

Title: Recipes to energize core-collapse supernova explosions

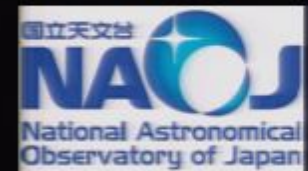
Date: Jun 21, 2011 11:00 AM

URL: <http://pirsa.org/11060021>

Abstract: Recent multidimensional supernova simulations seem to support an assumption that the neutrino-driven mechanism might work to blow up massive stars. However the explosion energies obtained in those simulations are usually not enough to account for the canonical explosion energy of 10^{51} ergs. In this contribution we'd like to address whether some new physical elements so far ignored in the supernova simulations would or would not have an impact on the neutrino-heating mechanism such as the effects of neutrino self-interactions nuclear burning and the turbulent heating due to the magneto-rotational instability. These effects are included in our 2D simulations with the spectral neutrino transport (Suwa et al. (2010)). In addition we will report our 3D results based on the 3D version of the code and discuss their potential impacts on the explosion mechanism. Based on these results we will compute the gravitational radiation and neutrino emission and then discuss some prospects towards multi-messenger astronomy of supernova explosions.

What do we have as a microphysical tool to solve the long-standing supernova puzzle ?

“Several toolkits in our group (NAOJ)”



✓ Leakage and light-bulb scheme

✓ Energy-integrated M1 scheme (in progress)

✓ IDSA scheme (developed by M.Liebendoerfer (2009))

✓ General relativistic ray-tracing scheme

Equations of State (EOSs): (Lattimer & Swesty (1991), Shen et al.(98))

✓ Lattimer-Swesty (Kx3) and H-Shen

What do we have as a microphysical tool to solve the long-standing supernova puzzle ?

“Several toolkits in our group (NAOJ)”



✓ Leakage and light-bulb scheme

✓ Energy-integrated M1 scheme (in progress)

✓ IDSA scheme (developed by M.Liebendoerfer (2009))

✓ General relativistic ray-tracing scheme

Equations of State (EOSs): (Lattimer & Swesty (1991), Shen et al.(98))

✓ Lattimer-Swesty (Kx3) and H-Shen

“Several lessons” (we have recently learned) in ever-lasting , day&night (unhealthy!), trial & error debugging to implement “*microphysics*” in our supernova code.

The first topic is about the **IDSA scheme**

(Liebendoerfer et al. (2009))

Pros: can reproduce the 1D Boltzmann results

: can save computational time (100 faster) than Boltzmann solvers
(good for the 1st generation 3D simulations!)

Cons: heavy lepton neutrinos :not yet included.

- should affect the post-bounce dynamics.

The first topic is about the **IDSA scheme**

(Liebendoerfer et al. (2009))

Pros: can reproduce the 1D Boltzmann results

: can save computational time (100 faster) than Boltzmann solvers
(good for the 1st generation 3D simulations!)

Cons: heavy lepton neutrinos :not yet included.

- should affect the post-bounce dynamics.

- ✓ The best way : implement them in the IDSA,
but not yet done (ultimate goal: Ott et al.(08), Sumiyoshi+(11))
- ✓ We treat cooling via ν_X by the following three schemes,
either by **leakage**, **FLD**, or **M1-closure scheme**.

The M1-based neutrino transport scheme for SN simulations

$$\partial_t E_\nu + \nabla F_\nu = Q_\nu^0 \quad (0^{\text{th}}\text{-order moment equation})$$

$$\partial_t F_\nu + \nabla P_\nu = Q_\nu^1 \quad (1^{\text{st}}\text{-order moment equation})$$

Obergaulinger and Janka (2010)

✓ In the M1-closure scheme, one solves up to the 1st-order moment of the Boltzmann equation

$P_\nu = P_\nu(E_\nu, F_\nu)$ For closing the hierarchy, one assumes the following relations

$$P_\nu^{jj} = \left(\frac{1 - p_\nu}{2} \delta^{jj} + \frac{3p_\nu - 1}{2} \frac{F_\nu^i F_\nu^j}{F_\nu^2} \right) E_\nu \quad (\text{Audit et al. 2002})$$

Eddington factor

$$p_\nu = \frac{1}{3} + \frac{1}{15} (6f_\nu^2 - 2f_\nu^3 + 6f_\nu^4)$$

Flux factor

$$f_\nu = F_\nu / cE_\nu$$

The M1-based neutrino transport scheme for SN simulations

$$\partial_t E_\nu + \nabla F_\nu = Q_\nu^0 \quad (0^{\text{th}}\text{-order moment equation})$$

$$\partial_t F_\nu + \nabla P_\nu = Q_\nu^1 \quad (1^{\text{st}}\text{-order moment equation})$$

Obergaulinger and Janka (2010)

✓ In the M1-closure scheme, one solves up to the 1st-order moment of the B eq

$P_\nu = P_\nu(E_\nu, F_\nu)$ For closing the hierarchy, one assumes the following relations

$$P_\nu^{jj} = \left(\frac{1 - p_\nu}{2} \delta^{jj} + \frac{3p_\nu - 1}{2} \frac{F_\nu^i F_\nu^j}{F_\nu^2} \right) E_\nu \quad (\text{Audit et al. 2002})$$

Eddington factor

$$p_\nu = \frac{1}{3} + \frac{1}{15} (6f_\nu^2 - 2f_\nu^3 + 6f_\nu^4)$$

Flux factor

$$f_\nu = F_\nu / cE_\nu$$

☆ Taking the diffusion limit, $f_\nu \rightarrow 0$

$$p_\nu \rightarrow 1/3, P_\nu \rightarrow 1/3 E_\nu$$

The M1-based neutrino transport scheme for SN simulations

$$\partial_t E_\nu + \nabla F_\nu = Q_\nu^0 \quad (0^{\text{th}}\text{-order moment equation})$$

$$\partial_t F_\nu + \nabla P_\nu = Q_\nu^1 \quad (1^{\text{st}}\text{-order moment equation})$$

Obergaulinger and Janka (2010)

✓ In the M1-closure scheme, one solves up to the 1st-order moment of the Boltzmann equation

$P_\nu = P_\nu(E_\nu, F_\nu)$ For closing the hierarchy, one assumes the following relations

$$P_\nu^{jj} = \left(\frac{1 - p_\nu}{2} \delta^{ij} + \frac{3p_\nu - 1}{2} \frac{F_\nu^i F_\nu^j}{F_\nu^2} \right) E_\nu \quad (\text{Audit et al. 2002})$$

Eddington factor

$$p_\nu = \frac{1}{3} + \frac{1}{15} (6f_\nu^2 - 2f_\nu^3 + 6f_\nu^4)$$

Flux factor

$$f_\nu = F_\nu / cE_\nu$$

☆ Taking the diffusion limit, $f_\nu \rightarrow 0$

$$p_\nu \rightarrow 1/3, P_\nu \rightarrow 1/3 E_\nu$$

☆ streaming limit, $f_\nu \rightarrow 1$

$$p_\nu \rightarrow 1, P_\nu \rightarrow E_\nu$$

The M1-based neutrino transport scheme for SN simulations

$$\partial_t E_\nu + \nabla F_\nu = Q_\nu^0 \quad (0^{\text{th}}\text{-order moment equation})$$

$$\partial_t F_\nu + \nabla P_\nu = Q_\nu^1 \quad (1^{\text{st}}\text{-order moment equation})$$

Obergaulinger and Janka (2010)

✓ In the M1-closure scheme, one solves up to the 1st-order moment of the Boltzmann equation

$P_\nu = P_\nu(E_\nu, F_\nu)$ For closing the hierarchy, one assumes the following relations

$$P_\nu^{jj} = \left(\frac{1 - p_\nu}{2} \delta^{jj} + \frac{3p_\nu - 1}{2} \frac{F_\nu^i F_\nu^j}{F_\nu^2} \right) E_\nu \quad (\text{Audit et al. 2002})$$

Eddington factor

$$p_\nu = \frac{1}{3} + \frac{1}{15} (6f_\nu^2 - 2f_\nu^3 + 6f_\nu^4)$$

Flux factor

$$f_\nu = F_\nu / cE_\nu$$

☆ Taking the diffusion limit, $f_\nu \rightarrow 0$

☆ streaming limit, $f_\nu \rightarrow 1$

$$p_\nu \rightarrow 1/3, P_\nu \rightarrow 1/3 E_\nu$$

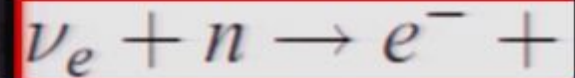
$$p_\nu \rightarrow 1, P_\nu \rightarrow E_\nu$$

✓ Like the FLD scheme, the M1 scheme bridges the two limits.

✓ This scheme may be better than FLD, because it can be used in GR simulations.

Two steps in evolving the radiation variables of E_{ν} , F_{ν}

electron-type neutrino absorption on neutrons



$$\begin{aligned} \left(\frac{\partial E_\nu}{\partial t}\right) &= \frac{c}{(2\pi\hbar c)^3} \int \omega^3 d\omega j(\omega)(1 - f(\omega, \mu, T)) - f(\omega, \mu, T) / \lambda^{(a)}(\omega) \\ &= \frac{c}{(2\pi\hbar c)^3} \int \omega^3 d\omega j(\omega) - \left(j(\omega) + 1/\lambda^{(a)}\right) f(\omega, \mu, T) \\ &= \frac{c}{(2\pi\hbar c)^3} \int \omega^3 d\omega j(\omega) - j(\omega) \left(1 + \exp\left(\frac{\omega - \mu_0}{kT}\right)\right) f(\omega, \nu, T) \\ &= \frac{c}{(2\pi\hbar c)^3} \int \omega^3 d\omega j(\omega) - j(\omega) / f_{\text{FD}}(\omega, \mu_0, T) f(\omega, \mu, T) \\ &\sim J_\beta E_e - K_\beta E_\nu \end{aligned}$$

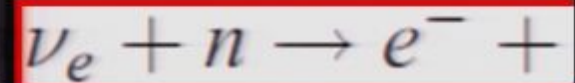
$$f(\omega, \mu) = f_{\text{FD}}(\omega) (1 + 3f_{\text{rad}}\mu)$$

$$\begin{aligned} \left(\frac{\partial F_\nu}{\partial t}\right) &= \frac{1}{2(2\pi\hbar c)^3} \int \mu d\mu \int \omega^3 d\omega j(\omega)(1 - f(\omega, \mu)) - f(\omega, \mu) / \lambda^{(a)}(\omega) \\ &= \frac{1}{2(2\pi\hbar c)^3} \int \mu d\mu \int \omega^3 d\omega - \left(j(\omega) + 1/\lambda^{(a)}\right) 3\mu f_{\text{rad}} f(\omega, \mu, T) \\ &= \frac{1}{(2\pi\hbar c)^3} \int \omega^3 d\omega - j(\omega) / f(\omega, \mu_0, T) f_{\text{rad}} f(\omega, \mu, T) \\ &= -K_\beta F_\nu \end{aligned}$$

✓ In computing the neutrino-matter coupling (r.h.s. of the B eqns) important to write them in a form that is proportional to $\Gamma_{\nu e} \Gamma_{\nu n}$

Two steps in evolving the radiation variables of E_{ν} , F_{ν}

electron-type neutrino absorption on neutrons



$$\left(\frac{\partial E_\nu}{\partial t}\right) = \frac{c}{(2\pi\hbar c)^3} \int \omega^3 d\omega j(\omega)(1 - f(\omega, \mu, T)) - f(\omega, \mu, T) / \lambda^{(a)}(\omega)$$

$$f(\omega, \mu) = f_{\text{FD}}(\omega) (1 + 3f_{\text{grad}}\mu)$$

$$= \frac{c}{(2\pi\hbar c)^3} \int \omega^3 d\omega j(\omega) (j(\omega) + 1 / \lambda^{(a)}(\omega)) f(\omega, \mu, T)$$

The second step is "advection" by the characteristic speed, which can be straightforwardly done.

$$\sim J_t$$

$$\partial_t E + \partial_x F^{\hat{x}} = 0$$

$$\partial_t F^{\hat{x}} + \partial_x \left(\frac{1-\chi}{2} E + \frac{3\chi-1}{2} F^{\hat{x}} F^{\hat{x}} / E \right) = 0$$

$$\left(\frac{\partial F_\nu}{\partial t}\right) = \frac{1}{2} \left(\partial_t E + \partial_x F^{\hat{x}} \right)$$

$$= \frac{1}{2} \left(\partial_t E + \partial_x F^{\hat{x}} \right)$$

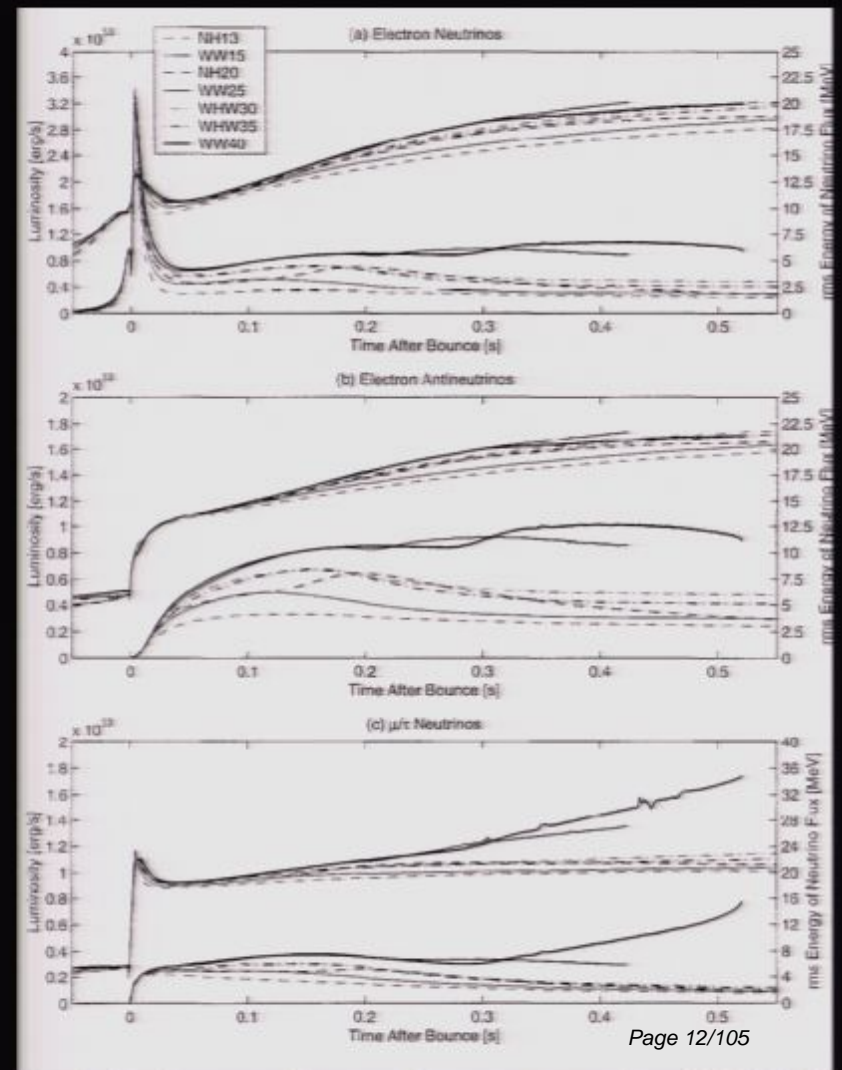
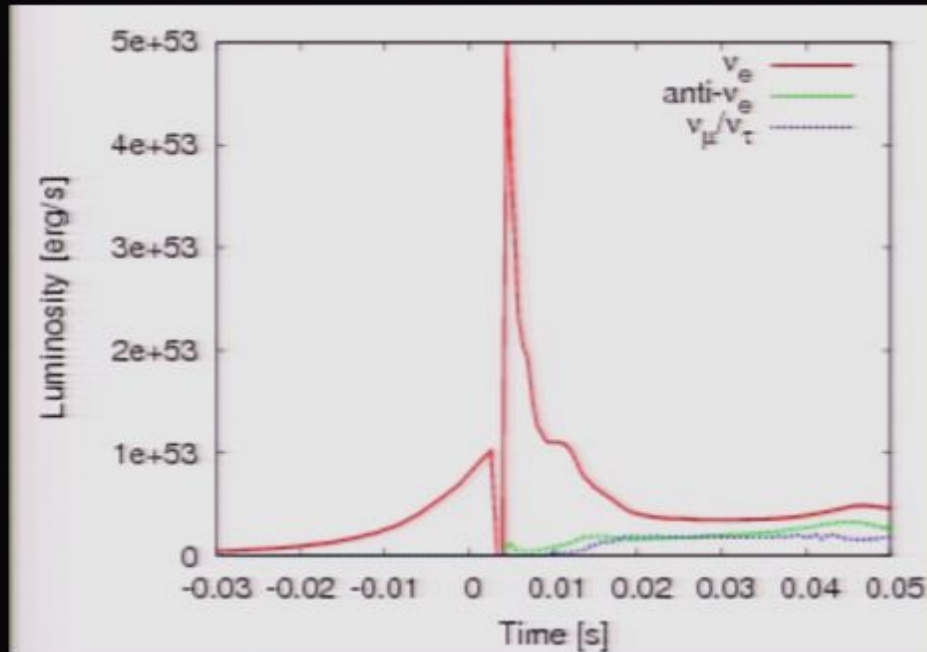
$$\partial_t \begin{pmatrix} E \\ F^{\hat{x}} \end{pmatrix} + \begin{pmatrix} 0 & 1 \\ \frac{1-\chi}{2} - \frac{3\chi-1}{2} \frac{F^{\hat{x}2}}{E^2} & \frac{3\chi-1}{2} 2 \frac{F^{\hat{x}}}{E} \end{pmatrix} \partial_x \begin{pmatrix} E \\ F^{\hat{x}} \end{pmatrix} = 0$$

$$= -K_\beta F_\nu$$

✓ In computing the neutrino-matter coupling (r.h.s. of the B eqns) important to write them in a form that is proportional to $\Gamma_{\nu} \Gamma_{\nu}$

Neutrino luminosities in M1

1D Boltzmann results



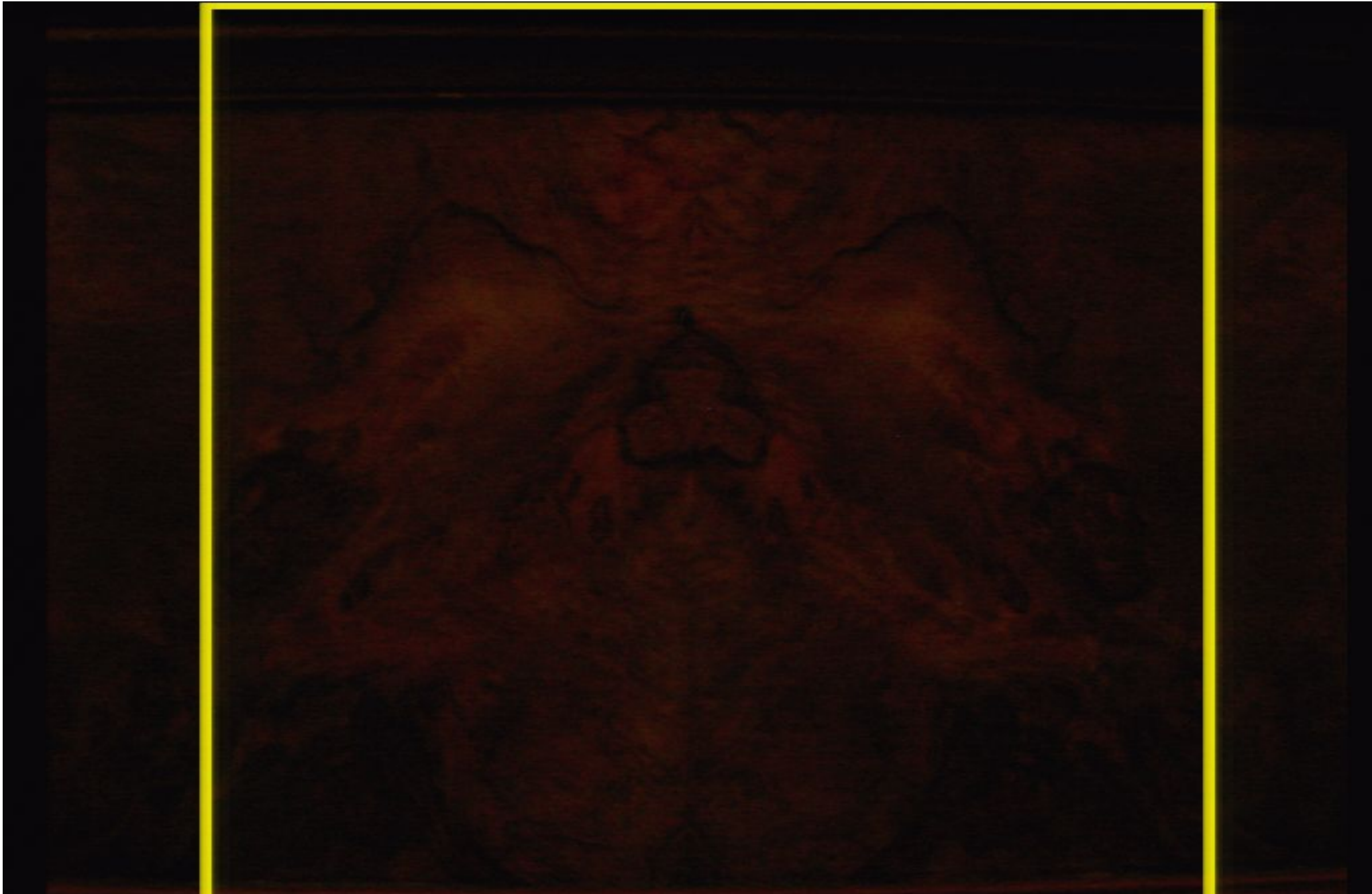
- ✓ The M1 scheme: Overall trends in agreement with the Boltzmann results.
- ✓ More detailed comparison will be given in our forthcoming paper(in progress).



My bed in the Waterloo hotel



My bed in the Waterloo hotel





My bed in the Waterloo hotel



3D Results with IDSA+

(Takiwaki, KK, Suwa in prep)

Preliminary

- ✓ 11.2 Ms progenitor (Woosley, Heger, Weaver '02)
- ✓ Numerical Resolution
 - Grid: 300(r)x32(Θ)x64(φ) × 20(energy)
 - Non-rotating case
 - ✓ **IDSA+ means IDSA for $\nu_e + \bar{\nu}_e$ bar leakage for ν_X**

3D Results with IDSA +

t = 0001ms

(Takiwaki, KK, Suwa in prep)

- ✓ 11.2 Ms progenitor (Woosley, Heger, Weaver '02)
- ✓ Numerical Resolution
 - Grid: 300(r)x32(Θ)x64(φ) × 20(energy)
 - Non-rotating case
 - ✓ **IDSA+ means IDSA for $\nu_e + \bar{\nu}_e$ bar leakage for ν_X**

Preliminary

3D Re

t= 0006 ms

- ✓ 11.2 M
- ✓ Num
- C
- N
- ✓

ary



3D Re

t= 0048 ms

✓ 11.2 M

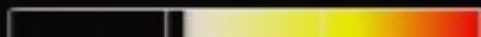
✓ Num

• C

• N

✓

ary



3D Re

t= 0050 ms

✓ 11.2 M

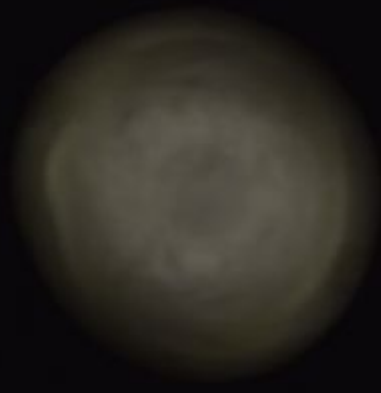
✓ Num

• C

• N

✓

ary

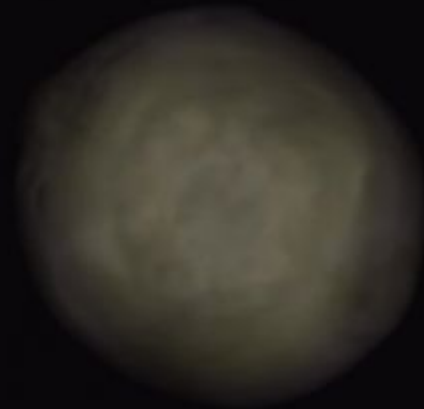


3D Re

t= 0082 ms

- ✓ 11.2 M
- ✓ Num
- C
- N
- ✓

ary



3D Re

t= 0093 ms

✓ 11.2 M

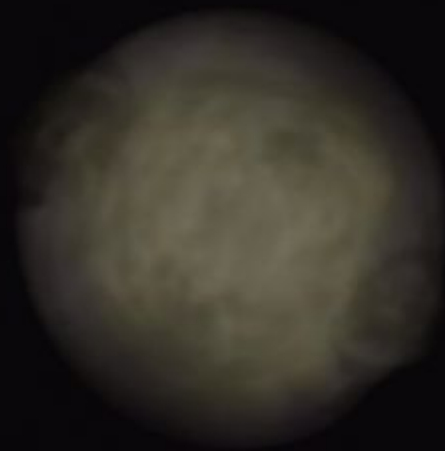
✓ Num

• C

• N



ary

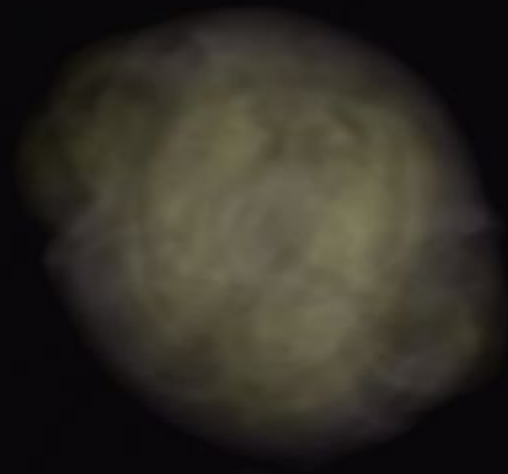


3D Re

t= 0108 ms

- ✓ 11.2M
- ✓ Num
- C
- N
- ✓

ary

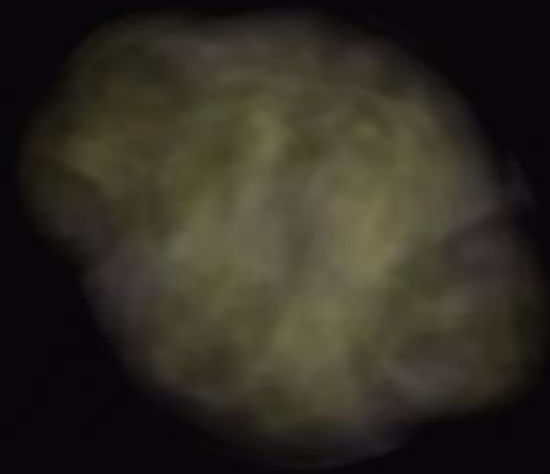


3D Re

t= 0117 ms

- ✓ 11.2 M
- ✓ Num
- C
- N
- ✓

ary



3D Re

t= 0120 ms

✓ 11.2 M

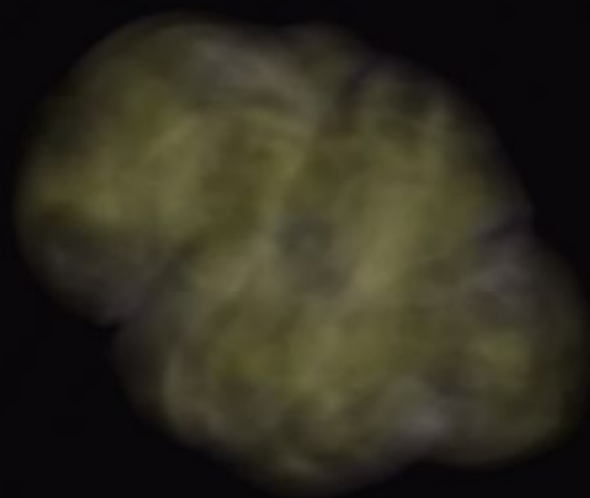
✓ Num

• C

• N

✓

ary



3D Re

t= 0138 ms

✓ 11.2M

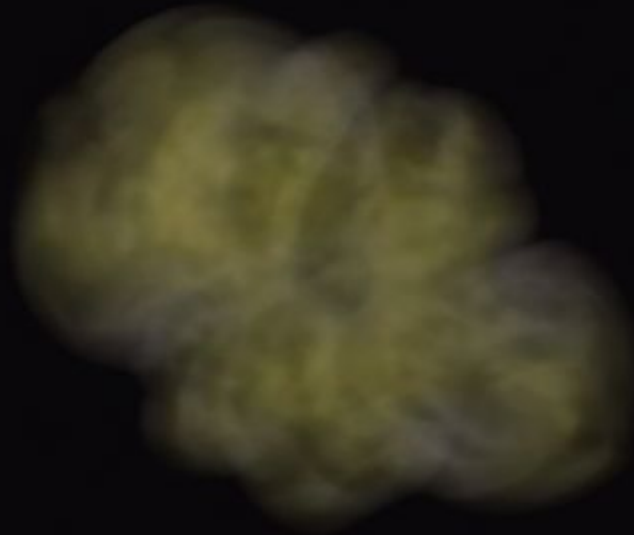
✓ Num

•C

•N

✓

ary



3D Re

t= 0166 ms

✓ 11.2 M

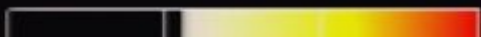
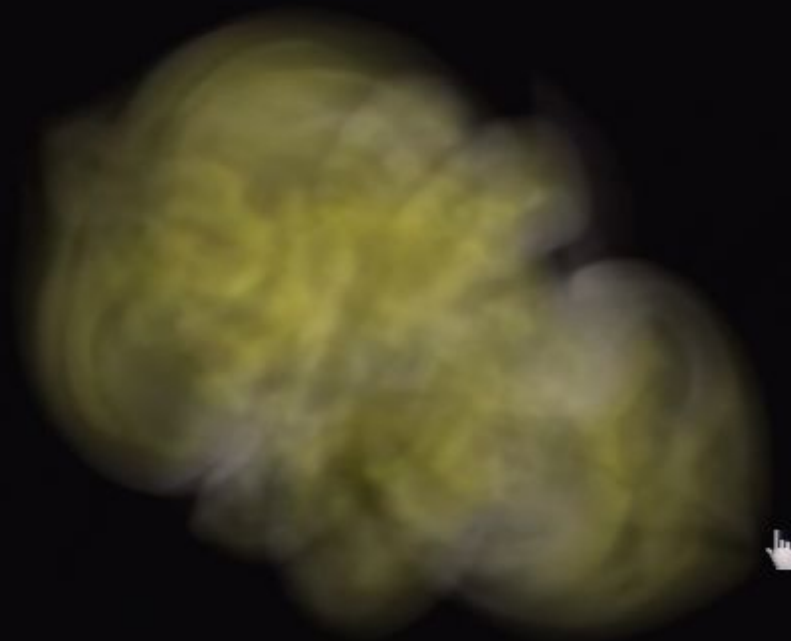
✓ Num

• C

• N

✓

ary

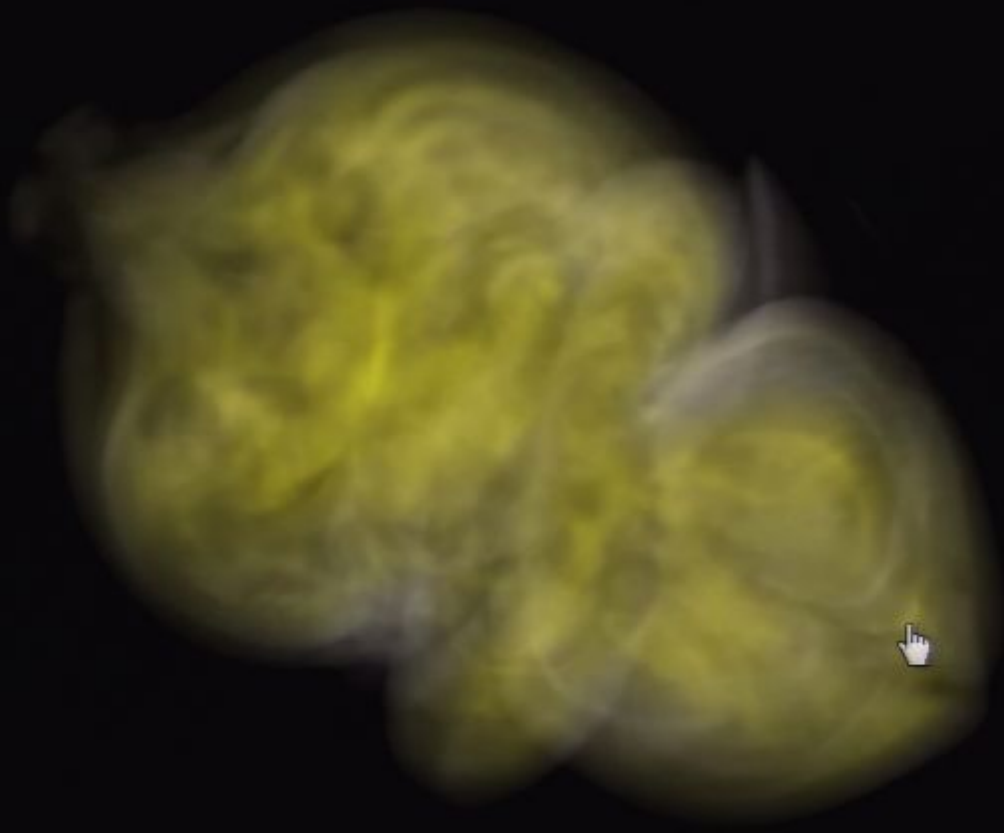


3D Re

t= 0193 ms

- ✓ 11.2M
- ✓ Num
- C
- N
- ✓

ary

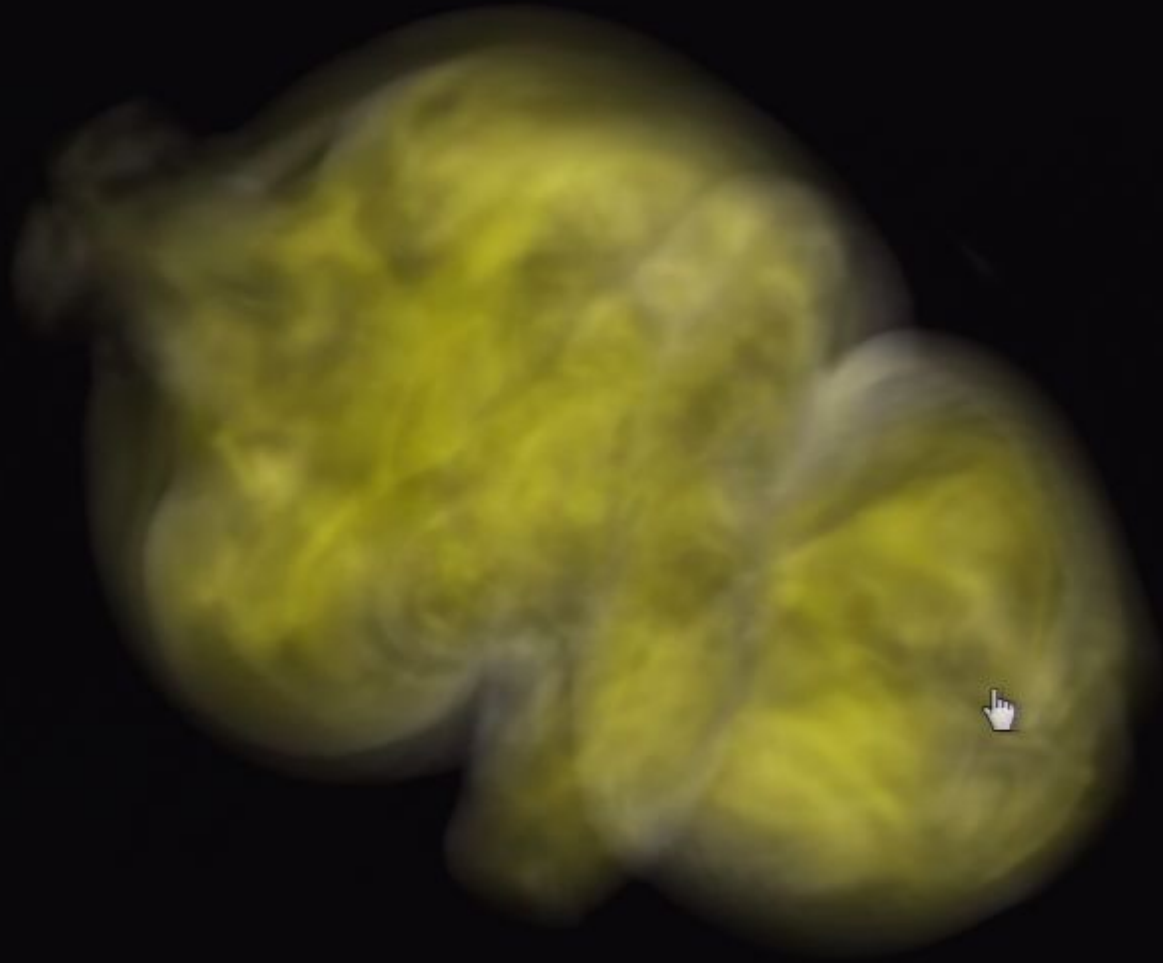


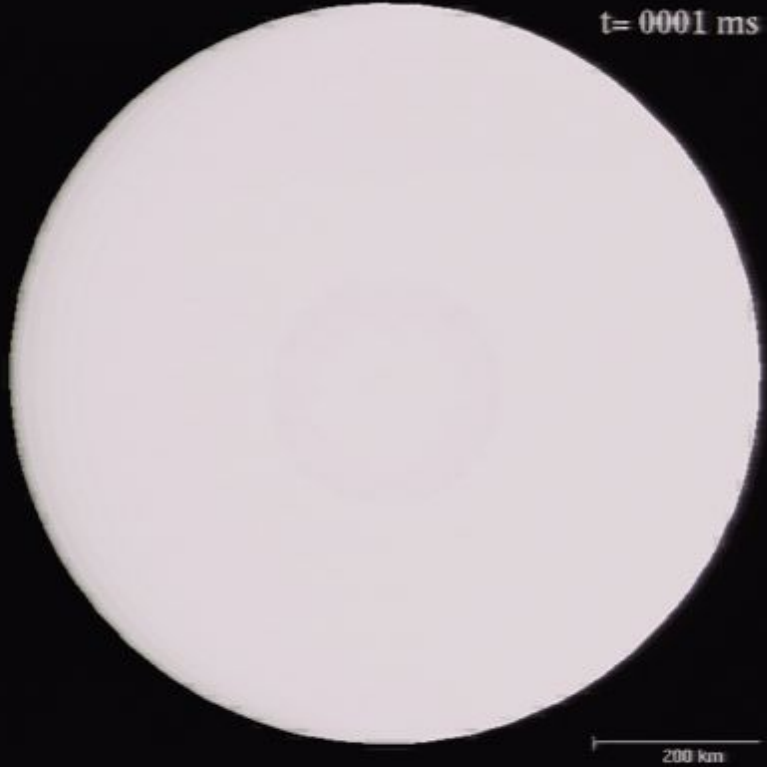
3D Re

t= 0208 ms

- ✓ 11.2M
- ✓ Num
- C
- N
- ✓

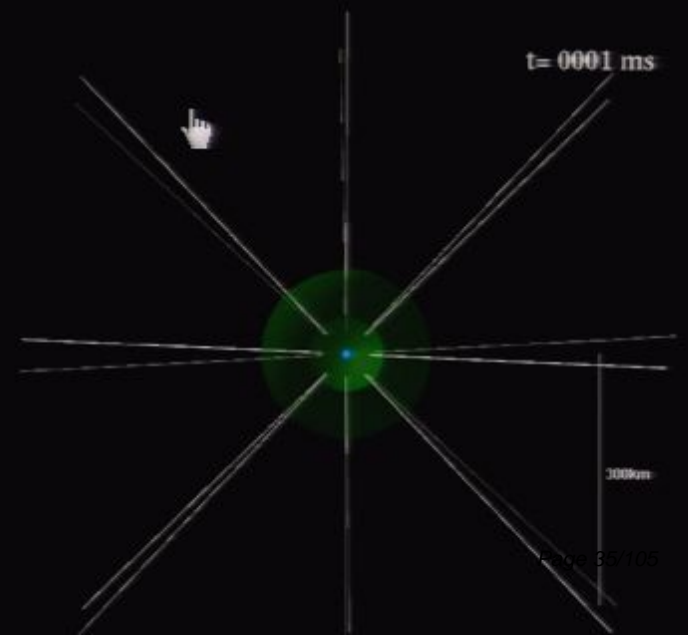
ary

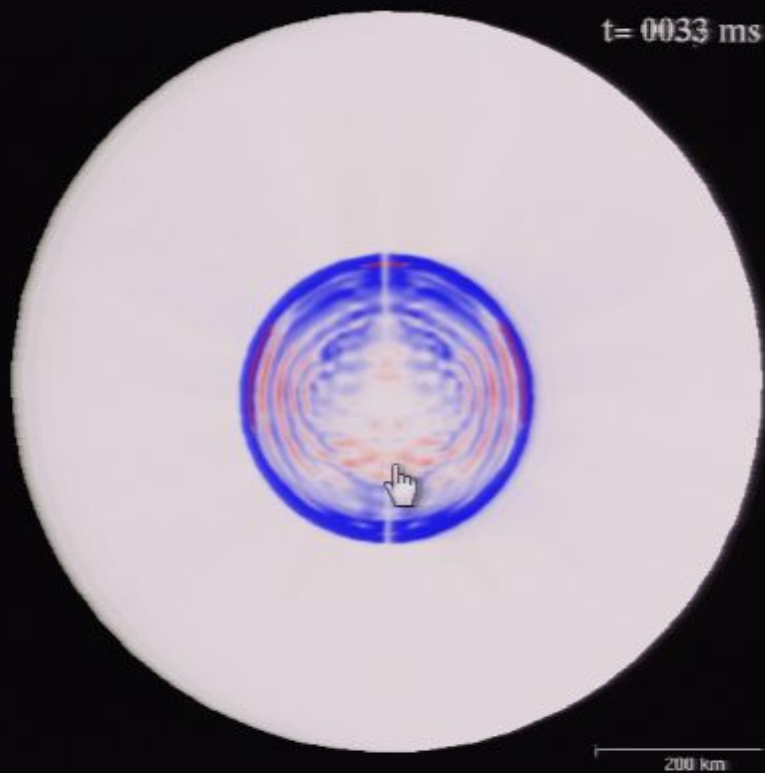




Pressure perturbation for equatorial observer ($\delta P/P$)

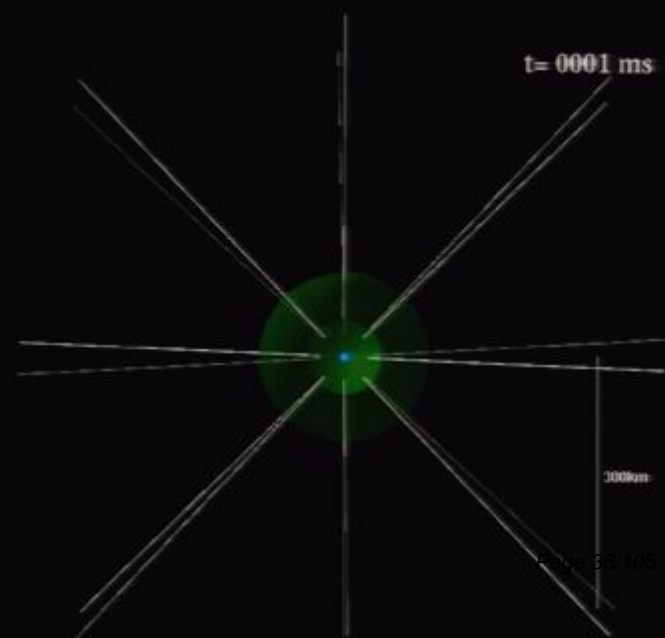
Sketch of streamline for polar observer

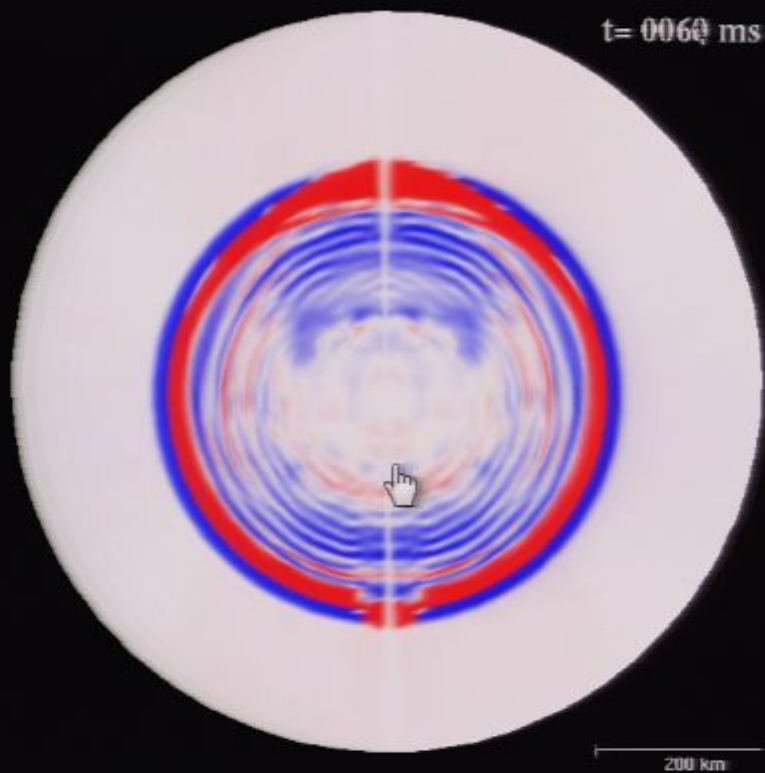




Pressure perturbation for equatorial observer ($\delta P/P$)

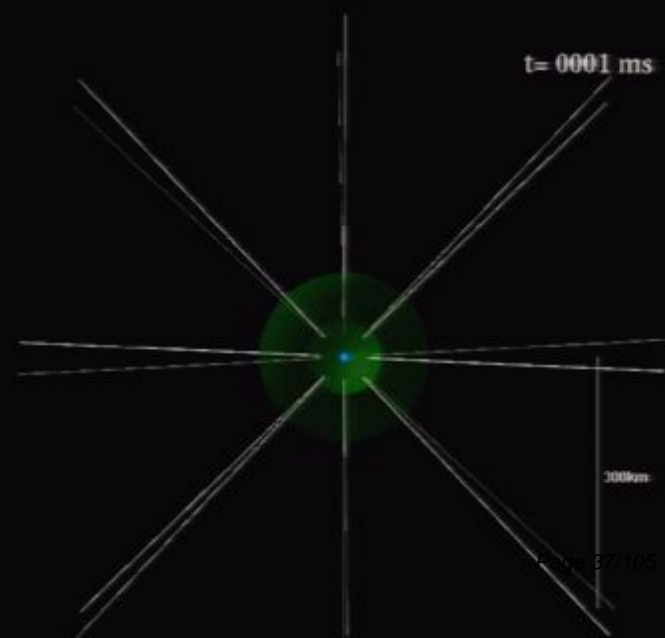
Sketch of streamline for polar observer

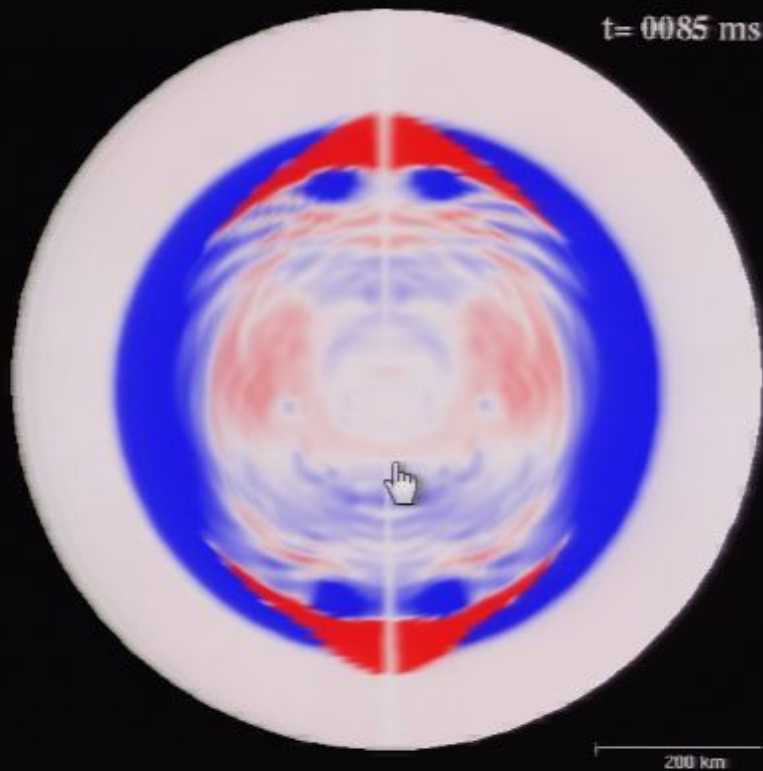




Pressure perturbation for equatorial observer ($\delta P/P$)

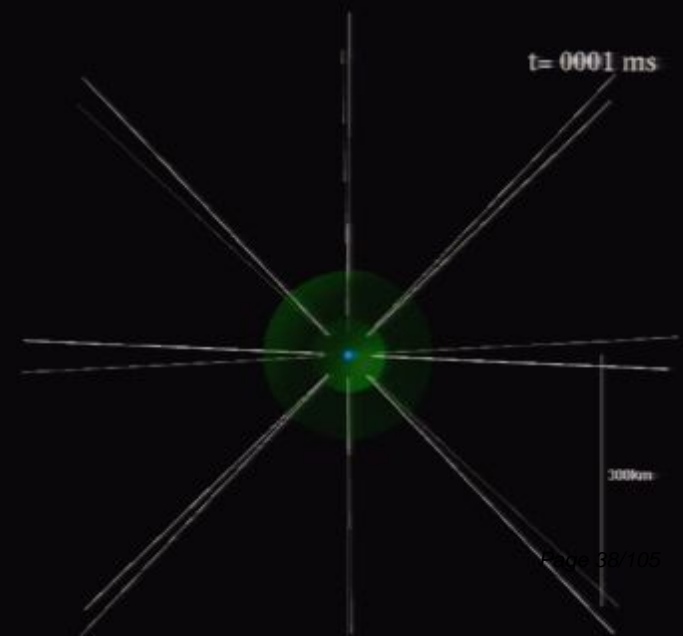
Sketch of streamline for polar observer

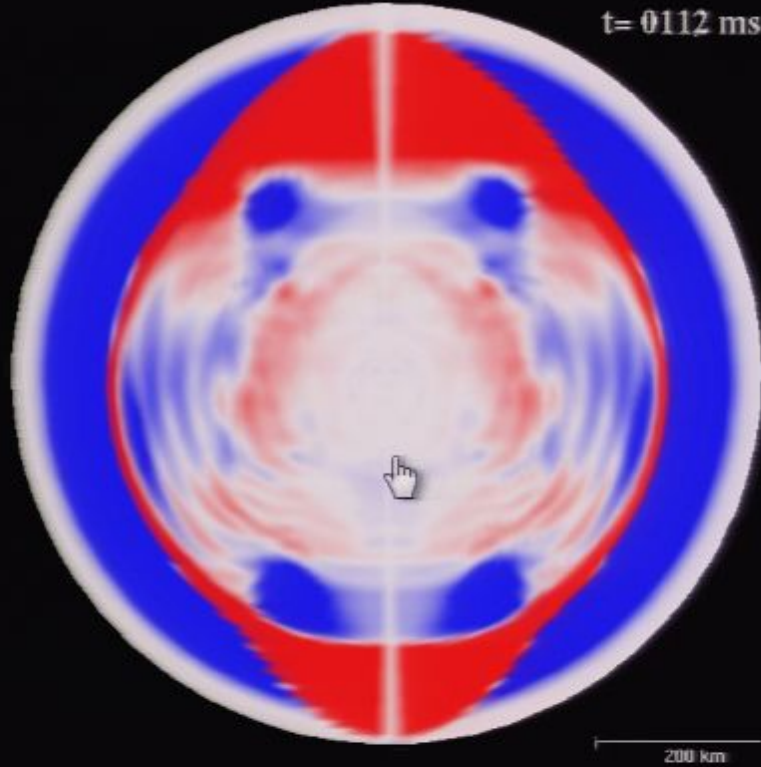




Pressure perturbation for equatorial observer ($\delta P/P$)

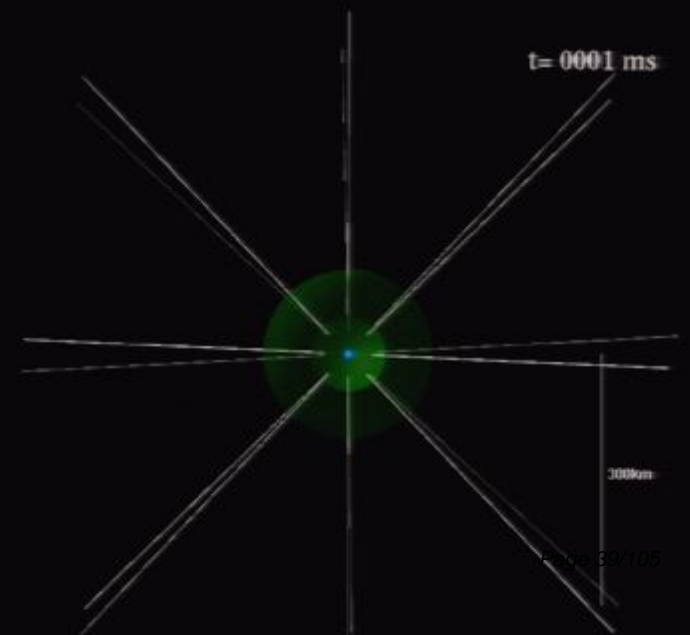
Sketch of streamline for polar observer

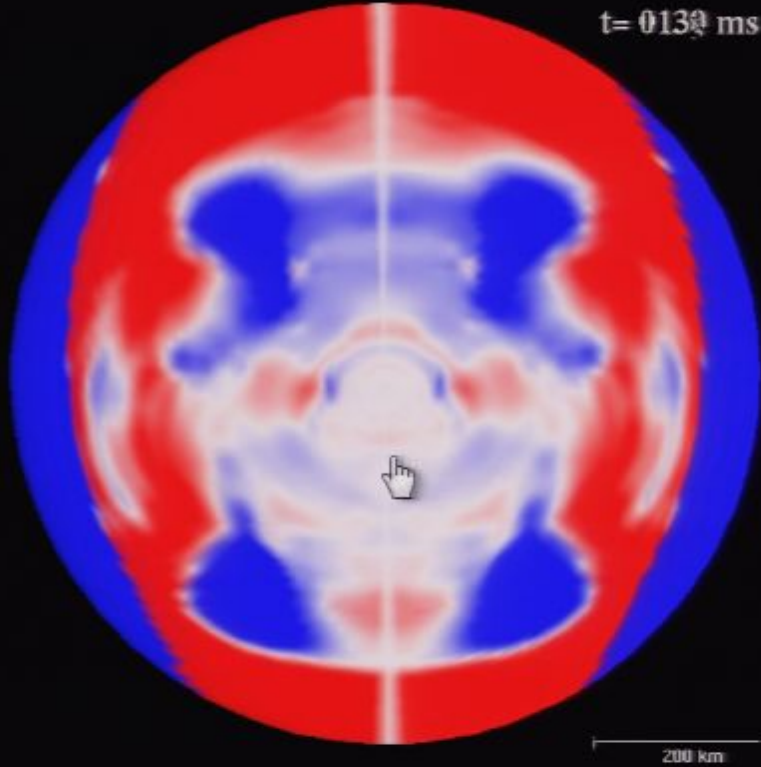




Pressure perturbation for equatorial observer ($\delta P/P$)

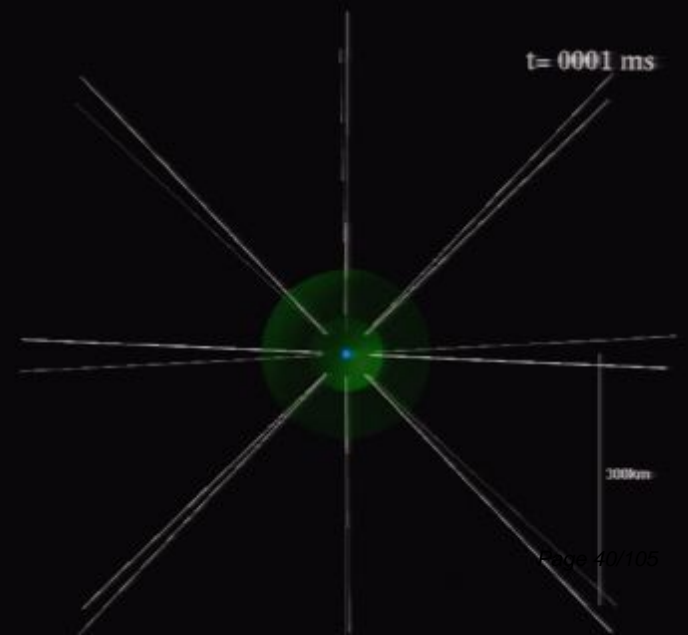
Sketch of streamline for polar observer

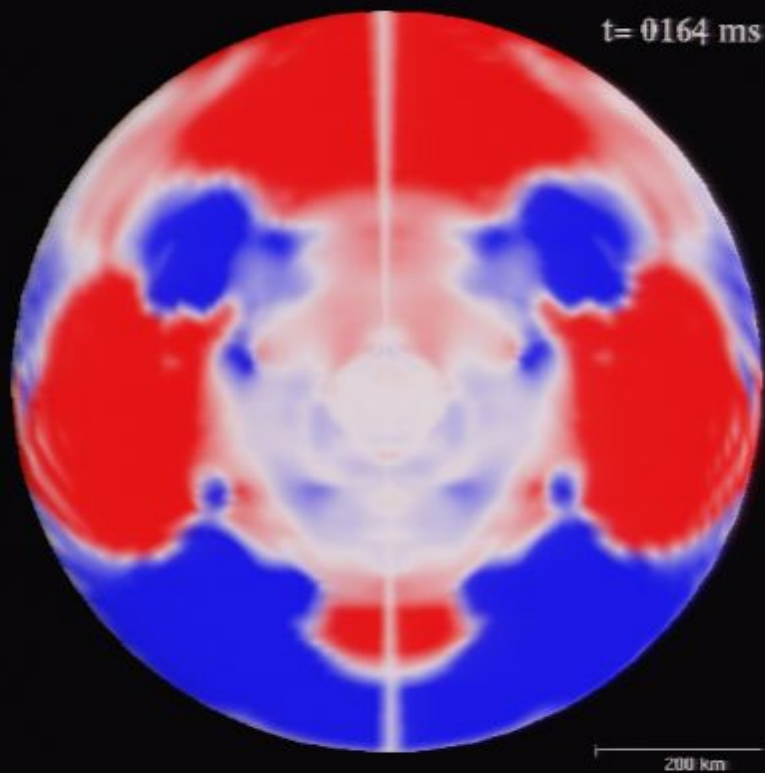




Pressure perturbation for equatorial observer ($\delta P/P$)

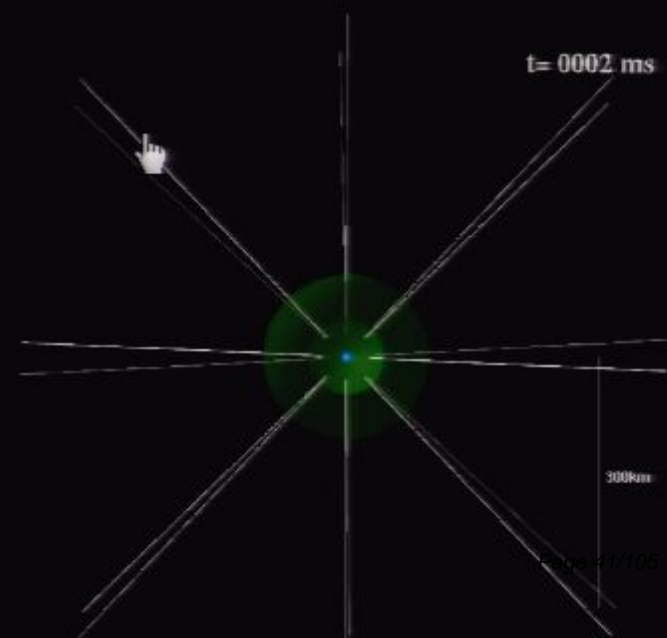
Sketch of streamline for polar observer

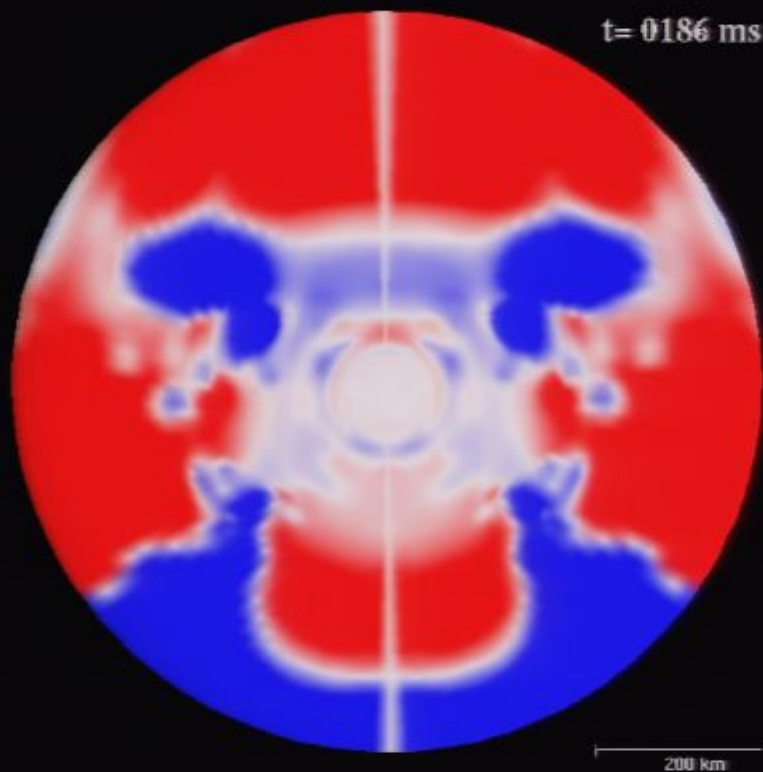




Pressure perturbation for equatorial observer ($\delta P/P$)

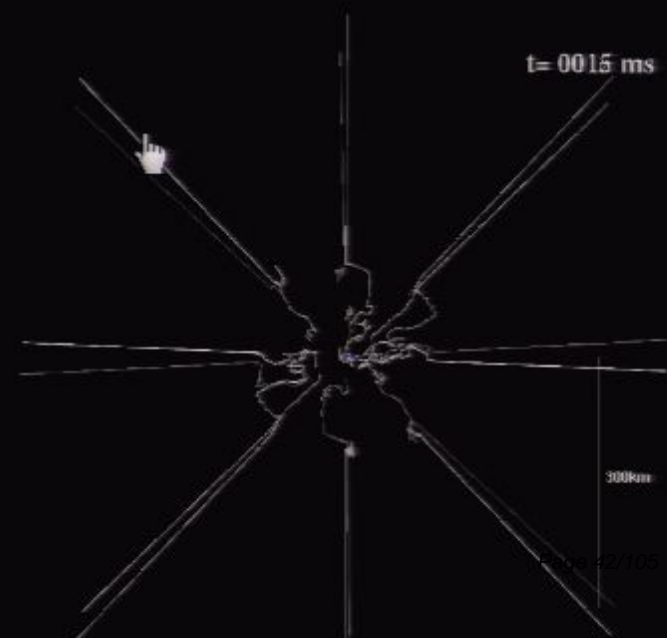
Sketch of streamline for polar observer

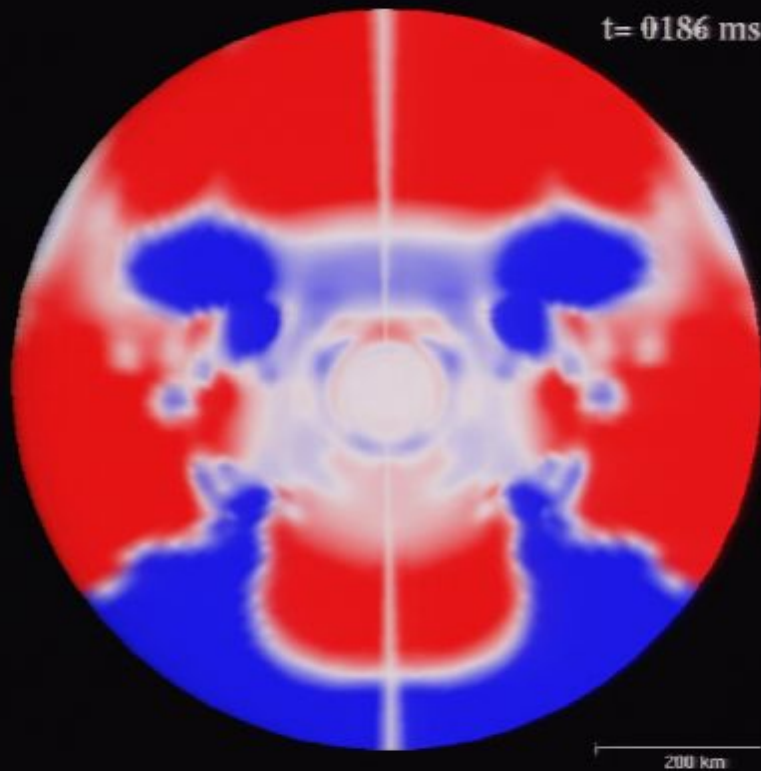




Pressure perturbation for equatorial observer ($\delta P/P$)

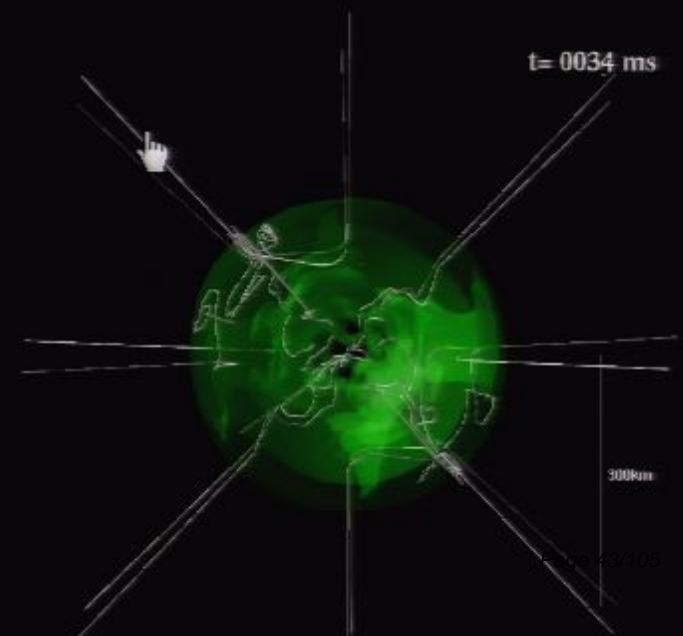
Sketch of streamline for polar observer

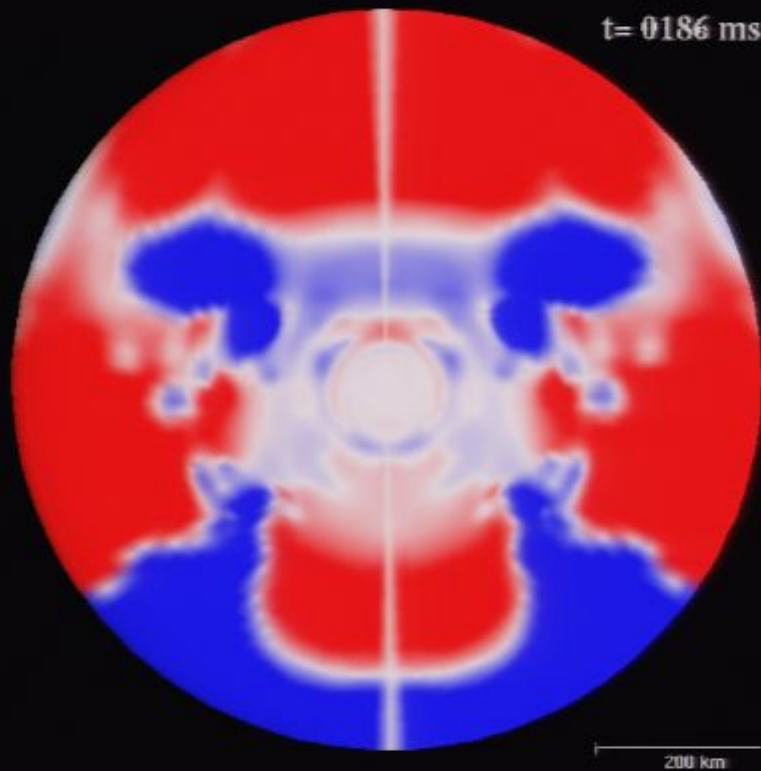




Pressure perturbation for equatorial observer ($\delta P/P$)

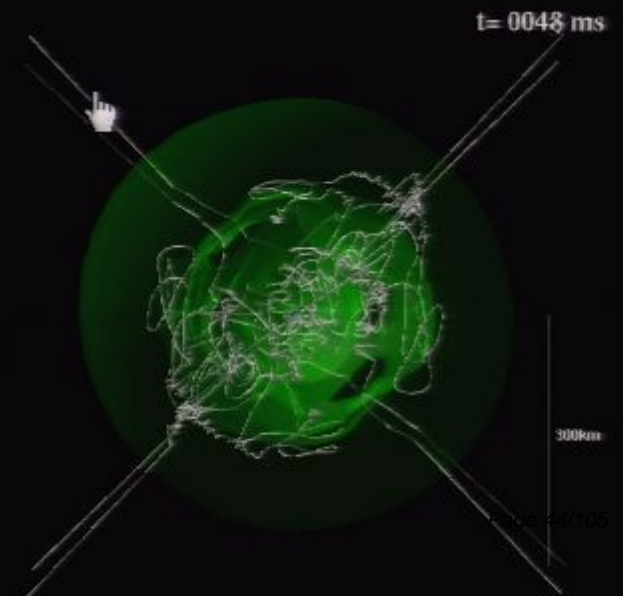
Sketch of streamline for polar observer

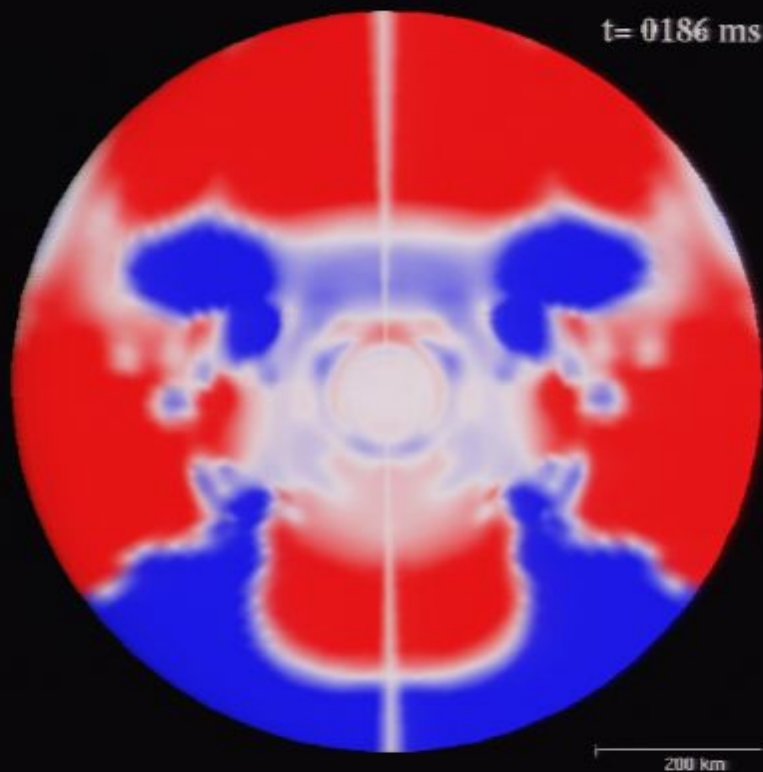




Pressure perturbation for equatorial observer ($\delta P/P$)

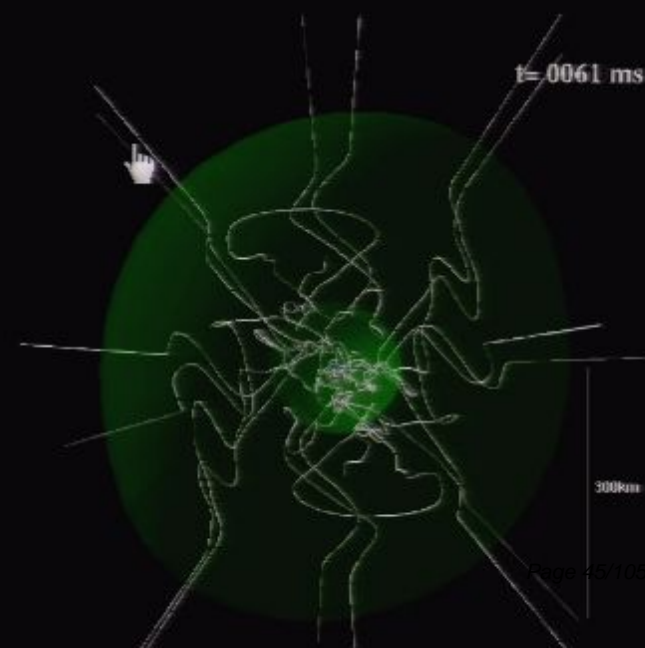
Sketch of streamline for polar observer

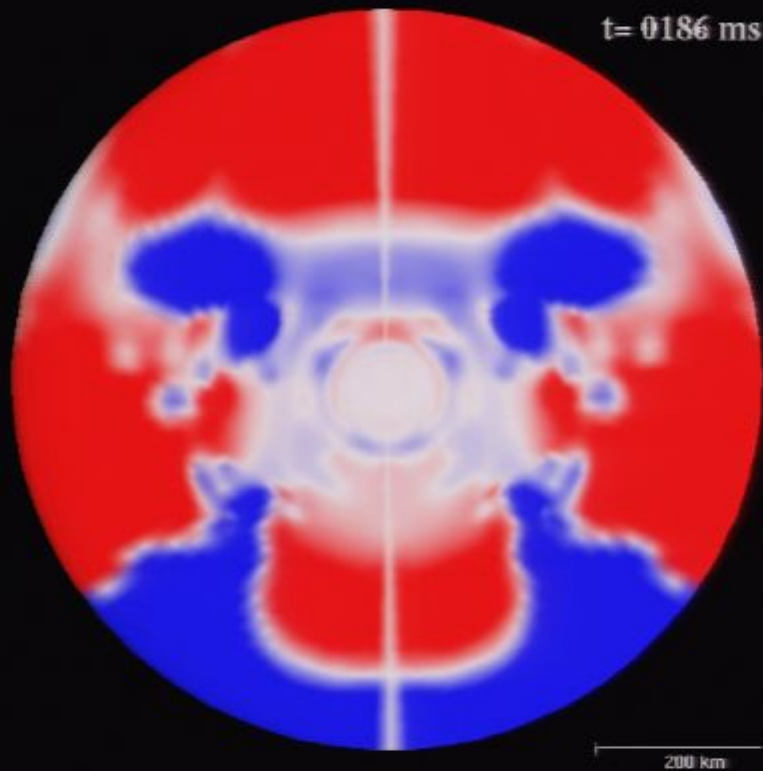




Pressure perturbation for equatorial observer ($\delta P/P$)

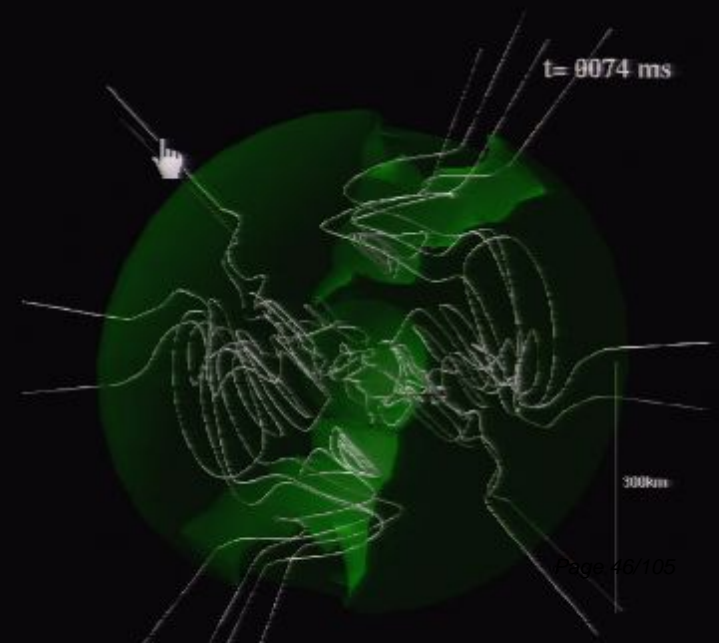
Sketch of streamline for polar observer

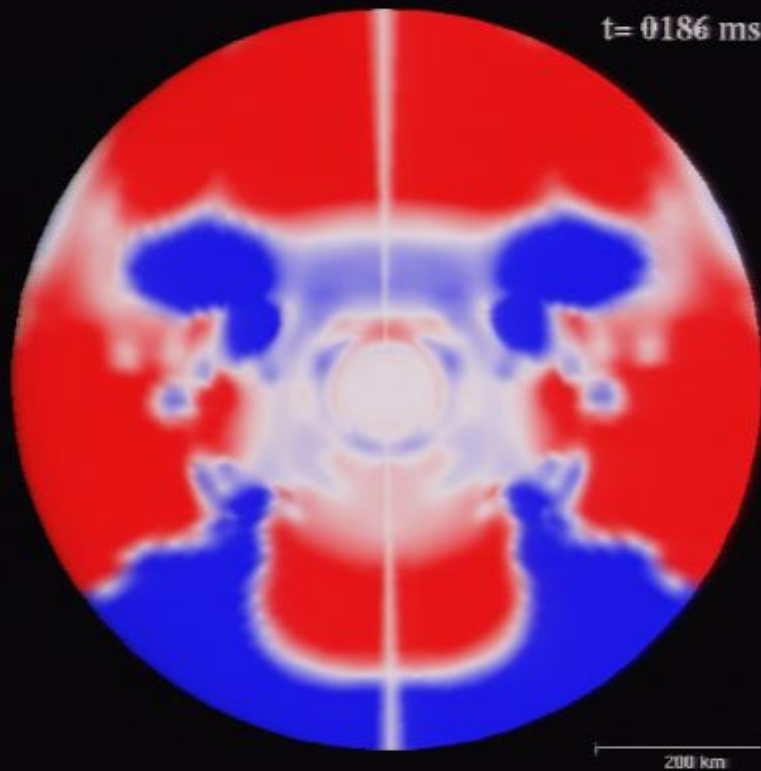




Pressure perturbation for equatorial observer ($\delta P/P$)

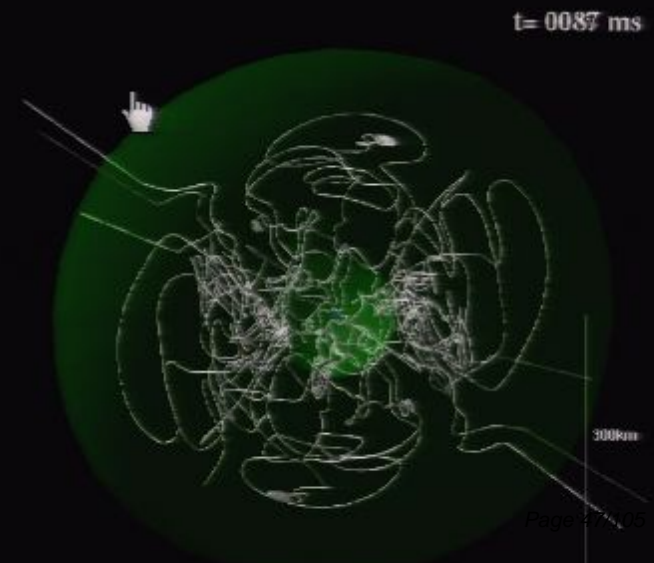
Sketch of streamline for polar observer

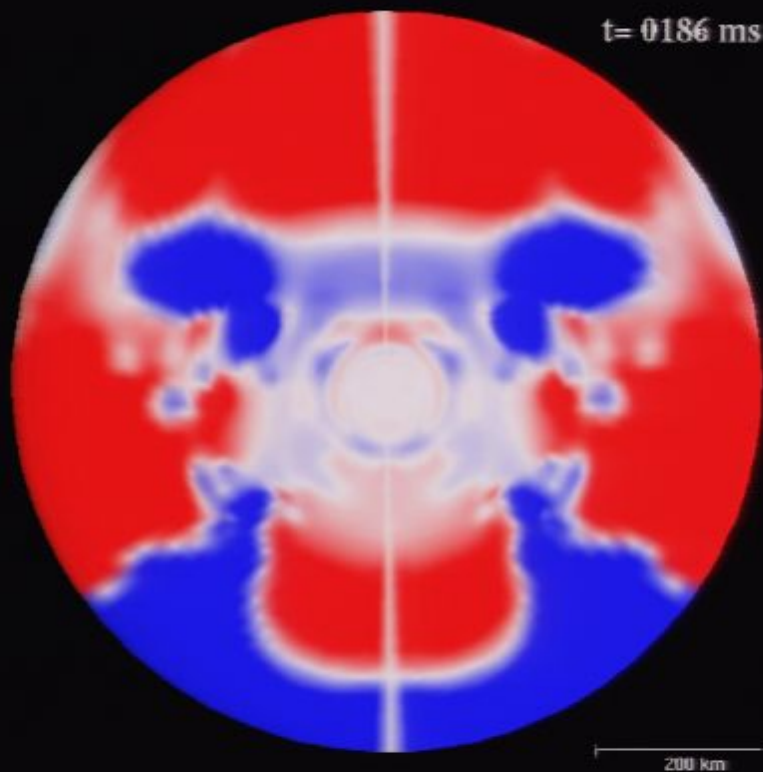




Pressure perturbation for equatorial observer ($\delta P/P$)

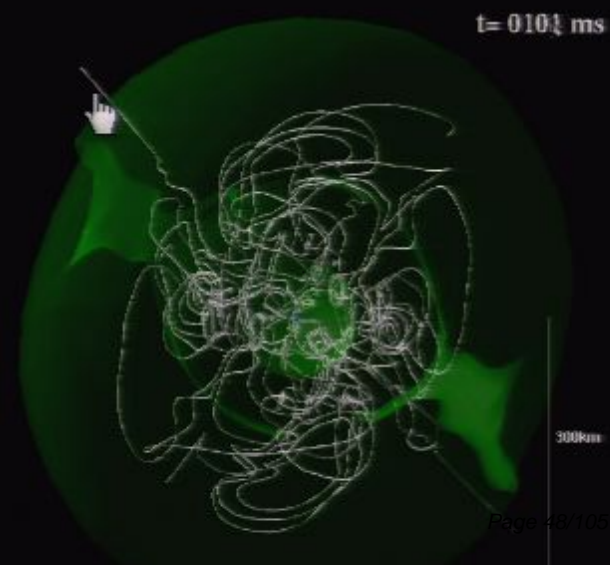
Sketch of streamline for polar observer

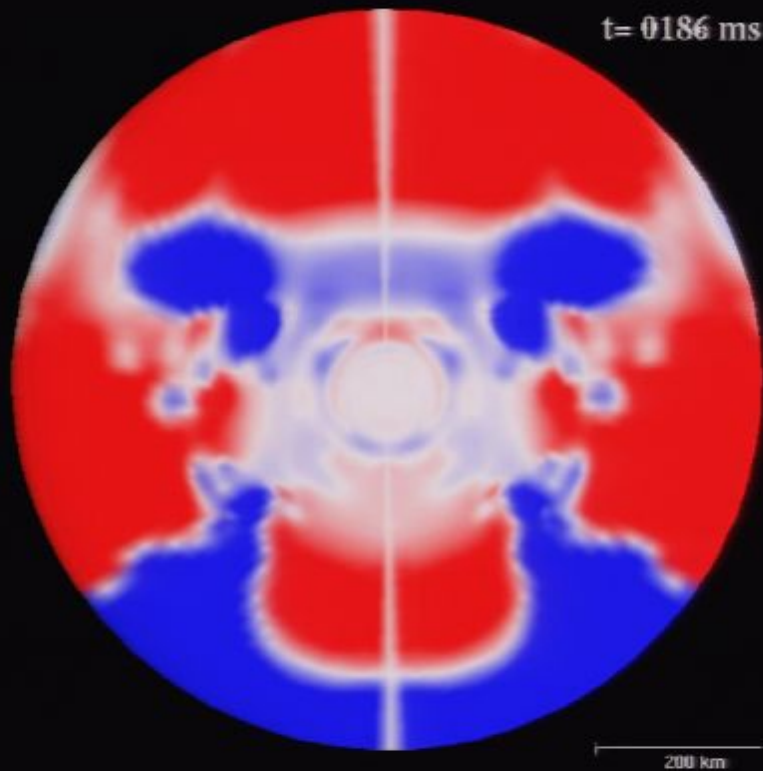




Pressure perturbation for equatorial observer ($\delta P/P$)

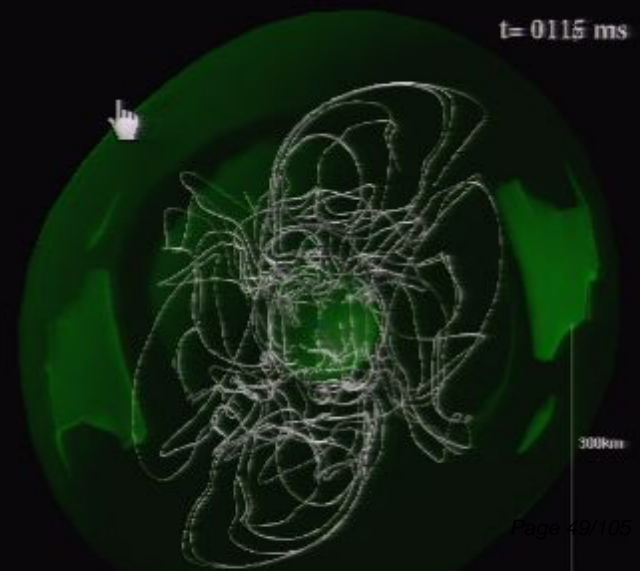
Sketch of streamline for polar observer

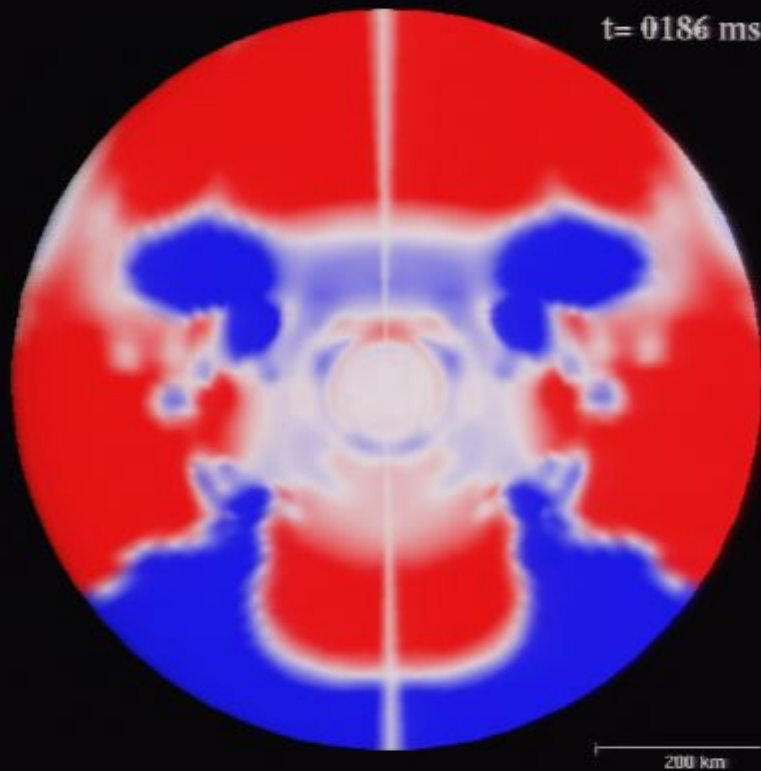




Pressure perturbation for equatorial observer ($\delta P/P$)

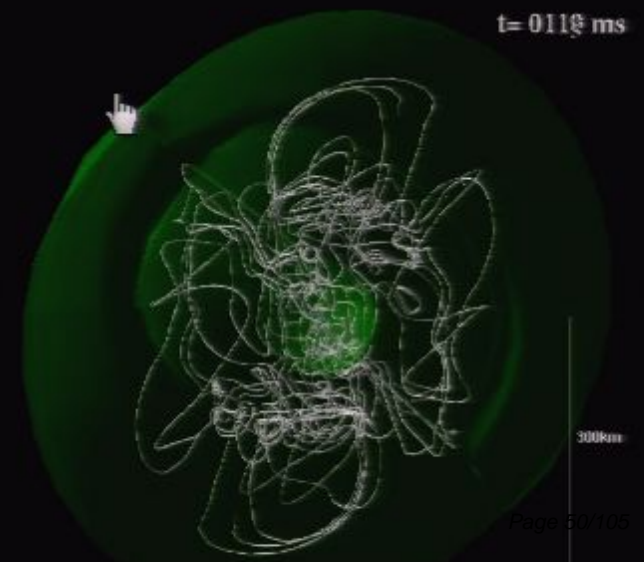
Sketch of streamline for polar observer



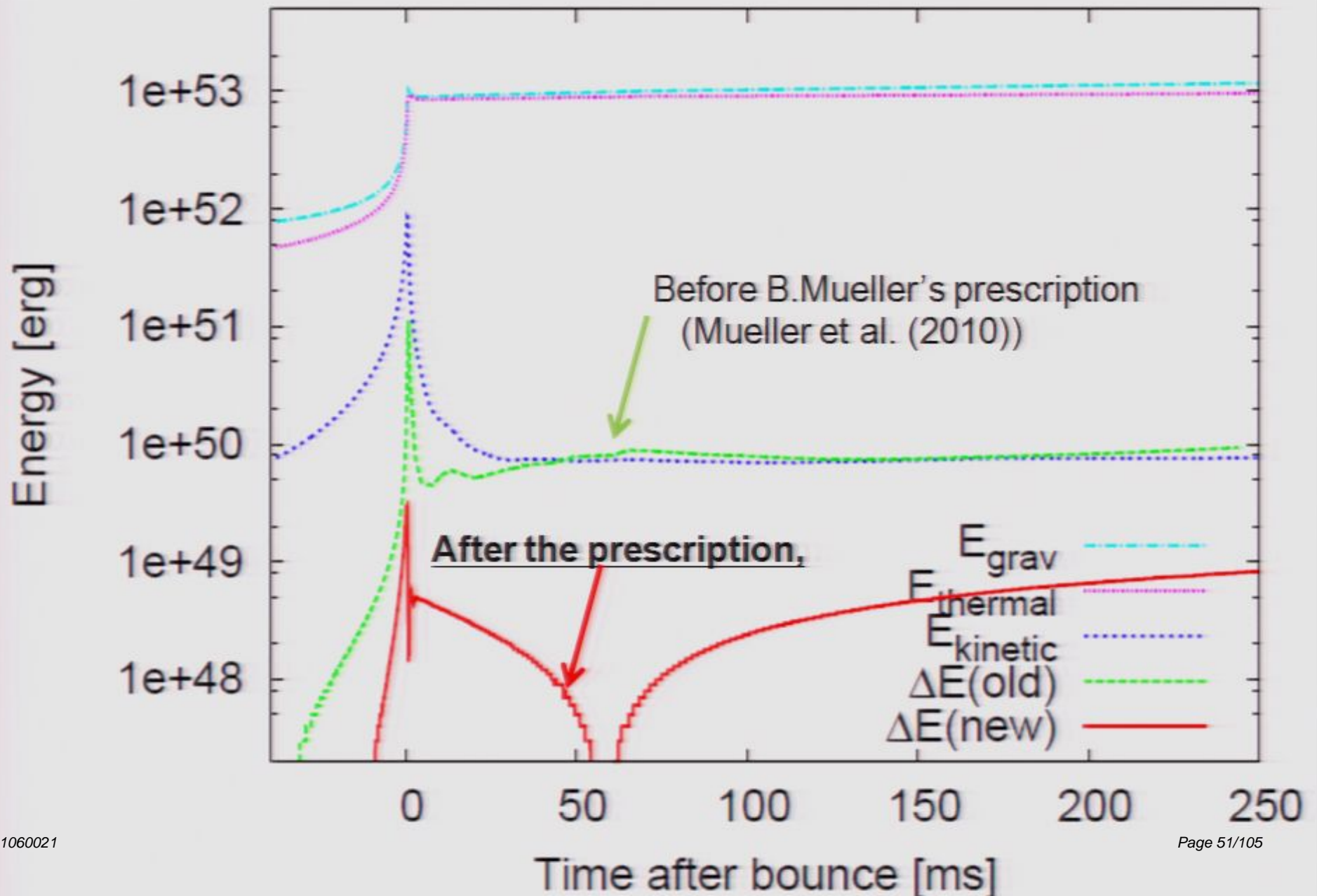


Pressure perturbation for equatorial observer ($\delta P/P$)

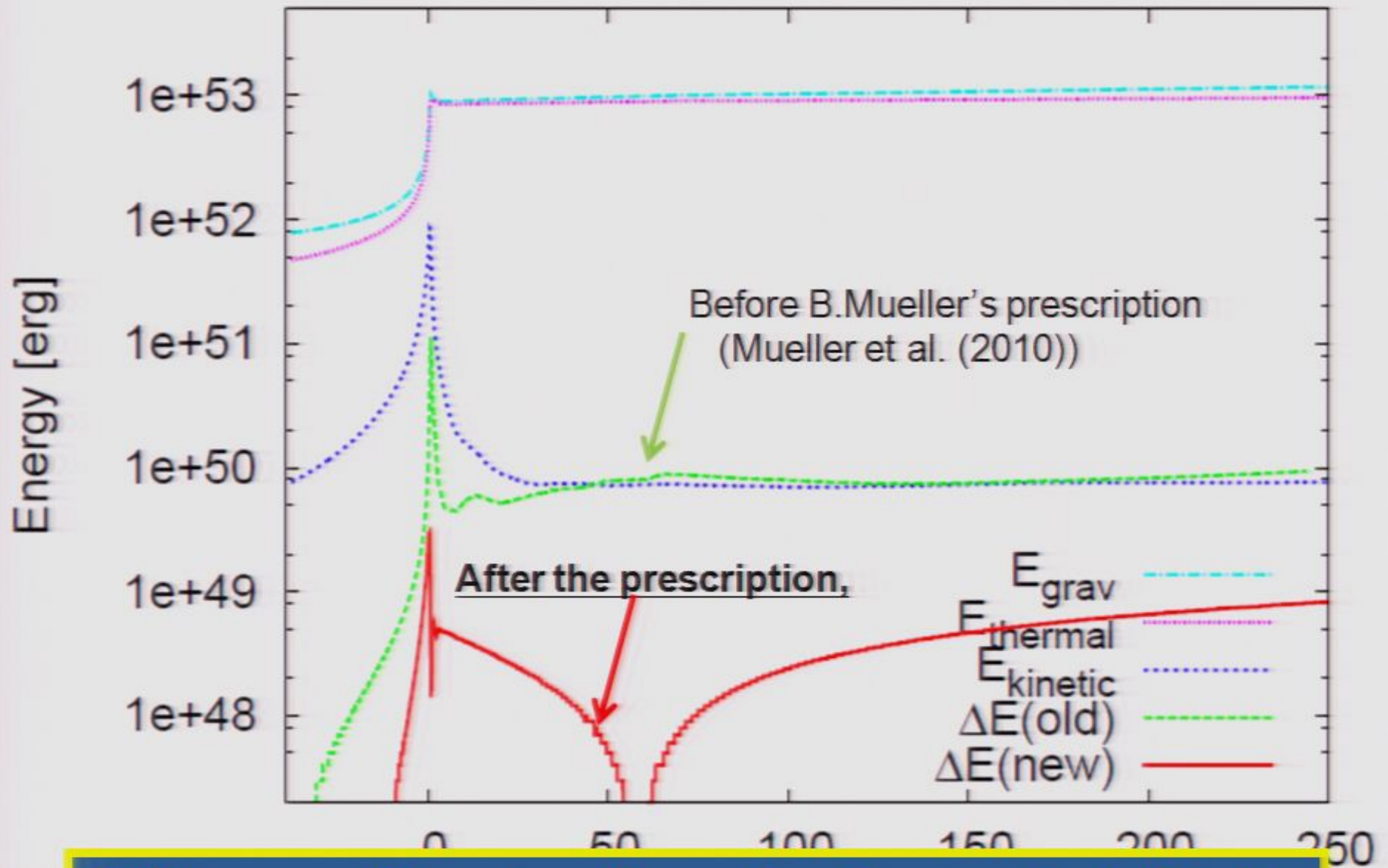
Sketch of streamline for polar observer



Energy conservation should be kept in good accuracy!



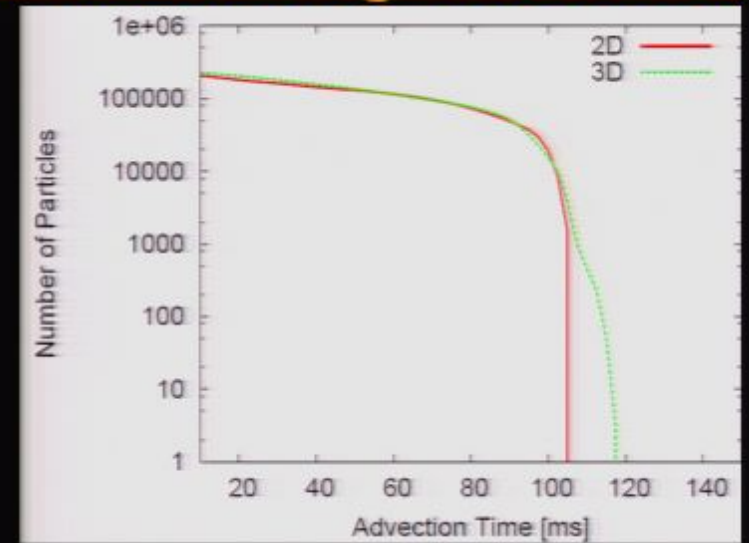
Energy conservation should be kept in good accuracy!



Easy to obtain explosions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



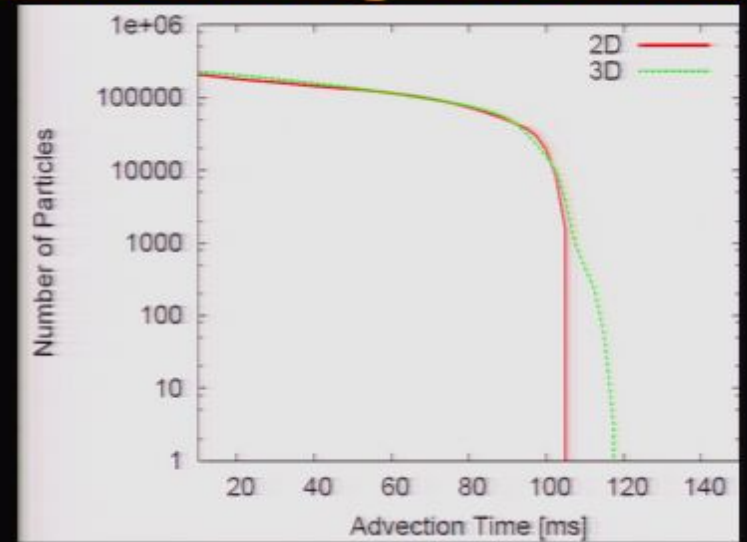
The advection timescales become longer in 3D than in 2D.

t= 0107 ms

Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



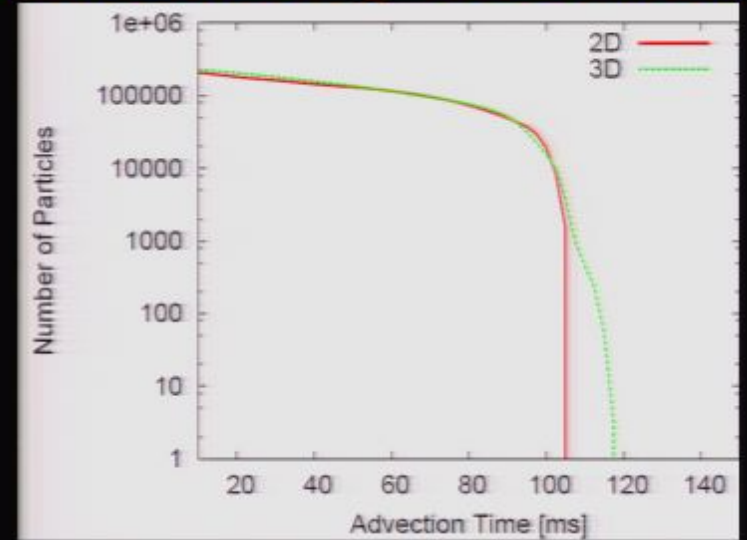
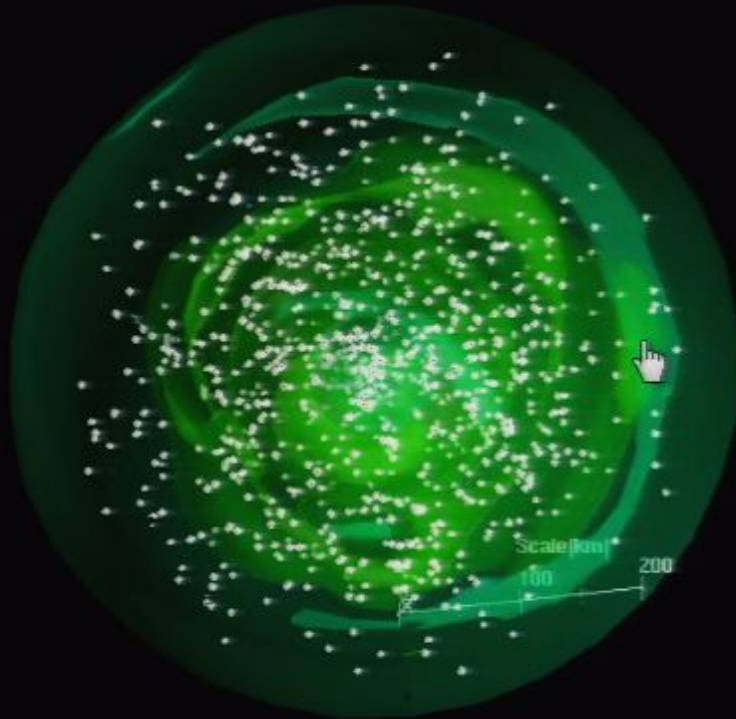
The advection timescales become longer in 3D than in 2D.

t= 0116 ms

Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



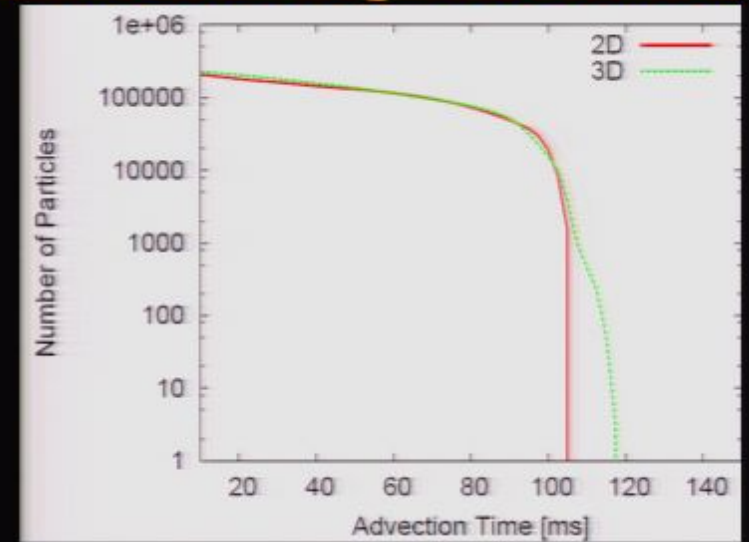
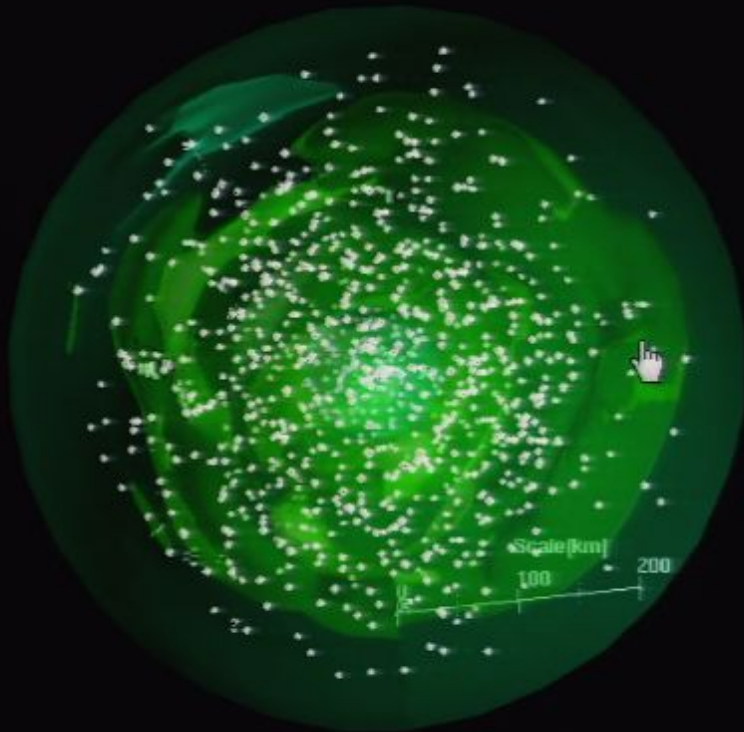
The advection timescales become longer in 3D than in 2D.

t= 0123 ms

Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



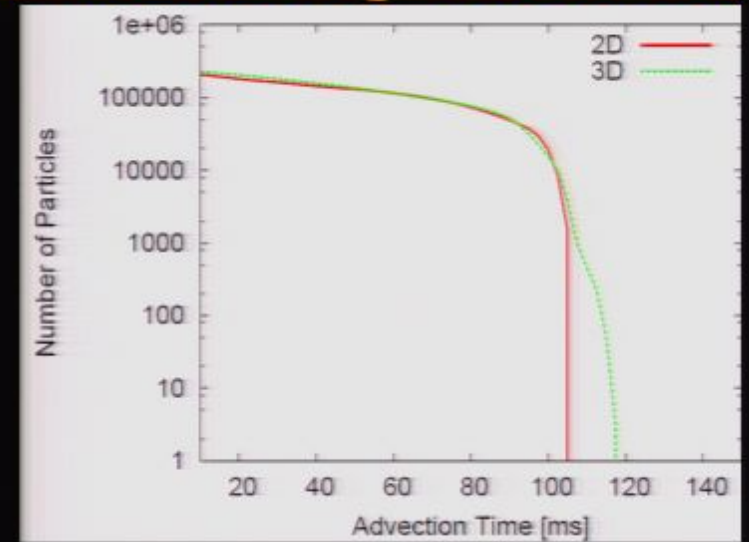
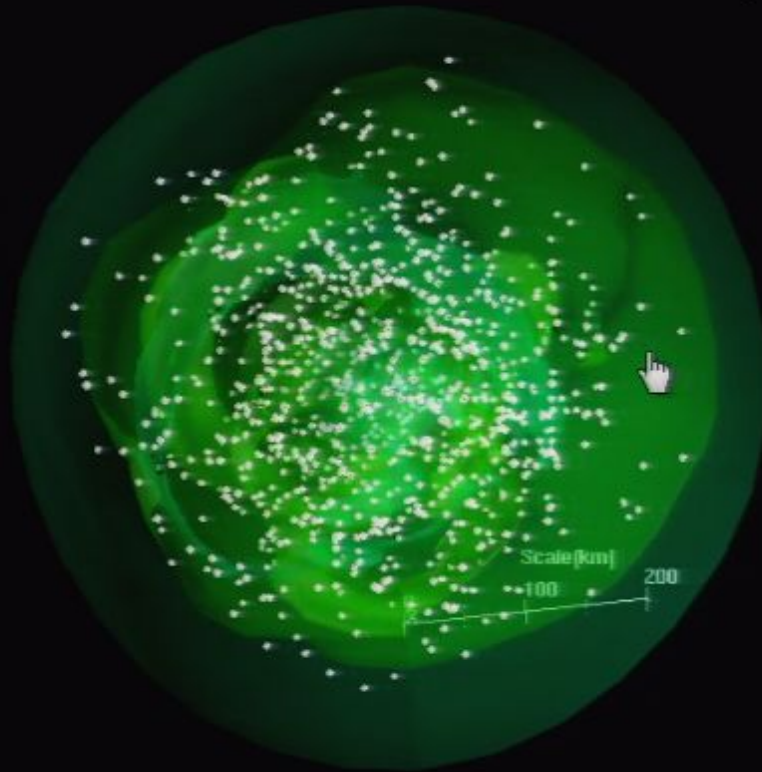
The advection timescales become longer in 3D than in 2D.

t= 0131 ms

Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



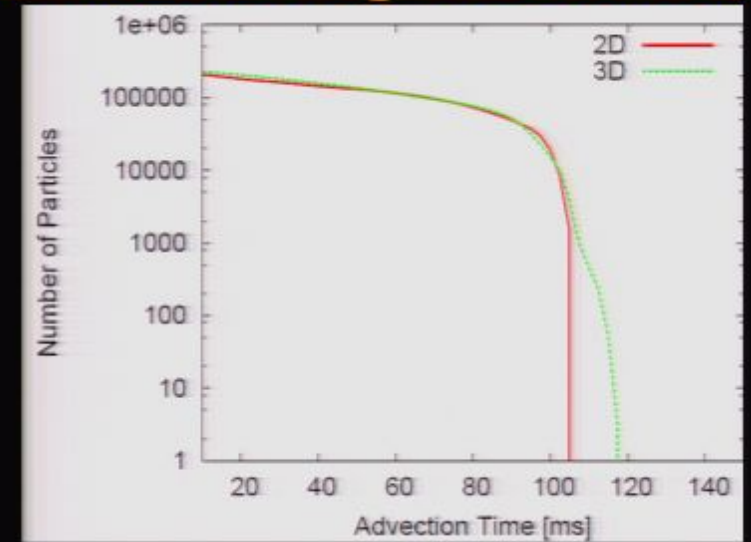
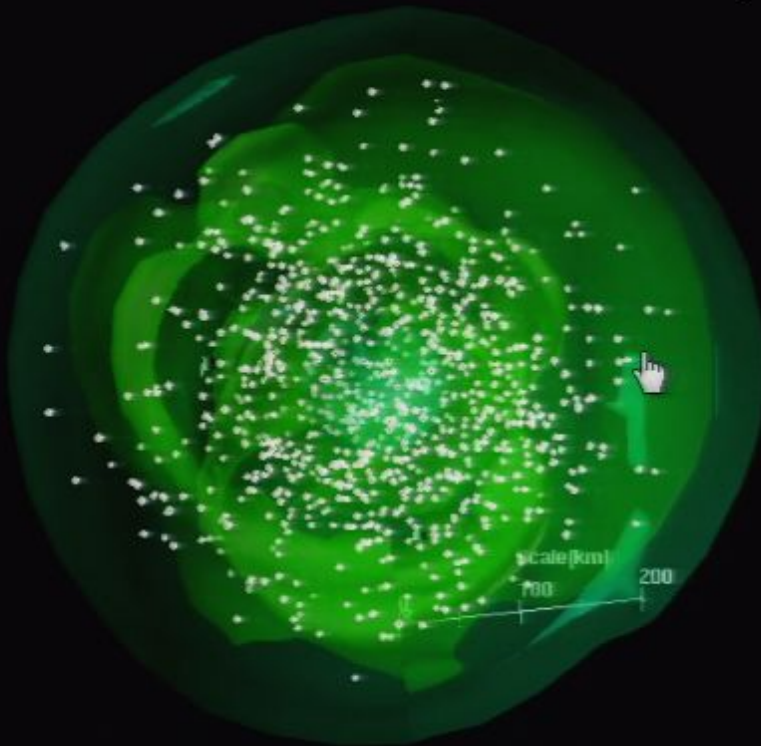
The advection timescales become longer in 3D than in 2D.

t= 0130 ms

Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



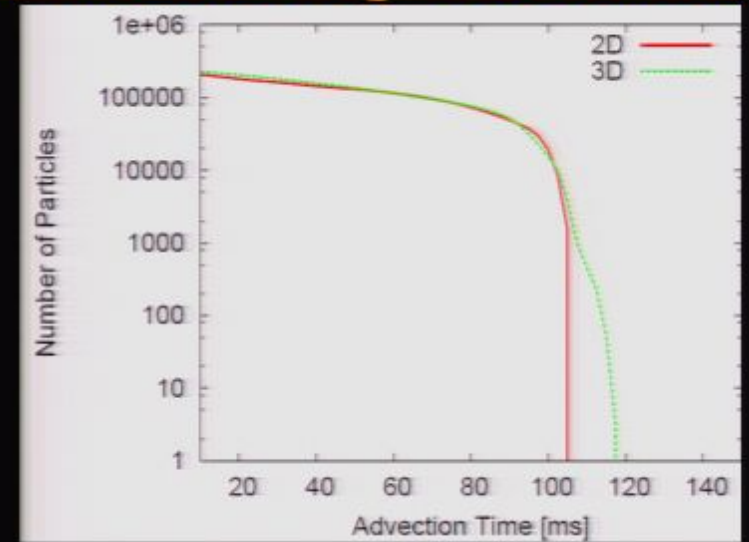
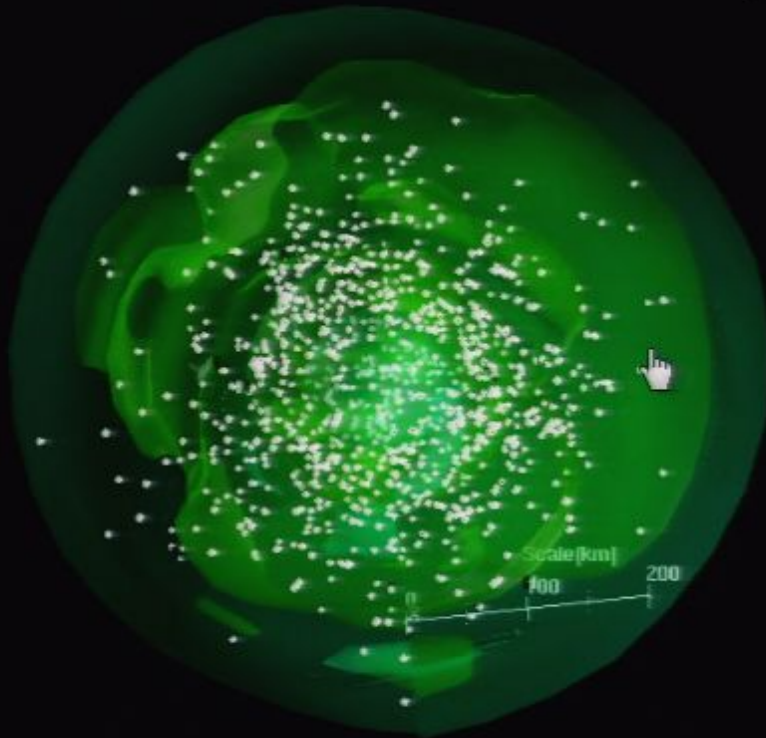
The advection timescales become longer in 3D than in 2D.

t= 0147 ms

Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



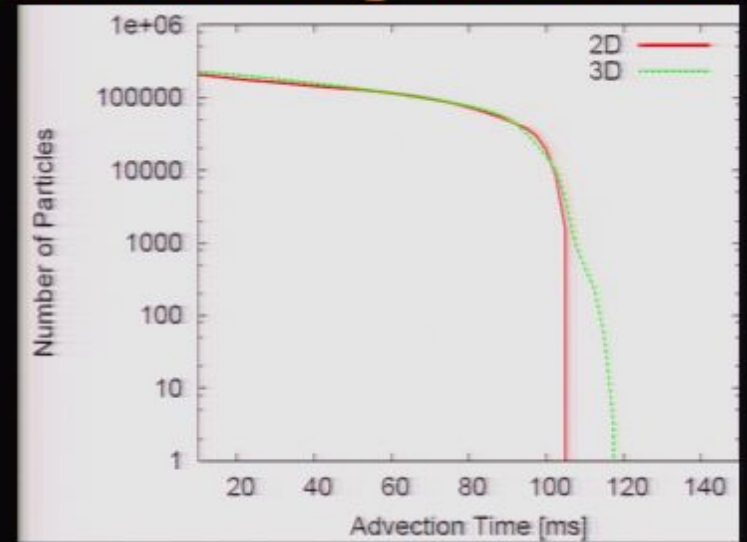
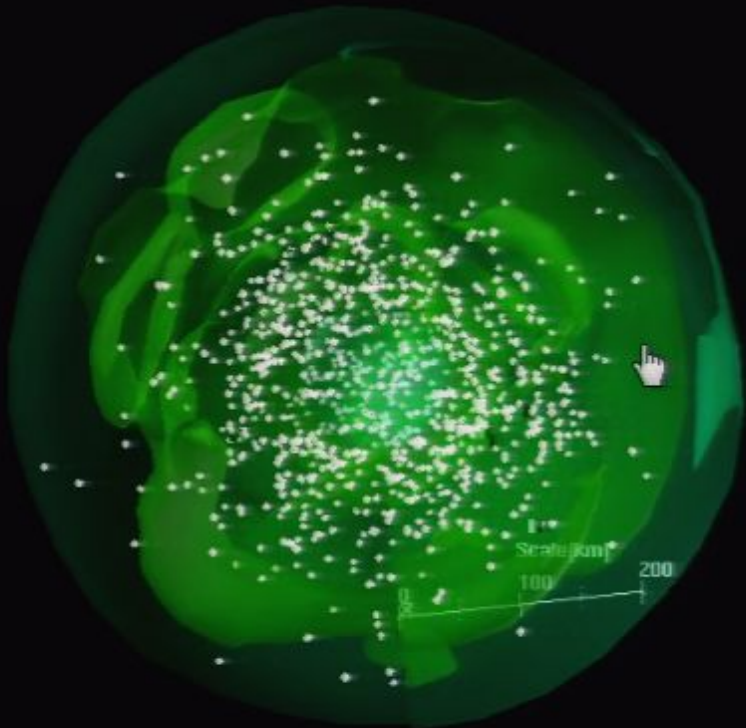
The advection timescales become longer in 3D than in 2D.

t= 0155 ms

Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



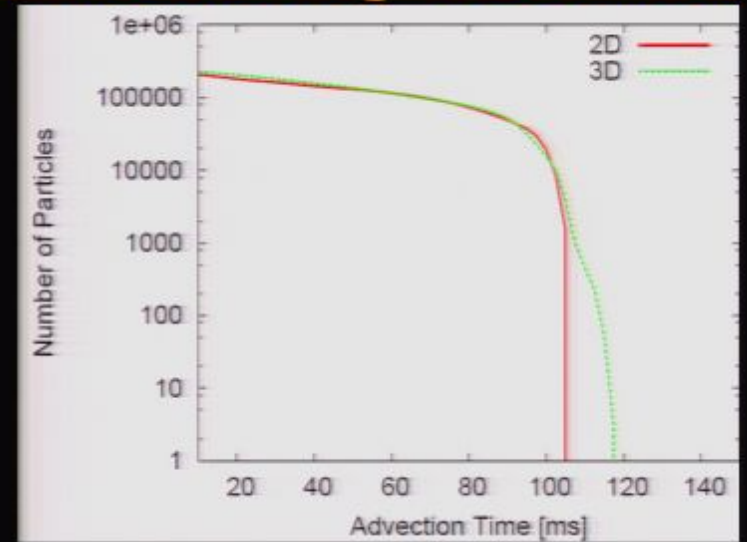
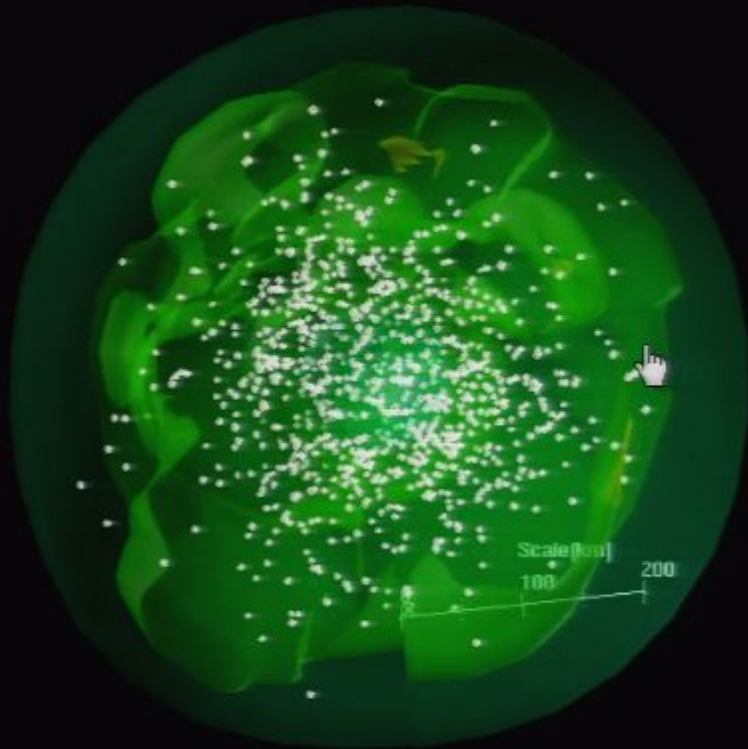
The advection timescales become longer in 3D than in 2D.

t= 0163 ms

Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



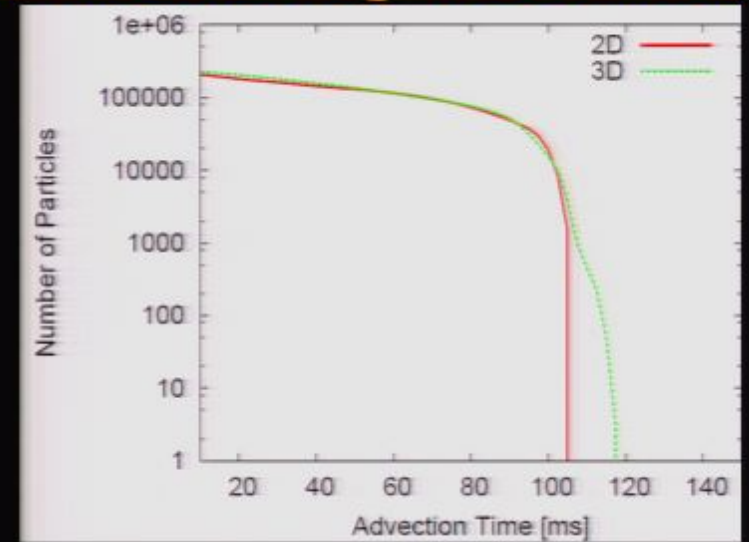
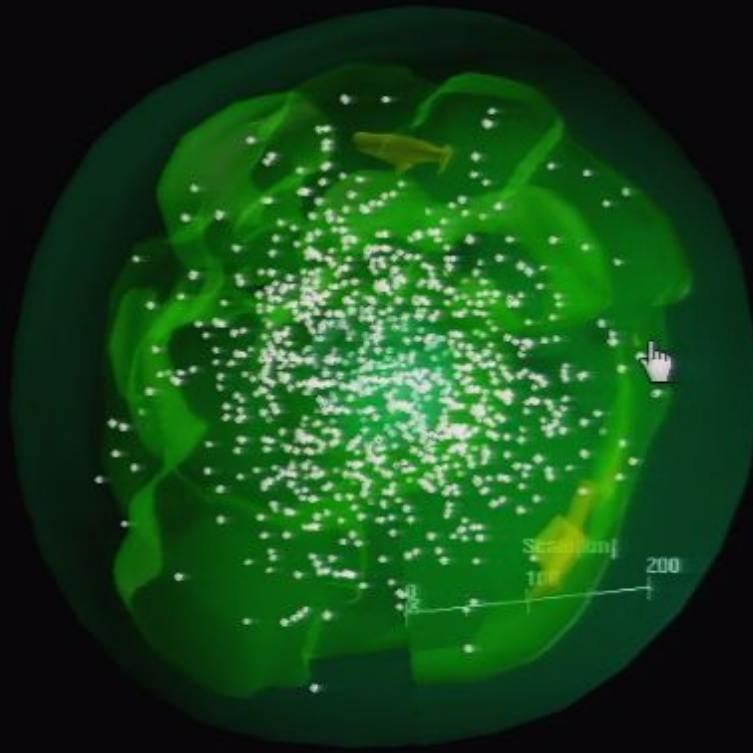
The advection timescales become longer in 3D than in 2D.

t= 0165 ms

Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



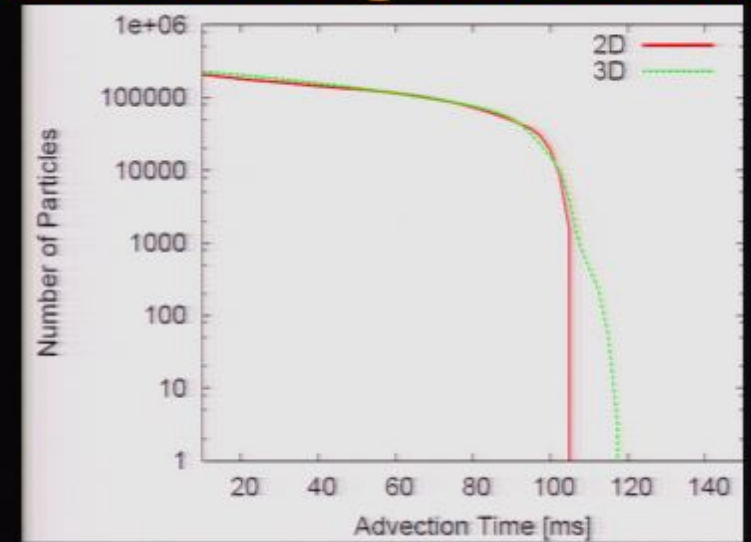
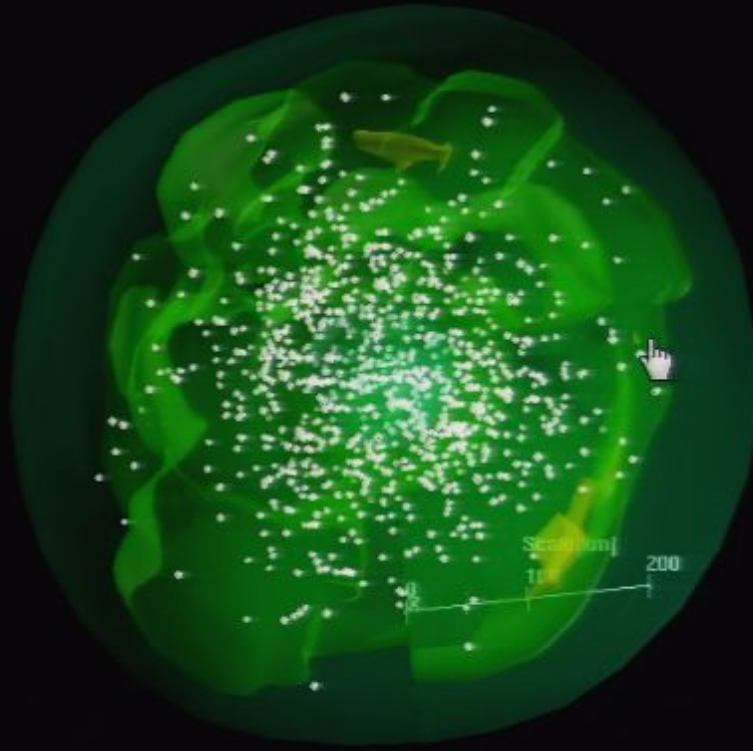
The advection timescales become longer in 3D than in 2D.

t= 0165 ms

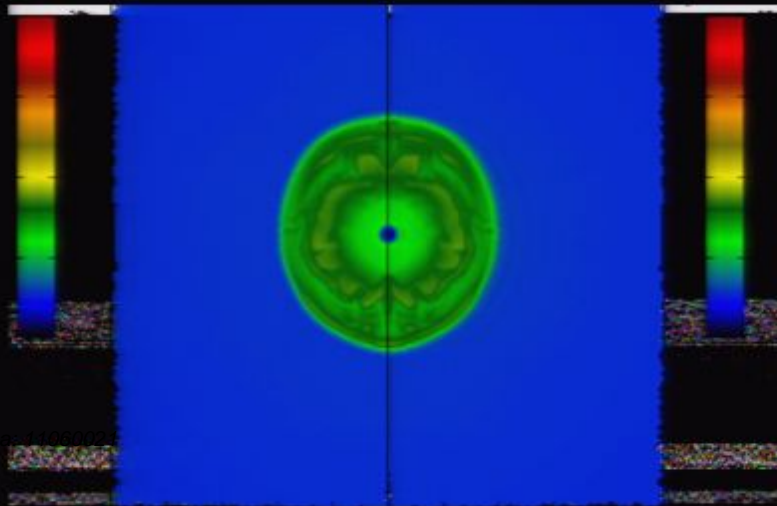
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



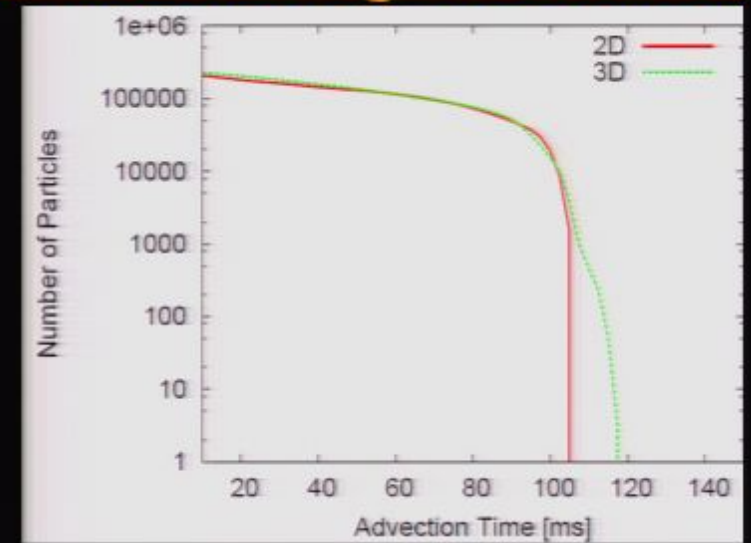
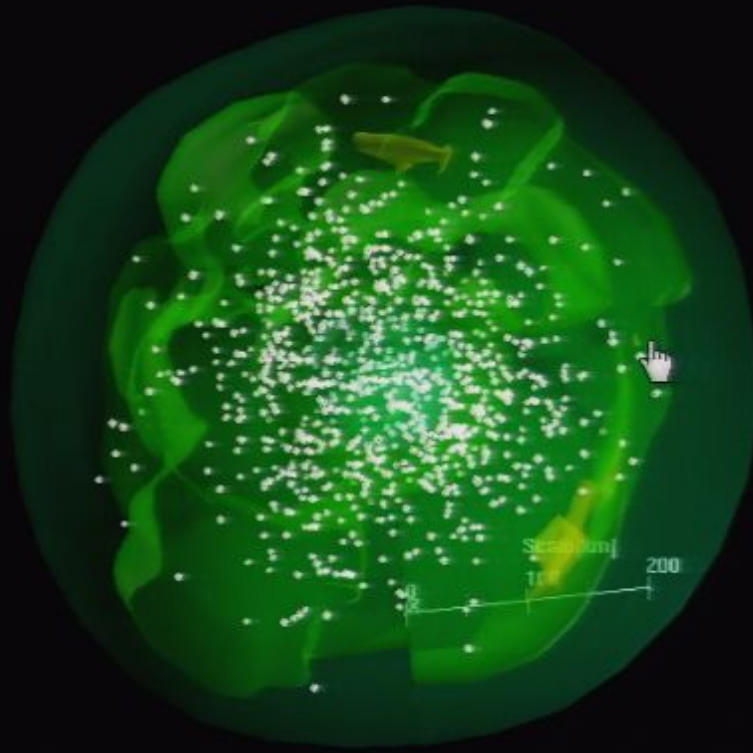
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

t= 0165 ms

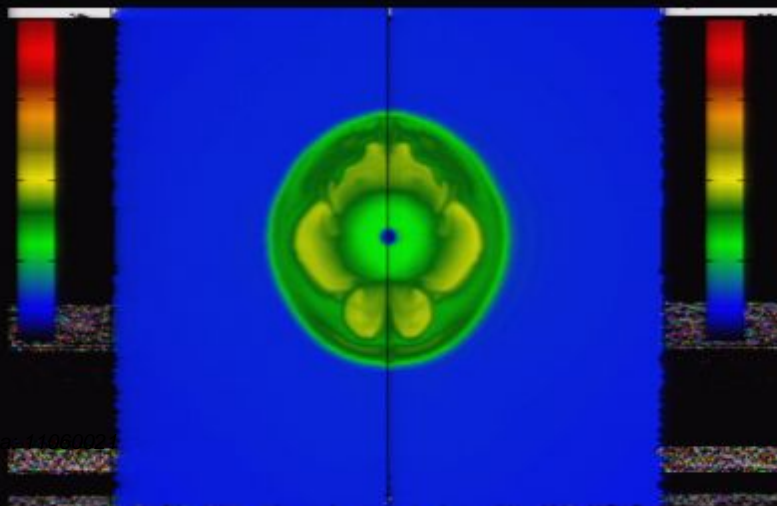
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



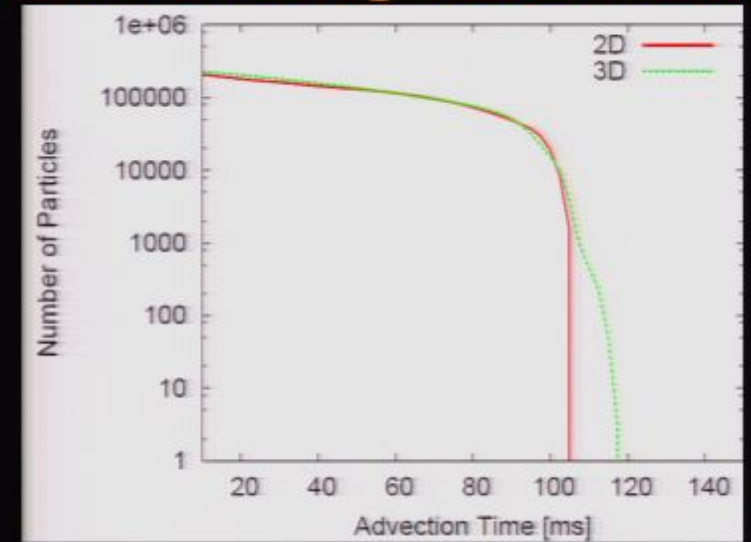
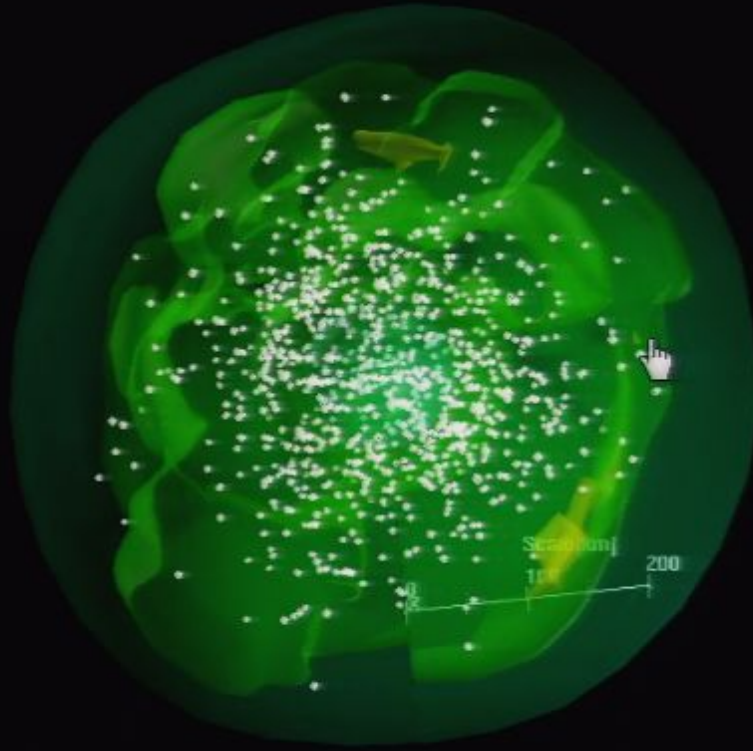
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

t= 0165 ms

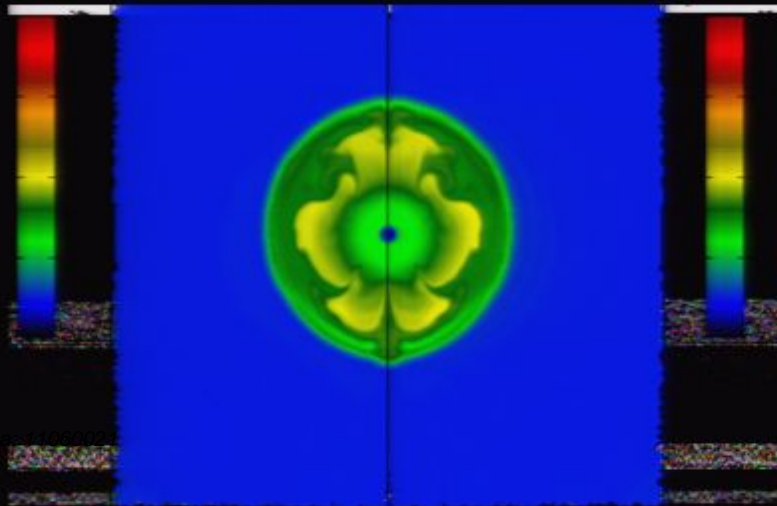
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



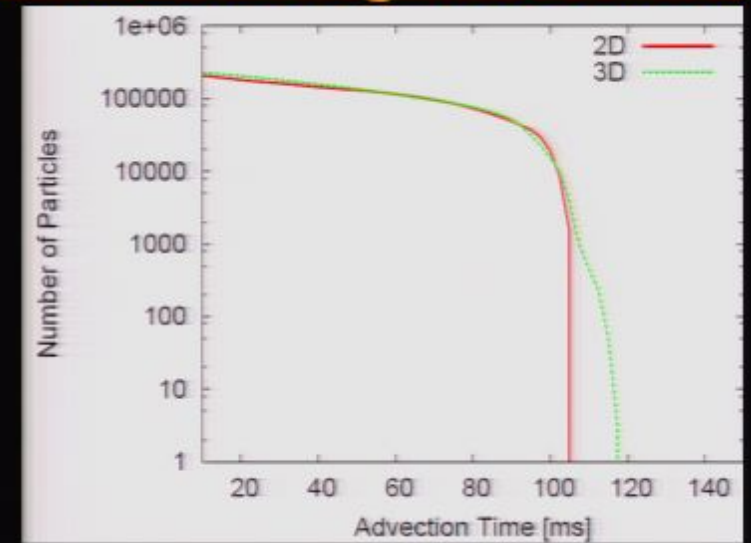
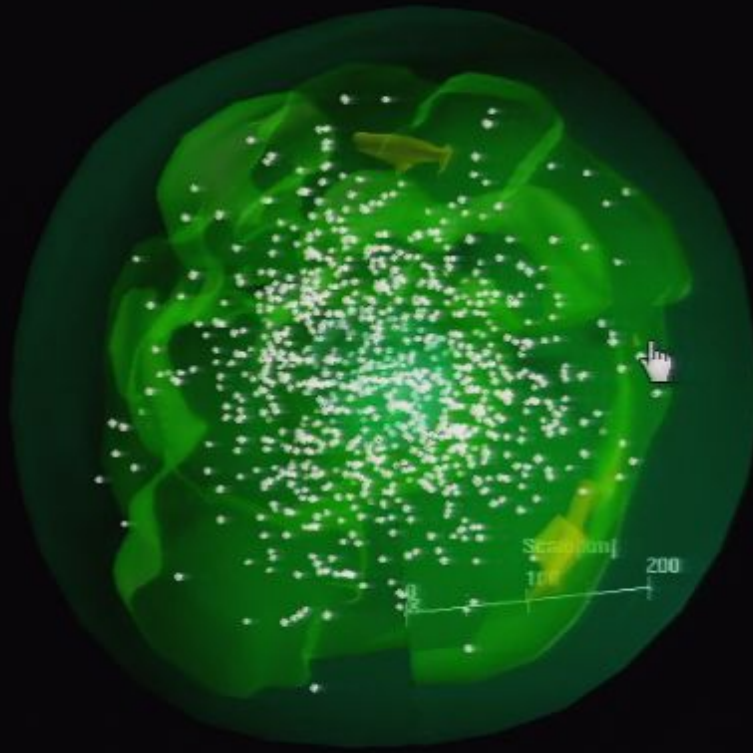
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

t= 0165 ms

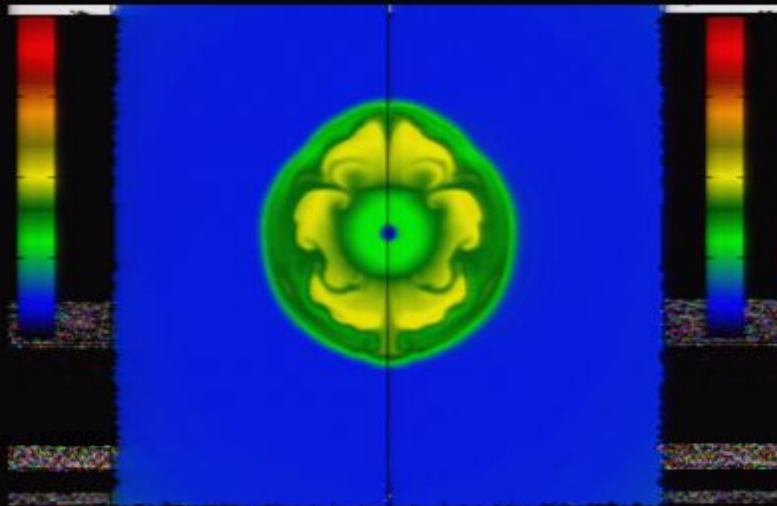
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



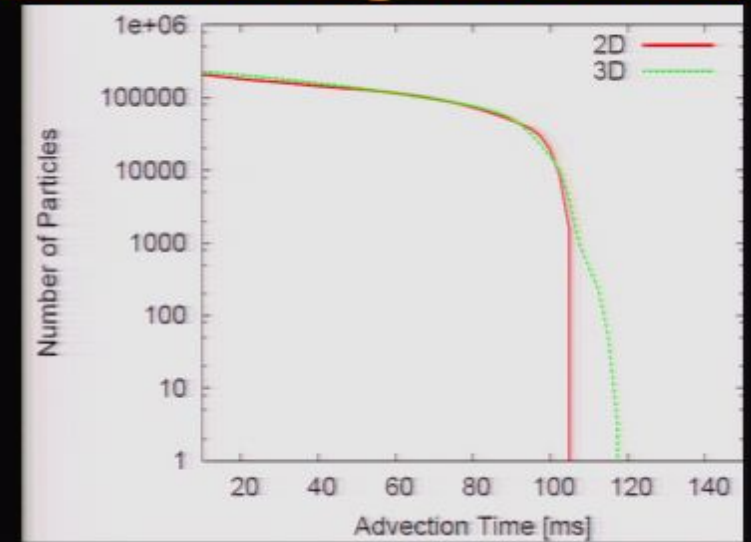
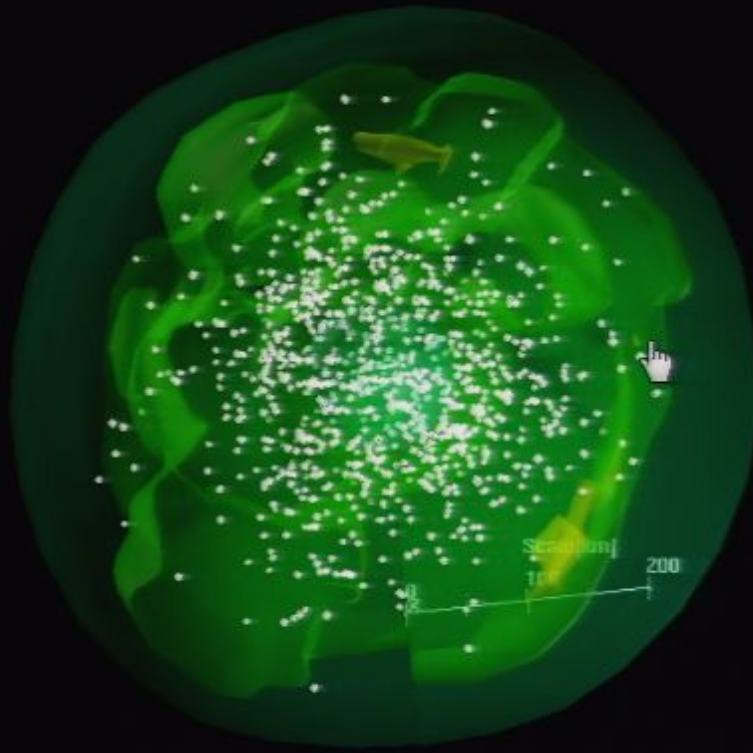
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

t= 0165 ms

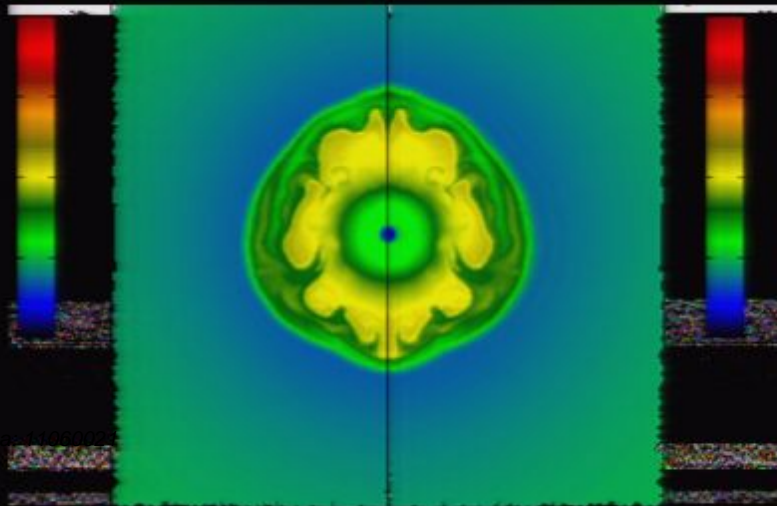
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



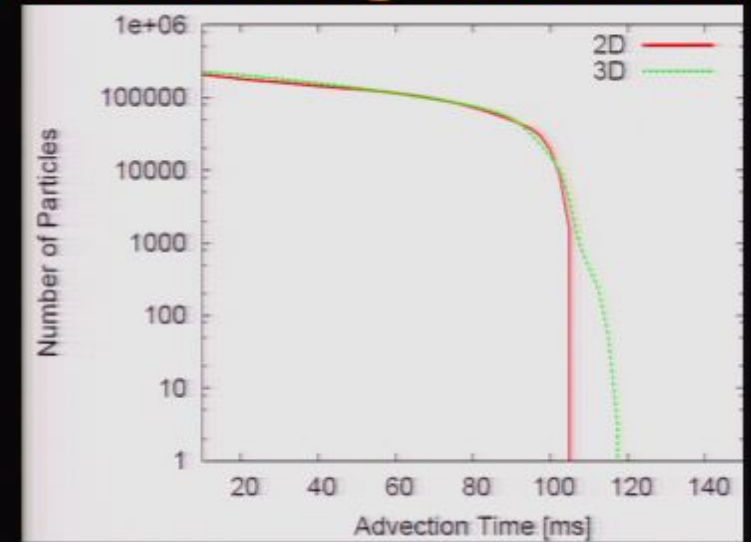
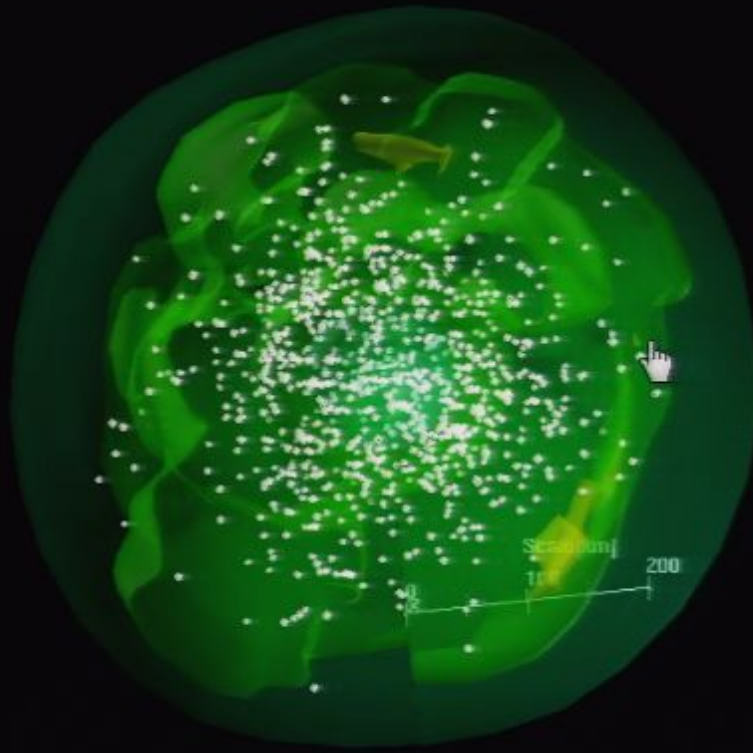
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

t= 0165 ms

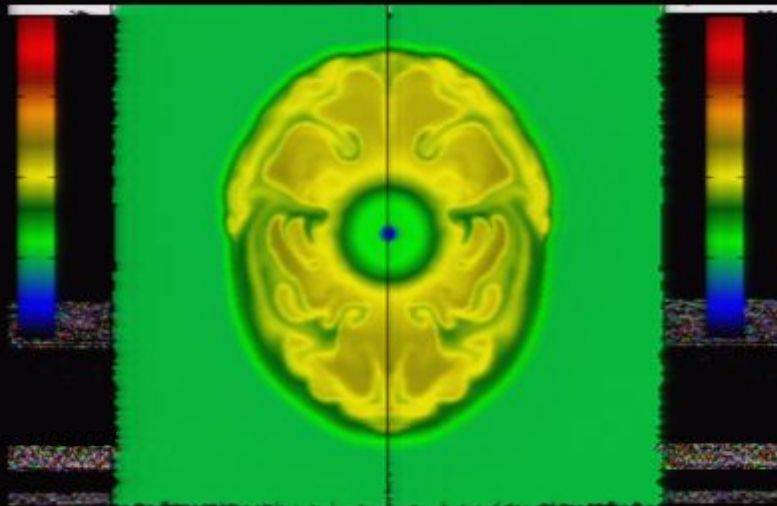
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



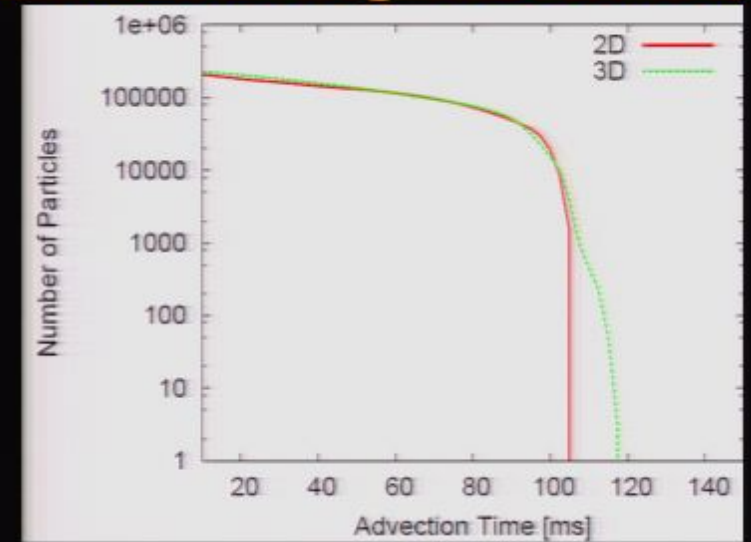
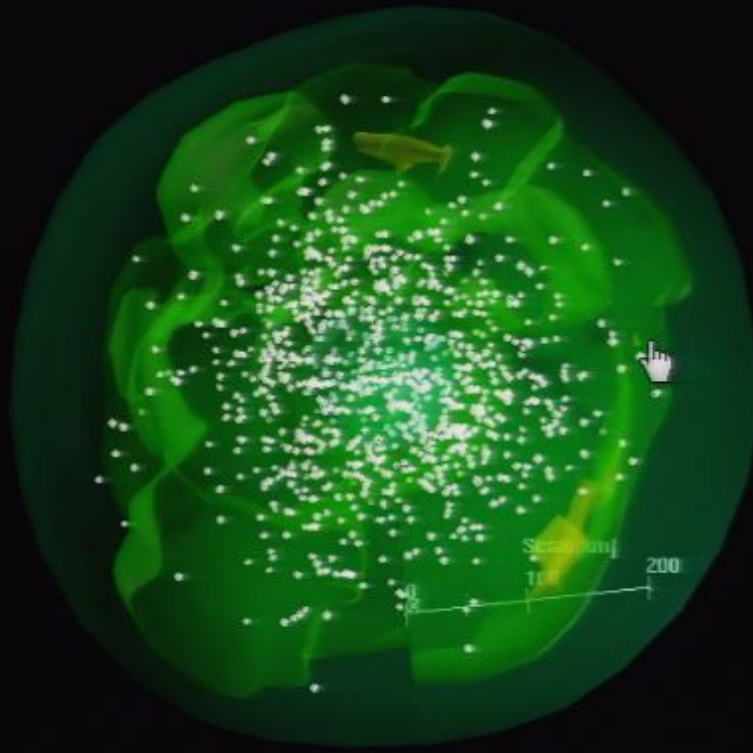
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

t= 0165 ms

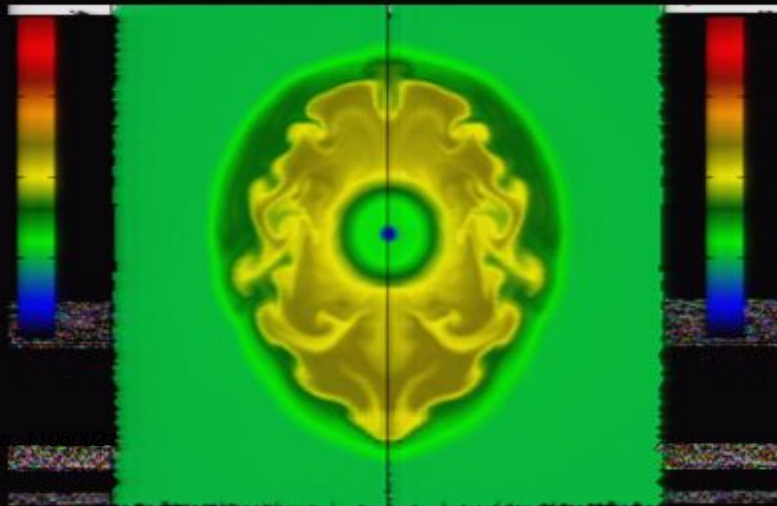
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



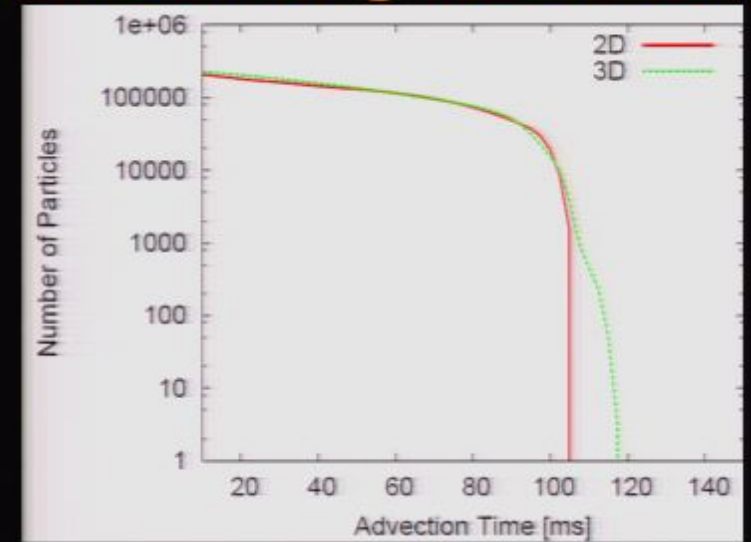
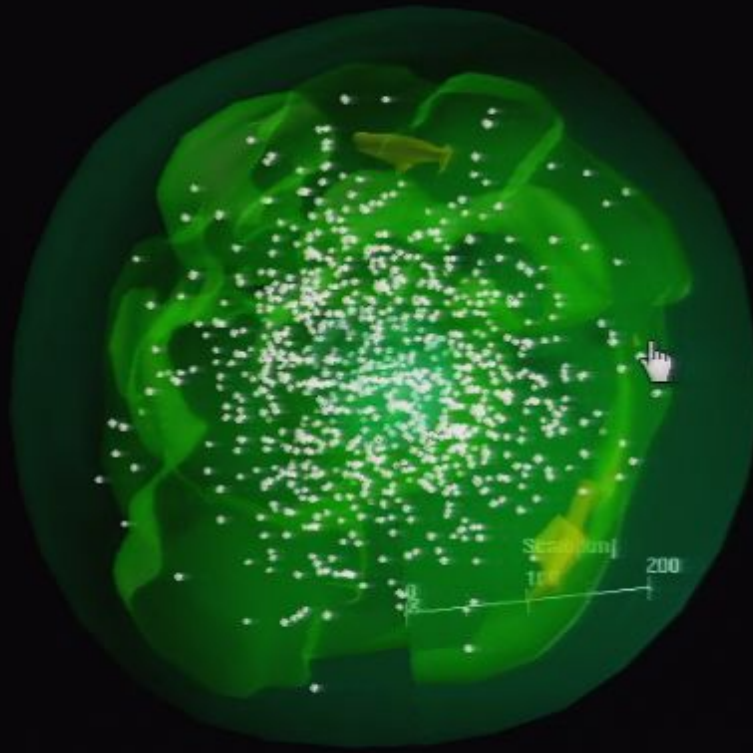
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

t= 0165 ms

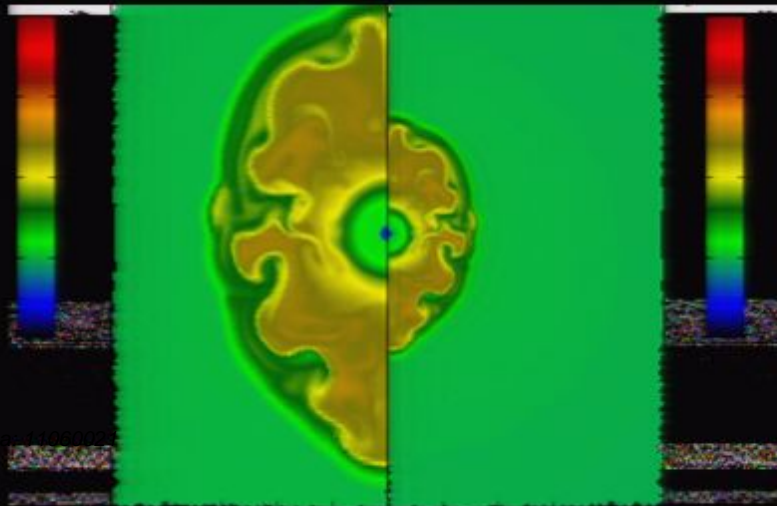
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



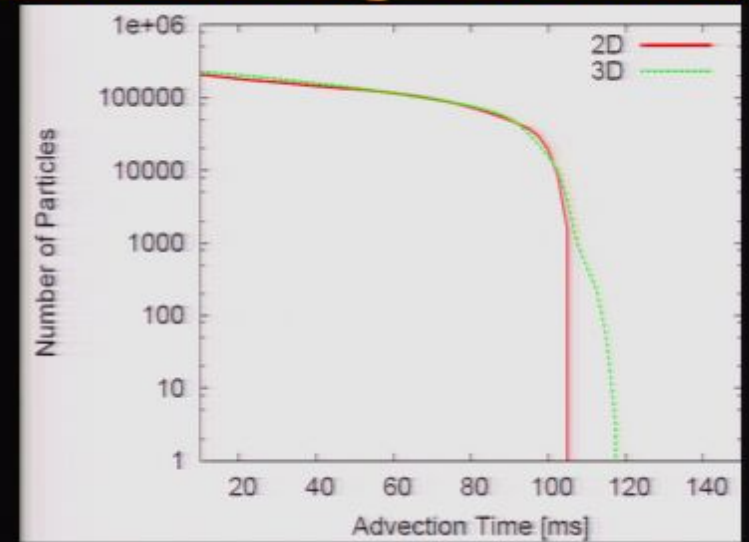
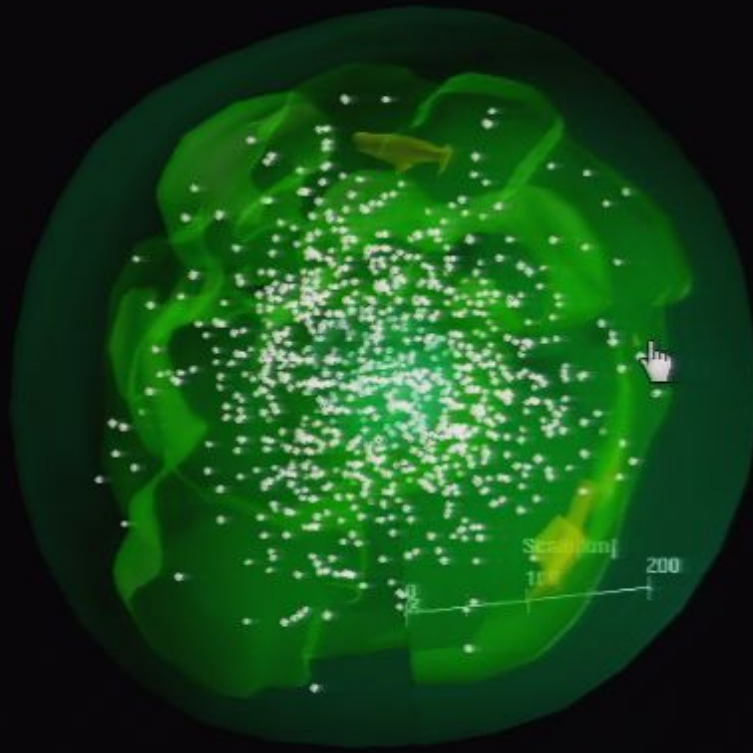
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

t= 0165 ms

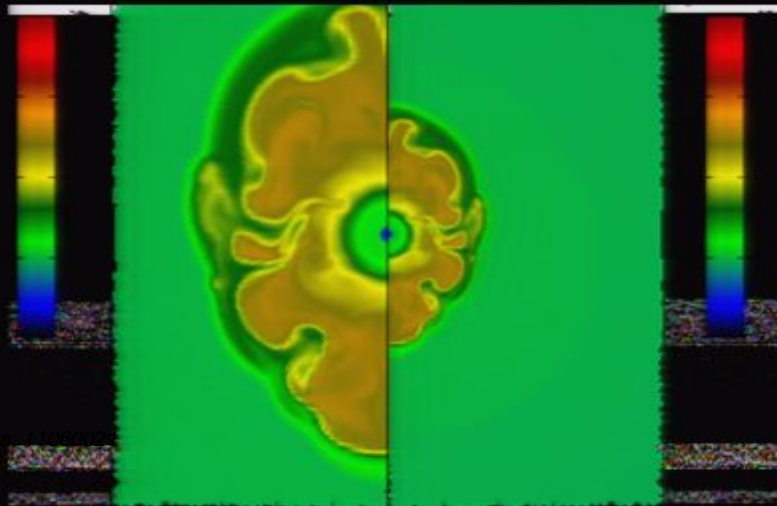
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



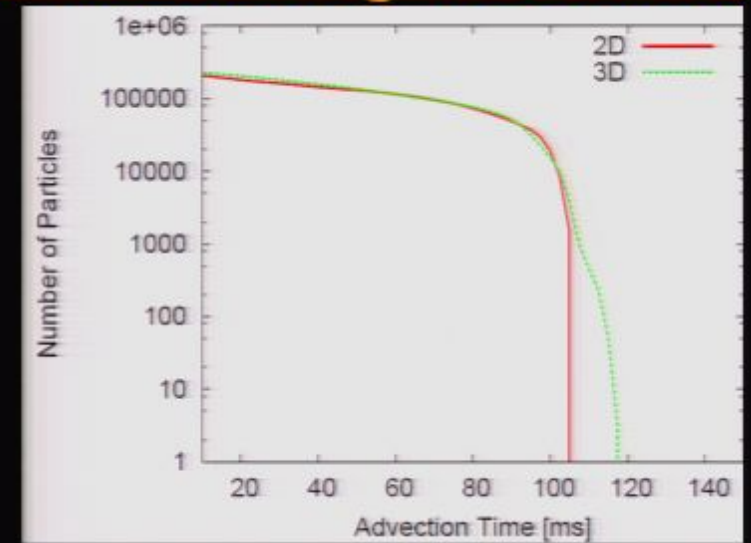
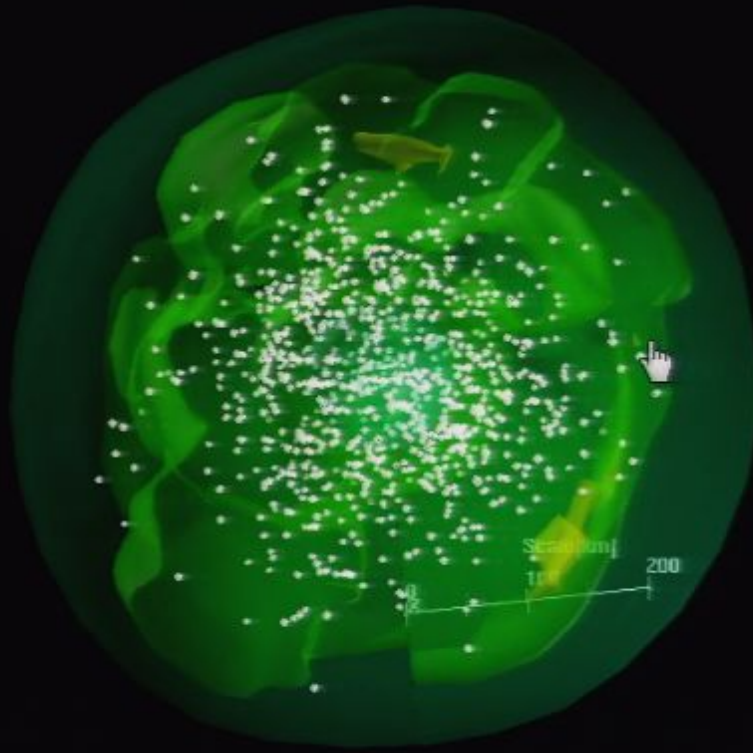
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

t= 0165 ms

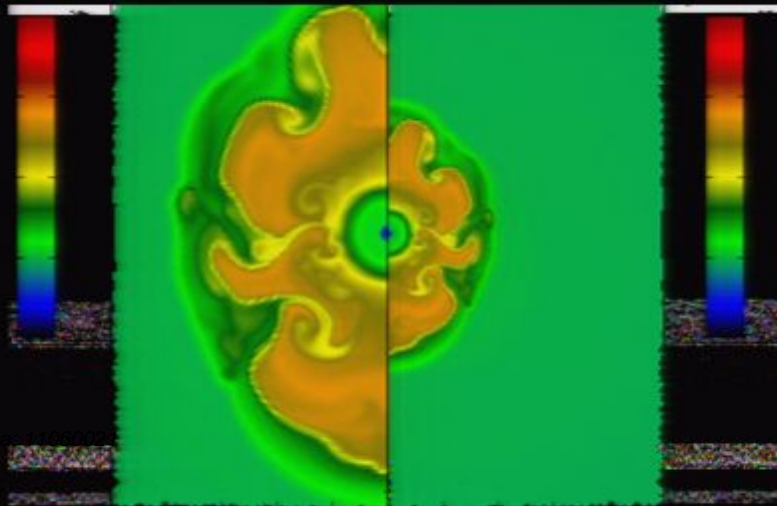
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



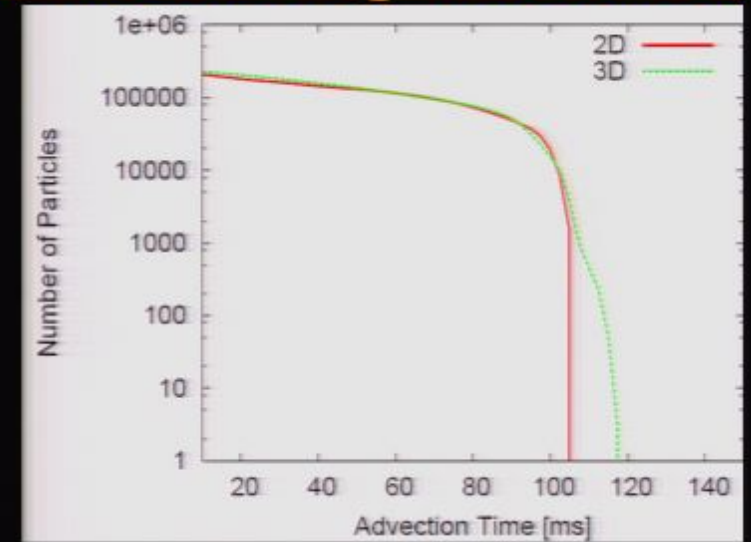
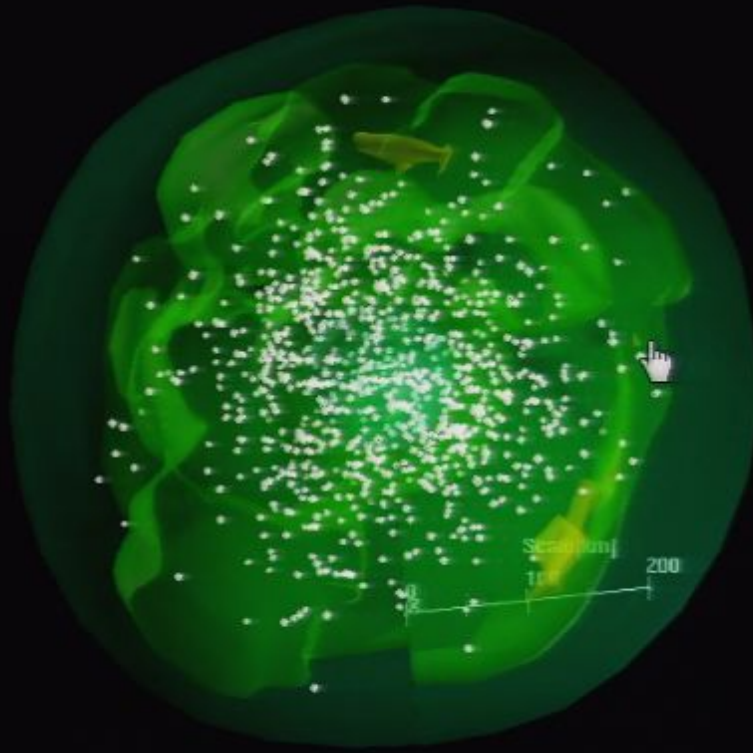
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

t= 0165 ms

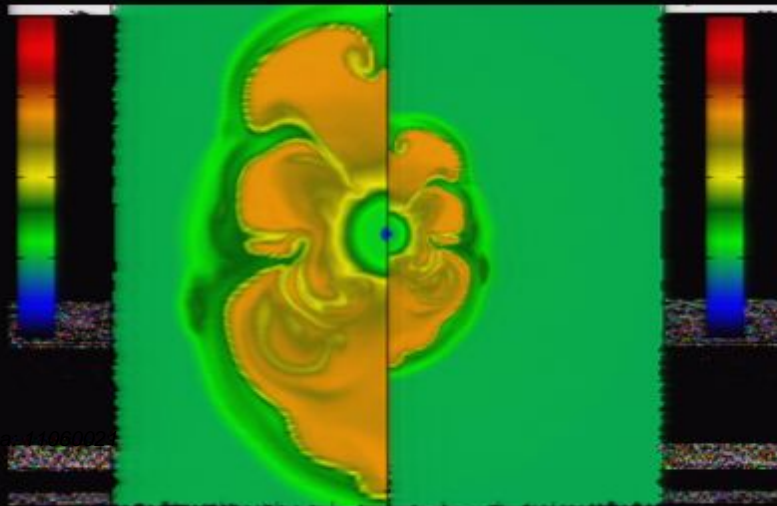
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



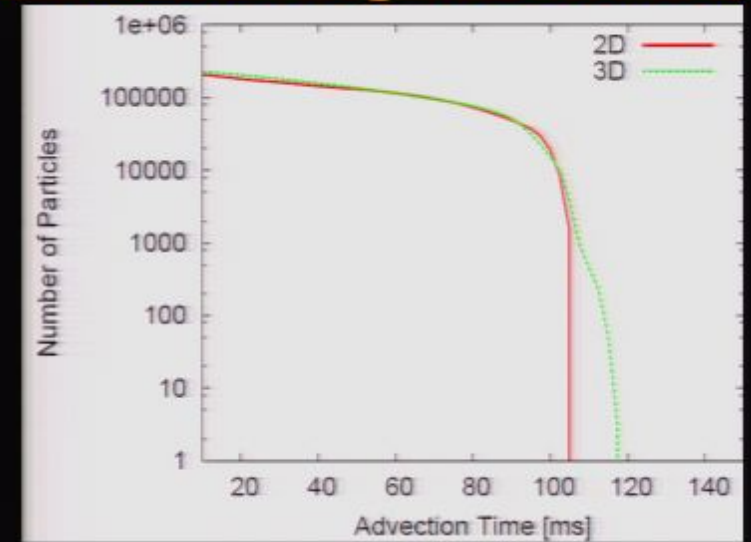
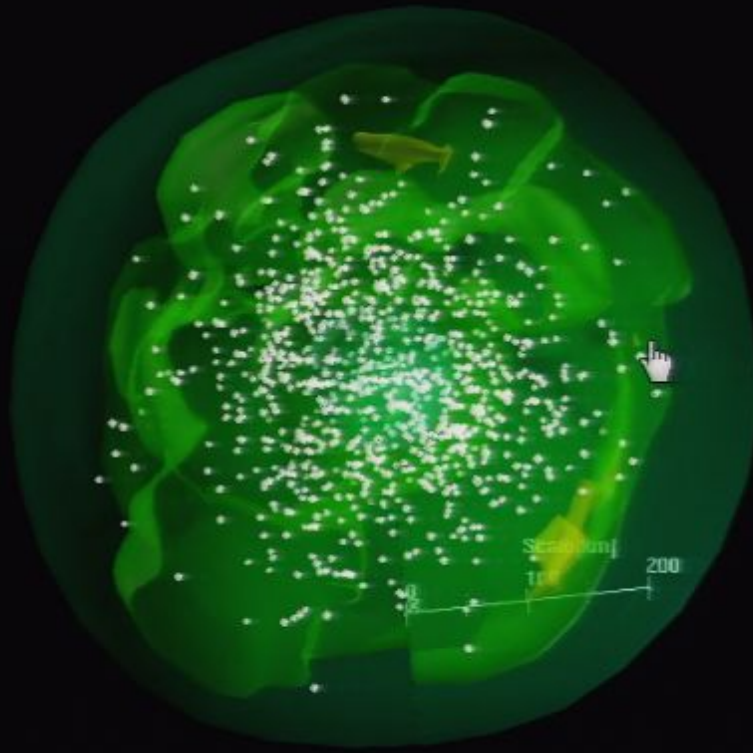
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

t= 0165 ms

Lossions in 3D than 2D ?

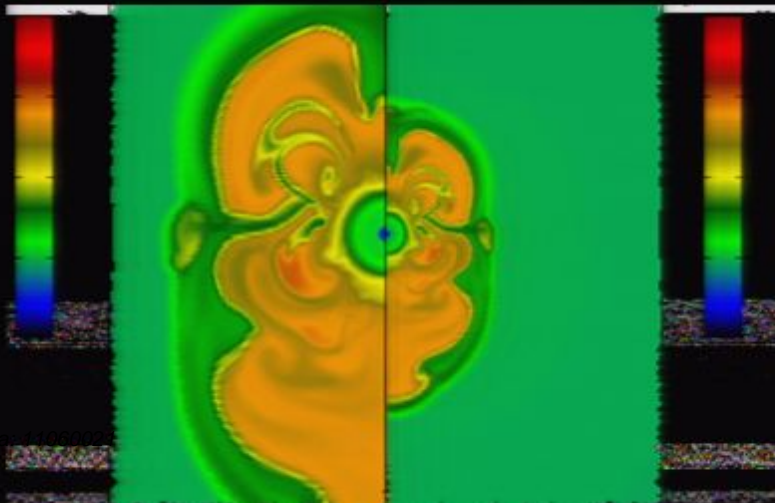
(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.

✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

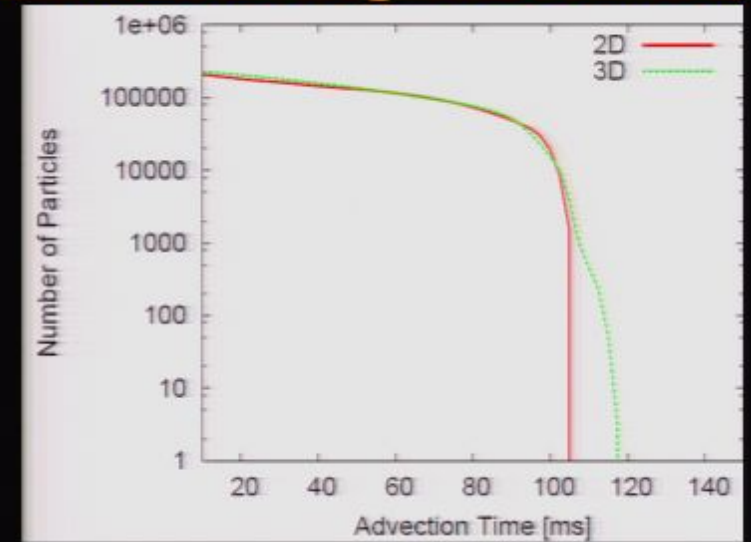
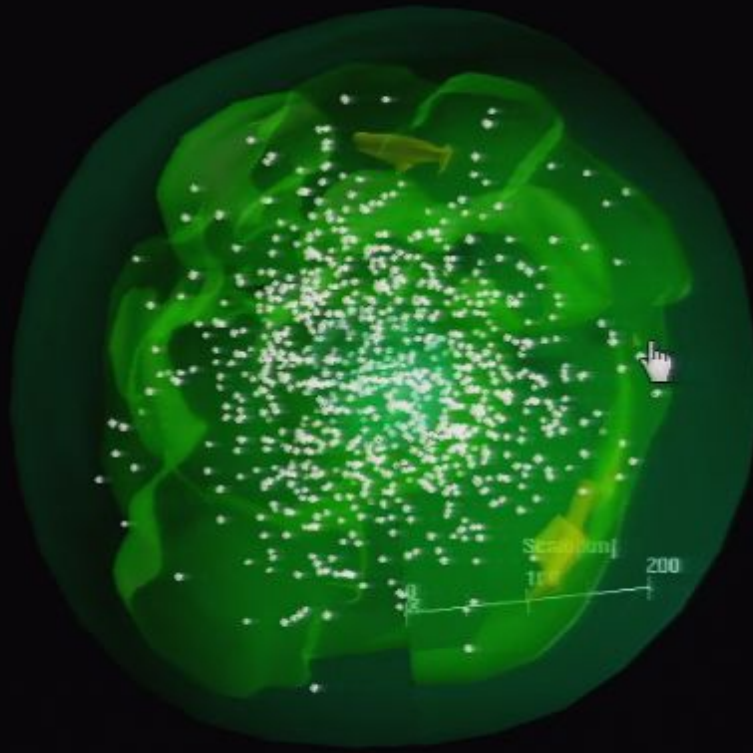


t= 0165 ms

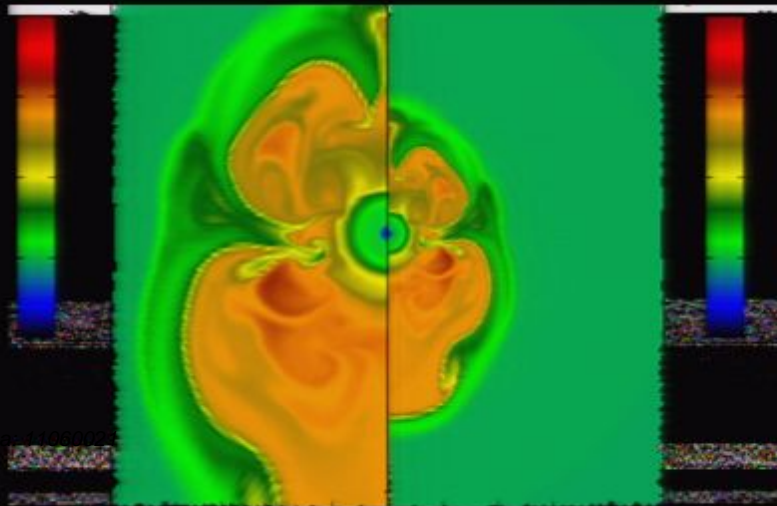
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



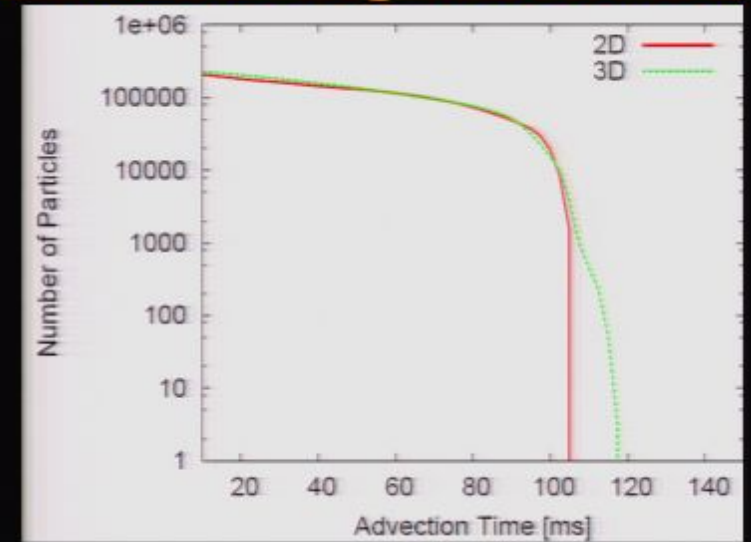
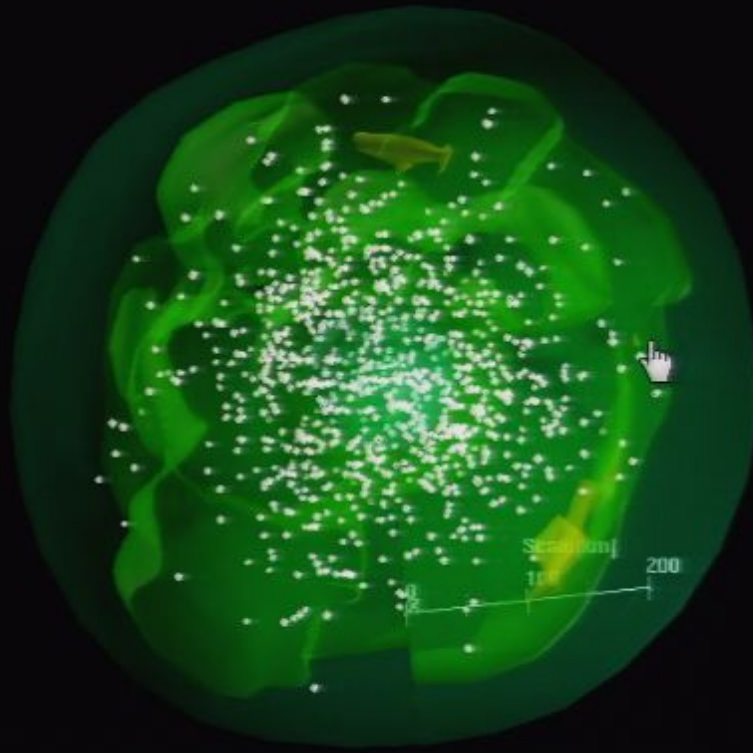
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

t= 0165 ms

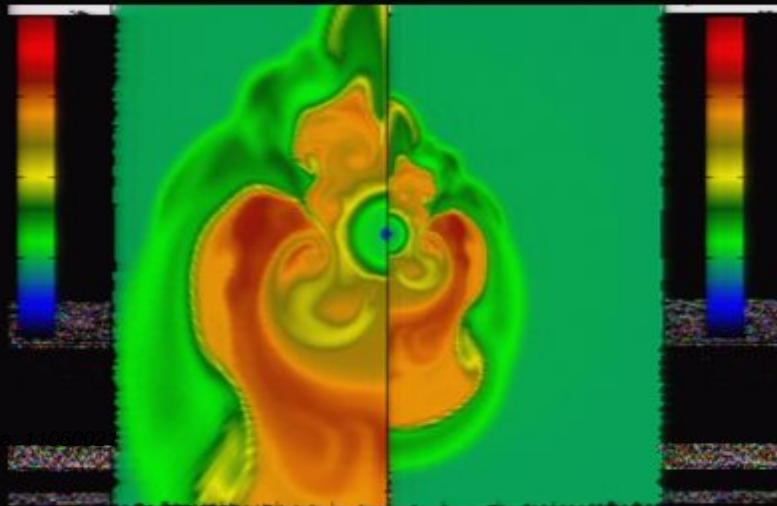
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



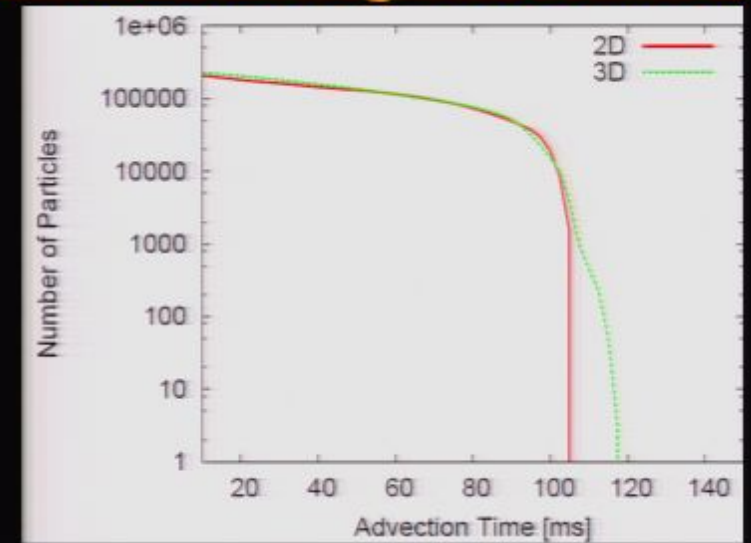
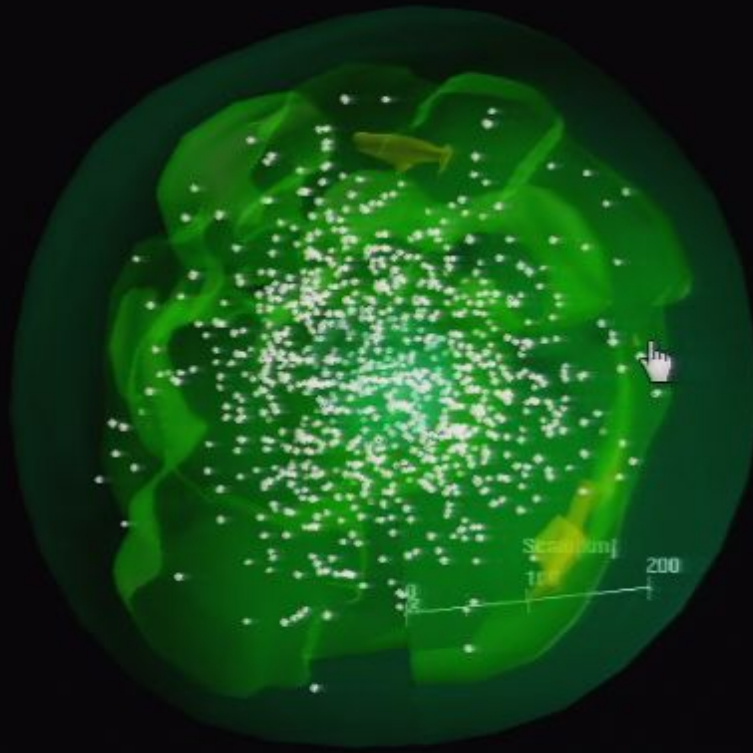
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

t= 0165 ms

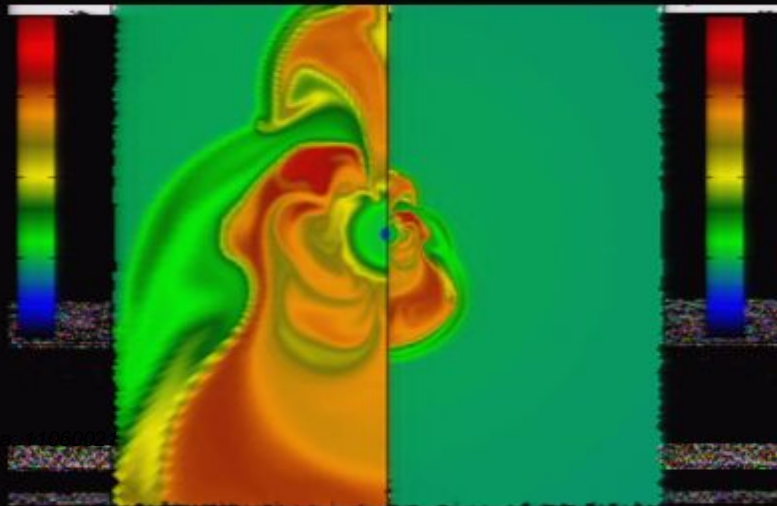
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



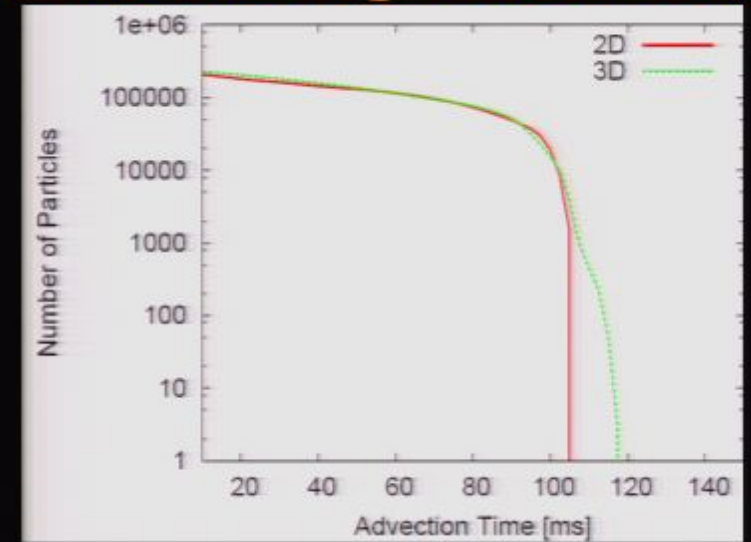
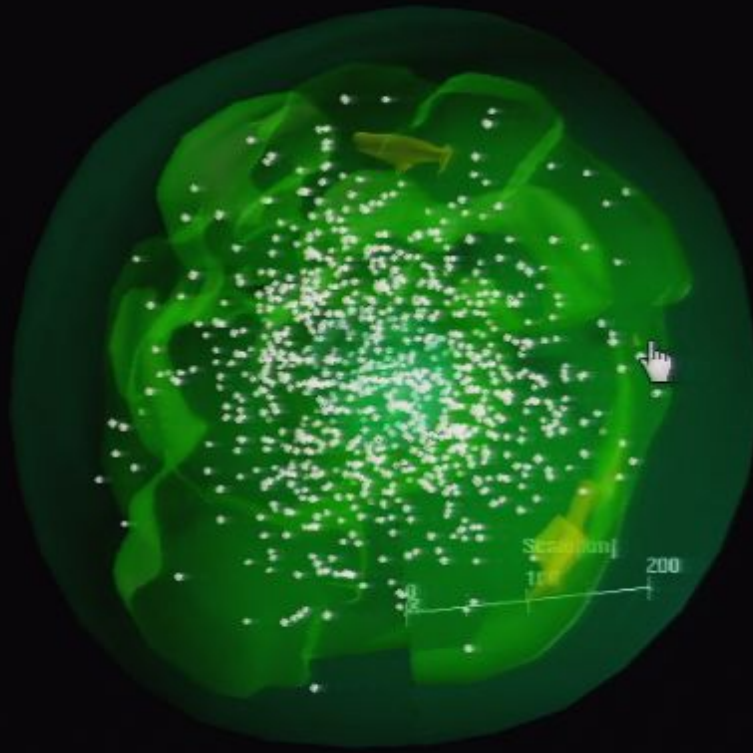
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

t= 0165 ms

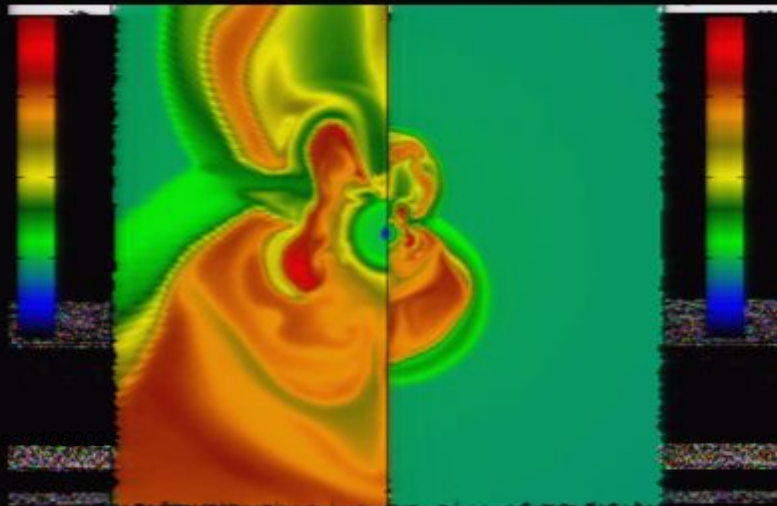
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



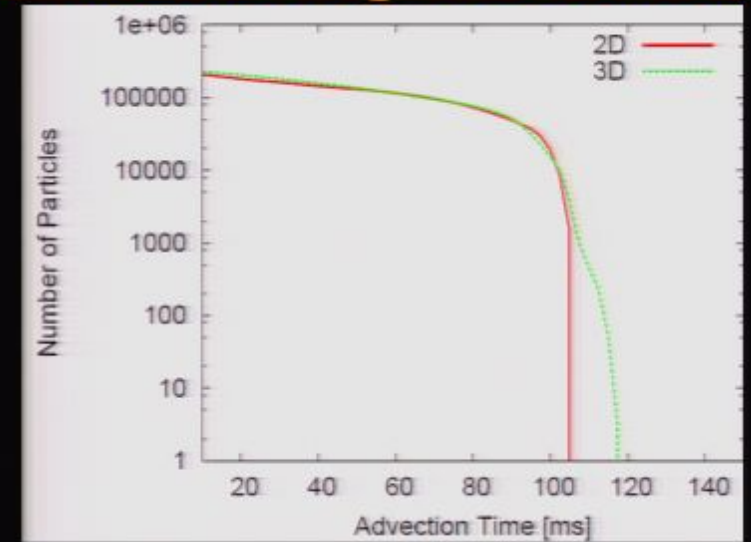
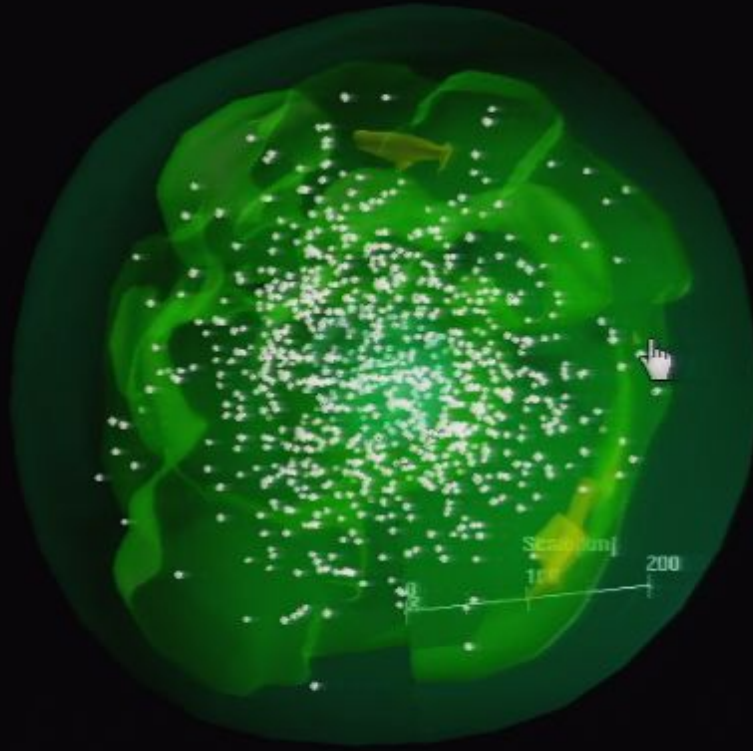
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

t= 0165 ms

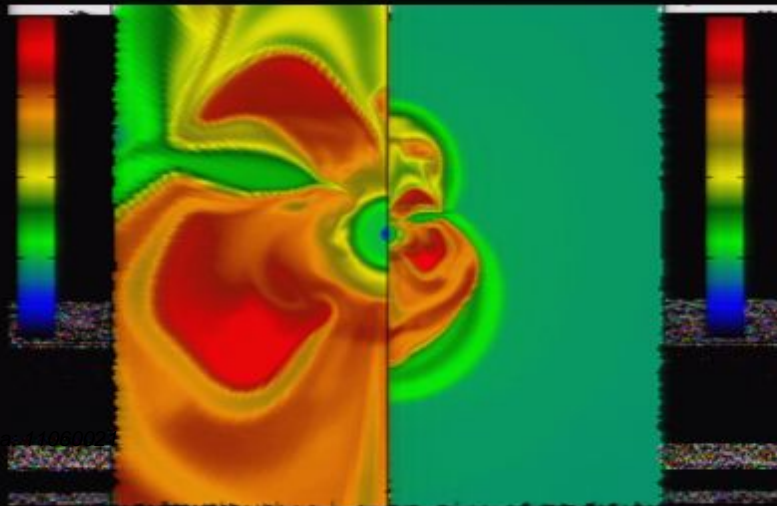
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

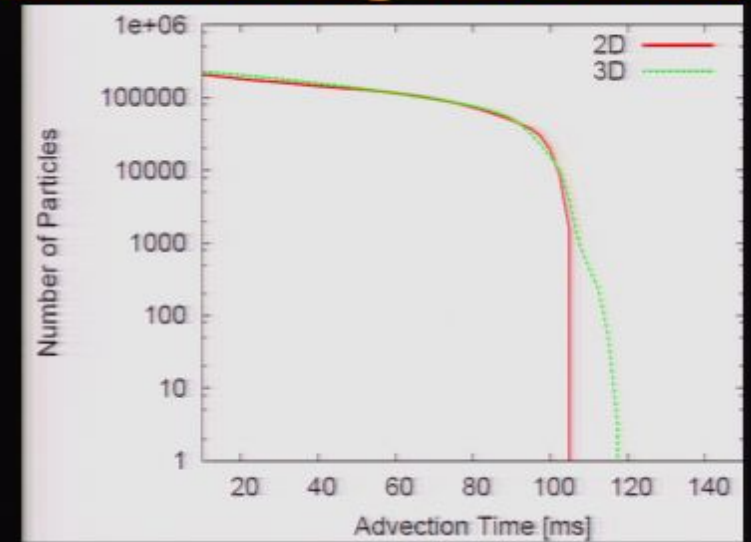
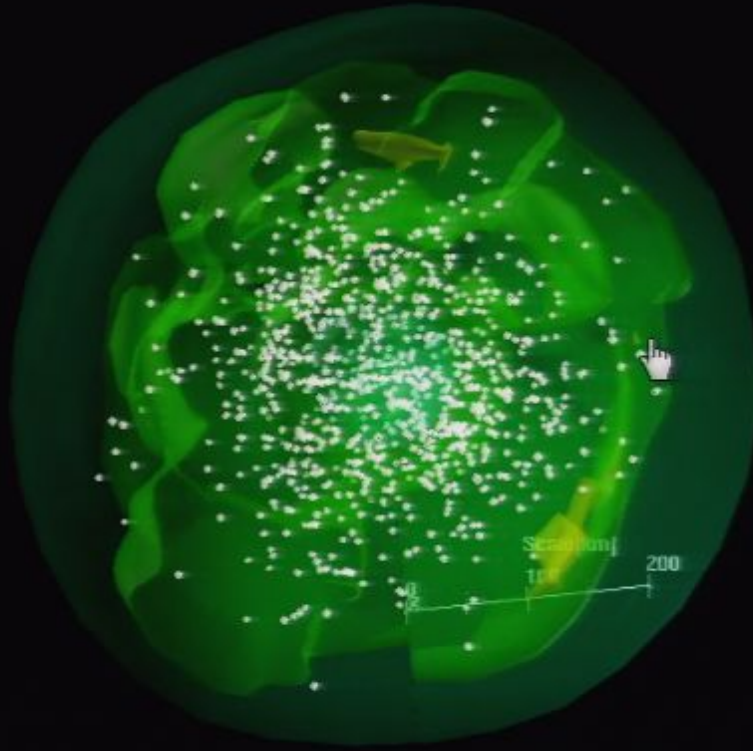
3D simulations with high resolutions are in progress.

t= 0165 ms

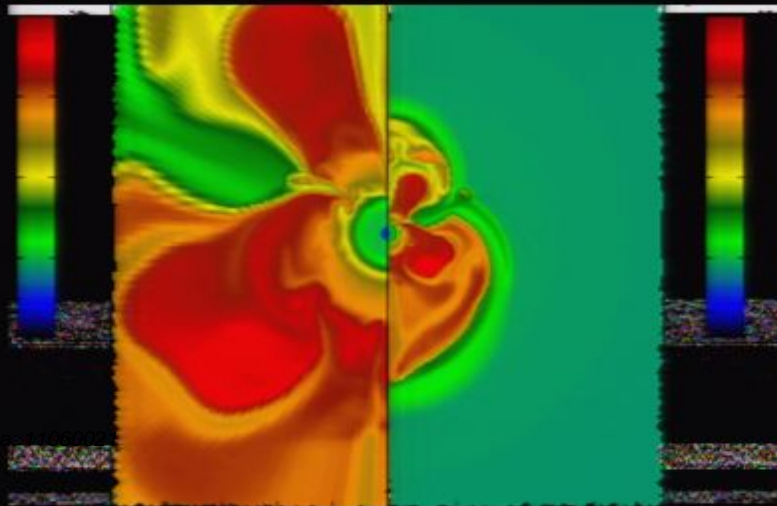
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

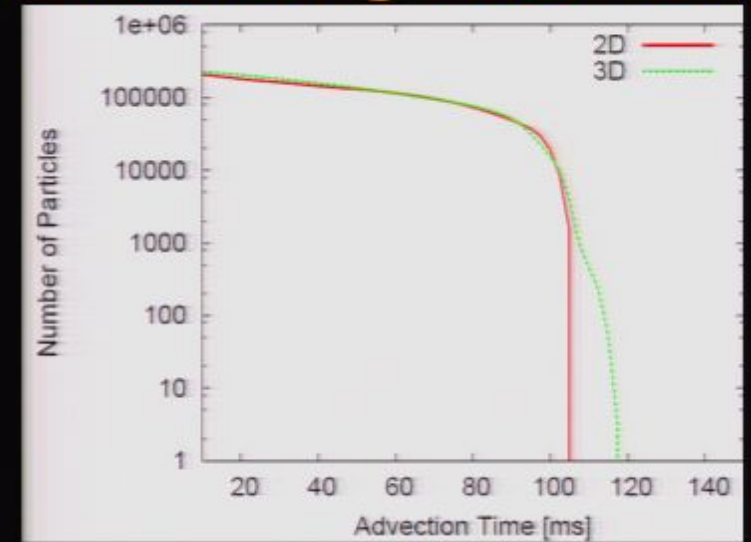
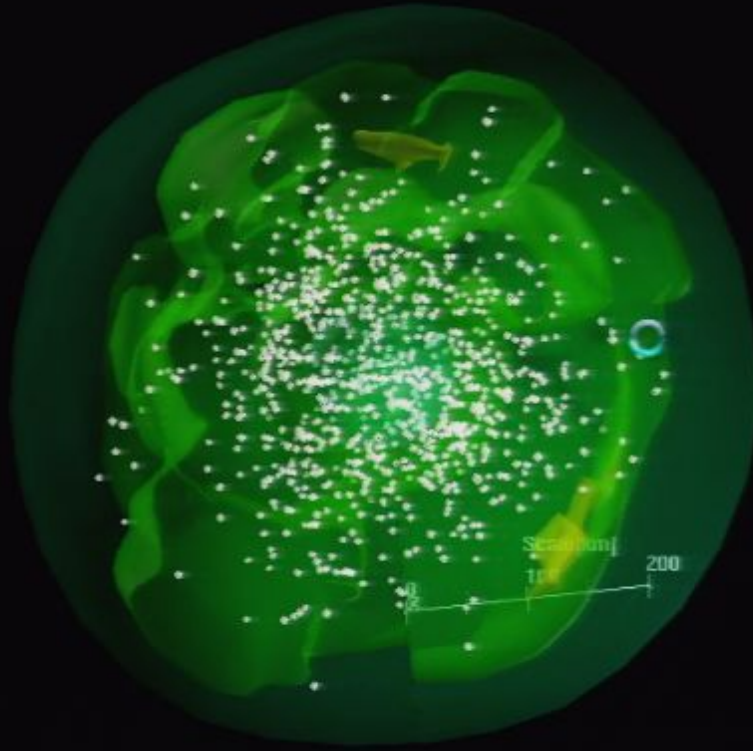
3D simulations with high resolutions are in progress.

t= 0165 ms

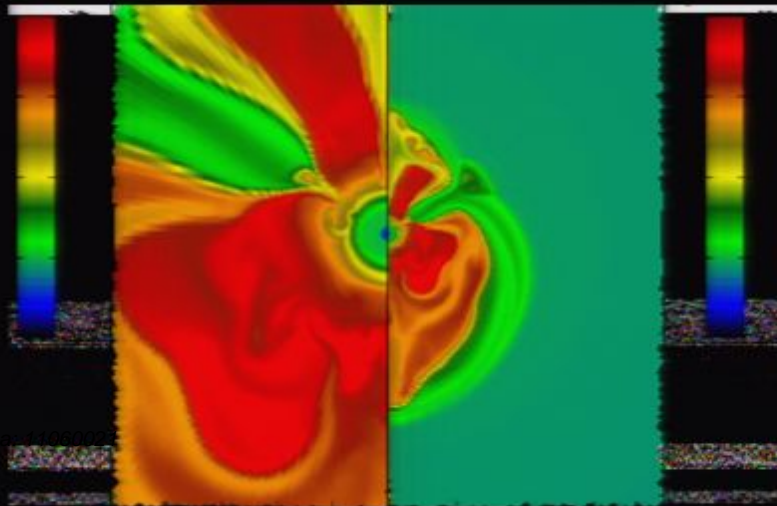
Lossions in 3D than 2D ?

(e.g., Nordhaus et al. (1

✓ For working the neutrino-heating mechanism



The advection timescales become longer in 3D than in 2D.



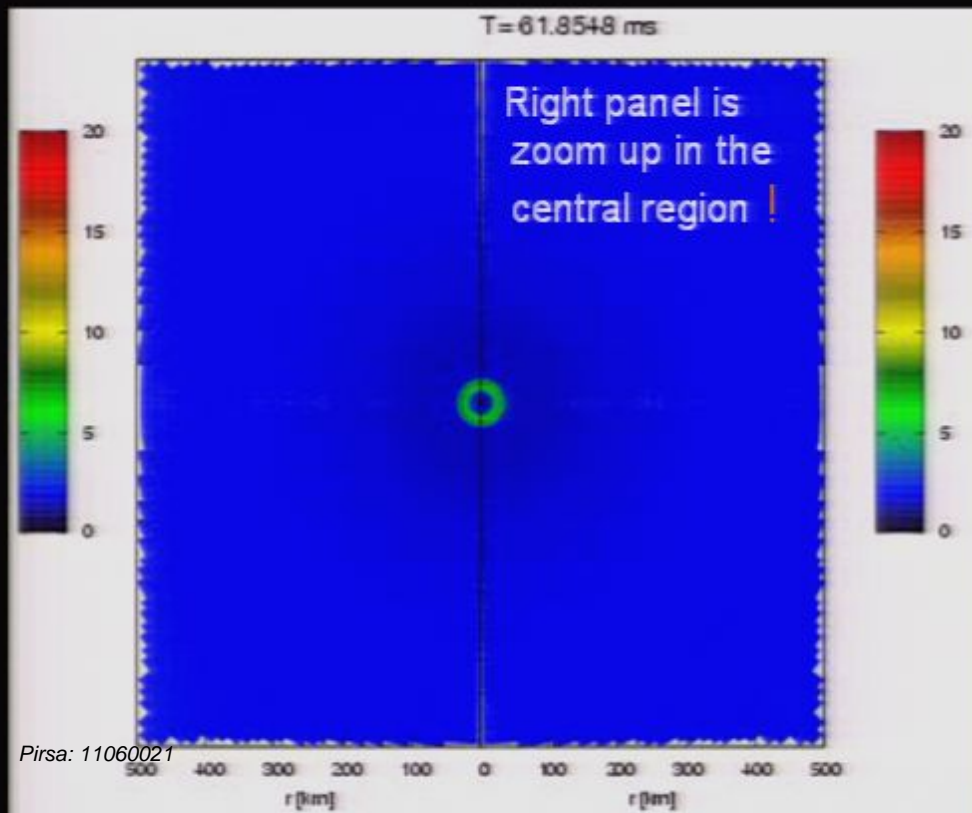
✓ For the hydrodynamic point of view it may be more easier for 2D.
(because matter motions can be concentrated along the special direction)

3D simulations with high resolutions are in progress.

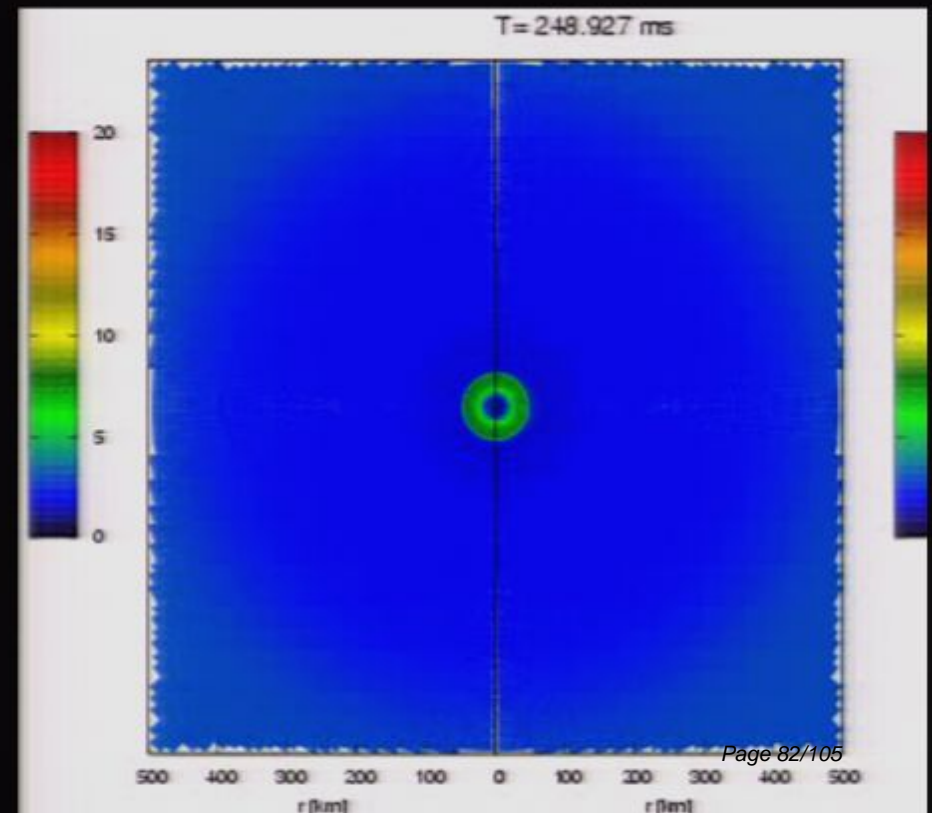
The third lesson is about EOSs(1/2)

- ✓ 2D models of a $15M_{\text{sun}}$ progenitor by WW (1995)
- ✓ The IDSA is implemented (nu_X 's : not yet).

LS EOS(K=180MeV)



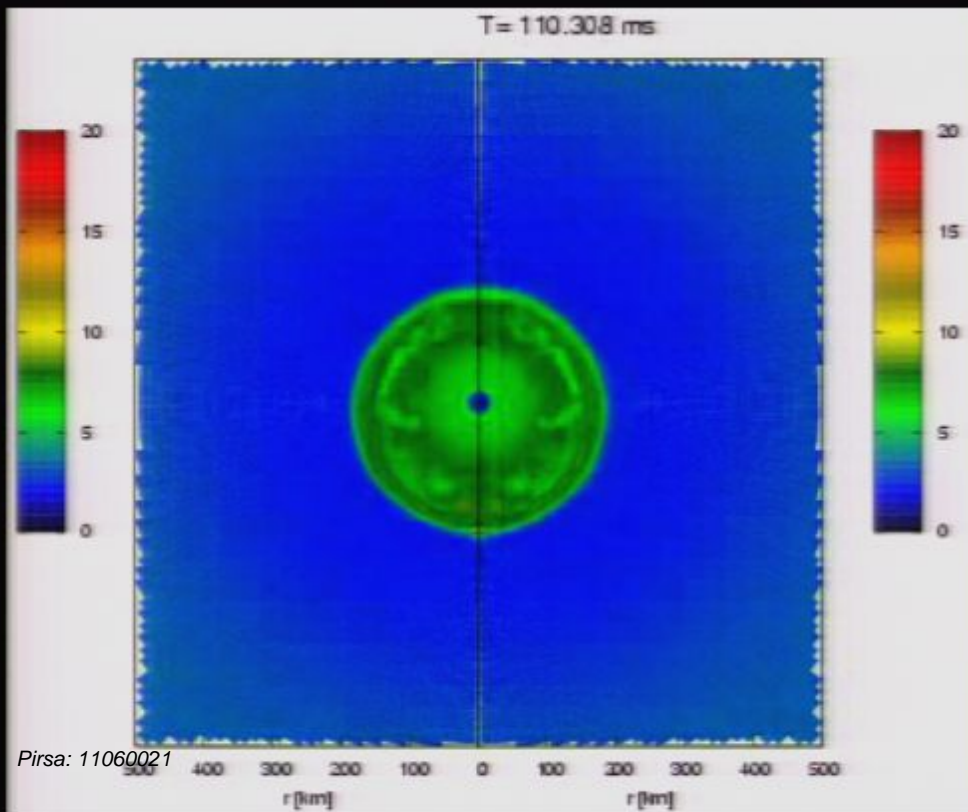
H-Shen EOS(K=281MeV)



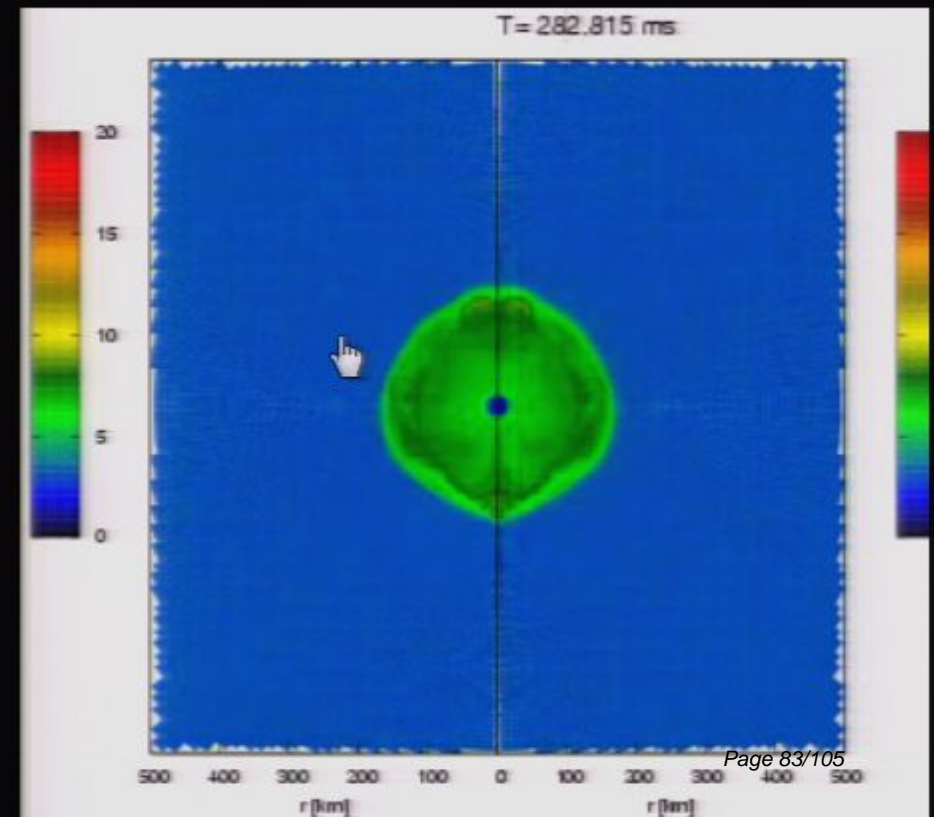
The third lesson is about EOSs(1/2)

- ✓ 2D models of a $15M_{\text{sun}}$ progenitor by WW (1995)
- ✓ The IDSA is implemented (nu_X 's : not yet).

LS EOS(K=180MeV)



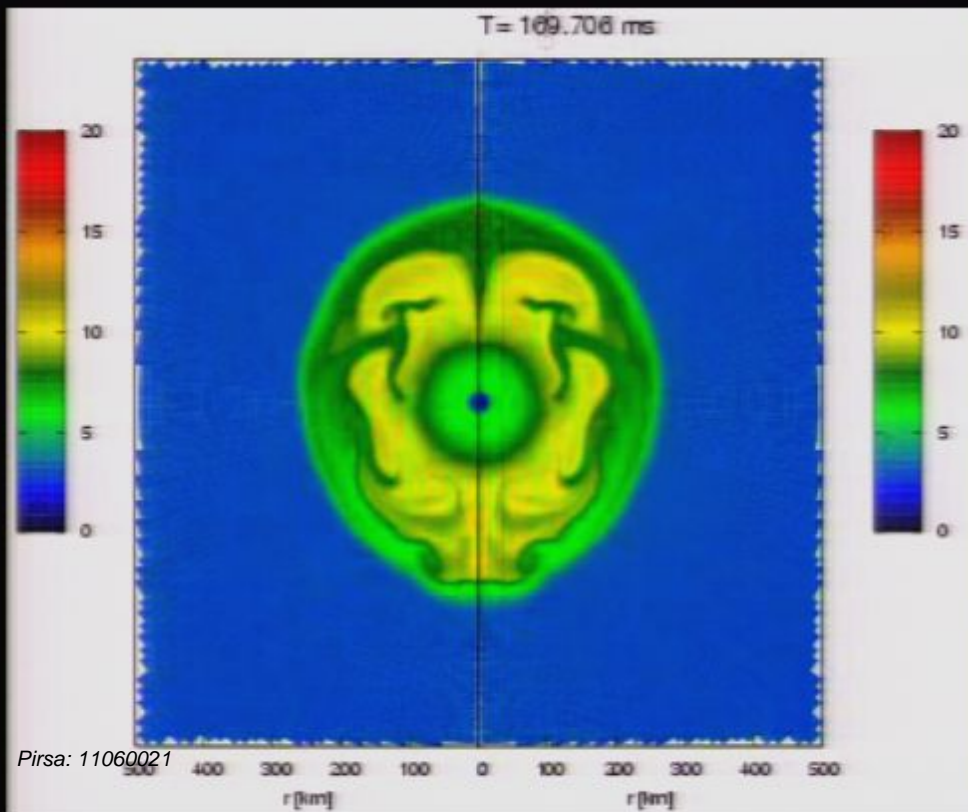
H-Shen EOS(K=281MeV)



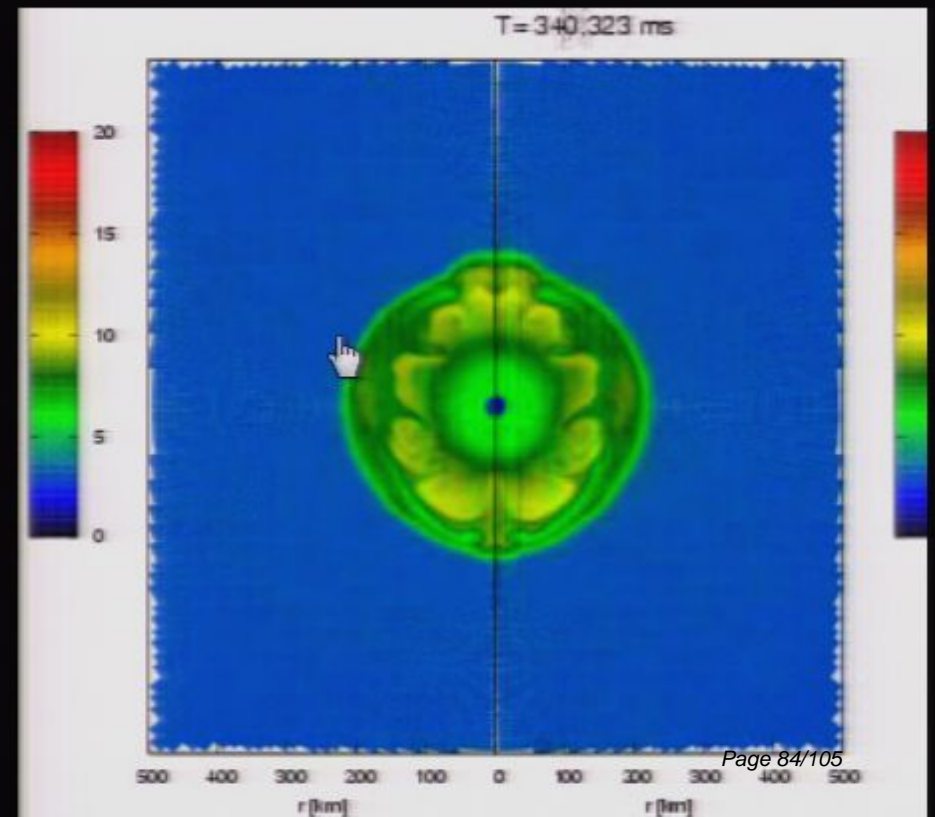
The third lesson is about EOSs(1/2)

- ✓ 2D models of a $15M_{\text{sun}}$ progenitor by WW (1995)
- ✓ The IDSA is implemented (nu_X 's : not yet).

LS EOS(K=180MeV)



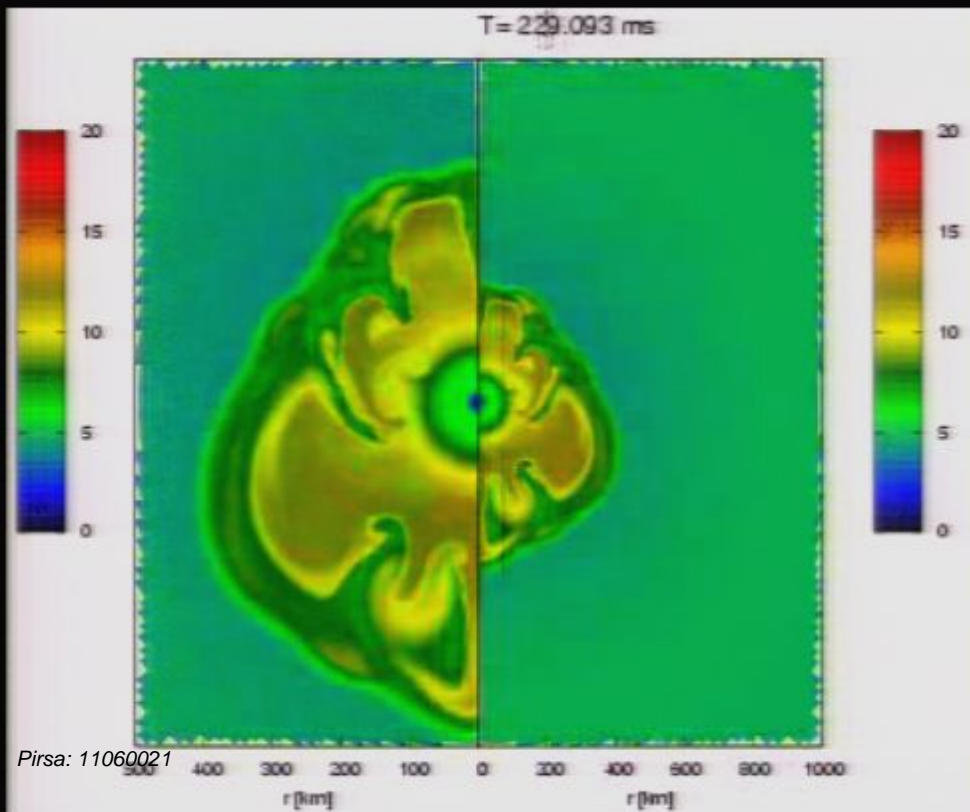
H-Shen EOS(K=281MeV)



The third lesson is about EOSs(1/2)

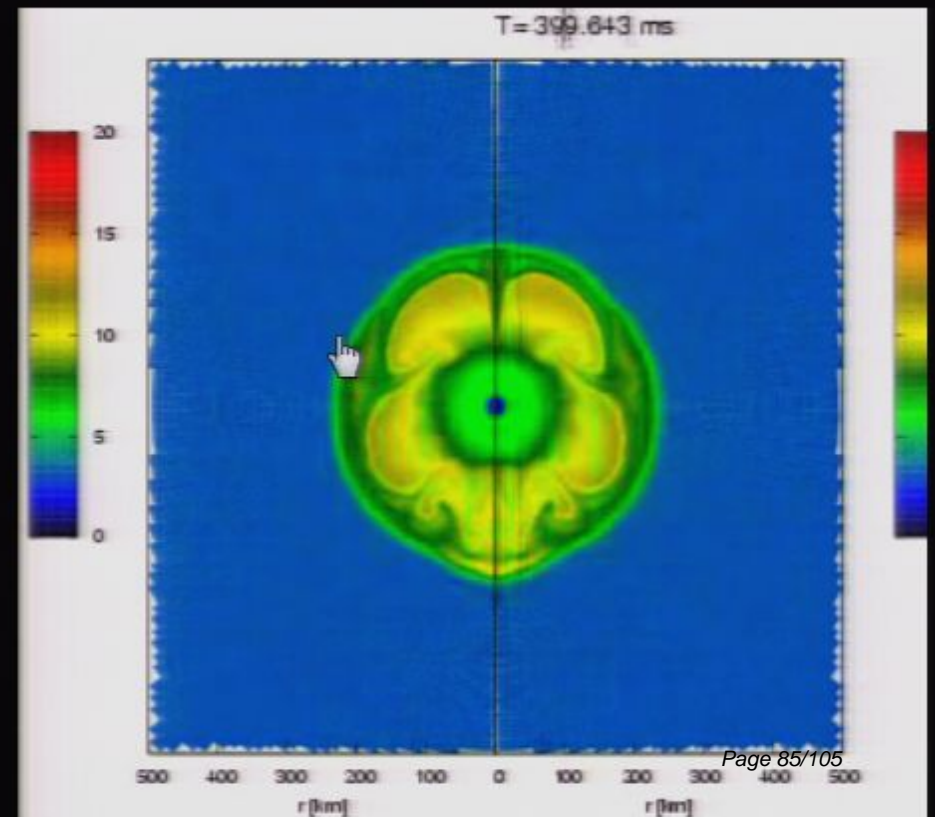
- ✓ 2D models of a $15M_{\text{sun}}$ progenitor by WW (1995)
- ✓ The IDSA is implemented (nu_X 's : not yet).

LS EOS(K=180MeV)



Pirsa: 11060021

H-Shen EOS(K=281MeV)

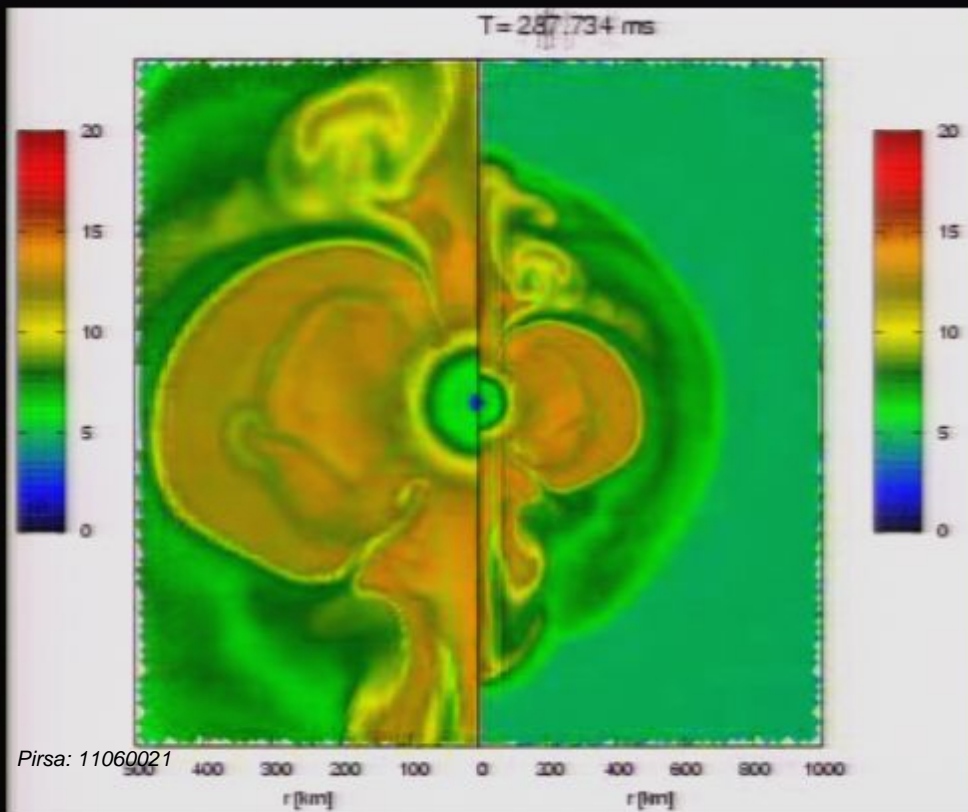


Page 85/105

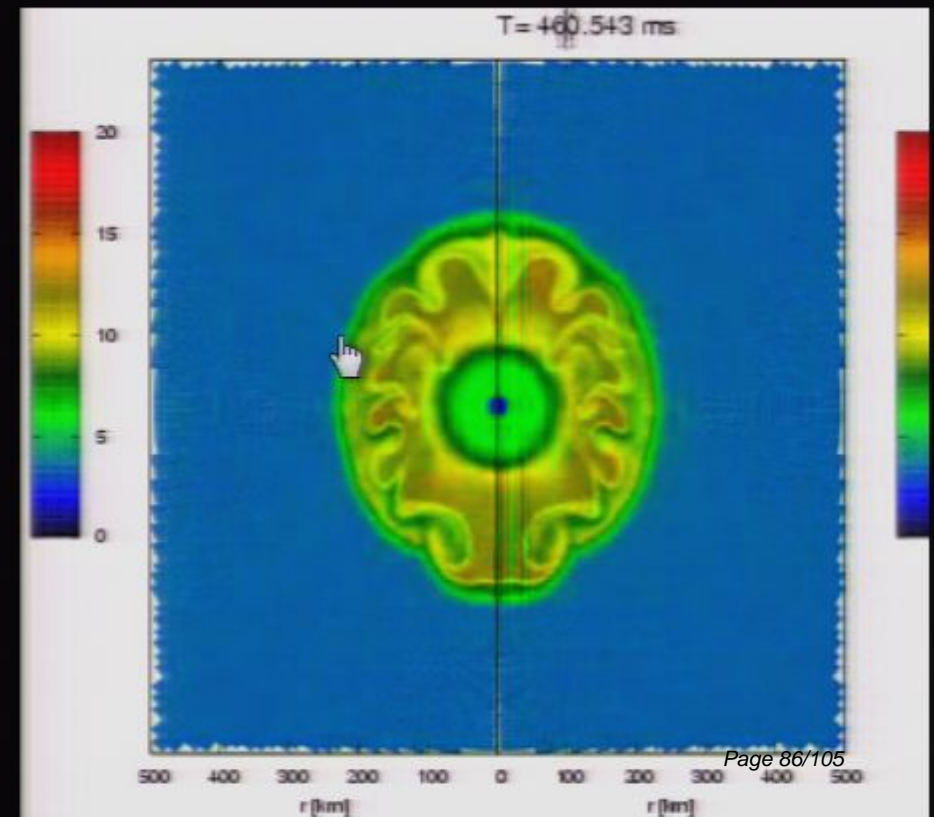
The third lesson is about EOSs(1/2)

- ✓ 2D models of a $15M_{\text{sun}}$ progenitor by WW (1995)
- ✓ The IDSA is implemented (nu_X 's : not yet).

LS EOS(K=180MeV)



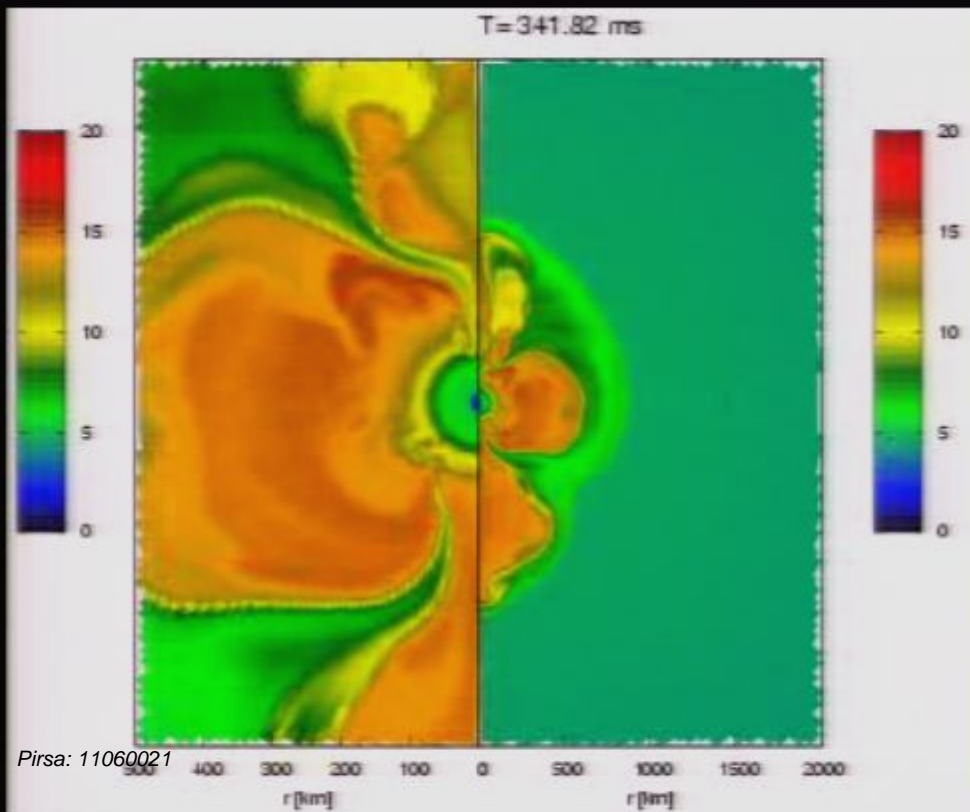
H-Shen EOS(K=281MeV)



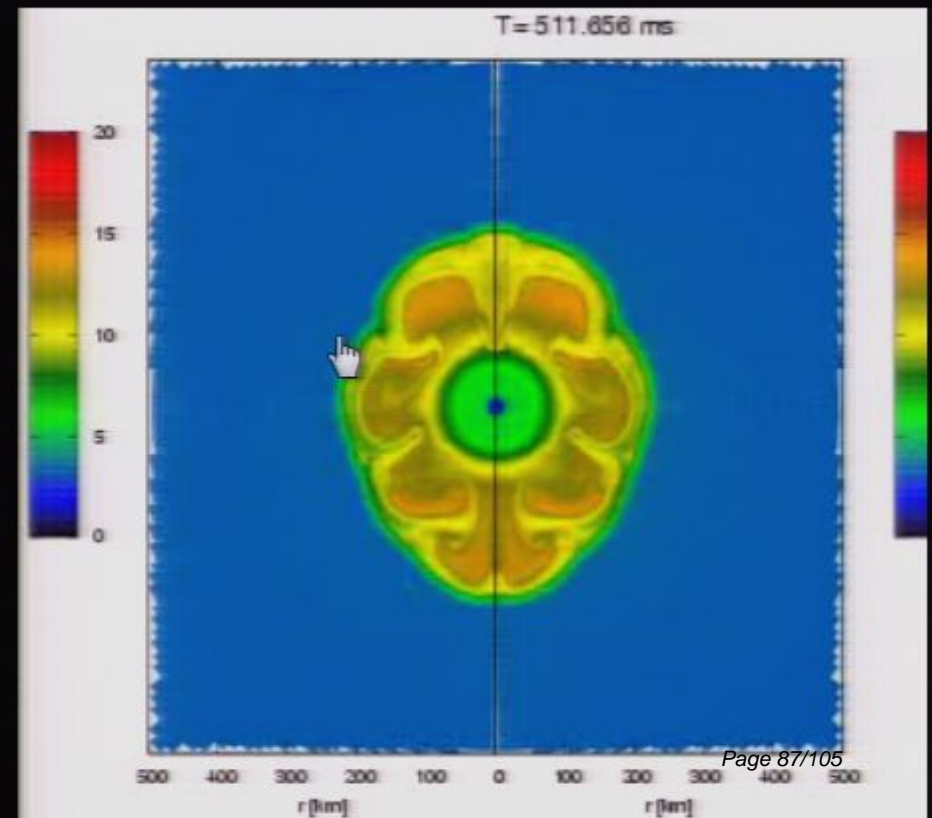
The third lesson is about EOSs(1/2)

- ✓ 2D models of a $15M_{\text{sun}}$ progenitor by WW (1995)
- ✓ The IDSA is implemented (nu_X 's : not yet).

LS EOS(K=180MeV)



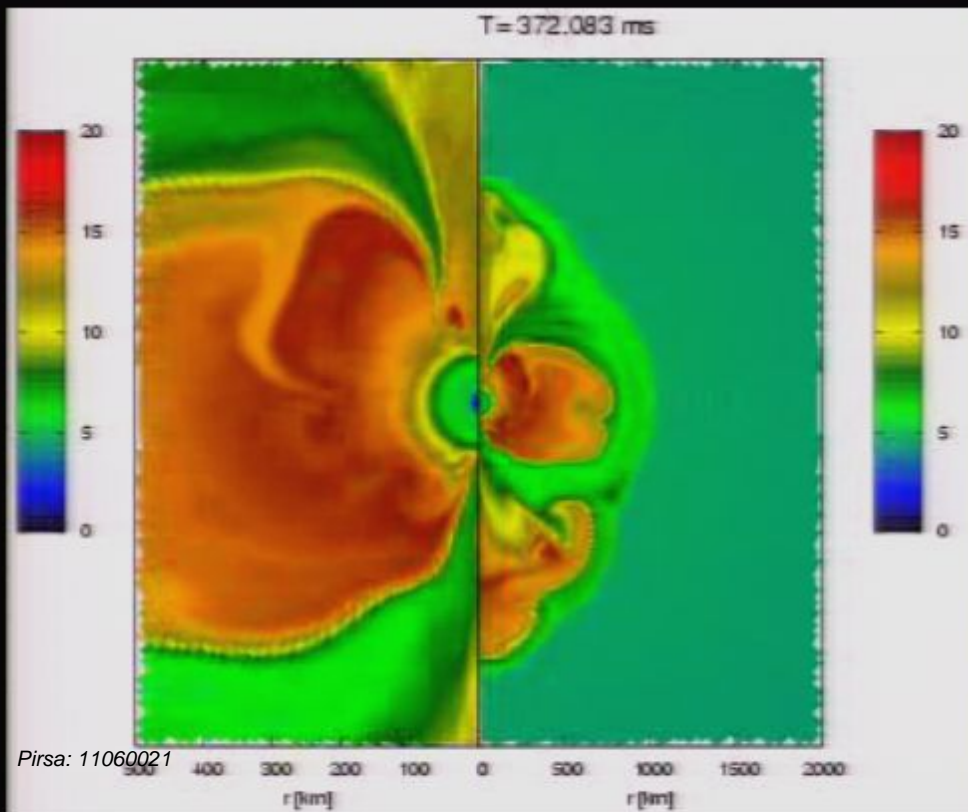
H-Shen EOS(K=281MeV)



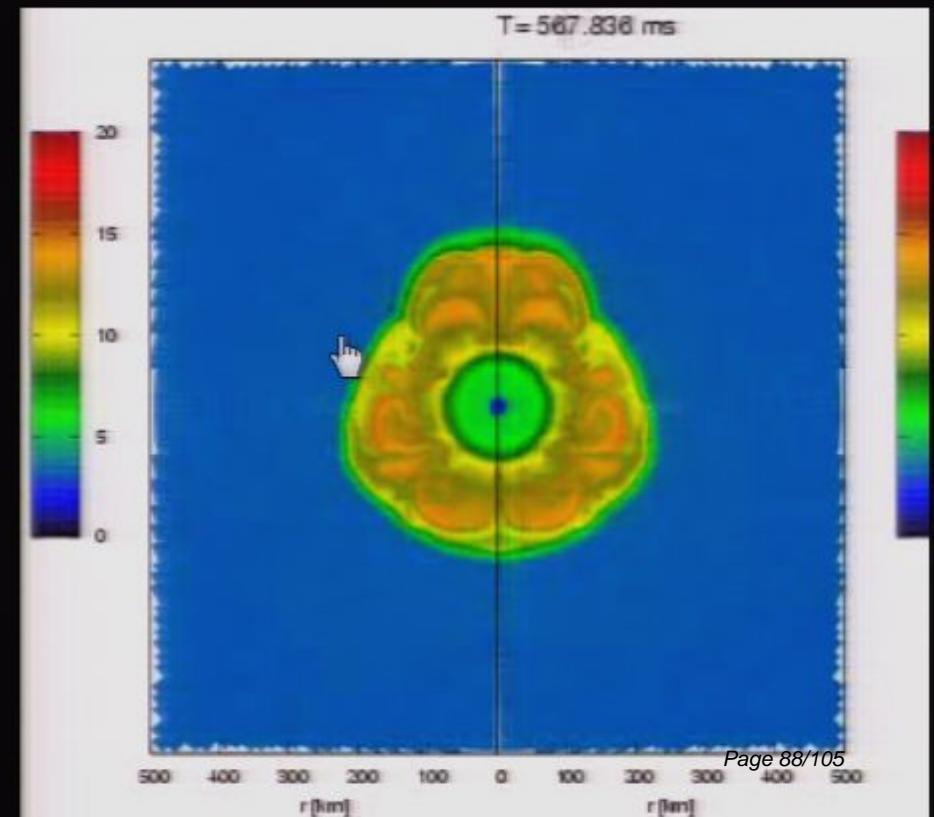
The third lesson is about EOSs(1/2)

- ✓ 2D models of a $15M_{\text{sun}}$ progenitor by WW (1995)
- ✓ The IDSA is implemented (nu_X 's : not yet).

LS EOS(K=180MeV)



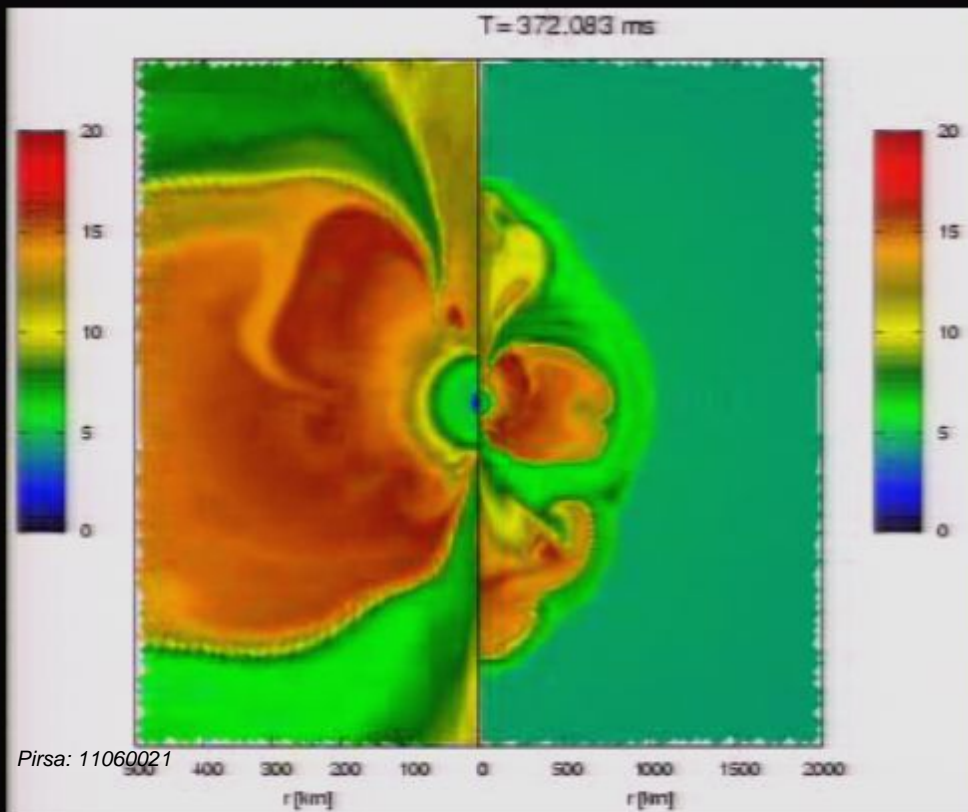
H-Shen EOS(K=281MeV)



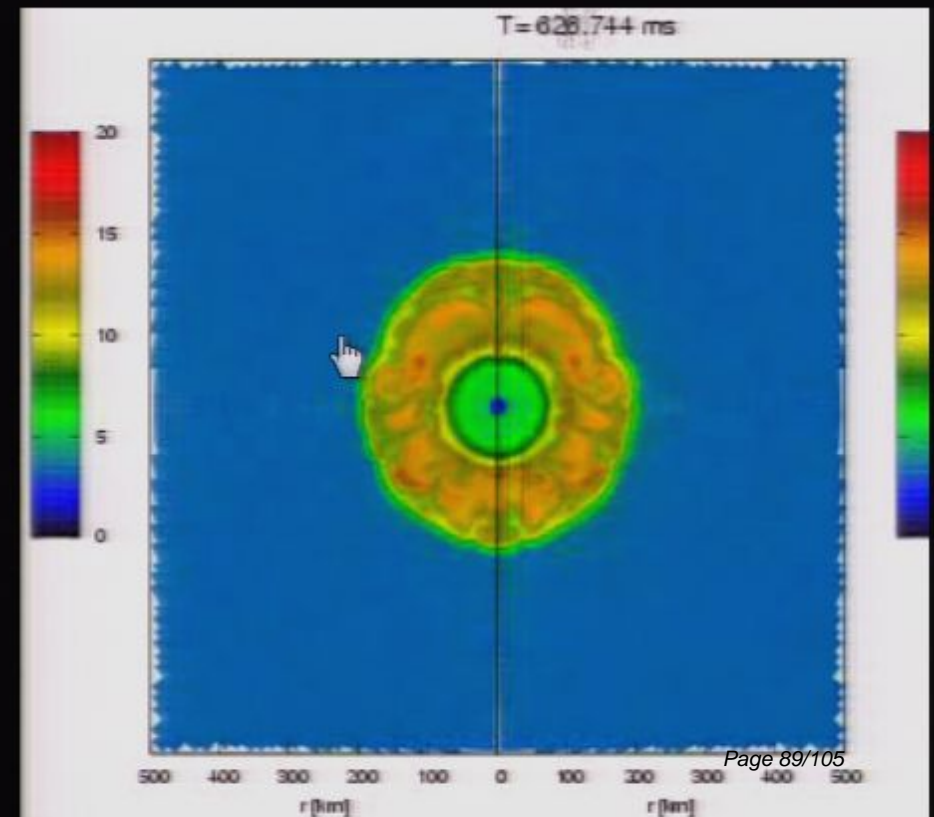
The third lesson is about EOSs(1/2)

- ✓ 2D models of a $15M_{\text{sun}}$ progenitor by WW (1995)
- ✓ The IDSA is implemented (nu_X 's : not yet).

LS EOS(K=180MeV)



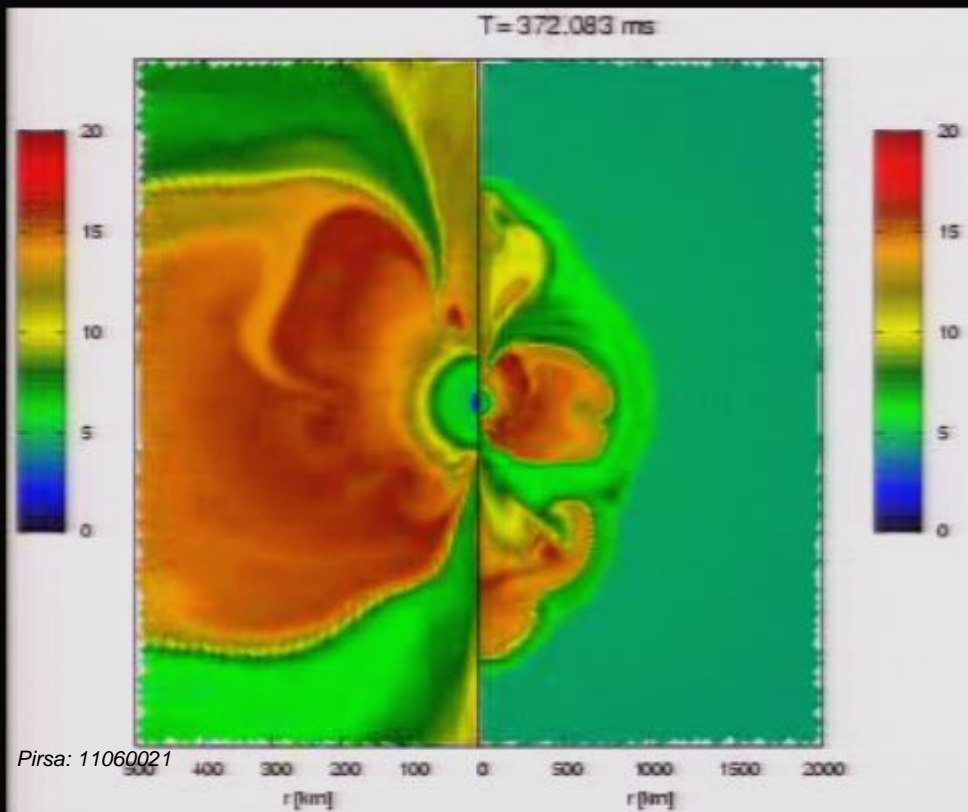
H-Shen EOS(K=281MeV)



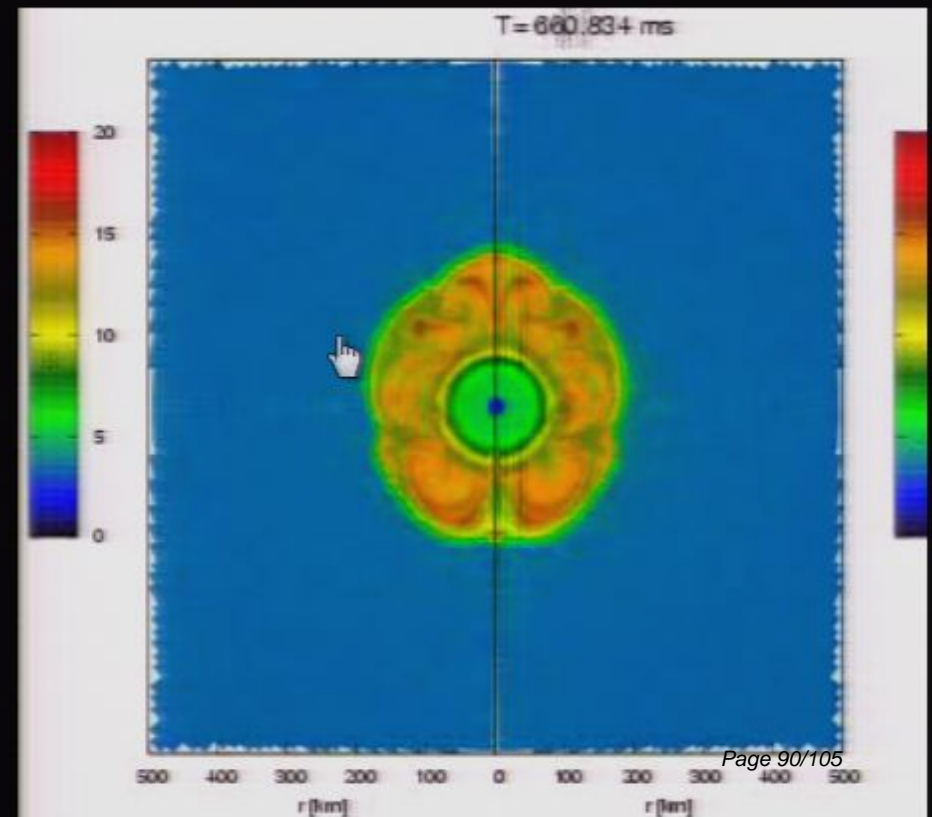
The third lesson is about EOSs(1/2)

- ✓ 2D models of a $15M_{\text{sun}}$ progenitor by WW (1995)
- ✓ The IDSA is implemented (nu_X 's : not yet).

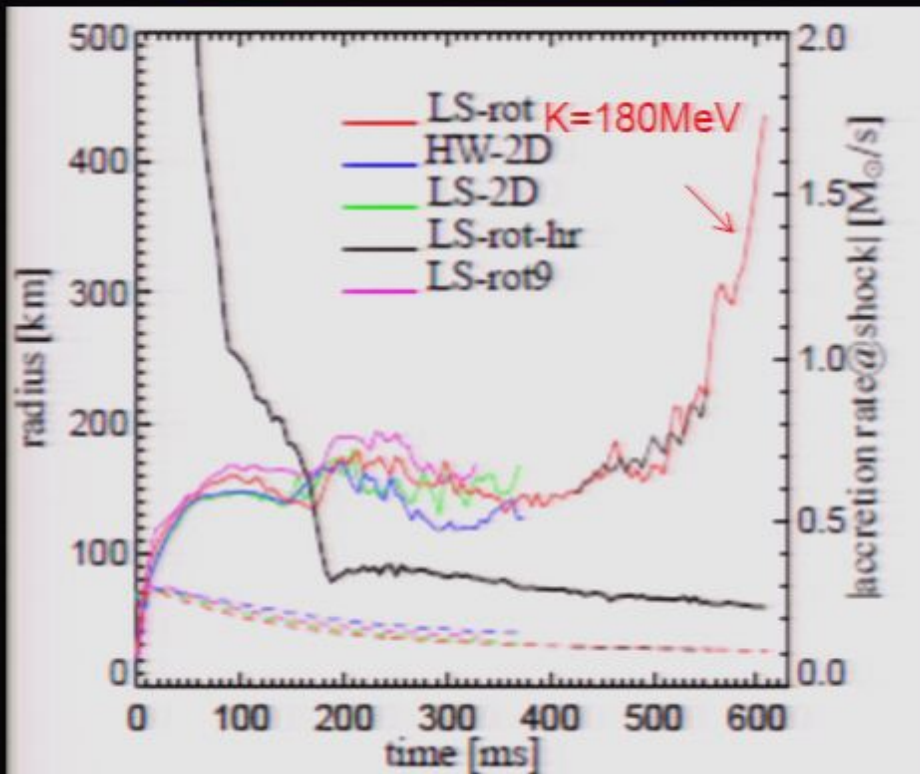
LS EOS(K=180MeV)



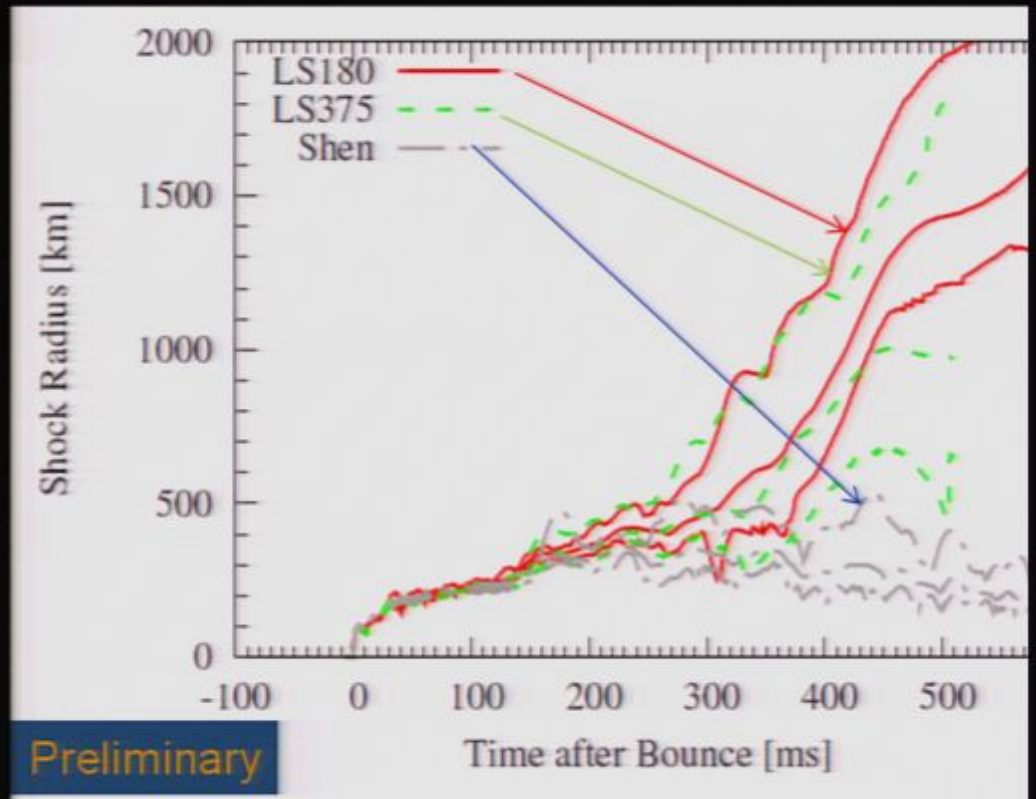
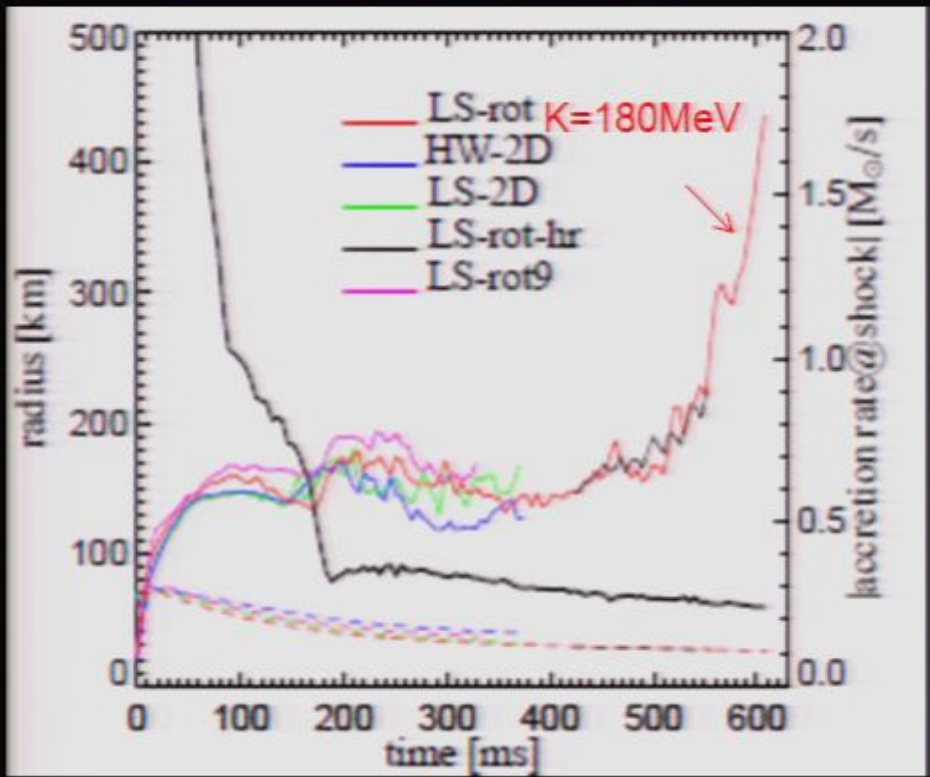
H-Shen EOS(K=281MeV)



Marek & Janka (2009)

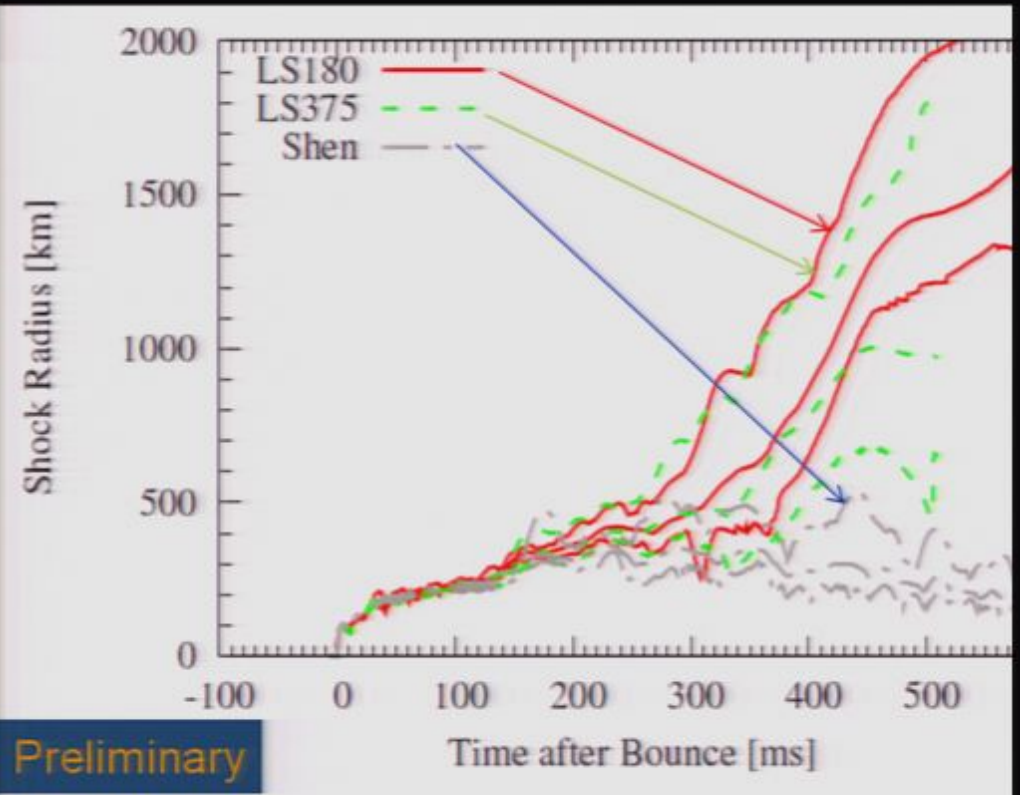
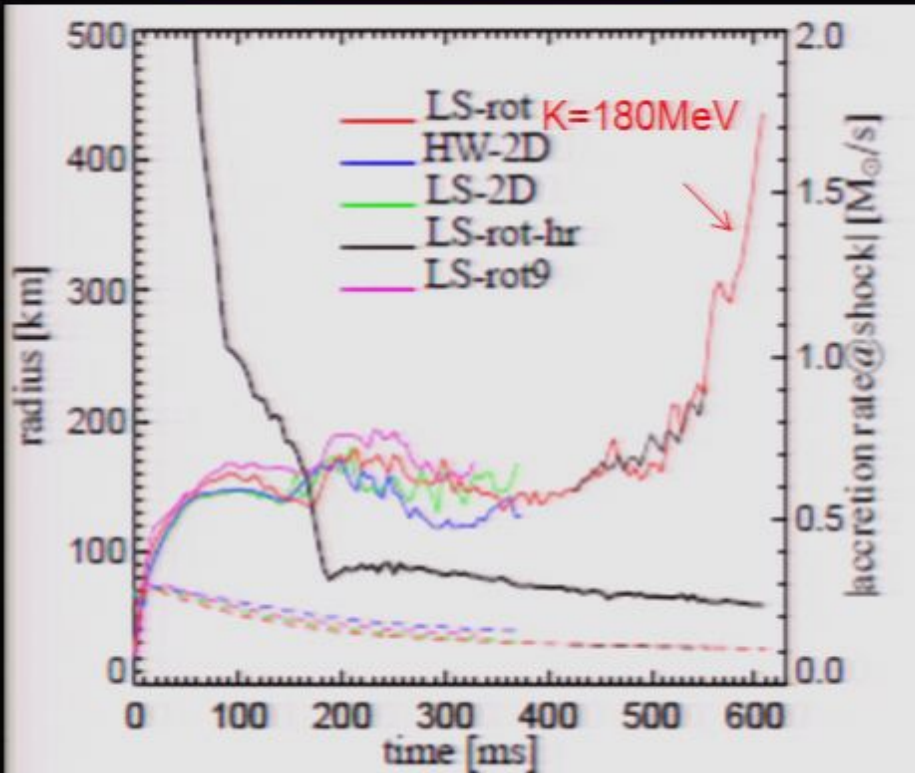


Marek & Janka (2009)

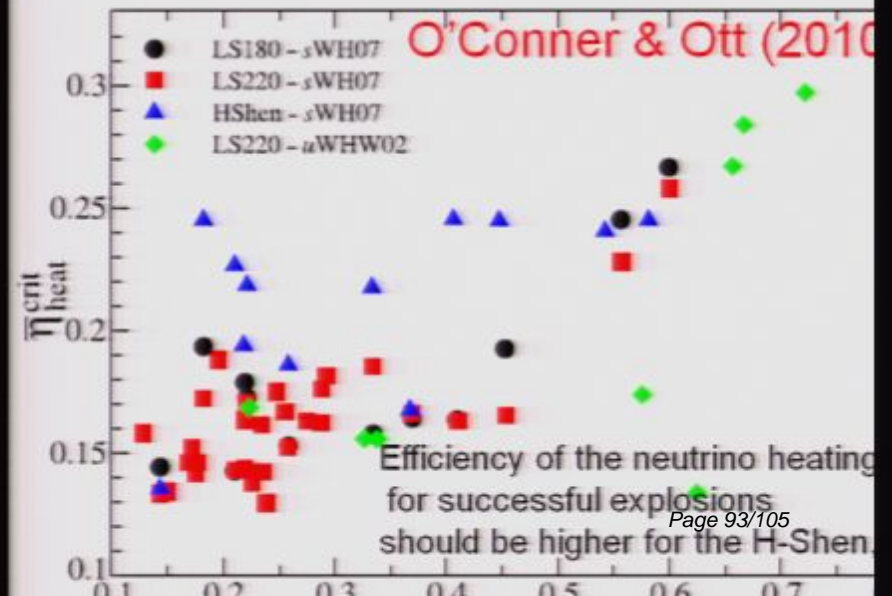


Preliminary

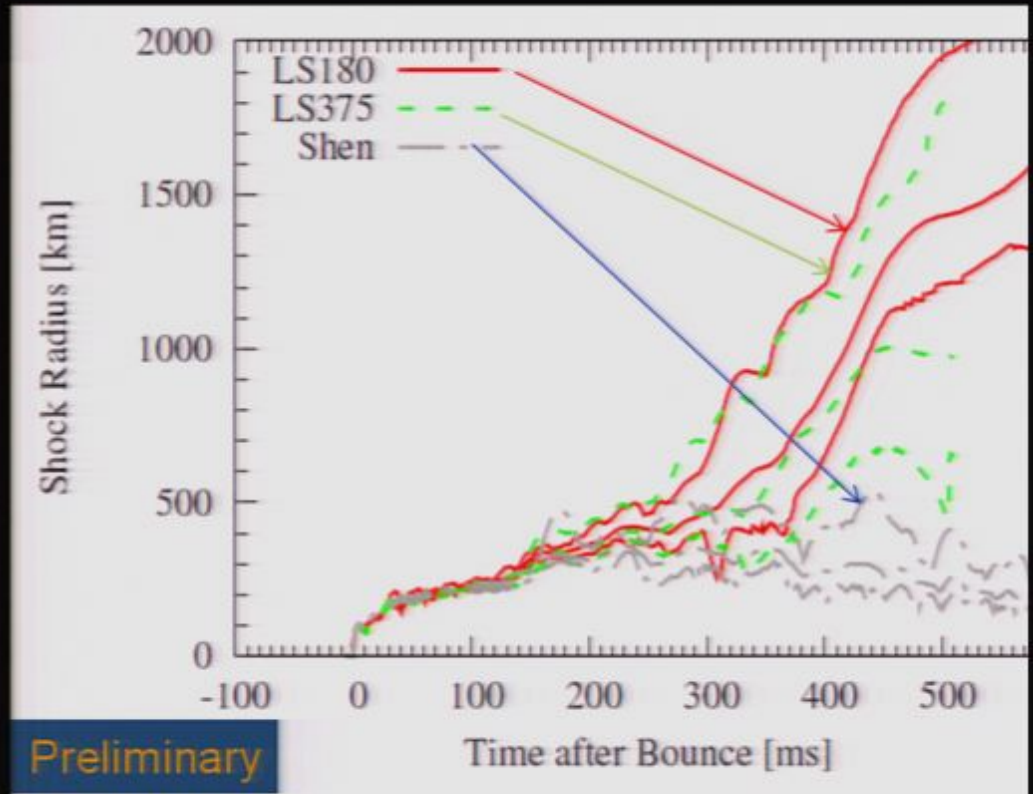
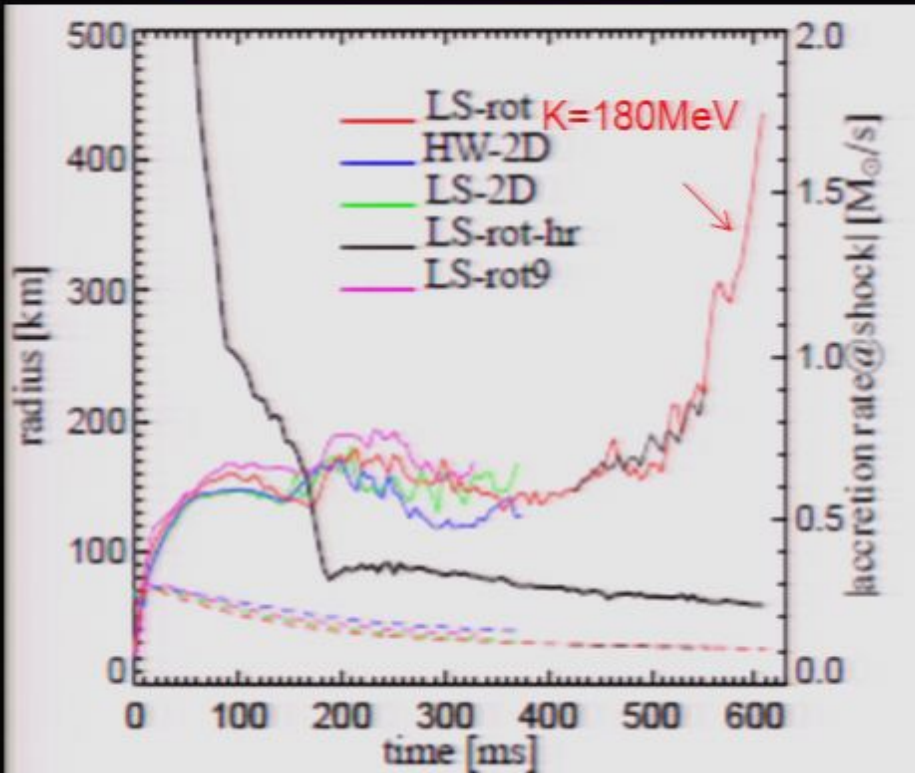
Marek & Janka (2009)



Preliminary

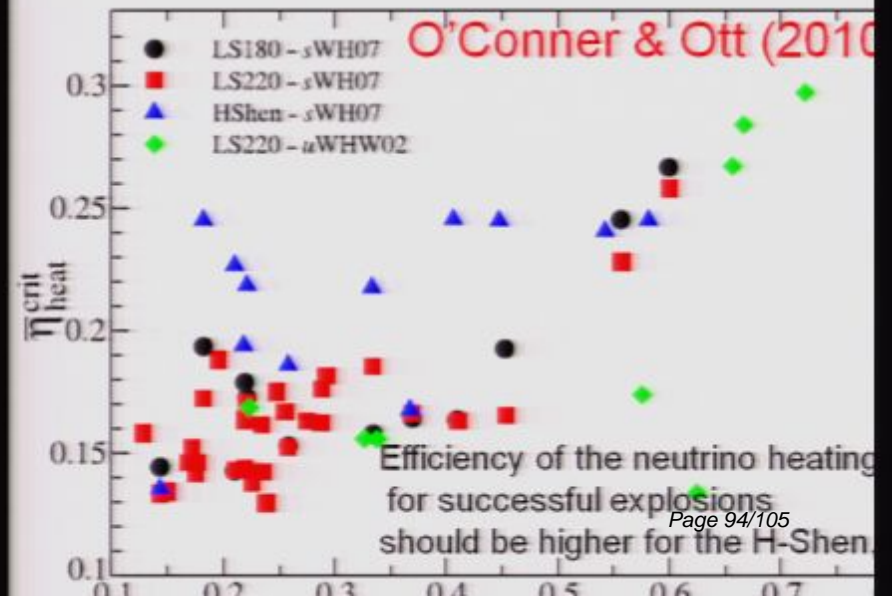


Marek & Janka (2009)



Preliminary

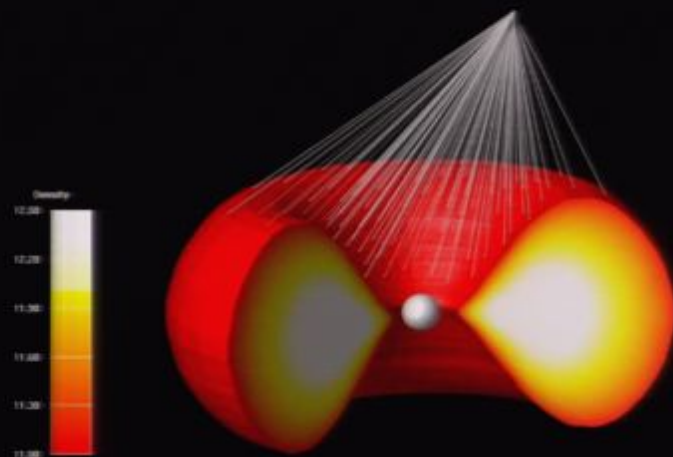
The third lesson is that the roles of “symmetry energy” in the explosion dynamics may still remain to be studied. (thank to Sumi, O’Conner, Fernandes, Gabriel, Matthias)



Neutrino pair annihilation $\nu + \bar{\nu} \rightarrow e^+ + e^-$: important heating source in collapsars

(Goodman '87, Asano & Fukuyama 2000, Dessart +07, Birkel +06)

✓ We proposed a GR ray-tracing method (Harikae, KK+ (10))



Energy/Momentum deposition rates

$$Q_{\mu}^L(r) = 2K G_{\text{F}}^2 \int d^3 p_{\nu}^L d^3 p_{\bar{\nu}}^L \times (\epsilon_{\nu}^L \epsilon_{\bar{\nu}}^L) (p_{\nu}^L + p_{\bar{\nu}}^L)_{\mu} \underline{f_{\nu}^L(p_{\nu}^L, r)} \underline{f_{\bar{\nu}}^L(p_{\bar{\nu}}^L, r)} \times [1 - \sin \theta_{\nu} \sin \theta_{\bar{\nu}} \cos(\varphi_{\nu} - \varphi_{\bar{\nu}}) - \cos \theta_{\nu} \cos \theta_{\bar{\nu}}]^2$$

Neutrino distribution functions: determined by B-eqn.

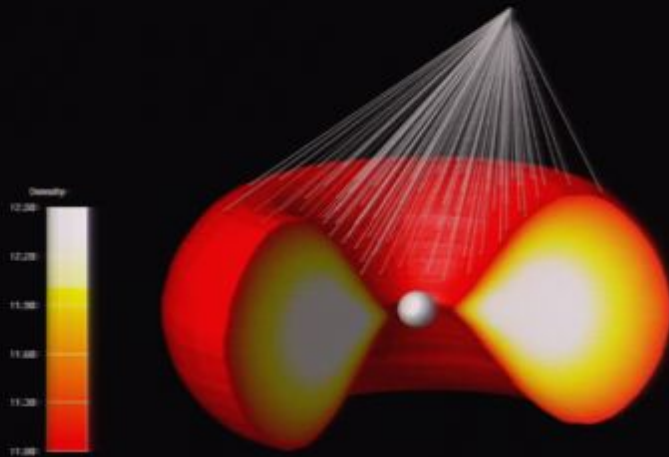
$$\frac{df_{\nu(\bar{\nu})}}{d\lambda} = p^{\alpha} \frac{Df_{\nu(\bar{\nu})}}{Dx^{\alpha}} = \left(\frac{df_{\nu(\bar{\nu})}}{d\lambda} \right)_{\text{coll}}$$

$$\frac{D}{Dx^{\alpha}} \equiv \frac{\partial}{\partial x^{\alpha}} - \Gamma_{\alpha\gamma}^{\beta} p^{\gamma} \frac{\partial}{\partial p^{\beta}},$$

Neutrino pair annihilation $\nu + \bar{\nu} \rightarrow e^+ + e^-$: important heating source in collapsars

(Goodman '87, Asano & Fukuyama 2000, Dessart +07, Birkel +06)

✓ We proposed a GR ray-tracing method (Harikae, KK+ (10))



Boltzmann eqn (for photons)

$$\frac{df}{d\lambda} = n(Q - \kappa f)$$

$$Q(x, p) = Q_e(x, \epsilon^R) + Q_s(x, p)$$

$$Q_e(x, \epsilon^R) = \frac{j(x, \epsilon^R)}{4\pi(\epsilon^R)^2}$$

Energy coupling scattering reactions are neglected.

$$Q_s(x, p) = \int \epsilon'^R d\epsilon'^R d\Omega(x, p') \xi(x; p' \rightarrow p) f(x, p)$$

Formal solution of the Boltzmann equation.

$$f(\epsilon, \Omega) = \int_{\lambda_0}^{\lambda_S} n(\lambda'') Q(\lambda, '' f) e^{-\int_{\lambda''}^{\lambda_S} n(\lambda') \kappa(\lambda') d\lambda'} d\lambda, ''$$

(e.g., Zink (07))

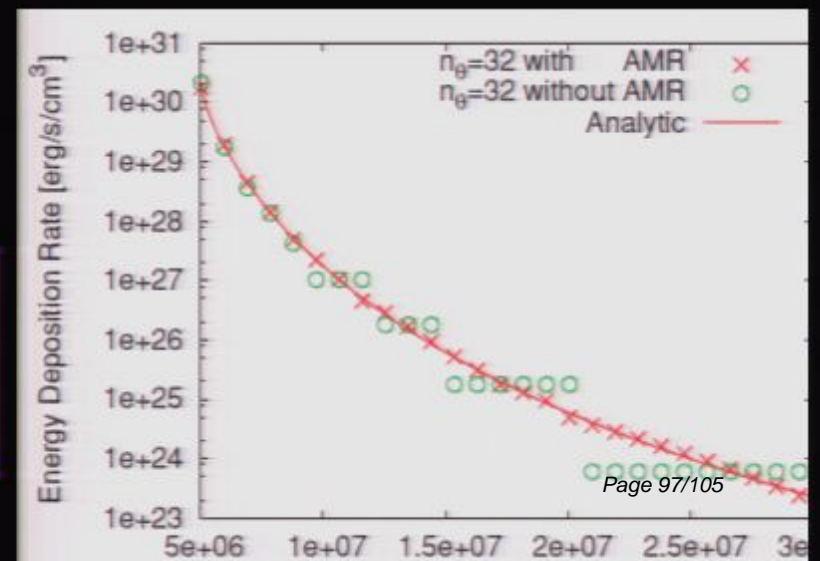
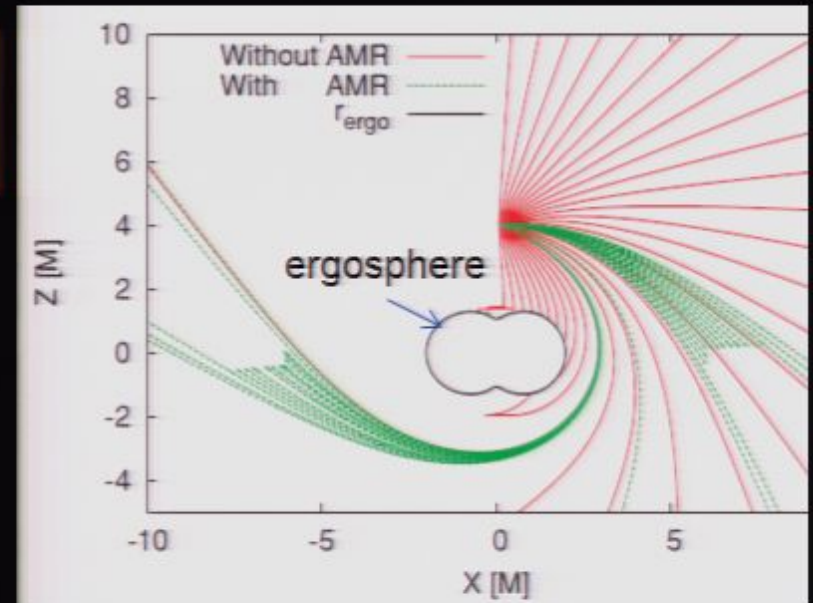
- ✓ Along the geodesics, we perform a (backward) ray-trace calculation.
- ✓ For casting rays as much as possible in the regions where the intensity is large

$$I_{\text{crit}}(\epsilon, \theta, \phi) \geq \mathcal{K} I_{\text{max}}$$

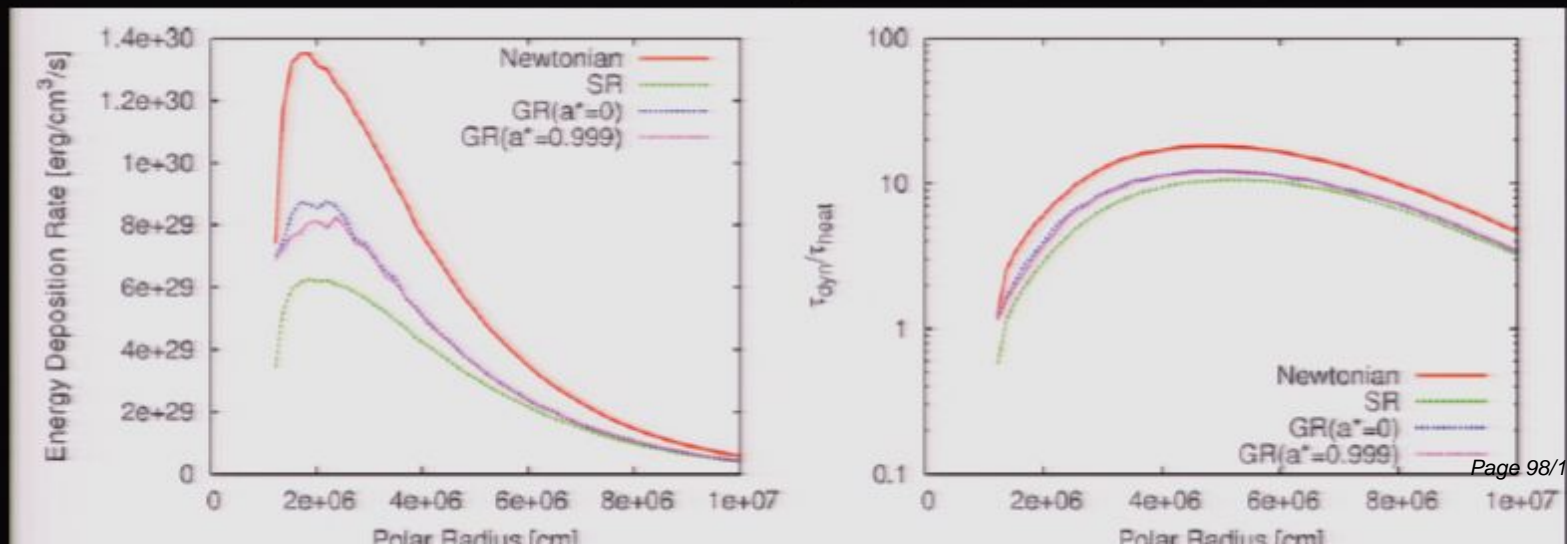
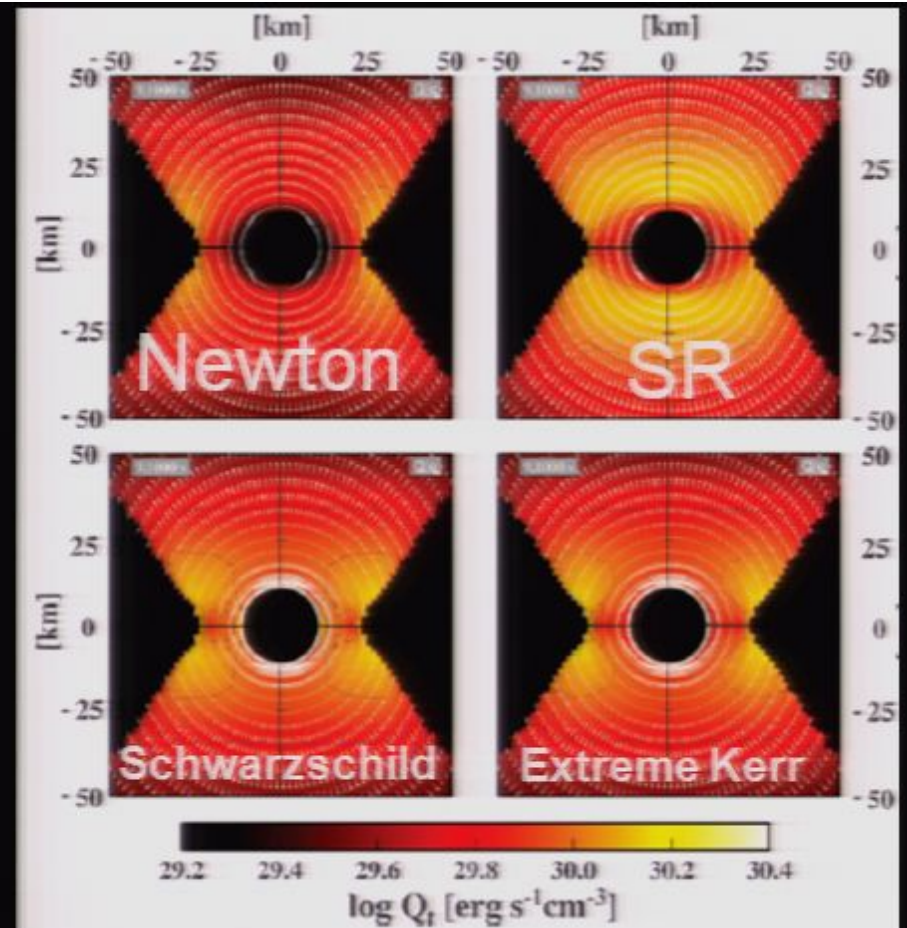
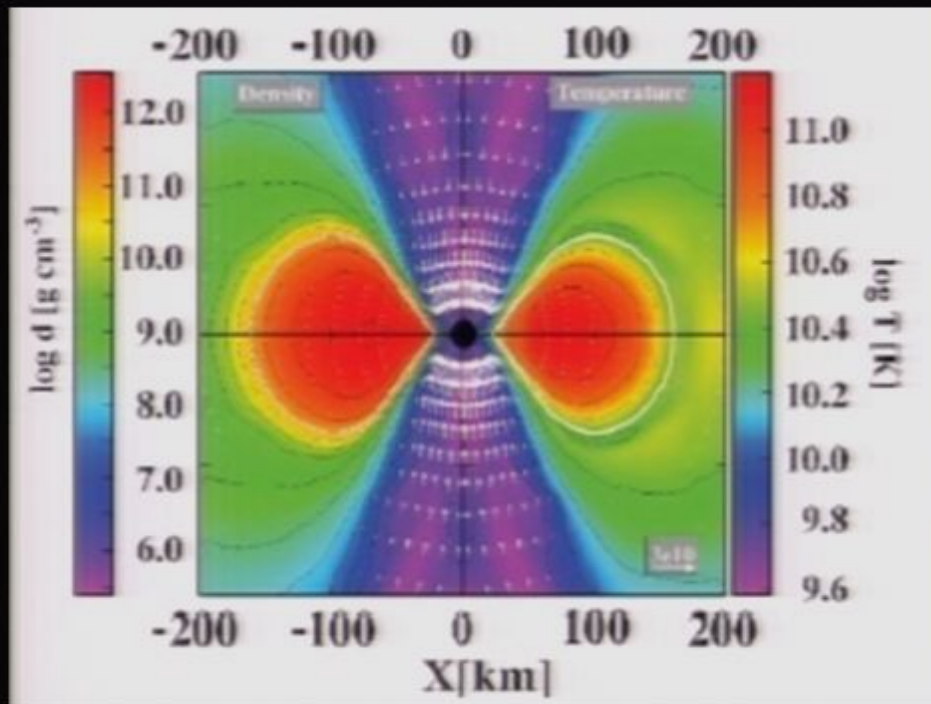
We choose the rays that satisfy the condition, and refine the resolutions for them.

Our GR ray-trace method:

- ✓ Adaptive-Ray-Casting is very useful !
- ✓ Limited to reaction (e.g., scattering)



Applications to collapsars



Summary

- ☆ **Cooling by nu_x is being treatable** in the IDSA simulations, either by leakage or grey-M1 scheme.
- ☆ **A good energy conservation in multi-D simulations:** the recipe in Mueller et al. (2010)).
- ☆ **“Symmetry energy”** may hold a key importance.
- ☆ **“Adaptive-Ray-Casting” in the GR ray-trace scheme** reduces the computational cost significantly.
Scattering reactions: remained to be included.
This scheme would **be powerful in collapsar simulations.**

Summary

- ☆ Cooling by nu_x is being treatable in the IDSA simulations, either by leakage or grey-M1 scheme.
- ☆ A good energy conservation in multi-D simulations: the recipe in Mueller et al. (2010).
- ☆ “Symmetry energy” may hold a key importance.
- ☆ “Adaptive-Ray-Casting” in the GR ray-trace scheme reduces the computational cost significantly.
Scattering reactions: remained to be included.
This scheme would be powerful in other simulations.

Thank you

Summary

- ☆ Cooling by nu_x is being treatable in the IDSA simulations, either by leakage or grey-M1 scheme.
- ☆ A good energy conservation in multi-D simulations: the recipe in Mueller et al. (2010)).
- ☆ “Symmetry energy” may hold a key importance.
- ☆ “Adaptive-Ray-Casting” in the GR ray-trace scheme reduces the computational cost significantly.
Scattering reactions: remained to be included.
This scheme would be powerful in other simulations.

Thank you very much !

Formal solution of the Boltzmann equation.

$$f(\epsilon, \Omega) = \int_{\lambda_0}^{\lambda_S} n(\lambda'') Q(\lambda, \lambda'') f e^{-\int_{\lambda''}^{\lambda_S} n(\lambda') \kappa(\lambda') d\lambda'} d\lambda, \lambda''$$

(e.g., Zink (07))

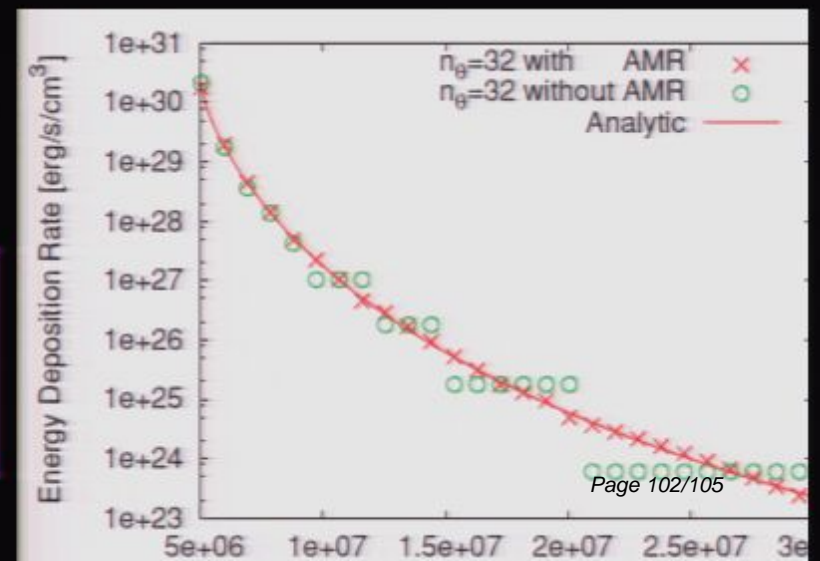
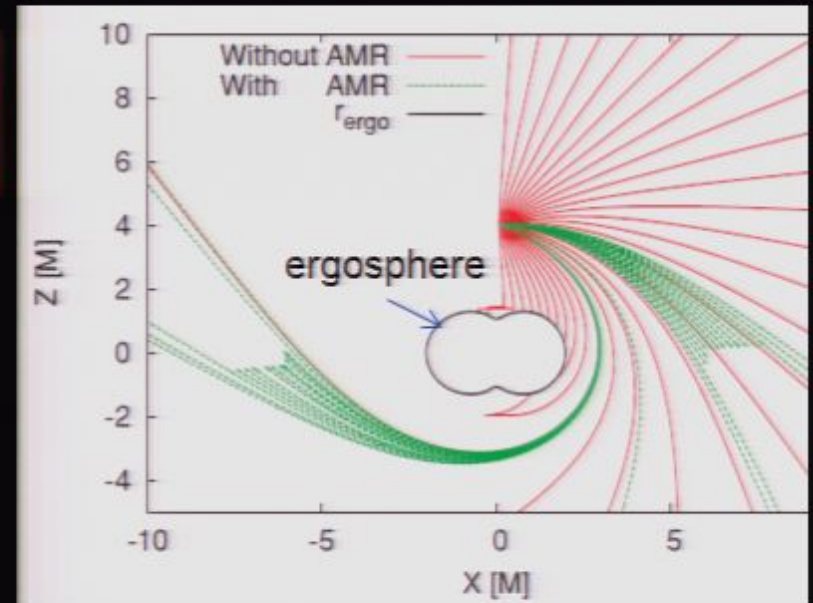
- ✓ Along the geodesics, we perform a (backward) ray-trace calculation.
- ✓ For casting rays as much as possible in the regions where the intensity is large

$$I_{\text{crit}}(\epsilon, \theta, \phi) \geq \mathcal{K} I_{\text{max}}$$

We choose the rays that satisfy the condition, and refine the resolutions for them.

Our GR ray-trace method:

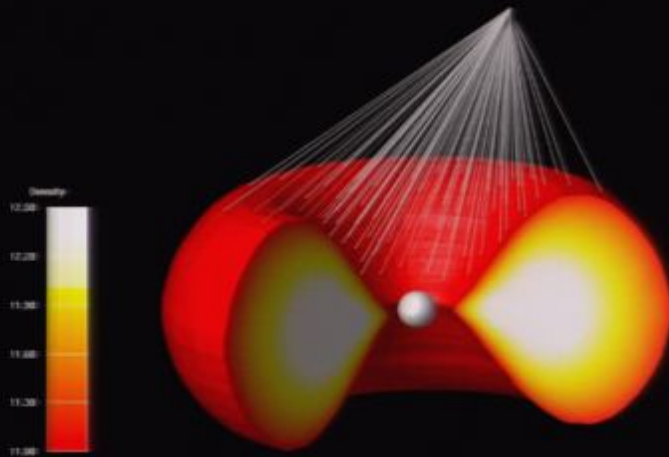
- ✓ Adaptive-Ray-Casting is very useful !
- ✓ Limited to reaction (e.g., scattering)



Neutrino pair annihilation $\nu + \bar{\nu} \rightarrow e^+ + e^-$: important heating source in collapsars

(Goodman '87, Asano & Fukuyama 2000, Dessart +07, Birkel +06)

✓ We proposed a GR ray-tracing method (Harikae, KK+ (10))



Boltzmann eqn (for photons)

$$\frac{df}{d\lambda} = n(Q - \kappa f)$$

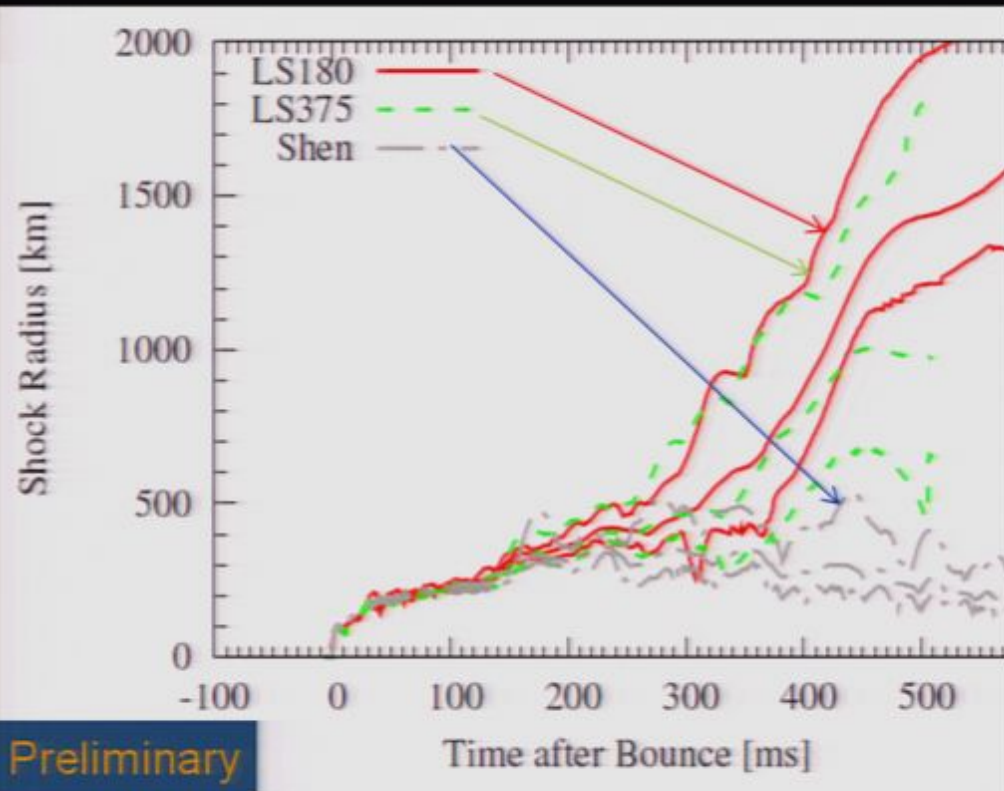
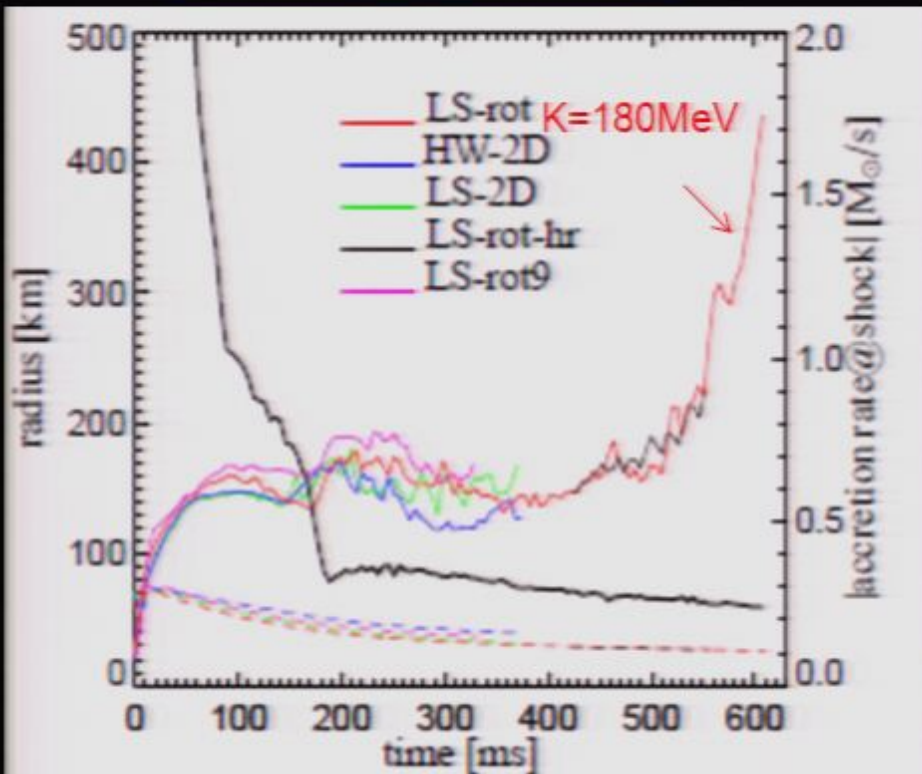
$$Q(x, p) = Q_e(x, \epsilon^R) + Q_s(x, p)$$

$$Q_e(x, \epsilon^R) = \frac{j(x, \epsilon^R)}{4\pi(\epsilon^R)^2}$$

Energy coupling scattering reactions are neglected.

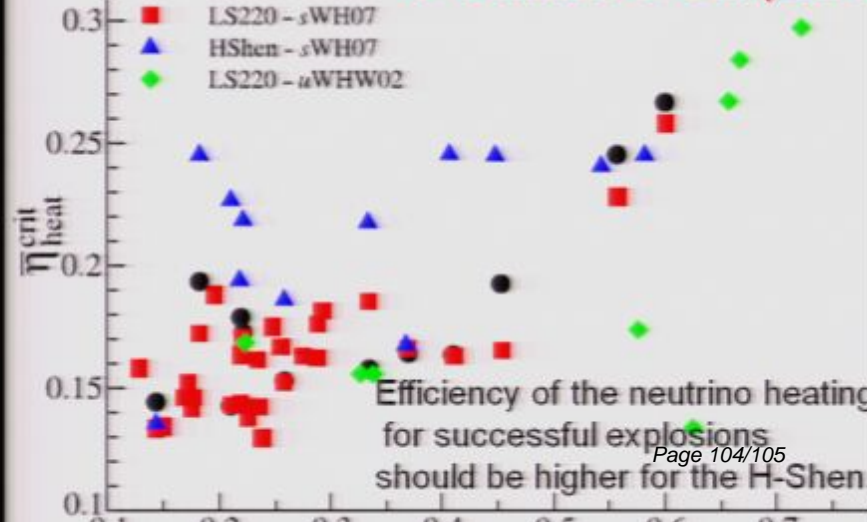
$$Q_s(x, p) = \int \epsilon'^R d\epsilon'^R d\Omega(x, p') \xi(x; p' \rightarrow p) f(x, p')$$

Marek & Janka (2009)



Preliminary

O'Conner & Ott (2010)



Applications to collapsars

