

Title: Explorations in Particle Theory - Lecture 1

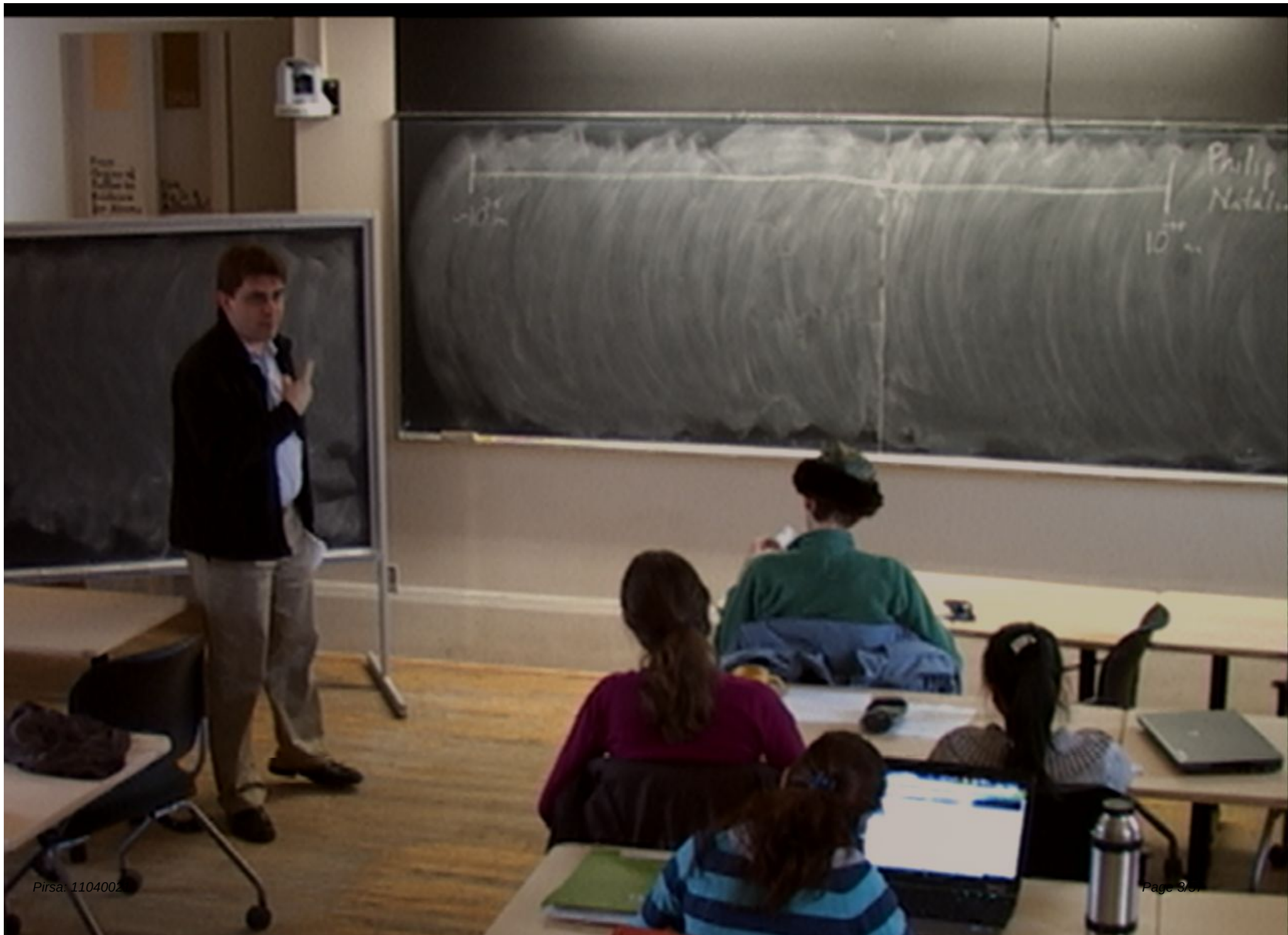
Date: Apr 04, 2011 10:15 AM

URL: <http://pirsa.org/11040021>

Abstract:

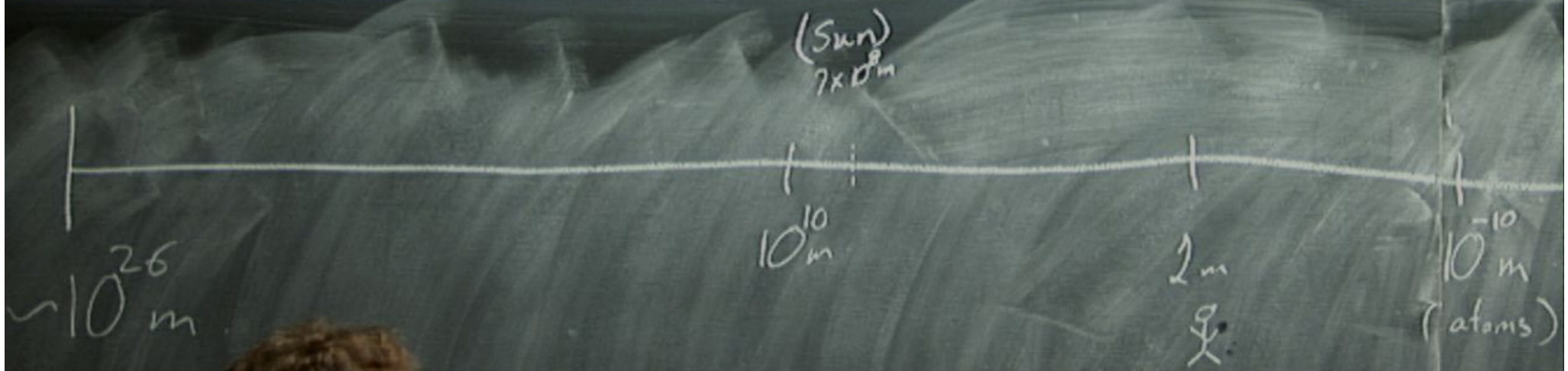


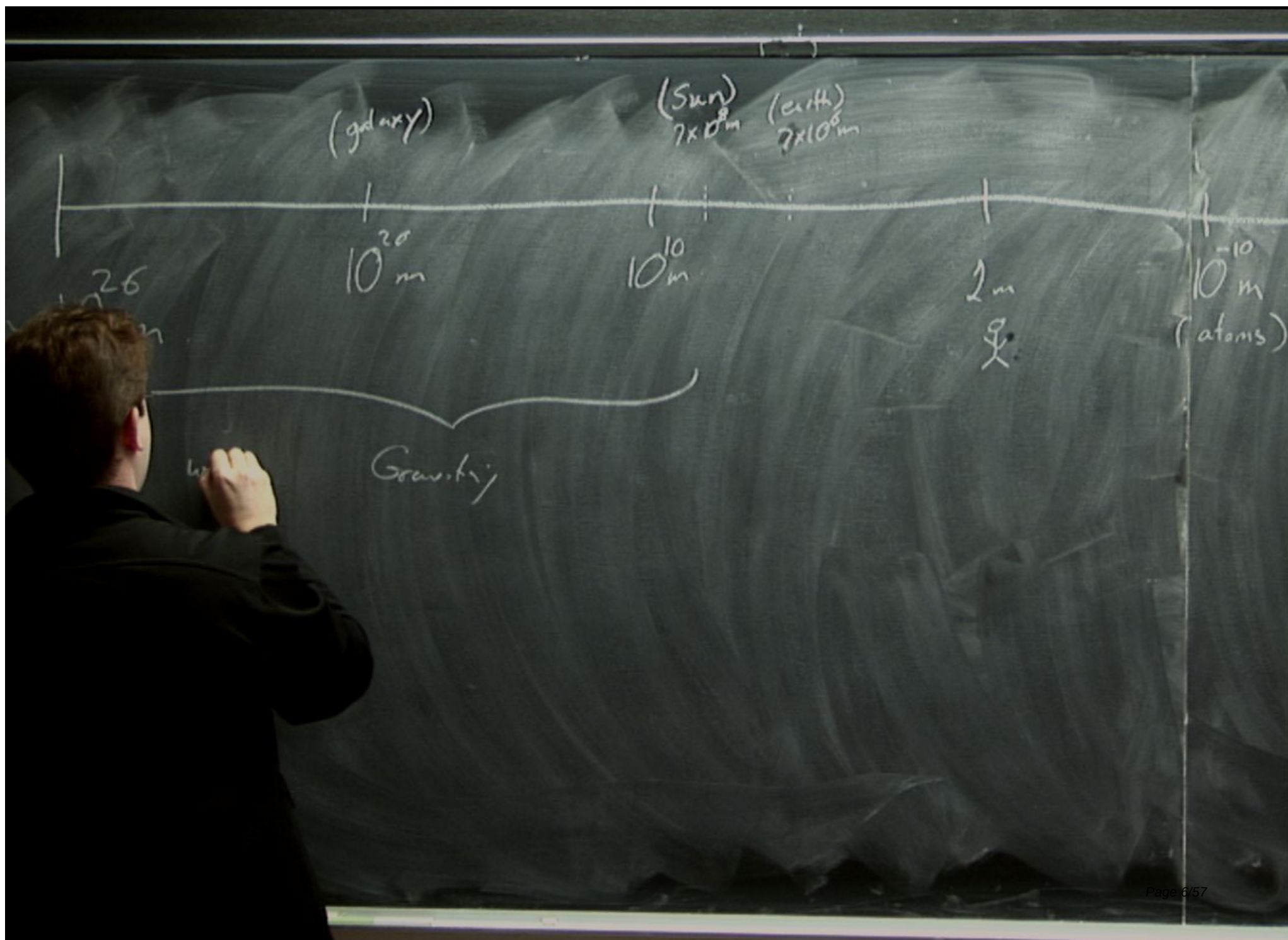
perimeter scholars
international



|
2 m
⊗

|
⁻¹⁰
10 m
(atoms)





2 m
⚗

10^{-10} m
(atoms)

10^{-16} m
(nuclei)
 10^{-18} m

weak
interactions
 10^{-20} m

?

10^{-35} m

Phil
Nat

Philip Schuster
Natalia Toro

10^{-35} m



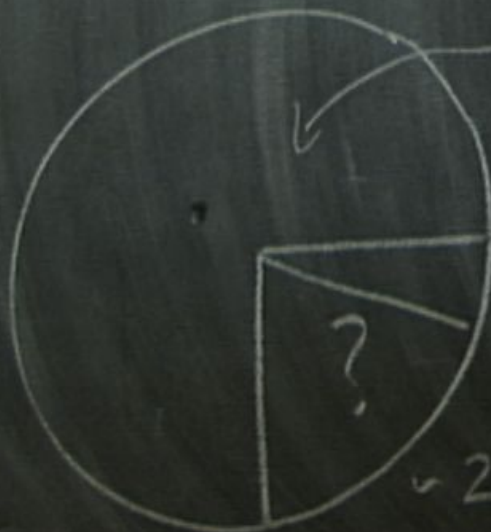
few % atoms, baryons.

-18
10m
work
interval
-20
10m
?

Philip Schuster
Natalia Toro

10^{-35} m

~70 %



few % atoms

~23 %

Philip Schuster
Natalia Toro

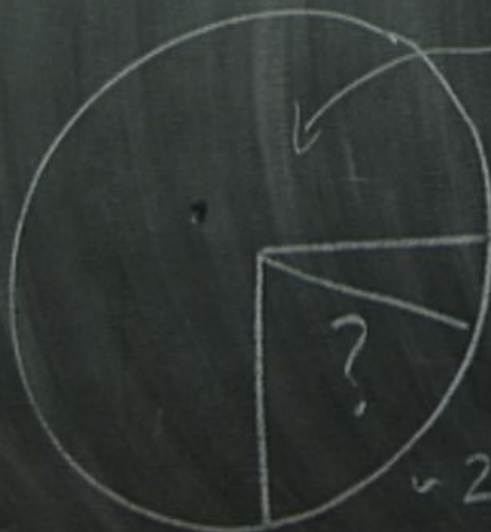
10^{-35} m

~70 %

9Y

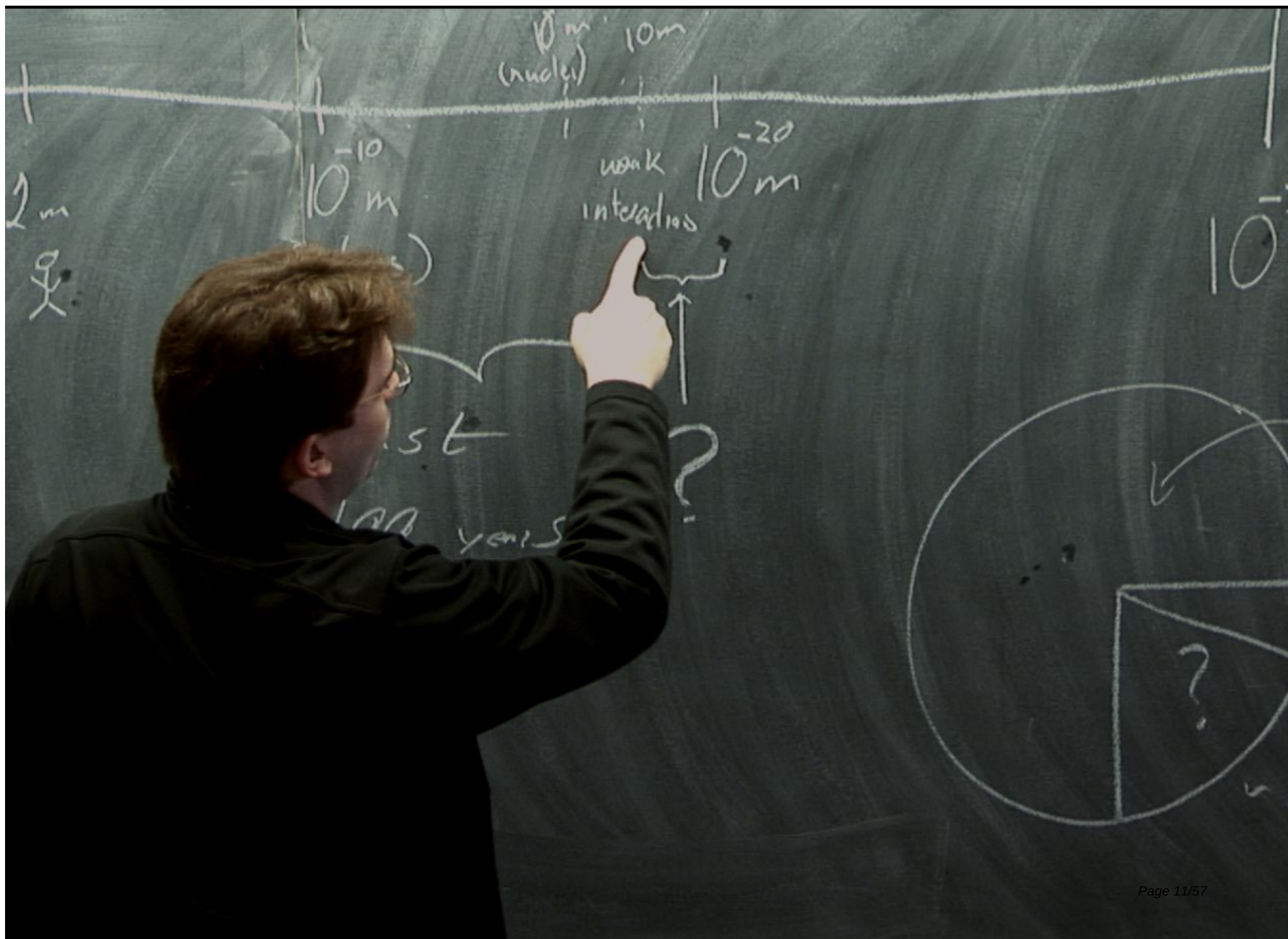
few % atoms, baryons

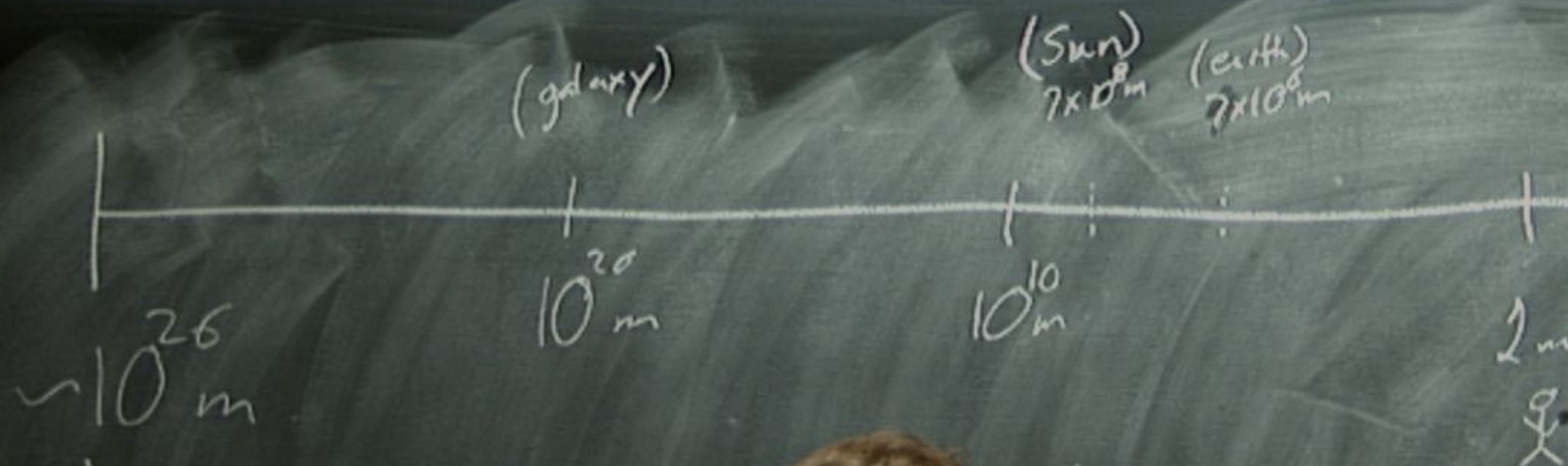
~23 % dark matter



-18
10m
work
interval
-20
10m

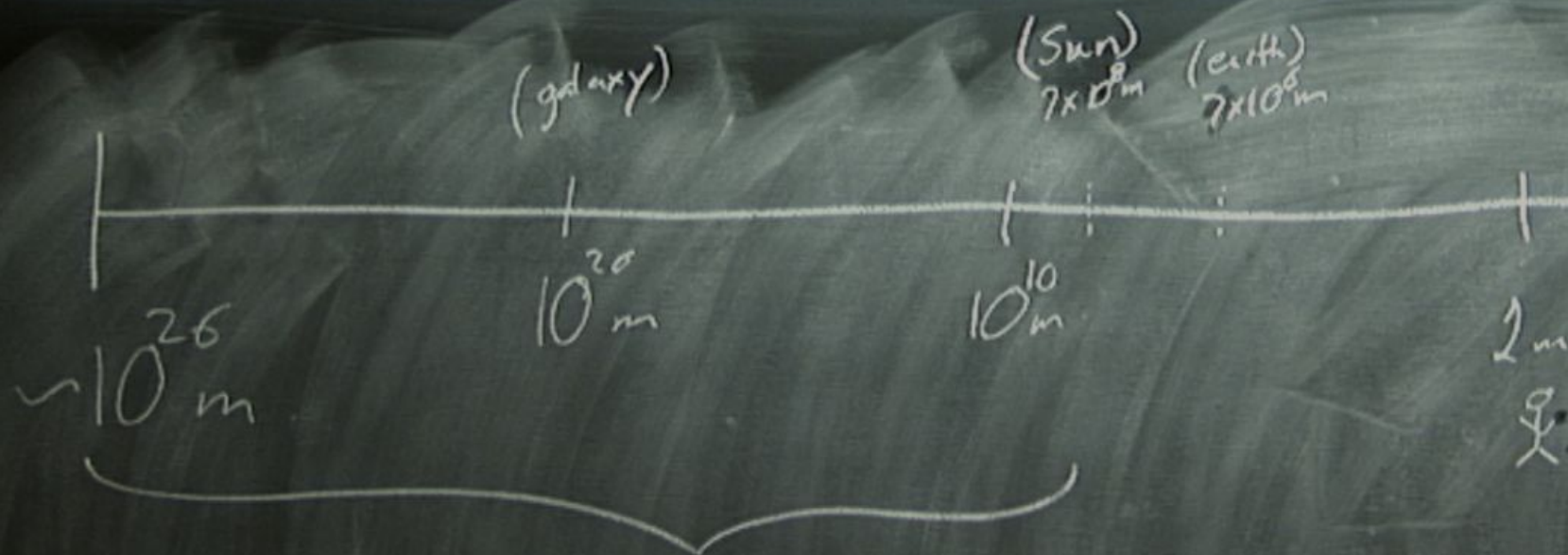
?





we see Gravity
Con

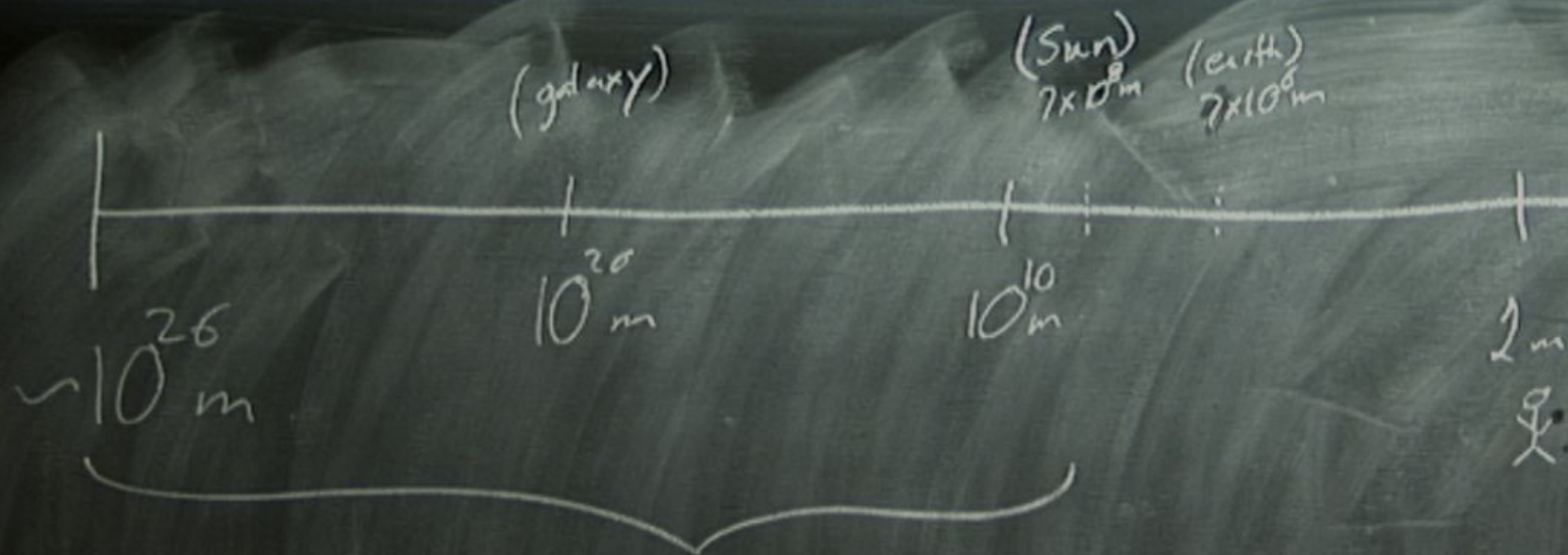
Experiments to
watch



we see Gravity/
Cosmology

Experiments to
watch

- Large Hadron Collider



we see Gravity/
Cosmology

Experiments to
watch

- Large Hadron Collider
- XENON100, etc

Grains of
Poller to
Evidence
for Atoms

How
Big Is A
Molecule?

	J^P	Mass	Lifetime
p	$\frac{1}{2}^+$	938 MeV	
e^-	$\frac{1}{2}^-$	0.511 MeV	
γ	1^-		
n	$\frac{1}{2}^+$		

Grains of
Poller to
Evidence
for Atoms

How
Big Is A
Molecule?

J^P

Mass

Lifetime

p

$\frac{1}{2}^+$

938 MeV

e^-

$\frac{1}{2}^-$

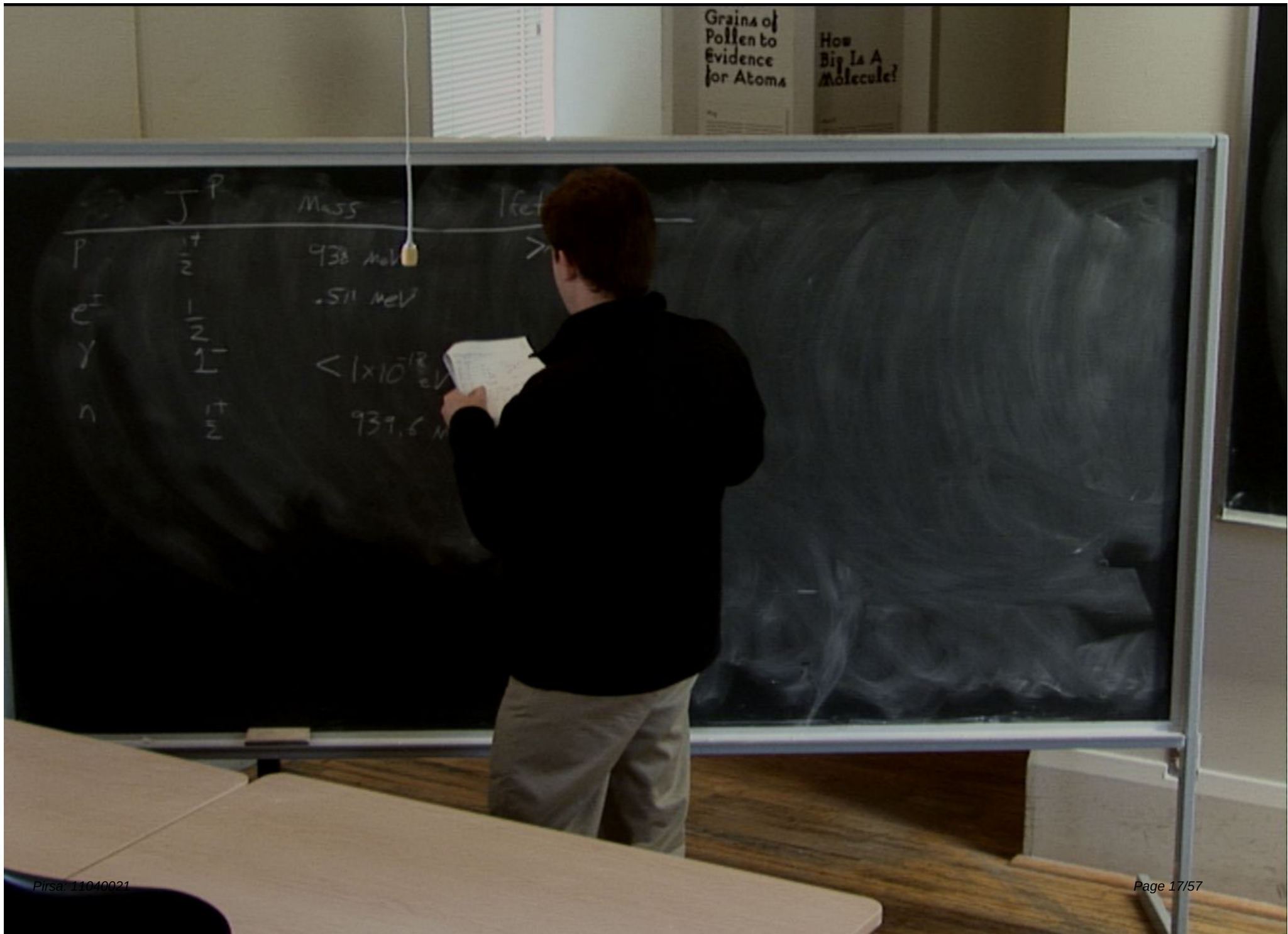
0.511 MeV

γ

0^-

$< 1 \times 10^{-18}$ s

938



Grains of
Pollen to
Evidence
for Atoms

How
Big Is A
Molecule?

	J	P	mass	t
p	$\frac{1}{2}$	$+$	938 MeV	$>$
e ⁻	$\frac{1}{2}$	$-$	0.511 MeV	
γ	1	$-$	$< 1 \times 10^{-18}$ s	
n	$\frac{1}{2}$	$+$	939.6 MeV	

J^P

Mass

lifetime

$\frac{1}{2}^+$

938 meV

$> (2 \times 10^{27} \text{ yrs or } 10^{31-33} \text{ yrs})$

$\frac{1}{2}^-$

939 meV

$> 4.6 \times 10^{26} \text{ yrs.}$

1^-

$< 1 \times 10^{-18} \text{ eV}$

stable

$\frac{1}{2}^+$

939.6 meV

$\sim 900 \text{ s}$

$(n \rightarrow p e \bar{\nu}_e)$

J^P	Mass	lifetime	
$\frac{1}{2}^+$	938 MeV	$> (2 \times 10^{27} \text{ yrs or } 10^{31-33} \text{ yrs})$	} $\Rightarrow$ QED
$\frac{1}{2}^+$	511 MeV	$> 4.6 \times 10^{26} \text{ yrs.}$	
1^-	$< 1 \times 10^{-18} \text{ eV}$	stable	
$\frac{1}{2}^+$	939.6 MeV	$\sim 900 \text{ s}$ ($n \rightarrow p e \bar{\nu}_e$)	

	J ^P	Mass	lifetime	
p	$\frac{1}{2}^+$	938 MeV	$> (2 \times 10^{27} \text{ yr or } 10^{31-33} \text{ yrs})$	} $\Rightarrow$ QED
$e^\pm$		.511 MeV	$> 4.6 \times 10^{26} \text{ yrs.}$	
γ		$< 1 \times 10^{-18} \text{ eV}$	stable	
n		MeV	$\sim 900 \text{ s}$ ($n \rightarrow p e \bar{\nu}_e$)	
$\mu^\pm$			$2.6 \times 10^{-8} \text{ s}$ ($c\tau \approx 660 \text{ m}$) $\mu^\pm \rightarrow e \bar{\nu}_e \nu_\mu$	
$\pi^\pm$				

	J^P	Mass	lifetime	
p	$\frac{1}{2}^+$	938 MeV	$> (2 \times 10^{27} \text{ yrs or } 10^{31-33} \text{ yrs})$	} $\Rightarrow$ QED
e^-	$\frac{1}{2}^-$	0.511 MeV	$> 4.6 \times 10^{26} \text{ yrs}$	
γ	1^-	$< 1 \times 10^{-18} \text{ eV}$	stable	
n	$\frac{1}{2}^+$	939.6 MeV	$\sim 900 \text{ s}$ ($n \rightarrow p e^- \bar{\nu}_e$)	
$\mu^\pm$	$\frac{1}{2}^\pm$	105.7 MeV	$2.7 \times 10^{-6} \text{ s}$ ($c\tau \approx 660 \text{ m}$)	$\mu^\pm \rightarrow e^\pm \bar{\nu}_e \nu_\mu$
$\pi^\pm$	0^-	139.6 MeV	$2.6 \times 10^{-8} \text{ s}$ ($c\tau \approx 7.8 \text{ m}$)	

	J^P	Mass	lifetime	
p	$\frac{1}{2}^+$	938 MeV	$> (2 \times 10^{29} \text{ yrs or } 10^{31-33} \text{ yrs})$	} $\Rightarrow$ QED
$e^\pm$	$\frac{1}{2}^-$	0.511 MeV	$> 4.6 \times 10^{26} \text{ yrs}$	
γ	1^-	$< 1 \times 10^{-18} \text{ eV}$	stable	
n	$\frac{1}{2}^+$	939.6 MeV	$\sim 900 \text{ s}$ ($n \rightarrow p e \bar{\nu}_e$)	
$\mu^\pm$	$\frac{1}{2}^-$	105.7 MeV	$2.7 \times 10^{-6} \text{ s}$ ($c\tau \approx 660 \text{ m}$)	$\mu^\pm \rightarrow e \bar{\nu}_e \nu_\mu$
$\pi^\pm$	0^-	139.6 MeV	$2.6 \times 10^{-8} \text{ s}$ ($c\tau \approx 7.8 \text{ m}$)	$\pi^\pm \rightarrow \mu^\pm \nu_\mu$ $\rightarrow e \bar{\nu}_e \nu_\mu$

	J^P	Mass	lifetime	
p	$\frac{1}{2}^+$	938 MeV	$> (2 \times 10^{29} \text{ yrs or } 10^{31-33} \text{ yrs})$	} $\Rightarrow$ QED
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n	$\frac{1}{2}^+$	939.6 MeV	$\sim 900 \text{ s}$ ($n \rightarrow p e \bar{\nu}_e$)	
$\mu^\pm$	$\frac{1}{2}^\pm$	105.7 MeV	$2.7 \times 10^{-6} \text{ s}$ ($c\tau \approx 660 \text{ m}$)	$\mu^\pm \rightarrow e \bar{\nu}_e \nu_\mu$
$\pi^\pm$	$0^\pm$	139.6 MeV	$2.6 \times 10^{-8} \text{ s}$ ($c\tau \approx 7.8 \text{ m}$)	$\pi^\pm \rightarrow \mu^\pm \bar{\nu}_\mu \rightarrow 100\%$ $\rightarrow e \bar{\nu}_e 10^{-4}$

	J^P	Mass	lifetime	
p	$\frac{1}{2}^+$	938 MeV	$> (2 \times 10^{27} \text{ yr or } 10^{31-33} \text{ yrs})$	} $\Rightarrow$ Q.E.
$e^\pm$	$\frac{1}{2}$	.511 MeV	$> 4.6 \times 10^{26} \text{ yrs.}$	
γ	1^-	$< 1 \times 10^{-18} \text{ eV}$	stable	
n	$\frac{1}{2}^+$	939.6 MeV	$\sim 900 \text{ s}$ ($n \rightarrow p e \bar{\nu}_e$)	
$\mu^\pm$	$\frac{1}{2}$	105.7 MeV	$2.2 \times 10^{-6} \text{ s}$ ($c\tau \approx 660 \text{ m}$)	$\mu^\pm \rightarrow e \bar{\nu}_e \nu_\mu$
$\pi^\pm$	0^-	139.6 MeV	$2.6 \times 10^{-8} \text{ s}$ ($c\tau \approx 7.8 \text{ m}$)	$\pi^\pm \rightarrow \mu^\pm \bar{\nu}_\mu$
π^0	0^-	135 MeV	$\approx 1 \times 10^{-16} \text{ s}$ ($c\tau \approx 25 \text{ nm}$)	$\rightarrow e \bar{\nu}_e \nu_e$
				$\pi^0 \rightarrow \gamma\gamma$

Scattering of n, p, π

Sum

Scattering of n, p, π

$$\sigma_{n,p,\pi} \approx (1-100) \text{ mb} \approx (1-100) 10^{-3} 10^{-24} \text{ cm}^2$$

$$\sigma_{e\gamma} \approx$$

Scattering of n, p, π

$$\sigma_{n,p,\pi} \simeq (1-100) \text{ mb} \simeq (1-100) 10^{-3} 10^{-24} \text{ cm}^2$$

$$\sigma_{e\gamma} \simeq 10^{-24} \text{ cm}^2$$

$$m_e^2 \sigma_{e\gamma} \ll 1$$

Scattering of n, p, π

$$\sigma_{n,p,\pi} \simeq (1-100) \text{ mb} \simeq (1-100) 10^{-3} 10^{-24} \text{ cm}^2$$

$$\sigma_{e\gamma} \simeq 10^{-24} \text{ cm}^2$$

$$m_e^2 \sigma_{e\gamma} \ll 1$$

(Sun)

Scattering of n, p, π

$$\sigma_{n,p,\pi} \simeq (1-100) \text{ mb} \simeq (1-100) 10^{-3} 10^{-24} \text{ cm}^2$$

$$\sigma_{e\gamma} \simeq 10^{-24} \text{ cm}^2$$

$$m_e^2 \sigma_{e\gamma} \ll 1$$

$\sim \alpha^2$

$$m_{n,p,\pi} \sigma_{n,p,\pi} \simeq 1$$

Scattering of n, p, π

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$$\sigma_{e\gamma} \simeq 10^{-24} \text{ cm}^2$$

$$m_e^2 \sigma_{e\gamma} \ll 1$$

$\sim \alpha^2$

$$m_{n,p,\pi} \sigma_{n,p,\pi} \simeq 1$$

$$\hbar c \simeq 200 \text{ MeV fm}$$
$$\equiv 1$$

$$\sigma_{n,p,\pi} \simeq \frac{\mathcal{O}(1)}{(\text{GeV})^2}$$

Scattering of n, p, π

$$\sigma_{n,p,\pi} \approx (1-100) \text{ mb} \approx (1-100) 10^{-3} 10^{-24} \text{ cm}^2$$

$$\sigma_{e\gamma} \approx 10^{-24} \text{ cm}^2$$

$$m_e^2 \sigma_{e\gamma} \ll 1$$

$\sim \alpha^2$

$$m_{n,p,\pi} \sigma_{n,p,\pi} \approx 1$$

$$\hbar c \approx 200 \text{ MeV fm}$$
$$\approx 1$$

$$\sigma_{n,p,\pi} \approx \frac{\mathcal{O}(1)}{(\text{GeV})^2}$$

$$e p \longrightarrow e p n$$

1 cm²

100 MeV 5m

$$= \frac{\sigma(l)}{(\text{GeV})^2}$$

$$e p \rightarrow e p n$$

$$e \pi \rightarrow e \pi + \pi \dots$$

$$e p \not\rightarrow e p n$$

$$e \pi \longrightarrow e \pi + \pi \dots$$

Baryon #

$$e p \not\rightarrow e p n$$

$$e \pi \longrightarrow e \pi + \pi \dots$$

Baryon #

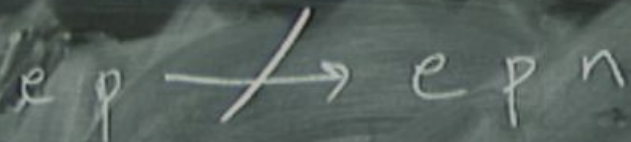
B	1-e
---	-----

$$e p \not\rightarrow e p n$$

$$e \pi \longrightarrow e \pi + \pi \dots$$

Baryon #

B	particle
1	p
1	n
0	$\pi^{\pm}$
	π^0
	$\vdots$



Baryon #

Lepton #

S_m

B	particle
1	p
1	n
0	$\pi^\pm$
	π^0
	$\vdots$

L	
	p
	n
1	e
1	ν_e
1	μ
1	ν_μ

$$e p \not\rightarrow e p n$$

$$e \pi \longrightarrow e \pi + \pi \dots$$

Baryon #

Lepton #

S_m

B	
1	p
1	n
0	$\pi^\pm$
	π^0
	$\vdots$

L	
0	p n
1	e
1	ν_e
1	μ
1	ν_μ

$$e p \not\rightarrow e p n$$

$$e \pi \longrightarrow e \pi + \pi \dots$$

Baryon #

B	particle
1	p
1	n
0	$\pi^\pm$
	π^0
	$\vdots$

Lepton #

L	p	π
0	n	
1	e	
1	ν_e	
1	μ	
1	ν_μ	

$n + n \rightarrow \dots$

$n + p \rightarrow \dots$

$p + p \rightarrow \dots$

(strong)

$$n + n \rightarrow n + n$$

$$n + p \rightarrow n + p$$

$$p + p \rightarrow p + p$$

...

(strong)

$$n + n \rightarrow n + n$$

$$n + p \rightarrow n + p$$

$$p + p \rightarrow p + p$$

"the same"

$$\pi^+ p \rightarrow \pi^+ p$$

$$\pi^- n \rightarrow \pi^- n$$

"the same"

(strong)

$$n + n \rightarrow n + n$$

$$n + p \rightarrow n + p$$

$$p + p \rightarrow p + p$$

"the same"

$$\pi^+ p \rightarrow \pi^+ p$$

$$\pi^- n \rightarrow \pi^- n$$

"the same"

(strong)

$$n + n \rightarrow n + n$$

$$n + p \rightarrow n + p$$

$$p + p \rightarrow p + p$$

"the same"

$$\pi^+ p \rightarrow \pi^+ p$$

$$\pi^- n \rightarrow \pi^- n$$

"the same"

Isospin $SU(2)$

$$\begin{pmatrix} p \\ n \end{pmatrix}, \begin{pmatrix} \pi^+ \\ \pi^0 \\ \pi^- \end{pmatrix}$$

$$j_{\text{isospin}} = \frac{1}{2}$$

$$j_I = 1$$

Isospin · SU(2)

$$\begin{pmatrix} p \\ n \end{pmatrix}$$

$$\begin{pmatrix} \pi^+ \\ \pi^0 \\ \pi^- \end{pmatrix}$$

$$j_{\text{isospin}} = \frac{1}{2}$$

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Isospin $SU(2)$

$$\begin{pmatrix} p \\ n \end{pmatrix}, \begin{pmatrix} \pi^+ \\ \pi^0 \\ \pi^- \end{pmatrix}$$

$$j_{\text{isospin}} = \frac{1}{2}$$

$$j_I = 1$$

$$H_{\text{universe}} = H_{\text{strong}} + \dots$$

↳ conserves

Isospin $SU(2)$

$$\begin{pmatrix} p \\ n \end{pmatrix}, \begin{pmatrix} \pi^+ \\ \pi^0 \\ \pi^- \end{pmatrix}$$

$$j_{\text{isospin}} = \frac{1}{2}$$

$$j_I = 1$$

$$I = \frac{1}{2}$$

$$\begin{pmatrix} p \\ n \end{pmatrix} I_3$$

$$H_{\text{universe}} = H_{\text{strong}} + \dots$$

$\hookrightarrow$ conserves Isospin

Isospin $SU(2)$

$$\begin{pmatrix} p \\ n \end{pmatrix}, \begin{pmatrix} \pi^+ \\ \pi^0 \\ \pi^- \end{pmatrix}$$

$$j_{\text{isospin}} = \frac{1}{2}$$

$$j_I = 1$$

$$H_{\text{universe}} = H_{\text{strong}} + \dots$$

↳ conserves Isospin

$$I = \frac{1}{2}$$

$$\begin{pmatrix} p \\ n \end{pmatrix} \quad I_3 = \begin{matrix} +\frac{1}{2} \\ -\frac{1}{2} \end{matrix}$$

$$I = 1$$

$$\begin{pmatrix} \pi^+ \\ \pi^0 \\ \pi^- \end{pmatrix} \quad \begin{matrix} +1 \\ 0 \\ -1 \end{matrix}$$

$$\frac{Q}{e} = I_3 + \frac{B}{2}$$

Isospin $SU(2)$

$$\begin{pmatrix} p \\ n \end{pmatrix}$$

$$\begin{pmatrix} \pi^+ \\ \pi^0 \\ \pi^- \end{pmatrix}$$

$$J_I = 1$$

$$I = \frac{1}{2}$$

$$\begin{pmatrix} p \\ n \end{pmatrix} \quad I_3 = \begin{matrix} +\frac{1}{2} \\ -\frac{1}{2} \end{matrix}$$

$$I = 1$$

$$\begin{pmatrix} \pi^+ \\ \pi^0 \\ \pi^- \end{pmatrix} \quad I_3 = \begin{matrix} +1 \\ 0 \\ -1 \end{matrix}$$

$$Q = I_3 + \frac{B}{2}$$

$\gamma_{\pi^+} > \gamma_{\pi^0} > 10^{-23} \text{ s}$
(strong)

$$\gamma_{\pi^+} > \gamma_{\pi^0} > 10^{-23} \text{ s (strong)}$$

$$\gamma_{\pi^-}$$

$$\tau_{\pi^\pm} \gg \tau_{\pi^0} \gg 10^{-23} \text{ s} \text{ (strong)}$$

$$\Gamma_{\pi^0 \rightarrow \gamma\gamma} \approx \alpha^2 m_{\pi^0}$$

$$\tau_{\mu} \approx 100 \tau_{\pi^{\pm}}$$

$$\tau_{\pi^{\pm}}$$

$$>>$$

$$\tau_{\pi^0}$$

$$>>$$

$$10^{-23} \text{ s}$$

(strong)

$$\Gamma_{\pi^0 \rightarrow \gamma\gamma} \approx \alpha^2 m_{\pi^0}$$

$$\tau_{\mu} \approx 100 \tau_{\pi^+}$$

$$\tau_{\pi^+} \gg \tau_{\pi^0} \gg 10^{-23} \text{ s} \text{ (strong)}$$

$$\Gamma_{\pi^0 \rightarrow \gamma\gamma} \approx \alpha^2 m_{\pi^0}$$

$$n \rightarrow p e \bar{\nu}_e \quad \tau \sim 900 \text{ s} \gg \tau_{\pi^0}$$

$$\text{phase space} \approx 1 \text{ MeV}$$

$$M_{\text{weak}} \sim G_F J_{\text{baryon}}^M J_{\text{lepton}}^M$$

$$M_{\text{weak}} \sim G_F J_{\text{baryon}}^M J_{\text{lepton}}^M$$