Title: Creating Spacetime

Date: Jul 19, 2011 04:50 PM

URL: http://pirsa.org/11070060

Abstract: Our understanding of the physical world at the most fundamental level is based on two theories: quantum theory and general relativity. They are impressively successful but only when each is considered on its own. In situations where both play a role, we are reduced to puzzles and absurdity. Hence the search for a quantum theory of gravity, the currently missing theory that will work sensibly in exactly these situations. To the great frustration of researchers in this field, candidate quantum theories of gravity tend to produce more puzzles instead of answers. We shall take a tour of some of the problems, focusing on the role of spacetime and causality. We will consider the possibility that spacetime did not always exist but is instead emergent and explore how one can create a spacetime from a world with no notion of " here" and " there"

Pirsa: 11070060 Page 1/67

Creating Spacetime: Spin Systems as Toy Models for Emergent Gravity

Fotini Markopoulou Perimeter Institute / U.Waterloo / Albert Einstein Institute

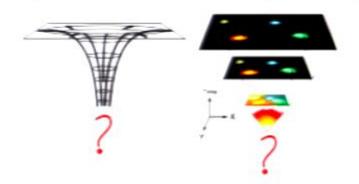
T. Konopka, FM & S. Severini
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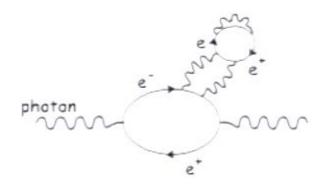
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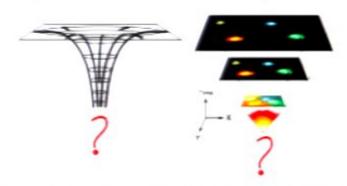
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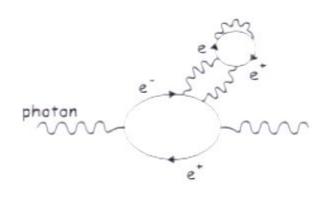
General Relativity and Quantum Field Theory ultimately fail.





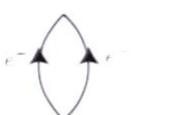
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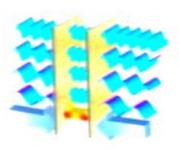


More bad things happen if we combine the two theories.

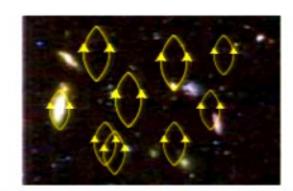
$$\Delta E \Delta t > h$$





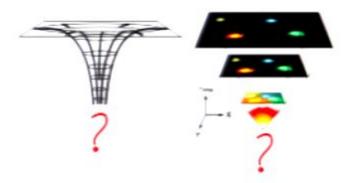


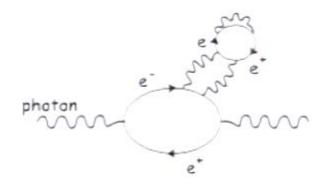




Quantum gravity seeks to reconcile general relativity and quantum theory

General Relativity and Quantum Field Theory ultimately fail.





More bad things happen if we combine the two theories.

Background Independence

 Matter tells spacetime how to curve and spacetime tells matter where to go



$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R + g_{\mu\nu}\Lambda = T_{\mu\nu}$$

- gur dynamical
- Physical quantity: $g_{\mu\nu}$ Diff.M

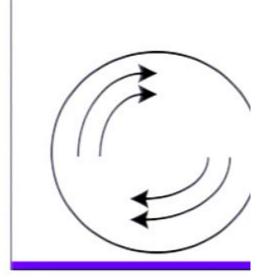
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The problem of time in quantum gravity

 Matter tells spacetime how to curve and spacetime tells matter where to go

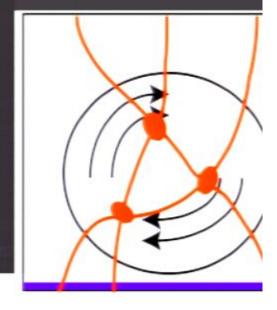


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Only events and their causal relations are physical; the metric is dynamical=

Background Independence



Background Independence

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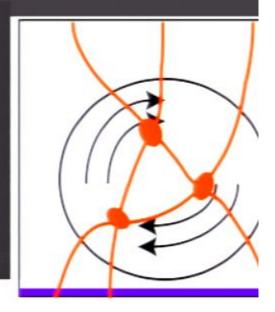


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- g_{µν} dynamical
- Physical quantity: |g_{μν | Diff, M}

Only events and their causal relations are physical; the metric is dynamical= Background

Independence



- In pure gravity ($T_{\mu\nu}=0$), time evolution is a diffeomorphism (timelessness).
 - If we quantize GR we find that the Hamiltonian is a constraint:

$$\hat{H}|\Psi_{\mathrm{U}}\rangle=0$$

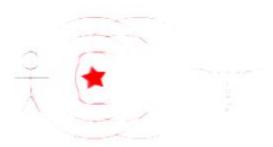
Wheeler-deWitt equation instead of a Schroedinger equation. What does the RHS mean?

What is an observable?

The problem of time in quantum gravity

Scale of quantum gravity: Planck length
$$l_{\rm Pl} = \sqrt{\frac{G\hbar}{c^4}} = 10^{-35} m$$

- · at this scale the quantum effects of the gravitational field become important
- · at this scale we reach fundamental limits to space and time measurements



Spacetime metric ← causal structure is dynamical

The Planck scale is not beyond reach

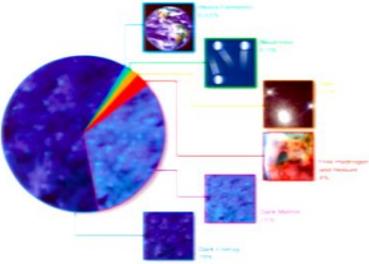
The need for new physics is not restricted to $l_{\rm Planck}$:

- · Constraints on Lorentz invariance violation
- · Dark energy and dark matter
- The inflation (transplanckian signatures in inflation)
- · The coincidence problem
- · Quantum to classical transition in macroscopic systems

• ...

After all, we only know 5% of the universe!

COMPOSITION OF THE COSMOS



We need a quantum theory of gravity

BE SIMPLE AND ELEGANT BE MATHEMATICALLY RIGOROUS TELL US IF THE UNIVERSE IS FINITE OR INFINITE DESCRIBE THE ENTIRE UNIVERSE DESCRIBE THE INTERIOR OF A BLACK HOLE BE A UNIFIED THEORY OF EVERYTHING EXPLAIN OBSERVATIONAL COSMOLOGY DATA EXPLAIN DARK ENERGY AND DARK MATTER EXPLAIN THE NATURE OF TIME EXPLAIN QUANTUM THEORY GO BEYOND GENERAL RELATIVITY

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Background independence: principle in quantum gravity

Background Independence I:

There should be no preferred geometry in the formulation of the quantum theory of gravity.

Quantum gravity is given by a quantum superposition of quantum geometries.



The science of quantum spacetimes

Spacetime = physical events
Physical events are Quantum
Quantum = superpositions
Superpositions of spacetimes?



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To make sense of a quantum superposition of spacetimes, we must show that it is possible to start from such a superposition and find a nice regular spacetime (our world) as the most likely one.

The science of quantum spacetimes

Spacetime = physical events
Physical events are Quantum
Quantum = superpositions
Superpositions of spacetimes?

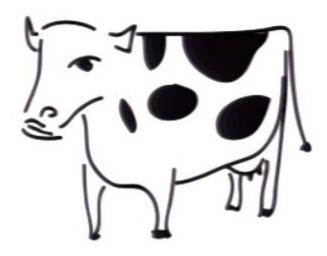


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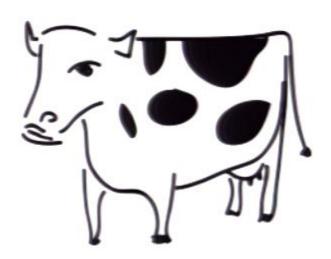
First we need some tools...

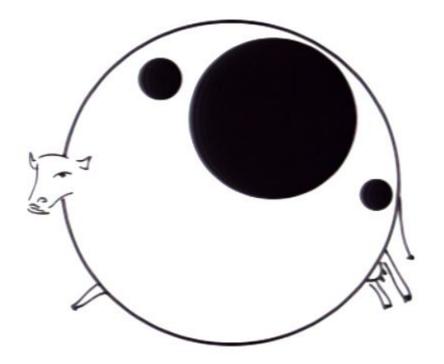
What does it mean to be a model?

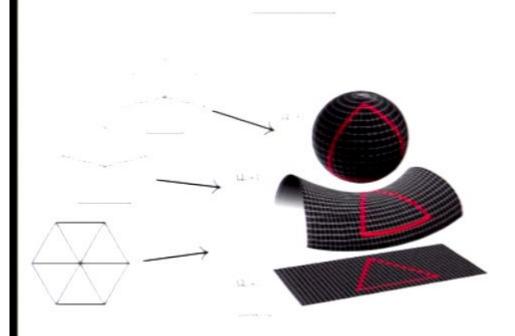
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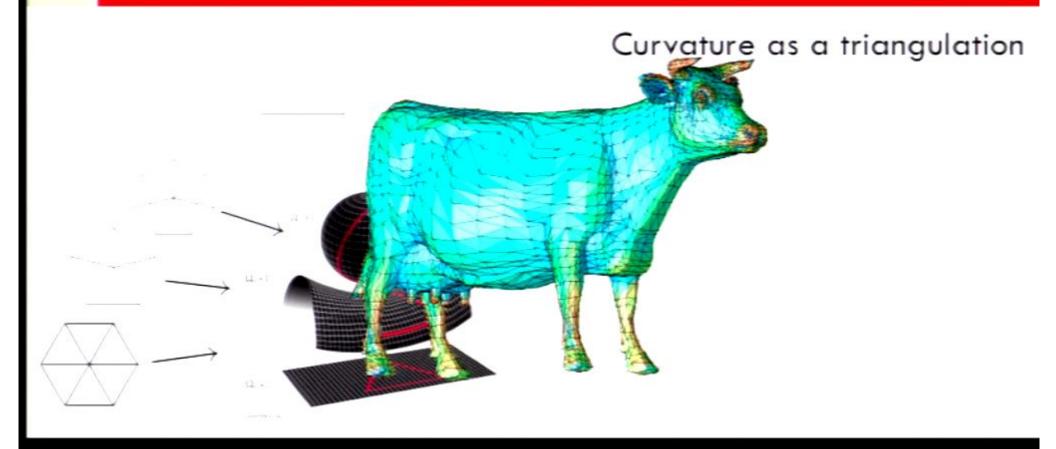


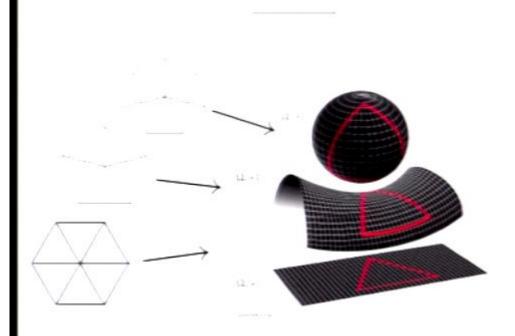
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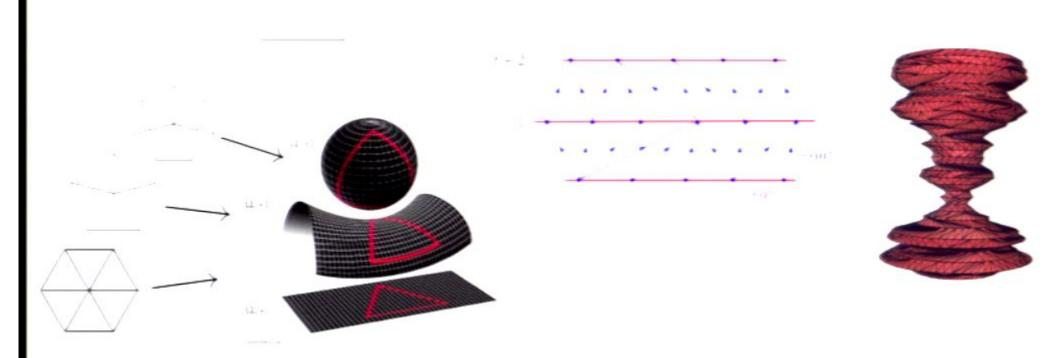




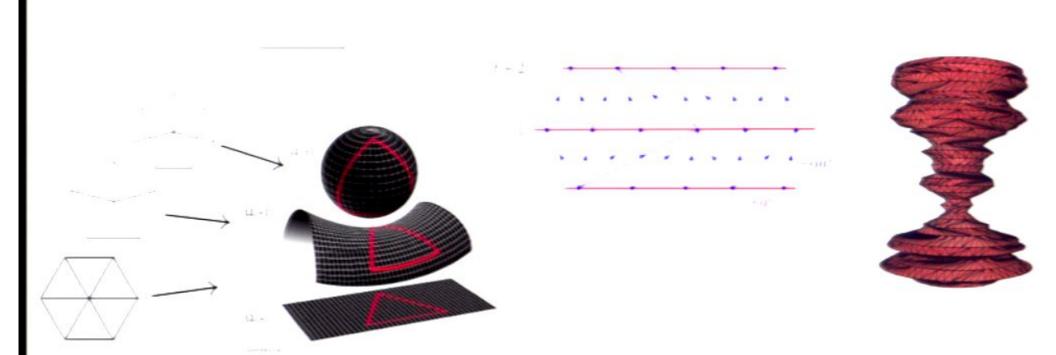








Triangulation reduce the problem to combinatoric Count!

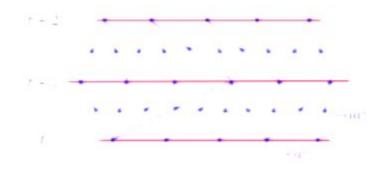


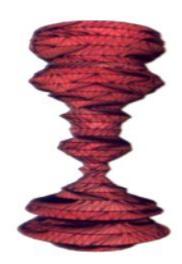
Causal Dynamical Triangulations:

A statistical model of quantum geometries.

$$A\left(L(in),L(out),1\right) = \frac{g^2L_1L_2}{(1-L_1)(1-gL_1-gL_2)}$$

$$A_{L(\imath n) \rightarrow L(out)} = \sum_{t=0}^{\infty} A\left(L(\imath n), L(out), t\right)$$





Causality condition: advance everyone at every step.

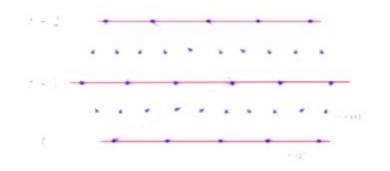


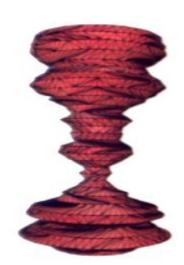
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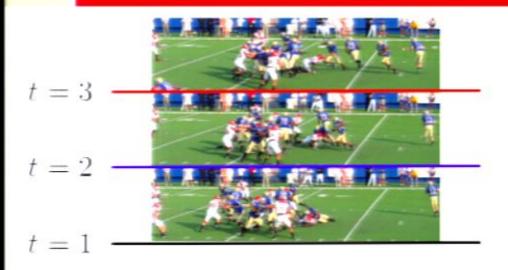
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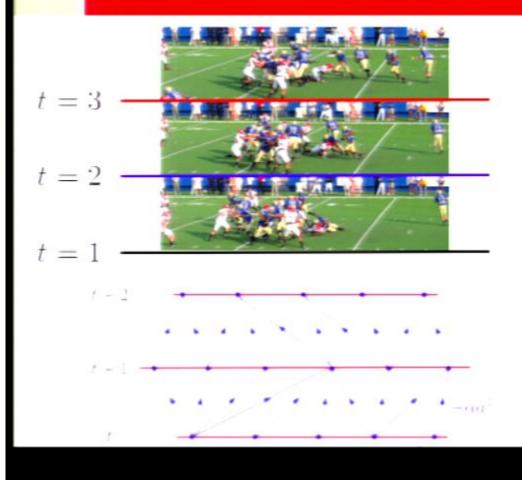
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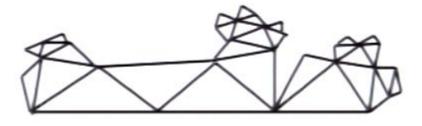
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Time in general relativity:





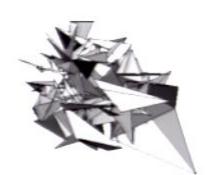




Most likely spacetime:



 $d_H \sim \infty$



 $\sim \infty$ $d_H \sim 2$

Dimension: $d_H = 3.10 \pm 0.15$

J. Ambjorn, R. Loll et al

Are we most likely?

Yes, if by "we" we mean 3+1 dimensions and smoothly varying in time.

Requires a notion of time which may disagree with General Relativity.

- √ Convergent, tractable
- √ Well-behaved typical histories
- √ Also when matter is added
- √ Correct dimension
- √ High-energy prediction: evidence for 2d
- √ New universality class discovered.



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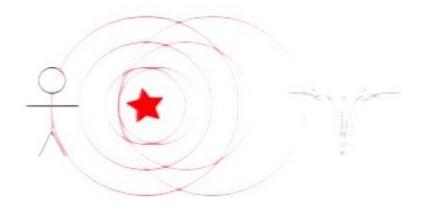
Requires a notion of time which may disagree with General Relativity.

Is this the answer to the problem of Quantum Gravity?

We need more than smooth geometry and the correct dimension.

Verdict: Need to show that apples fall in quantum spacetimes

Back to start: does this make sense?



Maybe wrong

Background independence: principle in quantum gravity

Revisit Background Independence

Background Independence

There should be no preferred geometry in the formulation of the quantum theory of gravity

Quantum gray by is given by a quantum suberbosition of quantum geometries

Background Independence II:

There are no geometric or gravitational degrees of freedom in the fundamental theory.

Geometry is only a classical, emergent concept.

Emergent space(time)

Emergence: the behavior of the system has no explanation in terms of its constituent particles, but instead of their collective behavior and interactions.

The whole is more than its parts.



River or water molecules?

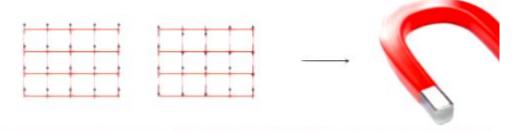
Would you say the river fundamentally exists?

Emergent space(time)

Emergence: the behavior of the system has no explanation in terms of its constituent particles, but instead of their collective behavior and interactions.

The whole is more than its parts.

The paradigm: the Ising mode



What is the Ising model for gravit

Emergent space: emergent locality and order

What is space(time)?

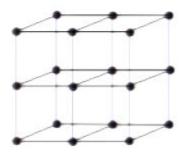


here

Space=locality

What is space(time)?





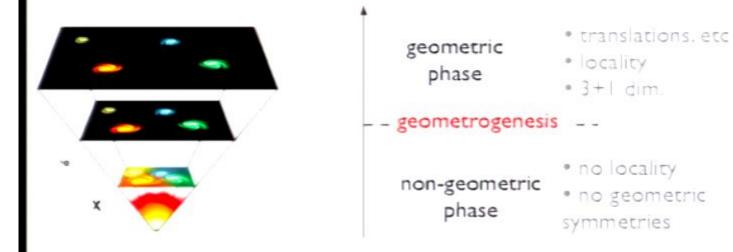
Space=order

translation invariance

Emergent space(time)

We currently assume an FRW geometry all the way to the Big Bang.

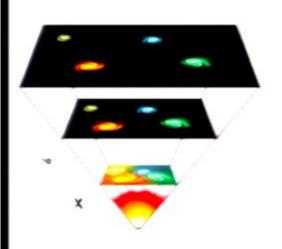
Alternative scenario: What if geometry is not fundamental?



Emergent space(time)

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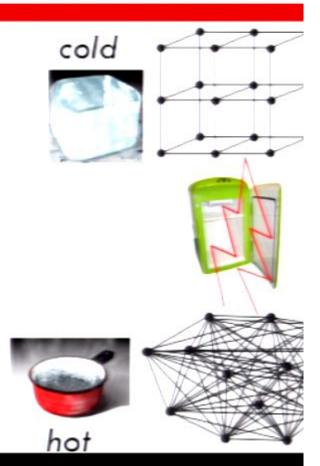
geometric
phase

- geometrogenesis

non-geometric
phase

- translations, etc
locality
3+1 dim.

- no locality
no geometric
symmetries



The dynamical lattice: lattice links as spins

Konopka, FM & L.Smolin, hep-th/061

Basic idea:



Promote link to a quantum degree of freedom { 1). (1) qubits of adjacency

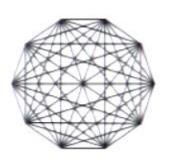
In a universe of N constituents, there are $\frac{N(N-1)}{2}$ possible links.

quantum geometry: superposition of adjacent/not adjacent

State space of models:

$$\mathcal{H} = \bigotimes \mathcal{H}$$

Model 1: Emergent space and matter







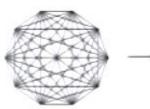
- no locality
- no geometric symmetries

- · translations, etc.
- locality
- 3+1 dim.

Model 1: Emergent space and matter

T. Konopka, FM & S. Severini, PF

•
$$H_{\mathcal{N}} = q_{\mathcal{K}} \sum_{i} e^{p_{\mathcal{K}} H_{i} t} = \sum_{i} N_{i,i-1}^{i}$$







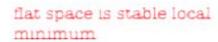
• on H 1.0

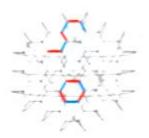
$$H_{\text{targe}} = \sum_{i} \left(-\sum_{i} j_{i} + \sum_{k=i}^{\infty} \frac{-j}{f_{i}!} N_{2\delta}^{i,k} \right)$$

• on full H

$$\begin{split} H_{\text{become}} &= -\sum_{i} \sum_{l=20}^{\infty} \frac{s^{il}}{L^{i}} g_B \prod_{i=1}^{l} M_i^2 \\ H_{\text{storing}} &= g_i \sum_{l} \left(\sum_{i} M_{ib} \right)^2 + g_D \sum_{i0} M_{i0}^2 \end{split}$$







emergent photons and fermions for

$$g_B \gg g_C \cdot g_D$$

X.G.Wen. Quantum Field Theory of Many Body

Speed of light from local interactions A.Hamma, FM, I. Premont-Schwarz, S. Severini, PRL 2

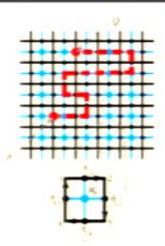
Given local Hamiltonian
$$H = \sum_{i,j} h_{i,j}$$
.

Lieb-Robinson speed of information propagation:

$$\begin{split} &[O_P(t),O_Q(0)]\| \leq 2\|O_P\| \|O_Q\| \sum \frac{|2|t|h_{max})^n}{n!} N_{PQ}(n) \\ &[O_P(t),O_Q(0)]\| \leq 2\|O_P\| \|O_Q\| C\| \exp[-a(d_{PQ}-\mathbf{r}t)] \end{split}$$

Find:
$$r_{LR} = \sqrt{2g_Bg_C}$$

- $v_{LR} = \epsilon$ in the emergent Maxwell equations
- . Effective finite light cones consistent with non-relativistic quantum mechanics
- v_{IR} ~ d



Speed of light from local interactions A.Hamma, FM, I. Premont-Schwarz, S. Severini, PRL 2

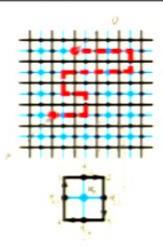
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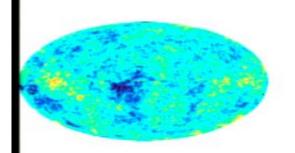


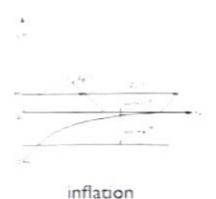
Does an emergent observer Minkowski space?

Emergent locality is NOT a Planck scale effect

A. Hamma, FM, I. Premont-Schwarz, S. Severini, PRL 2

Evolving speed of light and the horizon problem:

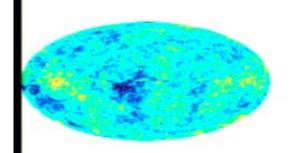


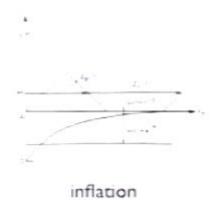


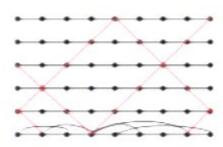
Emergent locality is NOT a Planck scale effect

A.Hamma, FM, I. Premont-Schwarz, S. Severini, PRL 2

Evolving speed of light and the horizon problem:







Model illustrates the effect of a transition in the local structure: in principle an observable effect (not a Planck scale effect).

Note: a phase transition in the speed of light can also reproduce the scale invariant CMB spectrum (Variable Speed of Light cosmology)

Model 2: Interacting matter-geometry

Gravity



geometry tells matter where to go and matter tells geometry how to curve.

Model 2: Interacting matter-geometry





geometry tells matter where to go and matter tells geometry how to curve.



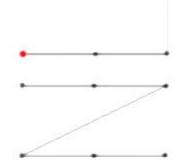
$$\mathcal{H} = \bigotimes_{r} \mathcal{H}_{r} \bigotimes_{r} \mathcal{H}_{r}$$



$$H_{\rm ex} = \sum_{ij} |P_{ij}^L(-|0\rangle\langle 1_{ij}|b_i^\dagger b_j^\dagger| - |1\rangle\langle 0|_{ij}|b_i b_j|)$$



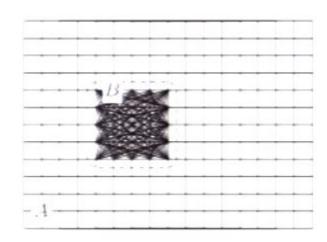
$$P_{ij} = |1\rangle\langle 1|_{ij}$$





The matter gives the graph the meaning of space:

Adjacency is defined by interactions. The graph determines where the matte allowed to go.

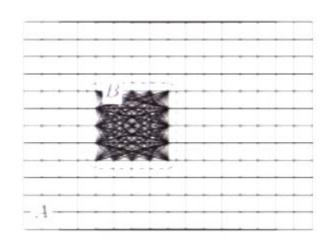


$$e^A \propto 1$$

$$e^B \propto N^B$$

$$\theta_{c} = \sin^{-1} \frac{c^{B}}{c^{A}} \sim \sin^{-1} N^{B}$$

Probability of light escaping $\sim \frac{1}{N^B} \rightarrow 0$



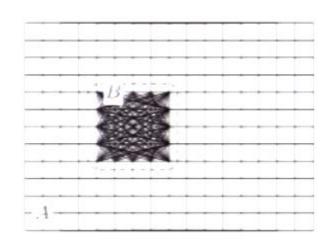
$$e^A \propto 4$$

$$e^B \propto N^B$$

$$\theta_c = \sin^{-1} \frac{c^B}{c^A} \sim \sin^{-1} N^B$$

Probability of light escaping $\sim \frac{1}{N^B} \rightarrow 0$

- The dense geometry creates more bosons and the bosons make more links (cf gravitational collapse)
- . Eventually the "black hole" evaporates (faster as it gets smaller)
- . Unitary evolution, mixed radiation (no singularity): matter entangled with remnant geometry



$$e^4 \times 1$$

$$e^B \propto N^B$$

$$\theta_c = \sin^{-1} \frac{c^B}{c^A} \sim \sin^{-1} N^B$$

Probability of light escaping
$$\sim \frac{1}{N^B} \rightarrow 0$$

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Can make all this very precise: particles obeying this Hamiltonian see an effective curved geometry. Construct experimental realizations of such models in the lab? (Analogue models of gravity).



Background Independence: a guiding principle in quantum gravity, but how?

Background Independence I:

There should be no preferred geometry in the formulation of the quantum theory of gravity. Quantum gravity is given by a quantum superposition of quantum geometries.

$$A_{L(\imath n) \rightarrow L(out)} = \sum_{t=0}^{\infty} A(L(\imath n), L(out), t)$$

Background Independence II:

There are no geometric or gravitational degrees of freedom in the fundamental theory.

Geometry is only a classical, emergent concept.

From quantum to gravity?

Underlying spatial geometry is the notion of adjacency.



metric: neighbours or not?



E.g. a 3d euclidean geometry is a particular *order* of adjacencies that exhibits certain symmetries. Our geometric world is a *phase* (geometrogenesis), we froze to that phase.

- By promoting adjacency to a qubit and considering any network as a subgraph of K we have a convenient way to deal with superposition of quantum geometries.
- When the adjacency qubits are dynamical dofs, we have an important ingredient of GR (dynamical geometry).
- Local interactions mean a finite speed of information propagation. Given local dynamics on a network of adjacencies, we can define a spacetime with finite lightcone structure. (Is it also universal?)
- . If we find microscopic dynamics that simulate GR, we will have reconciled quantum with gravity.
- · With emergent gravity, we need to explain, not quantize the Einstein Equations!

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Analogue models of gravity (simulating gravity):

If it looks like a duck, walks like a duck and quacks like a duck, can we call it a duck?

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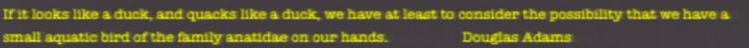
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Analogue models of gravity (simulating gravity):

small aquatic bird of the family anatidae on our hands.

If it looks like a duck, walks like a duck and quacks like a duck, can we call it a duck?

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Space does not exist

We only know 5% of our world. It will take a miracle to explain the other 95% without major change.

My bet: the major change is that space is not fundamental.

Can make models of emergent space and test them.

- Caution: Must not raise more problems that we solve!
- Good news: More observational data on the way, and we have models to test.

What is space(time)?



Are we most likely? It depends on time

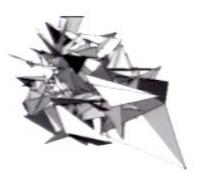




Most likely spacetime:







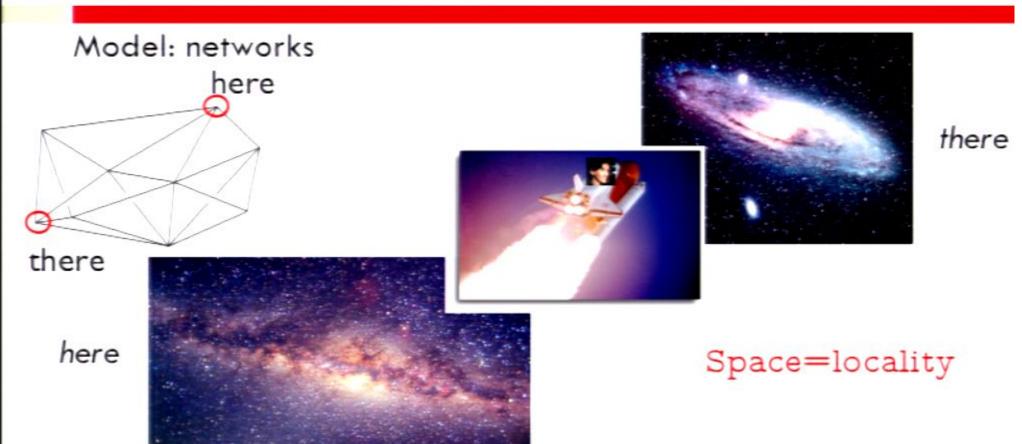
Dimension: $d_H = 3.10 \pm 0.15$

 $d_H \sim \infty$

 $d_H \sim 2$

J. Ambjorn, R. Loll et al

What is space(time)?



The dynamical lattice: lattice links as spins

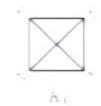
TKonopka, FM & L.Smolin, hep-th/061

Basic idea:



Promote link to a quantum degree of freedom { 1). (1) } qubits of adjacency

In a universe of N constituents, there are $\frac{N(N-1)}{2}$ possible links.

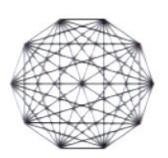


quantum geometry: superposition of adjacent/not adjacent

State space of models:

$$\mathcal{H} = \bigotimes \mathcal{H}$$

Model 1: Emergent space and matter







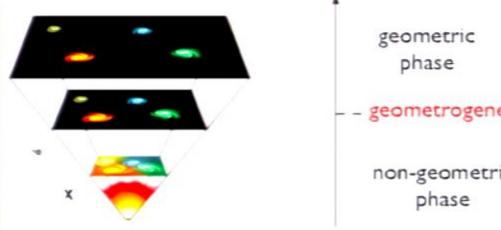
- no locality
- no geometric symmetries

- · translations, etc.
- locality
- 3+1 dim.

Emergent space(time)

We currently assume an FRW geometry all the way to the Big Bang.

Alternative scenario: What if geometry is not fundamental?



geometric
phase

- geometrogenesis

non-geometric
phase

* translations. etc
| locality
| 3+1 dim.

-
no locality
| no geometric
| symmetries

Background independence: principle in quantum gravity

Revisit Background Independence

Background Independence

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