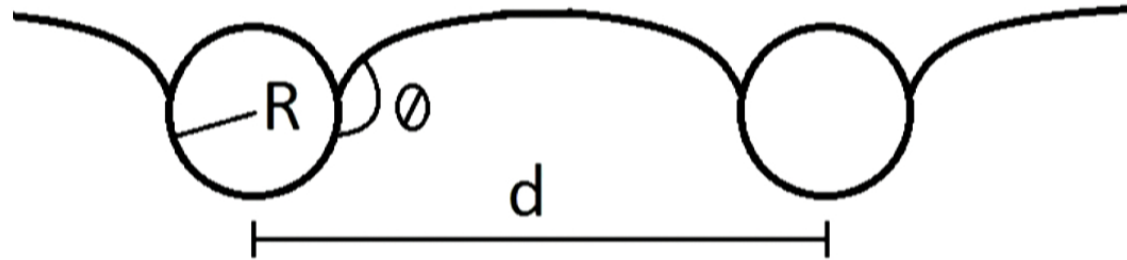
For two identical spheres, the attractive force is roughly

$$F_c = \beta e^{-d/L_c}$$

$$L_c = \sqrt{\frac{\sigma}{\rho_f g}}$$



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Young-Laplace Equation

The shape of the fluid-gas interface is described by the Young-Laplace equation

$$\Delta p = 2\sigma H = \sigma \left(\frac{1}{R_1} + \frac{1}{R_2} \right) = -\sigma \nabla \cdot \hat{n}$$

It can be derived by balancing the pressure and surface tension forces in a small region, where gravity is negligible.



Young-Laplace Equation

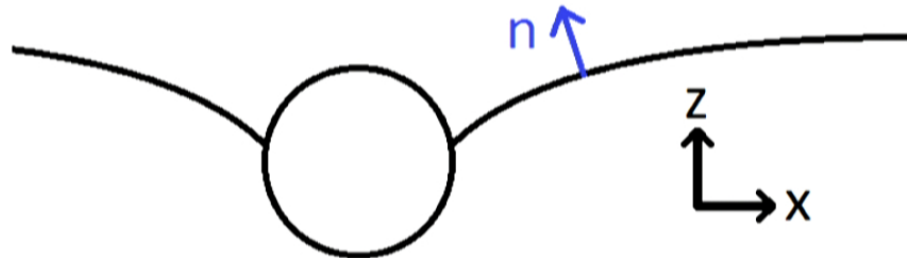
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Young-Laplace Equation



In a simple two dimensional system we can write $z = f(x)$.

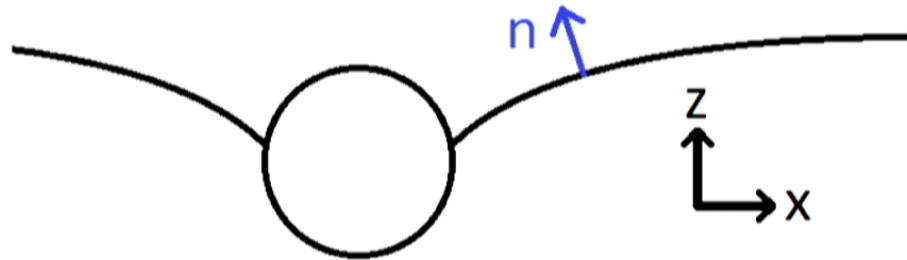
We then have

$$\nabla \cdot \hat{n} = \frac{\ddot{f}}{(1 + (\dot{f})^2)^{3/2}} \approx \ddot{f}$$

for small slopes.



Young-Laplace Equation

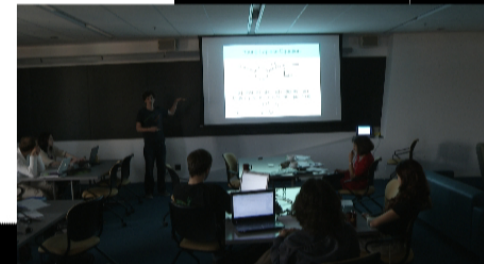


The pressure of the fluid under the force of gravity is $p_0 + \rho g z$, so the equation is

$$\rho g f = \sigma \ddot{f}$$

so

$$z \approx z_0 e^{-x/L_c}$$



Summary

- Surface tension is caused by attractive intermolecular forces, and the minimization of the surface energy.
- It allows dense objects to float, provided that they are sufficiently small.
- It also gives rise to a force between floating objects.
- Surface tension effects typically decay exponentially with distance

