

Title: Neutrino oscillations and the CCSN mechanism

Date: Jun 21, 2011 03:20 PM

URL: <http://pirsa.org/11060024>

Abstract:

Question: How can we revive the core-collapse supernova shock?

Answer: ??

1. Increased dimensionality (Nordhaus et al. 2010) may be enough to get robust explosion.
2. May be missing some crucial microphysics which could naturally increase the heating rate?

Question: How can we revive the core-collapse supernova shock?

Answer: ??

1. Increased dimensionality (Nordhaus et al. 2010) may be enough to get robust explosion.
2. May be missing some crucial microphysics which could naturally increase the heating rate?

Question: How can we revive the core-collapse supernova shock?

Answer: ??

1. Increased dimensionality (Nordhaus et al. 2010) may be enough to get robust explosion.
2. May be missing some crucial microphysics which could naturally increase the heating rate?

Outline:

- Formalism neutrino oscillations
- Neutrino heating in the postshock region
- Influence of collective neutrino oscillations on shock revival + prospects of this mechanism

Neutrino Oscillations

$$|\nu_{\text{mass}}\rangle = U_M |\nu_{\text{flavour}}\rangle$$

$$U_M = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

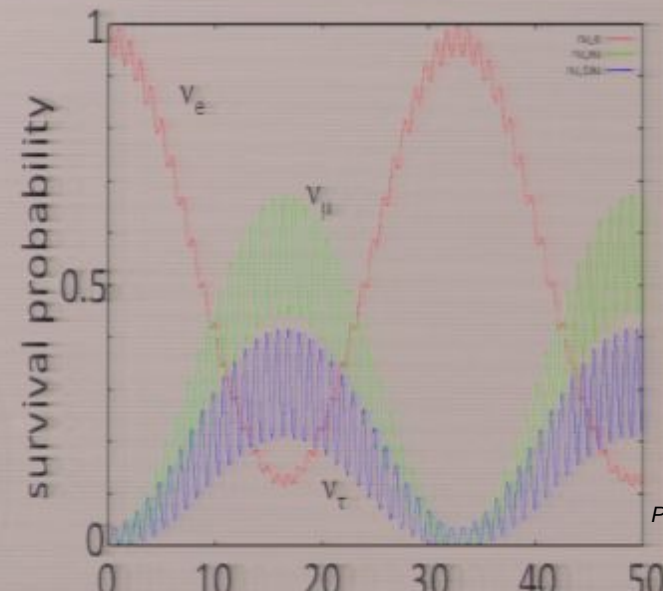
$$|\nu_{\text{mass}}(t)\rangle = e^{-i\mathcal{H}t} |\nu_{\text{mass}}\rangle$$

$$|\nu_{\text{flavour}}(t)\rangle = U_M^{-1} |\nu_{\text{mass}}(t)\rangle$$

- Vacuum Oscillations

$$\begin{pmatrix} |\nu_1(t)\rangle \\ |\nu_2(t)\rangle \\ |\nu_3(t)\rangle \end{pmatrix} =$$

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{-i\Delta m_{21}^2 t/2E} & 0 \\ 0 & 0 & e^{-i\Delta m_{31}^2 t/2E} \end{pmatrix} \begin{pmatrix} |\nu_1(0)\rangle \\ |\nu_2(0)\rangle \\ |\nu_3(0)\rangle \end{pmatrix}$$



Neutrino Oscillations

- *Matter Oscillations*

Matter introduces extra potential in Hamiltonian due to forward scattering of electrons and neutrinos, the MSW potential:

$$\mathcal{H}_{\text{matter}} = \sqrt{2}G_F(N_{e^-} - N_{e^+})$$

- *Collective Oscillations*

High neutrino densities in the core-collapse supernova environment leads to appreciable neutrino-neutrino forward scattering:

$$\mathcal{H}_{\text{collective}} = G_F \frac{R_{\nu_e}^2}{2r^2 - R_{\nu_e}^2} \int \frac{R_{\nu_e}^2}{r^2} [\Phi_{\nu_e} - \Phi_{\bar{\nu}_e}] dE$$



interaction angle closes $\sim 1/r^2$



differential neutrino flux $\sim 1/r^2$

Neutrino Oscillations

- Hamiltonians give equations of motion of the system

$$\mathcal{H}_{\text{vacuum}} = -\frac{|\Delta m_{31}^2|}{2E} \quad \mathcal{H}_{\text{matter}} = \sqrt{2}G_{\text{F}}(N_{e^-} - N_{e^+})$$

$$\mathcal{H}_{\text{collective}} = G_{\text{F}} \frac{R_{\nu_e}^2}{2r^2 - R_{\nu_e}^2} \int \frac{R_{\nu_e}^2}{r^2} [\Phi_{\nu_e} - \Phi_{\bar{\nu}_e}] dE$$

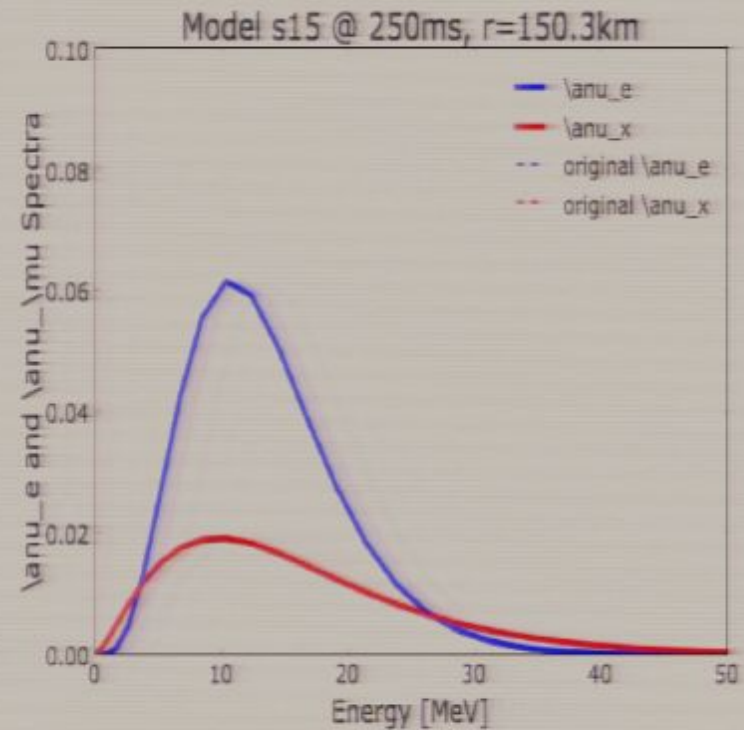
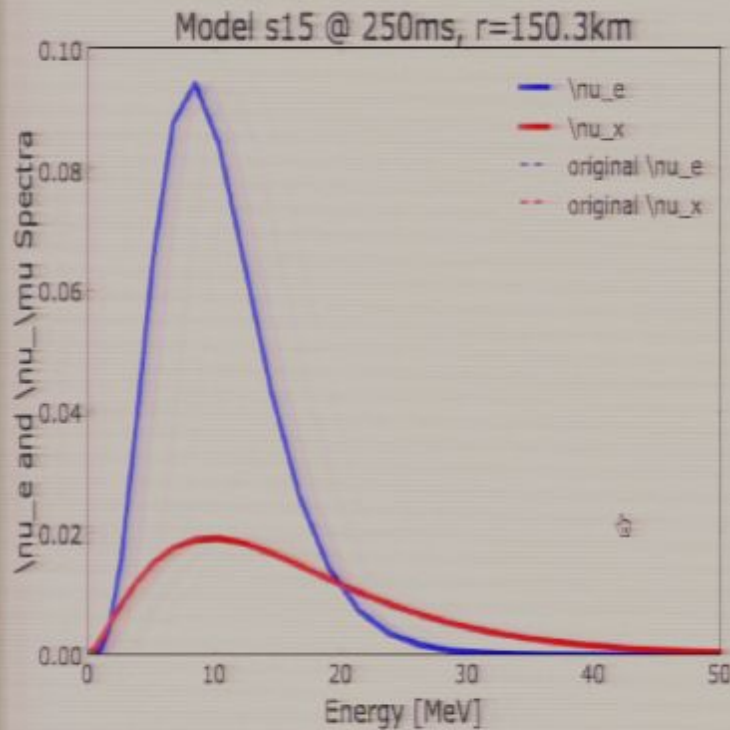
$$\frac{\partial \Phi_{\nu}}{\partial t} = -\frac{i}{\hbar} [+\mathcal{H}_{\text{vacuum}} + \mathcal{H}_{\text{matter}} + \mathcal{H}_{\text{collective}}, \Phi_{\nu}]$$

$$\frac{\partial \Phi_{\bar{\nu}}}{\partial t} = -\frac{i}{\hbar} [-\mathcal{H}_{\text{vacuum}} + \mathcal{H}_{\text{matter}} + \mathcal{H}_{\text{collective}}, \Phi_{\bar{\nu}}]$$

- Evolution is complicated due to non-linear coupling of neutrino and antineutrino fields

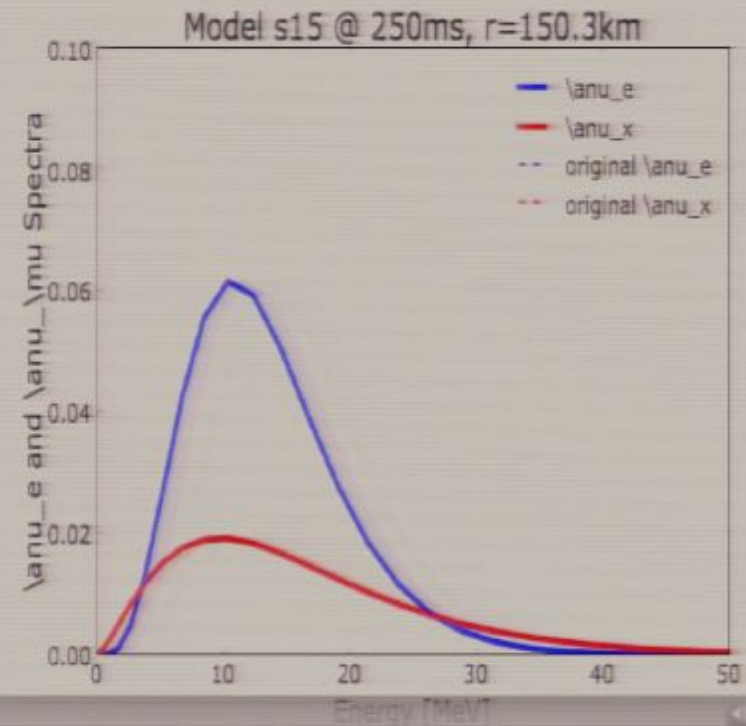
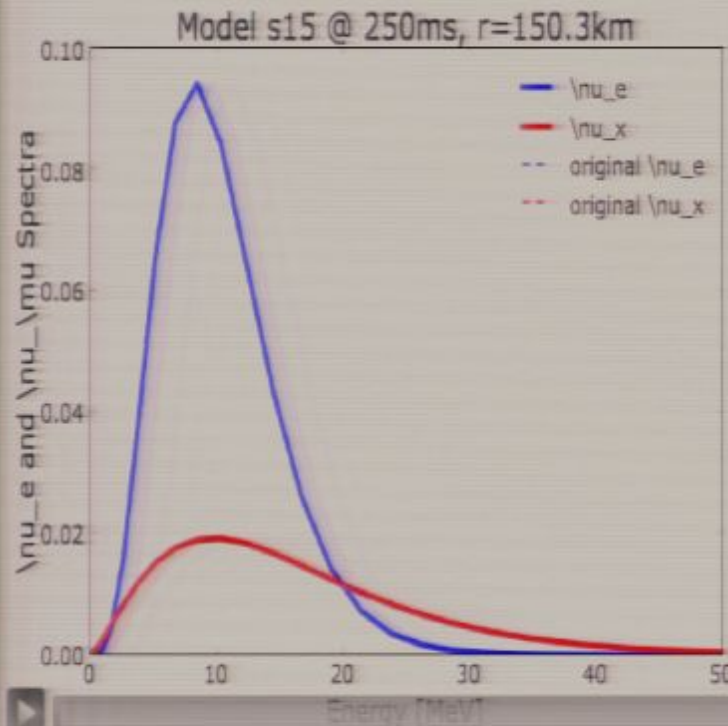
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



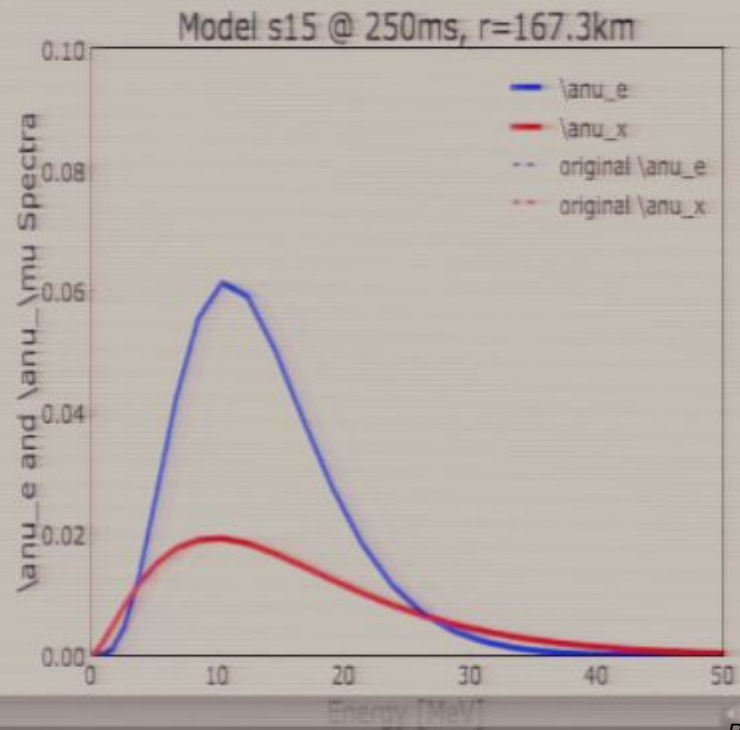
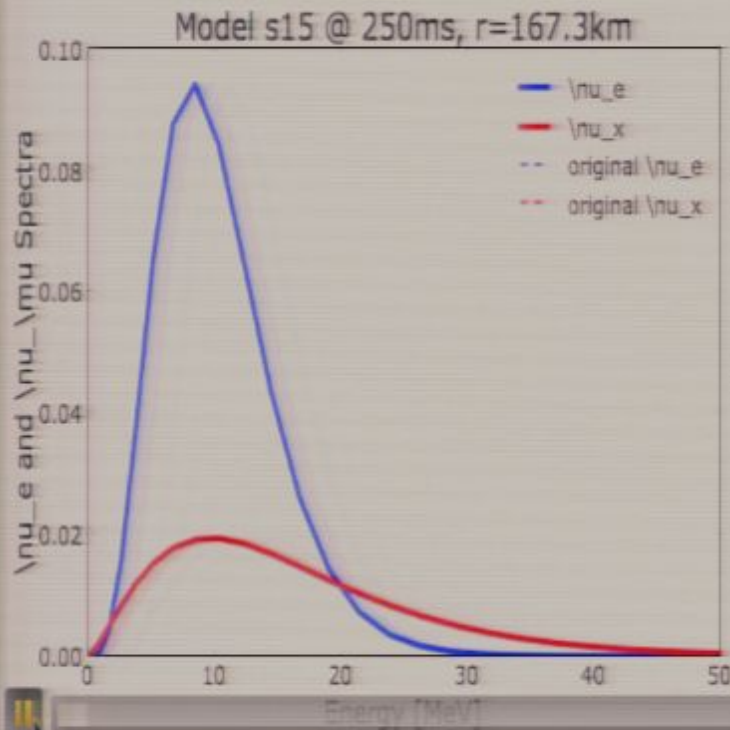
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



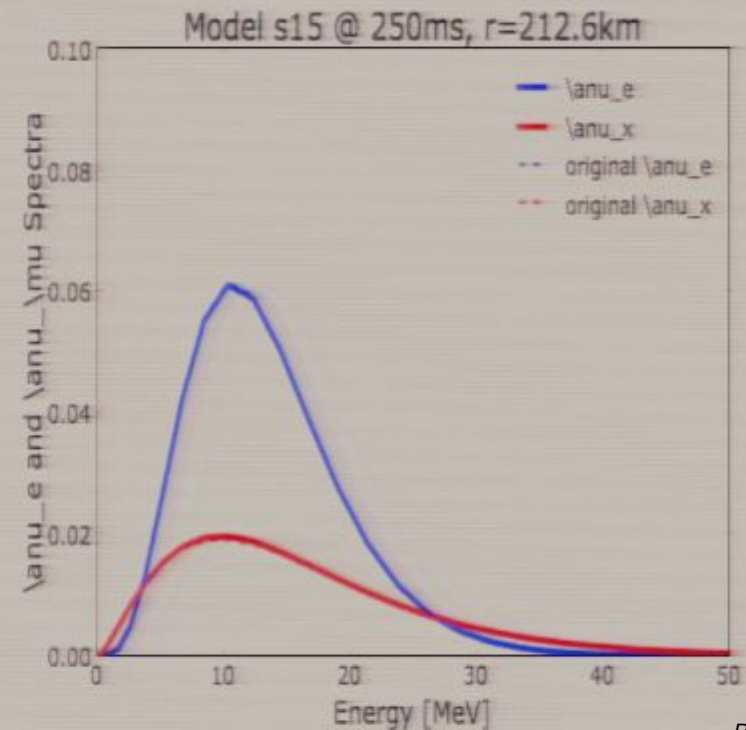
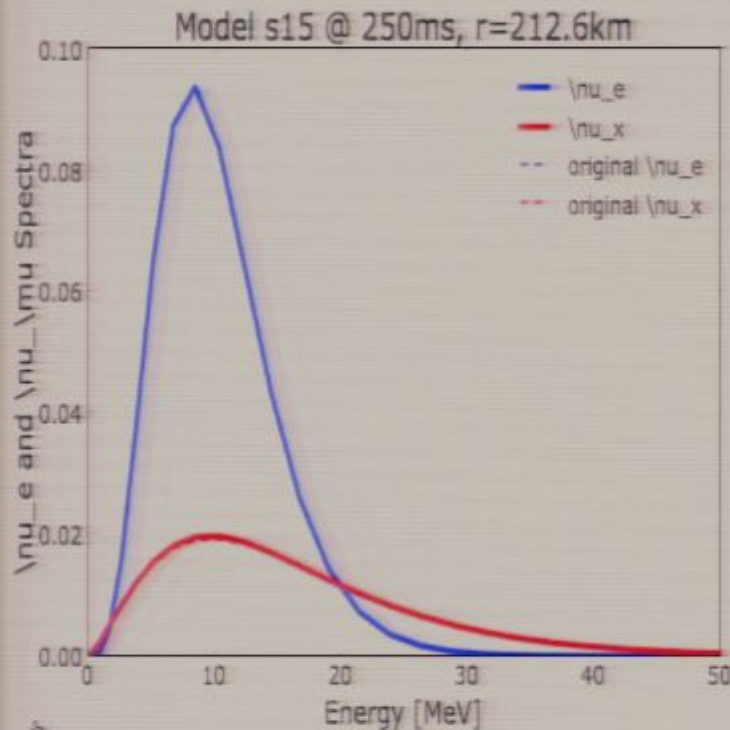
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



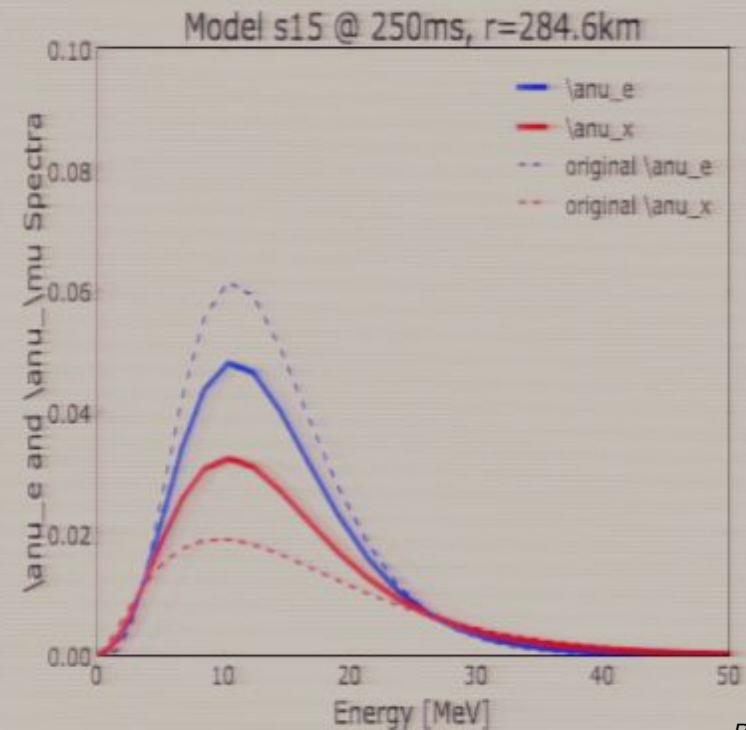
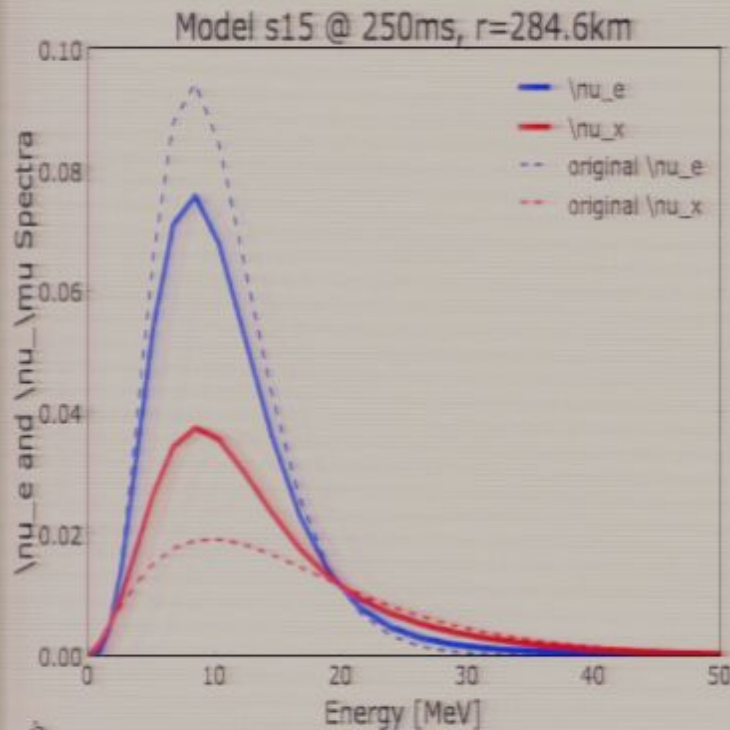
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



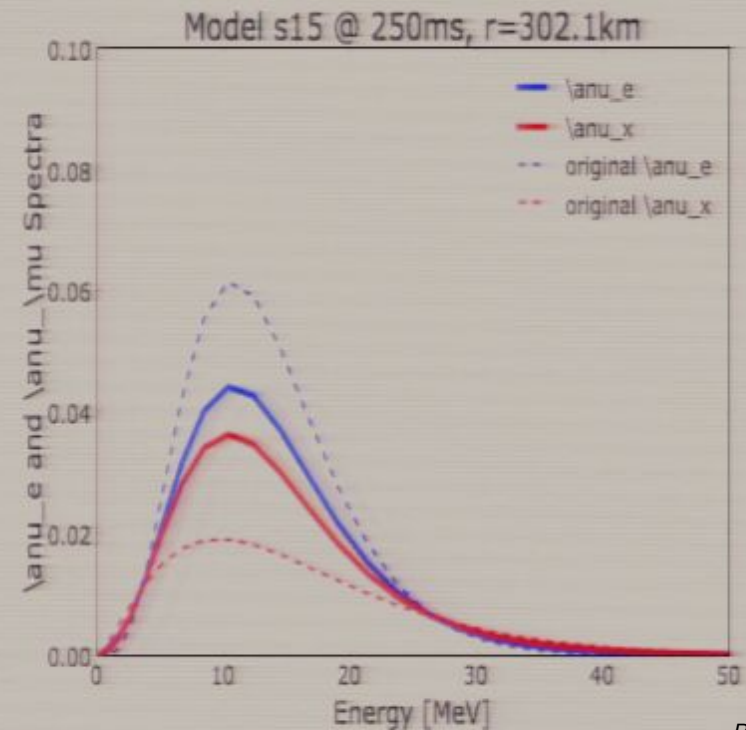
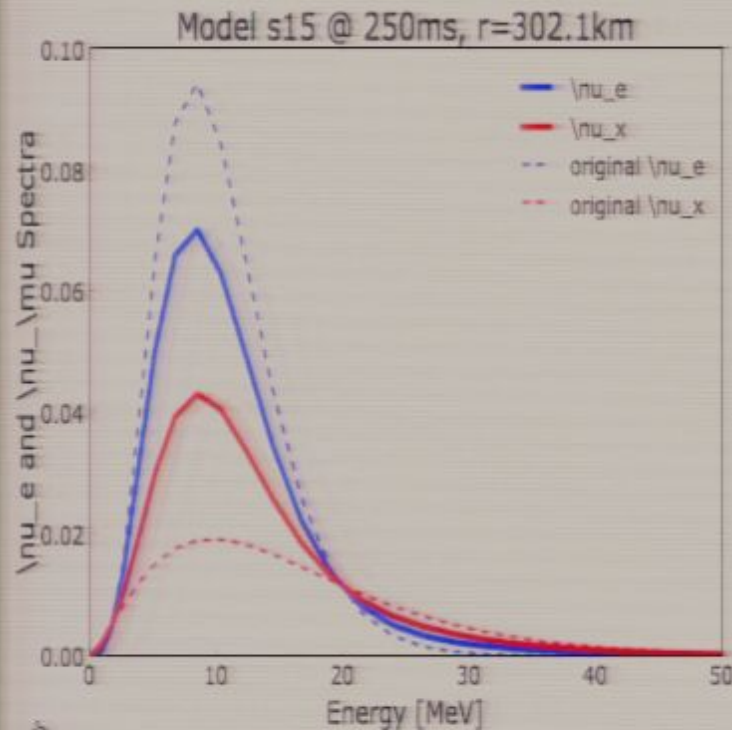
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



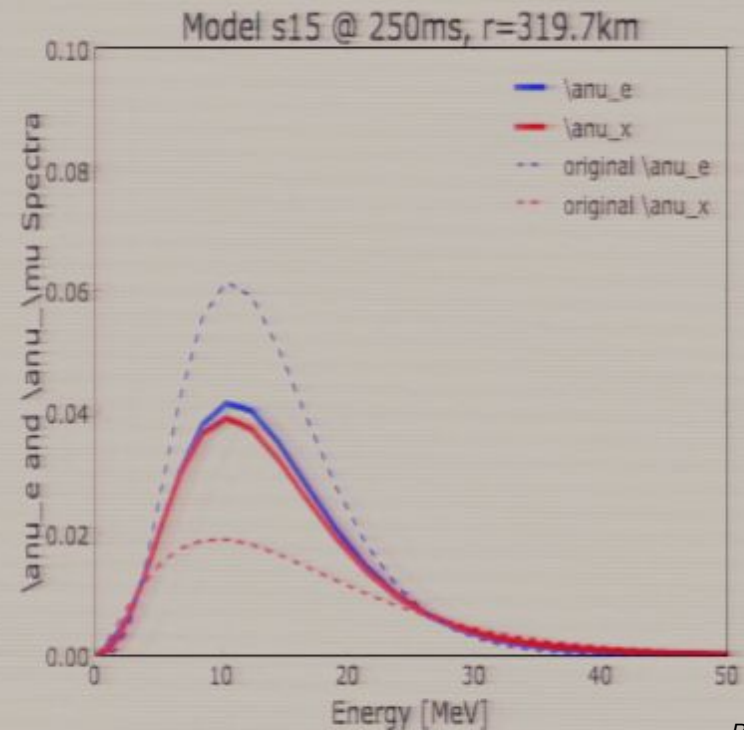
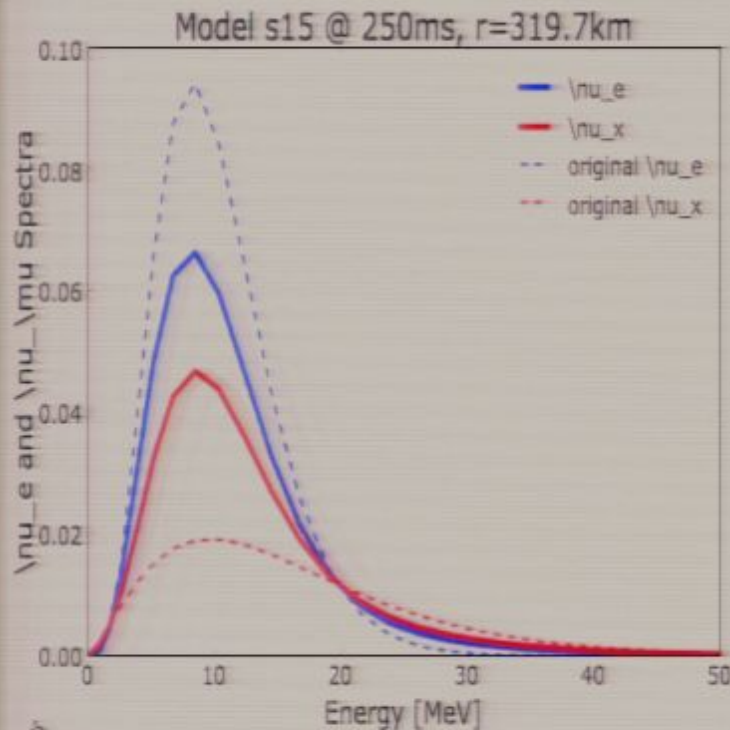
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



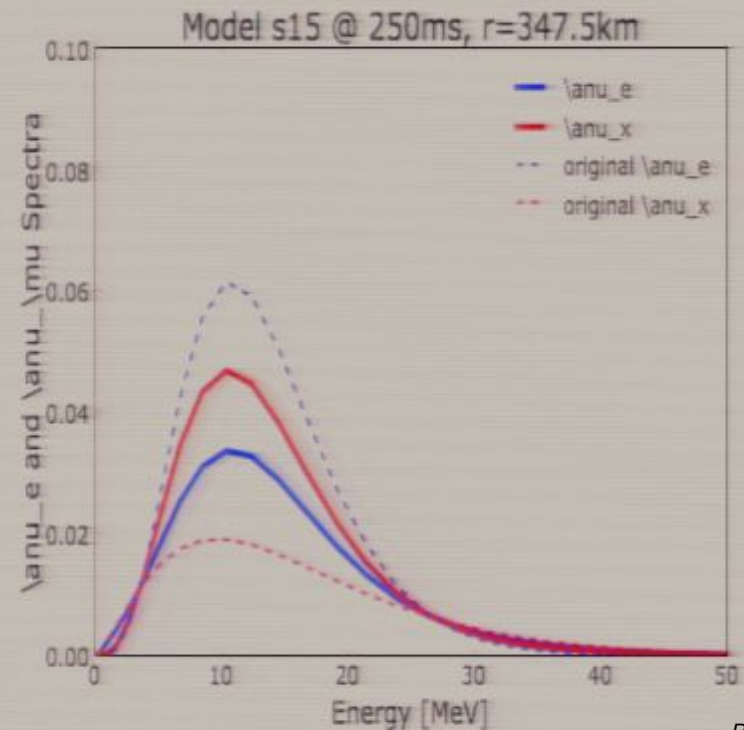
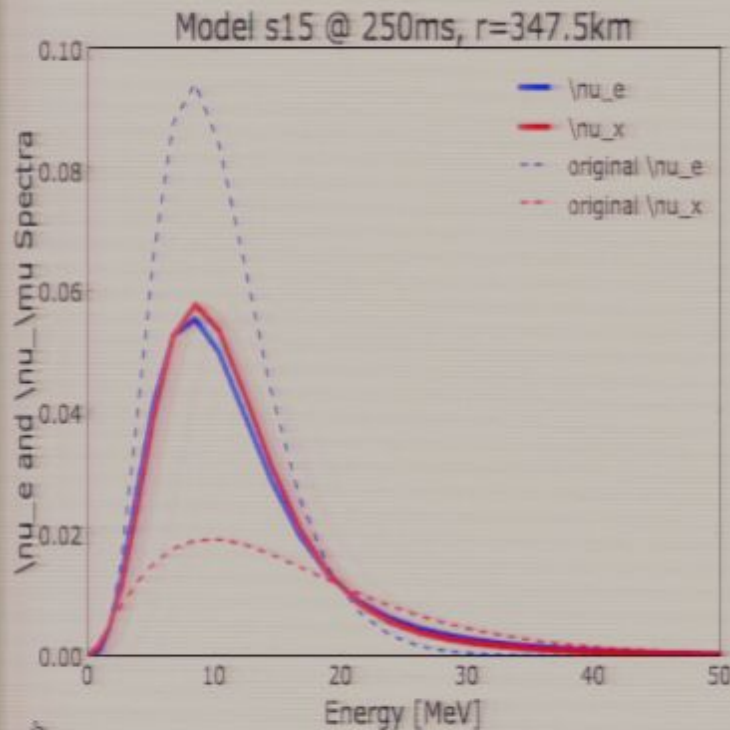
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



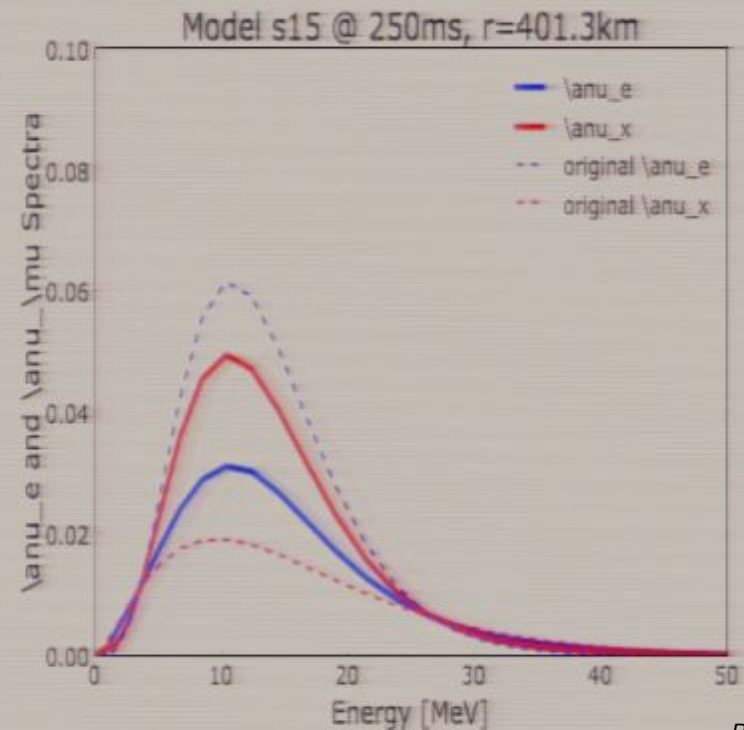
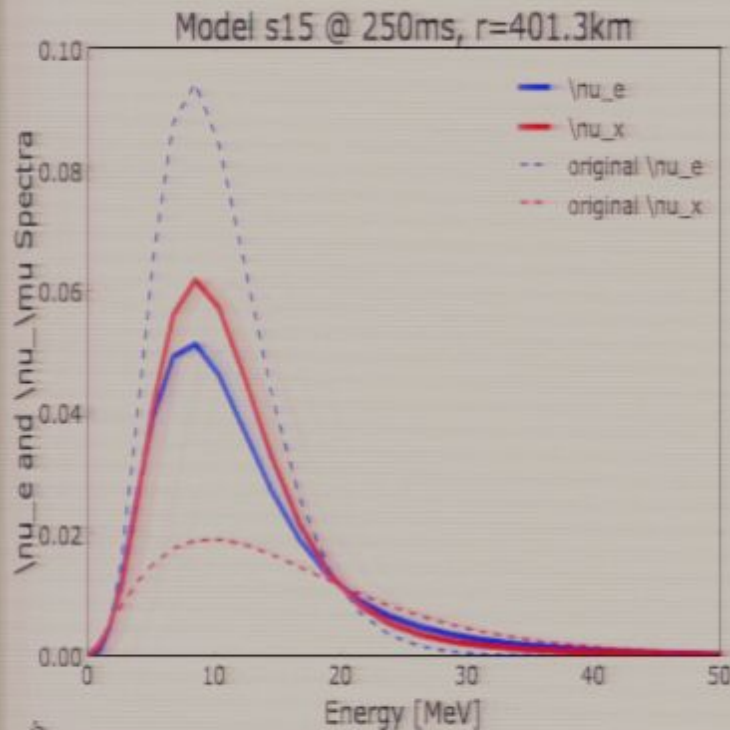
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



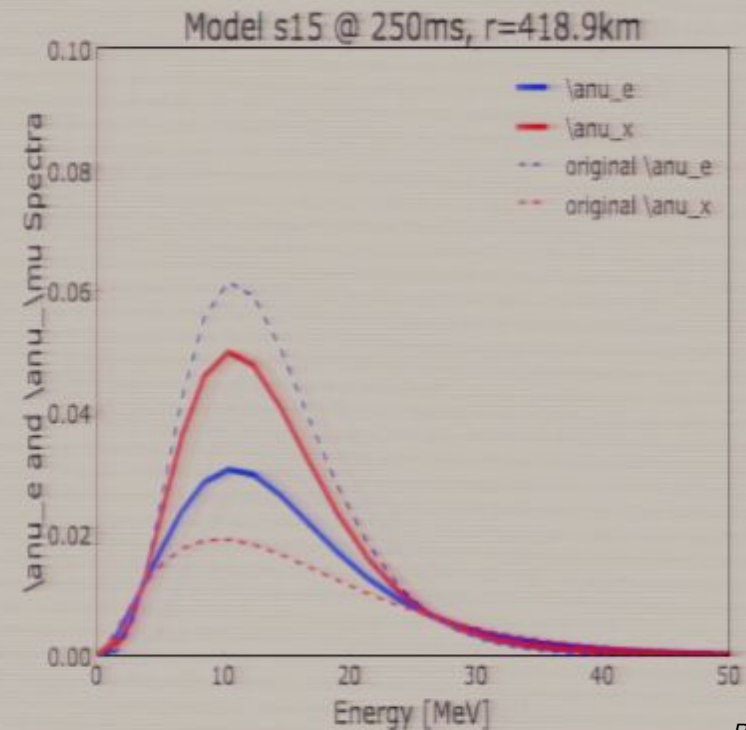
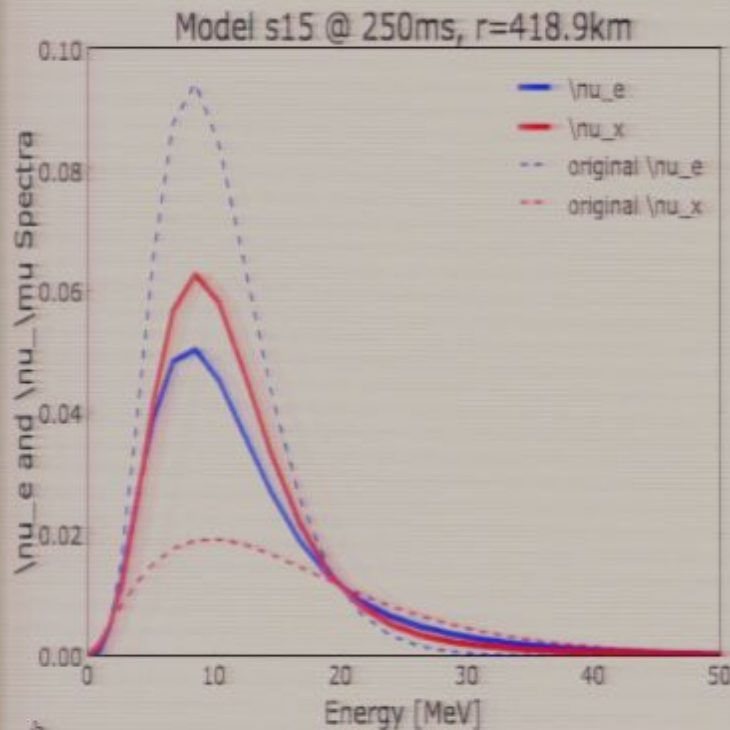
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



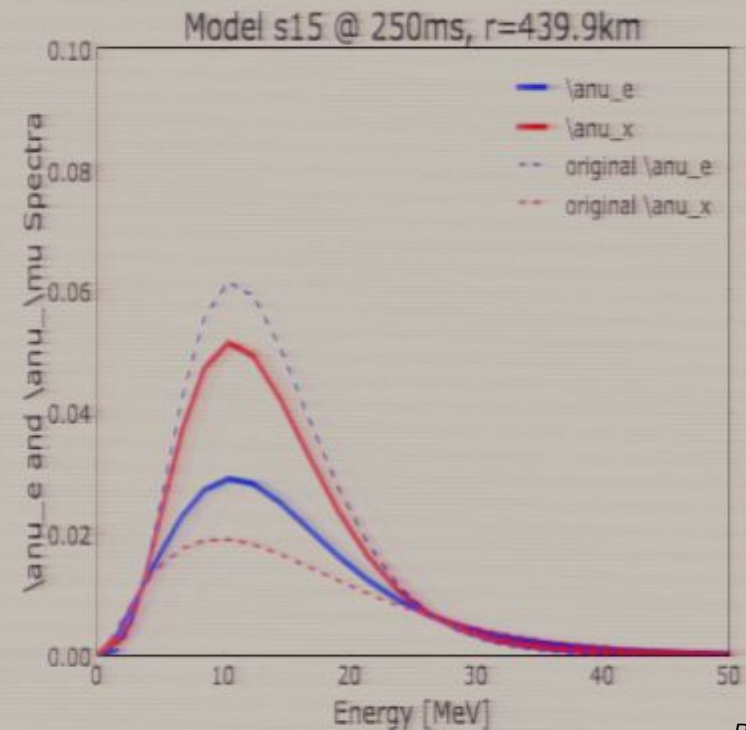
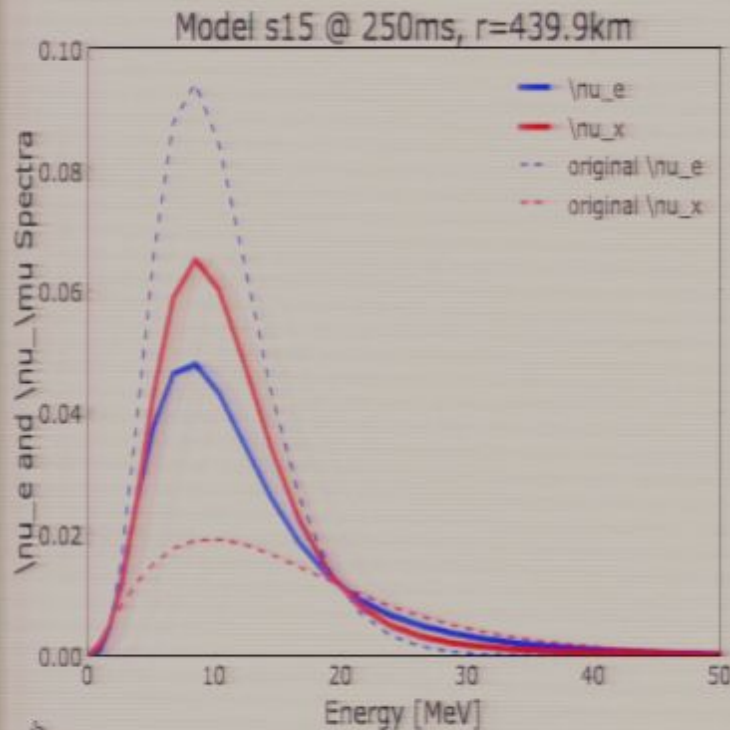
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



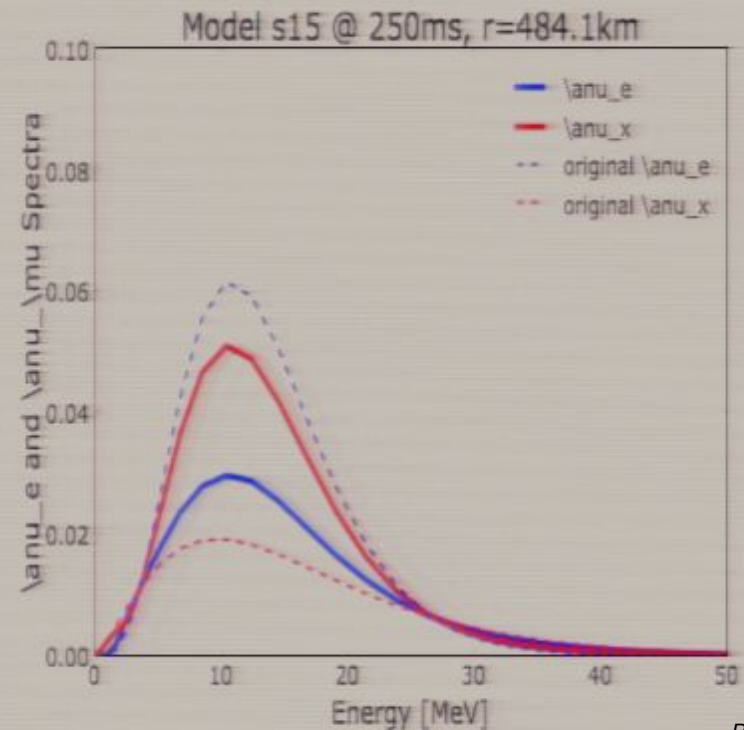
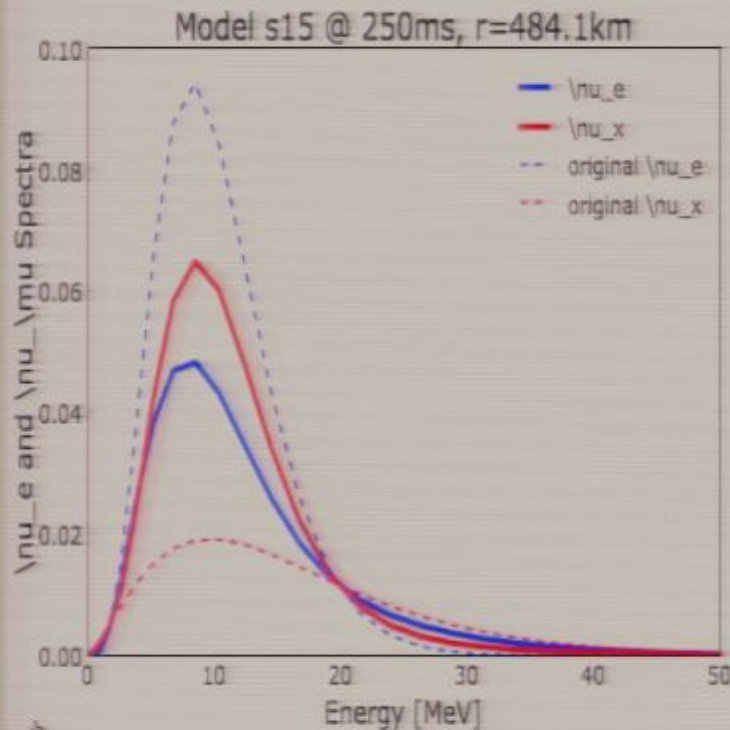
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



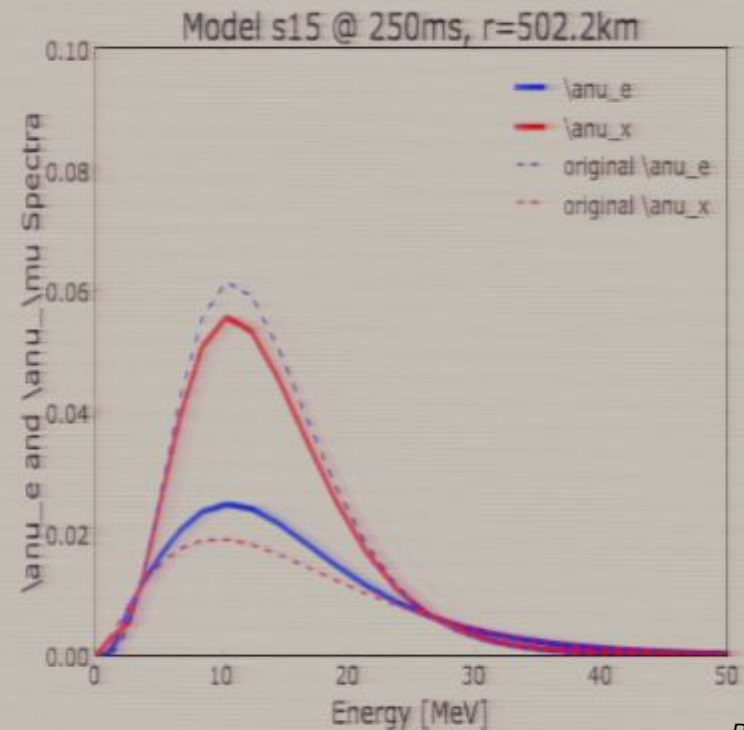
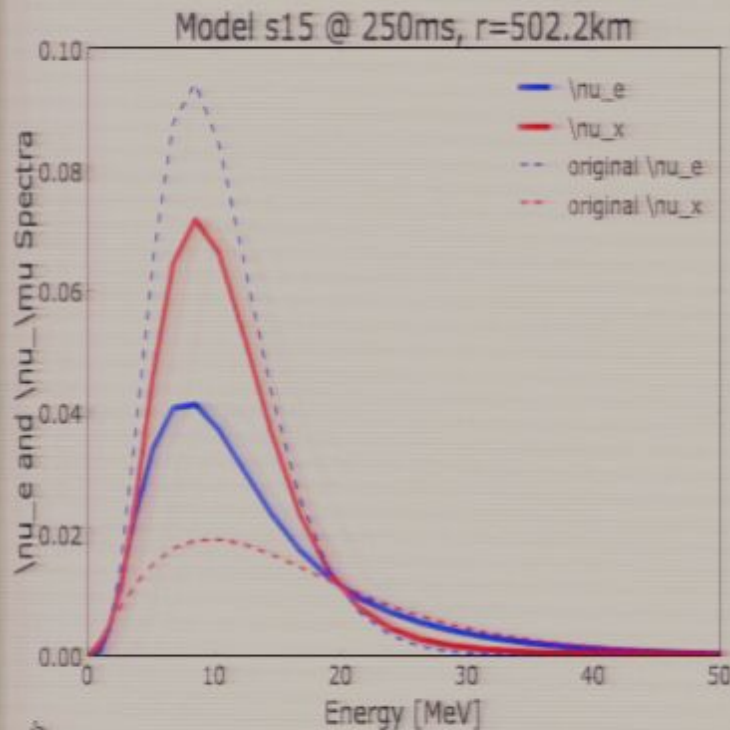
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



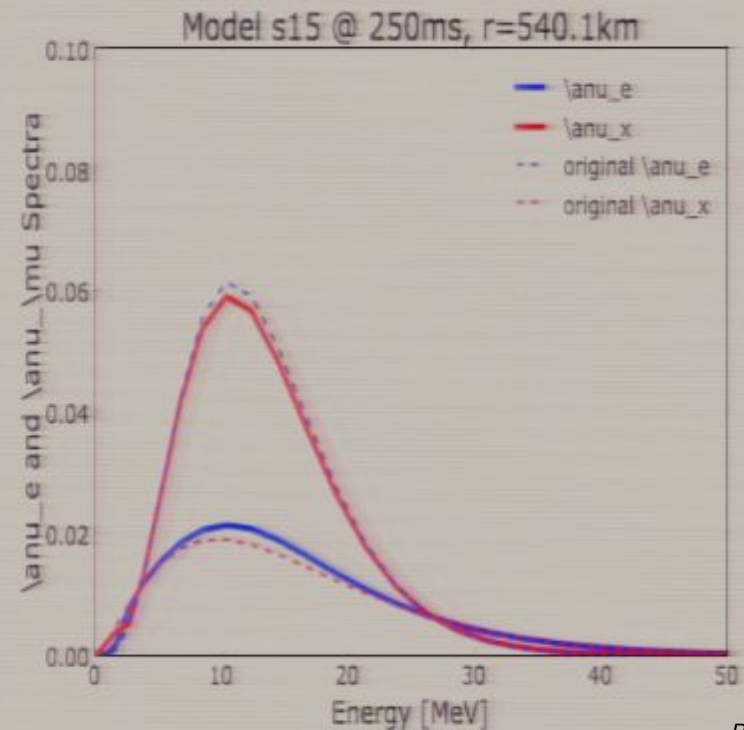
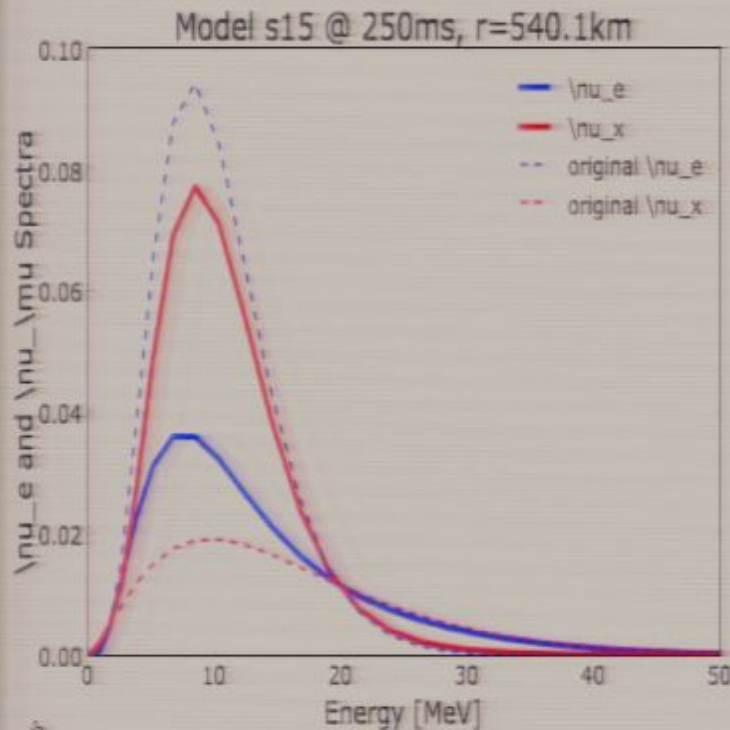
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



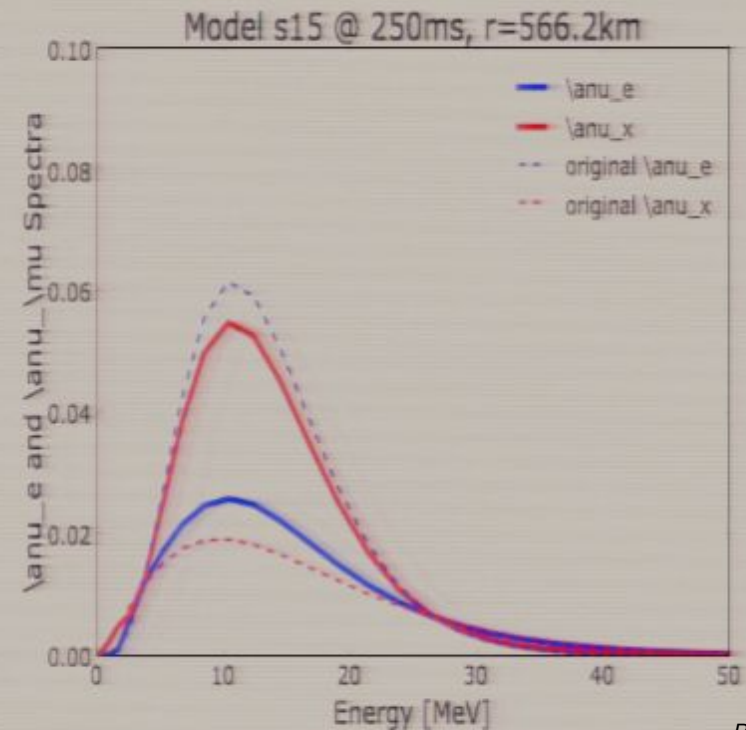
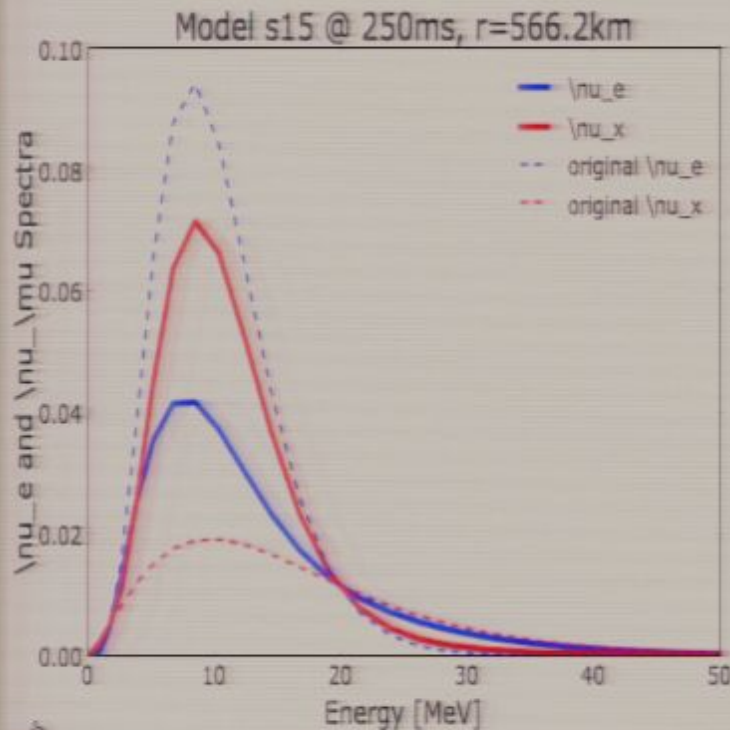
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



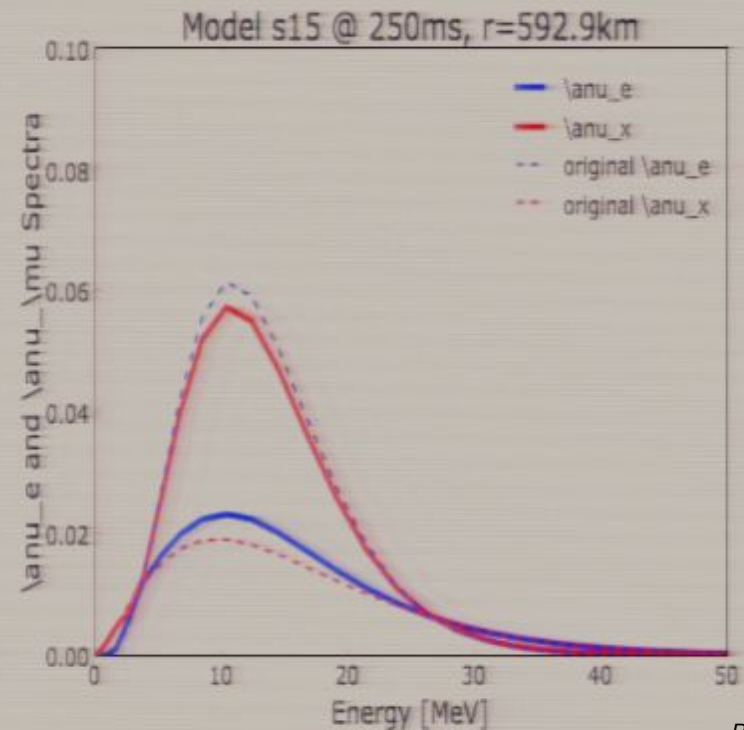
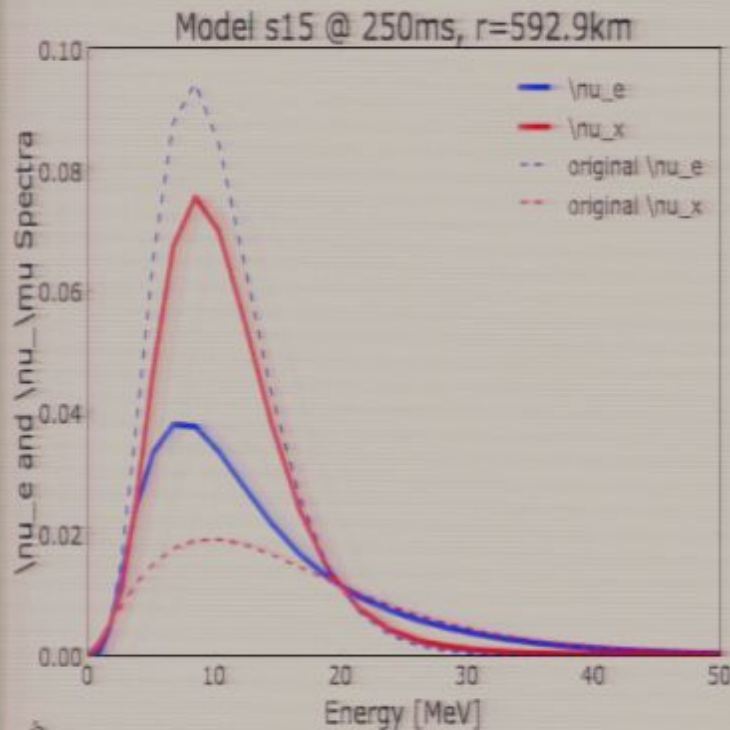
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



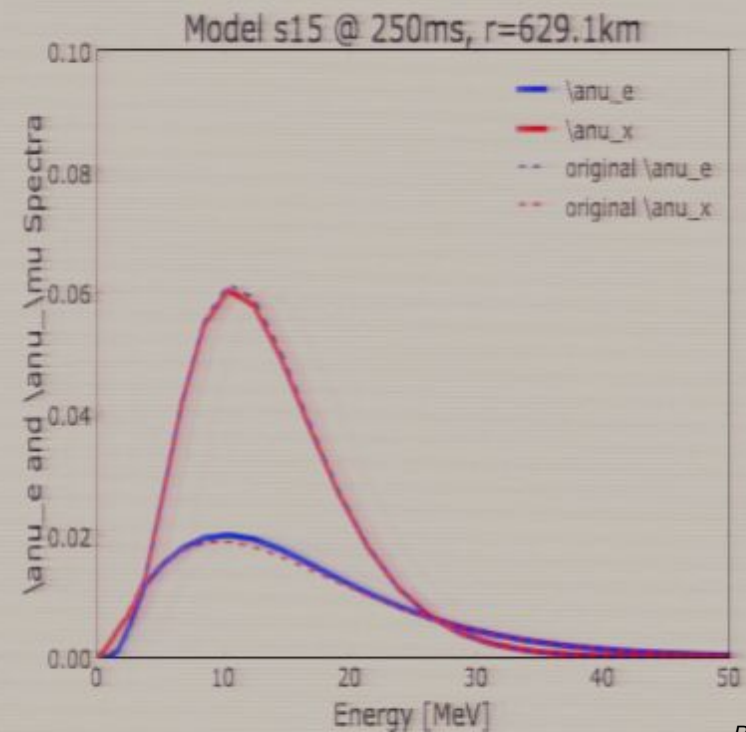
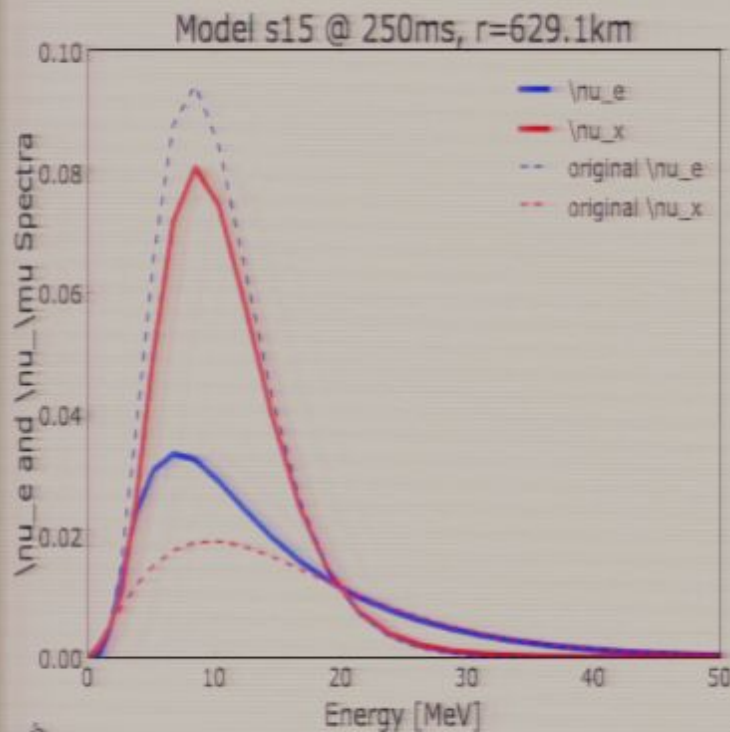
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



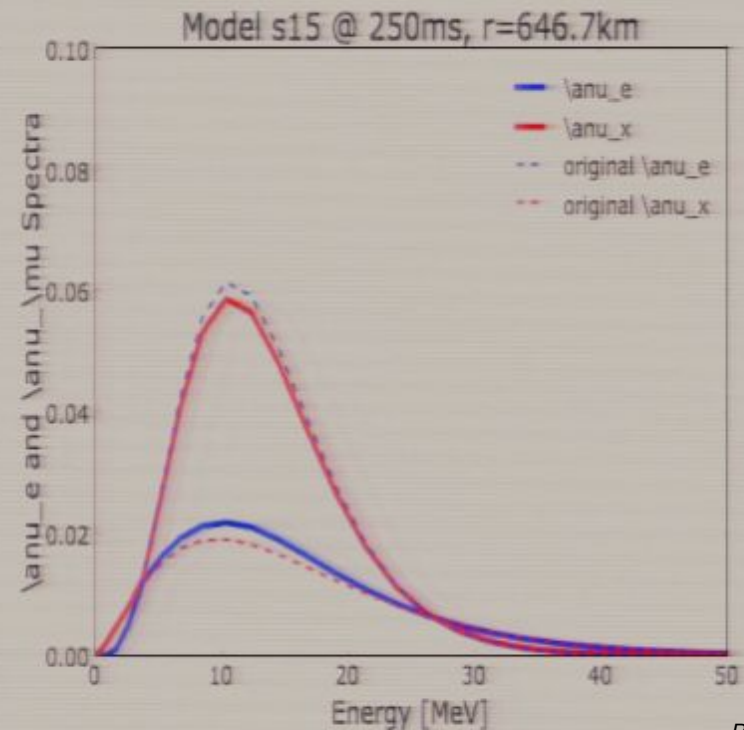
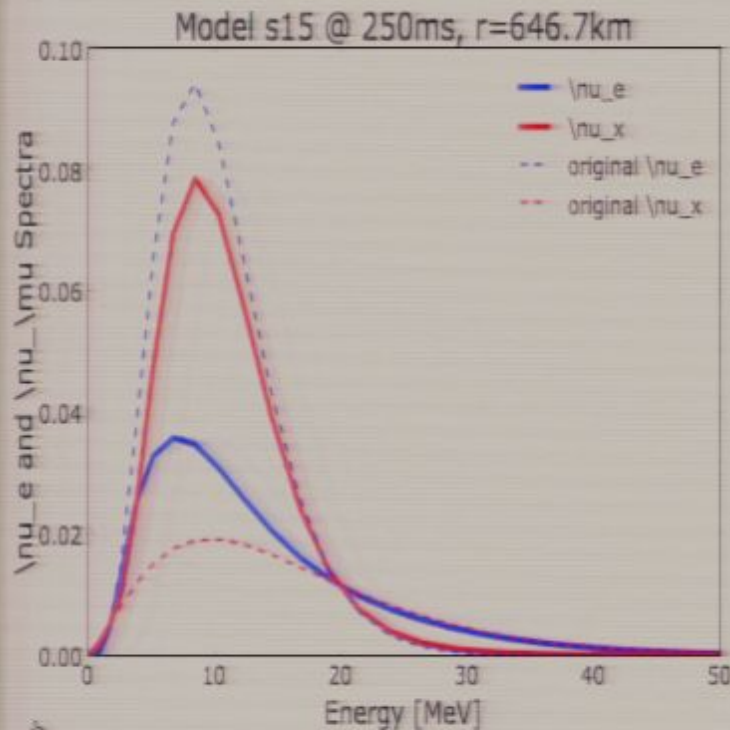
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



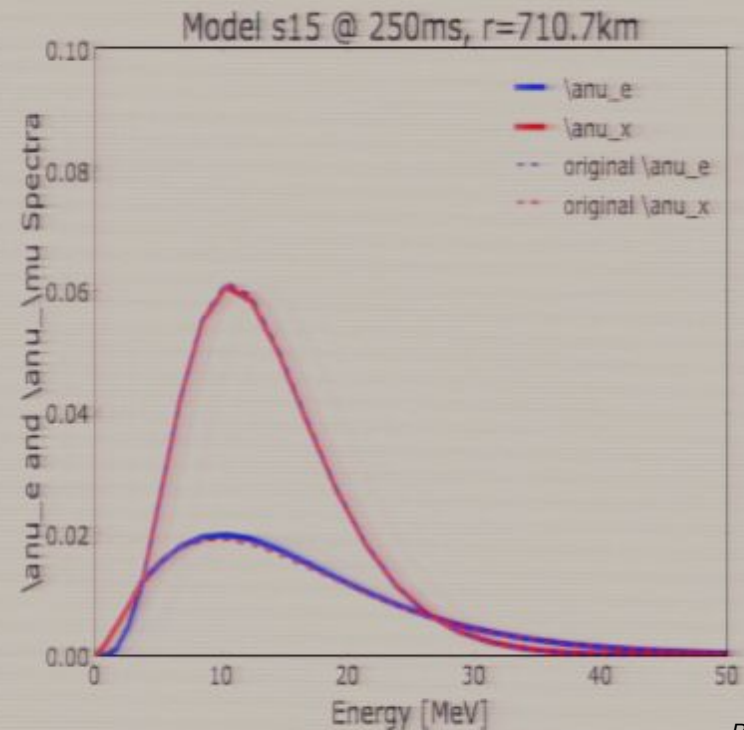
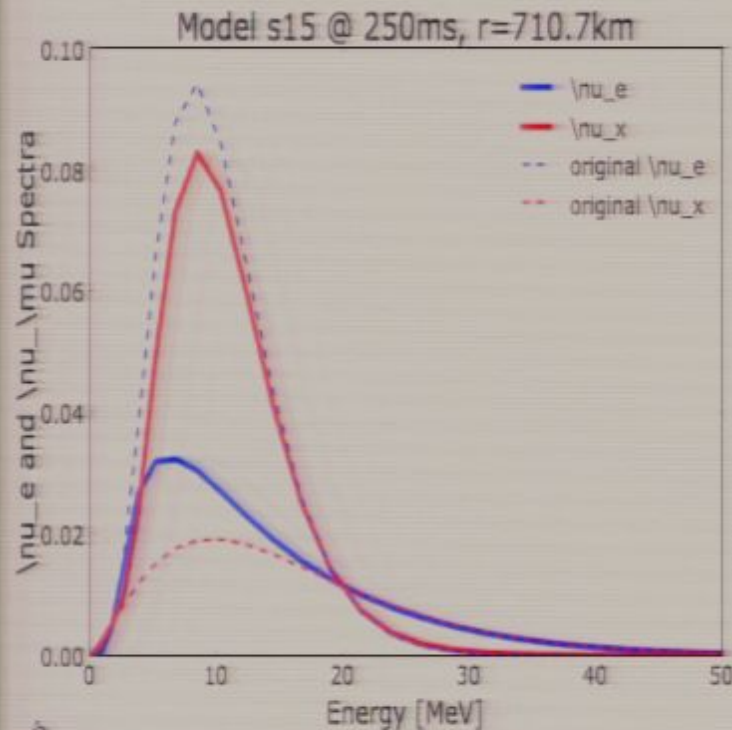
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



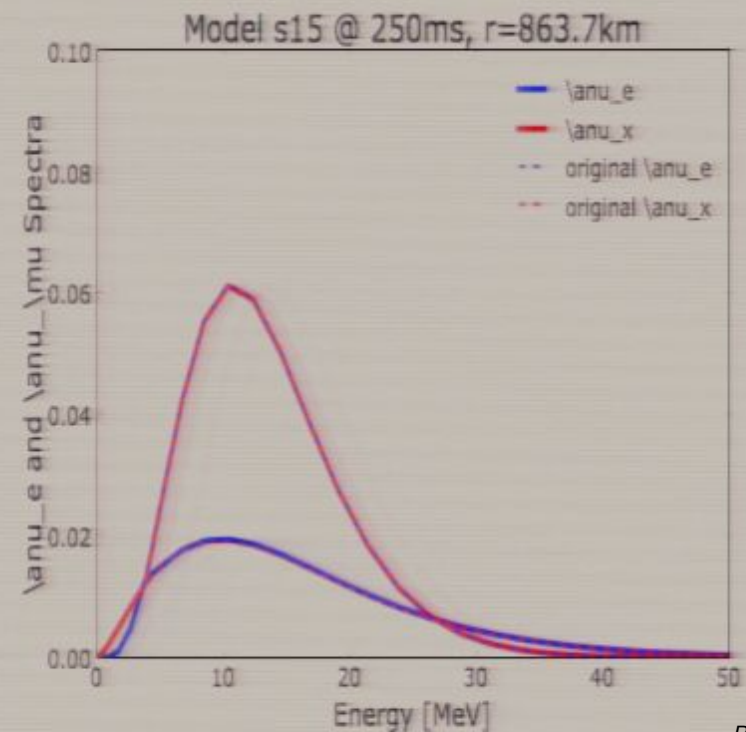
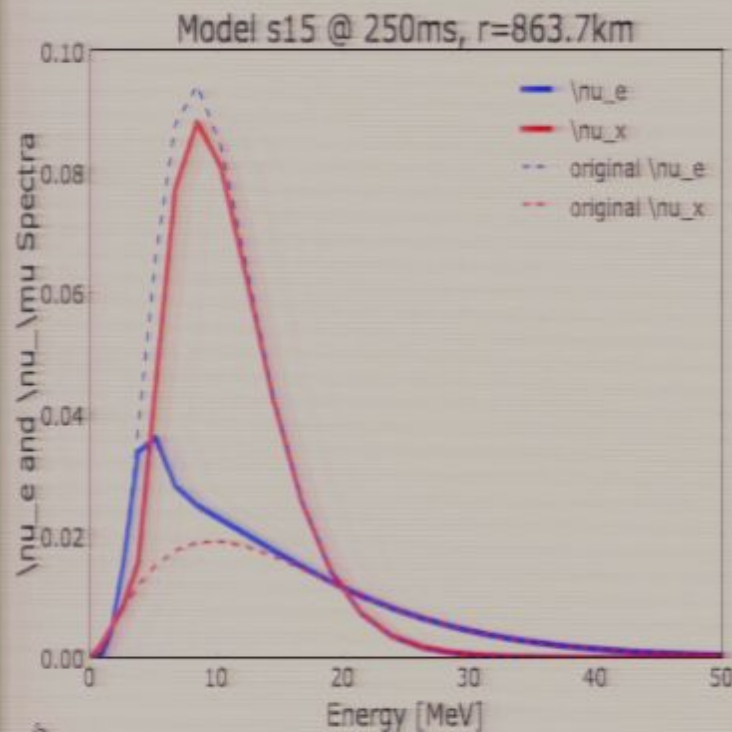
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



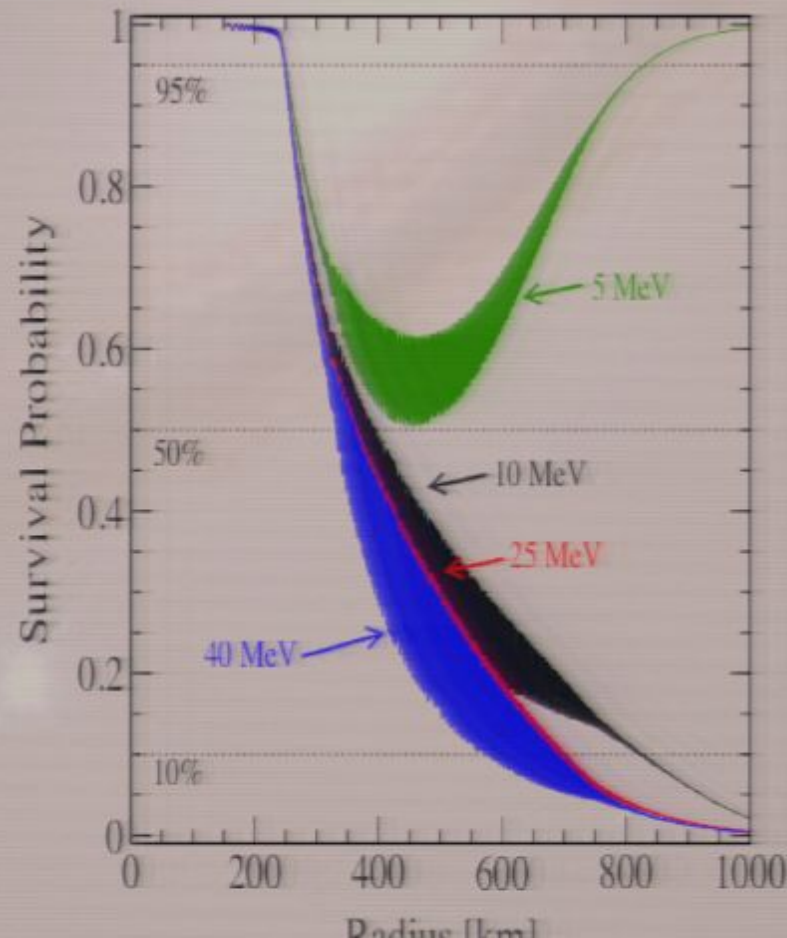
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



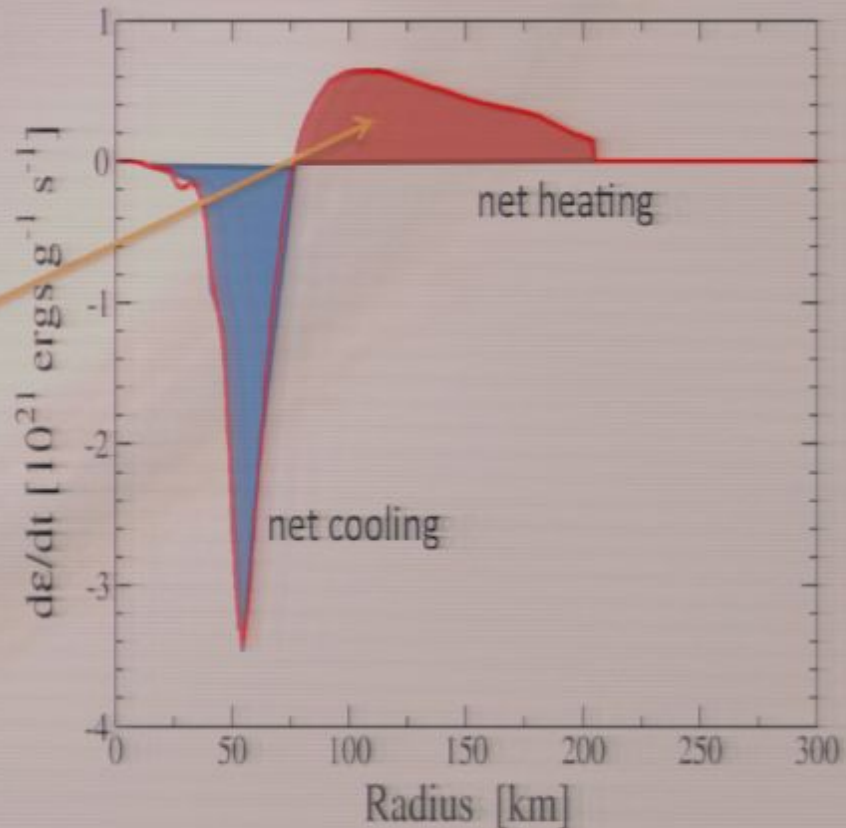
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



Theory of Neutrino Heating

- Neutrinos diffusing from core have a net energy deposition in the postshock region, the so called 'gain region'
- The neutrino mechanism works by having sufficient heating in the gain region to reenergize the shock



$$\mathcal{H} = \sum_{\nu_e, \bar{\nu}_e} \int_{r_g}^{r_s} dr 4\pi r^2 n_i \int_0^\infty d\epsilon \sigma_{\nu_i}(\epsilon) \frac{\epsilon d\Phi_{\nu_i}}{d\epsilon}$$

$$\sim \hat{\sigma} [\langle \epsilon_{\nu_e}^2 \rangle \mathcal{L}_{\nu_e} c_N + \langle \epsilon_{\bar{\nu}_e}^2 \rangle \mathcal{L}_{\bar{\nu}_e} c_P]$$

Exploratory simulations with VULCAN/2D

Livne, E. 1993, Burrows, A. et al. 2006

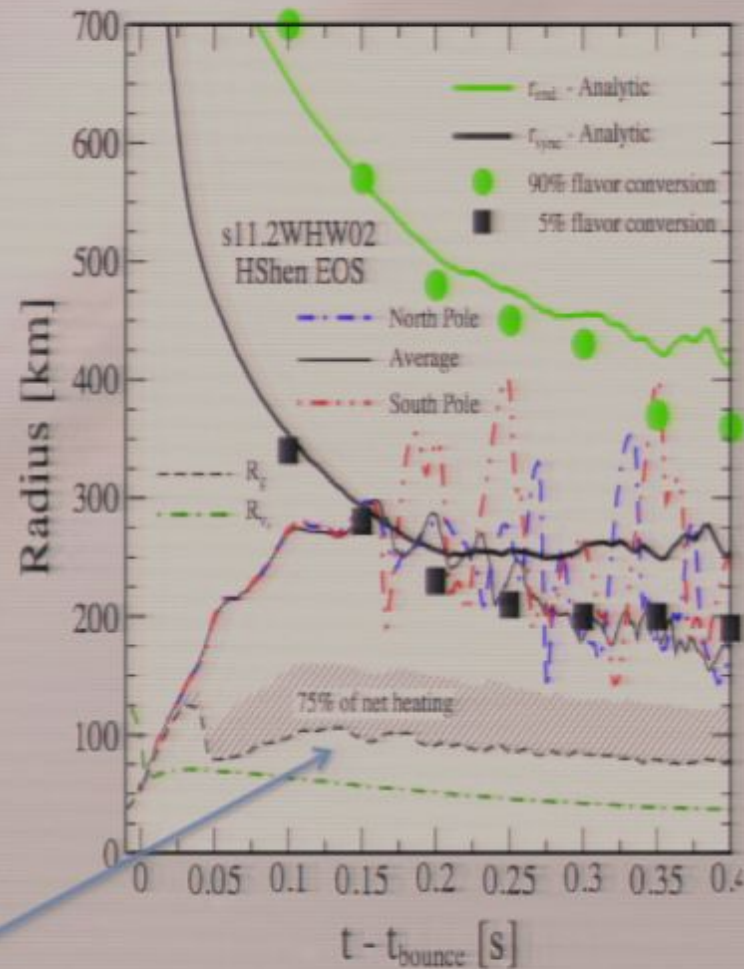
- Use 11.2 Msun progenitor from Woosley et al. 2002 and the Shen, H. et al. 1998 EOS
- Extract neutrino spectra at ν -sphere and run through dynamical neutrino evolution taking into account collective oscillations



Exploratory simulations with VULCAN/2D

Livne, E. 1993, Burrows, A. et al. 2006

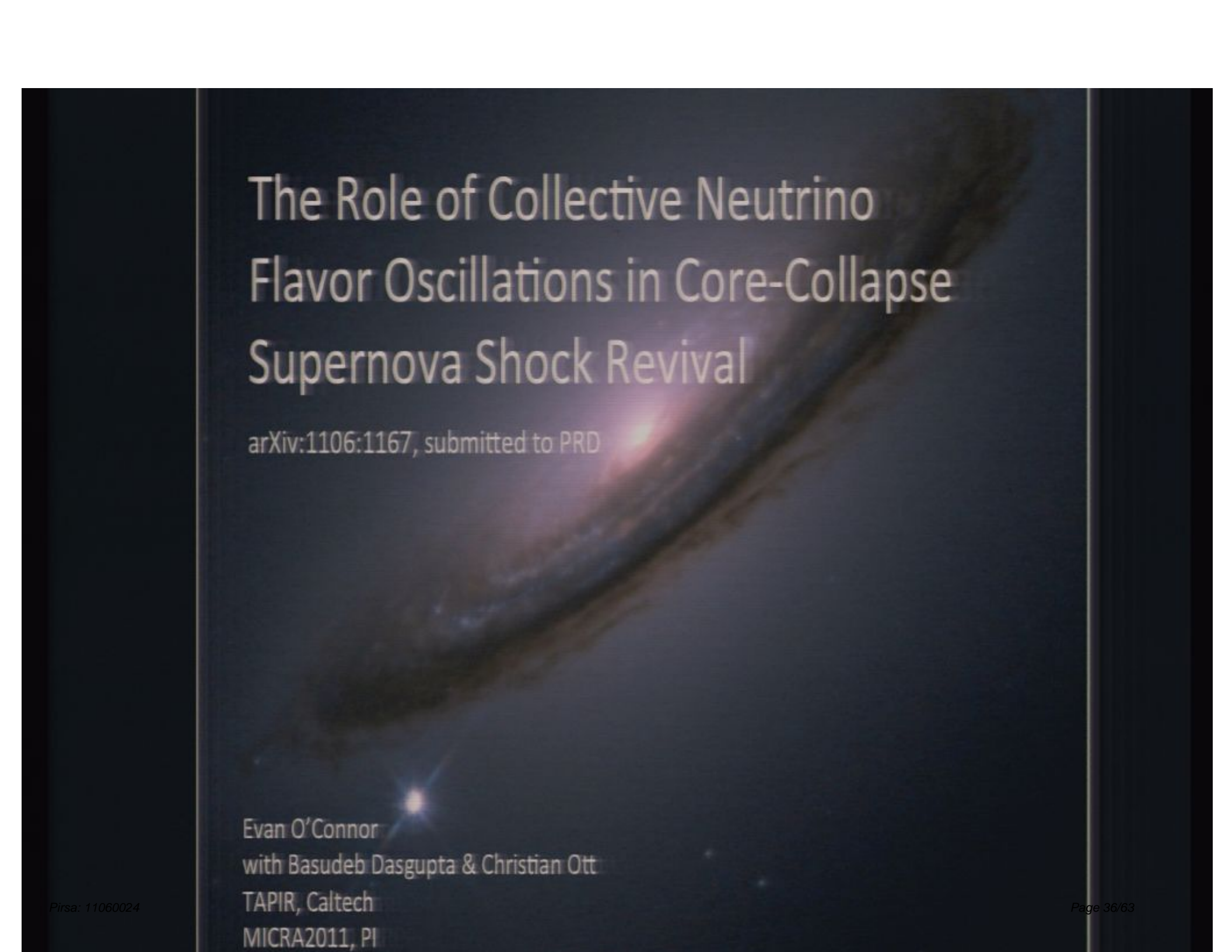
- Oscillation radii are large due to high neutrino luminosities and large neutrinosphere radii
- Even though oscillations being inside shock, not complete until well outside.
- Significant heating will occur only if oscillations occur before gain radius



Exploratory simulations with VULCAN/2D

Livne, E. 1993, Burrows, A. et al. 2006

- Use 11.2 Msun progenitor from Woosley et al. 2002 and the Shen, H. et al. 1998 EOS
- Extract neutrino spectra at ν -sphere and run through dynamical neutrino evolution taking into account collective oscillations



The Role of Collective Neutrino Flavor Oscillations in Core-Collapse Supernova Shock Revival

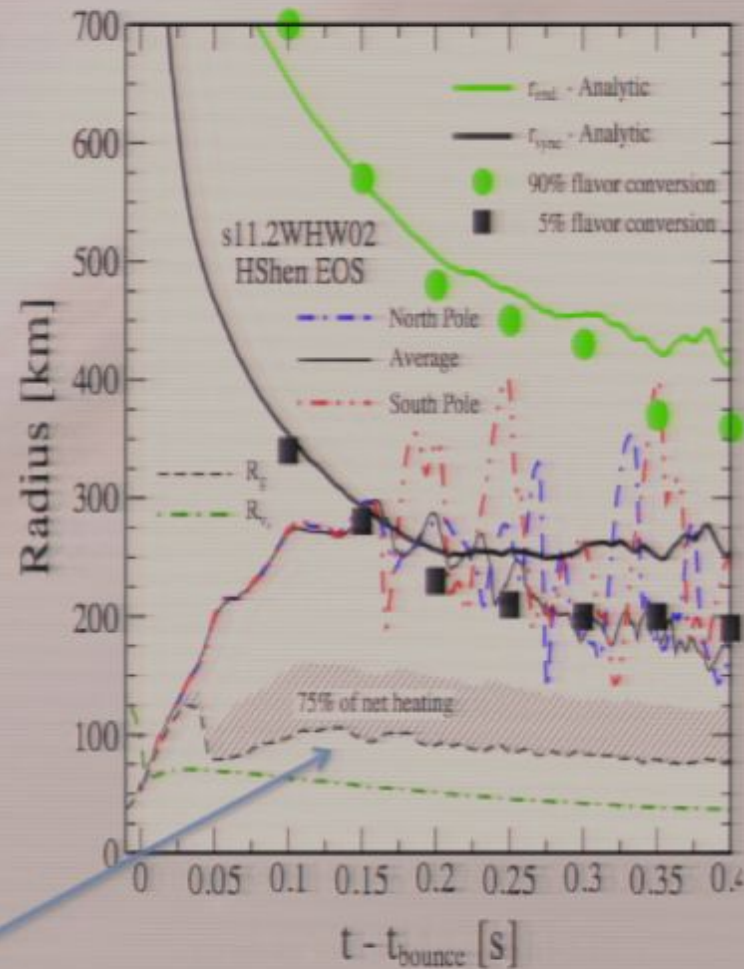
arXiv:1106.1167, submitted to PRD

Evan O'Connor
with Basudeb Dasgupta & Christian Ott
TAPIR, Caltech
MICRA2011, PI

Exploratory simulations with VULCAN/2D

Livne, E. 1993, Burrows, A. et al. 2006

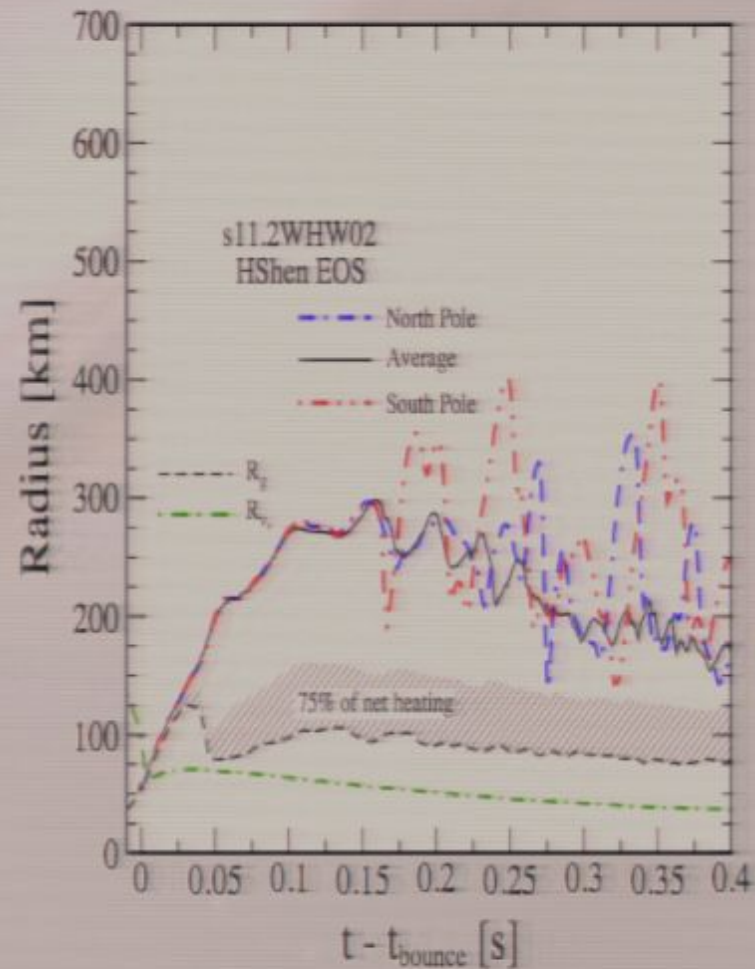
- Oscillation radii are large due to high neutrino luminosities and large neutrinosphere radii
- Even though oscillations being inside shock, not complete until well outside.
- Significant heating will occur only if oscillations occur before gain radius



Exploratory simulations with VULCAN/2D

Livne, E. 1993, Burrows, A. et al. 2006

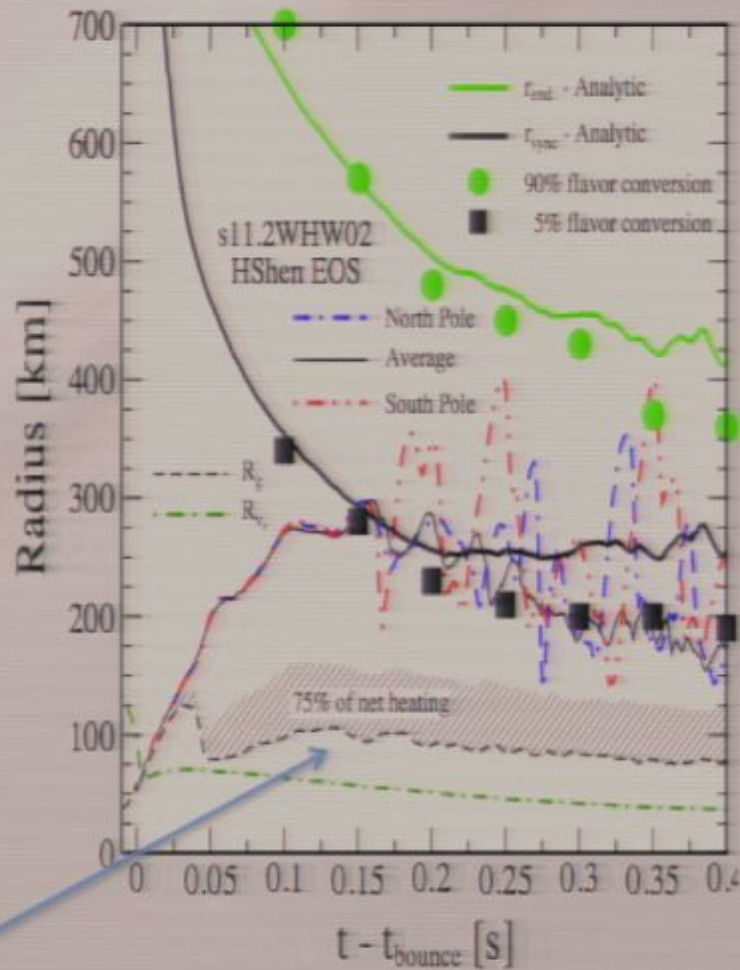
- Use 11.2 Msun progenitor from Woosley et al. 2002 and the Shen, H. et al. 1998 EOS
- Extract neutrino spectra at ν -sphere and run through dynamical neutrino evolution taking into account collective oscillations



Exploratory simulations with VULCAN/2D

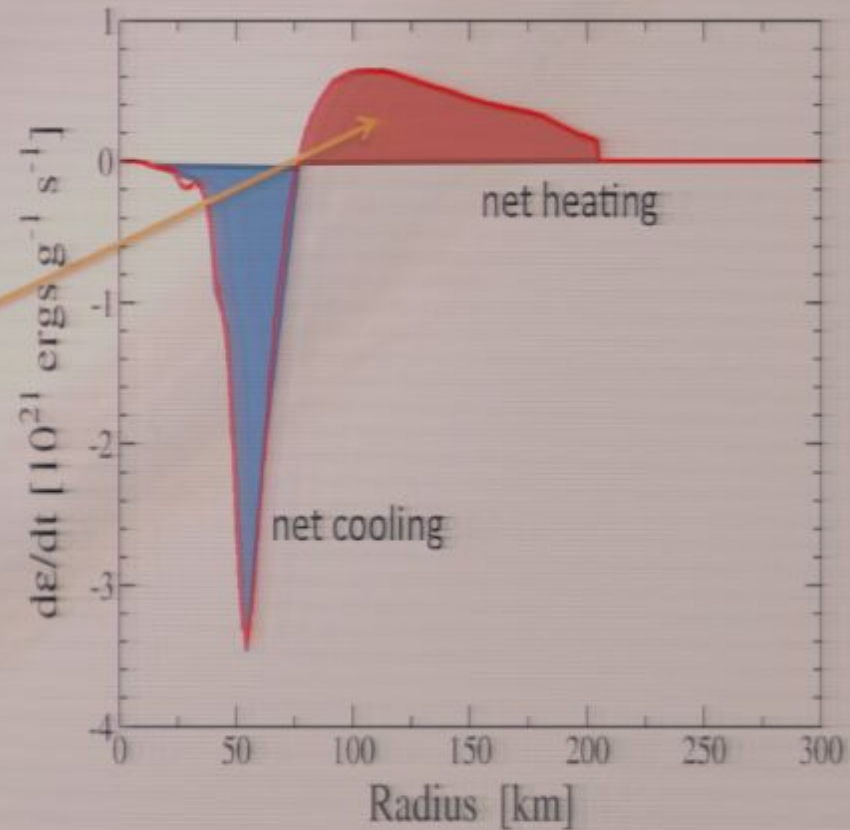
Livne, E. 1993, Burrows, A. et al. 2006

- Oscillation radii are large due to high neutrino luminosities and large neutrinosphere radii
- Even though oscillations being inside shock, not complete until well outside.
- Significant heating will occur only if oscillations occur before gain radius



Theory of Neutrino Heating

- Neutrinos diffusing from core have a net energy deposition in the postshock region, the so called 'gain region'
- The neutrino mechanism works by having sufficient heating in the gain region to reenergize the shock

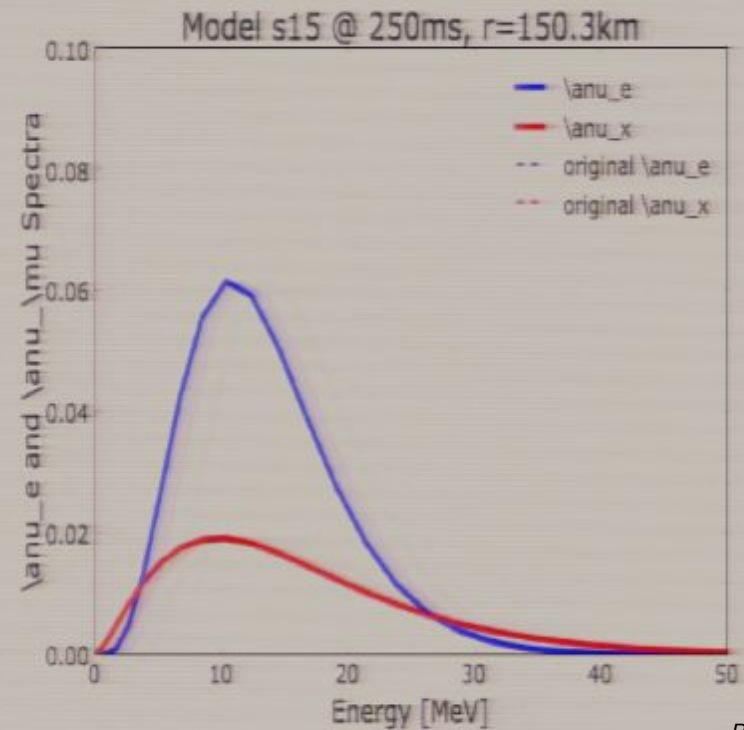
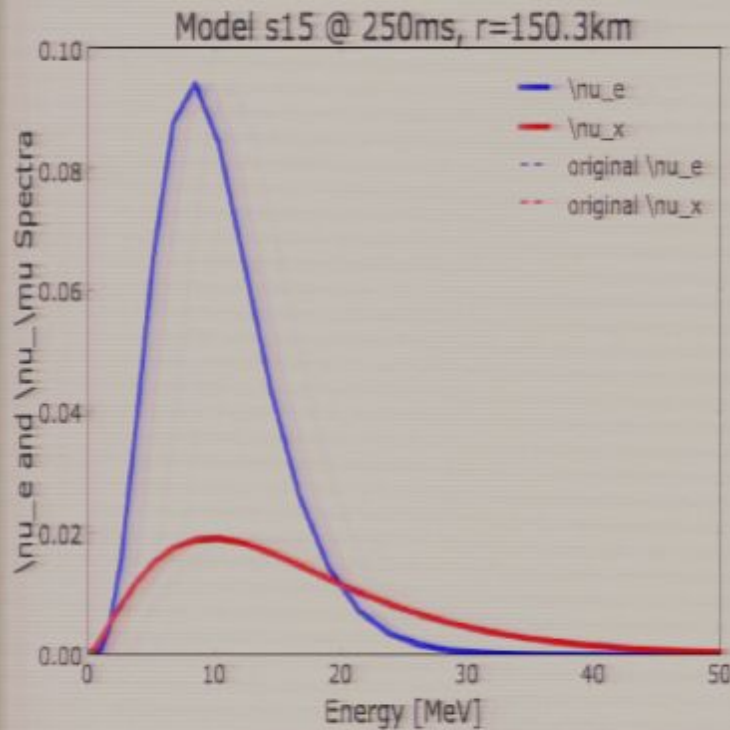


$$\mathcal{H} = \sum_{\nu_e, \bar{\nu}_e} \int_{r_g}^{r_s} dr 4\pi r^2 n_i \int_0^\infty d\epsilon \sigma_{\nu_i}(\epsilon) \frac{\epsilon d\Phi_{\nu_i}}{d\epsilon}$$

$$\sim \hat{\sigma} [\langle \epsilon_{\nu_e}^2 \rangle \mathcal{L}_{\nu_e} c_N + \langle \epsilon_{\bar{\nu}_e}^2 \rangle \mathcal{L}_{\bar{\nu}_e} c_P]$$

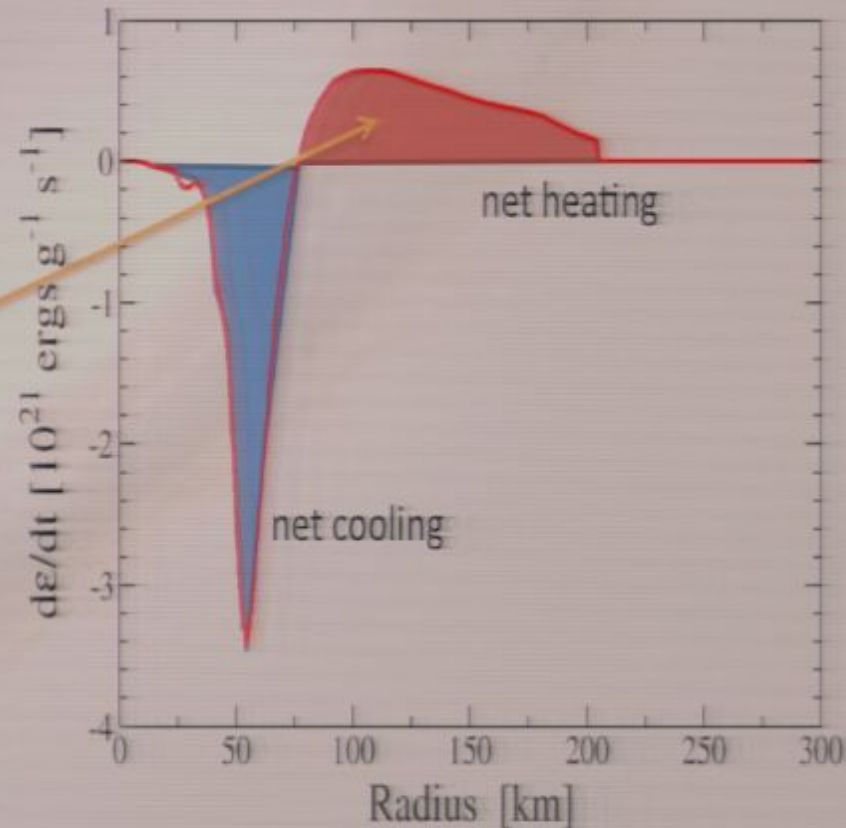
Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail



Theory of Neutrino Heating

- Neutrinos diffusing from core have a net energy deposition in the postshock region, the so called 'gain region'
- The neutrino mechanism works by having sufficient heating in the gain region to reenergize the shock



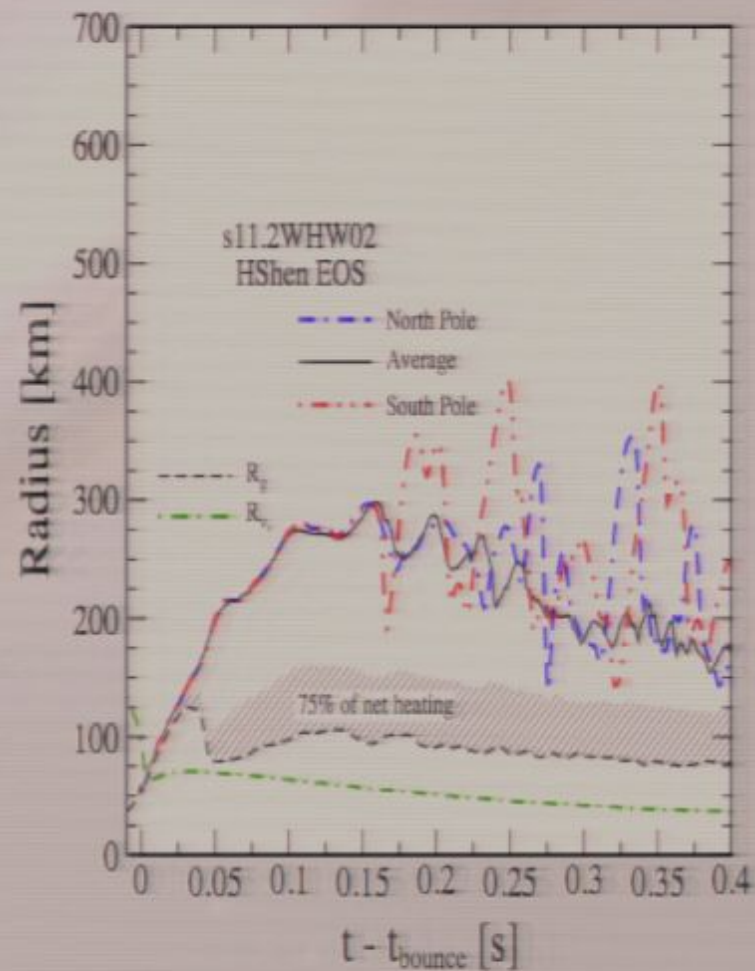
$$\mathcal{H} = \sum_{\nu_e, \bar{\nu}_e} \int_{r_g}^{r_s} dr 4\pi r^2 n_i \int_0^{\infty} d\epsilon \sigma_{\nu_i}(\epsilon) \frac{\epsilon d\Phi_{\nu_i}}{d\epsilon}$$

$$\sim \hat{\sigma} [\langle \epsilon_{\nu}^2 \rangle \mathcal{L}_{\nu} c_N + \langle \epsilon_{\bar{\nu}}^2 \rangle \mathcal{L}_{\bar{\nu}} c_P]$$

Exploratory simulations with VULCAN/2D

Livne, E. 1993, Burrows, A. et al. 2006

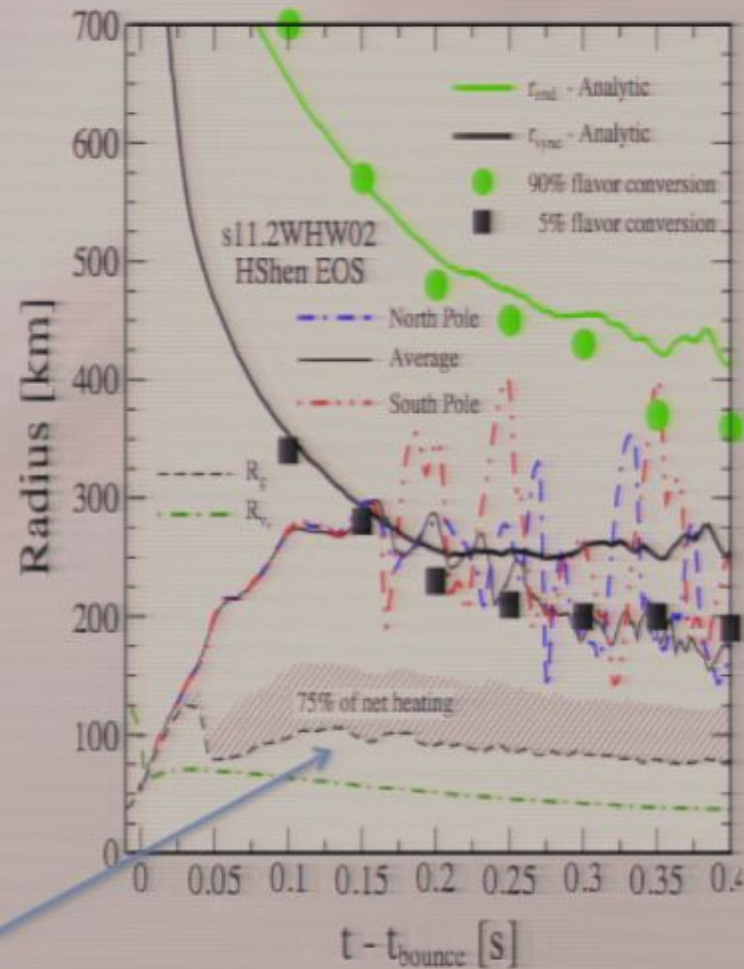
- Use 11.2 Msun progenitor from Woosley et al. 2002 and the Shen, H. et al. 1998 EOS
- Extract neutrino spectra at ν -sphere and run through dynamical neutrino evolution taking into account collective oscillations



Exploratory simulations with VULCAN/2D

Livne, E. 1993, Burrows, A. et al. 2006

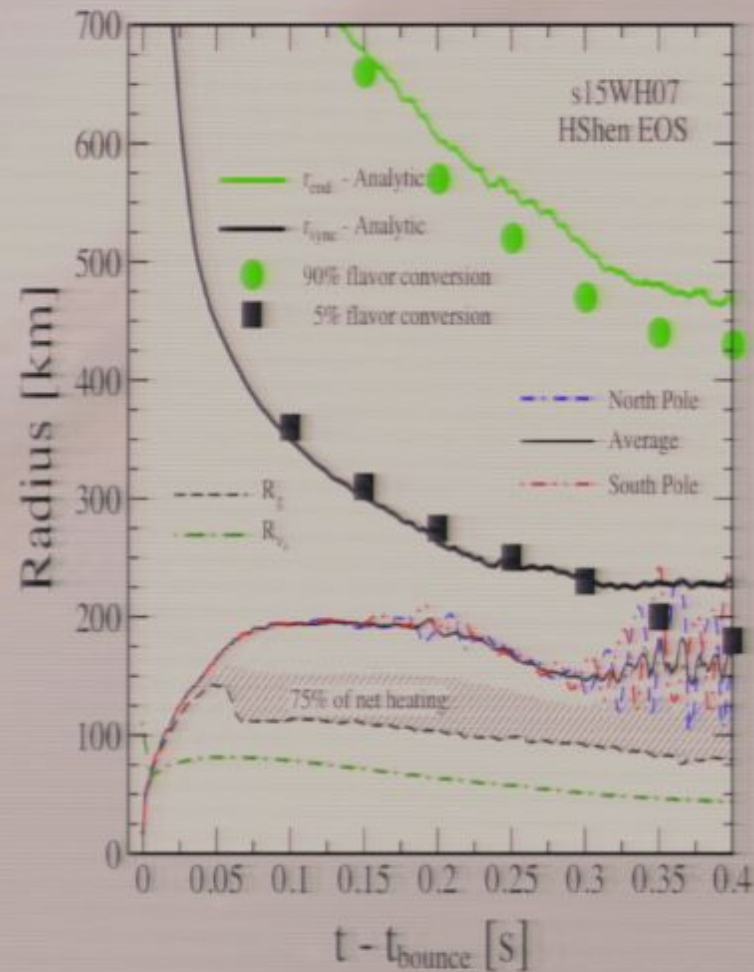
- Oscillation radii are large due to high neutrino luminosities and large neutrinosphere radii
- Even though oscillations being inside shock, not complete until well outside.
- Significant heating will occur only if oscillations occur before gain radius



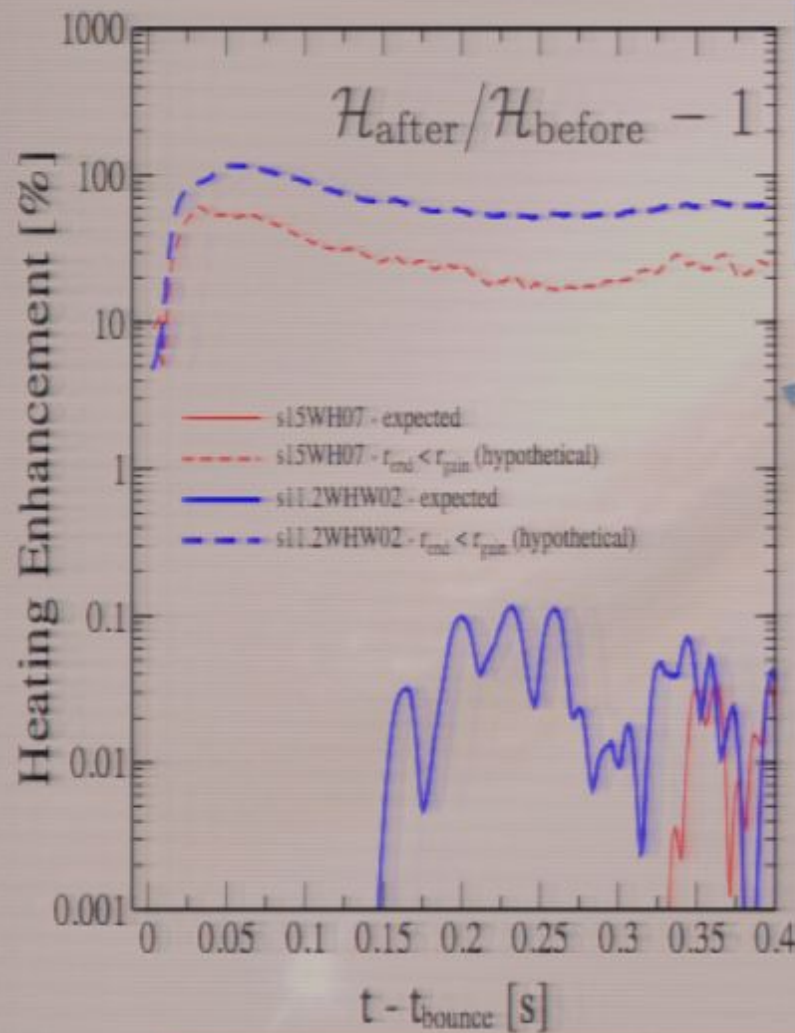
Exploratory simulations with VULCAN/2D

Livne, E. 1993, Burrows, A. et al. 2006

- Use 15 Msun progenitor from Woosley et al. 2007 and the Shen, H. et al. 1998 EOS
- Higher accretion rates suppress SASI and keep shock at lower radii
- Neutrino oscillations occur at roughly same location as 11.2 model, little affect on heating



Expected Heating Enhancement



$$\mathcal{H}_{\text{after}} \sim \mathcal{H}_{\text{before}}$$

$$+ \hat{\sigma} [\langle \epsilon_{\nu_e}^2 \rangle \mathcal{L}_{\nu_e}^{\text{ns}} - \langle \epsilon_{\nu_e}^2 \rangle \mathcal{L}_{\nu_e}^{\text{ns}}] c_N^O$$

$$+ \hat{\sigma} [\langle \epsilon_{\nu_e}^2 \rangle \mathcal{L}_{\nu_e}^{\text{ns}} - \langle \epsilon_{\nu_e}^2 \rangle \mathcal{L}_{\nu_e}^{\text{ns}}] c_P^O$$

$$+ \hat{\sigma} \langle \epsilon_{\nu_e}^2 \rangle^* [\langle \epsilon_{\nu_e} \rangle^* (\mathcal{N}_{\nu_e}^{\text{ns}} - \mathcal{N}_{\nu_e}^{\text{ns}})] c_N^O$$

- Hypothetical situation where oscillations complete before gain radius

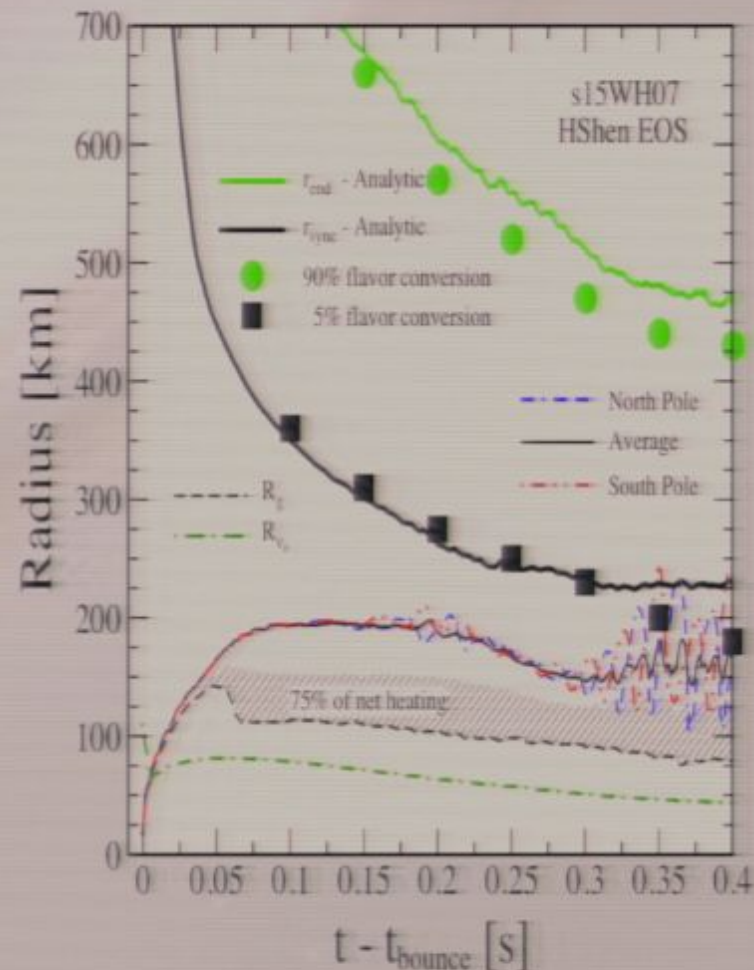
- Actual heating enhancement is much less, $< 1\%$

Take home message, collective neutrino oscillations do not help explode CCSNe

Exploratory simulations with VULCAN/2D

Livne, E. 1993, Burrows, A. et al. 2006

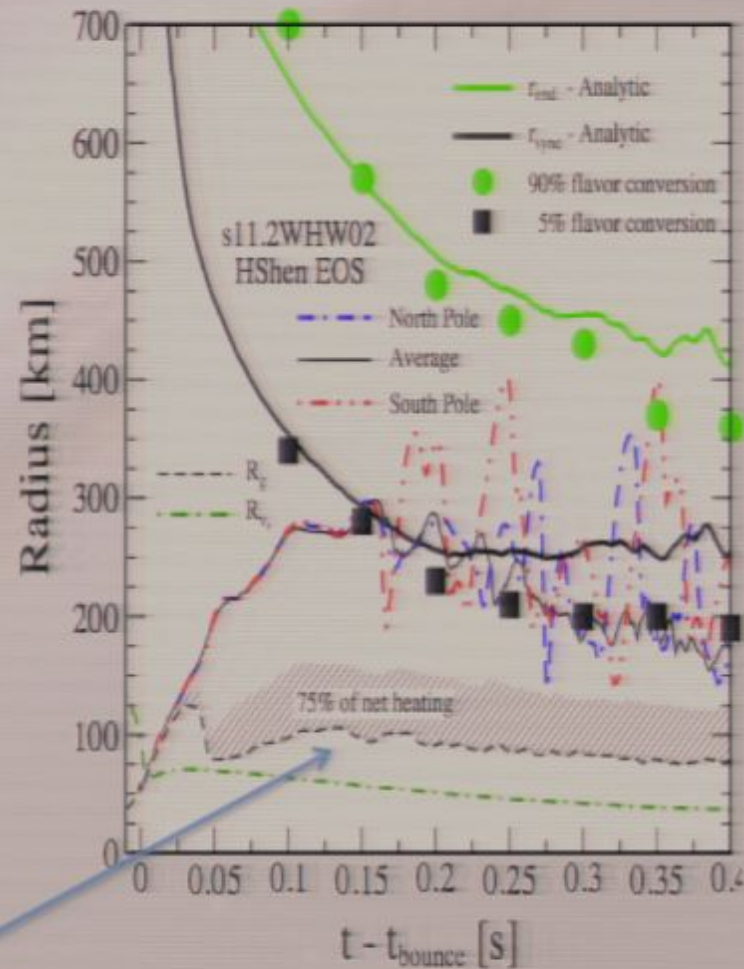
- Use 15 Msun progenitor from Woosley et al. 2007 and the Shen, H. et al. 1998 EOS
- Higher accretion rates suppress SASI and keep shock at lower radii
- Neutrino oscillations occur at roughly same location as 11.2 model, little affect on heating



Exploratory simulations with VULCAN/2D

Livne, E. 1993, Burrows, A. et al. 2006

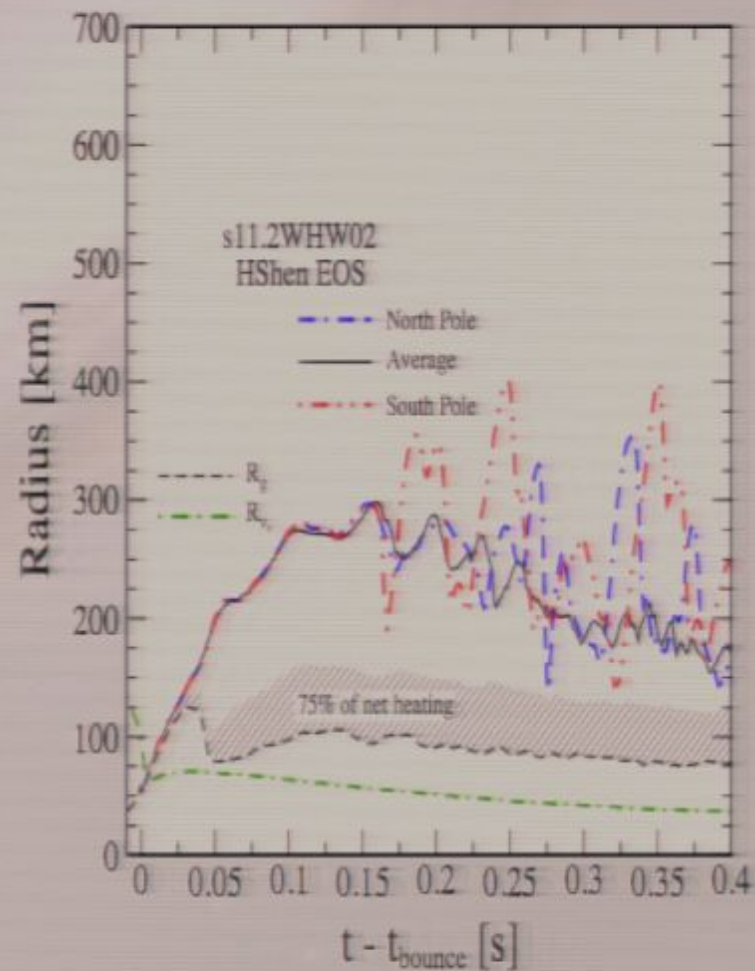
- Oscillation radii are large due to high neutrino luminosities and large neutrinosphere radii
- Even though oscillations being inside shock, not complete until well outside.
- Significant heating will occur only if oscillations occur before gain radius



Exploratory simulations with VULCAN/2D

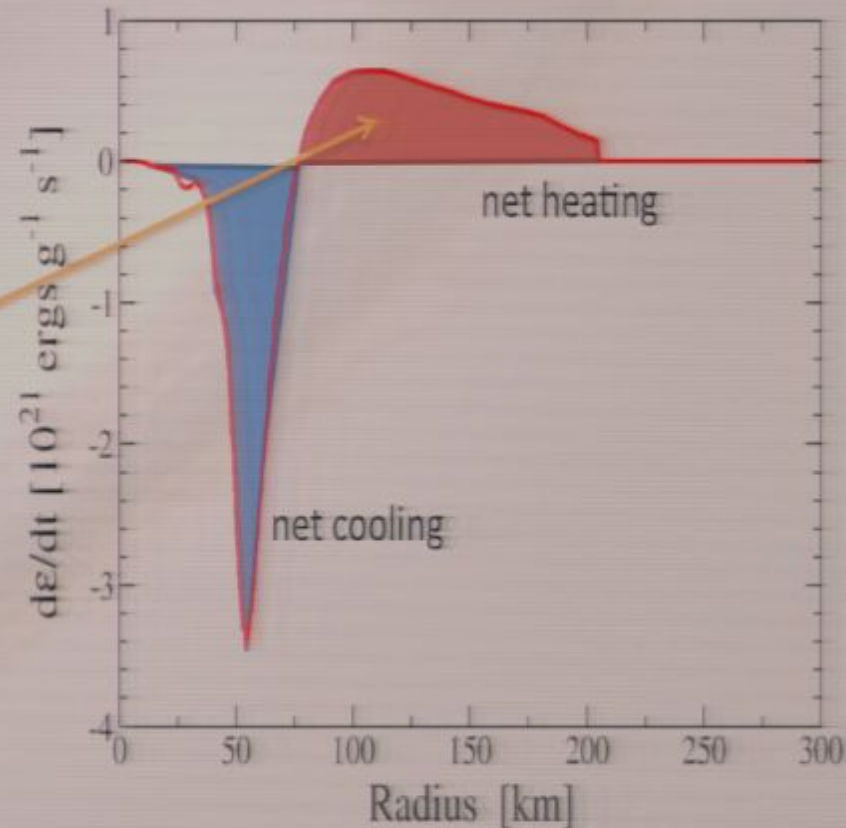
Livne, E. 1993, Burrows, A. et al. 2006

- Use 11.2 Msun progenitor from Woosley et al. 2002 and the Shen, H. et al. 1998 EOS
- Extract neutrino spectra at ν -sphere and run through dynamical neutrino evolution taking into account collective oscillations



Theory of Neutrino Heating

- Neutrinos diffusing from core have a net energy deposition in the postshock region, the so called 'gain region'
- The neutrino mechanism works by having sufficient heating in the gain region to reenergize the shock



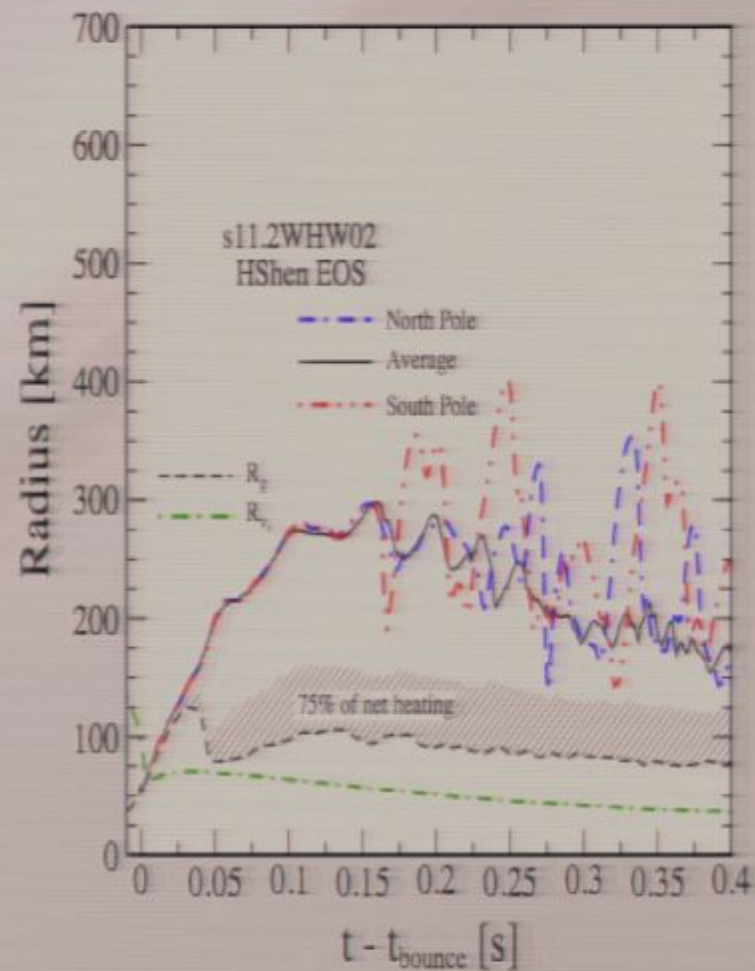
$$\mathcal{H} = \sum_{\nu_e, \bar{\nu}_e} \int_{r_g}^{r_s} dr 4\pi r^2 n_i \int_0^\infty d\epsilon \sigma_{\nu_i}(\epsilon) \frac{\epsilon d\Phi_{\nu_i}}{d\epsilon}$$

$$\sim \hat{\sigma} [\langle \epsilon_{\nu_e}^2 \rangle \mathcal{L}_{\nu_e} c_N + \langle \epsilon_{\bar{\nu}_e}^2 \rangle \mathcal{L}_{\bar{\nu}_e} c_P]$$

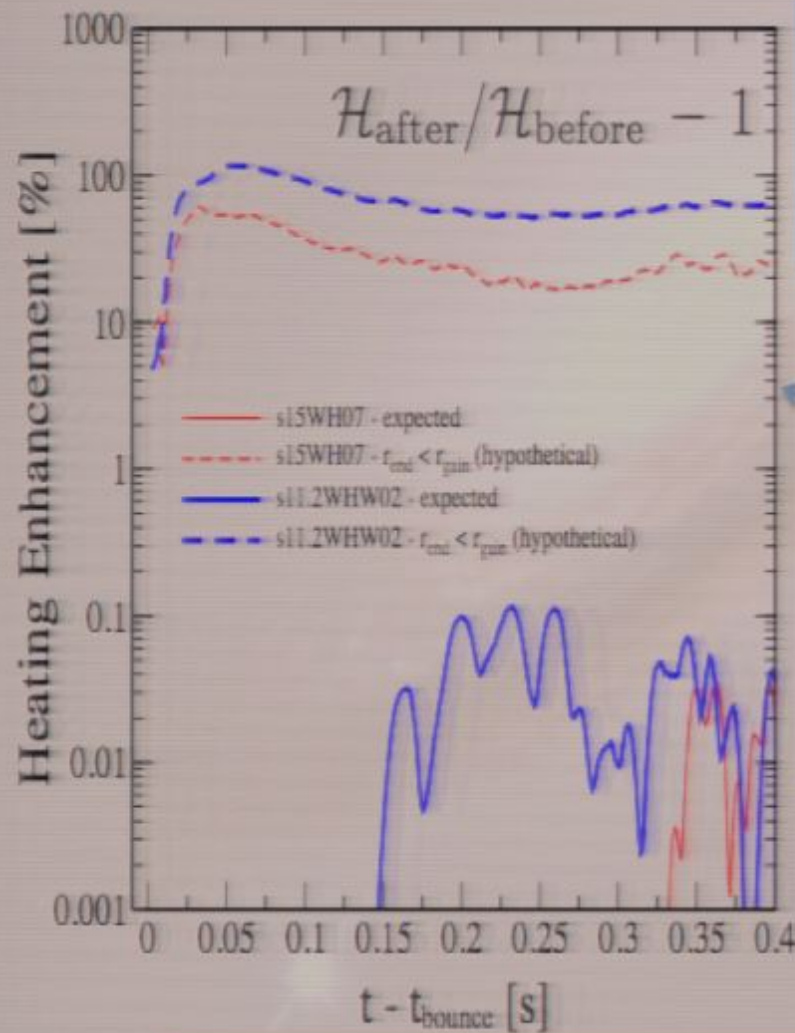
Exploratory simulations with VULCAN/2D

Livne, E. 1993, Burrows, A. et al. 2006

- Use 11.2 Msun progenitor from Woosley et al. 2002 and the Shen, H. et al. 1998 EOS
- Extract neutrino spectra at ν -sphere and run through dynamical neutrino evolution taking into account collective oscillations



Expected Heating Enhancement



$$\mathcal{H}_{\text{after}} \sim \mathcal{H}_{\text{before}} + \hat{\sigma} [\langle \epsilon_{\nu_e}^2 \rangle \mathcal{L}_{\nu_e}^{\text{ns}} - \langle \epsilon_{\nu_e}^2 \rangle \mathcal{L}_{\nu_e}^{\text{ns}}] c_N^O + \hat{\sigma} [\langle \epsilon_{\nu_e}^2 \rangle \mathcal{L}_{\nu_e}^{\text{ns}} - \langle \epsilon_{\nu_e}^2 \rangle \mathcal{L}_{\nu_e}^{\text{ns}}] c_P^O + \hat{\sigma} \langle \epsilon_{\nu_e}^2 \rangle^* [\langle \epsilon_{\nu_e} \rangle^* (\mathcal{N}_{\nu_e}^{\text{ns}} - \mathcal{N}_{\nu_e}^{\text{ns}})] c_N^O$$

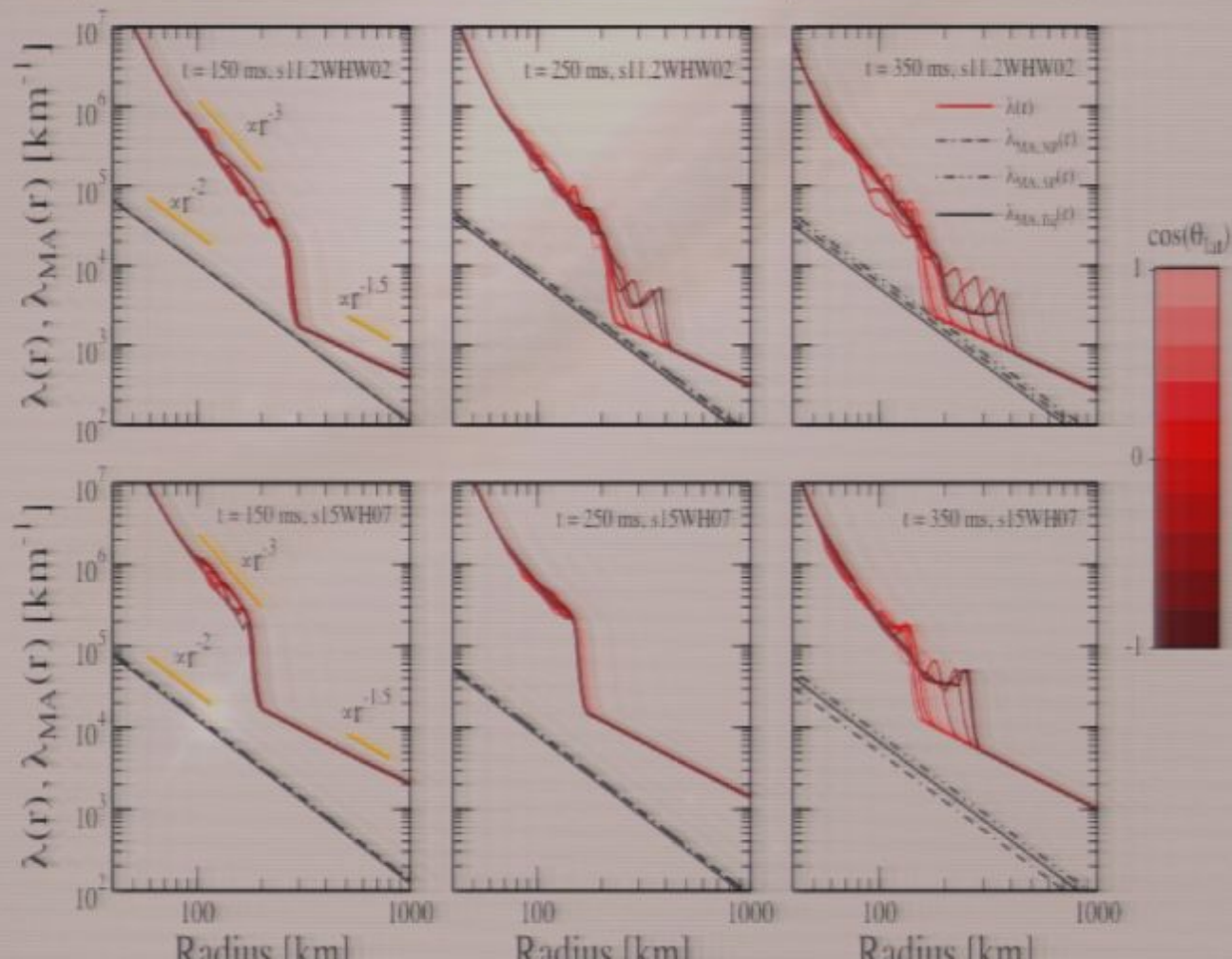
- Hypothetical situation where oscillations complete before gain radius
- Actual heating enhancement is much less, $< 1\%$

Take home message, collective neutrino oscillations do not help explode CCSNe

Multiangle suppression of Oscillations

(see also Chakraborty et al. 2011ab)

- In single angle approximation one can 'rotate' away the matter potential
- Recent development in multiangle collective neutrino oscillations leads to a suppression of oscillations until the electron density < neutrino density



Should we expect this to be relevant in improved models/EOS/codes/dimensions/neutrinos...?

- Models with higher accretion rates not only suppress SASI but lead to higher ν -sphere radii and neutrino densities. We chose low mass-range models for this reason (...O-Ne-Mg?)

$$r_{\text{sync}} \propto \sqrt{R_{\nu_e}} \left(\Phi_{\nu, \bar{\nu}} R_{\nu_e}^2 \right)^{1/4}$$

- Different EOS do not significantly change R_{ν} or Φ_{ν}
- 3D may lead to larger shock radii, however need to get oscillations deep down below gain radius to see significant effect – that's hard

Should we expect this to be relevant in improved models/EOS/codes/dimensions/neutrinos...?

Note: here neutrino evolution means the collect oscillation evolution

- Results here in single-angle approximation, multiangle may lead to larger swap radii:
 - multiangle matter effects (Chakraborty et al. 2011)
 - multiangle treatment of neutrino evolution
- If $\Phi_{\nu_e} \sim \Phi_{\bar{\nu}_e}$ then multiangle decoherence, spectra equilibrate
- Full Boltzmann treatment of neutrino oscillations (lingering matter effects)
- Some as-of-yet unknown collective neutrino physics
- Collective neutrino Oscillations still will influence observed signal

Should we expect this to be relevant in improved models/EOS/codes/dimensions/neutrinos...?

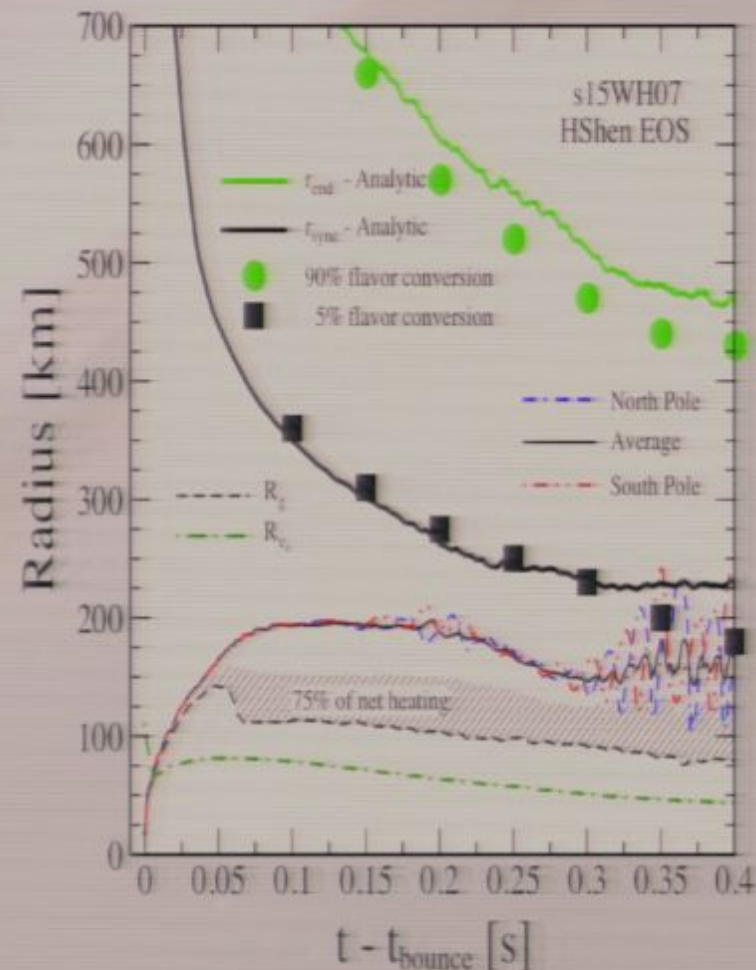
Note: here neutrino evolution means the collect oscillation evolution

- Results here in single-angle approximation, multiangle may lead to larger swap radii:
 - multiangle matter effects (Chakraborty et al. 2011)
 - multiangle treatment of neutrino evolution
- If $\Phi_{\nu_e} \sim \Phi_{\bar{\nu}_e}$ then multiangle decoherence, spectra equilibrate
- Full Boltzmann treatment of neutrino oscillations (lingering matter effects)
- Some as-of-yet unknown collective neutrino physics
- Collective neutrino Oscillations still will influence observed signal

Exploratory simulations with VULCAN/2D

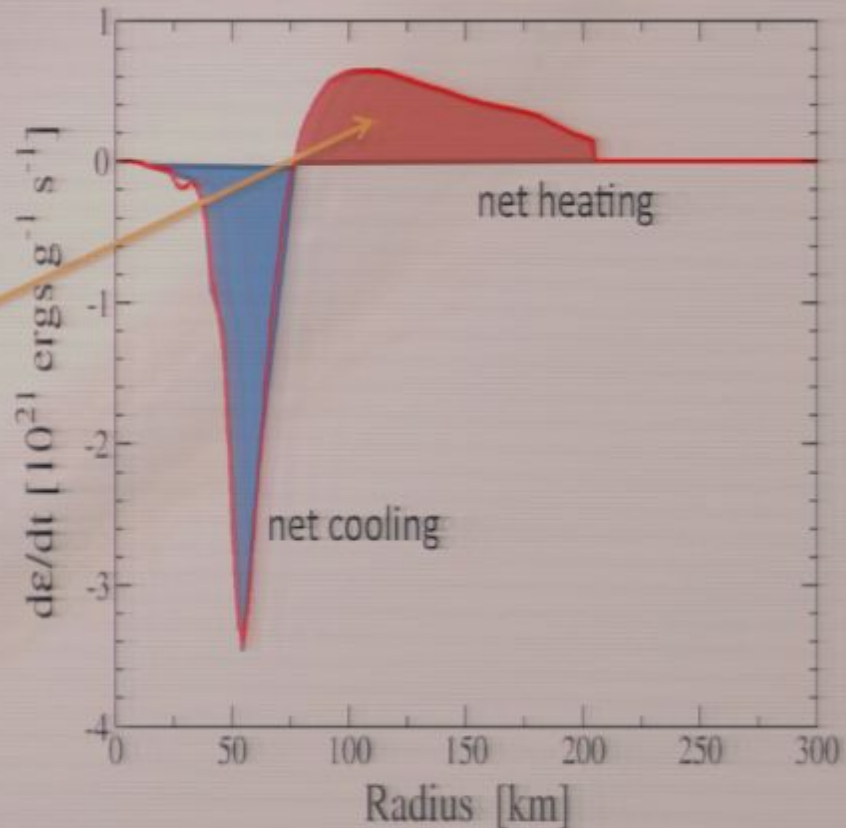
Livne, E. 1993, Burrows, A. et al. 2006

- Use 15 Msun progenitor from Woosley et al. 2007 and the Shen, H. et al. 1998 EOS
- Higher accretion rates suppress SASI and keep shock at lower radii
- Neutrino oscillations occur at roughly same location as 11.2 model, little affect on heating



Theory of Neutrino Heating

- Neutrinos diffusing from core have a net energy deposition in the postshock region, the so called 'gain region'
- The neutrino mechanism works by having sufficient heating in the gain region to reenergize the shock

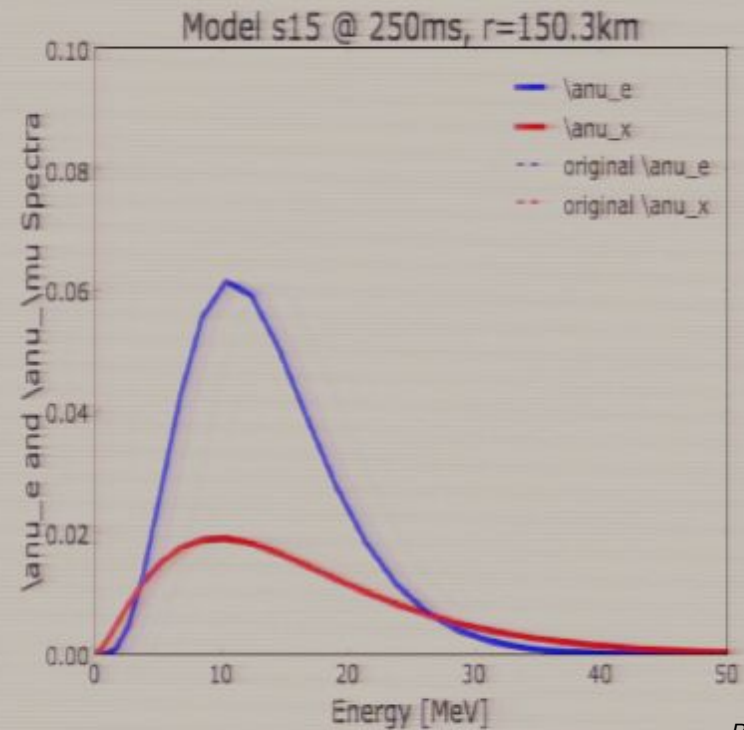
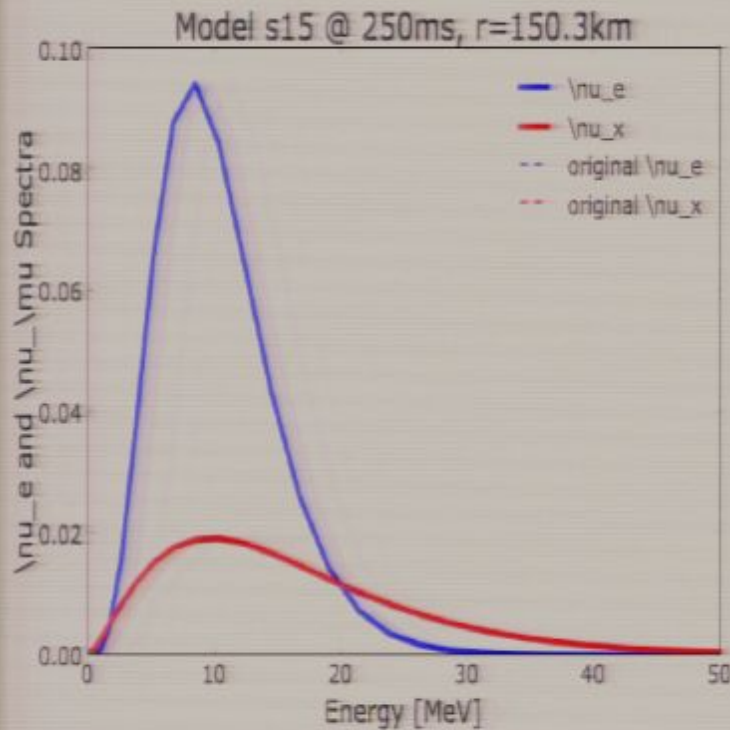


$$\mathcal{H} = \sum_{\nu_e, \bar{\nu}_e} \int_{r_g}^{r_s} dr 4\pi r^2 n_i \int_0^{\infty} d\epsilon \sigma_{\nu_i}(\epsilon) \frac{\epsilon d\Phi_{\nu_i}}{d\epsilon}$$

$$\sim \hat{\sigma} [\langle \epsilon_{\nu}^2 \rangle \mathcal{L}_{\nu} c_N + \langle \epsilon_{\bar{\nu}}^2 \rangle \mathcal{L}_{\bar{\nu}} c_P]$$

Neutrino Evolution

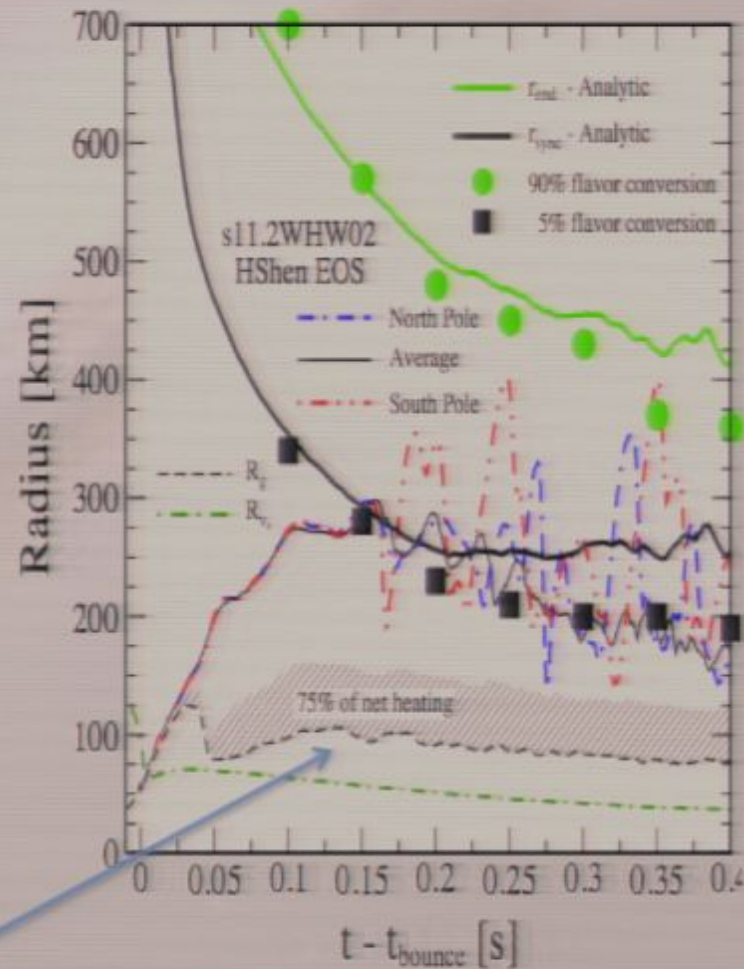
- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail

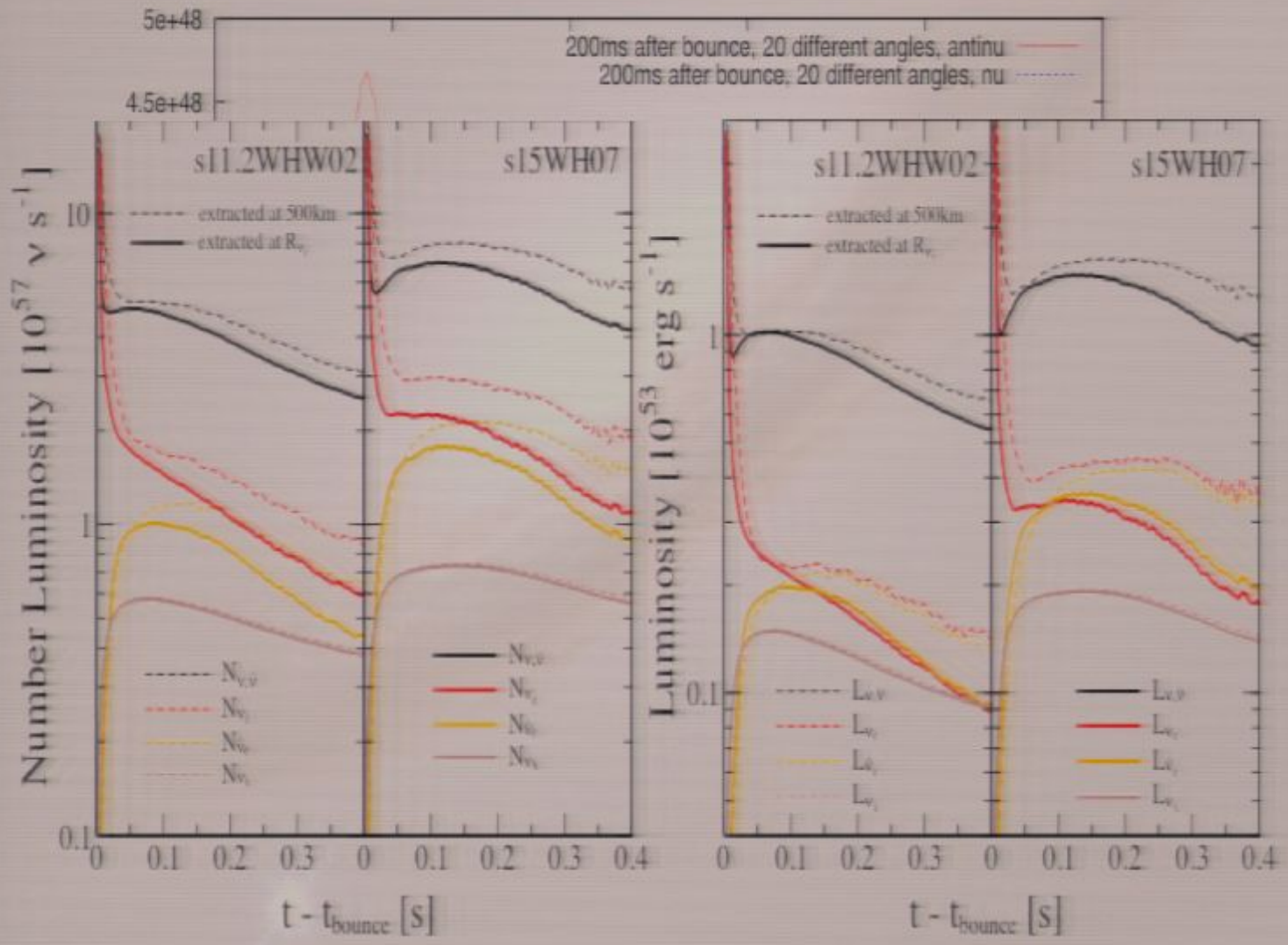


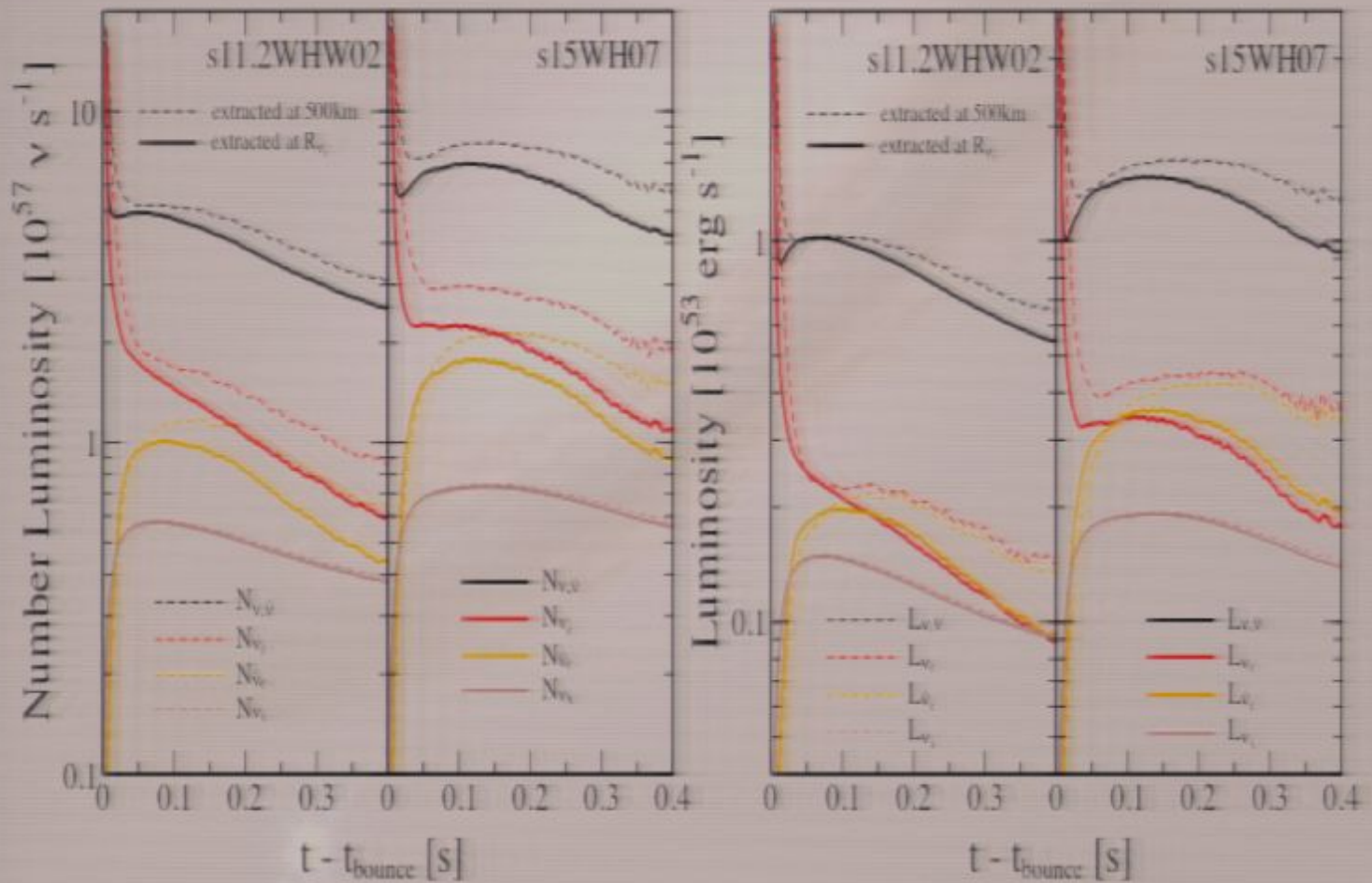
Exploratory simulations with VULCAN/2D

Livne, E. 1993, Burrows, A. et al. 2006

- Oscillation radii are large due to high neutrino luminosities and large neutrinosphere radii
- Even though oscillations being inside shock, not complete until well outside.
- Significant heating will occur only if oscillations occur before gain radius







Neutrino Evolution

- As an example of oscillations, here is a movie showing the evolution of the ν spectra from the ν -sphere out in radius
- Will describe simulations in more detail

